Greater strength of selection and higher proportion of beneficial amino acid changing

mutations in humans compared to mice and *Drosophila melanogaster*

Running title: Differences in adaptive evolution across species

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ABSTRACT

Quantifying and comparing the amount of adaptive evolution among different species is

key to understanding evolutionary processes. Previous studies have shown differences in

adaptive evolution across species; however, their specific causes remain elusive. Here, we use

improved modeling of weakly deleterious mutations and the demographic history of the outgroup

species and ancestral population and estimate that at least 20% of nonsynonymous substitutions

between humans and an outgroup species were fixed by positive selection. This estimate is much

higher than previous estimates, which did not correct for the sizes of the outgroup species and

ancestral population. Next, we directly estimate the proportion and selection coefficients (p^+ and

s^+, respectively) of newly arising beneficial nonsynonymous mutations in humans, mice, and

Drosophila melanogaster by examining patterns of polymorphism and divergence. We develop a

novel composite likelihood framework to test whether these parameters differ across species.

Overall, we reject a model with the same p^+ and s^+ of beneficial mutations across species, and

estimate that humans have a higher p^+s^+ compared to *D. melanogaster* and mice. We

demonstrate that this result cannot be caused by biased gene conversion or hypermutable CpG

sites. In summary, we find the proportion of beneficial mutations to be higher in humans than in

D. melanogaster or mice, suggesting that organismal complexity, which increases the number of

steps required in adaptive walks, may be a key predictor of the amount of adaptive evolution

within a species.

INTRODUCTION

Since the inception of molecular population genetics, there has been tremendous interest in quantifying the amount of adaptive evolution in different organisms. The neutral theory of molecular evolution postulated that beneficial mutations are rare, and that many of the substitutions between species are neutral (Kimura 1983). One early challenge to this theory originated from a comparison of polymorphisms and divergence at synonymous and nonsynonymous sites in *Drosophila* (Fay et al. 2002; Smith and Eyre-Walker 2002). Under models without positive selection, the ratio of nonsynonymous to synonymous changes should remain equal when comparing polymorphisms (*i.e.* differences within species) and divergence (*i.e.* differences between species). In contrast to this prediction, a genome-wide excess of nonsynonymous divergence between species was observed, a pattern indicative of an abundance of positive selection in *Drosophila*. More formally, Smith and Eyre-Walker (2002) proposed a statistic, α, which is the proportion of nonsynonymous substitutions between species that can be attributed to positive selection. Application of their approach in *Drosophila* has found that at least 40% of nonsynonymous substitutions have been fixed by positive selection (Smith and Eyre-Walker 2002).

Since the publication of the original study, α has been estimated from different species across the tree of life (Fay 2011). Estimates of α vary tremendously across species, tending to be higher in insects (Andolfatto 2005; Eyre-Walker and Keightley 2009), but much lower in primates and plants (Boyko et al. 2008; Eyre-Walker and Keightley 2009; Gossmann et al. 2010). In these latter species, formal tests have been unable to reject the hypothesis that α is zero (*i.e.* no positive selection; Boyko et al. 2008; Foxe et al. 2008; Eyre-Walker and Keightley 2009). It is not clear why α varies across species. One possibility is that α is higher for species

with larger population sizes, which could occur if adaptation is mutation limited. Here, species

with larger population sizes would have a higher rate of beneficial mutations. The fixation

probability of a given beneficial mutation also would be higher in species with larger population

size, but this effect is likely to only be important for very weakly beneficial mutations. Evidence

indicates that, in some cases, α is indeed correlated with population size. For example, Phifer-

Rixey et al. (2012) found that estimates of α were higher for species of mice that have larger

population sizes compared to species with smaller population sizes. Further, studies found a

positive correlation between α and population size when comparing different species of

sunflowers (Strasburg et al. 2011) and from phylogenetically diverse taxa (Gossmann et al.

2012). More recently, Galtier (2016) found a positive correlation between α and effective

population size for 44 animal species. Additional evidence that there is more positive selection in

larger populations stems from recent analyses of linked selection. Corbett-Detig et al. (2015)

found increased evidence for linked selection in species with larger population sizes, though the

mechanism driving this pattern is not immediately clear. Further, Nam et al. (2017) have

suggested that across primates, species with larger population sizes have had more selective

sweeps.

While this evidence suggests that adaptation could be mutation limited and that this could

be driving the variation in α across species, it is important to note that other factors could be

influencing the α statistic (Rousselle et al. 2018; Messer and Petrov 2013). As the denominator

of α is the total number of observed differences between species, it is sensitive to the fixation of

weakly deleterious mutations. For two populations with the same number of beneficial

substitutions, the one with a higher number of substitutions due to weakly deleterious mutations

will have a lower α. Indeed, because the number of fixed weakly deleterious mutations is

inversely related to population size (Ohta 1973, 1992), this effect could drive the correlation

between α and population size. In support of this prediction, Galtier (2016) found that the rate of

adaptive divergence (omega-a), which does not depend on the total number of divergent sites

between species (Gossmann et al. 2012), showed no correlation with population size. Similar

arguments have been made by Phifer-Rixey et al. (2012). Further, for humans, it has been

suggested that α had been underestimated due to the presence of weakly beneficial mutations still

segregating as polymorphisms (Galtier 2016; Uricchio et al. 2019). Indeed, methods that account

for weakly beneficial mutations still segregating as polymorphisms infer slightly higher values of

$\alpha = 0.24$ between humans and chimpanzee, and $\alpha = 0.135$ in the human lineage (Galtier 2016;

Uricchio et al. 2019). In addition, population sizes of the outgroup and ancestral population

determine the rate of fixation of weakly deleterious mutations in the outgroup lineage and in the

ancestral population, and could potentially influence the estimate of α (Rousselle et al. 2018;

McDonald and Kreitman 1991; Eyre-Walker 2002).

Other studies quantified positive selection by focusing on the proportion of beneficial

mutations (p^+) and their selection coefficients (s^+). Boyko *et al.* (2008) found that by assuming a

fraction (0 to 1.86%) of new mutations is positively selected, they could better match the

frequency spectrum of polymorphisms and the counts of human-chimpanzee divergence. Models

with weaker selection coefficients for beneficial mutations tended to have a higher proportion of

positively selected mutations than models with stronger selection (Boyko et al. 2008). Several

studies also have estimated p^+ and s^+ in *Drosophila* species and mice (Sella et al. 2009;

Schneider et al. 2011; Elyashiv et al. 2016; Campos et al. 2017; Keightley et al. 2016; Booker

and Keightley 2018). However, there has not been a systematic comparison across species.

Here we compare the amount of adaptive evolution in primates, rodents, and *Drosophila*.

We use two complementary approaches that quantify different aspects of the adaptive process.

First, we use improved modeling of weakly deleterious mutations and demographic models,

particularly correcting for the sizes of outgroup species and ancestral population to infer α.

Second, we estimate p^+ and s^+ of newly arising beneficial mutations by examining patterns of

polymorphism and divergence. We develop a composite likelihood framework to test whether

these parameters differ across taxa. This approach enables a more direct comparison of the

amount of beneficial mutations across species and is less confounded by the fixation of weakly

deleterious mutations.

RESULTS

Estimates of α for multiple species using the MK method

We first estimated α from coding regions of primates, rodents, and *Drosophila*. We

analyzed published genomic datasets to obtain counts of synonymous and nonsynonymous

polymorphisms (P_S and P_N) and divergent sties between species (D_S and D_N). For computation of

α in humans, we used chimpanzee and macaque as outgroup species. For mice and *D.*

melanogaster, we used rat and *D. simulans* as the outgroup species, respectively. In total, 19.1

Mb of coding sequence for primates, 26.6 Mb of coding sequence for rodents, and 15.8 Mb of

coding sequence for *Drosophila* were used in our analysis (see Methods).

An extension of the McDonald-Kreitman test was used to estimate α (Smith and Eyre-

Walker 2002; Table 1; Supplemental Table S1). To examine the effect of slightly deleterious

mutations on α, we filtered the data with several minor allele frequency (MAF) cutoffs (Messer

and Petrov 2013; Fay et al. 2001; Charlesworth and Eyre-Walker 2008) (Supplemental Table

S2). For example, after removing low frequency polymorphisms with MAF less than 20% , the

estimated α is close to zero for the human-chimpanzee comparison (Table 1), consistent with

previous estimates (Boyko et al. 2008; Eyre-Walker and Keightley 2009). However, for the

human-macaque comparison, α is -0.22 (Table 1), suggesting that the choice of outgroup species

could greatly influence α. Nevertheless, these results suggest at most only a very small

proportion of nonsynonymous substitutions have been fixed by positive selection in primates. In

contrast, for the *D. melanogaster*-*D. simulans* and mouse-rat comparisons, the estimated α is

49% and 40%, respectively, with MAF filter at 20% (Table 1). Both of these estimates are

comparable to previous studies (Andolfatto 2005; Eyre-Walker and Keightley 2009; Phifer-

Rixey et al. 2012). These results suggest that the proportion of substitutions fixed by positive

selection varies drastically across species, and for taxa with larger population sizes, like rodents

and *Drosophila*, adaptive forces may have had a greater contribution to divergence.

Model-based inference of α

Model-based approaches estimate α by contrasting the observed number of

nonsynonymous differences between species D_{NO} with the number expected under a

demographic model and a distribution of fitness effects (DFE) including only neutral and

deleterious mutations D_{NE} (Boyko et al. 2008; Eyre-Walker and Keightley 2009). The excess of

observed D_{NO} compared to the predicted D_{NE} is attributed to fixations driven by positive

selection. These methods also assume that the population sizes of outgroup species and the

ancestral population of the ingroup and outgroup are the same as the ancestral size of the ingroup

population (*Nanc.in*). We refer to this demographic model as the Simple model (Fig. 1A).

Using the Simple model, we first estimated the divergence time that best fit our data

using the observed D_S. We then predicted D_{NE} using this estimated divergence time, the gamma-

distributed DFE inferred in Huber et al. (2017), and the demographic model of the ingroup

species (Supplemental Text; Supplemental Table S3 and S4). We then estimated that α=11% for

humans and chimpanzee. This estimate is comparable to the inference by Boyko *et al.*, where

authors implemented a similar approach and estimated that approximately 10% of human-

chimpanzee nonsynonymous substitutions were fixed by positive selection (Boyko et al. 2008).

When using macaque as the outgroup species, we estimate that α is negative (Table 1). While it

is possible that this difference could reflect distinct evolutionary events experienced by different

outgroups, it could also be an artifact of the modeling assumptions. Previous estimates of the

human-chimpanzee ancestral population size (*Nanc*) range from 12,000 to 125,000 using

different datasets and methods (Chen and Li 2001; Hobolth et al. 2007; Burgess and Yang 2008;

Prado-Martinez et al. 2013; Schrago 2014). The estimated chimpanzee population size (*Nout)* is

around 30,000 (Prado-Martinez et al. 2013; Hvilsom et al. 2012; Fischer et al. 2004)

(Supplemental Table S5). However, the ancestral size inferred for the human lineage using

human polymorphism data is 7067, which is much smaller than all previous estimates of *Nanc*

and *Nout*. Using values of *Nanc* and *Nout* that are too small likely biases estimates of α because

more of the nonsynonymous substitutions are incorrectly attributed to the fixation of weakly

deleterious mutations, causing α to be under-estimated.

To more accurately model the larger *Nanc* and *Nout*, we use the Complex model which

allows *Nout* and *Nanc* to differ from *Nanc.in* (Fig. 1A). For humans, the larger *Nanc* is very

ancient, thus it does not affect the polymorphism pattern within humans (confirmed by

coalescent simulations, see Supplemental Text). We calculated the number of substitutions fixed

in the ingroup, outgroup, and ancestral populations. The total expected number of differences

between a pair of species is the sum of differences at all three stages. We first explored how *Nout*

and *Nanc* affect the inferred α. For the human-chimpanzee comparison, the inferred α changes

dramatically with different values of *Nout* and *Nanc*. Larger values result in larger estimates of α

(Fig. 1B). For example, when *Nout* = 30,000 (Prado-Martinez et al. 2013; Hvilsom et al. 2012;

Fischer et al. 2004) and *Nanc* = 60,000 (Chen and Li 2001; Hobolth et al. 2007; Prado-Martinez

et al. 2013), supported by many previous studies (Supplemental Table S5), α is approximately

24.6%. When using other values of *Nout* and *Nanc* within the ranges of previous estimates, the

corresponding estimates of α may differ, but remain above 20% (Fig. 1B). We next revisited the

human-macaque comparison under the Complex model (Supplemental Fig. S1), using *Nout* =

73,000 (Hernandez et al. 2007; Xue et al. 2016), *Nanc* = 48,000 (McVicker et al. 2009), and

changing the ingroup population size to 60,000 at human-chimpanzee divergence time to match

what we modeled in human-chimpanzee (Supplemental Table S4). Here we infer approximately

26.0% of human-macaque nonsynonymous substitutions were fixed by positive selection which

is comparable to what we found for the human-chimpanzee analysis. These estimates of α for

primates using the more realistic Complex demographic model are much higher than previous

estimates, implying that there is a greater contribution of positive selection to nonsynonymous

divergence than previously appreciated.

Similarly, we estimated α for *Drosophila* and rodents using the Complex demographic

model. For *Drosophila* , it had been inferred that *D. simulans* have slightly larger N_e than *D.*

melanogaster (Andolfatto et al. 2011), so we set *Nout* to be 1.5× the current population size of *D.*

melanogaster (*Ncur*) at the species' split (Supplemental Table S4). For mice, a previous study

estimated that the outgroup rat species has an effective population size about fivefold lower than

wild house mice (Ness et al. 2012). Thus, we set the *Nout* to be 0.2× *Ncur* of mice (Supplemental

Table S4). Since there is limited knowledge of the population sizes of the ancestor of *D.*

melanogaster and *D. simulans*, and ancestor of mice and rat, for these two comparisons, we

assume *Nanc = Nout.* Using these Complex models for *D. melanogaster-D.simulans* and mouse-

rat, we estimated their α to be 60% and 41%, compared with 53% and 45% using the Simple

model, respectively (Table 1). The differences between these estimates reflect the importance of

accurately modeling the population size of outgroup species for calculations of α.

We estimated α for substitutions that occurred exclusively on the human lineage, using

the human-macaque alignment to polarize sequence differences between human and chimpanzee.

We estimate that α = 6.2% using the Simple model, and 16.0% using the Complex model (Table

1).

To compare our estimates of α to those from another model-based method that assumes

Nanc=Nout=Nanc.in, we used *DFE-alpha*, to infer α for our three species pairs. Using this

method, α is estimated to be 24% and 2% for humans using chimpanzee and macaque as

outgroup respectively, 71% for *D. melanogaster-D. simulans*, and 51% for mouse-rat (Table 1).

These estimates are all higher compared to estimates from Simple models. However, the

estimates of α for primates differ significantly depending on whether the macaque or chimpanzee

is used as the outgroup for humans.

Testing whether p^+ and s^+ differ across species

We next estimated the DFE including new beneficial mutations. Our model of the DFE

includes two additional parameters compared to the base model that only includes deleterious

mutations. For each species, we estimate the proportion of new mutations that are beneficial (p^+)

and their selection coefficient (s^+). We then test whether these two parameters differ across

species.

The number of nonsynonymous differences between a pair of species (D_N) is assumed to

be Poisson-distributed (Sawyer and Hartl 1992), with rate parameter equal to:

$$E[D_N] = 2N\mu[\int G(s)u(s)(1-p^+) + u(s^+)p^+]$$ eq.(1)

where $G(s)$ is the DFE of deleterious and neutral mutations from Huber et al. (2017), $u(s)$ is the

fixation probability (Kimura 1962) of deleterious and neutral mutations, $u(s^+)$ is the fixation

probability of beneficial mutations, and p^+ is the proportion of new mutations that are beneficial.

We then use a Poisson log-likelihood function for D_N in each species and a series of likelihood

ratio tests (LRTs) to determine whether p^+ and s^+ differ across primates, rodents, and *Drosophila*

(see Methods).

Using this framework, we find that the full model H1, where each taxon is allowed to

have its own p^+ and s^+, fits D_N significantly better than the constrained null model, where p^+ and

s^+ are constrained to be the same across all three taxa (LRT statistic Λ=124,974, df=4, P<10^{-16};

Fig. 2; Supplemental Fig. S2; Supplemental Table S6).

We estimate that humans have a higher proportion of beneficial nonsynonymous

mutations than *D. melanogaster* and mice (Supplemental Table S6 and Fig. 2). Specifically, we

estimate that approximately 1.55% of new nonsynonymous mutations in humans are beneficial

with s^+ of approximately 1.12×10^{-4} (outgroup: chimpanzee), approximately 0.0675% of new

nonsynonymous mutations in *D. melanogaster* are beneficial with s^+ of approximately 1.58×10^{-5},

and approximately 1.02% of new nonsynonymous mutations in mice are beneficial with s^+ of

1.60×10^{-5} (Supplemental Table S6). Models with a larger s^+ tend to have a lower proportion of

positively selected mutations than models with smaller s^+. Consequently, the likelihoods of these

parameter values can be very close to the likelihoods at the MLEs. We also compared p^+ and s^+

between pairs of taxa (*i.e.* primate *vs.* rodent; primate *vs. Drosophila*; rodent *vs. Drosophila*). In

all pairwise tests (regardless of outgroup or demography), the model where each species has its

own p^+ and s^+ fits the observed D_N significantly better than a model where p^+ and s^+ are

constrained to be the same in the tested two taxa (Supplemental Table S6).

252   We next investigated whether it is possible that either p^+ or s^+ is the same across taxa but

the other parameter varies. Specifically, we allowed p^+ to differ across primates, rodents, and

Drosophila, then explored whether a model with the same s^+ could fit all species. This is shown

in conditional likelihood plots, where assuming the same s^+ for all species, humans would need a

higher proportion of beneficial mutations compared to mice and *D. melanogaster* to match the

observed D_N (Fig. 3A). Similarly, allowing s^+ to differ across species, a model with the same p^+

across all species could fit the data. When we forced the same p^+ for all species, s^+ for beneficial

mutations in humans would be larger compared to that in mice and *D. melanogaster* (Fig. 3B).

However, for the same p^+ value, s^+ could not be the same in all species. Similarly, for the same

s^+ value, p^+ could not be the same across species.

262   Motivated by the observation that larger values of p^+ and smaller values of s^+ can fit the

data as well as models with smaller values of p^+ and larger values of s^+, we also estimated a

composite parameter p^+s^+, the product of p^+ and s^+. We find clear evidence that regardless of the

model of ancestral demography or outgroup, humans have a significantly higher p^+s^+ than do *D.*

melanogaster and mice (Fig. 4). This can be seen by looking at the log-likelihood curves, which

are quite peaked, with little overlap across species. Thus, approximate 95% confidence intervals

on p^+s^+ for the different species do not overlap, implying more positive selection in humans than

in *D. melanogaster* and mice.

Testing whether γ+ and p+ differ across species

Humans, *D. melanogaster*, and mice have drastically different population sizes, which

can influence the efficacy of selection within each species. Thus, we next examined whether the

selection coefficient scaled by current population size ($\gamma^+=2Ns^+$) and p^+ differ across primates,

rodents, and *Drosophila*.

We find the model (Full model H1) where each taxon has its own different γ^+ and p^+ fits

the observed D_N significantly better than a model (constrained model H0) where γ^+ and p^+ are

constrained to be the same across all three taxa (LRT statistic $\Lambda=3{,}541$; df=4, $P<10^{-16}$, Fig. 5;

Supplemental Fig. S2; Supplemental Table S6).

Under the full model, we estimate that approximately 1% of new nonsynonymous

mutations in humans are beneficial with γ^+ of 6.05, approximately 2% of new nonsynonymous

mutations in *D. melanogaster* are beneficial with γ^+ of 4.92, and approximately 4% of new

nonsynonymous mutations in mice are beneficial with γ^+ of 3.76 (Supplemental Table S6).

Models with larger γ^+ tended to have a lower proportion of positively selected mutations than

models with smaller γ^+, and the likelihoods can be very close to those at the MLEs. The current

population sizes are 16,539, 7,616,700, 488,948 for humans, *D. melanogaster* and mice,

respectively. As a result, we are searching for p^+ within the same range of γ^+ (see Methods), but

markedly different ranges of s^+ for these three species. Thus, the relative ordering of the MLEs

of p^+ across species considering γ^+ is not necessarily the same as that for the s^+ results described

above.

We also compared γ^+ and p^+ between pairs of taxa. We find that for the human- *D.*

melanogaster and human-mice pairs, the models where each species has its own different γ^+ and

p^+ fit the observed D_N significantly better than a model where γ^+ and p^+ are constrained to be the

same in the tested two taxa (Supplemental Table S6). This result is robust regardless of outgroup

species. However, we cannot reject the hypothesis that mice and *D. melanogaster* have same γ^+

and p^+ (Supplemental Table S6).

We next investigated whether it is possible that either γ^+ or p^+ is the same across taxa,

while the other parameter varies. With the same γ^+ for all species, humans would need a lower

proportion of beneficial mutations compared to mice and *D. melanogaster* to fit the observed D_N

(Supplemental Fig. S3A). When we constrain p^+ to be the same for all taxa, humans have a

smaller γ^+ for beneficial mutations (Supplemental Fig. S3B). However, for the same p^+ value, γ^+

cannot be the same in all taxa. Similarly, for the same γ^+ value, p^+ cannot be the same across

taxa. We also estimated a composite parameter $p^+\gamma^+$, the product of p^+ and γ^+. We find that $p^+\gamma$

$^+$ is not as distinct across different taxa as is p^+s^+. In the Complex models, humans have a

smaller $p^+\gamma^+$ than mice. However, the log-likelihood curves of $p^+\gamma^+$ overlap between *D.*

melanogaster and mice, and between *D. melanogaster* and humans, suggesting they are not

significantly different (Supplemental Fig. S4).

Effects of biased gene conversion and hypermutable* CpG *sites

Biased gene conversion (BGC) is the preferred transmission of G/C alleles (S: strong

alleles) at the expense of A/T alleles (W: weak alleles). This process is common in mammals and

could impact patterns of genetic diversity (Duret and Galtier 2009; Lachance and Tishkoff 2014;

Bolívar et al. 2015) and bias estimates of rate of positive selection (Corcoran et al. 2017),

especially when comparing between taxa with BGC and taxa without BGC, *i.e. D. melanogaster*

(Robinson et al. 2014). Further, methylated CpG sites in mammals have a higher mutation rate to

T alleles due to deamination of the C nucleotide (Sved and Bird 1990; Duncan and Miller 1980),

which could possibly bias inferences of selection.

To test whether BGC and hypermutable CpG sites drive the observed pattern of positive

selection across primates, rodents, and *Drosophila*, we filtered primate and rodent data to keep

only strong to strong or weak to weak mutations (herein called SSWW mutations), which are not

affected by BGC and are not CpG changes (Supplemental Text, Supplemental Fig. S5). We then

re-inferred α. For primates, α is comparable to that without filtering (Table 1). For rodents,

however, α is substantially lower than that before filtering, suggesting that biased gene

conversion and CpG mutational processes may account for some of the nonsynonymous

differences between mouse and rat.

Removing the effect of BGC and CpG sites in primates and rodents, we again quantify

and compare the strength and proportion of new beneficial mutations across all three taxa. The

model where each taxon has its own p^+ and s^+ fits the observed D_N significantly better than a

model where p^+ and s^+ are constrained to be the same across all three taxa (LRT statistic Λ=825,

df=4, $P<10^{-16}$; Supplemental Fig. S6; Supplemental Table S6). Models comparing each pair of

taxa (*e.g.* primates *vs.* rodents; primates *vs. Drosophila*; rodents *vs. Drosophila*) suggest that

each taxon has its own unique p^+ and s^+, regardless of demography (Supplemental Table S6).

Allowing p^+ to differ across taxa, a model with the same s^+ across all taxa could fit the data, and

vice versa. When we force the same s^+ for all species, humans still have the highest proportion of

new beneficial mutations (Supplemental Fig. S6E). Constraining p^+ to be the same for all

species, humans have the largest selection coefficient (Supplemental Fig. S6F).

Similarly, the model where each taxon has its own p^+ and $\boldsymbol{\gamma}^+$ fits the observed D_N

significantly better than a model where p^+ and $\boldsymbol{\gamma}^+$ are constrained to be the same across all three

taxa (LRT Λ=4496, df=4, P<10^{-16}; Supplemental Table S6 and Fig. S7). Models comparing each

pair of taxa suggest that each taxon has its own unique p^+ and γ^+, regardless of demography

(Supplemental Table S6). Allowing p^+ to differ across species, a model with the same γ^+ across

all taxa could fit the data, and *vice versa*. When we constrain γ^+ to be the same for all species, *D.*

melanogaster have the highest proportion of new mutations being beneficial, and mice have the

lowest proportion of new mutations that are beneficial. When we constrain p^+ to be the same for

all species, *D. melanogaster* have the largest γ^+, and mice have the smallest γ^+(Supplemental

Fig. S7).

Lastly, we estimated two composite parameters, p^+s^+ and $p^+\gamma^+$ for SSWW mutations.

Humans again have a significantly higher p^+s^+ than *D. melanogaster* and mice (Supplemental

Fig. S8), suggesting more positive selection in humans than in *D. melanogaster* and mice.

Similar to the full dataset, $p^+\gamma^+$ is not as distinct across different species as p^+s^+. Under the

Complex model, we find that humans and *D. melanogaster* have a significantly (*i.e.* the log-

likelihood curves do not overlap within 2 units of the MLEs) larger $p^+\gamma^+$ than mice, and the log-

likelihood curves of $p^+\gamma^+$ for humans and *D. melanogaster* overlap near the MLEs

(Supplemental Fig. S8).

DISCUSSION

We have quantified the amount of adaptive evolution in multiple species with differing

degrees of complexity and population size using two different approaches. First, we examined

the proportion of nonsynonymous substitutions fixed by positive selection and found that this

proportion is higher in *Drosophila* than in rodents and primates, consistent with prior work

(Andolfatto 2005; Eyre-Walker and Keightley 2009; Boyko et al. 2008; Fay 2011). However,

after correcting for the population sizes of the outgroup and ancestral population, we infer that α

is much higher in primates than what was inferred in previous studies. Second, we show that the

DFE of new beneficial mutations differs across species. The species with the smaller population

size and greater complexity (*i.e.* humans) has stronger and/or more abundant new beneficial

mutations than the other two species with much larger population sizes (*i.e.* mice and *D.*

melanogaster). These results are robust to the choice of outgroups, BGC, and hypermutable CpG

sites.

One major improvement of our method to infer α over previous similar approaches from

Boyko et al. and *DFE-alpha* (Boyko et al. 2008; Eyre-Walker and Keightley 2009) is that we

allow the outgroup and ancestral population sizes to differ from the ancestral population size of

the ingroup. In Boyko *et al.* (2008), the outgroup population size is assumed to be the same as

that found in the ancestral ingroup population. *DFE-alpha* allows for inference of demographic

parameters of one- to three- epoch models, and the outgroup population size is assumed to be the

same as the ancestral ingroup population. When considering species like humans in relation to

other primates, like chimpanzee or macaque, this assumption certainly does not hold as primate

species have population sizes at least several fold larger than the estimated ancestral human

population size of approximately 7,000 individuals (Chen and Li 2001; Hobolth et al. 2007;

Burgess and Yang 2008; Prado-Martinez et al. 2013; Schrago 2014; Hernandez et al. 2007;

McVicker et al. 2009; Hvilsom et al. 2012; Wall 2013; Xue et al. 2016). The sizes of the

outgroup and ancestral population matter because they affect the fixation probability of weakly

deleterious alleles (Kimura 1983; Ohta 1973, 1992). As such, the number of nonsynonymous

substitutions attributed to weakly deleterious mutations is highly affected by the population sizes

of the outgroup and ancestral population. Consequently, estimates of α are affected as well. Our

approach includes a more complex demographic model that allows the ancestral and outgroup

populations to have their own sizes (*Nanc* and *Nout*). By using these more realistic population

sizes, the α estimates we obtained for primates are similar when using chimpanzee or macaque as

outgroup species. This is strong evidence that our method is more accurate as all the other

methods give drastically different estimates of α using these two different outgroups.

Interestingly, Eyre-Walker and Keightley (2009) also suggested that α in humans could be as

high as 0.31 if the effective population size of humans and macaques was much higher than

10,000 until very recently, foreshadowing our current estimates. Future studies of adaptive

substitutions should carefully consider ancestral and outgroup population sizes and should use

statistical methods that model them realistically.

Here we have quantified adaptive evolution from two different perspectives. First, we

estimate the proportion of adaptive nonsynonymous substitutions between species, α. This

statistic measures the endpoint where a number of factors such as demography, genetic drift, and

natural selection all come into play. Second, we estimate the DFE of newly arising beneficial

mutations, *i.e.* p^+ and s^+. This approach aims to understand the properties of new beneficial

mutations, the beginning point where beneficial mutations appear and enter the population. Thus,

it is possible that these two approaches can yield qualitative opposite results. Indeed, we have

shown that *D. melanogaster* have the largest values of α, but the smallest p^+s^+.

We previously found 15% of nonsynonymous mutations in humans are weakly beneficial

(Huber et al. 2017). Importantly, because Huber *et al.* only analyzed polymorphism data, they

did not consider strongly beneficial mutations that became substitutions between species. Our

present study leverages genome sequences of several related species pairs to estimate the

proportion of strongly beneficial ($s^+>10^{-5}$) mutations that are fixed between species. Weakly

beneficial mutations are already accounted for in our model using the DFE from Huber *et al.*

(2017) as many weakly beneficial mutations are likely segregating as polymorphisms.

Intriguingly, we find that humans have a higher proportion of strongly beneficial mutations than

D. melanogaster, mirroring the qualitative trend seen for weakly beneficial mutations in Huber *et*

al. (2017). In the context of human evolution, it has been shown that weakly beneficial mutations

that are still segregating could result in an underestimate of α (Uricchio et al. 2019; Galtier

2016). Thus, the estimate of α in humans could be even higher if adaptive polymorphisms were

taken into account. Alternatively, our current approach of modeling the complex demography in

the outgroup and ancestral population should correct for some of the bias in inferring α due to

weakly beneficial mutations still segregating as polymorphisms. The reason for this is that

weakly beneficial mutations still segregating as polymorphisms will be accounted for in the

parametric DFE fit to the site frequency spectrum (SFS; as discussed above in the context of

Huber et al. 2017). A parametric DFE including only deleterious and neutral mutations will treat

this class of weakly beneficial mutations as nearly neutral (Tataru et al. 2017), inflating the

expected divergence that can be accounted for by non-adaptive forces. Modeling the complex

demography reduces the number of fixations from nearly neutral mutations that are treated in the

model to be non-adaptive, including those from segregating weakly beneficial mutations.

Our estimate of α for human lineage is 16.0% using the Complex model, which is

comparable to the estimate of human-lineage α by Uricchio *et al.* (2019)*,* despite the use of

different analytical approaches. α is expected to be lower on the human lineage as compared to

the chimpanzee or macaque lineage due to the higher proportion of weakly deleterious amino

acid substitutions on the human lineage to their smaller population size (Ohta 1973, 1992). For

D. melanogaster, using the Complex model we estimate $p^+\gamma^+$ to be ~0.1 which is within a factor

of 2 of a previous estimate of Keightley et al. (2016). For mice, using the Complex model, we

estimate $p^+\gamma^+$ to be ~0.15 which is somewhat greater than the value of ~0.05 inferred in Booker

and Keightley (2018). The differences in estimates could be due to the use of different methods

and models, such as our detailed modeling of the ancestral and outgroup population sizes.

We make several key modeling assumptions. First, we assume that the DFE is the same

between the ingroup and outgroup for each pair of species (*e.g.* humans and chimpanzee have the

same DFE). This assumption could be relaxed by using only polymorphism data to infer the

beneficial DFE (Tataru et al. 2017), though not including divergence to an outgroup species

considerably reduces the power to infer positive selection (Booker 2019). Second, our inference

of p^+ and s^+, as well as related approaches (Schneider et al. 2011; Tataru et al. 2017; Booker and

Keightley 2018), make the assumption of selection starting from a single mutation, since we use

the fixation probability of a mutation introduced as a single copy. Selection on standing variation

(*i.e.* one type of soft sweep) might bias the parameter estimates, though the meaning of p^+ and s^+

are not as clear under models with soft sweeps. α, however, should be accurately estimated even

as long as the beneficial mutation reaches fixation. Furthermore, as our approach only focuses on

strongly beneficial mutations that contribute to divergence, it is not sensitive to types of selection

that do not reach fixation. These include another type of soft sweeps (Pritchard et al. 2010),

where multiple independent beneficial mutations in the same gene are selected simultaneously,

but no mutation becomes fixed, as well as polygenic adaptation where beneficial alleles only

slightly increase in frequency, without reaching fixation. A last limitation comes from the model

itself. It has been suggested that models where s^+ does not change over time may not model the

complexity of adaptive walks, where the first beneficial mutation may have a more strongly

beneficial effect on fitness than subsequent beneficial mutations (Gillespie 2004; Lourenço et al.

2013). Thus, our estimates of p^+ and s^+ should be interpreted in this context as the average values

over longer time periods and over different genetic backgrounds, rather than literal values that

have stayed constant over time. In fact, our findings show that p^+ and s^+ have changed over deep

evolutionary time, pointing to their dynamic nature.

One previous explanation for varying estimates of α across species was that adaptation is

mutation limited and there are more beneficial mutations in organisms with larger population

sizes. This view was not supported by conceptual arguments by Gillespie (2004) who suggested

that the rate of environment change will matter more than the population size in determining the

rate of adaptive evolution. The simulation study by Lourenço et al. (2013) that considered a

changing DFE over time in the context of Fisher's geometric model found that the population

size only weakly related to α. Instead, the rate at which the environment changed was an

important predictor of the amount of adaptive evolution, as environmental shifts moved the

population from the fitness optimum, creating the opportunity for new beneficial mutations.

Further, Rousselle et al. (2019) recently found a weak negative correlation between the amount

of adaptive evolution and the amount of genetic diversity in modern populations, which supports

the models of Lourenco *et al.*(2013) and Gillespie (2004). However, not all studies are in

agreement on the role of the environment as Connallon and Clark (2015) found that

environmental heterogeneity reduces the fraction of beneficial mutations by inflating the

standardized mutation size in Fisher's geometric model. Lourenço et al. (2013) also found that

organismal complexity, here defined as the number of phenotypes under selection, was a key

predictor of the amount of adaptive evolution within species. Through a "cost of complexity",

more complex organisms have a harder time adapting to new environmental conditions due to

the additional constraints imposed by the increased number of traits under selection. As such,

adaptive walks require more beneficial mutations (Orr 1998).

Our results presented here are in broad agreement with the conceptual model of Lourenço

et al. (2013). Specifically, we do not find that species with larger population sizes (*i.e. D.*

melanogaster) have more beneficial mutations. Instead, we find that p^+ (as well as p^+s^+) is

higher in humans than in *D. melanogaster* or mice. Second, while it is hard to precisely define

organismal complexity, previous work has found more protein-protein interactions in humans

than in *Drosophila* (Valentine et al. 1994; Stumpf et al. 2008), suggesting that humans may be

more complex than *Drosophila*. If this is the case, then our findings of a higher p^+ (and p^+s^+) in

humans than *D. melanogaster* and mice supports the arguments from Lourenço et al. (2013) that

adaptive walks after an environmental shift are less efficient and require more steps (*i.e.*

beneficial mutations) in more complex organisms, leading to higher p^+ in complex organisms.

Additionally, differences in the degree of environmental change across species could also

contribute to the disparate inferences of p^+s^+ across taxa. While it is hard to say which species

has experienced more environmental shifts, it has been suggested that those species with longer

generation times, like primates, may experience more environmental change per generation than

species with shorter generation times, like *Drosophila* or rodents (Rousselle et al. 2019;

Romiguier et al. 2014). Our finding of higher p^+ in humans than *Drosophila* supports this

intriguing prediction.

METHODS

Polymorphism and divergence data for humans, mice, and D. melanogaster

For humans, we used polymorphism data from 112 individuals from Yoruba in Ibadan,

Nigeria (YRI) from the 1000 Genomes Project (1000 Genomes Project Consortium 2012).

Published genome alignments of human and chimpanzee (hg19/pantro4), and human and

Macaca mulatta (hg19/rheMac3) were downloaded from the UCSC genome browser

(http://hgdownload.soe.ucsc.edu/goldenPath/hg19/). For *D. melanogaster*, we used the

Drosophila Population Genomics Project phase 3 data, including 197 African *D. melanogaster*

lines from Zambia, Africa (Lack et al. 2015). For divergence, *D. melanogaster* and *D. simulans*

genic alignments (Dmel v5/Dsim v2) were extracted from the multi-species alignments from Hu

et al. (2013). Only autosomal regions were used in our analysis. Human and *D. melanogaster*

polymorphism data were filtered and down-sampled to 100 chromosomes as described in Huber

et al. (2017).

For mice, raw data (fastq) was downloaded for 10 *M. m. castaneus* individuals that were

collected in the northwest Indian state of Himachal Pradesh (Halligan et al. 2010, 2013). Reads

were mapped against mouse genome mm9 using bwa (Li and Durbin 2009) and stampy (Lunter

and Goodson 2011). Duplicate reads were marked using Picard, and further pre-processing was

done following GATK Best Practice guidelines (McKenna et al. 2010). Variants were called

using the GATK UnifiedGenotyper and filtered using the GATK VQSR using Affymetrix Mouse

Diversity Genotyping Array sites (Yang et al. 2009). We further filtered the dataset to only retain

sites with a sample size of at least 16 chromosomes and down-sampled all sites with larger

sample size to a sample size of 16 chromosomes using the hypergeometric probability

distribution. Published genome alignments of mice and rat (mm9/rn5) were downloaded from

UCSC (http://hgdownload.soe.ucsc.edu/goldenPath/mm9/vsRn5/axtNet/). For each species,

polymorphism and divergence data were intersected, and only coding regions shared by both

datasets were used in our analysis.

In total, 19.1Mb of coding sequences for primates, 26.6 Mb of coding sequences for

rodents and 15.8Mb of coding sequences for *Drosophila* were included. The nonsynonymous

and synonymous total sequence lengths (L_{NS}, L_S) were estimated using multipliers of $L_{NS} = 2.85$

$\times L_S$ in *D. melanogaster*, and $L_{NS} = 2.31 \times L_S$ in mammals from Huber et al. (2017). In these

filtered coding sequences, we annotated synonymous and nonsynonymous sites in both

polymorphism and substitution data for each species. Human variants were annotated using the

SeattleSeq Annotation pipeline (http://snp.gs.washington.edu/SeattleSeqAnnotation138/). Mice

and Drosophila variants were annotated using SnpEeff v3.6 using the mice NCBIM37.66

annotation database and the *D. melanogaster* BDGP5.75 annotation database, respectively. Sites

that are annotated as near-splice, or loss of function were removed. The ratio of

nonsynonymous/synonymous differences between human and chimp sequences in our dataset is

approximately 0.65, which is consistent with several previous reports from different datasets

(Bustamante et al. 2005; Torgerson et al. 2009; Enard et al. 2014).

From the down-sampled polymorphism data, we calculated the synonymous and

nonsynonymous SFS, and used the folded SFS for all further inferences to avoid

misidentification of the ancestral state.

Model-based estimates of α

To implement a model-based approach to estimate α, for each pair of species, we need a

demographic model and a DFE for neutral and deleterious mutations to predict the D_{NE} that is

accounted for by neutral and deleterious mutations. For primates and *Drosophila*, we use

demographic and DFE parameters from Huber *et al.* (2017; Supplemental Table S3). For rodents,

we conducted our own inference of these parameters by summarizing the polymorphism data in

mice by the folded SFS (Supplemental Text).

To compute the expected divergence between species, we computed the divergence

accumulated in ingroup population, outgroup population and ancestral population separately and

summed them up. The divergence in the ingroup and outgroup population is a function of

divergence time, effective population size, mutation rate, and selection coefficient and was

calculated according to equation 13 in Sawyer and Hartl (1992). We computed the expected

divergence under a gamma DFE model by Monte Carlo integration using one million gamma

distributed selection coefficients. The contribution of the ancestral population to divergence

between two species was computed numerically based on the diffusion equation, using *prfreq*

(Boyko et al. 2008) and assuming the same gamma DFE. These calculations are implemented in

our program *predicDiv* (https://github.com/LohmuellerLab/predicDiv). For both the Simple and

the Complex models, we first estimate the divergence times (Supplemental Table S4) that fit the

observed number of synonymous differences between a pair of species because there is a wide

range of divergence times from the literature for each species. Here the number of synonymous

differences equals 2 × divergence time × mutation rate. Second, using this divergence time,

demography, and DFE inferred from Huber *et al.*(2017), or as described above for mice, we

estimated the expected number nonsynonymous differences (D_{NE}) according to Sawyer and Hartl

eqn 13 (Sawyer and Hartl 1992; Boyko et al. 2008). Then, α is calculated as

$$\alpha = \frac{D_{NO} - D_{NE}}{D_{NO}} \quad , \qquad\qquad\qquad \text{eq. (2)}$$

where D_{NO} is the observed number of nonsynonymous differences between species.

DFE-alpha

Data files and the program v2.15 were downloaded from the following link:

http://www.homepages.ed.ac.uk/pkeightl//dfe_alpha/download-dfe-alpha.html. Folded

synonymous and nonsynonymous SFS were used as input in the inferences. The

est_alpha_omega program was used to estimate the proportion of adaptive divergence.

Composite likelihood approach for testing whether p^+ and s^+ differ across species

We first used *predicDiv* and *prfreq* to generate a look-up table for the expected number

of nonsynonymous differences between species for a range of s^+ (10^{-5}-10^{-2}) for each species. We

focused on this range to capture strongly advantageous mutations. Given a demographic model,

we again assume a substitution rate according to equation 13 in Sawyer and Hartl (1992). The

contribution of the ancestral population to the divergence between two species is computed by

numerically solving the diffusion equation using *predicDiv* and *prfreq* (Boyko et al. 2008). For

each species, we then did a grid search of $\log_{10}(s^+)$ (-5 to -2) and p^+ (0-7.5%). We are interested

in this range of strong s^+ because weakly beneficial mutations still segregating as polymorphisms

and are accounted for by the DFE fit to the SFS. We use a Poisson log-likelihood function to

calculate the log-likelihood (LL) for each combination of s^+ and p^+. We find the MLE of s^+ and

p^+ for each taxon under each demographic model that maximizes the LL and best fit the observed

D_N. This is the full model (H1) where each taxon (*i.e.* primates, rodent and *Drosophila*) is

allowed to have its own s^+ and p^+. Our H0 hypothesis is the constrained model, where two or

three taxa have the same s^+ and p^+. The LL of the constrained model is the sum of LL for each s^+

and p^+ for each taxon under comparison. We then found the MLE for the constrained model and

calculate the likelihood ratio between H1 and H0.

Composite likelihood approach for testing whether p^+ and γ^+ differ across species

   Similarly, we used *predicDiv* and *prfreq* (Boyko et al. 2008) to generate a look-up table

for the expected number of nonsynonymous differences for a range of γ^+ (1-10^3) for each taxon

under each demographic model. For each species, we performed a grid search of $\log_{10}(\gamma^+)$ (0-3)

and p^+(0-7.5%). Note, because effective population sizes differ over several orders of magnitude

across our three taxa, we are searching across drastically different ranges of s^+ as compared to

our previous inference described above. We again use a Poisson log-likelihood function to

calculate the LL for each combination of γ^+ and p^+ and use a similar LRT framework as

described above for s^+ and p^+.

Composite parameters p^+s^+ and $p^+\gamma^+$

   We examined two composite parameters, the product of p^+ and s^+ and the product of p^+

and γ^+ for each taxon. Multiple combinations of parameters could give the same product p^+s^+

and $p^+\gamma^+$ and distinct combinations could have different LL. Thus we found the values of p^+ and

s^+ that gave the highest LL for each p^+s^+ value (and similarly each p^+ and γ^+ for each $p^+\gamma^+$).

Values of $\log_{10}(p^+s^+)$ and $p^+\gamma^+$ were rounded to three digits prior to this comparison.

Conditional log-likelihoods

   To examine whether primates, rodents, and *Drosophila* could have the same s^+ or p^+, we

examined the conditional log-likelihoods. To make the conditional log-likelihood curve for p^+,

for each s^+ value, we find the p^+ that maximizes the LL as well as the p^+ values that have a LL

within three LL units of this maximum LL for this s^+ (*i.e.* $p^+|s^+$). To make the conditional log-

likelihood curve for s^+, for each p^+ value, we look for the s^+ that maximizes the log-likelihood as

well as the s^+ values that have a LL within three LL units of this maximum LL for this p^+ (*i.e.* $s^+|$

p^+). The same approach was used to construct the conditional log-likelihood curve for p^+ and $\boldsymbol{\gamma}^+$.

Estimating α on the human lineage

Human-chimpanzee differences were polarized by the macaque sequence. Differences

between human and chimpanzee were assigned to human lineage if the bases differ between

human and macaque, but were the same between chimpanzee and macaque in the pairwise

genome alignments. Differences that are in regions where the human and macaque sequences

were un-alignable and sites that differ among human, chimp, and macaque cannot be polarized

(3.8% total) and were filtered out. The total length of coding regions was scaled by this filter

accordingly. A total of 30,530 synonymous substitutions and 20,013 nonsynonymous differences

were observed on human lineage. We assume the human lineage and the outgroup lineage

contribute equally to neutral D_S, thus the total D_S between human and chimpanzee would be

61,060. We then adjusted divergence time to match predicted D_S to 61,060, and use this adjusted

divergence time, DFE of deleterious mutations and demography of human to predict D_N as

described in *Model-based estimates of α*. The human lineage α is then calculated using equation

(2).

Filtering to only include sites not affected by biased gene conversion or CpG hypermutation

Full polymorphism and substitutions datasets of primates and rodents were filtered to

keep only strong to strong or weak to weak (SSWW) mutations because these changes were not

affected by BGC or increased mutation rates due to deamination of methylated CpG sites. These

changes include only A to T, T to A, C to G and G to C changes. These changes are only a small

subset of all variable sites. The nonsynonymous and synonymous sequence lengths (L_{NS}, L_S)

depend on the transition/transversion ratio and the CpG mutational bias. SSWW mutations are all

transversions and do not included any CpG mutations, leading to a multiplier of $L_{NS} = 5.21$ x L_S

in both primates and rodents. To compute this: 1) we used numbers of 0-, 2-, 3- and 4- fold sites

in the human exome from Veeramah et al. (2014); 2) we consider all 2-fold sites to be

nonsynonymous (because SSWW mutations are all transversions); and 3) we do not consider a

mutational bias of CpG sites (because CpG sites are not included in the SSWW set). In addition,

because SSWW mutations are only a small subset of all mutations, mutation rates need to be

scaled down to the SSWW specific mutation rate. To estimate the demographic parameters and

DFE for SSWW polymorphisms in rodents, first, we used the observed number of synonymous

SSWW polymorphisms to estimate the mutation rate for mice SSWW mutations to be 5.99×10^{-10}

^{10}. Then, using the SFS for SSWW synonymous polymorphisms, we inferred that the ancestral

population size in mice is approximately 246,256 which expanded 1.7-fold approximately

262,000 generations ago (Supplemental Table S3). Conditional on this demographic model, we

estimated the DFE for new nonsynonymous SSWW mutations in mice. We assume that the DFE

follows a gamma distribution and estimate its shape parameter α to be 0.21 and scale parameter

beta to be 0.050 (Supplemental Table S3). These estimates are within the same magnitude of the

estimates from the full dataset and a previous study (Huber et al. 2017). We re-estimated the

mouse-rat divergence time that fits best with the observed SSWW D_S. We then re-inferred p^+, s^+,

and γ^+ as done previously, using the filtered data, new mutation rates, and new values of L_{NS}.

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Author contributions

K.E.L conceived of and supervised the study. Y.Z. carried out all analyses on positive selection

and generated all figures. C.D.H carried demographic and gamma-DFE inference. R.W.D.

processed mice raw data to genotypes. Y.Z., C.D.H., R.W.D and K.E.L. all participated in

manuscript preparation.

DISCLOSURE DECLARATION

The authors declare no competing interests.

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873 Table 1. Estimates of α using different methods

	Species	Outgroup	Method of Inference					
			MK-method: all	MK-method: MAF>20%	Model-based: Simple Model	Model-based: Complex Model	DFEα: α	DFEα: omega_a
Full data	Human	Chimpanzee	-0.41	-0.01	0.11	0.25	0.24	0.07
	Human	Macaque	-0.70	-0.22	-0.08	0.26	0.02	0.01
	Human lineage	-	-	-	0.06	0.16	-	-
	D. melanogaster	*D. simulans*	-0.13	0.49	0.53	0.60	0.71	0.14
	Mice	Rat	0.25	0.40	0.45	0.41	0.51	0.12
SSWW only	Human	Chimpanzee	-0.37	0.08	0.13	0.26	-	-
	Mice	Rat	-0.14	0.08	0.20	0.10	-	-

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Figure 1. The ancestral and outgroup population sizes greatly influence α. (A). Schematic

demographic models illustrate the Simple and the Complex model with associated parameters. In

the Simple model, the size of the ancestral population (*Nanc)* as well as the size of the outgroup

(*Nout*) are assumed to be the same as the ancestral size of the ingroup (*Nanc.in*). This assumption

is relaxed in the Complex model. (B). Effect of *Nanc* and *Nout* on estimates of α for humans

using the chimpanzee as an outgroup. Colors denote different values of *Nanc*. Arrow points to

the estimate of α from the Simple model where *Nanc = Nout = Nanc.in* = 7067.

Figure 2. Log-likelihood surfaces for p^+ and s^+ for different species. (A) Human. (B) *D.*

melanogaster. (C) Mouse. (D) The constrained model (H0), where p^+ and s^+ are constrained to

be the same across all three taxa. Log-Likelihoods (LL) are calculated using grid search method

of $\log_{10}(s^+)$ in the range of -5 to -2 and p^+ in the range of 0-7.5%. Blue denotes human, red

denotes *D. melanogaster*, and green denotes mouse. The large points represent the MLE for each

species, the black cross in panel D represents the MLE of the constrained model, and the lighter

colors show grid points within 3 LL units of each MLE. The Complex model is used for each

species and we use the chimpanzee as the outgroup for humans.

Figure 3. Conditional log-likelihood surfaces. (A) Maximizing p^+ given particular values of s^+

and (B) maximizing s^+ given particular values of p^+. Only grid points within 3 LL units of the

MLEs for each parameter for each species are shown. Light blue denotes human, pink denotes *D.*

melanogaster, and light green denotes mouse.

Figure 4. The composite parameter p^+s^+, capturing the proportion of beneficial mutations

and the strength of selection, differs across species. Log-likelihood curves for p^+s^+ in the

three species. Red denotes the inference for *D. melanogaster*, green denotes the inference for

mouse, blue denotes the inference for human using the chimpanzee as the outgroup, and purple

denotes the inference for human using the macaque as the outgroup. Lighter colors denote the

Simple model. Darker colors denote the Complex model that better models the ancestral

demography and population size of the outgroup. Note that regardless of which demographic

model is used, the log-likelihood curves from the different species do not overlap within the top

500 log-likelihood units, suggesting p^+s^+ is significantly different among taxa.

Figure 5. Log-likelihood surfaces for p^+ and γ^+ for different species. (A) Human. (B) *D.*

melanogaster. (C) Mouse. (D) The constrained model, H0, where p^+ and γ^+ are constrained to be

the same across all three taxa. Log-likelihoods are calculated using grid search method of

$\log_{10}(\gamma^+)$ in the range of 0-3 and p^+ in the range of 0-7.5%. Blue denotes human, red denotes *D.*

melanogaster, and green denotes mouse. The large points represent the MLE for each species,

the black cross in panel D represents the MLE of the constrained model, and the lighter colors

show grid points within 3 LL units of each MLE. The Complex model is used for each species

and we use chimpanzee as the outgroup for humans.