The joint evolution of lifespan and self-fertilisation

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Abstract

In Angiosperms, there exists a strong association between mating system and lifespan. Most self-fertilising species are short-lived and most predominant or obligate outcrossers are long-lived. This association is generally explained by the influence of lifespan on the evolution of the mating system, considering lifespan as fixed. Yet, lifespan can itself evolve, and the mating system may as well influence the evolution of lifespan, as is suggested by joint evolutionary shifts of lifespan and mating system between sister species for instance. In this paper, we build modifier models to study the joint evolution of self-fertilisation and lifespan, including both juvenile and adult inbreeding depression. We show that self-fertilisation is expected to promote evolution towards shorter lifespan, and that the range of conditions under which selfing can evolve rapidly shrinks as lifespan increases. In particular, we show how extrinsic mortality conditions affect the evolutionary associations between lifespan and selfing.

1 Introduction

In Angiosperms, strong associations exist between mating systems and other life-history traits, such as dispersal (Auld and Rubio de Casas, 2012), allocation to male *vs.* female functions (Brunet, 1992), or lifespan (Barrett and Harder, 1996). The latter association has received limited attention. Indeed, while it has long been recognised that most self-fertilising species are short-lived and most predominant or obligate outcrossers are long-lived (Stebbins, 1950; Barrett and Harder, 1996; Duminil et al., 2009; Munoz et al., 2016), relatively few arguments have been advanced to explain this association.

Stebbins (1950) proposed that the reproductive assurance provided by self-fertilisation could be less beneficial to perennials than it is to annuals, since they get more than one try at reproducing. Later, Lloyd (1992) suggested that self-fertilisation in perennials could cause the consumption of resources that could have been more advantageously allocated to post-breeding survival or future outcrossed reproduction (between-seasons seed discounting). Morgan et al. (1997) investigated the validity of these arguments by developing a phenotypic model and concluded that the association between annuality and selfing is more likely to be due to between-seasons seed discounting, rather than reproductive assurance. They also showed the importance of the repeated effect of adult inbreeding depression for the maintenance of outcrossing in perennials. Empirical evidence also suggests that inbreeding depression is overall higher in perennials than in annuals (Angeloni et al., 2011), which could constitute an additionnal barrier to the evolution of self-fertilisation in perennials.

These arguments focus on the consequences of perenniality for the evolution of self-fertilisation, considering lifespan as a fixed characteristic. Yet, lifespans evolve in nature (Stearns, 1992), and joint evolutionary shifts of lifespan and mating system have been documented. Indeed, the transition to self-fertilisation is often associated with significant morphological changes, such as vegetative size and flower size reduction (the selfing syndrome, Sicard and Lenhard, 2011), and lifespan shortening compared to outcrossing relatives (Ehrlén and Lehtilä, 2002). For example, *Arabidopsis thaliana* is a highly selfing annual that recently differentiated from its self-incompatible and perennial relatives *A. lyrata* and *A. halleri* (Clauss and Mitchell-Olds, 2006). Furthermore, studying pairs of

sister species, Grossenbacher et al. (2015) found numerous joint shifts towards selfing and annuality from outcrossing, perennial ancestors in genus such as *Mimulus* or *Medicago*, and very few shifts to longer lifespans in association with selfing. In fact, the only such shifts they found were observed in the *Oenothera* genus, where segregation and recombination are suppressed when reproducing by self-fertilisation, which implies that selfing individuals are effectively reproducing clonally (Johnson et al., 2009).

These examples show that joint shifts of mating system and lifespan almost always occur in the same direction, that is towards lifespan shortening in association with selfing from outcrossing ancestors with longer lifespans. In such situations, lifespan shortening could have allowed for the evolution of self-fertilisation. Alternatively, the transition to self-fertilisation could have induced evolution towards a shorter lifespan. This possibility has seldom been investigated. Indeed, classical studies of the evolution of lifespan predict that it should be fine tuned to best fit the extrinsic mortality conditions experienced by the considered population, through optimal allocation of resources to reproduction, growth or survival (e.g. Schaffer, 1974; Cichoń, 1997) and senescence (e.g. Silvertown et al., 2001), but rarely consider the evolution of lifespan in interaction with other traits. From a theoretical standpoint, the only study that, to our knowledge, investigated the influence of the mating system on lifespan evolution is that of Zhang (2000), who developed a phenotypic model for the joint evolution of reproductive effort and sex allocation in partially self-fertilising hermaphrodites. Assuming a survival *vs.* reproduction trade-off (Stearns, 1992), they reached the conclusion that reproductive effort increases (and lifespan decreases) when the selfing rate increases through greater allocation to the female function, provided that inbreeding depression is weak ($\delta < \frac{1}{2}$), female reproduction is very costly, and juvenile survivorship is constrained within a narrow range of values. Importantly however, Zhang (2000) assumed inbreeding depression to only affect the survival of juveniles to maturity, although inbreeding depression typically occurs over all stages of the life cycle (Husband and Schemske, 1996).

In summary, on one hand, the influence of lifespan on the evolution of the mating system has been studied, considering lifespan as a fixed characteristic (Morgan et al., 1997). On the other hand, the potential influence of the mating system on the evolution of lifespan was only scarcely investigated, assuming no inbreeding depression occured in

adults (Zhang, 2000). Finally, the question of the joint evolution of lifespan and mating system was never tackled. In this paper, we build modifier models (Kirkpatrick et al., 2002) to investigate the joint evolution of lifespan and selfing, including both juvenile and adult inbreeding depressions as fixed parameters. Following previous authors, we model the evolution of lifespan through that of reproductive effort, assuming a survival *vs* reproduction trade-off for which we consider various shapes (Stearns, 1992), and incorporate extrinsic mortality as a constant parameter (Schaffer, 1974; Zhang, 2000). To study the joint evolution of mating system and lifespan, we proceed in three steps. We first study the influence of selfing on the evolution of lifespan, and show that self-fertilisation is expected to favour evolution towards shorter lifespans when inbreeding depression affects adult survival. Then, we examine the consequences of lifespan for the evolution of self-fertilisation, and show that the range of inbreeding depression under which selfing can evolve rapidly shrinks as lifespan increases, in agreement with anterior work (Morgan et al., 1997). Finally, we consider the joint evolution of lifespan and selfing and show how extrinsic mortality conditions are expected to affect evolutionary associations.

2 Model

Life cycle and demographic assumptions. We consider a very large population made of partially selfing hermaphrodites, which are assumed to be diploid. We assume the population stays at carrying capacity. This implies that juveniles may only settle in replacement of recently deceased adults (Figure 1). Once settled, juveniles reach maturity before the next mating event.

We assume that adults keep the same fecundity and survival probability throughout their lives (*i.e.* no age-specific effects). Established individuals allocate a fraction e of their resources to reproduction, and the remaining fraction $1 - e$ to post-breeding survival. Consequently, sexually mature individuals have a certain probability of survival between mating events (say, flowering seasons) and generations may overlap: the more resources an individual allocates to reproduction, the larger its reproductive output, but the lower its chance of survival until the next mating event. During each mating event, individuals reproduce by self-fertilisation in a proportion α, and by random mating other-

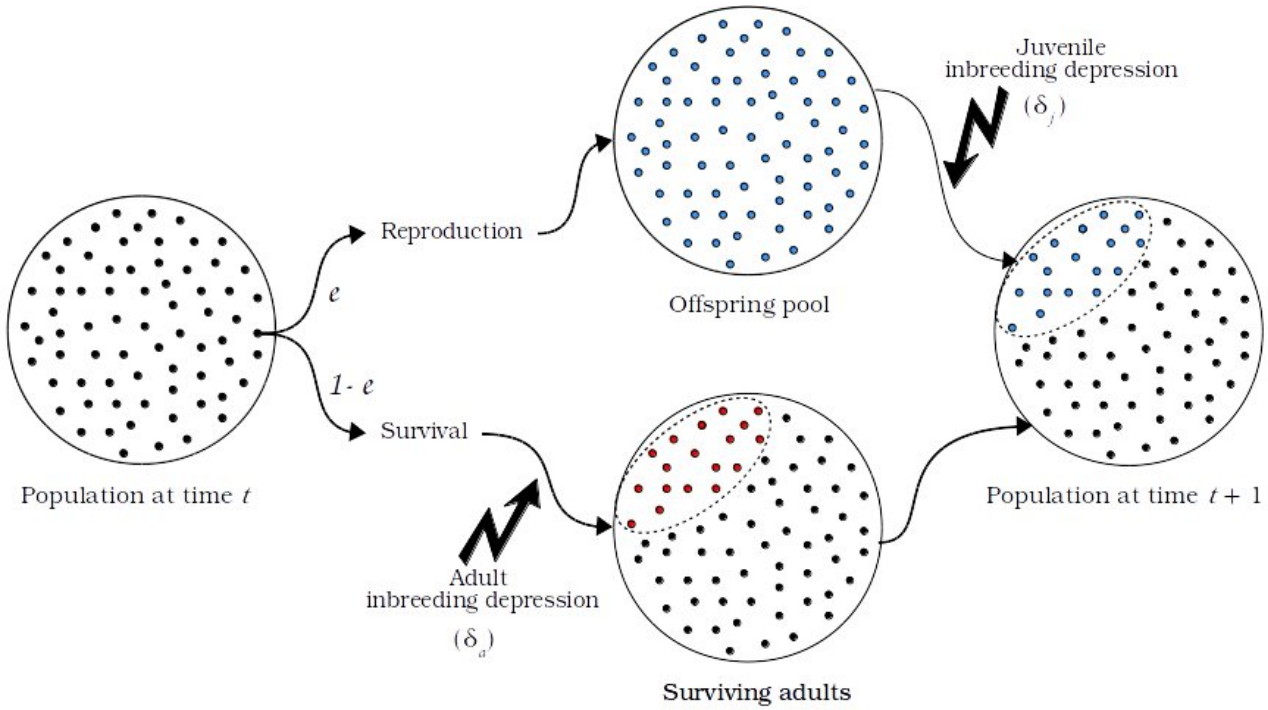

Figure 1: Schematic representation of the life cycle and demography assumed in the model. Established individuals allocate a fraction e of their resources to reproduction, and the remaining $1 - e$ to survival. Juveniles replace deceased adults. Red dots depict deceased adults, and blue dots depict juveniles

wise. Selfed offspring suffer from inbreeding depression (Charlesworth and Charlesworth, 1987) differently depending on their development stage. As juveniles, they suffer from juvenile inbreeding depression, denoted δ_j, which decreases their probability of survival to maturity. If they reach maturity, they suffer from adult inbreeding depression, denoted δ_a, which decreases their survival probability between mating events. Denoting $\mathcal{S}_o(e)$ the survival probability between two mating events of an outcrossed individual as a function of its reproductive effort, that of a selfed individual, $\mathcal{S}_s(e)$, is therefore given by $\mathcal{S}_s(e) = \mathcal{S}_o(e) \times (1 - \delta_a)$.

Genetic assumptions. We assume that the individuals' selfing rate and reproductive effort are each entirely determined by a single biallelic modifier locus. In each case, we consider the population to be initially fixed with one allele (the resident) and introduce a rare mutant allele which has a small effect on its bearer's phenotype. We then follow the

change in frequency of this mutant, and look for situations where no mutant can increase in frequency, that is, Evolutionarily Stable Strategies (ESS, Maynard Smith and Price, 1973).

Proportion of selfed individuals. We track the proportion of selfed individuals in the population (Θ), which stays close to its equilibrium value in the absence of mutants (Θ^*) when mutants at modifier loci are rare and only weakly deviate from the resident strategy. As shown in Appendix I, this equilibrium value is given by

$$\Theta^* = \frac{\alpha\,(1-\delta_j)\,(1-\mathcal{S}_o(e))}{\alpha\,(1-\delta_j)\,(1-\mathcal{S}_o(e)) + (1-\alpha)\,\delta_a\mathcal{S}_o(e)}. \tag{1}$$

Equation (1) is a decreasing function of $\mathcal{S}_o(e)$, that is the equilibrium proportion of selfed individuals in the population is decreased by generations overlap. We show in Appendix I that this is due to the repeated effect of adult inbreeding depression on post-breeding survival.

Numerical analyses. The analytical results we obtain with approximations are compared with that of exact numerical analyses. For each model, the exact recursions, that is tracking genotypic frequencies (rather than allelic frequencies and genetic associations) with no approximation made, are run for 10^6 generations with a rare mutant ($p_m = 10^{-4}$) introduced at $t = 0$, and the resulting frequency of the mutant is compared to its initial one. When the mutant increases in frequency, the mutant allele is taken as resident, and recursions are run again introducing a new mutant, until mutants no longer increase in frequency or the analysis hits a bound (*i.e.* 0 or 1). As these analyses were only conducted for validation purpose, outputs are presented in Appendix V. Our results showed that the approximations we obtain are very close to the numerically obtained ESS.

2.1 Evolution of lifespan in a partially selfing population

In this section, we analyse a model for the evolution of lifespan under partial selfing through the evolution of reproductive effort, considering the selfing rate α as a parameter. We assume that the reproductive effort of a given individual is entirely determined by its genotype at a single biallelic modifier locus. Alleles M and m, which we assume

to be codominant, code for a reproductive effort $e = e_0$ and $e = e_0 + \varepsilon$, respectively. Furthermore, following Zhang (2000), we assume that the survival probability between two mating events of an outcrossed individual as a function of its reproductive effort e, is given by

$$\mathcal{S}_o(e) = S\left(1 - e^x\right), \tag{2}$$

where S is the maximal survival probability, that is a measure of extrinsic mortality, and x controls the shape of the survival *vs* reproduction trade-off. The detailed recursions are given in Appendix II. In brief, we follow the variation of three variables, namely, the frequency of allele m (p_m), which is assumed to be a very rare mutant with a small effect (ε), the deviation in homozygosity at the modifier locus as compared to the panmictic expectation ($D_{m,m}$), and the proportion of selfed individuals in the population (Θ), which is assumed to remain close to its equilibrium value Θ^*. We look for *Evolutionarily Stable Strategies* (ESS, Maynard Smith and Price, 1973), that is situations where no mutant allele m may invade the population and replace the resident allele M.

Allelic frequencies change. To leading order in ε, we can express the change in frequency of allele m between two timesteps (Δp_m) as

$$\Delta p_m = \frac{\varepsilon}{2e_0}\Big(p_m\left(1 - p_m\right) + D_{m,m}\Big)V + o(\varepsilon^2), \tag{3}$$

with $V = 1 - S\left(1 - \Theta\delta_a\right)\left(1 + (x-1)\, e_0^x\right)$. Using a separation of timescales approximation (Kirkpatrick et al., 2002), that is assuming the deviation in homozygosity at the modifier rapidly reaches a quasi-equilibrium value as compared to allelic frequencies, we show in Appendix II that $D_{m,m} \geqslant 0$, as expected at a locus under directional selection in a partially selfing population. Thus, the first term in Equation (3) is always of the sign of ε, and only V matters for the determination of the equilibrium.

Evolutionarily Stable Strategy. In order to determine the equilibrium reproductive effort e^*, we plug Equation (1) into V, and solve $V = 0$ for e_0, which yields

$$e^* = \left[\frac{\mathcal{B} + \sqrt{(-\mathcal{B})^2 + 4(1-S)(x-1)(1-\delta_a)[1 - SS(1-\delta_a)](1-\alpha\delta_j)^2}}{2S(x-1)(1-\delta_a)(1-\alpha\delta_j)}\right]^{\frac{1}{x}}, \tag{4}$$

with $\mathcal{B} = (1-S)(2-x)(1-\alpha\delta_j) - \delta_a\left[(1 - S(2-x))(1-\alpha\delta_j) - x\alpha(1-\delta_j)\right]$.

For this equilibrium to be stable, that is for Equation (4) to be an ESS, it is required that

$$\frac{\partial V}{\partial e} = x(1-x)e^{x-1}S(1-\Theta\delta_a) < 0. \tag{5}$$

One can see that when the survival *vs.* reproduction trade-off is convex or linear ($x \leqslant 1$), condition (5) is not fulfilled, which implies that $\Delta p_m \geqslant 0$. Thus, alleles increasing their bearer's reproductive effort are always favoured, and only annuality ($e^* = 1$) can evolve. On the other hand, when the trade-off is concave ($x > 1$), $\frac{\partial V}{\partial e} < 0$, Equation (4) is an ESS and perennial strategies can be maintained. This result is classical, and has been reached by numerous authors before (e.g. Schaffer, 1974; Bell, 1980; Zhang, 2000). Besides, Equation (4) is a decreasing function of S. That is, higher extrinsic mortality favours higher reproductive efforts: allocating resources to survival becomes less and less advantageous as extrinsic mortality increases (*i.e.* as S decreases), because individuals get more likely to die independently of the resources they spend on survival. Hence, our model also predicts the classical observation that annuals are more likely to evolve in more disturbed habitats, where extrinsic mortality is higher.

Assuming $x > 1$, that is a concave trade-off, deriving Equation (4) with respect to α yields

$$\frac{\partial e^*}{\partial \alpha} = \frac{\delta_a\,(1-\delta_j)\,e^*}{(1-\alpha\delta_j)\sqrt{(-\mathcal{B})^2 + 4(1-P)(x-1)(1-\delta_a)[1-S(1-\delta_a)](1-\alpha\delta_j)^2}} \geqslant 0. \tag{6}$$

Equation (6) shows that the ESS reproductive effort is an increasing function of the selfing rate α, as long as some selfed juveniles survive to maturity ($\delta_j \neq 1$), and adults suffer from inbreeding depression ($\delta_a \neq 0$). In other words, through its impact on adult survival, self-fertilisation favours evolution towards higher reproductive efforts, and hence shorter lifespans. This effect becomes stronger as adult inbreeding depression increases, because allocating resources to survival becomes less beneficial in selfed adults, and as juvenile inbreeding depression decreases, because it reduces the proportion of selfed individuals entering the adult population. Therefore, we show that self-fertilisation favours evolution of shorter lifespans.

2.2 Influence of lifespan on the evolution of self-fertilisation

We now study the influence of lifespan on the evolution of self-fertilisation, taking reproductive effort, *i.e.* lifespan, as a fixed parameter. We assume that the selfing rate of a given parent is entirely determined by a single biallelic locus. Alleles M and m, which are assumed to be codominant, code for selfing rates α_0 and $\alpha_0 + a$, respectively. Allele m is assumed to be a rare mutant with a weak effect (*i.e.* a is small). In this section, we do not need to make any assumption regarding the shape of the survival *vs* reproduction trade-off. Hence, the general $\mathcal{S}_o(e)$ notation will be used. Recursions are given in Appendix III. As in the previous section, we follow three variables: the frequency of the mutant allele (p_m), the deviation in homozygosity at the modifier locus as compared to the panmictic expectation ($D_{m,m}$), and the proportion of selfed individuals in the population (Θ), which is assumed to remain close to its equilibrium value (Θ^*, Equation (1)) when the mutant is rare. We look for the conditions under which allele m invades the population.

Allelic frequencies change. Plugging Equation (1) into the allelic frequencies change (Δp_m), yields, to leading order a,

$$\Delta p_m \approx -\frac{a\,(1-\alpha_0\delta_j)\,D_{m,m}\,(1-\mathcal{S}_o(e))}{2\,[\mathcal{S}_o(e)\,(1-\alpha_0)\,\delta_a + (1-\mathcal{S}_o(e))\,(1-\alpha_0\delta_j)]^2} \times T \tag{7}$$

with $T = [1-\mathcal{S}_o(e)\,(1+\delta_a)]\,[\mathcal{S}_o(e)\delta_a - (1-\mathcal{S}_o(e))\,(1-2\delta_j)]$.

Using the same arguments as in the previous section, we show in Appendix III that for all α, $D_{m,m} > 0$. Hence, the first term in Equation (7) is always negative, and only T matters for the determination of the equilibrium. Since T does not depend on the selfing rate, there is only two possible situations: either $T > 0$ and full outcrossing ($\alpha = 0$) is favoured, or $T < 0$ and full selfing evolves ($\alpha = 1$), similar to the findings of previous authors (e.g. Lande and Schemske, 1985). Solving $T < 0$ for δ_j, we have

$$T < 0 \;\Leftrightarrow \delta_j < \frac{1-\mathcal{S}_o(e)\,(1+\delta_a)}{2\,(1-\mathcal{S}_o(e))}, \tag{8}$$

which simplifies to $\delta_j < \frac{1}{2}$ in the annual case ($\mathcal{S}_o(e) = 0$). Otherwise, this threshold is a decreasing function of $\mathcal{S}_o(e)$ when $\delta_a > 0$. Hence, assuming lifespan is fixed, we find that the range of conditions under which self-fertilisation can evolve in a population decreases when lifespan increases, provided that inbreeding depression affects adult survival, in

agreement with previous results (Morgan et al., 1997). This result implies that even very weak adult inbreeding depression is sufficient to prevent evolution of self-fertilisation in long-lived species.

2.3 Joint evolution of lifespan and self-fertilisation

Since we showed that only full selfing ($\alpha = 1$) and full outcrossing ($\alpha = 0$) are evolutionarily stable no matter the individuals' lifespan in the considered population, and since evolution of self-fertilisation is likely to be irreversible (e.g. Igic and Busch, 2013), we focus on the case of an initially outcrossing population ($\alpha = 0$). In such a population, from Equation (4), the evolutionarily stable reproductive effort simplifies to

$$e_o^* = \left(\frac{1-S}{S(x-1)}\right)^{\frac{1}{x}}. \tag{9}$$

Therefore, using Equations (2), (8) and (9), the threshold juvenile inbreeding depression for the evolution of self-fertilisation becomes, assuming $x > 1$,

$$\delta_j < \frac{1}{2}\left[1 + \frac{(1 - x\ S)\,\delta_a}{x\,(1-S)}\right]. \tag{10}$$

Above this threshold, the population remains outcrossing and stabilises at the reproductive effort e_o^* (Equation (9)), while below it, it becomes fully self-fertilising and stabilises at the following reproductive effort (from Equation (4)):

$$e_s^* = \left(\frac{1 - S\,(1-\delta_a)}{S\,(1-\delta_a)\,(x-1)}\right)^{\frac{1}{x}}. \tag{11}$$

Let us define the life expectancy ($\mathcal{L}$) of an individual, given its survival probability to maturity ($\mathcal{P}_j$) and its survival probability between mating events ($\mathcal{P}_a$), as

$$\mathcal{L} = \mathcal{P}_j\,(1-\mathcal{P}_a)\sum_{n=0}^{\infty}(n+1)\mathcal{P}_a^n = \frac{\mathcal{P}_j}{1-\mathcal{P}_a}. \tag{12}$$

In a fully outcrossing population, offspring do not suffer from inbreeding depression, and we have $\mathcal{P}_j = 1$. Using Equations (2) and (9) to compute $\mathcal{P}_a$, the life expectancy of a given individual ($\mathcal{L}_o$) is:

$$\mathcal{L}_o = \frac{x-1}{x(1-S)}, \tag{13}$$

In a fully selfing population, all individuals suffer from inbreeding depression. Therefore $\mathcal{P}_j = 1 - \delta_j$, and, using Equations (2) and (11), the life expectancy of a given individual ($\mathcal{L}_s$) is:

$$\mathcal{L}_s = \frac{(x-1)(1-\delta_a)(1-\delta_j)}{x(1-S) + [1 - x(1-S)]\delta_a}. \tag{14}$$

For the sake of clarity, let us define annuals as species living for less than two flowering seasons on average ($\mathcal{L} < 2$), and distinguish between short-lived perennials ($2 \leqslant \mathcal{L} \leqslant 9$) and long-lived perennials ($\mathcal{L} \geqslant 10$). Figure 2 presents evolutionary outcomes for various levels of extrinsic mortality, starting from an outcrossing population. Under high extrinsic mortality conditions ($S = 0.5$, Fig. 2a), only annuals ($\mathcal{L} < 2$) persist and the threshold inbreeding depression for the evolution of self-fertilisation is simply $\delta_j < \frac{1}{2}$. Under moderate extrinsic mortality conditions, outcrossing, short-lived perennials can be maintained ($S = 0.75$ and $S = 0.85$, Fig. 2b and 2c). The transition to self-fertilisation is much less likely, and is in most cases associated with a shift to annuality. Under low extrinsic mortality conditions ($S = 0.95$, Figure 2d), long-lived perennials are maintained and the evolution of self-fertilisation becomes very unlikely. It is associated with a lifespan reduction of a greater magnitude than in short-lived perennials, though annuality is not reached. In every case, transition to self-fertilisation is associated with lifespan reduction, even when very low inbreeding depression is required for it to happen.

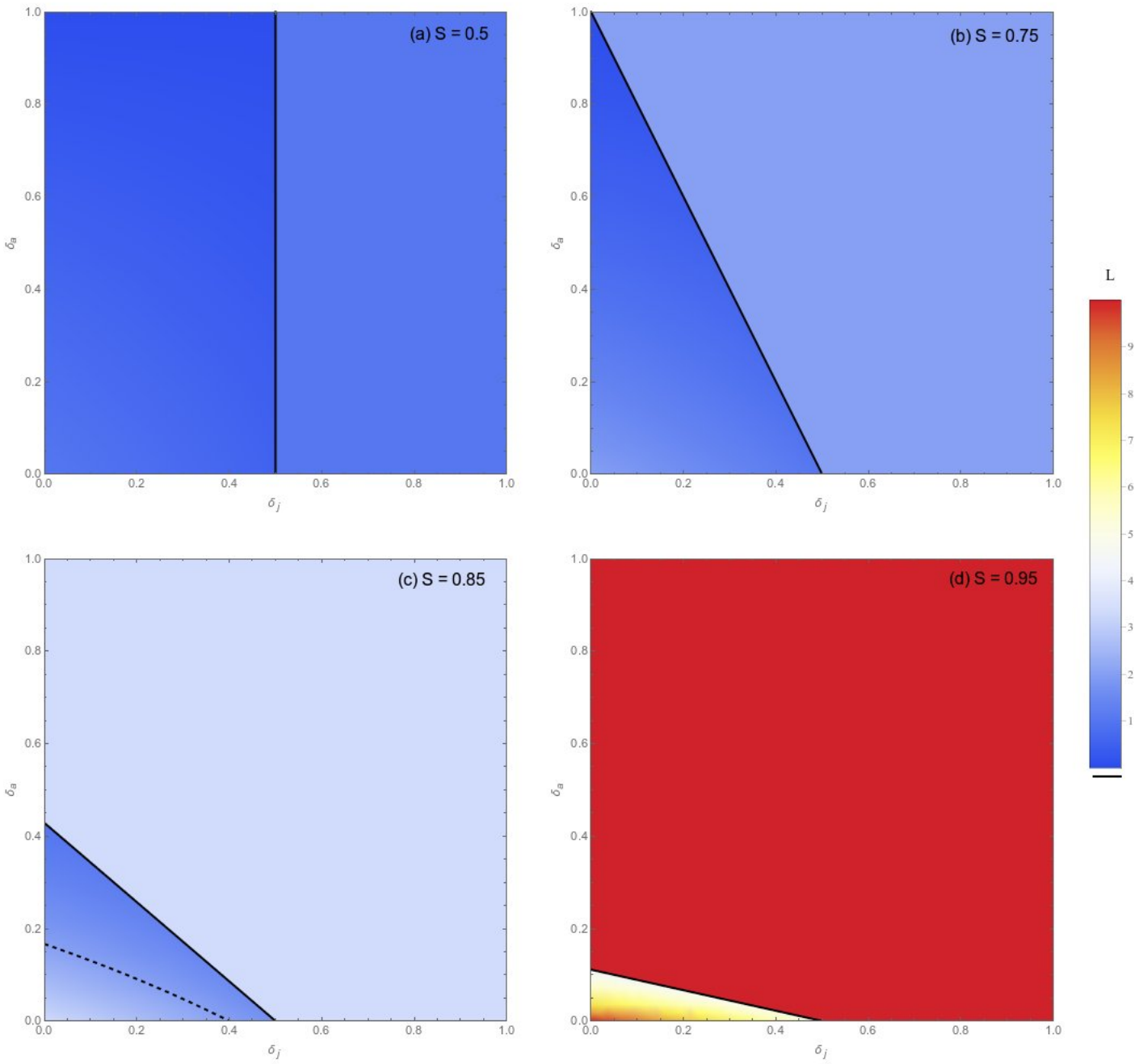

Figure 2: Evolutionary outcomes starting from an outcrossing population for various extrinsic mortality conditions. All results presented here assume $x = 2$. Y-axis is adult inbreeding depression (δ_a), and X-axis is juvenile inbreeding depression (δ_j). The solid line corresponds to the threshold inbreeding depression condition below which selfing evolves. The dashed line corresponds to the limit we defined between annuals ($\mathcal{L} < 2$) and short-lived perennials. The color gradient depicts the equilibrium life expectancy in the population.

3 Discussion

In this paper, we built modifier models to investigate the joint evolution of lifespan and mating system. To the best of our knowledge, this is the first time modifier models are used to study a population with overlapping generations. In agreement with previous authors, we found that increasing lifespan considerably reduced the range of conditions under which self-fertilisation can evolve (Morgan et al., 1997). Conversely, we showed that self-fertilisation is expected to cause evolution towards shorter lifespans due to inbreeding depression affecting adult survival, even under the low inbreeding depression conditions required for selfing to evolve in long-lived species. Overall, our results agree with the well-documented empirical association of short lifespans with selfing, and long lifespans with outcrossing (Munoz et al., 2016).

The only previous study of the influence of the mating system on the evolution of lifespan is that of Zhang (2000). While our main conclusions are in line with theirs, they also differ in a number of ways. Zhang (2000) concluded that self-fertilisation could induce evolution of shorter lifespans through increased allocation to female reproduction, without any role for adult inbreeding depression, provided that female reproduction is sufficiently costly, that inbreeding depression is low and that juvenile survivorship is constrained within a narrow range of values. Zhang (2000)'s results and ours are not mutually exclusive, since they rely on different mechanisms. However, we expect our prediction to apply more generally, as it only requires adult inbreeding depression to affect survival to apply, which seems reasonable, as inbreeding depression commonly occurs over all stages of life (Husband and Schemske, 1996).

Zhang (2000)'s approach and ours also differ widely in the methods used. While in our model, investing more or less resources into reproduction directly affects the probability to remain in the population, and therefore to carry out more mating events, Zhang (2000) model adult survival as an additive term (see Equation (3) in their study). In our opinion, this way of modelling survival does not incorporate the fact that surviving not only allows to bring one's own gene copies to the next flowering season, but also to carry out more mating events, and therefore merely depicts survival as a poor alternative to reproduction for gene transmission to the next flowering season. This implies that the survival *vs.*

reproduction trade-off is modelled incorrectly. In Appendix IV, we present an alternative approach based on a phenotypic model, by which conclusions similar to those we reach in the present study can be obtained.

Overall, both theoretical and empirical results indicate that predominantly selfing species are almost always short-lived, while predominantly outcrossing ones are mostly long-lived. Therefore, lifespan could act as a confounding factor when considering the joint evolution of self-fertilisation with other traits. For example, lifespan shortening following the transition to self-fertilisation could in part be responsible for the emergence of the selfing syndrome, rather than self-fertilisation *per se*. Indeed, as a shorter lifespan implies that individuals have to complete their cycle more rapidly, they could grow smaller flowers regardless of an adaptation to more efficient selfing (Sicard and Lenhard, 2011).

Accounting for lifespan could also shed new light on some long-standing evolutionary questions related to the evolution of mating systems. For instance, lifespan could influence the joint evolution of dispersal and self-fertilisation in two ways. First, increased lifespan induces higher local relatedness (Duputié and Massol, 2013), and perennials tend to occupy more saturated, competitive environments. Hence, kin competition should be greater in more long-lived species and long-distance dispersal could be favoured as a mean to avoid it. Since perennials outcross more than annuals, this could generate an indirect association between long-distance dispersal and outcrossing through lifespan. Second, the repeated effect of adult inbreeding depression considerably increases the consequences of mating among relatives in perennials. Long-distance dispersal and outcrossing could thus be favoured jointly in such species as an inbreeding avoidance strategy (Auld and Rubio de Casas, 2012).

Throughout this work, we assumed fixed inbreeding depression. Inbreeding depression is generally thought to be caused by recessive mildly deleterious mutations segregating at low frequencies in populations (Charlesworth and Willis, 2009). The population genetics of such mutations in populations with overlapping generations are poorly understood theoretically. Evidence from large-scale meta-analyses suggest that the measured magnitude of inbreeding depression increases as species' lifespan increases (Duminil et al., 2009; Angeloni et al., 2011). However, it is unclear whether this pattern is due to mating system differences between long-lived and short-lived species (Munoz et al., 2016), or to

lifespan. Additionally, empirical studies of inbreeding depression in perennials are rather scarce, and rarely span over several years, let alone individuals' entire lives (Husband and Schemske, 1996). Consequently, the quantities measured in such studies are not likely to depict inbreeding depression in its classic definition, that is the lifetime fitness decrease of selfed individuals as compared to outcrossed ones (Charlesworth and Charlesworth, 1987), but rather its magnitude at a given timestep or stage. Therefore, estimates in short-lived and long-lived species may not be readily comparable, and higher inbreeding depression levels reported in perennials could in part reflect measurement biases (Angeloni et al., 2011). Lifespan may also interact with the mutation load in non-trivial ways. On one hand, longer lifespan may increase selection against deleterious mutations, because of the increased number of opportunities for selection to occur, thereby leading to lower levels of inbreeding depression through better purging (Morgan, 2001). On the other hand, more long-lived species may endure significantly more mitotic mutations throughout their lives owing to their overall larger stature, which could result in an increase in inbreeding depression as plants do not have a separated germline (Scofield and Schultz, 2006). Furthermore, perennials may experience reduced purging of mutations affecting juvenile fitness, as some of these mutations would remain as neutral mutations among adults, and be recurrently reintroduced in the population through reproduction (Abu Awad et al., 2016).

Importantly, these various predictions stem from vastly different approaches, and remain mostly verbal. In particular, the rare models that considered populations with overlapping generations vary considerably in terms of the life stage (e.g. juvenile survival, reproductive output, post-breeding survival...) they assume deleterious mutations to affect. Indeed, while some authors assume they only act on juvenile survival or gametes production (Abu Awad et al., 2016), others assume they affect their bearers' survival throughout their lives (Morgan, 2001). As for the accumulation and transmission of somatic mutations (Scofield and Schultz, 2006), the population-level consequences of this mechanism were never investigated theoretically. Besides, no study has yet considered the interaction between separate loads affecting different life stages, although these situations are likely to occur since differential purging has been reported between life stages (Angeloni et al., 2011). Finally, every theoretical study so far has assumed individuals' fecundities and survivorship to not depend upon their age, which is a strong simplifying

assumption (Franco and Silvertown, 1996; Petit and Hampe, 2006). In the future, significant insight for the evolution of mating systems and life-histories is to be gained through investigations of the dynamics of mutation loads in perennials.

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APPENDIX I

Proportion of selfed individuals and lifetime inbreeding depression

In this section, we detail the derivation of the equilibrium proportion of selfed individuals in the population, and show that its decrease when longevity increases is attributable to stronger selection against inbred individuals.

Proportion of selfed individuals. Following reproduction, adult individuals survive with probability $\mathcal{S}_o(e)$ if they were produced by outcrossing, and $(1-\delta_a)\,\mathcal{S}_o(e)$ if they were selfed. Therefore, denoting Θ the proportion of selfed individuals in the population at a given timestep, the proportion of adult individuals surviving between two mating events ($\bar{\mathcal{S}}$) is given by

$$\bar{\mathcal{S}} = \mathcal{S}_o(e)\left[\Theta\,(1-\delta_a) + 1 - \Theta\right], \tag{A1}$$

and the proportion of selfed individuals among them, Θ^s is

$$\Theta^s = \frac{\Theta\,(1-\delta_a)}{\Theta\,(1-\delta_a) + 1 - \Theta}. \tag{A2}$$

Among the juveniles settling in the population at a given mating event, the proportion of selfed individuals (Θ^j) given the selfing rate α can be expressed as

$$\Theta^j = \frac{\alpha(1-\delta_j)}{\alpha(1-\delta_j) + 1 - \alpha}. \tag{A3}$$

Hence, the proportion of selfed individuals at the next timestep (Θ') is

$$\Theta' = \bar{\mathcal{S}}\;\Theta^s + \left(1-\bar{\mathcal{S}}\right)\Theta^j, \tag{A4}$$

and, solving $\Delta\Theta = \Theta' - \Theta = 0$, we obtain the equilibrium proportion of selfed individuals in the population, Θ^* :

$$\Theta^* = \frac{\alpha\,(1-\delta_j)\,(1-\mathcal{S}_o(e))}{\alpha\,(1-\delta_j)\,(1-\mathcal{S}_o(e)) + (1-\alpha)\,\delta_a\mathcal{S}_o(e)}. \tag{A5}$$

Lifetime inbreeding depression. In our model, inbreeding depression only affects survival, in juveniles and in adults. Thus, the decrease in fitness selfed individuals suffer from in comparison with the outcrossed throughout their lives, and not only between

two mating events (*i.e.* lifetime inbreeding depression) can be expressed in terms of life expectancies. Using Equation (12), we obtain the following life expectancies

$$\mathcal{L}_s = \frac{1-\delta_j}{1-\mathcal{S}_o(e)\,(1-\delta_a)} \quad \text{and,} \quad \mathcal{L}_o = \frac{1}{1-\mathcal{S}_o(e)}, \tag{A6}$$

for selfed ($\mathcal{L}_s$) and outcrossed ($\mathcal{L}_o$) individuals, respectively, and lifetime inbreeding depression can be expressed as

$$\bar{\delta} = 1 - \frac{\mathcal{L}_s}{\mathcal{L}_o} = 1 - \frac{(1-\mathcal{S}_o(e))\,(1-\delta_j)}{1-\mathcal{S}_o(e)\,(1-\delta_a)}. \tag{A7}$$

Equation (A7) is an increasing function of $\mathcal{S}_o(e)$, that is selection against selfed individuals grows stronger as longevity increases. This is due to the repeated effect of adult inbreeding depression on post-breeding survival.In the annual case ($\mathcal{S}_o(e) = 0$), Equation (A7) reduces to $\bar{\delta} = \delta_j$. Interestingly, Equation (A7) relates to Θ^* (Equation (A5)) in the following way:

$$\Theta^* = \frac{\alpha\left(1-\bar{\delta}\right)}{\alpha\left(1-\bar{\delta}\right)+1-\alpha}. \tag{A8}$$

Therefore, the equilibrium proportion of selfed individuals in the population decreases when generations overlap (that is, $\mathcal{S}_o(e)$) increases, due to stronger selection against selfed individuals owing to the repeated effect of adult inbreeding depression on adult survival.

APPENDIX II

Recursions for the evolution of reproductive effort in a partially selfing population

In this section, we detail the mathematical derivations leading to the ESS reproductive effort expression we obtain. The selfing rate is fixed and reproductive effort is controlled by a single modifier locus. To describe the changes happening in the population between two timesteps, we use the theoretical framework first described by Barton and Turelli (1991) and generalized by Kirkpatrick et al. (2002). We follow the variation of three variables, namely, the frequency (p_m) of the mutant allele, which is assumed to be a rare with a small effect (ϵ) on its bearer's reproductive effort, the excess in homozygosity at the modifier locus ($D_{m,m}$), and the proportion of selfed individuals in the population (Θ).

We define the indicator variables X and $\dot{X}$, corresponding to the two allelic positions of the modifier locus located on the paternally and maternally inherited chromosomes, respectively. These variables can take two values, 1 if the mutant allele (m) is present at the considered position, and 0 otherwise. Since there is no maternal or paternal effect on the expression of the alleles at the modifier, we have:

$$\mathbb{E}[X_m] = \mathbb{E}[\dot{X}_m] = p_m. \tag{A9}$$

Using these indicator variables, we may define the centered variables ζ_m and $\dot{\zeta}_m$ as follows:

$$\begin{cases} \zeta_m &= X_m - p_m \\ \dot{\zeta}_m &= \dot{X}_m - p_m \end{cases} \tag{A10}$$

which allows us to define the excess in homozygotes in the population as compared to the panmictic expectation ($D_{m,m}$) as:

$$D_{m,m} = \mathbb{E}[\zeta_{m,m}] = \mathbb{E}[X_m \dot{X}_m] - p_m^2. \tag{A11}$$

Reproduction Using indicator variables, the reproductive effort of a given individual, e, can be expressed as follows

$$e = e_0 + \frac{\varepsilon}{2}\left(X_m + \dot{X}_m\right) = e_0 + \varepsilon\, p_m + \frac{\varepsilon}{2}\left(\zeta_m + \dot{\zeta}_m\right). \tag{A12}$$

The average reproductive effort is thus

$$\bar{e} = \mathbb{E}[e] = e_0 + \varepsilon\, p_m, \tag{A13}$$

which yields, to leading order in ε, the relative contribution of a given individual to reproduction ($\tilde{e}$) during a given mating event

$$\tilde{e} = \frac{e}{\bar{e}} \approx 1 + \frac{\varepsilon}{2e_0}\left(\zeta_m + \dot{\zeta}_m\right). \tag{A14}$$

Frequency of the mutant. Using Equation (A14), the frequency of the mutant allele (p_m^j) among juveniles following reproduction is

$$p_m^j = \mathbb{E}\left[\tilde{e}\ \frac{X_m + \dot{X}_m}{2}\right] = \frac{1}{2}\mathbb{E}\left[\tilde{e}\ \left(\zeta_m + \dot{\zeta}_m + 2p_m\right)\right] = p_m + \frac{\varepsilon}{2e_0}\left[p_m(1-p_m) + D_{m,m}\right] \tag{A15}$$

Excess in homozygotes. The excess in homozygotes among the offspring is only produced among the selfed offspring, since mating is random otherwise. Hence, we may express it as

$$D_{m,m}^j = \Theta^j\ \mathbb{E}\left[\frac{1}{4}(X_m^j - p_m^j)^2 + \frac{1}{2}(X_m^j - p_m^j)(\dot{X}_m^j - p_m^j) + \frac{1}{4}(\dot{X}_m^j - p_m^j)^2\right], \tag{A16}$$

where Θ^j is the proportion of selfed individuals among the offspring (Equation (A3)). To leading order in ε and assuming the mutant is rare (i.e. p_m is of order ϵ), Equation (A16) simplifies to

$$D_{m,m}^j = \frac{\Theta^j}{2}\left(1 - \frac{\varepsilon}{2e_0}\right)\left(p_m(1-p_m) + D_{m,m}\right) + o\left(\varepsilon^2\right). \tag{A17}$$

Survival We denote by $\mathcal{S}$ the probability of survival of a parent taken at random in the parental population. Using our indicator variables, and given the proportion Θ of selfed individuals in the population, the probability of survival is

$$\mathcal{S} = \Theta\ (1-\delta_a)\,\mathcal{S}_o(e) + (1-\Theta)\mathcal{S}_o(e) = S\left[1 - \left(e_0 + \frac{\varepsilon}{2}\left(X_m + \dot{X}_m\right)\right)^x\right](\Theta\,(1-\delta_a) + 1 - \Theta). \tag{A18}$$

Substituting indicator variables with ζ-variables and assuming that ϵ and p_m are small, we obtain, to leading order,

$$\mathcal{S} = S\,(1 - \Theta\ \delta_a)\left[1 - {e_0}^x - \frac{x\ \varepsilon\ {e_0}^{x-1}}{2}\left(\zeta_m + \dot{\zeta}_m\right)\right] + o\left(\varepsilon^2\right). \tag{A19}$$

Thus, the mean survival probability is

$$\bar{S} = \mathbb{E}\left[\mathcal{S}\right] \approx S\,(1 - \Theta\ \delta_a)\left[1 - {e_0}^x\right], \tag{A20}$$

and the relative survival probability ($\tilde{\mathcal{S}}$) simplifies to

$$\tilde{\mathcal{S}} = \frac{\mathcal{S}}{\bar{\mathcal{S}}} \approx 1 - \frac{x\ \varepsilon\ {e_0}^{x-1}}{2\,(1-{e_0}^{x})}\left(\zeta_m + \dot{\zeta}_m\right). \tag{A21}$$

Frequency of the mutant. Using Equation (A21), the frequency of the mutant (p^s_m) among the surviving parents is

$$p^s_m = \mathbb{E}\left[\tilde{\mathcal{S}}\ \frac{X_m + \dot{X}_m}{2}\right] \approx p_m - \frac{x\ \varepsilon\ {e_0}^{x-1}}{2\,(1-{e_0}^{x})}\left(p_m\,(1-p_m) + D_{m,m}\right). \tag{A22}$$

Excess in homozygotes. Since only selection acts at this stage, the excess in homozygotes at the modifier locus among the parents ($D^s_{m,m}$) is given by

$$D^s_{m,m} = \mathbb{E}\left[(X^s_m - p^s_m)(\dot{X}^s_m - p^s_m)\right] \approx \mathbb{E}\left[\tilde{\mathcal{S}}\ \zeta^s_{m,m}\right] \approx D_{m,m}\left(1 - \frac{x\ \varepsilon\ {e_0}^{x-1}}{1-{e_0}^{x}}\right). \tag{A23}$$

Next timestep From our previously derived expressions, the frequency of the mutant (p'_m), the excess in homozygotes ($D'_{m,m}$) and the proportion of selfed individuals in the population (Θ') in the next timestep is

$$\begin{cases} p'_m = \bar{\mathcal{S}}\ p^s_m + (1-\bar{\mathcal{S}})\ p^j_m \\ D'_{m,m} = \bar{\mathcal{S}}\ D^s_{m,m} + (1-\bar{\mathcal{S}})D^j_{m,m} \\ \Theta' = \bar{\mathcal{S}}\ \Theta^s + (1-\bar{\mathcal{S}})\Theta^j. \end{cases}$$

In order to determine the *Evolutionary Stable Strategy* (ESS, Maynard Smith and Price, 1973) for the population given the parameters of the model, one has to determine the value of e_0 for which no mutant allele (m) may invade the population and replace the resident (M). To do so, we will consider the change in frequency of the mutant allele over one timestep (Δp_m), which can be expressed as

$$\Delta p_m = \frac{\varepsilon}{2e_0}\Big(p_m\,(1-p_m) + D_{m,m}\Big)V + o(\varepsilon^2), \tag{A24}$$

with $V = 1 - S\,(1-\Theta\delta_a)\,(1+(x-1)\,{e_0}^{x})$.

Separation of timescales approximation When selection is weak (ε is small), we may assume that the excess in homozygotes in the population reaches a value close to

equilibrium much faster than the allelic frequencies. Thus, assuming the mutant is rare (p_m is of order ε) we obtain, to second order in ε :

$$D^*_{m,m} = \frac{\alpha(1-\delta_j)p_m}{2-\alpha(1+\delta_j)}\Bigg[1 + \frac{\varepsilon}{(2-\alpha(1+\delta_j))\, e_0(1-{e_0}^x)(1-\bar{\mathcal{S}})} \times \Big((1-\bar{\mathcal{S}})(1-{e_0}^x)(1-\alpha\delta_j - 2(1-\alpha)) - \bar{\mathcal{S}}\ 2x{e_0}^x(1-\alpha\delta_j)\Big)\Bigg] + o(\varepsilon^2), \tag{A25}$$

Since we have $D^*_{m,m} \geqslant 0$ (Equation (A25)), the first term in Equation (A24) is always positive, and only V matters for the determination of the equilibrium.

Evolutionarily Stable Reproductive Effort Injecting Equation (A5) into Equation (A24), and solving $\Delta p_m = 0$ for e_0 yields the following ESS for the reproductive effort (e^*) :

$$e^* = \left[\frac{\mathcal{B} + \sqrt{(-\mathcal{B})^2 + 4\,(1-S)\,(x-1)\,(1-\delta_a)\,[1-\delta_a\,(1-S)]\,(1-\alpha\delta_j)^2}}{2S\,(x-1)\,(1-\delta_a)\,(1-\alpha\delta_j)}\right]^{\frac{1}{x}} \tag{A26}$$

with $\mathcal{B} = (1-S)\,(2-x)\,(1-\alpha\delta_j) + \delta_a\,[\alpha x\,(1-\delta_j) - [1-S\,(2-x)]\,(1-\alpha\delta_j)]$.

APPENDIX III

Recursions for the evolution of self-fertilisation in a perennial population

In this section, we detail the mathematical derivations for the evolution of self-fertilisation in a perennial population. Individuals reproduce by self-fertilisation at a rate given by their genotype at a single biallelic modifier locus, and by random mating otherwise. At the modifier, alleles M and m are assumed to be codominant, and code for selfing rates α_0 and $\alpha_0 + a$, respectively. Allele m is assumed to be a rare mutant with a weak effect (*i.e.* a is small). The theoretical framework we use is the same as in Appendix II.

Reproduction. Let us split the population into two groups: the *selfed* and the *outcrossed* individuals. The frequency of allele m in each of these groups are denoted $p_{m,s}$ and $p_{m,o}$, respectively, so that its frequency in the whole population is given by

$$p_m = \Theta\, p_{m,s} + (1 - \Theta)\, p_{m,o} \tag{A27}$$

where Θ is the proportion of selfed individuals in the population.

Frequency of the mutant among the selfed. The contribution of a given parent to the production of selfed offspring, α, is

$$\alpha = \alpha_0 + 2 \times \frac{a}{2}\left(X_m + \dot{X}_m\right) = \alpha_0 + a\left(X_m + \dot{X}_m\right), \tag{A28}$$

owing to the fact that increasing its selfing rate by $\frac{a}{2}$ induces a twofold transmission advantage in comparison with others (Fisher, 1941). Injecting ζ-variables into Equation (A28), we obtain the following expression for the relative contribution of a given parent to the production of offspring by self-fertilisation:

$$\tilde{\alpha} = \frac{\alpha}{\bar{\alpha}} = \frac{\alpha_0 + ap_m + a\left(\zeta_m + \dot{\zeta}_m\right)}{\alpha_0 + ap_m} = 1 + \frac{a}{\alpha_0 + ap_m}\left(\zeta_m + \dot{\zeta}_m\right). \tag{A29}$$

Thus, the frequency of allele m among the selfed offspring ($p^j_{m,s}$) is given by

$$p^j_{m,s} = \mathbb{E}\left[\widetilde{\alpha}\ \frac{X_m + \dot{X}_m}{2}\right] = p_m + \frac{a}{\alpha_0 + ap_m}\Big(p_m\,(1 - p_m) + D_{m,m}\Big). \tag{A30}$$

Frequency of the mutant among the outcrossed. The contribution of a given parent to the production of outcrossed offspring, o, is

$$o = 1 - \alpha_0 - \frac{a}{2}\left(X_m + \dot{X}_m\right), \tag{A31}$$

which yields the following expression for its relative contribution ($\widetilde{O}$):

$$\tilde{o} = 1 - \frac{a}{2\left(1 - \alpha_0 - ap_m\right)}\left(\zeta_m + \dot{\zeta}_m\right). \tag{A32}$$

Hence, the frequency of allele m among the outcrossed offspring ($p^j_{m,o}$) is

$$p^j_{m,o} = \mathbb{E}\left[\tilde{o}\ \frac{X_m + \dot{X}_m}{2}\right] = p_m - \frac{a}{2\left(1 - \alpha_0 - ap_m\right)}\Big(p_m\left(1 - p_m\right) + D_{m,m}\Big). \tag{A33}$$

Excess in homozygotes. Considering the whole offspring pool, we may neglect the effect of the mutant on the selfing rate. Thus, we may express the excess in homozygotes at the modifier among juveniles as

$$D^j_{m,m} \approx \frac{\Theta^j}{2}\Big(p_m\left(1 - p_m\right) + D_{m,m}\Big), \tag{A34}$$

where Θ^j is the proportion of selfed individuals among the juveniles settling in the population (Equation (A3)).

Survival. Among the parents, allelic frequencies among the selfed and among the outcrossed do not vary, because there is no direct selection acting on the modifier among them. Therefore,

$$p^s_{m,o} = p_{m,o} \quad \text{and} \quad p^s_{m,s} = p_{m,s}. \tag{A35}$$

Moreover, we have

$$D^s_{m,m} = D_{m,m}. \tag{A36}$$

Selfed individuals are however counterselected due to adult inbreeding depression. Thus, their proportion varies according to Equation (A2).

Next timestep. In the next timestep, assuming the proportion of selfed individuals remains close to its equilibrium value (Θ^*, Equation (A5)), the frequency of the mutant

$(p_m{}')$ and the excess in homozygotes $(D_{m,m}{}')$ are given by

$$\begin{cases} p_m{}' = \bar{\mathcal{S}}\ p_m^s + (1-\bar{\mathcal{S}})\ p_m^j \\ D_{m,m}{}' = \bar{\mathcal{S}}\ D_{m,m}^s + (1-\bar{\mathcal{S}}) D_{m,m}^j, \end{cases} \tag{A37}$$

where $\bar{\mathcal{S}} = \mathcal{S}_o(e)\,[\Theta^*\ \ (1-\delta_a) + 1 - \Theta^*]$ is the proportion of parents surviving until the next timestep. Using these recursions, we may express the change in allelic frequencies at the modifier (Δp_m) as

$$\Delta p_m = -\frac{a\,(1-\alpha_0\delta_j)\,D_{m,m}\,(1-\mathcal{S}_o(e))}{2\,[\mathcal{S}_o(e)\,(1-\alpha_0)\,\delta_a + (1-\mathcal{S}_o(e))\,(1-\alpha_0\delta_j)]^2} \times T \tag{A38}$$

with $T = [1-\mathcal{S}_o(e)\,(1+\delta_a)]\,[\mathcal{S}_o(e)\delta_a - (1-\mathcal{S}_o(e))\,(1-2\delta_j)]$.

Separation of timescales approximation. Assuming homozygosity equilibrates quickly in comparison with allelic frequencies at the modifier, we obtain a quasi-equilibrium expression (Kirkpatrick et al., 2002) for the excess in homozygotes at the modifier $(D^*_{m,m})$ by solving $D'_{m,m} - D_{m,m} = 0$,

$$D^*_{m,m} = p_m\,(1-p_m)\,\frac{\alpha_0\,(1-\delta_j)}{2-\alpha_0\,(1+\delta_j)} \geqslant 0. \tag{A39}$$

Using Equation (A39), one can see that the first term in Equation (A38) is always negative, and only T matters for the determination of the equilibria. Because T does not depend on α_0, there is only two situations: either $T > 0$ and full outcrossing is maintained $(\alpha^* = 0)$, or $T < 0$ and full selfing is favoured $(\alpha^* = 1)$. Hence, by solving $T < 0$, we obtain the following threshold for the evolution of self-fertilisation:

$$\delta_j < \frac{1-(1+\delta_a)\,\mathcal{S}_o(e)}{2\,(1-\mathcal{S}_o(e))} \tag{A40}$$

APPENDIX IV

Phenotypic approach to the evolution of self-fertilisation and the evolution of lifespan.

In this section, we derive a phenotypic approach to the evolution of self-fertilisation in a perennial population, and to the evolution of longevity in a partially selfing population. We express the fitness of the mutant as its *lifetime* reproductive success.

Evolution of longevity. All individuals have the same reproductive effort e during each mating event they participate in. Therefore, an individual's fitness (W), given its life expectancy ($\mathcal{L}$), is given by

$$W = \mathcal{L} \times e. \tag{A41}$$

With probability α, an individual is produced by self-fertilisation and its life expectancy ($\mathcal{L}_s$) is

$$\mathcal{L}_s = \frac{1-\delta_j}{1-(1-\delta_a)\,\mathcal{S}_o(e)}, \tag{A42}$$

while with probability $1-\alpha$, it is outcrossed, and its life expectancy ($\mathcal{L}_o$) is given by

$$\mathcal{L}_o = \frac{1}{1-\mathcal{S}_o(e)}, \tag{A43}$$

with $\mathcal{S}_o(e) = S\,(1-e^x)$. Therefore, we have

$$W = \Big(\alpha\ \mathcal{L}_s + (1-\alpha)\,\mathcal{L}_o\Big)e. \tag{A44}$$

Deriving Equation (A44) once with respect to e, we obtain

$$\frac{\partial W}{\partial e} = \frac{1-\alpha}{1-S\,(1-e^x)}\left[1-\frac{xSe^x}{1-S\,(1-e^x)}\right]+\frac{\alpha\,(1-\delta_j)}{1-S\,(1-\delta_a)\,(1-e^x)}\left[1-\frac{xS\,(1-\delta_a)\,e^x}{1-S\,(1-\delta_a)\,(1-e^x)}\right]. \tag{A45}$$

Finally, solving $\frac{\partial W}{\partial e} = 0$ for e, we obtain a high order polynomial expression for the equilibrium reproductive effort. In cases where $\alpha = 0$ and $\alpha = 1$, it reduces to

$$e_o^* = \left(\frac{1-S}{S(x-1)}\right)^{\frac{1}{x}} \quad \text{and} \quad E_s^* = \left(\frac{1-S\,(1-\delta_a)}{S\,(1-\delta_a)\,(x-1)}\right)^{\frac{1}{x}}, \text{ respectively,} \tag{A46}$$

which corresponds to Equations (9) and (11). Although its graphical behaviour is similar to that of the prediction we obtained in our main model (Figure A1, the analytical properties of this solution cannot be studied because of its complexity. Its stability cannot be easily

studied analytically either, because the second derivative of the fitness with respect to e is too complicated. It can however be assessed graphically. This highlights the interest of using modifier models rather than a classical phenotypic approach for the study of populations with overlapping generations: it allows one to neglect inconsequential terms in order to obtain understandable solutions.

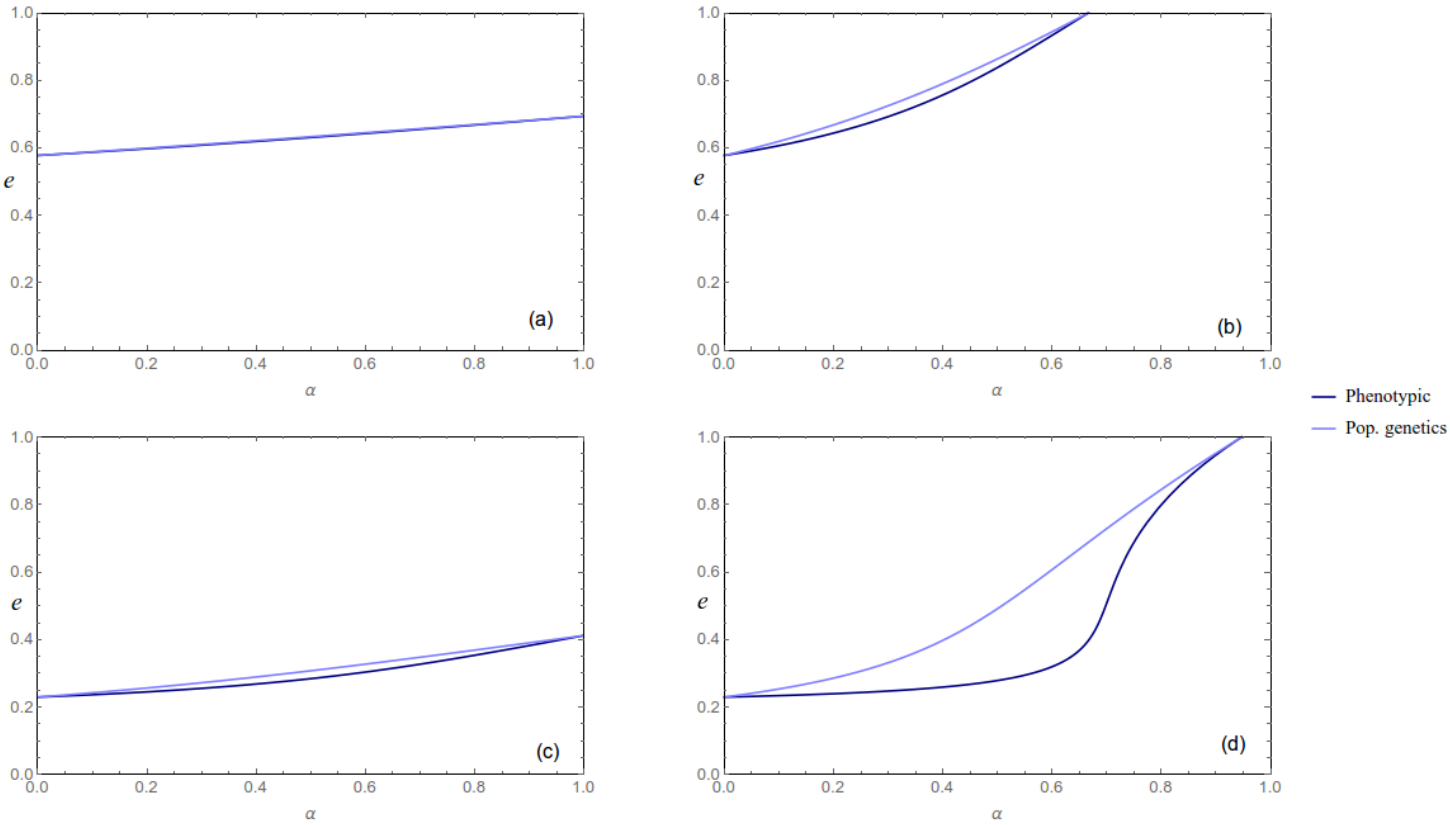

Figure A1: ESS reproductive effort is presented as a function of the selfing rate, in mild extrinsic mortality conditions ($S = 0.75$, Figures (a) and (b)), and in low extrinsic mortality conditions ($S = 0.95$, Fig. (c) and (d)), with low ($\delta_a = 0.1$, Fig. (a) and (c)) and high ($\delta_a = 0.1$, Fig. (b) and (d)) adult inbreeding depression. The analytical expression we obtain with our main model is presented in light blue. The one we obtain with our phenotypic approach is presented in dark blue.

Evolution of self-fertilisation. Using the same approach as for the evolution of lifespan, we now study the influence of lifespan for the evolution of self-fertilisation. For that matter, we do not need to specify any trade-off between survival and reproduction. There-

fore, we will use the notation $\mathcal{S}_o(e)$ to denote survival probability, and fitness becomes

$$W = 2\ \alpha\ \frac{1-\delta_j}{1-(1-\delta_a)\,\mathcal{S}_o(e)}\ +\ (1-\alpha)\,\frac{1}{1-\mathcal{S}_o(e)}, \tag{A47}$$

where the 2α term stands for Fisher's transmission advantage (Fisher, 1941). The fitness of an individual taken at random in a fully outcrossing population (W_o) is given by

$$W_o = \frac{1}{1-\mathcal{S}_o(e)}. \tag{A48}$$

Such a population will be invaded by a self-fertilising mutant if

$$W_o < W \Leftrightarrow \delta_j < \frac{1-(1+\delta_a)\,\mathcal{S}_o(e)}{2\,(1-\mathcal{S}_o(e))}. \tag{A49}$$

Furthermore, if this condition is satisfied, we have

$$\frac{\partial W}{\partial \alpha} = \frac{2\,(1-\delta_j)}{1-(1-\delta_a)\,\mathcal{S}_o(e)} - \frac{1}{1-\mathcal{S}_o(e)} > 0. \tag{A50}$$

Therefore, only two evolutionarily stable strategies can exist, either $\alpha = 1$ if Condition (A49) is satisfied, and $\alpha = 0$ otherwise. These results completely match with those we obtained using our modifier model.

APPENDIX V

Numerical analyses.

In this section, numerical analyses results are presented along with our analytical predictions.

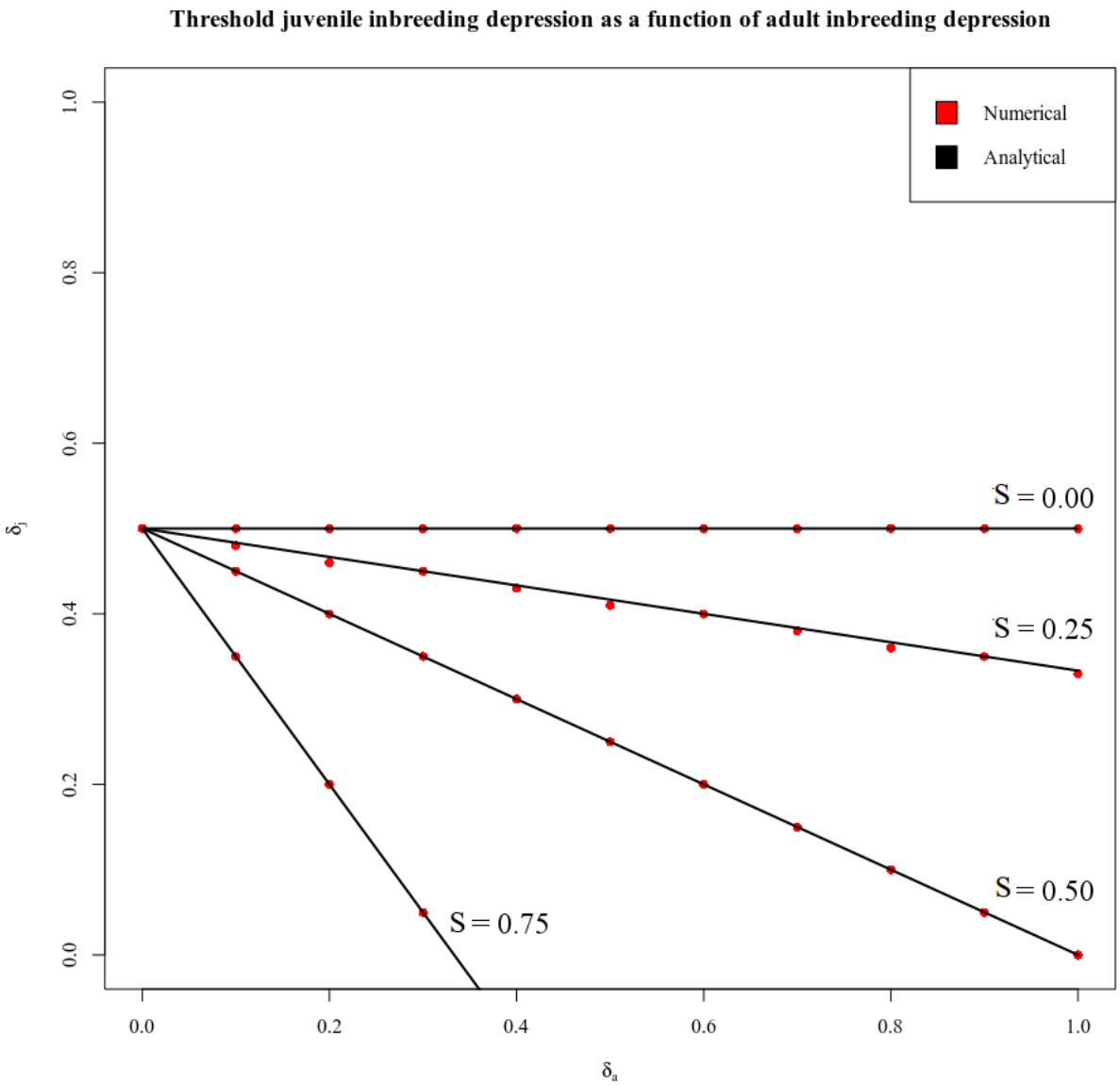

Figure A2: Numerical analyses results for the evolution of self-fertilisation. Threshold juvenile ID is presented as a function of adult ID, for various survival probabilities ($\mathcal{S}_o(e) = 0\ ; 0.25\ ; 0.5\ ; 0.75$).

For the evolution of self-fertilisation, the analysis was conducted starting from $\alpha_0 = 0$ and introducing mutants increasing the selfing rate. Good agreement was found between our analytical predictions and numerical analyses. Figure A2 shows some inbreeding depression threshold values obtained for various longevity situations. Either full selfing or strict outcrossing always evolved.

For the evolution of reproductive effort, two types of analyses were conducted: starting from $e_0 = 0$ and introducing mutants increasing reproductive effort (*upwards* analysis, presented in orange), and starting from $e_0 = 1$ and introducing mutants decreasing reproductive effort (*downwards* analysis, presented in blue). Part of the results are presented in Figure A3. Discrepancies between upwards and downwards analyses were observed in situations involving high adult inbreeding depression and low extrinsic mortality for intermediate selfing rates (Fig. A3b). Such situations are never reached in the context of the joint evolution of lifespan and selfing, because inbreeding depression is too high for selfing to evolve and intermediate selfing rates are never evolutionarily stable. Besides, good agreement was found between analytical predictions and numerical analyses in most cases, especially for selfing rates close to 0 or 1 (Fig. A3), which are the states that matter for the joint evolution of lifespan and selfing. Therefore, we considered our analytical prediction to satisfactorily agree with numerical analyses.

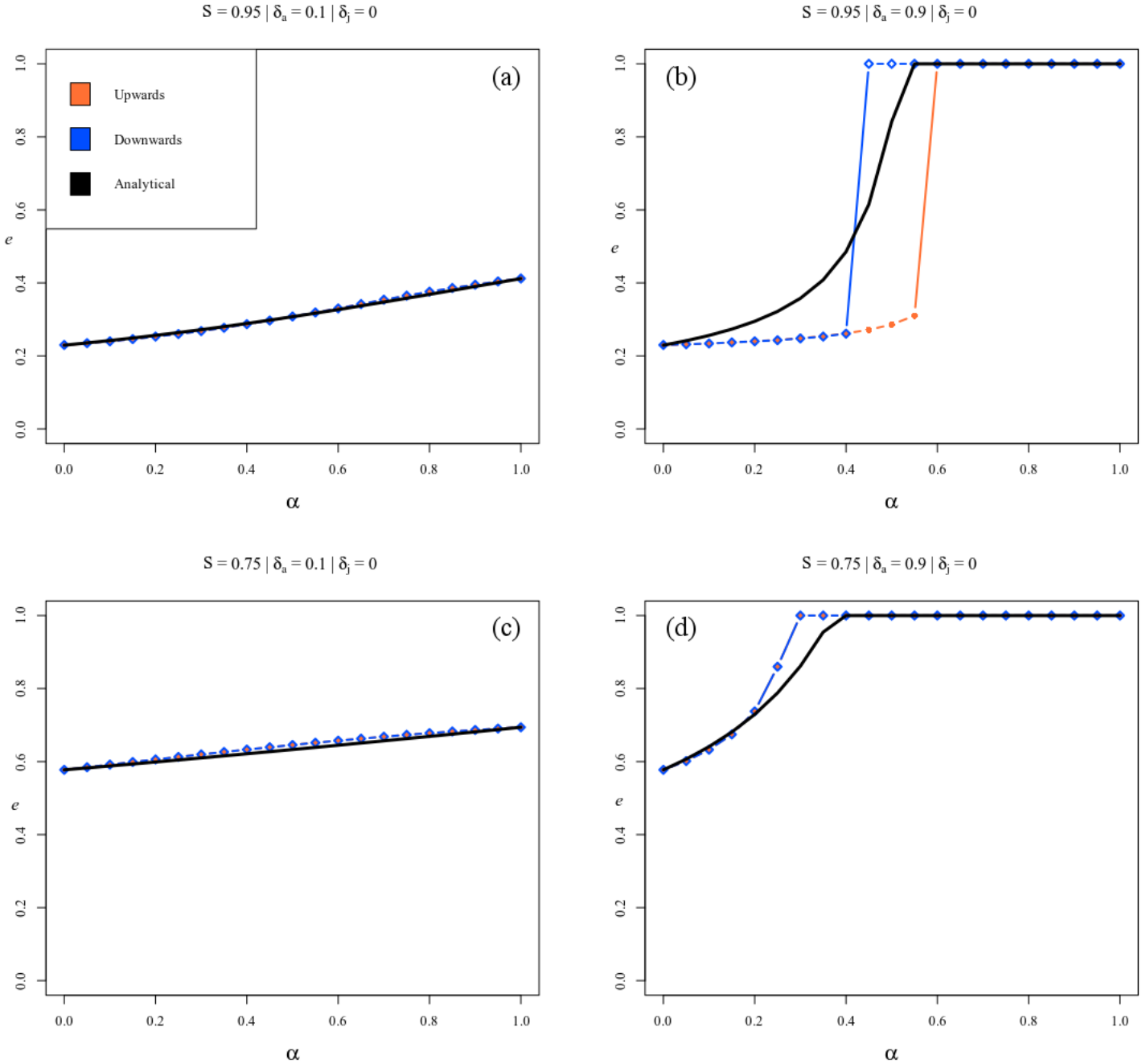

Figure A3: Numerical analyses results for the evolution of reproductive effort. ESS reproductive effort is presented as a function of the selfing rate, in low ($S = 0.95$, Fig. (a) and (b)) and mild ($S = 0.75$, Figures (c) and (d)) extrinsic mortality conditions, with low ($\delta_a = 0.1$, Fig. (a) and (c)) and high ($\delta_a = 0.9$, Fig. (b) and (d)) adult inbreeding depression. Numerical analyses are presented in orange (*upwards*) and blue (*downwards*). Analytical predictions are presented in black.