Constitutively active RAS in *S. pombe* causes persistent Cdc42 signalling but only transient MAPK activation

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Highlights

(1) Constitutively active Ras1.GV prolongs Cdc42 activation in *S. pombe* pheromone signalling

(2) Ras1.GV results in an immediate but only transient MAPK^{Spk1} activation

(3) The RAS effector pathways MAPK^{Spk1} and Cdc42 compete with each other for active Ras1

(4) Predictive modelling explains MAPK^{Spk1} activation dynamics in 24 signaling-mutants

eTOC Blurb

S. pombe Ras1 activates the MAPK^{Spk1} and Cdc42 pathways. Kelsall et al. report that the constitutively active Ras1.G17V mutation, which causes morphological anomalies, induces prolonged Cdc42 activation but only a transient MAPK^{Spk1} activation followed by attenuation. Mathematical modelling and biochemical data suggest a competition between the MAPK^{Spk1} and Cdc42 pathways for active Ras1.

Summary

The small GTPase RAS is a signalling hub for many pathways and oncogenic human RAS mutations are assumed to over-activate all of its downstream pathways. We tested this assumption in fission yeast, where, RAS-mediated pheromone signalling (PS) activates the MAPK^{Spk1} and Cdc42 pathways. Unexpectedly, we found that constitutively active Ras1.G17V induced immediate but only transient MAPK^{Spk1} activation, whilst Cdc42 activation persisted. Immediate but transient MAPK^{Spk1} activation was also seen in the deletion mutant of Cdc42-GEF^{Scd1}, a Cdc42 activator. We built a mathematical model using PS negative-feedback circuits and competition between the two Ras1 effectors, MAPKKK^{Byr2} and Cdc42-GEF^{Scd1}. The model robustly predicted the MAPK^{Spk1} activation dynamics of an additional 21 PS mutants. Supporting the model, we showed that a recombinant Cdc42-GEF^{Scd1} fragment competes with MAPKKK^{Byr2} for Ras1 binding. Our study has established a concept that the constitutively active RAS propagates differently to downstream pathways where the system prevents MAPK overactivation.

Key words

Ras, MAPK, Cdc42/Rac, yeast pheromone signalling

Introduction

Proto-oncogene Ras GTPase family members are widely conserved and play pivotal roles in cell growth, differentiation and apoptosis (Cox and Der, 2010). The physiological impact of Ras mutations is highlighted in the resultant tumorigenesis and developmental disorders (Prior et al., 2012; Schubbert et al., 2007). More than 99% of identified oncogenic RAS mutations occur at codons 12, 13 and 61 of human Ras isoforms (Prior et al., 2012) and impair efficient GTP hydrolysis (Trahey and McCormick, 1987). This results in accumulation of GTP-bound Ras, which is generally considered to cause constitutive activation of the downstream effector pathways, such as ERK and PI3K signalling pathways (Lin et al., 1998; Zhu et al., 1998). Interestingly, however, mouse embryonic fibroblasts (MEFs) derived from the *K-ras^{G12D}* mouse model show neither an increased basal level of active ERK and Akt nor constitutive activation of ERK and Akt upon growth factor stimulation even though the *K-ras^{G12D}* MEFs showed enhanced proliferation and partial transformation (Tuveson et al., 2004). This observation indicates that not all effector pathways become constitutively activated by oncogenic Ras, presumably because of an efficient negative feedback loop. Meanwhile, it is reasonable to expect that oncogenic RAS over-activates some of its effector pathways to initiate tumorigenesis. Small GTPases, including Cdc42 and Rac, may be such effector pathways, as they are required in oncogenic-RAS-driven tumorigenesis (Malliri et al., 2002; Qiu et al., 1997; Stengel and Zheng, 2012).

We wished to understand how multiple Ras effector pathways respond to the Ras-triggered signals in a physiological setting. We employed the model organism fission yeast. In this organism, a unique Ras homologue, Ras1, plays a key role in pheromone signalling to cause mating of haploid cells and sporulation in diploid cells (Yamamoto, 1996)(Fig. 1A, B). Upon nutritional starvation, cells of opposite mating types (*h$^+$* and *h$^-$*) exchange mating pheromones. Gpa1, the α-subunit of the pheromone receptor-coupled G-protein, relays the pheromone signal into the cell (Obara et al., 1991). Activated Gpa1 together with Ras1 then activate MAPK cascade consisting of Byr2 (MAPKKK), Byr1 (MAPKK) and Spk1 (MAPK) (Fukui et al., 1986; Masuda et al., 1995; Nadin-Davis and Nasim, 1988; Nadin-Davis et al., 1986a; Nadin-Davis et al., 1986b; Wang et al., 1991; Xu et al., 1994). An intriguing observation is that the *ras1.G17V* mutant, an equivalent of mammalian *ras.G12V* mutant prevalent in cancer, produces an excessively elongated shmoo, or a conjugation tube, upon exposure to the mating pheromone (Nadin-Davis et al., 1986a). This "elongated" *ras1.G17V* phenotype has been interpretted that Ras1 may be responsible for amplifying the pheromone signal (Yamamoto, 1996).

Ras1 also regulates cell morphology during vegetative growth; whilst deletion of either *gpa1*,

MAPKKK^byr2, *MAPKK^byr1* or *MAPK^spk1* does not result in any obvious phenotypes during vegetative

cell growth (Obara et al., 1991; Sipiczki, 1988; Toda et al., 1991), *ras1Δ* cells lose the typical rod-

shape morphology of fission yeast to become rounded (Fukui et al., 1989; Nadin-Davis et al.,

1986a). Studies based on recombinant protein assays and yeast-2-hybrid analysis demonstrated

that Ras1 interacts with both MAPKKK^Byr2 and Scd1, a GDP-GTP exchange factor (GEF) for Cdc42,

which regulates the actin cytoskeleton and cell morphology (Chang et al., 1994; Gronwald et al.,

2001; Tu et al., 1997). These observations suggest that Ras1 simultaneously regulates both the

pheromone MAPK^Spk1 and the Cdc42 pathways at the cell membrane (Weston et al., 2013).

Indeed, a dynamic "Cdc42 zone" at the cell cortex prior to mating has been observed (Merlini et

al., 2013) and Ras1 and MAPK^Spk1 cascade components are found there and are involved in the

process (Dudin et al., 2016; Merlini et al., 2013; Merlini et al., 2016; Merlini et al., 2018; Weston

et al., 2013). However, it is not yet understood how Ras1 interplay between the two pathways.

By establishing conditions to induce highly synchronous mating of fission yeast cells, for the first

time we were able to follow MAPK^Spk1 activation dynamics during the physiological mating

process in wildtype and in mutants showing various mating phenotypes. This comprehensive set

of quantitative measurements allowed us to build a mathematical model of the Ras-mediated

pheromone signalling. Our model serves as a prototype of a branched Ras-mediated signalling

pathway, demonstrating a competition of downstream pathways for a common upstream

activator, Ras1. The model also highlights the physiological importance of the bipartite

activation of MAPKKK^Byr2: a Ras1-dependent and a Ras1-independent mechanism, the latter of

which employs the adaptor protein Ste4 (Barr et al., 1996; Okazaki et al., 1991). The adaptor^Ste4

can be targeted to downregulate MAPK^Spk1 even in the presence of *ras1.G17V* mutation. Finally,

our study reveals the crucial role played by Cdc42 in the *ras1.G17V* mutant causing the

ras1.G17V phenotype.

Results

(1) A highly synchronous mating assay allows the precise measurement of MAPK^{Spk1} activity

To directly measure fission yeast pheromone signalling, we quantitated MAPK^{Spk1}

phosphorylation throughout the mating process (Supplementary Fig. S1, Fig. 1A and B). We

established a protocol to induce highly synchronous mating and employed cells where the

endogenous MAPK^{Spk1} is tagged with GFP-2xFLAG. Under these conditions, homothallic h^{90} cells

started to mate 7-hours after induction of mating (Fig. 1C, grey line). Phosphorylated (active)

MAPK^{Spk1} (**pp**MAPK^{Spk1}) levels were quantitated as described in Materials and Methods.

The **pp**MAPK^{Spk1} signal was first detected three hours after induction of mating and reached its

peak at about seven hours, when cell fusion was also initially observed (Fig. 1C, blue line.

Original membrane images presented in Supplementary Fig. S3). The **pp**MAPK^{Spk1} then gradually

decreased to a non-zero level as meiosis continued towards sporulation. The observation

established that the MAPK^{Spk1}-GFP activation occurs as the mating process progresses and

declines before sporulation, around 15 hours post induction. It was also noted that the total

MAPK^{Spk1}-GFP was essentially not expressed during the vegetative cycle, but it was promptly

induced by nitrogen starvation (Supplementary Fig. S2A and S2B). The *mapk^{spk1}* gene is a known

target of the transcription factor Ste11 (Mata and Bahler, 2006), which itself is activated

(phosphorylated) by MAPK^{Spk1} (Kjaerulff et al., 2005). This positive feedback loop likely

facilitates a swift increase of MAPK^{Spk1} expression upon nitrogen starvation.

We found that MAPK^{Spk1}-GFP localised to both the cytosol and the nucleus, with some nuclear

accumulation, before it gradually disappeared as the mating process came to the end (Fig. 1D).

Interestingly, transient foci of GFP signals were also found at the cell cortex, as has been

reported for MAPKK^{Byr1}, the activator of MAPK^{Spk1} (Dudin et al., 2016) (Fig. 1D, yellow arrows).

(2) Constitutively active MAPKK$^{Byr1.DD}$ mutant causes constitutive activation of MAPK^{Spk1}

Activation of MAPKK family kinases is mediated by dual phosphorylation of conserved Ser/Thr

residues (Zheng and Guan, 1994). These correspond to serine 214 and threonine 218 of the

MAPKK^{Byr1}. A MAPKK^{Byr1} mutant termed MAPKK$^{Byr1.DD}$, which carries aspartic acid substitution at

these sites, was expected to act as a constitutively active MAPKK (Ozoe et al., 2002). We

introduced the *MAPKK$^{byr1.DD}$* mutation at its chromosome locus and measured the activation

profile of its target, MAPK^{Spk1} during the mating process. The increase of the **pp**MAPK^{Spk1} signal

in the *MAPKK^byr1.DD* mutant strain was delayed compared to the wildtype strain and the

ppMAPK^Spk1 accumulated at a slower rate (Fig. 1E, light green line, original membrane images in

Fig. S3). However, the level of **pp**MAPK^Spk1 remained high after reaching its highest intensity at

around 16 hours after induction, resulting in a constitutive phosphorylation of MAPK^Spk1 (Fig. 1E

and Supplementary Fig. S2C and S2D). This result highlights that the suggested de-

phosphorylation of **pp**MAPK^Spk1 by phosphatases Pmp1 and Pyp1 (Didmon et al., 2002) is not

efficient in downregulating the pheromone signalling in the presence of MAPKK^Byr1.DD. The

MAPKK^Byr1.DD strain is also less competent in finding the partner mating cell than cells with

wildtype MAPKK^Byr1. We also confirmed the intriguing *"fus"* (fusion deficient) phenotype of cells

expressing MAPKK^Byr1.DD from its native promoter (Fig.1F) (Dudin et al., 2016; Ozoe et al., 2002).

These cells find their partners and pair up successfully but fail to fuse with each other, resulting

in *fus* phenotype. Consistent with the observed slower increase in **pp**MAPK^Spk1 (Fig.1E) the

nuclear localisation of MAPK^Spk1 was also delayed compared to Wildtype cells (Fig 1F). A strong

MAPK^Spk1-GFP signal was then observed in the nuclei of the paired *fus* cells and the nuclear

MAPK^Spk1-GFP signal persists even 24 hours after the induction of mating (Fig. 1F). Interestingly,

the projection tips of the paring cells often show increased MAPK^Spk1-GFP signal (Fig. 1F, yellow

arrows). These results conclude that MAPK^Spk1 activation is highly influenced by the MAPKK^Byr1

status and phosphatases directly regulating MAPK^Spk1 cannot counteract MAPKK^Byr1.DD.

(3) The *ras1.G17V* mutation causes immediate but transient MAPK^Spk1 activation

The fission yeast equivalent of human oncogenic *ras.G12V* is *ras1.G17V,* which induces an

excessively elongated shmoo, and the cells fail to recognize a partner and become sterile (Fukui

et al., 1986; Nadin-Davis et al., 1986a). The "elongated shmoo" phenotype was interpreted as

an excess activation of the downstream pathway(s) of Ras1, leading to a prediction that the

ras1.G17V causes over-activation of MAPK^Spk1 (Weston et al., 2013; Yamamoto, 1996). However,

no direct evidence has been provided.

Quantitation of the **pp**MAPK^Spk1-GFP in the *ras1.G17V* mutant showed an immediate increase of

the **pp**MAPK^Spk1-GFP upon induction of mating (Fig. 1G, Green line, original membrane images in

Fig. S3). However, the signal intensity declined gradually and by 16 hours after induction the

level was comparable to wildtype cells, indicating that down-regulation of **pp**MAPK^Spk1-GFP is

effective, unlike in *MAPKK^byr1.DD* mutant. Correspondingly, the cellular MAPK^Spk1-GFP signal also

declined 24 hours after induction of mating (Fig. 1H). Collectively, these observations indicate

that the down-regulation mechanism for **pp**MAPK^Spk1 is robust and resistant to Ras1.G17V. It

was also noted that the peak intensity of the **pp**MAPK^Spk1 was somewhat lower and the rate of

signal reduction was slightly decreased compared to wildtype cells (Fig. 1G).

(4) The elongated *ras1.G17V* shmoos develop with a minimum level of MAPK^Spk1: neither

amplitude nor duration of ppMAPK^Spk1 signal influences the *ras1.G17V* phenotype

Having observed that *MAPKK^byr1.DD* and *ras1.G17V* show different MAPK^Spk1 activation profiles

(sustained vs transient) and different morphological phenotypes ("*fus*" vs elongated), we

examined a link between the MAPK^Spk1 activation profiles and the cell morphology. The

MAPK^Spk1 phosphorylation profile of the cells harbouring both *ras1.G17V* and *MAPKK^byr1.DD*

mutations (*ras1.G17V MAPKK^byr1.DD* double mutant) was comparable to the cells harbouring

MAPKK^byr1.DD mutation only; it showed a slow increase of the **pp**MAPK^Spk1-GFP level, which

reached the plateau at about 16 hours after induction of mating (Fig. 2A, red line, original

membrane images in Fig. S3). The nuclear **pp**MAPK^Spk1-GFP signal in the *ras1.G17V MAPKK^byr1.DD*

double mutant was also present 24 hours after induction of mating, unlike the *ras1.G17V* single

mutant cells, confirming that the *ras1.G17V MAPKK^byr1.DD* double mutant cells retained a high

ppMAPK^Spk1 level. Thus, in terms of the activation status of MAPK^Spk1, *MAPKK^byr1.DD* is epistatic to

ras1.G17V.

In terms of cell morphology, the *ras1.G17V MAPKK^byr1.DD* double mutant cells showed the

"elongated" *ras1.G17V* phenotype (Fig. 2B), but not the "paired" *MAPKK^byr1.DD* phenotype.

Therefore, *ras1.G17V* was epistatic to *MAPKK^byr1.DD* in terms of the elongated shmoo

morphology.

Interestingly, obvious shmoo formation in the *ras1.G17V MAPKK^byr1.DD* double mutant was first

noticed 16 hours after induction of mating, much later than the *ras1.G17V* single mutant, but as

a similar timing as the *MAPKK^byr1.DD* single mutant (Fig. 2B). Given the slow increase of the

ppMAPK^Spk1 signal in mutants harbouring the *MAPKK^byr1.DD* mutation, we predicted that the

delayed appearance of the *ras1.G17V* shmoo meant that the *ras1.G17V* shmoo formation still

requires a certain level of MAPK^Spk1 activity. Indeed, when *MAPKK^byr1* was deleted in the

ras1.G17V mutant, not only was the MAPK^Spk1 activation and nuclear MAPK^Spk1-GFP signal

abolished (Fig. S1F), but also shmoo formation was abrogated as in the *MAPKK^byr1Δ* single

mutant (Fig. 2C). Based on these observations, we concluded that the cell morphology is

determined by the molecular status of Ras1, and not by the MAPK^Spk1 activation profile. Yet, the

ras1.G17V phenotype still requires MAPK^{Spk1} activity, which determines the timing of shmoo

formation.

(5) Cdc42 is required for the shmoo formation but not for the MAPK^{Spk1} activation

During the vegetative cycle, *ras1Δ* cells show spherical cell morphology (Fukui et al., 1986;

Nadin-Davis et al., 1986a) and polarised localisation of active Cdc42 is compromised (Kelly and

Nurse, 2011), (Fig. 4C, D), indicating that Ras1 is involved in Cdc42 activation. The GTP-loaded

Cdc42 is then predicted to activate the downstream Ste20-like kinase, Pak1/Shk1 (Endo et al.,

2003; Marcus et al., 1995; Ottilie et al., 1995; Verde et al., 1995), resulting in actin

reorganisation and shmoo formation under mating conditions (Bendezu and Martin, 2013;

Merlini et al., 2016).

To confirm that Cdc42 acts downstream of Ras1, we generated a double mutant strain

harbouring *ras1.G17V* and deletion of *scd1*, encoding a GDP-GTP exchanging factor for Cdc42

(Cdc42-GEF^{Scd1}). The *ras1.G17V* elongated shmoo phenotype was lost in the double mutant and

instead, the cells showed a mating-deficient phenotype similar to the *cdc42-GEF^{scd1}Δ* single

mutant (Fig 3A). The result supports the model that Cdc42 acts downstream of Ras1 to cause

morphological changes.

Intriguingly, in the strains harbouring the *cdc42-GEF^{scd1}Δ* mutation, a nuclear MAPK^{Spk1}-GFP

signal appeared (Fig. 3A), indicating that activation of MAPK^{Spk1} may not be impaired by lack of

active Cdc42. This was unexpected because in a previous study, it was predicted that activation

of Cdc42 contributes to activation of MAPKKK^{Byr2} (Tu et al., 1997). To clarify this issue, we

measured **pp**MAPK^{Spk1} in the *cdc42-GEF^{scd1}Δ* mutant. Strikingly, in these cells MAPK^{Spk1}

activation occurred with a reproducible advancement of the initial activation timing compared

to the wildtype cells (Fig. 3B, original membrane images in Fig. S3). The result shows that

MAPK^{Spk1} activation does not require Cdc42 activity. Additionally, the faster activation of

MAPK^{Spk1} raises the interesting possibility that two Ras1 effectors, MAPKKK^{Byr2} and Cdc42-

GEF^{Scd1}, are competing with each other for activated Ras1, thus, lack of Cdc42-GEF^{Scd1} results in

an advanced MAPK^{Spk1} activation (modelled in Fig. 7A).

Substantial MAPK^{Spk1} activation in the *cdc42-GEF^{scd1}Δ* mutant means that the mating deficiency

of this mutant is unlikely to be the result of the lack of MAPK^{Spk1} activation. Indeed, introduction

of *MAPKK$^{byr1.DD}$* to the *cdc42-GEF^{scd1}Δ* mutant did not restore the mating deficient phenotype,

even though nuclear MAPK^{Spk1}-GFP highly accumulated (Fig. 3C). The result shows that active

Cdc42 function is absolutely required for the mating process regardless of the MAPK^{Spk1}

activation status. Taken together with the essential role of MAPK^{Spk1}, we concluded that the

mating pheromone signalling feeds into at least two pathways, MAPK^{Spk1} and Cdc42.

(6) Ras1 activates two effector pathways, MAPK^{Spk1} and Cdc42.

In order to further clarify the role of Ras1 we examined the MAPK^{Spk1} activation status and cell

morphology in the following four strains: *ras1Δ* mutant, *ras1Δ MAPKK$^{byr1.DD}$* double mutant,

MAPKKK$^{byr2}Δ$ mutant and *MAPKKK$^{byr2}Δ$ MAPKK$^{byr1.DD}$* double mutant. As mentioned earlier,

deletion of *ras1* causes cells to show a round morphology (Fig. 3F), with reduced cortical signal

of CRIB-GFP, an indicator of the active GTP-bound form of Cdc42, showing that Cdc42 activation

is compromised (Fig.4C, D). *ras1* deletion also causes substantial reduction, but not complete

elimination, of the **pp**MAPK^{Spk1} (Fig. 3D, red line, and Supplementary Fig. S4A); thus, Ras1 plays

an important role in activating both Cdc42 and MAPK^{Spk1} pathways. Introduction of the

MAPKK$^{byr1.DD}$ mutation into the *ras1Δ* mutant cells induces the constitutive **pp**MAPK^{Spk1} (Fig. 3D,

green line and Supplementary Fig. S4A) but does not affect the round cell morphology and cells

remain sterile (Fig. 3F, the 2nd left panel. Note the accumulating MAPK^{Spk1}-GFP at 16 hours after

induction of mating), as was the case for the *Cdc42-GEF$^{Scd1}Δ$ MAPKK$^{byr1.DD}$* double mutant (Fig.

3C).

In a striking contrast, the sterile phenotype of the *MAPKKK$^{byr2}Δ$*, associated with complete lack

of shmoo formation (Fig. 3F, the 2nd right panel), was converted to the "*fus*" phenotype, when

combined with the *MAPKK$^{byr1.DD}$* mutation (Fig. 3F, the far right panel). As expected, the

MAPKKK$^{byr2}Δ$ MAPKK$^{byr1.DD}$ double mutant shows MAPK^{Spk1} constitutive activation (Fig. 3E and

Supplementary Fig. S4B). Thus, unlike the cases of *scd1Δ* or *ras1Δ*, lack of *MAPKKK^{byr2}* can be

bypassed by constitutive activation of MAPK^{Spk1}, indicating that the sole role of MAPKKK^{Byr2} is to

activate the MAPK^{Spk1} unlike its upstream activator, Ras1, which also activates Cdc42 pathway (a

model presented in Fig. 7A).

(7) Ras1.G17V causes accumulation of Cdc42-GTP at the cell cortex.

Having observed a relatively mild influence of Ras1.G17V towards the MAPK^{Spk1} activation, we

next examined whether the Cdc42 pathway was affected by the *ras1.G17V* mutation. We

visualized the active GTP-bound form of Cdc42 (Cdc42^{GTP}) using CRIB-GFP that specifically binds

to Cdc42^{GTP} (Tatebe et al., 2008). As previously observed, dynamic foci of CRIB-GFP appeared on

the cell cortex upon induction of mating (Bendezu and Martin, 2013)(Fig. 4A and B). In our

experimental condition, more than 80% of wildtype cells showed the cortical CRIB-GFP signal at

4.5 hours after induction of mating (Fig. 4B). The cortical CRIB-GFP foci became concentrated at

the site of mating and quickly disappeared once cells fused successfully to form zygotes (Fig. 4A

and B). In striking contrast, in the *ras1.G17V* mutant cells, the cortical CRIB-GFP signal persisted,

often at the elongated tip end of the cells, even 12.5 hours after induction of mating (Fig. 4A

and B). The signal could still be seen in about 40% of the cells 22.5 hours after induction of

mating (Fig. 4A and B). The result shows that the Cdc42 pathway is excessively activated in the

ras1.G17V mutant and the localisation pattern of Cdc42^{GTP} indicates that the signature

"elongated" *ras1.G17V* morphological phenotype is caused by deregulation of the Cdc42

pathway.

Ras1-mediated Cdc42 pathway activation has been also indicated during the vegetative growth

where the *ras1Δ* mutant shows a round cell morphology (Chang et al., 1994; Kelly and Nurse,

2011). However, unlike during the mating process, the *ras1.G17V* mutation does not cause an

obvious morphological phenotype during the vegetative growth. We predicted that, during the

vegetative growth, rigorous negative regulation occurs for Cdc42 by GTPase activation

protein(s) (GAPs), such as Rga4 (Das et al., 2007; Kelly and Nurse, 2011; Tatebe et al., 2008) to

counteract the effect of *ras1.G17V*. To examine this possibility, we compared Cdc42 activation

status of vegetatively growing wildtype, *ras1Δ*, *ras1.G17V*, *rga4Δ*, and *rga4Δ ras1.G17V* double

mutant cells (Fig. 4C and D). As previously described, CRIB-GFP showed a clearly polarized signal

at the growing cell tips in the wildtype strain (Tatebe et al., 2008)(Fig. 4C and D). In the *ras1Δ*

mutant, the cells were round and CRIB-GFP signal on the cell cortex had largely disappeared as

was seen in the *cdc42-GEF^{scd1}Δ* mutant (Kelly and Nurse, 2011). In contrast, the cortical CRIB-

GFP signal was clearly increased in the *ras1.G17V* single mutant although the cell morphology

appeared largely similar to the wildtype cells (Fig. 4C, D). These results indicate a direct

involvement of Ras1 in activating Cdc42. Meanwhile, the *rga4Δ* mutant cells showed slight

alterations to the cell morphology, accompanied with less polarized distribution of cortical CRIB-

GFP signal, as has been reported (Fig. 4C and D) (Das et al., 2007; Kelly and Nurse, 2011; Tatebe

et al., 2008). Strikingly, the *rga4Δ ras1.G17V* double mutant showed a clear morphological

alteration (big round cells) and the strongest cortical CRIB-GFP signal among all the mutants

examined (Fig. 4C and D). The result fits well with our hypothesis that Ras1.G17V is activating

Cdc42 even during vegetative growth, but the overall effect of Ras1.G17V is counteracted by the

Cdc42-GAP, Rga4.

(8) Ras1 and an adaptor protein Ste4 are both necessary to fully activate MAPKKK^{Byr2}

Although Ras1 clearly plays the major role to activate MAPK^{Spk1}, a marginal, but detectable level

of **pp**MAPK^{Spk1} was still induced in the *ras1Δ* mutant (Fig. 3D and Supplementary Fig. S4A),

indicating that there is a Ras1-independent mechanism to activate MAPK^{Spk1}. Previous studies

proposed an adaptor protein, Ste4, to be involved in the activation of MAPKKK^{Byr2}(Barr et al.,

1996; Okazaki et al., 1991; Ramachander et al., 2002; Tu et al., 1997). We therefore examined

whether Ste4 is required for MAPK^{Spk1} activation.

In contrast to the *ras1Δ* mutant, we detected virtually no MAPK^{Spk1} phosphorylation in the

ste4Δ mutant (Fig. 5A and Supplementary Figure S4C), indicating that the adaptor^{Ste4} is a

prerequisite for the MAPK^{Spk1} activation and the **pp**MAPK^{Spk1} signal observed in the *ras1Δ*

mutant is dependent on Ste4 function. Introduction of *ras1.G17V* mutation neither restored the

MAPK^{Spk1} activation nor mating (Fig. 5A, B), thus, activation of Ras1 cannot take over Ste4

function. In a striking contrast, the *ste4Δ MAPKK$^{byr1.DD}$* double mutant showed the *"fus"*

phenotype as the *MAPKK$^{byr1.DD}$* single mutant cells and induced constitutive MAPK^{Spk1} activation,

indicating that Ste4 is solely required for MAPK^{Spk1} activation (Fig. 5A, B).

Taken together, MAPKKK^{Byr2} is activated through a mechanism involving both Ras1 and Ste4, but

Ste4 only conveys the signal towards the MAPK^{Spk1}, while Ras1 also activates Cdc42.

(9) Ste6, a Ras1 GTP-GDP exchange factor, contributes to both the MAPK^{Spk1} and the Cdc42

pathway activation

There are two GDP-GTP exchange factors (GEFs) identified for Ras1: Ste6 and Efc25 (Hughes et

al., 1990; Tratner et al., 1997). As to the functional differences, Ste6 is essential for mating but is

dispensable during the vegetative cycle whilst Efc25 is dispensable for mating but is required to

maintain the cell morphology during the vegetative growth (Hughes et al., 1990; Tratner et al.,

1997). There has been an interesting proposition that Ste6 may specifically help Ras1 to activate

the MAPK^{Spk1} pathway, but not the Cdc42 pathway, whilst Efc25 specifically facilitates Ras1 to

activate the Cdc42 pathway (Papadaki et al., 2002). We examined this hypothesis by monitoring

the MAPK^{Spk1} activation status and conducting genetic epistasis analysis of *ras1.G17V* and *MAPKK$^{byr1.DD}$* in the *ste6Δ* mutant.

In *ste6Δ* cells, MAPK^{Spk1} phosphorylation was found somewhat reduced but occurred at a clearly detectable level. The signal increased when the *ras1.G17V* mutation was introduced (Fig. 5C and Supplementary Figure S4D). When *ste6Δ and MAPKK$^{byr1.DD}$* were combined, MAPK^{Spk1} signalling recapitulated the *MAPKK$^{byr1.DD}$* activation profile (Fig. 5C and Supplementary Figure S4D). Nonetheless, the "pheromone-insensitive sterile" morphology of *ste6Δ* was only rescued by *ras1.G17V*, as previously reported, exhibiting the "elongated" phenotype (Hughes et al., 1990), but not by MAPKK$^{byr1.DD}$ (Fig. 5D). The result indicates that, unlike *ste4Δ* mutant, the mating deficiency of *ste6Δ* is not caused by mere lack of MAPK^{Spk1} activation but by lack of Ras1 activation. We concluded that Ste6 functions to activate Ras1, which then activates *both* the MAPK and Cdc42 pathways in response to pheromone signalling.

(10) Activation mutant of Gpa1 mimics the full pheromone signalling

In order to generate an integrated prototype Ras signalling model, we further investigated the upstream signal input machinery. Previous studies showed that Gpa1 plays the primary role in pheromone signalling (Obara et al., 1991). In agreement, in the *gpa1Δ* mutant we detected no MAPK^{Spk1} activation nor nuclear accumulation of MAPK^{Spk1}-GFP (Fig. 6A, B and Supplementary Fig. S5A). Introducing the *ras1.G17V* to the *gpa1Δ* strain did not rescue the complete lack of *MAPK^{Spk1}* activation nor did it induce a shmoo-like morphological change (Fig. 6A, B and Supplementary Fig. S5A), supporting our earlier observation that a Ras1-independent mechanism, involving Ste4 is essential for MAPK^{Spk1} activation. Meanwhile, introducing the *MAPKK$^{byr1.DD}$* mutation caused the constitutive activation of MAPK^{Spk1} (Fig. 6A and Supplementary Fig. S5A), but cells showed no morphological change (Fig. 6B). When both *ras1.G17V* and *MAPKK$^{byr1.DD}$* mutations were introduced into the *gpa1Δ* strain, MAPK^{Spk1} was activated and a shmoo-like morphological change occurred (Fig. 6A, B and Supplementary Fig. S5A). Therefore, activation of both of these two molecules is required and sufficient to mimic the pheromone signalling.

To further confirm that the Gpa1 is a central component of pheromone signalling, we looked into the MAPK^{Spk1} activation status in the constitutively active *gpa1.QL* mutant, which exhibits a "shmoo-like" morphological change in the heterothallic *h⁻* strain without the mating partner (Obara et al., 1991).

Upon nitrogen starvation, the *h⁻ gpa1.QL* mutant strain showed morphological changes and a

strong MAPK^{Spk1} activation (Fig. 6C red line, Fig. 6D and Supplementary Fig. S5B). This response

was largely dependent on the Ras1 function as the *h⁻ gpa1.QL ras1Δ* double mutant exhibited a

significantly reduced level of **pp**MAPK^{Spk1} and a round cell morphology, two typical features of

ras1Δ cells (Fig. 6C, D and Supplementary Fig. S5B). On the other hand, the *h⁻ ras1.G17V* single

mutant showed a very low level of MAPK^{Spk1} activation, comparable to the one observed in the

h⁻ wildtype strain, with no apparent morphological alternation, confirming that sole activation

of Ras1 does not substitute the pheromone signalling.

The *h⁻ MAPKK$^{byr1.DD}$* mutant induced a strong constitutive MAPK^{Spk1} activation, confirming that

the MAPKK$^{Byr1.DD}$ molecule can activate MAPK^{Spk1} regardless of the pheromone signal input (Fig.

6C, light-blue line and Supplementary Fig. S5B). However, cell morphology was unchanged (Fig.

6D). Collectively, these results support the model where Gpa1 acts as the central transducer of

the pheromone signalling, which can be mimicked only if both MAPK^{Spk1} and Ras1 are activated.

(11) A holistic modelling framwork of MAPK^{Spk1} activation

Based on quantitative **pp**MAPK^{Spk1} measurements in wildtype and various mutant strains (Fig.

1C, E, G, and Fig. 3B), we constructed a mathematical model of the MAPK^{Spk1} signalling

dynamics. The aim of the model is to test whether a simple competition of the MAPK and the

Cdc42 pathways for a shared pool of active Ras^{GTP}, can explain why the *scd1Δ* strain shows the

similar **pp**MAPK^{Spk1} activation profile as the *ras1.G17V* strain.

We designed a reductionist model of 6 ordinary differential equations to represent key steps of

pheromone signalling (Fig. 7A, Supplementary Fig. S6 and materials and methods). Model

simulations and parameter estimations were performed in COPASI (Hoops et al., 2006) and

details of the modelling process are described in Materials and Methods. Each biochemical

process is referred as [L1]-[L10] as depicted in Fig. 7A. All the signalling components were set to

be in close proximity, based on our own observation (Fig. 1 and Fig. 4) and recent series of

localization studies (Dudin et al., 2016; Merlini et al., 2016; Merlini et al., 2018). This allowed the

model to predict some signaling to involve protein-protein interactions.

The framework of the modelling process is as follows: Genes encoding pheromones, receptors,

Gpa1, Ste4 and Ste6 are all known to be under regulation of Ste11, the master transcriptional

regulator for meiotic genes (Hughes et al., 1994; Mata and Bahler, 2006; Mata et al., 2002; Mata

et al., 2007; Sugimoto et al., 1991) and these components are grouped into the Pheromone

Sensing (PS) unit. During the vegetative growth, the PS unit is set to zero. Nitrogen starvation

activates Ste11 (Kjaerulff et al., 2007; Sugimoto et al., 1991), which induces the PS unit [L1]. The

PS unit activates MAPKKK[Byr2] in a twofold manner: Directly by Ste4 [L3] and through Ras1

[L4](Fig. 7A). Activated MAPKKK[Byr2] then triggers activation of MAPKK[Byr1] [L5] that activates

MAPK[Spk1] [L6]. Since activated MAPK[Spk1] further activates Ste11 (Kjaerulff et al., 2005), MAPK[Spk1]

has a positive feedback loop on its own expression via Ste11 [L2,L7] (Fig. 7A).

As the pheromone signalling was found to induce a transient **pp**MAPK[Spk1] peak (Fig. 1C),

ppMAPK[Spk1] activity is ought to be regulated by a delayed downregulation. Because the

MAPKK[byr1.DD] mutant completely lacks downregulation (Fig. 1E), downregulation occurring

downstream of MAPKK[byr1] (e.g.: Pyp1 and Pmp1) were considered physiologically insignificant.

Meanwhile, Sxa2 (a serine carboxypeptidase against a mating pheromone P-factor) and Rgs1 (a

regulator of Gpa1), both of which are induced upon successful pheromone signalling (Imai and

Yamamoto, 1992; Mata and Bahler, 2006; Pereira and Jones, 2001; Watson et al., 1999),

receptor internalization (Hirota et al., 2001) and regulation of the *mapk[spk1]* transcript or other

components by antisense RNA (Bitton et al., 2011) fit well to the criteria for the negative

feedback. We represented all these potential negative feedbacks collectively as a single circuit,

[L8]. Importantly, this downregulation [L8] works unperturbed in the presence of Ras1.G17V, by

acting through the Ste4-dependent MAPKKK[Byr2] activation process (Fig. 1G, Fig. 7A).

Ras1-GTP activates both the MAPKKK[Byr2] and the Cdc42 pathways [L9] (Chang et al., 1994). As

opposed to previous expectations that active Cdc42[GTP] is required to activate MAPKKK[Byr2] (Tu et

al., 1997), deletion of Cdc42-GEF[Scd1] does not compromise MAPK[Spk1] activation (Fig. 3B) and

rather, it makes **pp**MAPK[Spk1] dynamics remarkably similar to that of the Ras1.G17V strain (Fig.

3B and Fig. 1G, plotted together in Fig. 7B): in both cases, **pp**MAPK[Spk1] peaks earlier than the

wildtype case. At a molecular level, reactions depleting the Ras1[GTP] pool are compromised in

both strains. Therefore, to explain these observations, we hypothesized that MAPK[Spk1] and

Cdc42 pathways are competing for the common Ras1[GTP] pool. In this manner, one of the

pathways can modulate the other by changing the amount of unbound (available) Ras1[GTP].

In support of this prediction, we showed that binding of recombinant Ras1.G17V[GTP] to a

MAPKKK[Byr2] fragment was reduced by the presence of a Cdc42-GEF[Scd1] fragment *in vitro* (Fig. 7C,

D). In this assay, bacterially expressed GST tagged fragments of both MAPKKK[Byr2] (65-180) and

Cdc42-GEF[Scd1] (760-872) showed a specific binding towards the GTP-loaded Ras1.G17V (1-172)

(Fig. 7C). However, the binding of Ras1.G17V[GTP] to MAPKKK[Byr2] was substantially decreased

when the Cdc42-GEF^{Scd1} fragment was added (Fig. 7D). The result likely refects the intrinsic

biochemical competitive nature of MAPKKK^{Byr2} and Cdc42-GEF^{Scd1} for Ras1 binding. As we show

below, this simple hypothesis successfully describes pheromone signalling mutants tested in this

study, suggesting that no unproven cross links are necessary to reproduce the *in vivo*

observations.

An intriguing common feature observed in both Cdc42-GEF^{scd1}Δ and *ras1.G17V* mutants is that

ppMAPK^{Spk1} peaks not only at an earlier time point, but also with a *lower amplitude* as

compared to the wildtype. If increased Ras1^{GTP} levels simply accelerate MAPK^{Spk1} activation, as

has been conventionally assumed, **pp**MAPK^{Spk1} production should peak earlier *and higher*

(Supplementary Fig S7B, best fit out of 1000 global fits), and the addition of Ras1^{GTP} only should

increase the amplitude, but not affect timing (Supplementary Fig S7C). We confirmed these

results in the best models from 1000 global fits (Materials and Methods). The comparison

between our experimental results and the *in silico* predictions suggests that the role of Ras1^{GTP}

is more complex than previously thought.

Strikingly, if we hypothesize that Ras1^{GTP} also contributes to the negative feedback [L10] (Fig.

7A), we recapitulate the "*earlier and lower*" peak of **pp**MAPK^{Spk1} in both the *ras1.G17V* and the

Cdc42-GEF^{scd1}Δ mutants (Fig. 7B). We currently do not have a direct experimental evidence to

support [L10]. However, considering the fact that Ras1^{GTP} likely acts as a physical signalling hub

at the cell cortex, mediating MAPKKK^{Byr2} recruitment and activation, which leads to recruitment

of MAPKK^{Byr1} and MAPK^{Spk1}, Ras1^{GTP} may work as a two-way amplifier, both assisting localized

MAPK^{Spk1} activation at the shmoo site, as well as helping the negative feedback by concentrating

the affected molecules.

The model successfully recapitulated the experimental results for wildtype, *ras1.G17V*,

MAPKK$^{Byr1.DD}$ and *cdc42-GEF^{scd1}Δ* mutants (Fig. 7B). To test the predictive capacity of the model,

we next performed an *in silico* experiment where we titrated increasing amounts of Ras1^{GTP} in

the wildtype condition before nitorgen removal. In agreement with our hypothesis, we obtained

a *ras1.G17V*-like **pp**MAPK^{Spk1} activation profile with increasing amount of Ras1^{GTP}, i.e., the

ppMAPK^{Spk1} peaks earlier with a lower peak intensity (Fig. 7E). The result further supported that

Ras1^{GTP} availability alone is sufficient to explain both the *ras1.G17V* and *Cdc42-GEF^{scd1}Δ*

phenotypes.

To further test the predictive value of the model, we asked whether it could predict **pp**MAPK^{Spk1}

dynamics in the 21 other strains, which were measured (Fig. 2-6), but not used for fitting the

model. We implemented each mutation in the wildtype model (Supplementary Table S2) and

the model accurately predicted relative **pp**MAPK^{Spk1} dynamics in 17 cases, or showed

predicitons in close proximity to the observed **pp**MAPK^{Spk1} dynamics in the 4 remaining cases

(Fig. 7F). Concluding from these results, our model likely represents the physiological framework

of fission yeast RAS-MAPK signalling.

Discussion

By quantitating the MAPK^{Spk1} and Cdc42 activation status during the mating process and

conducting epistasis analysis between numerous signalling mutants, we showed that Ras1

coordinates activation of both the MAPK^{Spk1} cascade and the Cdc42 pathway. Furthermore, we

revealed that the *ras1.G17V* mutant phenotype is caused by deregulation of Cdc42, rather than

altered activation of MAPK^{Spk1} in physiological setting. Based on the experimental data, we built

a mathematical model, incorporating an assumption that two Ras1 effectors, Cdc42-GEF^{Scd1} and

MAPKKK^{Byr2}, are competing for active Ras1. This is the first simulation of a physiological Ras

signalling network in a whole organism. The model faithfully recapitulates MAPK^{Spk1} activation

profiles in the wildtype and all mutant strains examined in this study. The model implies that

targeting one of the RAS effector pathways can potentially result in a complex outcome, rather

than simply shutting down the targeted effector pathway. We concluded that fission yeast

pheromone Ras signalling is not only defined by compartmentalisation (Onken et al., 2006) but

rather a coordination of events involving both the MAPK^{Spk1} and Cdc42 pathways.

Coordinated activation of MAPK and Cdc42 pathways upon pheromone stimulation is a

common feature shared by budding yeast pheromone signalling. In budding yeast, however, Ras

homologues are not involved in the process. β and γ subunits of the receptor-coupled trimeric

G-protein act as the hub to activate both pathways ((Hegemann et al., 2015; McClure et al.,

2015), reviewed in (Atay and Skotheim, 2017)). It is intriguing that the key hub moleucules are

evolutionary diverged in these yeast species whilst the effector pathways are conserved to bring

comparable biological outcomes.

In this study, we confirmed that Gpa1, the α subunit of the receptor-coupled trimeric G-protein,

is the central player of the pheromone signalling. It is likely that Gpa1 is the most downstream

molecule conveying the complete pheromone signal. Considering that all the pheromone

signalling components examined so far have been found at the shmoo site (Dudin et al., 2016;

Merlini et al., 2016; Merlini et al., 2018)(this study), an attractive hypothesis is as follows: firstly,

the activated pheromone receptor Map3/Mam2 locally activates Gpa1, which activates Ras1

and MAPK[Spk1]. This then leads to a localised activation of the Cdc42, causing shmoo formation in

the direction of a mating partner (Fig. 8A).

The *ras1.G17V* mutation led to an immediate activation of MAPK[Spk1] compared with the

wildtype cells. The G17V mutation of Ras1 is equivalent of G12V mutation of mammalian RAS,

which results in a substantial reduction of both intrinsic and GAP-mediated GTPase activities

(Trahey and McCormick, 1987). Therefore a larger fraction of Ras1 is expected to be in the

active GTP-bound form in the *ras1.G17V* mutant cells. By mathematical modelling, we showed

that the increased Ras1[GTP] pool can explain a faster activation of MAPK[Spk1].

To our surprise, the constitutive Ras1.G17V mutation did not induce over-activation of

MAPK[Spk1]. The attenuated MAPK[Spk1] activation in the presence of Ras1.G17V indicated that an

efficient feedback mechanism is in place to counteract the effect of Ras1.G17V. Strikingly, the

same trend has been reported in the mouse model of the *K-ras[G12D]* mutation integrated at the

endogenous chromosome locus (Tuveson et al., 2004). Therefore it is highly likely that the

MAPK cascade is generally robust against upstream oncogenic constitutive stimulation.

Based on our observation that the MAPK[Spk1] is constitutively activated in the *MAPKK[byr1.DD]*

mutant, we predict that the negative regulation occurs upstream of, or at the same level as,

MAPKK[Byr1], rather than phosphatases that directly regulate MAPK[Spk1]. In humans, ERK is shown

to phosphorylate RAF proteins, the prototype MAPKKKs, to contribute to ERK signal attenuation

(Brummer et al., 2003; Dougherty et al., 2005; Ritt et al., 2010). In future studies it will be

important to determine whether MAPK[Spk1] can directly downregulate MAPKKK[Byr2] in a

physiological setting.

Our results also show that an adaptor[Ste4] plays a crucial role in activating MAPKKK[Byr2], abolishing

ppMAPK[Spk1] production even in the presence of *ras1.G17V* mutation. This suggests that the

adaptor[Ste4] fits well to be one of the major targets by the negative feedback loop against

ppMAPK[Spk1]. This mechanism is shared by budding yeast, where an adaptor protein, Ste50,

modulates MAPKKK[Ste11] (Ramezani-Rad, 2003). In humans, although such an adaptor protein for

RAF proteins has yet to be identified, multiple RAF-interacting proteins, including 14-3-3

proteins, as well as formation of heterodimers between BRAF and CRAF, have been studied for

their Ras-independent mechanism to activate RAF proteins (Lavoie and Therrien, 2015).

Collectively, MAPK cascades seem to retain a general resistance to oncogenic RAS mutations in

physiological settings (Fig. 8B).

Whilst lack of Cdc42 activation does not impair MAPK^{Spk1} activation, we found that MAPK^{Spk1}

activity is required for shmoo formation even in the presence of Ras1.G17V (Fig. 2C). Therefore,

the two Ras1 effectors, Cdc42 and MAPK^{Spk1} pathways, are not completely separable. The

situation is reminiscent of the *K-ras^{G12D}* MEFs (Tuveson et al., 2004). In this system, the *K-ras^{G12D}*

MEFs showed morphological anomalies. As both ERK and AKT phosphorylation levels in the *K-*

ras^{G12D} MEFs resembled wildtype, these pathways unlikely caused the morphological

phenotype. Nonetheless, inhibitors against MAPK and PI3K pathways reverted the *K-ras^{G12D}*–

induced abnormal morphology back to the one similar to wildtype. The observation suggests

that MAPK and PI3K pathways somehow contribute to the *K-ras^{G12D}* morphological phenotype;

for example, a basal level of MAPK and PI3K pathway activation may be a prerequisite for the *K-*

ras^{G12D}–induced morphological anomalies.

The molecular mechanism of how MAPK^{Spk1} contributes to Cdc42 activation will require further

studies. Key components in pheromone signalling are transcriptionally up-regulated upon

pheromone signalling (Xue-Franzen et al., 2006). This is driven by MAPK^{Spk1}, which activates the

master transcriptional regulator Ste11 (Kjaerulff et al., 2005; Mata and Bahler, 2006; Xue-

Franzen et al., 2006). Therefore, the contribution of MAPK^{Spk1} to Cdc42 activation is expected to

occur, at least partly, through transcriptional activation.

In addition, localisation of signalling components may be regulated by MAPK^{Spk1}. In budding

yeast, MAPK^{Fus3} brings Cdc24, the GEF for Cdc42, to the shmoo site by phosphorylating an

adaptor protein Far1 (Hegemann et al., 2015), which otherwise sequesters Cdc24 into the

nucleus (Nern and Arkowitz, 2000; Shimada et al., 2000). Fission yeast does not have an obvious

Far1 homologue but MAPK^{Spk1} may also directly phosphorylate and activate Cdc42 and/or its

regulatory proteins such as Cdc42-GEF^{Scd1}, Scd2 or GAP-Cdc42^{Rga4}, all of which function at the

shmoo site during the mating (Bendezu and Martin, 2013; Dudin et al., 2016)(Fig.4 A and B). In

agreement with this hypothesis, a transient MAPK^{Spk1} and MAPKK^{Byr1} signal on the cell cortex

was observed during the mating process (Fig. 1)(Dudin et al., 2016). Localisation of MAPK at the

growing cell tips was also observed in other fungi including *S. cerevisiae* and *N. crassa* (Chen et

al., 2010; Fleissner et al., 2009; Maeder et al., 2007; van Drogen et al., 2001). In budding yeast,

MAPK^{Fus3} can directly phosphorylates Bni1, a formin that organises actin filaments, to facilitate

shmoo formation (Matheos et al., 2004). It will be important to determine whether this is also

the case in fission yeast.

Interestingly, during the vegetative growth when expression of MAPK^{Spk1} is repressed,

Ras1.G17V is still capable of activating Cdc42 (Fig. 4C and D). Whether other MAPKs, such as

Sty1 or Pmk1, contribute to Cdc42 activation during the vegetative cell cycle will be an

important question to answer. Intriguingly, recent studies show that Sty1 inhibits, rather than

assists, establishment of the Cdc42 polarity module (Mutavchiev et al., 2016). Collectively, it is

likely that the Cdc42 polarity module is regulated in a context dependent manner by multiple

MAPKs in a range of ways.

In this study we revealed the vital contribution of Cdc42 to induce the *ras1.G17V* phenotype in

fission yeast pheromone signalling (Fig. 8B). In mouse models, small GTPases, Cdc42 and Rac,

are required for *H-ras^{G12V}* induced transformation (Malliri et al., 2002; Stengel and Zheng, 2012).

Therefore, oncogenic RAS-induced Cdc42/Rac misregulation may be a common basis of

oncogenicity of mutated-RAS-induced signalling. Specifically targeting this process may

therefore be an effective strategy against oncogenic RAS-driven tumourigenesis.

Materials and methods

Yeast strains and media

Genotypes of the *Schizosaccharomyces pombe* strains used are listed in the supplementary Table S1. Gene disruption and 2xFLAG-GFP-tagging of genes were performed using the direct chromosomal integration method described previously (Bahler et al., 1998; Funaya et al., 2012; Wach, 1996). Fission yeast media (YE, MM-N and SPA) and basic genetic manipulations are described in (Moreno et al., 1991).

Plate mating assay for synchronous mating

In order to induce synchronous mating, we established the "Plate mating assay" system as follows: Cells were grown in YE supplemented with adenine (0.2g/L) until the cell density reaches $8\text{-}10 \times 10^6$ cells/ml. Cells were then washed with MM-N (1% glucose, supplemented with Leucine 40mg/L) using a filtration unit. These cells were resuspended to a cell density of $0.8\text{-}1 \times 10^7$ cells/ml in MM-N. In the timecourse experiments, this moment was considered time 0. 8×10^7 cells were re-filtered onto a PDVF membrane of 47 mm diameter (Millipore DVPP04700) in order to evenly place the cells across the defined area. The filters bearing the cells over their surface were carefully transferred onto sporulation agar plates (SPA+Leucine 40mg /L, 50ml SPA agar / 14cm diameter for 6 membranes), cell side up, and incubated at 30°C. During the time course experiments, at each time-point one membrane, which initially had 8×10^7 cells at time 0, was removed from the SPA plate and placed into 5 ml of ice-cold 20% trichloroacetic acid (TCA) in a 50 ml falcon tube. The tube was shaken vigorously to remove cells from the membrane. The tube was briefly centrifuged and the membrane removed from the tube. The tube was then centrifuged for 1 minute at 2000rpm to pellet cells. Supernatant was discarded, cells were resuspended in 1 ml 20% TCA and transferred to a tube capable of storage at -80˚C. The cells were pelleted again using a bench top centrifuge, supernatant discarded, and the pellet snap frozen in liquid nitrogen. Tubes were stored at -80˚C ready for protein extraction.

Preparation of whole cell extracts

This method is based on that described by Keogh lab Protocols (https://sites.google.com/site/mckeogh2/protocols). All steps were performed on ice unless otherwise stated. Cell pellets were thawed on ice and resuspended in 250 µl 20% TCA. 250 µl of acid washed glass beads (SIGMA) were added and sampled chilled on ice for 5 minutes. Cells were broken in a FastPrep24 cell beater (MP Biomedicals, speed 6.5 x 1 minute x 3 with 1

minute intervals). Cell extracts were collected by piercing the bottom of tubes with a needle and

placing them into collection tubes and centrifuged at 2000 rpm for 1 minute. Beads were

washed with 300 µl of 5% TCA and centrifuged at 2000 rpm for 1 minute, this was repeated

twice. The contents of the collection tube were transferred to a 1.5 ml tube and centrifuged at

14K rpm for 10 minutes at 4°C. The liquid was discarded and the cell pellet washed with 750 µl

of 100% ethanol. Tubes were centrifuged briefly (~1min 14000rpm) again. Ethanol was

completely removed with a pipette and the pellet resuspended in 100 µl 1M Tris pH8.0 and 100

µl 3x protein loading buffer (Laemmli, 1970). Cell extracts were then heated for 5 minutes at

95˚C, centrifuged for 5 minutes at 14K rpm and the supernatant transferred to a fresh 1.5 ml

tube. Samples were stores at -20˚C.

Western Blotting

Protein extracts were subject to SDS-PAGE and were transferred to Immobilon-FL PVDF

membrane (Millipore). Membranes were blocked for a minimum of 1-hour in Odyssey Blocking

Buffer (OBB) (Li-cor) diluted 1:1 in PBS. Primary antibody incubation was carried out overnight

in OBB 1:1 in PBS with the anti phospho-p44/42 MAPK (Erk1/2) (Thr202/Tyr204) rabbit

monoclonal antibody (#4370 Cell Signaling technology. Used at 1:2000 dilution), the monoclonal

anti GFP antibody ((0.4mg/ml), Roche Cat No 11814460001. Used at a 1:2000 dilution) and the

anti α-tubulin antibody, TAT1 (generous gift from Keith Gull, 1:3000). Membranes were washed

3x10 minutes with 20 ml TBST (50 mM Tris, pH 7.4 – 150 mM NaCl – 0.1% Tween 20) whilst

gently shaking followed by secondary antibody incubation (IRDye 680LT goat anti-mouse

antibody, Li-cor 926-32211(1.0 mg/ml), 1:16,000 dilution and IRDye 800CW goat anti-rabbit

secondary antibody Li-cor 926-68020 (1.0 mg/ml), 1:16000 dilution in 0.01% SDS, 0.1% Tween

20 in OBB 1:1 PBS) for 1 hour in the dark to prevent fluorophore bleaching. This was followed by

2x 10 minute TBST washes and a 1x 10 minute TBS (50 mM Tris, pH 7.4 – 150 mM NaCl) wash

before scanning on the Odyssey CLx infrared Imaging System (Li-cor). Protein quantitation using

the Image Studio V2.1 software supplied with the Odyssey CLx scanner. The background method

used was median with a border of 3 pixels to the left and right of quantitation boxes.

Quantitation of MAPK^{Spk1} phosphorylation

To detect the activated MAPK^{Spk1}, whole cell extracts were prepared and Western blotting

analysis was carried out using the anti-phospho ERK antibody (#4370 Cell Signalling Technology)

that recognises the dual phosphorylation at the conserved TEY motif. Specificity of the antibody

against the phosphorylated MAPK^{Spk1} (**pp**MAPK^{Spk1}) in the fission yeast cell extracts was

confirmed before proceeding with further experiments as shown in Supplementary Fig. S1. As

described above in the "**Plate mating assay for synchronous mating**", during the time course

experiments, at each time-point, one membrane, which initially had 8x10^{7}cells at time 0, was

used to prepare the whole cell extracts. Then an equal volume of each sample was loaded to the

Western blotting. In this manner, we observed that the change of the protein level throughout

the mating process per a defined starting material. We noticed that the level of α-tubulin during

the wildtype mating process is relatively constant; less than 25% fluctuation throughout the

timecourse for all three biological replicates (an example shown in Fig. S2B). Based on these

observations, we chose to use α-tubulin as an internal control to quantitate the **pp**MAPK^{Spk1}

signal.

In order to quantitate **pp**MAPK^{Spk1} levels in wildtype, *byr1.DD*, *ras1.G17V* and *scd1Δ* mutants,

Western blotting of three biological replicates of time-course experiments was conducted

(original membranes presented in Fig. S3). Because the SDS-PAGE gels we used had only 25

wells, only two out of three biological replicates could be run simultaneously on the same gel.

The third replicate was run separately on a different gel as shown in Fig. S3 (A). Definite

measurement values of the third replicate were multiplied by a constant to bring the values

closest to the rest of the two replicates. In order to directly compare results of wildtype,

byr1.DD, *ras1.G17V* and *scd1Δ* mutants, technical replicates of Western blotting were generated

by directly comparing one of the biological replicates of each strain as follows: the third

replicate of the wildtype and *byr1.DD* samples (WT-3 and *byr1.DD*-3) (Fig. S3A), the second

replicate of the wildtype and *ras1.G17V* samples (WT-2 and *ras1.G17V* -2) and the second

replicate of the wildtype and *scd1Δ* samples (WT-2 and *scd1Δ* -2) (Fig. 3B).

Cell Imaging for bright field and Spk1-GFP signals

A Nikon Eclipse Ti-E microscope equipped with CoolLED PrecisExcite High Power LED

Fluorescent Excitation System, an Andor iXon EM-DU897 camera and aCFI Plan Apo VC

100x/1.4 objective was used for cell imaging to capture the morphology of cells and the

localisation of the GFP-tagged MAPK^{Spk1} during mating time-courses. For cell images presented

in Figure 4, a 2D array scanning laser confocal microscope (Infinity 3, VisiTech) was used (see

below). Each time point comprises 15-25 serial images with 0.4 µm intervals along the Z axis

taken to span the full thickness of the cell. All of the Spk1-GFP images were deconvolved using

the Huygens Essential Deconvolution software (Scientific Volume Imaging). Deconvolved images

were Z-projected (maximum intensity), cropped and combined using Fiji (Schindelin et al.,

2012).

Imaging and quantitation of CRIB-GFP signal

A 2D array scanning laser confocal microscope (Infinity 3, VisiTech) on a NikonTi-E microscope

stand equipped with a Hamamatsu Flash 4.0V2 sCMOS camera and a Plan Apo 100x/1.45

objective was used to capture CRIB-GFP signal to examine activation status of Cdc42. For images

presented in Fig. 4A, 25 serial Z images with step size of 0.25 μm were taken. Images were

deconvolved using Huygens Essential (Scientific Volume Imaging) and maximum intensity

projections are presented.

For images presented in Fig. 4C, for each image, 30-45 serial images with 0.2 μm interval along

the Z axis were taken to span the full thickness of the cell. Using FIJI software maximum

intensity Z-projections were created and used for quantitation. Intensity of GFP signal on the

cell cortex was measured using FIJI along one of the cell tips that shows stronger GFP signal as

indicated in an example image in Fig. 4D. 40 cells without septum were measured for each

strain. Quantified CRIB-GFP intensity traces were analysed in R (R Core Team http://www.R-

project.org/). First, rolling averages over +/-5 measurement points were calculated. Next, the X-

coordinates of these traces were aligned by their peak intensity. Finally, the average curve from

all aligned traces per strain was calculated, and displayed in Fig 4.D with respective standard

error of the mean curves (dashed lines). Analysis script will be accessible on the GiHub

repository upon publication (see availability section 1.1.16).

Glutathione-S-transferase (GST) tag pull-down assays

Fission yeast cDNA fragments encoding Ras1.G17V (1-172), Byr2 (65-180) and Scd1 (760-872)

were cloned in the pLEICS1 (Ras1.G17V) and pLEICS4 (Byr2 and Scd1) vectors (Protex [Protein

Expression Laboratory], University of Leicester) to produce N-terminally His6-tagged Ras1.G17V

(1-172), N-terminally GST-tagged Byr2 (65-180) and N-terminally GST-tagged Scd1 (760-872).

Constructs were expressed in *E.coli* BL21 Rosetta cells in LB. All bacteria cell lysates were

prepared in phosphate-buffered saline (PBS), pH 7.4.

His6-Ras1.G17V (1-172) was purified using Ni Sepharose 6 Fast Flow (GE Healthcare) and

dialysed into buffer A (20 mM Tris-Cl (pH 7.5), 100 mM NaCl, 5mM MgCl2, 1mM β-

mercaptoethanol). For GTP loading, buffer A of the Ras1.G17V (1-172) preparation was firstly

replaced by Exchange buffer (20 mM Tris-Cl (pH 7.5), 1mM EDTA, 1mM β-mercaptoethanol)

using a filtration unit (Amicon Ultra Centrifugal Filter Unit, 10K cut off, Millipore). GDP-GTP

exchange reaction was carried out by adding GTP and EDTA to a final concentration of 8 mM

and 12 mM respectively and incubating the sample at 37°C for 10 min. The exchange reaction

was terminated by adding MgCl2 to a final concentration of 20.5 mM. The resultant GTP-loaded

Ras1.G17V (1-172) was washed with buffer A using the filtration unit and immediately used for

the GST pull-down assays.

GST-Byr2 (65-180) and GST-Scd1 (760-872) were purified using glutathione sepharose 4B (GE

Healthcare). The proteins bound on the glutathione beads were washed with buffer A and used

for the GST pull-down assays together with the Ras1.G17V (1-172) preparation. For the

competition assays shown in Fig. 7D, Scd1 (760-872) fragment was prepared by cleaving it out

from the N-terminal GST, which was bound to the glutathione beads, using TEV protease.

GST pull-down assays were carried out by incubating Ras1.G17V (1-172) (GDP bound or GTP

bound) and GST-Byr2 (65-180) or GST-Scd1 (760-872) with or without Scd1 (760-872) fragment

at 4 °C for 30 min. Supernatant of the reaction was saved and mixed with the same volume of

the 3x loading buffer (Laemmli, 1970) to generate the "unbound" fraction. The remaining beads

were washed twice, resuspended in buffer A of the original volume and mixed with the same

volume of the 3x loading buffer to generate the "bound" fraction. Protein samples were run on

a SDS-PAGE gel and proteins were visualised by InstantBlue protein stain (Expedeon).

Quantitation of the intensities of Ras1.G17V (1-172) bands in Fig. 7D was carried out using Fiji

software.

Mathematical Modelling

We built a mathematical model in form of a system of ordinary differential equations (ODE) for

the dynamics of the signaling pathway downstream of the pheromone receptor. The model

consists of 6 ordinary differential equations representing 9 chemical reactions connecting 6

variables (1.1.14).

We focused on the competition between the MAPK^{Spk1} and Cdc42 pathways for active Ras1^{GTP}

molecules, but no other pathway "cross-talks" were instigated. We estimated the model

parameters from the measured time courses of **pp**MAPK^{Spk1} in wild type and the three key

mutant strains (*ras1.G17V*, *MAPKK^{byr1.DD}* and *Cdc42-GEF^{scd1}Δ*) examined in this study.

Time courses in these strains are precisely reproduced by the model, thereby we have made it

plausible that the competition between MAPK^{Spk1} and Cdc42 pathways is sufficient to cause the

ppMAPK^{Spk1} early activation phenotype observed in the *ras1.G17V* and *Cdc42-GEF^{scd1}Δ* mutants.

The model also successfully predicted the **pp**MAPK^{Spk1} temporal dynamics in the 21 other

mutant strains examined in this study (Fig.7D). We therefore concluded that the model may

serve as a general framework for pheromone signalling in *S. pombe* and can be used for further

in silico experimental design.

1.1.1   Pathway components

Previous studies showed that more than 20 proteins, more than 20 biochemical and at least 10

relevant genetic interactions are involved in the fission yeast pheromone pathway (Mata and

Bahler, 2006; Mata et al., 2002; Otsubo and Yamamoto, 2012; Xue-Franzen et al., 2006). Given

the complexity of the pathway, and in order to attain the simplest model fulfilling our criteria,

several pathway components and steps were simplified in the presented model as detailed

below.

1.1.2   Nitrogen withdrawal, and subsequent pathway activation

Nitrogen starvation induces the expression of the meiotic transcriptional regulator Ste11, which

then induces expression of the key components of the pheromone pathway (Egel, 2004).

Experimentally, this initial process occurs as a step-like nitrogen removal from the media, which

is implemented as a change of starvation signal *S* from 0 →1, i.e. activator step-function in the

model.

The response to starvation is two fold. First of all, various signaling components under the

regulation of Ste11 are induced: the pheromone (M- or P-factor), the pheromone receptors

(Map3 or Mam2), the receptor-coupled G-protein (Gpa1), a GDP-GTP exchange factor (GEF) for

Ras1 (Ste6) and an adaptor Ste4. For simplicity, the pheromone sensing and upstream signal

transduction machinery is modelled by one variable, called here the Pheromone Sensing (PS)

unit (Fig. 7A). The PS unit is sometimes also referred to as the "upstream pheromone pathway".

Induction of the PS unit by Ste11 as well as pheromone binding, subsequent Gpa1 activation

and consequential activation of Ste4 and Ste6 are all encompassed in the process [L1] in Fig. 7A.

As Ste11 is induced by starvation, PS is also created proportionally to starvation sensing (*S,* Eq.

1). Since downregulation of PS occurs in form of a long negative feedback loop, the term

$v_{downregulation}(PS)$ depends on **pp**MAPK^{Spk1} (Eq. 2); and it is explained in a later section.

Eq. 1

$$\frac{d(PS)}{dt} = S \cdot k_0 - v_{downregulation}(PS)$$

Eq. 2

$$v_{downregulation}(PS) = k_8 \cdot \mathbf{pp}\text{MAPK}^{\text{Spk1}} \cdot PS$$

The second response to starvation is the activation of a basal MAPK$^{\text{Spk1}}$ transcription through Ste11. MAPK$^{\text{Spk1}}$ is then activated by phosphorylation to ppMAPK$^{\text{Spk1}}$, if (active) ppMAPKK$^{\text{Byr1}}$ is present. This basal activation (F1) is also proportional to starvation sensing (Eq. 3), also see (*Eq. 7*) and section (1.1.6) for details.

Eq. 3

$$F_1 = S \cdot k_1 \cdot \mathbf{pp}\text{MAPKK}^{\text{Byr1}} activity$$

1.1.3   The upstream pheromone pathway (PS)

The PS unit activates the downstream MAPK cascade in two ways:

   1. PS activates Ras1$^{\text{GDP}}$ (process [L4] in Fig. 7A), which in turn activates MAPKKK$^{\text{Byr2}}$, and

   2. Ste4, a PS unit component, directly activates MAPKKK$^{\text{Byr2}}$ independently of Ras1 (process [L3] in Fig. 7A).

Both of these steps are necessary to functionally activate MAPKKK$^{\text{Byr2}}$ (Eq. 6).

Finally, the upstream pheromone pathway is downregulated in a negative feedback loop as discussed in a later section (1.1.7).

1.1.4   Ras1

In the *S. pombe* pheromone response, Ras1 is a central component as it both activates the transcriptional response via MAPKKK$^{\text{Byr2}}$, and the morphological response via Cdc42-GEF$^{\text{Scd1}}$. Both molecules form protein complexes that anchor pools of Ras1$^{\text{GTP}}$ (Chang et al., 1994; Tu et

al., 1997; Weston et al., 2013), thus we hypothesised that the two pathway branches might

affect each other by changing the amount of available, unbound Ras1^{GTP}. In other words,

MAPK^{Spk1} and Cdc42 pathways compete with each other for unbound Ras1^{GTP}. As the model

focuses on the **pp**MAPK^{Spk1} levels, but not on Cdc42^{GTP} production / localisation, the Cdc42

branch (the process [L9]) is simply represented as a change in available Ras1^{GTP} for MAPKKK^{Byr2}

in the model. This is further discussed in the section on the *Cdc42-GEF^{scd1}Δ* mutant strain

(1.1.11).

In the wildtype model, Ras1^{GDP} is activated by the PS unit and deactivated by a Ras-GAP. Both

reactions are described by mass action kinetics in (Eq. 4 and Eq. 5). For simplification of

parameters, see section (1.1.8).

Eq. 4

795
$$\frac{d(Ras1^{GTP})}{dt} = k_2 \cdot PS \cdot Ras1^{GDP} - k_2 \cdot Ras1^{GTP}$$

796 *Eq. 5*

797
$$Ras1^{GTP} + Ras1^{GDP} = \text{constant}$$

1.1.5   MAPKKK^{Byr2} and MAPKK^{Byr1}

Following the PS unit and Ras1^{GDP} activation, MAPKKK^{Byr2} is activated by a twofold mechanism

involving Ste4 (a component in the PS unit) and Ras1^{GTP}. Note, that MAPK^{Spk1} is the only

member of the kinase cascade whose transcription is regulated by Ste11 (the process [L2])

(Mata and Bahler, 2006). Therefore, accordingly, the expression levels of MAPKKK^{Byr2} and

MAPKK^{Byr1} were not subject to Ste11 activity in our model. Compared to the 24hrs time scale of

pheromone signaling, the MAPKKK^{Byr2} -> MAPKK^{Byr1} activation likely happens on a much faster

time scale. Therefore, and for simplicity, we grouped MAPKKK^{Byr2} and MAPKK^{Byr1} into one unit

(Fig. 7A). Thus, MAPKK^{Byr1} activation (phosphorylation) (the process [L5]) is given as in (Eq. 6 and

Eq. 7) and both activation and deactivation follows mass action kinetics. For simplification of

parameters, see section (1.1.8).

Eq. 6

$$\frac{d(pp\text{MAPKK}^{\text{Byr1}})}{dt} = (k_4 \cdot \text{MAPKK}^{\text{Byr1}} \cdot Ras1^{GTP} \cdot PS) - k_4 \cdot pp\text{MAPKK}^{\text{Byr1}}$$

813 *Eq. 7*

$$\boldsymbol{pp}\text{MAPKK}^{\text{Byr1}} activity = \boldsymbol{pp}\text{MAPKK}^{\text{Byr1}} \cdot k_6$$

816 *Eq. 8*

$$MAPKK^{\text{Byr1}} + \boldsymbol{pp}MAPKK^{\text{Byr1}} = \text{constant}$$

1.1.6 MAPK$^{\text{Spk1}}$

In the cells, MAPK$^{\text{Spk1}}$ protein expression is induced upon nitrogen removal (the process [L2] in

Fig. 7A). MAPK$^{\text{Spk1}}$ is then phosphorylated and activated to **pp**MAPK$^{\text{Spk1}}$ by **pp**MAPKK$^{\text{Byr1}}$ (the

process [L6]). Experimentally we observed very similar dynamics for MAPK$^{\text{Spk1}}$ and **pp**MAPK$^{\text{Spk1}}$.

Therefore, we assumed that MAPK$^{\text{Spk1}}$ ~ **pp**MAPK$^{\text{Spk1}}$ system is in equilibrium, so creation and

destruction reactions for each state can be disregarded. Thus, for simplicity, MAPK$^{\text{Spk1}}$ is only

present in its phosphorylated form (**pp**MAPK$^{\text{Spk1}}$) in the model.

Despite the simplification, the model represents the three main processes contributing to

ppMAPK$^{\text{Spk1}}$ levels: it is created proportionally to starvation and to MAPKK$^{\text{Byr1}}$ activity (F$_1$, *Eq. 3*);

it is also self-induced (which is again proportional to MAPKK$^{\text{Byr1}}$ activity (F$_6$, *Eq. 7-Eq. 9*); and it is

degraded by mass action kinetics (*Eq. 11*).

1.1.6.1 Positive Feedback

Previous studies have shown that **pp**MAPK$^{\text{Spk1}}$ activates Ste11 (Kjaerulff et al., 2005), which in

turn transcribes more *mapk^{spk1}*. This forms a positive feedback loop (the process [L7]) if

ppMAPKK$^{\text{Byr1}}$ is present to phosphorylate MAPK$^{\text{Spk1}}$. A simplest form of an abstract positive

feedback is given as the self-dependence term **pp**MAPK$^{\text{Spk1}}{}^{k_9}$ in Eq. 9.

Eq. 9

$$F_6 = \boldsymbol{pp}\text{MAPKK}^{\text{Byr1}} activity \cdot S \cdot \boldsymbol{pp}\text{MAPK}^{\text{Spk1}^{k_9}}; k_9 \geq 0$$

Eq. 10

$$v_{creation}\left(\boldsymbol{pp}\text{MAPK}^{\text{Spk1}}\right) = F_1 + F_6$$

F1 is described in (*Eq. 3*).

Finally, MAPK$^{\text{Spk1}}$ is set to be degraded following simple mass action kinetic, thus the final

equation for ppMAPK$^{\text{Spk1}}$ kinetics in wild type yeast is given as (Eq. 11).

Eq. 11

$$\frac{d(\boldsymbol{pp}\text{MAPK}^{\text{Spk1}})}{dt} = v_{creation}\left(\boldsymbol{pp}\text{MAPK}^{\text{Spk1}}\right) - \boldsymbol{pp}\text{MAPK}^{\text{Spk1}} \cdot k_7$$

1.1.7   Down regulation of the pathway by a negative feedback loop

Transient MAPK$^{\text{Spk1}}$ activation in the wildtype cells (Fig.1C) suggests that there is a delayed

negative feedback to downregulate the **pp**MAPK$^{\text{Spk1}}$ in the pathway, which leaves only a certain

time-window for activity. As this downregulation was found abolished in the constitutively

active *MAPKK^{byr1.DD}* mutant (Fig. 1E), the target(s) of the negative feedback must be MAPKK$^{\text{Byr1}}$

or upstream components. Hence, potential negative regulators, such as phosphatases Pyp1 and

Pmp1 that are proposed to directly deactivate ppMAPK$^{\text{Spk1}}$ (Didmon et al., 2002), were excluded

from our model. Meanwhile, the negative regulators Sxa2 (encoding a serine carboxypeptidase

against a mating pheromone P-factor) and Rgs1 (encoding a regulator of Gpa1), both of which

are transcriptionally induced upon pheromone signalling, fit well to the criteria of a negative

feedback component (Imai and Yamamoto, 1992; Mata and Bahler, 2006; Pereira and Jones,

2001; Watson et al., 1999). Receptor internalization is also expected to be a part of the negative

feedback (Hirota et al., 2001) and regulation by antisense RNA for the *mapk^{spk1}* transcript as well

as other signalling components may also play a role (Bitton et al., 2011). As relative

contributions of each remain to be quantified, we represented all these potential negative

feedbacks collectively as a single circuit in our model that inactivates the PS unit (the process

[L8]) (Fig 7A). The chemical equation is therefore given as: $Ras1^{GTP} + ppMAPK^{Spk1} + PS \rightarrow$

$Ras1^{GTP} + ppMAPK^{Spk1}$, which gives rise to the negative term in Eq. 12.

Eq. 12

867
$$\frac{d(PS)}{dt} = S \cdot k_0 - (k_8 \cdot \mathbf{pp}\text{MAPK}^{\text{Spk1}} \cdot PS \cdot Ras1^{GTP})$$

868
1.1.7.1 Ras1^{GTP} contribution to the negative feedback

Transient, peaking ppMAPK^{Spk1} activation in wildtype solely requires a delayed negative

feedback. However, as described in the main text, a more complex regulation is necessary to

describe the both earlier and lower peak in *ras1.G17V* and *cdc42-GEF^{Scd1}Δ* mutants. By

incorporating Ras1^{GTP} in this feedback (the process [L10], see: Eq. 12), we could precisely

recapitulate both phenotypes.

1.1.7.2 The "simple-activator-Ras" model variant

We wanted to show the behaviour of the model if Ras1^{GTP} would only act as an activator. From

the wild type model presented in Fig.7 we removed Ras1^{GTP} from the downregulation resulting

in (Eq. 13).

Eq. 13

881
$$\frac{d(PS)}{dt} = S \cdot k_0 - (k_8 \cdot \mathbf{pp}\text{MAPK}^{\text{Spk1}} \cdot PS)$$

882
We fitted this model variant to the data sets as before, using Hooke–Jeeves (Hooke and Jeeves,

1961) and particle swarm optimisation methods (Kennedy and Eberhart, 1995). The objective

value for the best fit was ~3 higher for this model variant than for the original model. Although

it recapitulated the main features (Fig.S7B), it could not describe the observed "earlier and

lower" signalling phenotype observed in the *ras1.G17V* and *cdc42-GEF^{Scd1}Δ* strains. Finally, we

also show that the addition of Ras1^{GTP} to this model only leads to increased amplitude, not to

earlier timing (Fig.S7C).

1.1.8   Model simplification

After extensive parameter estimations, we found that the model can be simplified in the number of individual parameters for forward and reverse reaction of the same species without compromising the quality of fit. For the Ras1^{GDP} $\leftrightarrow$ Ras1^{GTP} and MAPKK^{Byr1} $\leftrightarrow$ ppMAPKK^{Byr1} reactions we could set the forward and reverse parameters to the same value, and achieve virtually identical quality fits, while reducing the number of free dimensions in the parameter space by two. With this simplification the remaining model parameters became uniquely identifiable, with the exception of k1 (Fig.S6). We also fitted the models with these as free parameters and achieved very similar fit qualities, but most parameters became unidentifiable, therefore, we decided for the simpler model.

Mutant strains

1.1.9   MAPKK$^{byr1.DD}$

MAPKK$^{Byr1.DD}$ harbors two phosphomimetic point mutations, which keep MAPKK$^{Byr1.DD}$ active even in the absence of its activator MAPKKK^{Byr2} (Fig. 3). Therefore, this mutation effectively uncouples MAPK^{Spk1} from the upstream part of the pathway, as represented in Fig. 7A, *MAPK$^{byr1.DD}$* panel. In this mutant, MAPK^{Spk1} (its substrate) also becomes constitutively phosphorylated and activated (Fig. 1E).

It is known that the phosphomimetic substitution of the amino acids often does not fully "mimic" the phosphorylated status and often fails to bring a full activation of the modified kinase. This is likely happening to the MAPKK$^{Byr1.DD}$ mutant molecule: the initial production of **pp**MAPK^{Spk1} upon nitrogen starvation was much slower in the *MAPKK$^{byr1.DD}$* mutant than in wildtype (Fig. 1E). This effect is represented by the f_{Byr1DD} <1 fitted parameter in the MAPK$^{Byr1.DD}$ model variant (see: Eq. 14).

Eq. 14

$$\pmb{pp}\text{MAPKK}^{Byr1} activity = \pmb{pp}\text{MAPKK}^{Byr1} \cdot k_6 \cdot f_{Byr1DD}$$

As MAPK^{Byr1} is not induced upon starvation (Nadin-Davis and Nasim, 1990), in the mutant strain,

we could implement the mutation by setting initial concentrations $[Byr1]_0 = 0$ and

$[Byr1^{PP}]_0 = 1$; and setting the respective activation and inactivation reactions to zero.

1.1.10 ras1.G17V

The *ras1.G17V* strain contains a point mutation, equivalent to human Ras G12V oncogenic

mutation, which impairs the GTPase activity of the molecule (Trahey and McCormick, 1987).

This results in being most of the molecules to stay in the Ras1^{GTP} form.

In the model, the following changes are implemented to represent the mutation: The initial

concentration of $[Ras1^{GTP}]_0$ is set to 1, while that of $[Ras1^{GDP}]_0$ is set to 0, which is the

opposite of the wildtype initial state. Also, the deactivation and activation reactions are set to

zero.

1.1.11 Cdc42-GEF^{scd1}Δ

Ras1^{GTP} is proposed to interact with and activate Cdc42-GEF^{Scd1}, which then activates Cdc42 by

acting as a GDP-GTP exchange factor (GEF) (Chang et al., 1994). Because Cdc42-GEF^{Scd1} binds

Ras1, the loss of it leads to an increased pool of unbound Ras1^{GTP}. In our model this mutation is

implemented as additional, unbound Ras1^{GTP} added to the wildtype system. In this setting the

amount of Ras1^{GTP} available for MAPKKK^{Byr2} determines the **pp**MAPK^{Spk1} dynamics. Since it is

unknown, how much Ras1^{GTP} is bound by Cdc42-GEF^{Scd1}, we fit the $[Ras1^{GTP}]_0$ as a free

parameter in the otherwise intact, wild type model.

1.1.12 Implementation and availability

The **pp**MAPK^{Spk1} temporal dynamics in the four strains, wildtype, *MAPKK$^{byr1.DD}$*, *ras1.G17V* and

cdc42-GEF^{Scd1}Δ, were described by 6 ODEs and 8 parameters shared across all species (List of

Differential Equations, Supplementary Table S2). *MAPK$^{byr1.DD}$* has an additional parameter,

f$_{Byr1DD}$, while $[Ras1^{GTP}]_0$ is fitted the *Cdc42-GEF^{scd1}Δ* strain as described above. The model

represents relative concentrations of proteins on an absolute time scale. Initial concentrations

of components are therefore either set to 1, if the component is present prior to starvation, or

0, if the component is not present, and it is induced or activated during starvation or

pheromone response. To show that the model is at steady state before nitrogen removal, it was

simulated for 100 hours prior to starvation in every case. All variables remained constant during

this time. All other plots start from T=t-100 as origin, when nitrogen is removed.

Model simulation and parameter estimation (model fitting) was performed in COPASI 4.20

(Hoops et al., 2006). Visualisation and data analysis was done in python v2.7 and R v3.2. Plotting

was performed by base R graphics and by the MarkdownReports v2.9.5 (Vertesy, 2017),

pheatmap (Kolde, 2013) and plotly v4.7.1 (Sievert et al., 2017) packages.

1.1.13 Parameter Estimation

Parameter estimation consisted in fitting of 8 rate constants (parameters) and one additional

parameter per mutant strain. We used the gradient-free Hooke–Jeeves (Hooke and Jeeves,

1961) and particle swarm optimisation methods (Kennedy and Eberhart, 1995) implemented in

COPASI.

We found that the algorithm converges better to the optimal solution, if key time points in the

dataset are counted with different weights for optimisation. Therefore, data points 102 (early

activation), 108 and 109 (peak) were passed on with triple weight to the optimisation function.

1.1.13.1   Parameter identifiability, multiplex parameter estimation and ensemble

modelling

To investigate parameter identifiability, we performed multiplexed parameter estimation by

5000 parallelised particle swarm optimisation. In each of the estimation rounds, the model was

fitted to the data, starting from randomised parameters. Parameters were sampled uniformly

+/- 4 orders of magnitudes around the previously achieved best fit, except the exponent (N).

This is the exponent of the positive feedback loop, is therefore an 'explosive' parameter, and

there is no reason to assume a stronger dependence than 4-th order (x^4) for **pp**MAPK^{Spk1} in the

positive feedback. The range for this parameter was therefore set to [1e-5, 4].

We repeated the estimations with +/- 5 magnitudes (5000 times), but we achieved no better fit,

while the convergence of optimisation dramatically decreased (i.e. >90% of the optimisations

did not get close to the optimal fit).

We found that with increasing fit quality (lower objective value) all parameters except k_1

converge to a single value, or a very limited range (Fig.S6D, top row, objective value <5).

In Fig.S7A, we further show the convergence on linear scale for an extended number of

simulations (objective value <8). The convergence of parameters is even more pronounced. In

suboptimal fits (O.V. >>3.6) $[Ras1^{GTP}]_0$ in the *scd1Δ* strain frequently hits the upper boundary,

which marks a 10-fold increase in available Ras1^{GTP}. Although the boundary is arbitrary, it is

unreasonable to think that there will be a bigger increase to the available Ras1^{GTP} pool by the

knockout of *scd1*.

Multiplexed parameter estimation for the simple-Ras model performed in the same manner as

for the wildtype, 1000 fits with particle swarm optimisation from randomly sampled starting

points from a parameter space +/- 4 magnitudes around the best previous fit.

1.1.13.2   Ensemble modelling

To show the reliability of the model dynamics in spite of the un-identifiability of certain

parameters, we applied ensemble modelling (Brannmark et al., 2010). In this approach, we

analysed the predicted time courses of the 100 best fitting models to show that regardless of

the residual parameter uncertainty, the simulated variables' dynamics are robustly predicted

(Fig. S8). To show the variation of the individual simulation, ten thousand randomly sampled

simulation points are displayed behind the running average.

1.1.14 List of Differential Equations

As introduced above, here listed and separately defined for all species. Equations 4b and 6b are

only listed here, and provided for completeness: they are simply the reverse reactions for 4 and

6 respectively, thus not discussed in the section above.

1001

1002   *Eq. 1*

1003
$$\frac{d(PS)}{dt} = S \cdot k_0 - v_{downregulation}(PS)$$

1004   *Eq. 4*

1005
$$\frac{d(Ras1^{GTP})}{dt} = k_2 \cdot PS \cdot Ras1^{GDP} - k_2 \cdot Ras1^{GTP}$$

1006 *Eq. 4b*

1007
$$\frac{d(Ras1^{GDP})}{dt} = k_2 \cdot Ras1^{GTP} - k_2 \cdot PS \cdot Ras1^{GDP}$$

1008 *Eq. 6*

1009
$$\frac{d(ppMAPKK^{Byr1})}{dt} = (k_4 \cdot MAPKK^{Byr1} \cdot Ras1^{GTP} \cdot PS) - k_4 \cdot ppMAPKK^{Byr1}$$

1010 *Eq. 6b*

1011
$$\frac{d(MAPKK^{Byr1})}{dt} = k_4 \cdot ppMAPKK^{Byr1} - (k_4 \cdot MAPKK^{Byr1} \cdot Ras1^{GTP} \cdot PS)$$

1012 *Eq. 11*

1013
$$\frac{d(\mathbf{pp}MAPK^{Spk1})}{dt} = v_{creation}(\mathbf{pp}MAPK^{Spk1}) - \mathbf{pp}MAPK^{Spk1} \cdot k_7$$

1014

1015 1.1.15 List of Algebraic Equations

1016 (All introduced above)

1017

1018 *Eq. 7*

1019
$$\boldsymbol{pp}MAPKK^{Byr1}activity = \boldsymbol{pp}MAPKK^{Byr1} \cdot k_6$$

1020 *Eq. 3*

1021
$$F_1 = S \cdot k_1 \cdot \boldsymbol{pp}MAPKK^{Byr1}activity$$

1022 *Eq. 9*

1023
$$F_6 = \boldsymbol{pp}MAPKK^{Byr1}activity \cdot S \cdot \mathbf{pp}MAPK^{Spk1^{k_9}}; k_9 \geq 0$$

1024 *Eq. 10*

1025
$$\boldsymbol{v_{creation}}(\boldsymbol{ppMAPK^{Spk1}}) = \boldsymbol{F_1} + \boldsymbol{F_6}$$

1026 *Eq. 2*

1027
$$v_{downregulation}(PS) = k_8 \cdot \mathbf{pp}MAPK^{Spk1} \cdot PS$$

1028 *Eq. 5*

1029
$$Ras1^{GTP} + Ras1^{GDP} = 1$$

1030

1031 *Eq. 8*

1032
$$MAPKK^{\text{Byr1}} + \boldsymbol{pp}MAPKK^{\text{Byr1}} = 1$$

1033

1.1.16 Availability

Upon acceptance, the source code for analysis is available "as-is" under GNU GPLv3 at

https://github.com/vertesy/Competition.Model.of.Ras.in.Pombe.Pheromone.Response. The

model file will be provided at https://www.ebi.ac.uk/biomodels-main/ in SBML "Level 3: Version

1" format exported from COPASI. The recommended COPASI format model file will be available

at the GitHub repository.

1040

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1050

1051 **Author Contributions**

1052 E.J.K., S.R. and K.T. generated yeast strains. E.J.K., G.S. and K.T. monitored activation status of

1053 MAPK$^{\text{Spk1}}$ and Cdc42. A.V. and E.K. conducted mathematical modelling. E.J.K., K.S. and K.T.

1054 conducted image analysis. M.T., R.G., C.P. and C.D. conducted biochemical analysis of Ras1, Byr2

1055 and Scd1. E.J.K., A.V., E.K and K.T. designed the experiments and interpreted the data.

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1057 **Declaration of Interests**

1058	The authors declare no competing interests.

1059

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Figure legends

Figure 1. Distinct modes of MAPK^{Spk1} temporal phosphorylation profile and morphological changes during sexual differentiation in wildtype, *MAPKK$^{byr1.DD}$* and *ras1.G17V* mutants.

(A) A pictorial representation of wildtype fission yeast sexual differentiation. (B) A list of key signalling components of the fission yeast pheromone signalling pathway. The diagram reflects the prediction that Gpa1 and Ras1 separately contribute to activation of MAPKKK^{Byr2} activation although the precise mechanism is unknown (Xu et al., 1994). At the same time, Ras1 activation is expected to be at least partly under influence of active Gpa1 because the *ste6* gene, encoding a Ras1 activator, is strongly induced upon successful pheromone signaling (Hughes et al., 1994). (C)-(H) Cells were induced for sexual differentiation by the plate mating assay system as described in the materials and methods. (C), (E) and (G) Quantified **pp**MAPK^{Spk1} signal from western blots of wildtype (KT3082) (C), *MAPKK$^{byr1.DD}$* (KT3435) (E) and *ras1.G17V* (KT3084) (G) cells. Three biological replicates were used for quantitation (error bars are ±SEM). α-tubulin was used as a loading control and quantitation was carried out using the Image Studio ver2.1 software (Licor Odyssey CLx Scanner). For the wildtype samples in (C), the % of cells mating is also indicated (n=400, three biological replicates). The wildtype **pp**MAPK^{Spk1} result (C) is also presented in (E) and (G) as a reference. (D), (F) and (H) Cellular morphology (brightfield) and localization of MAPK^{Spk1}-GFP over a 24 hour time-course in wildtype (D), *MAPKK$^{byr1.DD}$* (F) and *ras1.G17V* (H) cells. Time after induction of mating in hours is indicated on the left. At each time point, a bright-field image and a GFP signal image were taken and processed as described in materials and methods. Green asterisks in the time 24 h in the *ras1.G17V* cell image (H) indicate auto-fluorescence signal from inviable cell debris, which were produced through cytokinesis failure or cell lysis. Yellow arrows in panels (D) and (F) indicate transient accumulation of MAPK^{Spk1}-GFP at the shmoo tips. Scale bars represent 10μm.

Figure 2. In the *ras1.G17V MAPKK$^{byr1.DD}$* double mutant, the MAPK^{Spk1} phosphorylation profile follows *MAPKK$^{byr1.DD}$* single mutant phenotype whilst cell morphology mimics the *ras1.G17V* single mutant phenotype.

(A) MAPK^{Spk1} phosphorylation status in the *ras1.G17V MAPKK$^{byr1.DD}$* double mutant cells (KT3439). Cells were induced for mating by the plate mating assay system as described in the materials and methods. Quantitated **pp**MAPK^{Spk1} signal (arbitrary unit) from western blots is

presented. Results of two biological replicates (each derived from three technical replicates,

error bars are ±SEM) are presented in red. (B) The terminal mating phenotype of *ras1.G17V*

MAPKK^byr1.DD double mutant is a phenocopy of *ras1.G17V* single mutant which shows the

"elongated" morphology. Images were taken of *ras1.G17V MAPKK^byr1.DD* double mutant

(KT3439) in the same way as in Fig. 1. Time after induction of mating in hours is indicated on the

left. (C) There is no morphological change in the absence of MAPK^Spk1 signalling. Cell images of

MAPKK^byr1Δ (KT4700) and *ras1.G17V MAPKK^byr1Δ* (KT5030) strains are shown. Images were

taken in the same way as in Fig. 1. Time after induction of mating in hours is indicated on the

left of each series. Scale bars represent 10μm.

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Figure 3. Ras1 activates both MAPK^Spk1 and Cdc42 pathways during pheromone signalling.

(A) *scd1Δ* morphology and MAPK^Spk1-GFP signal. Images of WT (KT3082), *scd1Δ* (KT4061) and

scd1Δ ras1.G17V double mutant (KT4056) were taken in the same way as in Fig.1. Numbers on

the left represents hours after induction of mating. (B) MAPK^Spk1 phosphorylation state in *scd1Δ*

(KT4061) cells after mating induction. Results of three biological replicates (error bars are ±SEM)

are presented. The wildtype **pp**MAPK^Spk1 result presented in Fig.1 (C) is also shown in blue as a

reference. (C) Cell images of *scd1Δ MAPKK^byr1.DD* double mutant (KT4047) were taken in the

same way as in Fig.1. Numbers on the left represents hours after induction of mating. (D)

MAPK^Spk1 phosphorylation state in *ras1Δ* (KT4323), *MAPKK^byr1.DD* (KT3435) and *ras1Δ*

MAPKK^byr1.DD (KT4359) cell extracts. Original Western blotting data is presented in Fig. S4A. (E)

MAPK^Spk1 phosphorylation state in *mapkkk^byr2Δ* (KT3763), *MAPKK^byr1.DD* (KT3435) and

mapkkk^byr2Δ MAPKK^byr1.DD (KT4010) cell extracts. Original Western blotting data is presented in

Fig. S4B. For (D) and (E), quantification was carried out using the Image Studio ver2.1 (Li-cor). (F)

Cell images of the strains mentioned in (D) and (E) were taken in the same way as in Fig.1.

Numbers on the left represents hours after induction of mating. For all the images presented in

(A), (C) and (F), scale bars represent 10μm.

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Figure 4. Ras1.G17V induces cortical Cdc42^GTP accumulation

(A) Cell morphology and localisation of Cdc42^GTP, indicated by CRIB-GFP signal, during the sexual

differentiation process. Wildtype (KT5077) and *ras1.G17V* (KT5082) mutant cells were induced

for mating/sexual differentiation by the plate mating assay condition (Materials and Methods)

and live cell images were taken at the indicated time after induction of mating/sexual

differentiation. Representative CRIB-GFP signal images are presented. Cells with cortical CRIB-

GFP foci are indicated by orange stars. Rapidly-disappearing CRIB-GFP signals at the fusion site

of wildtype mating cells are indicated by green arrows at time 8.5h image. Scale bar: 10 μm. (B)

Quantitation of the results presented in (A). At each time point (4.5h, 6.5h, 10.5h, 12.5h and

22.5h after induction of mating/sexual differentiation), 150 cells were examined whether they

have cortical CRIB-GFP foci. % cells with cortical CRIB-GFP foci is presented. The experiment was

repeated for three times and the mean values and SDs are plotted in the graph. (C) Cell

morphology and localisation of Cdc42^{GTP}, indicated by CRIB-GFP signal, during vegetative

growth. Representative CRIB-GFP signal images of cells of wildtype (KT5077), *ras1Δ* (5107),

ras1.G17V (KT5082), *rga4Δ* (5551) and *rga4Δ ras1.G17V* (KT5554) are presented. Scale bar: 10

μm. (D) Quantitated CRIB-GFP signals on the cell cortex of cells presented in (C). Intensity of GFP

signal on the cell cortex was measured along one of the cell tips as indicated as a magenta

dotted line in the example image on the right (Scale bar: 10 μm) as stated in the Materials and

Methods. 40 cells without septum were measured for each strain and the average curve from all

aligned traces per strain was calculated, and displayed with respective standard error of the

mean curves (dashed lines) as described in Materials and Methods.

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Fig. 5. Distinct contributions of Ste4 and Ste6 to MAPK^{Spk1} phosphorylation.

(A) Ste4 is essential for MAPK^{Spk1} activation. MAPK^{Spk1} phosphorylation status in *ste4Δ* (KT4376),

ste4Δ ras1.G17V (KT5143) and *ste4Δ MAPKK$^{byr1.DD}$* (KT5136) at times-points 0, 8 ,16 and 24

hours post mating induction are presented. Original Western blotting membranes are presented

in Fig. S4C. (B) Incapability of *ste4Δ* to cause pheromone-induced morphological change is

suppressed by *MAPKK$^{byr1.DD}$* but not by *ras1.G17V*. Cell images of *ste4Δ* (KT4376), *ste4Δ*

ras1.G17V (KT5143) and *ste4Δ MAPKK$^{byr1.DD}$* (KT5136) strains were taken 24 hours after

induction of mating. Scale bar: 10 μm. (C) Lack of Ste6 does not result in the complete loss of

MAPK^{Spk1} phosphorylation. MAPK^{Spk1} phosphorylation status in *ste6Δ* (KT4333), *ste6Δ ras1.G17V*

(KT4998) and *ste6Δ MAPKK$^{byr1.DD}$* (KT5139) at times-points 0, 8 ,16 and 24 hours post mating

induction are presented. Original Western blotting membranes are presented in Fig. S4D. (D)

Incapability of *ste6Δ* to cause pheromone-induced morphological change is suppressed by

ras1.G17V mutation but not by *MAPKK$^{byr1.DD}$* mutation. Cell images of *ste6Δ* (KT4333), *ste6Δ*

ras1.G17V (KT4998) and *ste6Δ MAPKK^byr1.DD* (KT5139) strains were taken 24 hours after

induction of mating. Scale bar: 10 μm.

1388

Fig. 6. Gpa1 transduces the pheromone signalling by activating MAPK^Spk1 and Ras1 pathways

(A) MAPK^Spk1 phosphorylation status in homothallic *gpa1Δ* (KT4335), *gpa1Δ ras1.G17V*

(KT5023), *gpa1Δ MAPKK^byr1.DD* (KT4353) and *gpa1Δ ras1.val17 MAPKK^byr1.DD* (KT5035) at times-

points 0, 8 ,12, 16 and 24 hours after mating induction. Original Western membrane is

presented in Fig. S5A. (B) Cell images of the above mentioned strains at 16 hours after mating

induction. All the cell images were taken and processed as in Figure 1. Scale bar is 10 μm. (C)

MAPK^Spk1 phosphorylation status in *h⁻* WT (KT4190), *h⁻ gpa1.QL* (KT5059), *h⁻ ras1.G17V* (KT4233),

h⁻ gpa1.QL ras1Δ (KT5070) and h⁻ *MAPKK^byr1.DD* (KT4194) at times-points 0, 8 ,12 and 24 after

mating induction. Note that while the activation induced in the *gpa1.QL* mutant was down-

regulated, *MAPKK^byr1.DD* induced a constitutive activation. Original Western membrane is

presented in Fig. S5B. (D) Cell images of the above strains at 12 h after induction of mating. All

the cell images were taken and processed as in Figure 1. Scale bar is 10 μm.

1401

Fig. 7. Mathematical modelling of the fission yeast pheromone pathway dynamics.

(A) Components and frameworks of the mathematical model in wildtype and signalling mutants:

ras1.G17V, *Cdc42GEF^scd1Δ,* and *MAPKK^byr1.DD*. Changes corresponding to each mutant are

indicated as follows: Grey: removed components or interactions, orange: increased level of

activity. For the exact implementation of the mutants, see Materials and Method. The

measured component, **pp**MAPK^Spk1, is highlighted in green. (B) Measured and simulated

ppMAPK^Spk1 activation profiles in wildtype, *ras1.G17V*, *Cdc42GEF^scd1Δ* and *MAPKK^byr1.DD* mutants.

Dashed lines: model simulations. Diamonds: experimental data presented in Fig. 1C, E, G, and

Fig. 3B; error bars: SEM. (C) GTP-loaded Ras1.G17V (1-172) directly binds to Byr2 (65-180) and

Scd1 (760-872). *In vitro* GST pull-down assays of bacterially expressed Ras1.G17V (1-172), GST-

Byr2 (65-180) and GST-Scd1 (760-872) were conducted as described in materials and methods.

GTP-loaded Ras1.G17V (1-172) was found to bind to both GST-Byr2 (65-180) and GST-Scd1 (760-

872). (D) Two Ras1 effectors, Byr2 and Scd1, compete for GTP-loaded Ras1.G17V (1-172). In

vitro GST pull-down assays of bacterially expressed Ras1.G17V (1-172) and GST-Byr2 (65-180)

were conducted as in (A). Addition of Scd1 (760-872) fragment interfered with Ras1-Byr2

binding (the 4th lane). Quantitated signal intensities of the Ras1.G17V (1-172) band in the gel are

shown in the right panel. (E) Simulated ppMAPK^{Spk1} dynamics in the wildtype model at

increasing concentrations of Ras1^{GTP} added *in silico* to the system. Increased Ras1^{GTP}

concentration causes advanced and reduced **pp**MAPK^{Spk1} peak intensities. (F) The model fitted

to the 4 strains (as above, in red) correctly predicts ppMAPK^{Spk1} dynamics in the additional 21

signalling mutant strains (in light and dark green) measured in this study.

Fig. 8. Schematic diagram of the fission yeast pheromone signalling pathway

(A) Wildtype fission yeast pheromone signalling pathway, highlighting the branched pheromone

sensing, and that both branches are necessary for mating. (B) Because of the robust regulatory

mechanism implemented for the MAPK pathway and the competition between the effectors,

the constitutively active Ras1.G17V mutation yields a biased overactivation of Cdc42.

Figure 1. Distinct modes of MAPK^{Spk1} temporal phosphorylation profile and morphological changes during sexual differentiation in wildtype, *MAPKK$^{byr1.DD}$* and *ras1.G17V* mutants.

(A) A pictorial representation of wildtype fission yeast sexual differentiation. (B) A list of key signalling components of the fission yeast pheromone signalling pathway. The diagram reflects the prediction that Gpa1 and Ras1 separately contribute to activation of MAPKKK^{Byr2} activation although the precise mechanism is unknown (Xu et al., 1994). At the same time, Ras1 activation is expected to be at least partly under influence of active Gpa1 because the ste6 gene, encoding a Ras1 activator, is strongly induced upon successful pheromone signaling (Hughes et al., 1994). (C)-(H) Cells were induced for sexual differentiation by the plate mating assay system as described in the materials and methods. (C), (E) and (G) Quantified ppMAPK^{Spk1} signal from western blots of wildtype (KT3082) (C), *MAPKK$^{byr1.DD}$* (KT3435) (E) and *ras1.G17V* (KT3084) (G) cells. Three biological replicates were used for quantitation (error bars are ±SEM). α-tubulin was used as a loading control and quantitation was carried out using the Image Studio ver2.1 software (Licor Odyssey CLx Scanner). For the wildtype samples in (C), the % of cells mating is also indicated (n=400, three biological replicates). The wildtype ppMAPK^{Spk1} result (C) is also presented in (E) and (G) as a reference. (D), (F) and (H) Cellular morphology (brightfield) and localization of MAPK^{Spk1}-GFP over a 24 hour time-course in wildtype (D), *MAPKK$^{byr1.DD}$* (F) and *ras1.G17V* (H) cells. Time after induction of mating in hours is indicated on the left. At each time point, a bright-field image and a GFP signal image were taken and processed as described in materials and methods. Green asterisks in the time 24 h in the ras1.G17V cell image (H) indicate auto-fluorescence signal from inviable cell debris, which were produced through cytokinesis failure or cell lysis. Yellow arrows in panels (D) and (F) indicate transient accumulation of MAPK^{Spk1}-GFP at the shmoo tips. Scale bars represent 10μm.

Figure 2. In the *ras1.G17V MAPKK^byr1.DD* double mutant, the MAPK^Spk1 phosphorylation profile follows *MAPKK^byr1.DD* single mutant phenotype whilst cell morphology mimics the *ras1.G17V* single mutant phenotype.

(A) MAPK^Spk1 phosphorylation status in the *ras1.G17V MAPKK^byr1.DD* double mutant cells (KT3439). Cells were induced for mating by the plate mating assay system as described in the materials and methods. Quantitated **pp**MAPK^Spk1 signal (arbitrary unit) from western blots is presented. Results of two biological replicates (each derived from three technical replicates, error bars are ±SEM) are presented in red. (B) The terminal mating phenotype of *ras1.G17V MAPKK^byr1.DD* double mutant is a phenocopy of *ras1.G17V* single mutant which shows the "elongated" morphology. Images were taken of *ras1.G17V MAPKK^byr1.DD* double mutant (KT3439) in the same way as in Fig. 1. Time after induction of mating in hours is indicated on the left. (C) There is no morphological change in the absence of MAPK^Spk1 signalling. Cell images of *MAPKK^byr1Δ* (KT4700) and *ras1.G17V MAPKK^byr1.DD* (KT5030) strains are shown. Images were taken in the same way as in Fig. 1. Time after induction of mating in hours is indicated on the left of each series. Scale bars represent 10μm.

Figure 3. Ras1 activates both MAPK^{Spk1} and Cdc42 pathways during pheromone signalling.
(A) *scd1Δ* morphology and MAPK^{Spk1}-GFP signal. Images of WT (KT3082), *scd1Δ* (KT4061) and *scd1Δ ras1.G17V* double mutant (KT4056) were taken in the same way as in Fig.1. Numbers on the left represents hours after induction of mating. (B) MAPK^{Spk1} phosphorylation state in *scd1Δ* (KT4061) cells after mating induction. Results of three biological replicates (error bars are ±SEM) are presented. The wildtype result presented in Fig.1 (C) is also shown in blue as a reference. (C) Cell images of *scd1Δ MAPKK$^{byr1.DD}$* double mutant (KT4047) were taken in the same way as in Fig.1. Numbers on the left represents hours after induction of mating. (D) MAPK^{Spk1} phosphorylation state in *ras1Δ* (KT4323), *MAPKK$^{byr1.DD}$* (KT3435) and *scd1Δ MAPKK$^{byr1.DD}$* (KT4359) cell extracts. Original Western blotting data is presented in Fig. S3A. (E) MAPK^{Spk1} phosphorylation state in *mapkkk$^{byr2}Δ$* (KT3763), *MAPKK$^{byr1.DD}$* (KT3435) and *mapkkk$^{byr2}Δ MAPKK$^{byr1.DD}$* (KT4010) cell extracts. Original Western blotting data is presented in Fig. S3B. For (D) and (E), quantification was carried out using the Image Studio ver2.1 (Li-cor). (F) Cell images of the strains mentioned in (D) and (E) were taken in the same way as in Fig.1. Numbers on the left represents hours after induction of mating. For all the images presented in (A), (C) and (F), scale bars represent 10μm.

Figure 4. Ras1.G17V induces cortical Cdc42^GTP accumulation

(A) Cell morphology and localisation of Cdc42^{GTP}, indicated by CRIB-GFP signal, during the sexual differentiation process. Wildtype (KT5077) and *ras1.G17V* (KT5082) mutant cells were induced for sexual differentiation by the plate mating assay condition (Materials and Methods) and live cell images were taken at the indicated time after induction of mating/sexual differentiation. Representative CRIB-GFP signal images are presented. Cells with cortical CRIB-GFP foci are indicated by orange stars. Rapidly-disappearing CRIB-GFP signals at the fusion site of wildtype mating cells are indicated by green arrows at time 8.5h image. Scale bar: 10 µm. (B) Quantitation of the results presented in (A). At each time point (4.5h, 6.5h, 10.5h, 12.5h and 22.5h after induction of mating/sexual differentiation), 150 cells were examined whether they have cortical CRIB-GFP foci. % cells with cortical CRIB-GFP foci is presented. The experiment was repeated for three times and the mean values and SDs are plotted in the graph. (C) Cell morphology and localisation of Cdc42^{GTP}, indicated by CRIB-GFP signal, during vegetative growth. Representative CRIB-GFP signal images of cells of wildtype (KT5077), *ras1Δ* (5107), *ras1.G17V* (KT5082), *rga4Δ* (5551) and *rga4Δ ras1.G17V* (KT5554) are presented. Scale bar: 10 µm. (D) Quantitated CRIB-GFP signals on the cell cortex of cells presented in (C). Intensity of GFP signal on the cell cortex was measured along one of the cell tips as indicated as a magenta dotted line in the example image on the right (Scale bar: 10 µm) as stated in the Materials and Methods. 40 cells without septum were measured for each strain and the average curve from all aligned traces per strain was calculated, and displayed with respective standard error of the mean curves (dashed lines) as described in Materials and Methods.

Fig. 5. Distinct contributions of Ste4 and Ste6 to MAPK^Spk1 phosphorylation.
(A) Ste4 is essential for MAPK^Spk1 activation. MAPK^Spk1 phosphorylation status in *ste4Δ* (KT4376), *ste4Δ ras1.G17V* (KT5143) and *ste4Δ MAPKK^byr1.DD* (KT5136) at times-points 0, 8 ,16 and 24 hours post mating induction are presented. Original Western blotting membranes are presented in Fig. S3C. (B) Incapability of *ste4Δ* to cause pheromone-induced morphological change is suppressed by *MAPKK^byr1.DD* but not by *ras1.G17V*. Cell images of *ste4Δ* (KT4376), *ste4Δ ras1.G17V* (KT5143) and *ste4Δ MAPKK^byr1.DD* (KT5136) strains were taken 24 hours after induction of mating. Scale bar: 10 μm. (C) Lack of Ste6 does not result in the complete loss of MAPK^Spk1 phosphorylation. MAPK^Spk1 phosphorylation status in *ste6Δ* (KT4333), *ste6Δ ras1.G17V* (KT4998) and *ste6Δ MAPKK^byr1.DD* (KT5139) at times-points 0, 8 ,16 and 24 hours post mating induction are presented. Original Western blotting membranes are presented in Fig. S3D. (D) Incapability of *ste6Δ* to cause pheromone-induced morphological change is suppressed by *ras1.G17V* mutation but not by *MAPKK^byr1.DD* mutation. Cell images of *ste6Δ* (KT4333), *ste6Δ ras1.G17V* (KT4998) and *ste6Δ MAPKK^byr1.DD* (KT5139) strains were taken 24 hours after induction of mating. Scale bar: 10 μm.

Fig. 6. Gpa1 transduces the pheromone signalling by activating MAPK^{Spk1} and Ras1 pathways.
(A) MAPK^{Spk1} phosphorylation status in homothallic *gpa1Δ* (KT4335), *gpa1Δ ras1.G17V* (KT5023), *gpa1Δ MAPKK$^{byr1.DD}$* (KT4353) and *gpa1Δ ras1.val17 MAPKK$^{byr1.DD}$* (KT5035) at times-points 0, 8 ,12, 16 and 24 hours after mating induction. Original Western membrane is presented in Fig. S4A. (B) Cell images of the above mentioned strains at 16 hours after mating induction. All the cell images were taken and processed as in Figure 1. Scale bar is 10 μm. (C) MAPK^{Spk1} phosphorylation status in *h⁻* WT (KT4190), *h⁻ gpa1.QL* (KT5059), *h⁻ ras1.G17V* (KT4233), *h⁻ gpa1.QL ras1Δ* (KT5070) and *h⁻ MAPKK$^{byr1.DD}$* (KT4194) at times-points 0, 8 ,12 and 24 after mating induction. Note that while the activation induced in the gpa1.QL mutant was down-regulated, *MAPKK$^{byr1.DD}$* induced a constitutive activation. Original Western membrane is presented in Fig. S4B. (D) Cell images of the above strains at 12 h after induction of mating. All the cell images were taken and processed as in Figure 1. Scale bar is 10 μm.

Fig. 7. Mathematical modelling of the fission yeast pheromone pathway dynamics.
(A) Components and frameworks of the mathematical model in wildtype and signalling mutants: *ras1.G17V, Cdc42GEF^scd1Δ*, and *MAPKK^byr1.DD*. Changes corresponding to each mutant are indicated as follows: Grey: removed components or interactions, orange: increased level of activity. For the exact implementation of the mutants, see Materials and Method. The measured component, **pp**MAPK^Spk1, is highlighted in green. (B) Measured and simulated **pp**MAPK^Spk1 activation profiles in wildtype, *ras1.G17V, Cdc42GEF^scd1Δ* and *MAPKK^byr1.DD* mutants. Dashed lines: model simulations. Diamonds: experimental data presented in Fig. 1C, E, G, and Fig. 3B; error bars: SEM. (C) GTP-loaded Ras1.G17V (1-172) directly binds to Byr2 (65-180) and Scd1 (760-872). *In vitro* GST pull-down assays of bacterially expressed Ras1.G17V (1-172), GST-Byr2 (65-180) and GST-Scd1 (760-872) were conducted as described in materials and methods. GTP-loaded Ras1.G17V (1-172) was found to bind to both GST-Byr2 (65-180) and GST-Scd1 (760-872). (D) Two Ras1 effectors, Byr2 and Scd1, compete for GTP-loaded Ras1.G17V (1-172). *In vitro* GST pull-down assays of bacterially expressed Ras1.G17V (1-172) and GST-Byr2 (65-180) were conducted as in (A). Addition of Scd1 (760-872) fragment interfered with Ras1-Byr2 binding (the 4th lane). Quantitated signal intensities of the Ras1.G17V (1-172) band in the gel are shown in the right panel. (E) Simulated **pp**MAPK^Spk1 dynamics in the wildtype model at increasing concentrations of Ras1-GTP added *in silico* to the system. Increased Ras1-GTP concentration causes advanced and reduced **pp**MAPK^Spk1 peak intensities. (F) The model fitted to the 4 strains (as above, in red) correctly predicts **pp**MAPK^Spk1 dynamics in the additional 21 signalling mutant strains (in light and dark green) measured in this study.

Fig. 8. Schematic diagram of the fission yeast pheromone signalling pathway
 (A) Wildtype fission yeast pheromone signalling pathway, highlighting the branched pheromone sensing, and that both branches are necessary for mating. (B) Because of the robust regulatory mechanism implemented for the MAPK pathway and the competition between the effectors, the constitutively active *ras1.G17V* mutation yields a biased overactivation of Cdc42.

Supplementary Figure S1. Validation of the use of a commercially available anti-GFP and anti- phospho-MAPK specific antibody. (A) Schematic outlining of the principal of a phospho-specific MAPK antibody, which specifically recognize the phosphorylated TEY motif (pTEpY) of MAPK. (B) Sequence alignment between mammalian ERK1, ERK2 and *S.pombe* MAPK^{Spk1} at the region of the dual phosphorylation required for activation and surrounding residues. Conserved residues are in light green and TEY is highlighted with orange-green. (C)-(E) A Western blot of a time-course of a WT (KT301) and a MAPK^{Spk1}-GFP strain (KT3082) over 24 hours, incubated with anti GFP, anti-pTEpY phospho-ERK and anti α-tubulin antibodies. Li-cor Odyssey system was used to detect the signals. (C) The signals obtained by the 700 nm wavelength scan to detect signals from a primary monoclonal mouse anti-GFP antibody ((0.4mg/ml), Roche Cat No 11814460001. Used at a 1:2000 dilution) and the primary anti α-tubulin antibody TAT1 (generous gift from Keith Gull, 1:3000), followed by the IRDye 680LT secondary antibody (goat anti-mouse antibody, Li-cor 926-32211(1.0 mg/ml), 1:16,000 dilution). α-tubulin was used as an internal loading control. (D)The exact same blot as in (C) but showing the 800 nm wavelength scan to detect signals from an anti pTEpY phospho-ERK antibody (#4370 Cell Signaling technology. Used at 1:2000 dilution) visualised by the IRDye 800CW goat anti-rabbit secondary antibody (Li-cor 926-68020 (1.0 mg/ml), 1:16000 dilution). The band indicated by a single asterisk (*) was concluded to be irrelevant to MAPK^{Spk1}-GFP because although this band runs very close to MAPK^{Spk1}-GFP, it does not exactly overlap with the MAPK^{Spk1}-GFP signal (in red) in (E) and (F). Furthermore, the band exists in non-tagged MAPK^{Spk1} strain seen in (D) and in *mapkk^{byr1}Δ* strains in (F), further supporting that the band is irrelevant to phospho-MAPK^{Spk1}-GFP. A double asterisk indicates a band which was also concluded not to be relevant to phospho-MAPK^{Spk1} because of the same reason. Considering the molecular weight, this double asterisk band may correspond to another MAPK, MAPK^{Pmk1}. (E) An overlay of the 700 and 800 nm channels presented in (C) and (D). (F) The phospho-ERK antibody is phospho-specific. Cell extracts were prepared from the time-course of MAPK^{Spk1}-GFP tagged WT (KT3082) and *mapkk^{byr1}Δ* strains (KT4300) and MAPK^{Spk1}-GFP was detected by anti-GFP (red) while phospho-MAPK^{Spk1} was detected by anti-pTEpY phosphor ERK antibody (green). In the *mapkk^{byr1}Δ* strain, phosphorylated MAPK^{Spk1}-GFP signal is missing although MAPK^{Spk1}-GFP was detectable at 8, 16 and 24 hours after induction of mating. The same background bands seen in (D) and (E) are indicated in the same way using a single (*) and double (**) asterisk.

A

Amount of total MAPK^{Spk1}-GFP

Total MAPK^{Spk1} / α-tubulin (arbitrary unit)

hours after induction of mating

B hours after induction of mating

Total MAPK^{Spk1}-GFP

Merged

Phospho-MAPK^{Spk1}-GFP

α-tubulin (Nda2 + Atb2)

C

hours after induction of mating

Phospho-MAPK^{Spk1}-GFP

α-tubulin (Nda2 + Atb2)

D

Phospho-MAPK^{Spk1}-GFP

Phospho MAPK^{Spk1} / α-tubulin (arbitrary unit)

hours after induction of mating

Supplementary Figure S2.
(A) and (B): Quantitation of total MAPK^{Spk1}-GFP during the mating process.
The total MAPK^{Spk1}-GFP protein level was detected using the anti-GFP antibody ((0.4mg/ml), Roche Cat No 11814460001. Used at a 1:2000 dilution). MAPK^{Spk1}-GFP Cells (KT3082) were induced for sexual differentiation by the plate mating assay system as described in the materials and methods. (A) Three biological replicates were used for quantitation to obtain the mean value (error bars are ±SEM). α-tubulin was used as a loading control and quantitation was carried out using the Image Studio ver2.1 software (Licor Odyssey CLx Scanner). (B) A typical example of Western blotting used for quantitation is shown. The green asterisk indicates the background band recognized by anti-phospho-ERK antibody (#4370 Cell Signaling technology. Used at 1:2000 dilution) as seen in the supplementary Figure S1.
(C) and (D): MAPKK$^{byr1.DD}$ mutation causes constitutive activation of MAPK^{Spk1}.
Cells carrying MAPKK$^{byr1.DD}$ mutation (KT3435) were induced for sexual differentiation by the plate mating assay system as described in the Materials and Methods. Western blotting of phospho-MAPK^{Spk1} and α-tubulin was conducted using ECL system (GE healthcare). (A) The results were visualized by exposing the signals to a X-ray film. (B) The bands were scanned and quantitated using ImageJ software (https://imagej.nih.gov/ij/). The α -tubulin signals were used as an internal control to estimate relative **ppMAPK^{Spk1}** levels.

Supplementary Figure S3. Original Western blotting images of WT, *ras1.G17V, byr1.DD, ras1.GV byr1.DD* and
***scd1Δ* mutants used to quantitate ppMAPK^Spk1-GFP during the mating process in Fig. 1, 2 and 3.**
MAPK^Spk1-GFP Cells were induced for sexual differentiation by the plate mating assay system as described in the materials
and methods. (A) Three biological replicates presented were used for quantitation to obtain the mean value and SEM. α-tubulin
was used as a loading control and quantitation was carried out using the Image Studio ver2.1 software (Licor Odyssey CLx Scanner).
ppMAPK^Spk1-GFP was detected by anti-phospho-ERK antibody (#4370 Cell Signaling technology. Used at 1:2000 dilution).
The green asterisk indicates the background band as seen in the supplementary Figure S1. Numbers indicate hours after induction
of mating. (B) Extracts of WT -2 and *ras1.G17V* -2 (left panel) and WT-2 and *scd1Δ* -2 (right panel) were re-run as technical replicates.
These membranes were used to estimate relative intensities of ppMAPK^Spk1-GFP between WT, *scd1Δ* and *ras1.G17V* strains.

Supplementary Figure S4. Oribinal Western blotting membranes used in Fig. 3 and 5.
(A) Original Western blotting membrane used to quantitate phospho-MAPK^{Spk1}-GFP to generate the graph presented in Figure 3 (D). Strains used were; *ras1Δ* (KT4323), *MAPKK$^{byr1.DD}$* (KT3435) and *ras1Δ MAPKK$^{byr1.DD}$* (KT4359) (B) Original Western blotting membrane used to quantitate phospho-MAPK^{Spk1}-GFP to generate the graph presented in Figure 3 (E).

A

B

Supplementary Figure S5. Original Western blotting membranes used in Fig. 6.
(A) Original Western blotting membranes used to quantitate phospho-MAPK^{Spk1}-GFP to generate the graph in Figure 6 (A) Strains used were; *gpa1Δ* (KT4335), *gpa1Δ ras1.G17V* (KT5023), *gpa1Δ MAPKK$^{byr1.DD}$* (KT4353) and *gpa1Δ ras1.val17 MAPKK$^{byr1.DD}$*.(KT5035). (B) Original Western blotting membrane used to quantitate phospho-MAPK^{Spk1}-GFP to generate the graph in Figure 6 (C). Strains used were; *h⁻* WT (KT4190), *h⁻ gpa1.QL* (KT5059), *h⁻ ras1.G17V* (KT4233), *h⁻ gpa1.QL ras1Δ* (KT5070), *h⁻ MAPKK$^{byr1.DD}$* (KT4194). The green asterisk indicates a background band recognized by anti-phospho-ERK antibody (#4370 Cell Signaling technology. Used at 1:2000 dilution). α-tubulin was used as a loading control and quantitation was carried out using the Image Studio ver2.1 software (Licor Odyssey CLx Scanner).

Supplementary Figure S6. Parameter distributions and relationships in multiplexed global parameter fitting.

Supplementary Figure S7. Convergence of parameters in linear scale, over an extended range

Supplementary Figure S8. Ensemble modeling shows that the dynamics of protein concentration are robustly predicted regardless of certain parameters' unidentifiability.
Time course simulation of the 100 best-fitted wild type models for all 6 variables. Rolling averages (window of 100) are displayed in color, and ten thousand randomly sampled simulation points (in grey) for each experiment show a narrow distribution of predicted concentration dynamics.

 Supplementary Information

 Supplementary Figures

 Supplementary Figure S1. Validation of the use of a commercially available anti-GFP and

 anti- phospho-MAPK specific antibody.

(A) Schematic outlining of the principal of a phospho-specific MAPK antibody, which

specifically recognize the phosphorylated TEY motif (pTEpY) of MAPK. (B) Sequence

alignment between mammalian ERK1, ERK2 and *S.pombe* MAPK^{Spk1} at the region of the dual

phosphorylation required for activation and surrounding residues. Conserved residues are in

light green and TEY is highlighted with orange-green. (C)-(E) A Western blot of a time-course

of a WT (KT301) and a MAPK^{Spk1}-GFP strain (KT3082) over 24 hours, incubated with anti GFP,

anti-pTEpY phospho-ERK and anti α-tubulin antibodies. Li-cor Odyssey system was used to

detect the signals. (C) The signals obtained by the 700 nm wavelength scan to detect signals

from a primary monoclonal mouse anti-GFP antibody ((0.4mg/ml), Roche Cat No

11814460001. Used at a 1:2000 dilution) and the primary anti α-tubulin antibody TAT1

(generous gift from Keith Gull, 1:3000), followed by the IRDye 680LT secondary antibody

(goat anti-mouse antibody, Li-cor 926-32211(1.0 mg/ml), 1:16,000 dilution). α-tubulin was

used as an internal loading control. (D)The exact same blot as in (C) but showing the 800 nm

wavelength scan to detect signals from an anti pTEpY phospho-ERK antibody (#4370 Cell

Signaling technology. Used at 1:2000 dilution) visualised by the IRDye 800CW goat anti-

rabbit secondary antibody (Li-cor 926-68020 (1.0 mg/ml), 1:16000 dilution). The band

indicated by a single asterisk (*) was concluded to be irrelevant to MAPK^{Spk1}-GFP because

although this band runs very close to MAPK^{Spk1}-GFP, it does not exactly overlap with the

MAPK^{Spk1}-GFP signal (in red) in (E) and (F). Furthermore, the band exists in non-tagged

MAPK^{Spk1} strain seen in (D) and in *mapkk^{byr1}Δ* strains in (F), further supporting that the band

is irrelevant to phospho-MAPK^{Spk1}-GFP. A double asterisk indicates a band which was also

concluded not to be relevant to phospho-MAPK^{Spk1} because of the same reason. Considering

the molecular weight, this double asterisk band may correspond to another MAPK,

MAPK^{Pmk1}. (E) An overlay of the 700 and 800 nm channels presented in (C) and (D). (F) The

phospho-ERK antibody is phospho-specific. Cell extracts were prepared from the time-

course of MAPK^{Spk1}-GFP tagged WT (KT3082) and *mapkk^{byr1}Δ* strains (KT4300) and MAPK^{Spk1}-

GFP was detected by anti-GFP (red) while phospho-MAPK^{Spk1} was detected by anti-pTEpY

phosphor ERK antibody (green). In the *mapkk^{byr1}Δ* strain, phosphorylated MAPK^{Spk1}-GFP

signal is missing although MAPK^{Spk1}-GFP was detectable at 8, 16 and 24 hours after

induction of mating. The same background bands seen in (D) and (E) are indicated in the

same way using a single (*) and double (**) asterisk.

Supplementary Figure S2.

(A) and (B): Quantitation of total MAPK^{Spk1}-GFP during the mating process.

The total MAPK^{Spk1}-GFP protein level was detected using the anti-GFP antibody ((0.4mg/ml),

Roche Cat No 11814460001. Used at a 1:2000 dilution). MAPK^{Spk1}-GFP Cells (KT3082) were

induced for sexual differentiation by the plate mating assay system as described in the

materials and methods. (A) Three biological replicates were used for quantitation to obtain

the mean value (error bars are ±SEM). α-tubulin was used as a loading control and

quantitation was carried out using the Image Studio ver2.1 software (Licor Odyssey CLx

Scanner). (B) A typical example of Western blotting used for quantitation is shown. The

green asterisk indicates the background band recognized by anti-phospho-ERK antibody

(#4370 Cell Signaling technology. Used at 1:2000 dilution) as seen in the supplementary

Figure S1.

(C) and (D): *MAPKK$^{byr1.DD}$* mutation causes constitutive activation of MAPK^{Spk1}.

Cells carrying *MAPKK$^{byr1.DD}$* mutation (KT3435) were induced for sexual differentiation by the

plate mating assay system as described in the Materials and Methods. Western blotting of

phospho-MAPK^{Spk1} and α-tubulin was conducted using ECL system (GE healthcare). (A) The

results were visualized by exposing the signals to a X-ray film. (B) The bands were scanned

and quantitated using ImageJ software (https://imagej.nih.gov/ij/). The α-tubulin signals

were used as an internal control to estimate relative ppMAPK^{Spk1} levels.

Supplementary Figure S3.

Original Western blotting images of WT, *ras1.G17V*, *byr1.DD*, *ras1.GV byr1.DD* and *scd1Δ*

mutants used to quantitate ppMAPK^{Spk1}-GFP during the mating process in Fig. 1, 2 and 3.

MAPK^{Spk1}-GFP Cells were induced for sexual differentiation by the plate mating assay system

as described in the materials and methods. (A) Three biological replicates presented were

used for quantitation to obtain the mean value and SEM. α-tubulin was used as a loading

control and quantitation was carried out using the Image Studio ver2.1 software (Licor

Odyssey CLx Scanner). **pp**MAPK^{Spk1}-GFP was detected by anti-phospho-ERK antibody (#4370

Cell Signaling technology. Used at 1:2000 dilution). The green asterisk indicates the

background band as seen in the supplementary Figure S1. Numbers indicate hours after

induction of mating. M: Marker lane. (B) Extracts of WT -2 and *ras1.G17V* -2 (left panel) and

WT-2 and *scd1Δ* -2 (right panel) were re-run as technical replicates. These membranes were

used to estimate relative **pp**MAPK^{Spk1} intensities between WT, *scd1Δ* and *ras1.G17V* strains.

Supplementary Figure S4. Original Western blotting membranes used in Fig. 3 and 5.

(A) Original Western blotting membrane used to quantitate phospho-MAPK^{Spk1}-GFP to

generate the graph presented in Figure 3 (D). Strains used were; *ras1Δ* (KT4323),

MAPKK$^{byr1.DD}$ (KT3435) and *ras1Δ MAPKK$^{byr1.DD}$* (KT4359) (B) Original Western blotting

membrane used to quantitate phospho-MAPK^{Spk1}-GFP to generate the graph presented in

Figure 3 (E). Strains used were; in *mapkkk^{byr2}Δ* (KT3763), *MAPKK$^{byr1.DD}$* (KT3435) and

mapkkk^{byr2}Δ MAPKK$^{byr1.DD}$ (KT4010). (C) Original Western blotting membrane used to

quantitate phospho-MAPK^{Spk1}-GFP to generate the graph in Figure 5 (A). Strains used were;

ste4Δ (KT4376), *ste4Δ ras1.G17V* (KT5143) and *ste4Δ MAPKK$^{byr1.DD}$* (KT5136). (D) Original

Western blotting membrane used to quantitate phospho-MAPK^{Spk1}-GFP to generate the

graph in Figure 5 (C). Strains used were; *ste6Δ* (KT4333), *ste6Δ ras1.G17V* (KT4998) and

ste6Δ MAPKK$^{byr1.DD}$ (KT5139). Indicated mutant cells were induced for mating by the plate

mating assay system as described in the Materials and Methods. Western blotting of

phospho-MAPK^{Spk1} and α-tubulin was conducted in the same way as Supplementary Figure

S1. The green asterisks indicate the same background band recognized by anti-phospho-ERK

antibody (#4370 Cell Signaling technology. Used at 1:2000 dilution) seen in the

Supplementary Figure S1 and do not overlap with the red signals that represent the "Total

MAPK^{Spk1}-GFP" in the "Merged" panel. α-tubulin was used as a loading control and

quantitation was carried out using the Image Studio ver2.1 software (Licor Odyssey CLx

Scanner).

Supplementary Figure S5. Original Western blotting membranes used in Fig. 6.

(A) Original Western blotting membranes used to quantitate phospho-MAPK^{Spk1}-GFP to generate the graph in Figure 6 (A) Strains used were; *gpa1Δ* (KT4335), *gpa1Δ ras1.G17V* (KT5023), *gpa1Δ MAPKK$^{byr1.DD}$* (KT4353) and *gpa1Δ ras1.val17 MAPKK$^{byr1.DD}$*.(KT5035). (B) Original Western blotting membrane used to quantitate phospho-MAPK^{Spk1}-GFP to generate the graph in Figure 6. (C) Strains used were; *h$^-$* WT (KT4190), *h$^-$ gpa1.QL* (KT5059), *h$^-$ ras1.G17V* (KT4233), *h$^-$ gpa1.QL ras1Δ* (KT5070), h$^-$ *MAPKK$^{byr1.DD}$* (KT4194). The green asterisk indicates a background band recognized by anti-phospho-ERK antibody (#4370 Cell Signaling technology. Used at 1:2000 dilution). α-tubulin was used as a loading control and quantitation was carried out using the Image Studio ver2.1 software (Licor Odyssey CLx Scanner).

Supplementary Figure S6. Parameter distributions and relationships in multiplexed global parameter fitting

(A) Distribution of objective values after 5000 parallel parameter estimations by the global optimization algorithm "particle swarm" with randomized starting values within +- 4 magnitudes around the previously achieved best fit. Fits with an objective value < 5 are accepted for further analysis (green). Simulations with +- 5 magnitudes resulted in the same best fits, but much smaller convergence (See Materials and Methods).

(B-C) Coefficient of variation and distribution of parameters within the 578 the accepted fits show unimodal distributions for all parameters, and most of them are narrowly distributed, suggesting a unique optimum. In (C), the only bimodal distribution is that of RasGTP0 (Scd1Δ) among fits below O.V.<5. In (D, top right corner) however it is shown that this parameter also converges to a single optima, below O.V. of 3.

(D) Pairwise scatterplots and Spearman correlation coefficients among all parameters and the objective value (log scale axes). In this figure, every dot is an independently fitted model (obj. value <5); and every panel shows a pairwise correlation between a fitted parameter and the objective value (top row), or between two fitted parameters (other rows). Green to

120 brown denotes the objective values between 3.4 and 5. The top row shows that with better

121 fits, all parameters (but k_1) converge to a single optimum (bottom most points, in green).

Supplementary Figure S7. Convergence of parameters in linear scale, over an extended

range

(A) Alternative representation of the top row of Fig.S6D. Parameter values are displayed on

a linear scale (X-axis) and fits below and objective value (O.V.) of 8 (instead of below 5) are

displayed.

(B) Simulated time course of MAPK^{Spk1} in the best fit of a simplified model variant shows no

advanced peaking in the *ras1.G17V* and *scd1Δ* mutant strains. This model is simplified from

the original model (Fig.7 A) by removing [L10], and models the scenario where Ras has no

complex interactions, it has only activating roles [L5, L9].

(C) Simulated ppMAPK^{Spk1} dynamics in the simplified model (B) at increasing concentrations

of Ras1^{GTP} added *in silico* to the system. Increased Ras1^{GTP} concentration causes advanced

and reduced **pp**MAPK^{Spk1} peak intensities.

Supplementary Figure S8. Ensemble modeling shows that the dynamics of protein

137 **concentration are robustly predicted regardless of certain parameters' unidentifiability.**

138 Time course simulation of the 100 best-fitted wild type models for all 6 variables. Rolling

139 averages (window of 100) are displayed in color, and ten thousand randomly sampled

140 simulation points (in grey) for each experiment show a narrow distribution of predicted

141 concentration dynamics.

Supplementary Table S1 : Strains used in this study

Figure 1

C, D

KT3082 *h⁹⁰ ade6.M216 leu1.32 spk1-GFP-2xFLAG::Kan^R*

E, F

KT3435 *h⁹⁰ ade6-M216 leu1.32 byr1.DD::Hyg^R spk1-GFP-2xFLAG::Kan^R*

G, H

KT3084 *h⁹⁰ ade6.M210 leu1.32 ras1.G17V::LEU2⁺ spk1-GFP-2xFLAG::Kan^R*

Figure 2

A, B

KT3439 *h⁹⁰ ade6.M210 leu1.32 ras1.G17V::LEU2⁺ byr1.DD::Hyg^R spk1-GFP-2xFLAG::Kan^R*

C

KT4300 *h⁹⁰ ade6.M216 leu1.32 byr1::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

KT5215 *h⁹⁰ ade6.M210 leu1.32 ras1.G17V::LEU2⁺ byr1::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

Figure 3

A

KT3082 *h⁹⁰ ade6.M216 leu1.32 spk1-GFP-2xFLAG::Kan^R*

KT4061 *h⁹⁰ ade6.M216 leu1.32 scd1::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

KT4056 *h⁹⁰ ade6.M210 leu1.32 ras1.G17V::LEU2⁺ scd1::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

B

KT3082 *h⁹⁰ ade6.M216 leu1.32 spk1-GFP-2xFLAG::Kan^R*

KT4061 *h⁹⁰ ade6.M216 leu1.32 scd1::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

C

KT4047 *h⁹⁰ ade6.M216 leu1.32 byr1.DD::Hyg^R scd1::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

D

KT4323 *h⁹⁰ ade6.M216 leu1.32 ras1::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

KT3435 *h⁹⁰ ade6-M216 leu1.32 byr1.DD::Hyg^R spk1-GFP-2xFLAG::Kan^R*

KT4359 *h⁹⁰ ade6.M216 leu1.32 byr1.DD::Hyg^R ras1::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

E

KT3763 *h⁹⁰ ade6.M216 leu1.32 byr2::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

KT3435 *h⁹⁰ ade6-M216 leu1.32 byr1.DD::Hyg^R spk1-GFP-2xFLAG::Kan^R*

KT4010 *h⁹⁰ ade6-M216 leu1.32 byr1.DD::Hyg^R byr2::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

F

KT4323 *h⁹⁰ ade6.M216 leu1.32 ras1::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

KT4359 *h⁹⁰ ade6.M216 leu1.32 byr1.DD::Hyg^R ras1::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

KT3763 *h⁹⁰ ade6.M216 leu1.32 byr2::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

KT4010 *h⁹⁰ ade6-M216 leu1.32 byr1.DD::Hyg^R byr2::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

Fig. 4

A, B

KT5077 *h⁹⁰ ade6.M210 leu1.32 ura4.294::[Pshk1:ScGIC2 CRIB:GFP3:ura4⁺]*

KT5082 *h⁹⁰ ade6.M216 leu1.32 ras1.G17V::LEU2⁺ ura4.294::[Pshk1:ScGIC2 CRIB:GFP3:ura4⁺]*

C, D

KT5107 *h⁹⁰ ade6.M210 leu1.32 ras1::ClonNAT^R ura4.294::[Pshk1:ScGIC2 CRIB:GFP3:ura4⁺]*

KT5077 *h⁹⁰ ade6.M210 leu1.32 ura4.294::[Pshk1:ScGIC2 CRIB:GFP3:ura4⁺]*

KT5082 *h⁹⁰ ade6.M216 leu1.32 ras1.G17V::LEU2⁺ ura4.294::[Pshk1:ScGIC2 CRIB:GFP3:ura4⁺]*

KT5551 *h⁹⁰ ade6.M210 leu1.32 rga4::Hyg^R ura4.294::[Pshk1:ScGIC2 CRIB:GFP3:ura4⁺]*

KT5554 *h⁹⁰ ade6.M216 leu1.32 ras1.G17V::LEU2⁺ rga4::Hyg^R ura4.294::[Pshk1:ScGIC2 CRIB:GFP3:ura4⁺]*

Fig. 5

A, B

KT4376 *h⁹⁰ ade6.M216 leu1.32 ste4::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

KT5143 *h⁹⁰ ade6.M210 leu1.32 ste4::ClonNAT^R ras1.G17V::LEU2⁺ spk1-GFP-2xFLAG::Kan^R*

KT5136 *h⁹⁰ ade6-M216 leu1.32 ste4::ClonNAT^R byr1.DD::Hyg^R spk1-GFP-2xFLAG::Kan^R*

C, D

KT4333 *h⁹⁰ ade6.M216 leu1.32 ste6::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

KT4998 *h⁹⁰ ade6.M210 leu1.32 ste6::Hyg^R ras1.G17V::LEU2⁺ spk1-GFP-2xFLAG::Kan^R*

KT5139 *h⁹⁰ ade6-M216 leu1.32 ste6::ClonNAT^R byr1.DD::Hyg^R spk1-GFP-2xFLAG::Kan^R*

Fig. 6

A, B

KT4335 *h⁹⁰ ade6.M216 leu1.32 gpa1::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

KT5023 *h⁹⁰ ade6.M210 leu1.32 gpa1::ClonNAT^R ras1.G17V::LEU2⁺ spk1-GFP-2xFLAG::Kan^R*

KT4353 *h⁹⁰ ade6-M216 leu1.32 gpa1::ClonNAT^R byr1.DD::Hyg^R spk1-GFP-2xFLAG::Kan^R*

KT5035 *h⁹⁰ ade6.M210 leu1.32 gpa1::ClonNAT^R ras1.G17V::LEU2⁺ byr1.DD::Hyg^R spk1-GFP-2xFLAG::Kan^R*

C, D

KT4190 *h⁻ ade6.M216 leu1.32 spk1-GFP-2xFLAG::Kan^R*

KT5059   *h⁻ ade6.M216 leu1.32 ura4.d18 gpa1.QL::ura4⁺ spk1-GFP-2xFLAG::Kan^R*

KT4233   *h⁻ ade6.M216 leu1.32 ras1.G17V::LEU2⁺ spk1-GFP-2xFLAG::Kan^R*

KT5070   *h⁻ ade6.M216 leu1.32 ura4.d18 ras1::ClonNAT^R gpa1.QL::ura4⁺ spk1-GFP-2xFLAG::Kan^R*

KT4194   *h⁻ ade6.M216 leu1.32 byr1.DD::Hyg^R spk1-GFP-2xFLAG::Kan^R*

Supplementary Figure S1

C, D and E

KT301   *h⁹⁰ ade6-M216 leu1.32*

KT3082   *h⁹⁰ ade6.M216 leu1.32 spk1-GFP-2xFLAG::Kan^R*

F

KT3082   *h⁹⁰ ade6.M216 leu1.32 spk1-GFP-2xFLAG::Kan^R*

KT4300   *h⁹⁰ ade6.M216 leu1.32 byr1::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

Supplementary Figure S2

A and B

KT3082   *h⁹⁰ ade6.M216 leu1.32 spk1-GFP-2xFLAG::Kan^R*

C and D

KT3435   *h⁹⁰ ade6-M216 leu1.32 byr1.DD::Hyg^R spk1-GFP-2xFLAG::Kan^R*

Supplementary Figure S3

KT3082   *h⁹⁰ ade6.M216 leu1.32 spk1-GFP-2xFLAG::Kan^R*

KT3435   *h⁹⁰ ade6-M216 leu1.32 byr1.DD::Hyg^R spk1-GFP-2xFLAG::Kan^R*

KT3084   *h⁹⁰ ade6.M210 leu1.32 ras1.G17V::LEU2⁺ spk1-GFP-2xFLAG::Kan^R*

KT3439   *h⁹⁰ ade6.M210 leu1.32 ras1.G17V::LEU2⁺ byr1.DD::Hyg^R spk1-GFP-2xFLAG::Kan^R*

KT4061   *h⁹⁰ ade6.M216 leu1.32 scd1::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

Supplementary Figure S4

A

KT4323   *h⁹⁰ ade6.M216 leu1.32 ras1::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

KT3435   *h⁹⁰ ade6-M216 leu1.32 byr1.DD::Hyg^R spk1-GFP-2xFLAG::Kan^R*

KT4359   *h⁹⁰ ade6.M216 leu1.32 byr1.DD::Hyg^R ras1::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

B

KT3763   *h⁹⁰ ade6.M216 leu1.32 byr2::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

KT3435   *h⁹⁰ ade6-M216 leu1.32 byr1.DD::Hyg^R spk1-GFP-2xFLAG::Kan^R*

KT4010   *h⁹⁰ ade6-M216 leu1.32 byr1.DD::Hyg^R byr2::ClonNAT^R spk1-GFP-2xFLAG::Kan^R*

C

KT4376 *h⁹⁰ ade6.M216 leu1.32 ste4::ClonNATᴿ spk1-GFP-2xFLAG::Kanᴿ*

KT5143 *h⁹⁰ ade6.M210 leu1.32 ste4::ClonNATᴿ ras1.G17V::LEU2⁺ spk1-GFP-2xFLAG::Kanᴿ*

KT5136 *h⁹⁰ ade6-M216 leu1.32 ste4::ClonNATᴿ byr1.DD::Hygᴿ spk1-GFP-2xFLAG::Kanᴿ*

D

KT4333 *h⁹⁰ ade6.M216 leu1.32 ste6::ClonNATᴿ spk1-GFP-2xFLAG::Kanᴿ*

KT4998 *h⁹⁰ ade6.M210 leu1.32 ste6::Hygᴿ ras1.G17V::LEU2⁺ spk1-GFP-2xFLAG::Kanᴿ*

KT5139 *h⁹⁰ ade6-M216 leu1.32 ste6::ClonNATᴿ byr1.DD::Hygᴿ spk1-GFP-2xFLAG::Kanᴿ*

Supplementary Figure S5

A

KT4335 *h⁹⁰ ade6.M216 leu1.32 gpa1::ClonNATᴿ spk1-GFP-2xFLAG::Kanᴿ*

KT5023 *h⁹⁰ ade6.M210 leu1.32 gpa1::ClonNATᴿ ras1.G17V::LEU2⁺ spk1-GFP-2xFLAG::Kanᴿ*

KT4353 *h⁹⁰ ade6-M216 leu1.32 gpa1::ClonNATᴿ byr1.DD::Hygᴿ spk1-GFP-2xFLAG::Kanᴿ*

KT5035 *h⁹⁰ ade6.M210 leu1.32 gpa1::ClonNATᴿ ras1.G17V::LEU2⁺ byr1.DD::Hygᴿ spk1-GFP-2xFLAG::Kanᴿ*

B

KT4190 *h⁻ ade6.M216 leu1.32 spk1-GFP-2xFLAG::Kanᴿ*

KT5059 *h⁻ ade6.M216 leu1.32 ura4.d18 gpa1.QL::ura4⁺ spk1-GFP-2xFLAG::Kanᴿ*

KT4233 *h⁻ ade6.M216 leu1.32 ras1.G17V::LEU2⁺ spk1-GFP-2xFLAG::Kanᴿ*

KT5070 *h⁻ ade6.M216 leu1.32 ura4.d18 ras1::ClonNATᴿ gpa1.QL::ura4⁺ spk1-GFP-2xFLAG::Kanᴿ*

KT4194 *h⁻ ade6.M216 leu1.32 byr1.DD::Hygᴿ spk1-GFP-2xFLAG::Kanᴿ*