

1 **Interaction modifications lead to greater robustness than pairwise**
2 **non-trophic effects in food webs**

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10 **Abstract**

- 11 1. Considerable emphasis has been placed recently on the importance of incorporating non-trophic
12 effects in to our understanding of ecological networks. Interaction modifications are well
13 established as generating strong non-trophic impacts by modulating the strength of inter-
14 specific interactions.
- 15 2. For simplicity and comparison with direct interactions within a network context, the
16 consequences of interaction modifications have often been described as direct pairwise
17 interactions. The consequences of this assumption have not been examined in non-equilibrium
18 settings where unexpected consequences of interaction modifications are most likely.
- 19 3. To test the distinct dynamic nature of these 'higher-order' effects we directly compare, using
20 dynamic simulations, the robustness to extinctions under perturbation of systems where
21 interaction modifications are either explicitly modelled or represented by corresponding
22 equivalent pairwise non-trophic interactions.

- 23 4. Full, multi-species representations of interaction modifications resulted in a greater robustness
24 to extinctions compared to equivalent pairwise effects. Explanations for this increased stability
25 despite apparent greater dynamic complexity can be found in additional routes for dynamic
26 feedbacks. Furthermore, interaction modifications changed the relative vulnerability of species
27 to extinction from those trophically connected close to the perturbed species towards those
28 receiving a large number of modifications.
- 29 5. Future empirical and theoretical research into non-trophic effects should distinguish interaction
30 modifications from direct pairwise effects in order to maximise information about the system
31 dynamics. Interaction modifications have the potential to shift expectations of species
32 vulnerability based exclusively on trophic networks.

33 **Key words**

34 ecological network, food web, higher-order effect, non-trophic effect, robustness, stability, trophic
35 interaction modification

36 **Introduction**

37 There is a building appreciation that to improve our understanding of the population dynamics of
38 ecological communities it is necessary to move beyond studies that focus on a single interaction
39 process at a time (Kéfi et al., 2012; Levine, Bascompte, Adler, & Allesina, 2017). Trophic interaction
40 modifications (Terry, Morris, & Bonsall, 2017; Wootton, 1993) occur when a consumer-resource
41 interaction is modulated by additional species. They are a class of higher-order processes since their
42 effects are not fundamentally pairwise. Examples include associational defences (P. Barbosa et al.,
43 2009), fear effects (Sih, Englund, & Wooster, 1998), certain impacts of ecosystem engineers (Sanders
44 et al., 2014) and foraging choices (Abrams, 2010). It has been empirically demonstrated that many
45 strong non-trophic effects are caused by such processes (Ohgushi, Schmitz, & Holt, 2012; Preisser,
46 Bolnick, & Benard, 2005; Werner & Peacor, 2003) with large implications for community structure

47 and dynamics (M. Barbosa, Fernandes, Lewis, & Morris, 2017; Donohue et al., 2017; Matassa,
48 Ewanchuk, & Trussell, 2018; van Veen, van Holland, & Godfray, 2005).

49 Approaches to understanding interaction modifications often try to distil the inherently multi-
50 species process into a pairwise non-trophic effect (or ‘trait-mediated indirect effect’) from the
51 modifier species onto one or both of the recipient species (Okuyama & Bolker, 2007). This allows the
52 direct comparison of non-trophic and trophic interaction strengths (Preisser et al., 2005) and
53 network structure (Pilosof, Porter, Pascual, & Kéfi, 2017) but is a representation of a different class
54 of dynamic process (Terry et al., 2017). While this simplification is fully justified in studies of
55 communities at equilibrium (Grilli, Barabás, Michalska-Smith, & Allesina, 2017), the consequences of
56 this assumption in a transient, fluctuating or heavily perturbed system has yet to be fully explored.

57 Previous studies introducing interaction modifications to trophic networks (Arditi, Michalski, &
58 Hirzel, 2005; Goudard & Loreau, 2008; Lin & Sutherland, 2014) have demonstrated their potential
59 impact on the dynamics of ecosystems, but not whether this is attributable to the higher-order
60 nature of interaction modifications, or rather shifts in connectance and interaction strength.

61 One such important case is the dynamics of ecological systems in the face of species removal, where
62 there is the potential for secondary extinctions and eventually the collapse of the ecosystem (Dunne,
63 Williams, & Martinez, 2002). This aspect of stability, often described as ‘robustness’, is an important
64 question both from the perspective of managing anthropogenic change and in terms of
65 understanding the fundamental stability of ecological communities. Since empirically testing how
66 whole communities respond to extinctions can be difficult or impossible (although see Sanders et al.
67 (2018)), a number of studies have attempted to determine the properties that make ecological
68 communities robust through simulation (Dunne & Williams, 2009; Säterberg, Sellman, & Ebenman,
69 2013). However, incorporating the acknowledged flexibility of ecological networks is a perennial
70 challenge for such studies (Montoya, Pimm, & Solé, 2006).

71 The impact on the robustness of ecological networks of one specific subset of interaction
72 modifications, those caused by the flexible foraging in response to resource availability, has been
73 examined by a number of studies (Valdovinos, Ramos-Jiliberto, Garay-Narváez, Urbani, & Dunne,
74 2010). Approaches have included topological rewiring (Gilljam, Curtsdotter, & Ebenman, 2015;
75 Kaiser-Bunbury, Muff, Memmott, Müller, & Caflisch, 2010; Staniczenko, Lewis, Jones, & Reed-
76 Tsochas, 2010; Thierry et al., 2011), multi-species functional responses (Uchida & Drossel, 2007) and
77 adaptive foraging models (Kondoh, 2003). These models showed that the additional dynamic
78 process impacted robustness in contrasting directions, but only addressed a restricted subset of
79 interaction modifications caused by predator switching. However, consumption rates are influenced
80 by more than the just the choice of prey available to them. Interaction modifications can also be
81 caused by the threats to the consumer (Suraci, Clinchy, Dill, Roberts, & Zanette, 2016), facilitation
82 (Bruno, Stachowicz, & Bertness, 2003), associational susceptibility (Underwood, Inouye, & Hambäck,
83 2014) or mutualistic defence (Holland, Ness, Boyle, & Bronstein, 2005), amongst others (Ohgushi et
84 al., 2012). This introduces a considerable number of additional links between species to ecological
85 communities, yet studies of generic interaction modifications in large networks are limited (Arditi et
86 al., 2005; Bairey, Kelsic, & Kishony, 2016; Garay-Narváez & Ramos-Jiliberto, 2009; Goudard & Loreau,
87 2008; Lin & Sutherland, 2014), with most theoretical analyses of interaction modifications focussing
88 on small community units (Abrams, 2010; Bolker, Holyoak, Křivan, Rowe, & Schmitz, 2003; Holt &
89 Barfield, 2013).

90 Calls to incorporate the full panoply of non-trophic effects into our understanding of ecological
91 networks have built substantially in recent years (Fontaine et al., 2011; Ings et al., 2009; Kéfi et al.,
92 2012; Levine et al., 2017; Ohgushi et al., 2012; Olf et al., 2009) and the first empirical inventories are
93 being established (Kéfi et al., 2015; Kéfi, Miele, Wieters, Navarrete, & Berlow, 2016). Theoretical
94 analyses can play a significant role in motivating the empirical construction of networks, identifying
95 the information necessary to best understand these systems. Here we demonstrate the distinctive
96 nature of interaction modifications compared to pairwise non-trophic effects through a direct

97 standardised comparison of their impacts on the robustness of large artificial networks. We then
98 examine the role of interaction modifications in determining the consequences of species loss and
99 species level vulnerability to secondary extinction.

100 **Methods**

101 We conducted our analyses using model food webs where system dynamics are derived from
102 metabolic scaling relationships. As detailed below, interaction modifications were introduced to
103 communities at an initial equilibrium before mortality was added to a single species at a time and
104 examined the resultant extinctions after the model was integrated to a new equilibrium.

105 *Bio-energetic Model*

106 The change in biomass density, B_i , of each species in the community was modelled using a simple
107 Lotka-Volterra type model with a linear (Holling Type I) functional response and logistic intrinsic
108 growth rates, parameterised using body-mass relationships:

$$109 \quad \frac{dB_i}{dt} = B_i \left(r_i - m_i - \frac{B_i}{K_i} - \sum_{j \in \text{consumers of } i} \mu_{ij} a_{ij} B_j + \sum_{l \in \text{resources of } i} \mu_{li} e_{li} a_{li} B_l \right) \quad (1)$$

110 Each species was assigned a body mass (M_i) drawn from a distribution based on their trophic level
111 (see SI 1) which was then used to calculate further parameters using quarter-power body-mass
112 scaling laws (Yodzis & Innes, 1992). Relative intrinsic growth or metabolic loss rates, r_i , were set at 1
113 for all producers (trophic level 1) and $r_i = -0.1M_i^{-0.25}$ for each consumer (trophic level ≥ 2).
114 Consumer-specific consumption rates were set at $a_{ij} = \omega_j M_j^{-0.25}$, where the generality term ω_j was
115 set to $1/n$, the number of resources of each consumer j . Assimilation efficiencies, e_{ij} , for each
116 trophic interaction were drawn from a uniform distribution, $e_{ij} \sim \mathcal{U}(0.05: 0.15)$. Carrying capacities,
117 K_i , were drawn from $K_i \sim \mathcal{U}(1: 10)$ for producers (to introduce a moderate degree of self-regulation)
118 and $K_i \sim 10^{\mathcal{U}(2:3)}$ for consumers (considerably higher than the starting populations and so

119 introducing only a small amount of self-regulation). Initially, external mortality, m_i , was set to 0 and
120 modification terms, μ_{ij} , set to 1.

121 Trophic topology and population densities of starting communities were determined as follows.

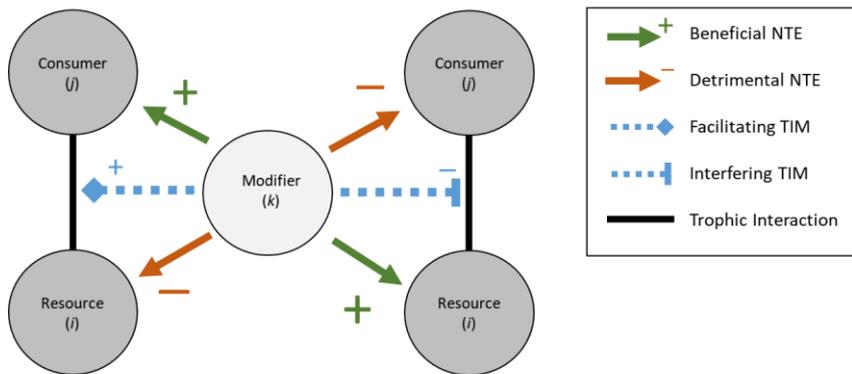
122 Initial trophic topologies were generated using the niche model (Williams & Martinez, 2000), with 35
123 species and a connectance of 0.14, removing cannibalistic interactions. Each population density was
124 initially set to 10 and these systems were then numerically integrated to a stable equilibrium (see SI
125 4 for criteria). This was repeated until 200 fully-connected communities with at least 18 persisting
126 species were generated to be used as starting communities for the robustness tests. Properties of
127 the starting communities are described in SI 2.

128 *Specification of TIMs*

129 Trophic interaction modifications were introduced to these communities through modification
130 terms, μ_{ijk} , that specify the impact of modifier species k on the consumption of species i by
131 species j , with the constraint that $i \neq j \neq k$. These are positive numbers that multiply the attack
132 rate as a function (detailed in the next section) of the divergence of the biomass density of a
133 modifying species, B_k , from its starting equilibrium value B_k^* . Where there are multiple modifications
134 of the same interaction these were assumed to combine multiplicatively $\mu_{ij} = \prod^k \mu_{ijk}$ (Golubski &
135 Abrams, 2011; Goudard & Loreau, 2008).

136 When $\mu_{ijk} < 1$, the interaction is weakened and when $\mu_{ijk} > 1$ the interaction is strengthened. In
137 our model μ_{ijk} can not be negative, preventing the reversal of the direction of the trophic
138 interaction. Where an increase in the modifier species leads to an increase in the strength of the
139 interaction, we describe it as a facilitating TIM. This can be said to be beneficial to the consumer and
140 detrimental to the resource, in the sense of the immediate impact from an increase in the modifier
141 population. We term the reverse situation an interfering TIM. See Figure 1 for diagrammatic
142 explanation of these terms.

143



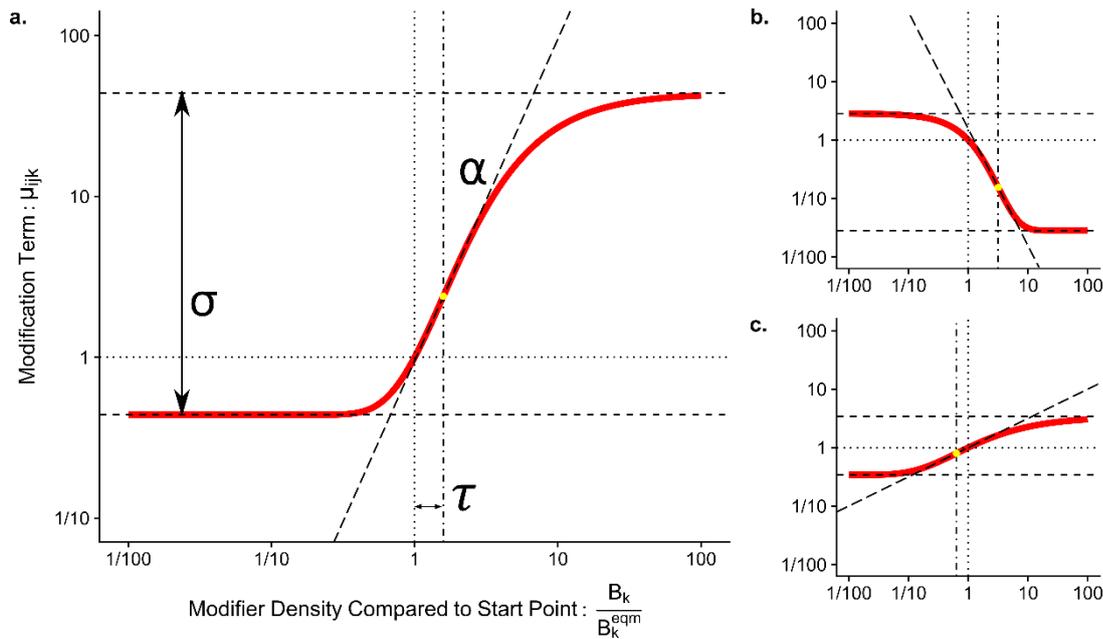
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145 *Figure 1. Distinctions between terms used to describe interaction modifications and their impacts in terms of*
 146 *the effect of an increase in the density of the modifier species (centre). ‘Facilitating’ and ‘interfering’ trophic*
 147 *interaction modifications (TIMs, dotted arrows) cause ‘beneficial’ and ‘detrimental’ short term non-trophic*
 148 *effects (NTEs, solid arrows), alternately on the consumer and the resource.*

149 *Functional Form of TIM*

150 To represent the relationship between the density of the modifier species and the modification of
 151 the interaction we used a Gompertz sigmoidal curve parameterised to control features of ecological
 152 relevance, detailed in full in SI 3. This function links the divergence of B_k from its start point,
 153 $\log_{10}(B_k/B_k^*)$, and three control parameters depicted in Figure 2. These are τ (the distance from the
 154 starting point the threshold point where the response to a change in modifier density is greatest), α
 155 (the direction and maximum rate of change in the modified interaction as the modifier density
 156 increases) and σ (the range of magnitudes over which μ_{ijk} spans). A positive α denotes a facilitatory
 157 modification and a negative α an interference modification. A key attribute of our parameterisation
 158 is that when $B_k = B_k^*$, $\mu_{ijk} = 1$. This maintains the original trophic interaction strength when the
 159 modifier is at its starting equilibrium point - in effect these strengths are assumed to already
 160 incorporate the effect of the modifier to the interaction at the equilibrium.

161



162

163 *Figure 2: Graphical representation of the relationship between the control parameters and the response of the*
 164 *sigmoidal function used to determine the modification term μ_{ijk} from the density of the modifier B_k . Panel a)*
 165 *uses a maximum slope (α) of 2, a distance to threshold (τ) of 0.2 and a range of effects (σ) to 2. Note that the*
 166 *function is calculated on a base 10 logarithmic scale. Parameters for panel b): $\alpha = -2$, $\tau = 0.5$, $\sigma = 2$ and panel c):*
 167 *$\alpha = 0.5$, $\tau = -0.2$, $\sigma = 1$.*

168 *Alternative representation of TIMs as Pairwise Non-Trophic Effects*

169 As an alternative to modelling the impact of trophic interaction modifications in full (using ‘higher
 170 order’ terms), equivalent pairwise non-trophic effects (NTEs) can be derived. These match the
 171 impact of the full TIM model, the only distinction being the NTE from a modifier k to a trophic
 172 interactor is no longer dependent on the biomass of the other member of the trophic pair (Figure 3).
 173 To maintain parity with the TIM model, this was done by first partitioning the process into trophic
 174 and non-trophic components, then fixing the value of the other trophic interactor to the density at
 175 the original equilibrium: $B_{int} = B_{int}^*$. Full steps of the derivation are in SI 6. A trophic interaction
 176 onto a resource influenced by a modifier can be partitioned from:

177

$$\frac{1}{B_i} \frac{dB_i}{dt} = \dots - \underbrace{\mu_{ij} a_{ij} B_j}_{\text{Trophic Term with TIM}} \quad (2)$$

178 to:

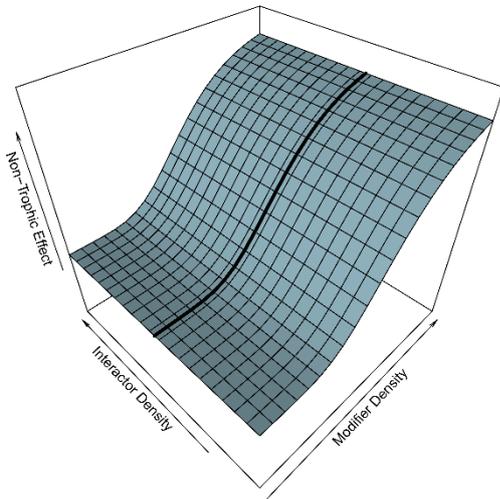
$$179 \quad \frac{1}{B_i} \frac{dB_i}{dt} = \dots \underbrace{-a_{ij}B_j}_{\text{Trophic Term}} + \underbrace{a_{ij}B_j^*(1 - \mu_{ij})}_{\text{Non-Trophic Term}} \quad (3)$$

180 The corresponding terms for the interactions onto the consumer, j , are:

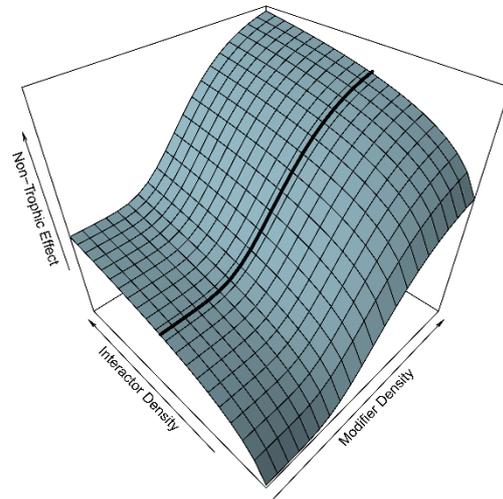
$$181 \quad \frac{1}{B_j} \frac{dB_j}{dt} = \dots + \underbrace{e_{ij}a_{ij}B_i}_{\text{Trophic Term}} + \underbrace{e_{ij}a_{ij}B_i^*(\mu_{ij} - 1)}_{\text{Non-Trophic Term}} \quad (4)$$

182 As an example, a facilitating TIM, when B_k increased, would lead to a μ_{ij} greater than 1. This would
 183 lead to a negative NTE on the resource i (independent of B_j) and a positive NTE on the consumer j
 184 (independent of B_i). This partitioning process is only straightforward when each trophic interaction
 185 is modified by at most one modifier species because of the synergistic relationship between multiple
 186 modifiers assumed by our model.

a. Pairwise Non-Trophic Effect



b. TIM Non-Trophic Effect



187

188 *Figure 3. Illustrative response surfaces showing the distinction between non-trophic effects caused by pairwise*
 189 *interactions and those from a higher-order interaction modification process involving three species. Per-capita*
 190 *effects are shown in the vertical axis on a logarithmic scale. In both cases, the response to the modifier is*
 191 *identical at the starting density of the trophic interaction partner of the focal species, shown by the black line.*
 192 *However, the density of the trophic interaction partner of the focal species (left-hand axis) does not affect the*

193 *non-trophic effect in the pairwise case (a), but does with the full interaction modification model (b). Note also*
194 *that as the interactor's density becomes small, the strength of the non-trophic effect rapidly declines.*

195 *Test 1. Comparison of robustness between pairwise NTE and higher-order TIMs*

196 To compare the consequences of introducing TIMs by the two approaches, we conducted three sets
197 of robustness tests using the same set of trophic networks. The first using the full-TIM model, the
198 second using the TIMs that had been converted to pairwise form, and a third case without any TIMs.

199 We randomly added TIMs to the set of initial communities such that each potential modification
200 (combination of trophic interaction and third species) had an equal 0.05 chance of existing. For this
201 test each interaction was modified by at most one other species to allow the conversion to non-
202 trophic effects. Shape parameters for each TIM were drawn from uniform distributions: slope
203 $\alpha \sim \mathcal{U}(-4: 4)$, range $\sigma \sim \mathcal{U}(0.1: 4)$ and threshold $\tau \sim \mathcal{U}(-1: 1)$. The location of TIMs and their
204 shape parameters were identical between the full-TIM and pairwise TIM cases.

205 For each robustness test, the external mortality rate (m_i) of a single species (to which we will refer
206 for convenience as the 'targeted' species, although the mortality could be attributable to a range of
207 non-directed processes) was then set to 1, the system numerically integrated to a new steady state
208 and the status of each species in the resultant community assessed. Species were considered
209 'extinct' if their biomass fell permanently below 10^{-4} (several orders of magnitude below the
210 starting values of most of the populations, SI 2), 'functionally extinct' if their biomass fell to below
211 $1/10^{\text{th}}$ of their starting value and considered to have 'exploded' if the final density was over 10 times
212 the starting value. Robustness tests were repeated targeting each species in turn, for each
213 community, to give a total of 3736 completed robustness tests (93.8% successful integrations, SI 4).
214 All analyses were carried out in R v.3.5.0 (R Core Team, 2018) using the *deSolve* numerical
215 integration package (Soetaert, Petzoldt, & Setzer, 2010).

216 *Test 2. TIMs and distribution of extinctions*

217 To examine the relationship between the distribution of TIMs and consequent secondary
218 extinctions, the robustness tests of the full TIM case as described above was repeated with a higher
219 occurrence rate of TIMs (0.08) and a relaxation of the assumption that only one modification can
220 affect each trophic interaction. Results are reported for parameters drawn from $\alpha \sim \mathcal{U}(-3: 3)$,
221 $\sigma \sim \mathcal{U}(0.1: 3)$, $\tau \sim \mathcal{U}(-1: 1)$. Further tests, with different TIM occurrence rates and distributions of
222 shape parameters, reached qualitatively similar results. Properties of the community and the
223 relationship between the ‘targeted’ species and the extinct species were then calculated.

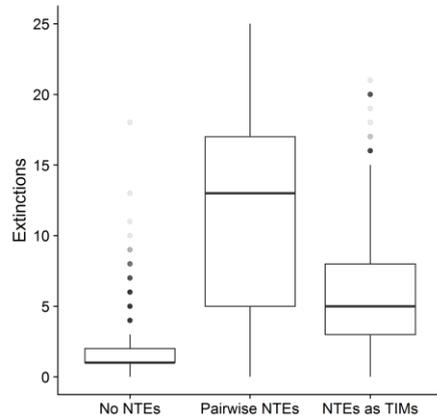
224 Firstly, for each robustness test, the trophic distance from the targeted species to each secondarily
225 extinct species was calculated. This is the number of trophic links between the targeted species and
226 the secondarily extinct species by the shortest route using the starting network. For this only the
227 trophic interactions were considered, not the TIMs. To generate a baseline to compare to, the
228 trophic distance from the targeted species to every other species was calculated.

229 Secondly, the NTEs affecting each extinct species was counted and classified by whether an increase
230 in the modifier would be beneficial or detrimental for the focal species. This was done for all NTEs
231 affecting the extinct species, and separately for just those derived from TIMs where the targeted
232 species was the modifier species. In our model, species that are involved in a greater number of
233 trophic interactions will tend to be the recipients of a greater number of NTEs. To distinguish the
234 effect of increased trophic degree from the number of NTEs, for each species we calculated the
235 expected number of incoming NTEs based on the number of trophic interactions and the species
236 richness of the network to generate a baseline. This actual number of incoming NTEs (beneficial or
237 detrimental) for each extinct species was then compared to this expectation baseline.

238 **Results**

239 The introduction of TIMs greatly increased the number of extinctions (Figure 4), but almost half the
240 number of extinctions were observed when the interaction modifications were modelled directly
241 compared to when they were modelled as pairwise effects (mean difference = 5.4, t-test paired by

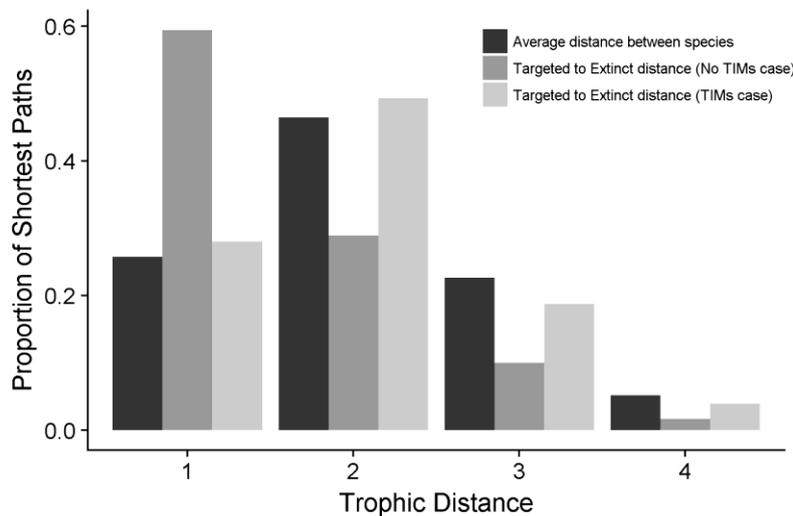
242 community and targeted species ID: $p < 0.0001$, $t = 61.5$, $df = 3941$). The number of functional
243 extinctions was very similar to full extinctions (means: No-TIM: 1.98, Pairwise: 11.33, Full-TIM: 5.85).
244 Population explosions were rare in all scenarios. Without NTEs there was a mean of 0.09 explosions
245 per robustness test, with nearly twice as many under pairwise NTE (0.189). The TIM case had the
246 fewest, only 0.05 explosions per robustness test.



247

248 *Figure 4. Boxplot showing that robustness was significantly lower when TIMs were modelled as pairwise*
249 *interactions rather than directly as interaction modifications. Both cases produced significantly more*
250 *extinctions than the no-TIM case.*

251 In robustness tests without TIMs nearly 60% of secondary extinctions were species directly
252 trophically linked to the targeted species (Figure 5). The introduction of TIMs shifted the trophic
253 distance (the number of trophic links between species by the shortest route) much closer to the
254 underlying distribution of trophic path lengths (Figure 5).



255

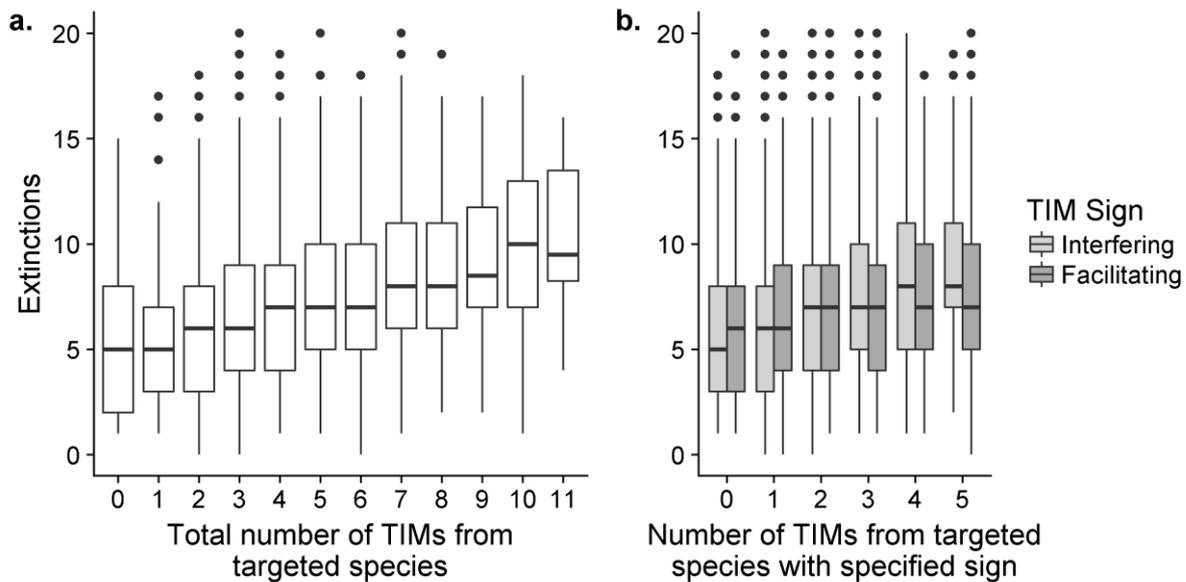
256 *Figure 5. Distribution of trophic distances between all species in the communities (black) and between targeted*
257 *species and secondarily extinct species in communities without TIMs (dark grey) and communities with TIMs*
258 *(light grey). The distance from the targeted species to the secondarily extinct species in the TIM case was*
259 *intermediate between the two baseline cases. Trophic distances above 4 were very rare in our model and not*
260 *shown.*

261 Secondarily extinct species tended to be recipients of both more beneficial (mean = 4.53) and more
262 detrimental (mean = 4.02) NTEs than would be expected to affect for a random species (mean =
263 3.79, (t-tests paired by species ID, all $p < 0.0001$, $n = 3576$). When counting just TIMs from the
264 targeted species, secondarily extinct species tended to have more beneficial (mean = 0.289) but
265 fewer detrimental (mean = 0.178) NTEs than the expected number (mean = 0.207, t-tests paired by
266 species ID, all $p < 0.0001$, $n = 3576$).

267 The targeting of species that caused more TIMs induced more extinctions (Figure 6a, Poisson glm,
268 $p < 0.0001$, $n = 3825$), with each additional TIM emanating from the targeting species leading on
269 average to an additional 7% secondary extinctions. Model fits splitting the sign of the TIMs (Figure
270 6b) indicated that each additional interference TIM caused a greater increase in the number of
271 extinctions (+10.4%), compared to each additional facilitatory TIM (+4.1%). Including the trophic

272 connectance of the web as an additional predictor variable did not give a significant improvement in
273 the model fit (χ^2 comparison of models, $p=0.113$).

274



275

276 *Figure 6. Boxplots showing the increase in the resultant number of extinctions as the number of TIMs caused by*
277 *the targeted species increased. Panel a) shows the response to the total number of TIMs, panel b) shows the*
278 *distinct responses to the number of each sign of TIM.*

279 Discussion

280 Here we have examined the ecological robustness of networks to demonstrate that interaction
281 modifications have distinct dynamic effects. In ecological systems, efforts to include non-trophic
282 effects into food webs (Fontaine et al., 2011; Piloosof et al., 2017) should take into account the
283 higher-order nature of interaction modifications. Without quantitative information of the
284 topological and strength distribution of TIMs it is not yet possible to precisely calculate their impacts
285 relative to trophic interactions. Nevertheless, it is clear that they have the potential to change our
286 expectation of both the relative vulnerability of species to extinction and the impact the loss of
287 certain species will have (Donohue et al., 2017).

288 We found that despite an increase in the number of ‘moving parts’ the full TIM model was more
289 robust than the exclusively pairwise model. Generally, unstructured dynamic models of community
290 stability suggest that a higher complexity is destabilising (May, 1972; Uchida & Drossel, 2007) making
291 our result somewhat surprising, but there are a number of explanations. The overall number of
292 direct relationships between species through all types of interaction (dynamic connectance)
293 between our two representations of TIMs is the same. In part, our result can be attributed to the
294 tendency for an overall decline in population densities under the perturbation. In the full-TIM model
295 the strength (and disruptive influence) of the impact is dependent on the product of two species and
296 so (in the context of generally declining species densities) will decline faster than when the strength
297 is dependent on just one species. Weaker effects between species due to TIMs will reduce the
298 potential for cascading effects. Furthermore, if the density of either a consumer or resource falls to
299 zero, any TIM impact on the species it is trophically linked to would also fall to zero under the full
300 TIM model. However, with the pairwise model the NTE is maintained even though the mechanism is
301 no longer extant. Hence, as species become extinct the effective dynamic connectance of the full
302 TIM model declines faster than in the pairwise case.

303 There are also differences between the full-TIM and the pairwise models in terms of the prevalence
304 and rapidity of local feedback loops. Feedbacks modulating the impact of TIMs are heavily
305 dependent on the relative speed and strength of multiple feedback loops, which in turn are derived
306 from properties of individual species. Despite our relatively simple model these loops are challenging
307 to trace in large complex systems (Dambacher & Ramos-Jiliberto, 2007), limiting qualitative analysis.
308 Nonetheless, as the impact of the more complex full-TIM model is dependent on more species, in
309 general, it appears that mitigating feedback loops can act faster in the full-TIM case. For example,
310 the effects caused by an interaction modification (however modelled) will cause an immediate
311 increase in one affected species and decrease in the other. In the full-TIM model, where the strength
312 of the interaction modification is dependent on $B_i \times B_j$, at least for a short time the strength of the
313 impact of the TIM on the consumer and the resource will be stay relatively constant since B_i and B_j

314 move in opposite directions. In the pairwise model the strength of the NTE on each species will
315 rapidly diverge with the potential to generate unrestricted positive effects on one of the
316 populations, with disruptive effects for the rest of the community. Over longer time-scales changes
317 in consumption rate lead to a consistent changes in the equilibrium values of both consumer and
318 resource, as can be demonstrated algebraically. In a simple module, a heightened consumption rate
319 leads to greater suppression of the resource which in turn can support a reduced population of
320 consumers (e.g. Morin, 2011). These distinct phases of responses to a change in consumption rate,
321 immediate biomass shifts in opposite directions before eventually moving towards a consistent
322 direction, highlights the multiple timescales over which TIMs operate. The analysis of the
323 contributing factors to these feedback loops would be a profitable area for future work.

324 At least in this simple model, it appears that TIMs determine extinction risk in a somewhat
325 predictable way. The extinction risk is shifted from those species that are closely trophically
326 connected to perturbed species, to be more evenly distributed throughout the network. Overall, the
327 species that went extinct tended to be those that were affected by more TIMs. When considering
328 NTEs from all species, this was true of both 'beneficial' and 'detrimental' NTEs. Those species that
329 directly benefit from the presence of other species are clearly affected by extinction cascades.
330 However, those species receiving an above-expectation number of detrimental NTEs were also at
331 higher risk of extinction. It would be expected that these species would benefit from the on-average
332 reduction or removal of their inhibitors. Note that the correlation between the increased species
333 level connectance and the number of modifications received was taken into account by comparing
334 expected number of TIMs on a per-species basis.

335 There are two complementary explanations for the equivalence of detrimental NTEs. Firstly, in a
336 complex model certain species do increase their density, at least for a period of time, which would
337 lead to have negative effect on the focal species. Initial responses to a small reduction in the
338 population of a single species were as commonly positive as negative (51.1% of non-zero growth-

339 rate responses to a 1% density reduction in a random species were positive in the TIM models, SI 5).
340 The low number of species maintaining large increases at the end of the process (what we defined
341 as population explosions) shows that such increases were relatively transient. When considering
342 only TIMs from the targeted species, which always decrease in density, extinct species received
343 fewer than expected detrimental NTEs, supporting this direct explanation. Secondly, in the simple
344 model of population dynamics we used, an increase in the attack rate of a consumer (which would
345 be classed as ‘beneficial’) eventually leads to a reduction in the equilibrium density of the consumer
346 since the population of resource is pushed down to a level that cannot sustain as high a consumer
347 population.

348 Much previous work has shown that complex networks are stabilised by consistent patterns in key
349 parameters, which can be derived from body-mass scaling rules (Brose, Williams, & Martinez, 2006;
350 Otto, Rall, & Brose, 2007). In our model this source of stability declines, as these patterns are
351 disrupted by interaction modifications that effectively push each a_{ij} value out of the allometrically
352 specified range in both directions. However, attack rates in real systems do take place in the context
353 of other species and significant disruptions to pairwise interaction strengths derived from laboratory
354 experiments caused by interaction modifications have been empirically observed (Jonsson,
355 Kaartinen, Jonsson, & Bommarco, 2018). Our results suggest that although species whose
356 interactions are aided by other species are indeed more sensitive to extinction, the overall number
357 of relationships with other species is as important and that both potential ‘beneficial’ and
358 ‘detrimental’ processes should be considered on an equal footing.

359 Our choice of function to represent interaction modifications, although mathematically complex in
360 form, offers certain advantages compared to previous linear (Arditi et al., 2005; Bairey et al., 2016),
361 exponential (Goudard & Loreau, 2008; Lin & Sutherland, 2014) or rational function (Sanders et al.,
362 2014) models. In particular, it has ability to directly and independently control salient features of the
363 function with clear ecological relevance (distance to threshold, maximum rate of change, range

364 between maximum and minimum). The dependence on the relative divergence from an equilibrial
365 starting point rather than the absolute value of the density of the modifier is also likely to be more
366 representative of ecological processes and considerably more straightforward to parameterise in an
367 ecologically meaningful manner.

368 Nevertheless, this is still a highly simplistic model. The interaction modifications included in this
369 study were introduced at random, in the sense that each potential modification had an equal chance
370 of existing. Considerable stabilising structuring has been observed within non-trophic effects
371 networks (Kéfi et al., 2015; Kéfi, Miele, et al., 2016) but there is not yet sufficient diversity of
372 examples to be able to determine whether there are consistent features across ecosystems.

373 Analyses of the stability of systems at equilibrium demonstrate the key role of the distribution in
374 terms of strength and position relative to the trophic network of interaction modifications (Terry,
375 Bonsall, & Morris, 2018) and the potential for emergent structure from the combination of trophic
376 and non-trophic interaction networks. The distribution of interaction modifications will have
377 important consequences for the use of structural network properties such as trophic coherence,
378 modularity and nestedness that have been demonstrated to affect stability (Johnson, Domínguez-
379 García, Donetti, & Muñoz, 2014; Stouffer & Bascompte, 2011; Thébault & Fontaine, 2010) since total
380 interaction networks, including non-trophic links, may display different patterns.

381 Interaction modifications do not solely affect consumption rates and there is considerable scope to
382 develop and test theoretical models of additional processes, such as non-trophic interaction
383 modifications and modification of other aspects of consumer functional responses (Kéfi et al., 2012).

384 The assumption of multiplicative combination of multiple TIMs in a synergistic manner in our second
385 analysis is also questionable. While empirical patterns have not been quantified, it is a reasonable
386 estimate that many modification effects act antagonistically to each other (Golubski & Abrams,
387 2011). For instance, the presence of a second fear-inducing predator may well have less effect than
388 the first, dampening the impact of a change in either modifier population.

389 Further opportunities are also open to introduce specific accounting for the timescale of changes
390 and the size of perturbations. It is possible that higher-order interactions are stabilising against small
391 perturbations, which may make the system as a whole more susceptible to large impacts, such as
392 the extinction of certain species (Levine et al., 2017). TIMs also have the potential to create the
393 necessary positive feedback structures to maintain alternative stable states (Holt & Barfield, 2013;
394 Kéfi, Holmgren, & Scheffer, 2016). As yet, the prevalence of these features is largely unknown. The
395 speed of interaction modifications themselves can also vary. While many TIMs are behaviourally
396 mediated and occur essentially instantaneously, others are due to accumulated environmental
397 changes (Sanders et al., 2014) or evolutionary processes (Benkman, Siepielski, & Smith, 2012) and
398 operate at somewhat slower timescales.

399 **Conclusion**

400 In summary, interaction modifications are potent forces that introduce distinct dynamics to
401 ecological networks. This distinctive nature of interaction modifications is of relevance for dynamic
402 systems in many fields that make use of networks (Strogatz, 2001) since our work shows that the
403 complexity of networks is more than the product of connectance and the number of interacting
404 units. Despite long-standing calls for the inclusion of non-trophic effects into the mainstream of
405 ecological network science that has been long dominated by food webs (Ings et al., 2009), and the
406 publication of the first empirical community level non-trophic network (Kéfi et al., 2015), there
407 remains a great number of significant unknowns about the role of non-trophic effects at the network
408 scale. Our work shows that maintaining interaction modifications as distinct processes within
409 empirical and theoretical networks, rather than as pairwise non-trophic effects (Grilli et al., 2017),
410 will enable us to have a more complete understanding of the system dynamics and allow better
411 predictions of community responses to perturbations. This need not require significant additional
412 effort on the part of the original investigator, but would be challenging for others to retroactively
413 discern from published pairwise interaction networks. Analyses of network robustness are used

414 extensively to understand anthropogenic impacts on natural communities (Evans, Pocock, &
415 Memmott, 2013; Kaiser-Bunbury et al., 2017; Säterberg et al., 2013); as the development and
416 analysis of comprehensive interaction networks expands (Kéfi, Miele, et al., 2016), we must
417 incorporate interaction modifications appropriately.

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421 **Data and Code Availability**

422 All R code used in this study and the generated simulation results are available on the Open Science
423 Framework: DOI: 10.17605/OSF.IO/W83BR

424 **Author Contributions**

425 JCDT initiated the research, and JCDT, MBB and RJM contributed to the ideas presented in the
426 manuscript. JCDT conducted the research, facilitated by discussions with RJM and MBB. JCDT wrote
427 the manuscript, and all authors contributed to revisions and approved the final version.

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