INSTRAL: Discordance-aware Phylogenetic Placement using Quartet Scores

Maryam Rabiee[1],* and Siavash Mirarab[2],*

[1] *Department of Computer Science and Engineering, UC San Diego, La Jolla, CA 92093, USA*
[2] *Department of Electrical and Computer Engineering, UC San Diego, La Jolla, CA 92093, USA*

* smirarab@ucsd.edu

Abstract

Phylogenomic analyses have increasingly adopted species tree reconstruction using methods that account for gene tree discordance using pipelines that require both effort and computational resources. As the number of available genomes continues to increase, a new problem is facing researchers. Once new species become available, they have to repeat the whole costly process from the beginning because updating available species trees is currently not possible. Such de-novo inference can be prohibitively costly in human effort or machine time. In this paper, we introduce INSTRAL, a method that extends ASTRAL to enable phylogenetic placement. INSTRAL is designed to add a new species onto an existing species tree after sequences from the new species have already been added to gene trees; thus, INSTRAL is complementary to existing placement methods such as pplacer and EPA that update gene trees with new sequences.

Key words: species tree reconstruction, gene trees, incomplete lineage sorting, phylogenetic placement, ASTRAL

Methods for reconstructing species trees while accounting for gene tree

discordance (Maddison, 1997) are now widely available (Szöllsi et al., 2014; Edwards et al., 2016; Warnow, 2017) and commonly used. Discordance-aware methods come in many forms, such as co-estimation of gene trees and species trees (e.g., Liu, 2008; Heled and Drummond, 2010; Boussau et al., 2013), site-based methods (e.g., Bryant et al., 2012; Chifman and Kubatko, 2014), and more recently, direct modeling of polymorphism (De Maio et al., 2013; Schrempf et al., 2016). The most scalable approach for species reconstruction has remained what has been called a summary approach (Mirarab et al., 2016): first gene trees are inferred independently for all loci, and then they are combined to infer a species tree. Many methods are available for combining gene trees (e.g., Kubatko et al., 2009; Liu et al., 2009; Mossel and Roch, 2010; Liu et al., 2010; Chaudhary et al., 2010; Liu and Yu, 2011; Wu, 2012; Bayzid et al., 2013; Sayyari and Mirarab, 2016a), and many of them have been proved statistically consistent under various models of genome evolution. In particular, many of the summary methods have established statistical guarantees (Liu et al., 2010; Allman et al., 2016; Shekhar et al., 2017) under the multi-species coalescent model (Pamilo and Nei, 1988; Rannala and Yang, 2003), which can generate incomplete lineage sorting (Degnan and Rosenberg, 2009). Several summary methods, including ASTRAL (Mirarab et al., 2014b; Mirarab and Warnow, 2015), NJst/ASTRID (Liu and Yu, 2011; Vachaspati and Warnow, 2015), and MP-EST (Liu et al., 2010) are in wide use.

Despite the progress for de-novo reconstruction of species trees, tree updating has received little attention. As new genomes become available, researchers often need to know their position on an existing phylogeny. An expensive approach to find the answer is to reconstruct the species tree from scratch each time new data becomes available. This process will require excessive computation and will not scale to groups with tens of thousands of genomes (more than a hundred thousand bacterial genomes are currently available).

A more efficient alternative is what has been called phylogenetic placement (Matsen

et al., 2010): adding a new *query* species onto an existing phylogeny. For placing a single sequence to an existing gene tree, we already have maximum likelihood (ML) methods such as `pplacer` (Matsen et al., 2010) and `EPA` (Berger et al., 2011) and divide-and-conquer methods such as `SEPP` (Mirarab et al., 2012). Even earlier, sequential sequence insertion algorithms, which essentially solve the same computational problem, existed (e.g., Desper and Gascuel, 2002; Felsenstein, 1981). However, all these algorithms place a new sequence onto a gene tree. Placing a new species on a species tree is equally needed. To our knowledge, discordance-aware methods for placement into species trees do not currently exist. Here, we present INSTRAL (Insertion of New Species using asTRAL) as an extension to the previously published method ASTRAL to add a species onto a species tree.

Description

Background

ASTRAL estimates an unrooted species tree given a set of unrooted gene trees and is statistically consistent under the multi-species coalescent model given true gene trees (Mirarab et al., 2014b). ASTRAL seeks to maximize the quartet score: the total number of induced quartet trees in the gene trees that match the species tree. It uses dynamic programming to exactly solve this NP-Hard problem (Lafond and Scornavacca, 2017). However, to allow scalability, it constrains its search space so that the output draws its clusters from a predefined set X, which consists of clusters from gene trees and others that are heuristically selected (a cluster is one side of a bipartition). The most recent version, ASTRAL-III (Zhang et al., 2018) guarantees polynomial running time and scales to datasets with many thousands of species.

Problem statement

Quartet Placement Problem. Given a set of k unrooted trees labeled with $n + 1$ species and a backbone tree on n species, find the tree that includes all $n + 1$ species and has the

maximum quartet score with respect to the input trees.

Thus, one species, called the *query*, is not present in the backbone tree, and the goal is to insert the query species into the backbone. A typical use case of this problem is placing a new species onto an existing species tree (Fig. 1). Imagine that previous analyses have already produced a set of k gene trees on n species and an ASTRAL tree (inferred from those k gene trees). Now, a new species with genome-wide data has become available. To insert the new species onto the existing ASTRAL tree, we first add it to each of the k gene trees using existing tools such as `SEPP, pplacer,` or `EPA`. Then, we use the updated gene trees in addition to the existing ASTRAL tree as input to the quartet placement problem; the output will be a species tree with the new species included. Just like ASTRAL, the use of the quartet score ensures that the inferred position of the new species is a statistically consistent estimator of its true position under the MSC model (and given true gene trees).

INSTRAL (single query)

INSTRAL finds the optimal solution to the quartet placement problem. Unlike ASTRAL, the number of possible solutions to the placement problem is small (grows linearly with n), and thus, INSTRAL can solve the problem exactly even for large trees. In principle, it is possible to develop algorithms that compute the quartet score for all possible branches, one at a time, and to select the optimal solution at the end. However, the ASTRAL dynamic programming allows for a more straight-forward solution.

To adopt the ASTRAL algorithm for the placement problem, we only need to define the search space (set X) such that only trees that induce the backbone tree are allowed. INSTRAL achieves this by setting X to the set of all clusters in the backbone tree with the new species once added to the cluster and once not added. More precisely, let $\mathcal{B}(T)$ denote the set of all (including trivial) bipartitions of the backbone tree T with leaf-set L (each bipartition represented as a tuple of two sets) and let q be a set containing only the

Fig. 1. Left: The placement problem using gene trees. A backbone species tree with four leaves ($\{x, y, w, z\}$) and $k = 4$ gene trees are given; each gene tree also has new species (here, $\{A, B, C\}$). Top right: placing a single new species (A) on the backbone tree can be performed by finding the position with the maximum quartet score. Middle right: placing multiple species can be done by ordering them and placing them one at a time. Bottom right: alternatively, all new species can be placed independently and merging the results at the end (creating polytomies when multiple new species are placed on the same branch).

new species, then

$$X = \{q, L \cup q\} \cup \bigcup_{(A,B) \in \mathcal{B}(T)} \{A, B, A \cup q, B \cup q\} \,.$$

Thus, the number of clusters in this search space is $2 + 4(2n - 3)$. Once we define the set X in this way, the standard dynamic programming will solve the quartet placement problem exactly because the search space will include all possible placement of the query on the backbone tree and ASTRAL is guaranteed to find the optimal placement restricted to the search space. Since the search space of INSTRAL has size $\Theta(n)$, its running time increases as $\Theta(n.D) = O(n^2 k)$ where D is the sum of degrees of all *unique* nodes in the input gene trees (see Zhang et al., 2018, for details).

Adding multiple new species

If multiple queries are available, we can still attempt to use the basic INSTRAL algorithm in one of two ways (Fig. 1). *i*) We add all the new queries independently without trying to find their relationships. This approach is reasonable if the goal is to detect the identity of some unknown species or if the set of new species are expected not to belong to the same branches of the backbone tree. If needed, we can merge separate placements into a single tree, introducing polytomies wherever multiple queries are placed on the same branch. *ii*) We order the queries (arbitrarily or according to some criterion) and then add them to the backbone one at a time, updating the backbone tree each time to include the latest query. This ordered placement approach gives us the relationships between queries. However, like similar greedy algorithms (Desper and Gascuel, 2002), it is not guaranteed to find the optimal tree at the end.

The advantage in using the independent insertion approach is that adding m queries requires time that increases only linearly with m whereas the time needed for the ordered placement increases proportionally to m^3. The *de novo* execution of ASTRAL-III on $n + m$ species requires $O(((n + m)k)^{2.73})$ in the worst case but its mean time on actual data is typically close to $O(n^2 m^2 k^2)$ (Zhang et al., 2018). In contrast, INSTRAL-independent would run in $\Theta(m.D.n) = O(n^2 mk)$ and INSTRAL-ordered would require $O(n^2 m^3 k)$. Thus, the relative running time of ASTRAL-III and INSTRAL-ordered depend on values of n, m, and k, while INSTRAL-independent is always faster than ASTRAL-III.

Benchmark

Datasets. We first benchmark INSTRAL on simulated datasets previously generated by Mirarab and Warnow (2015). This dataset has 200 ingroups and an outgroup species and is generated using SimPhy (Mallo et al., 2015). By setting the maximum tree heights to 10^7, 2×10^6, or 5×10^5 generations, this dataset has created three model conditions with,

respectively, moderate, high, or very high levels of ILS; the average normalized Robinson and Foulds (1981) distance (RF) between true gene trees and the true species tree are $15\%, 34\%, 69\%$, respectively. In our experiments, we use gene trees inferred using FastTree-II (Price et al., 2010) from sequence data. These inferred trees have relatively high levels of gene tree error ($25\%, 31\%$ and 47% for the three model conditions). We have 100 replicates per condition, and each replicate has 1000 gene trees, from which we randomly sampled 200 and 50 gene trees to create three different input sets. Thus, in total, we have 9 model conditions (ILS level/# Gene). Following the original publication, three replicates were removed because their gene trees were extremely unresolved (Mirarab and Warnow, 2015); this leaves us with $9 \times 97 = 891$ replicates in total.

Leave-one-out experiments.

For each replicate of this dataset, an ASTRAL species tree inferred from gene trees is available. For each of the 200 ingroup species in each replicate, we prune it from the ASTRAL tree and use INSTRAL to add it back onto the tree, using FastTree gene trees as input. Thus, overall, we have $891 \times 200 = 1.782 \times 10^5$ independent placements. When there are multiple placements with equal quartet scores (happens in only 63 cases), we break ties similarly to the full backbone ASTRAL tree.

Among all of these placements, in only 316 cases ($< 0.2\%$) the output trees have different quartet scores compared to the original ASTRAL tree. Note that INSTRAL is guaranteed to find the optimal placement, and theretofore, its quartet score is always at least as good as the ASTRAL tree. Thus, these 316 cases are those where ASTRAL has failed to find the optimal placement for a species. We note that 178 out of 316 cases correspond to the model condition with very high ILS and only 50 genes. Increasing the number of genes or reducing the amount of ILS decrease the number of cases where ASTRAL is sub-optimal (Table 1). For example, with moderate and 1000 genes, only 4 out of 20,000 placements using INSTRAL improved quartet scores compared to ASTRAL.

Table 1. For each condition, we show three numbers: the number of cases where the INSTRAL tree has a different (i.e., higher) quartet score than the ASTRAL tree, cases where the INSTRAL tree has a different RF distance to the true tree compared to the backbone ASTRAL tree, and number of cases where INSTRAL has an *improved* RF compared to ASTRAL. All numbers are out of 20,000 insertions, except for very high ILS, which is out of 19,400.

	50 genes	200 genes	1000 genes
Very high ILS	178/140/26	41/33/7	19/12/6
High ILS	41/ 31/13	12/ 8/5	5/ 3/2
Moderate ILS	11/ 8/ 1	5/ 3/0	4/ 4/0

Importantly, only 176 out of 316 cases result in any change in the RF distance of the inferred tree compared to the true tree, and only in 59 out of 176 cases did INSTRAL reduce the RF distance compared to ASTRAL. Thus, overall, removing and adding back a species generates results that are very consistent with the ASTRAL tree.

Ordered placement.

To see if the agreement with ASTRAL remains if more species are placed using INSTRAL, we perform a second experiment. Here, we first prune a portion ($\frac{1}{4}$, $\frac{1}{2}$, or $\frac{3}{4}$) of species from the ASTRAL species tree, order removed species randomly, and then place them one after another on the backbone tree, updating the backbone tree each time (as in ordered placement in Fig. 1). In the end, we have a tree on the full leaf-set; this tree, which we call the INSTRAL tree, can be thought of as a greedy solution to the same problem ASTRAL seeks to solve.

Comparing RF distances of the ASTRAL tree and the INSTRAL tree to the true tree, we observe that the two trees have similar accuracy, but ASTRAL is somewhat more accurate in the hardest conditions (Fig. 2). Overall, the RF error of ASTRAL is on average 0.3% lower than INSTRAL (corresponding to roughly half an edge) and these improvements are statistically significant ($p \ll 10^{-6}$). Among all 2,673 INSTRAL trees that we have computed, 1,470 have RF distances to the true tree that are identical to the ASTRAL tree. Differences in the RF distance are seen more often among replicates with

Fig. 2. ΔRF : The change in the RF distance with respect to the true tree when going from ASTRAL to INSTRAL. Results are shown for all three model conditions with moderate, high and very high ILS (boxes), numbers of genes (colors), and the size of the starting tree (51, 101 and 151 respectively). Each boxplot shows distributions over 100 replicates, except for very high ILS, where it is over 97 replicats.

very high ILS (mean RF difference: 0.7%), 50 genes (mean RF difference: 0.7%), or smaller starting trees with 1/4 of the species (mean RF difference: 0.6%). Increasing the number of genes, increasing the size of the starting tree, and reducing the ILS reduce the number of mismatches between ASTRAL and INSTRAL (Fig. 2).

Unlike the case of single insertion, when we use INSTRAL to add multiple species, the quartet score of INSTRAL can be higher or lower than ASTRAL. Overall, when the two trees do not agree, ASTRAL tends to have higher quartet scores (Figs. 3 and S1). Out of 2,673 cases, ASTRAL has higher quartet scores in 1,210 cases cases while INSTRAL is better in 231 (they tie in the remaining 1,232). Reducing the number of genes and increasing the level of ILS both magnify the improvements of ASTRAL compared to INSTRAL.

Finally, focusing on the running time, we observe that the running time of adding new species to a tree grows as the backbone grows and the number of genes increases (Fig. S2). The highest running is 17 seconds, corresponding to 1000 gene trees, very high ILS, and placing a new species on a backbone with 200 species. In comparison, when the backbone has 51 species, the running time is only 3 seconds on average. As expected, the

Fig. 3. Change in quartet score versus change in RF distance between ASTRAL and INSTRAL-ordered. Results are shown for all model conditions and the backbone portion of 1/4. The small red bars on the x and y axes is the projection of data on both axes and represents the distribution of data on each axis. See Figure S1 for other backbone sizes.

running grows faster than lineally with the size of the backbone (Fig. S2). The total running time to go from a starting tree of 50 species to 200 species is on average 56 minutes.

Biological Examples

We have tested INSTRAL on three biological datasets: two transcriptomic datasets on insects by Misof et al. (2014) and plants by (Wickett et al., 2014), and a genomic avian dataset by Jarvis et al. (2014). The insect dataset includes 1,478 protein-coding genes from 144 species spanning all of the insect diversity and has been recently re-analyzed using ASTRAL by Sayyari et al. (2017). The plant dataset includes 103 species and 424 genes, and the original study reported an ASTRAL tree. The avian dataset consists of 48 genomes representing all the orders of birds. For this dataset, statistical binning was used to build 2022 supergene trees (Mirarab et al., 2014a) and Sayyari and Mirarab (2016b)

Table 2. The RF distance between ASTRAL and INSTRAL trees on biological datasets as well as the change in the quartet score (INSTRAL-ASTRAL).

	Avian	Insects	1KP
RF	1/45	2/141	2/100
QS	-0.00000022	-0.00000264	-0.00000225

have published an ASTRAL tree on these super gene trees. Among these datasets, the avian dataset has extremely high levels of gene tree discordance. For each of these datasets, we removed leaves of the species tree one by one and placed back to the backbone tree using INSTRAL. In every case, INSTRAL found the same position for the new species as the backbone ASTRAL tree.

We also tried ordered placement, where were randomly selected half of the leaves, removed them, ordered them, and inserted them back on the remaining part of the tree using INSTRAL. Using this procedure, at most two branches change compared to the backbone ASTRAL tree. For example, in the avian tree, the extremely unstable taxon (Jarvis et al., 2014) Hoatzin moves by one branch in the INSTRAL tree. In the case of plants, one of the algal Zygnematales species (*M. endlicherianum*) moves two branches. The resulting INSTRAL trees have very small reductions in quartet scores compared to ASTRAL trees (Table 2).

AVAILABILITY

INSTRAL is open-source and freely available on github (https://github.com/maryamrabiee/INSTRAL). It is implemented in Java with straight-forward installation (the only dependency is Java 6+). A template tutorial and instructions to run INSTRAL is given also. The generated data, scripts to generate those data and results given in this paper are also available on github (https://github.com/maryamrabiee/INSTRAL-results).

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Supplement

Fig. S1. ΔQS of the output trees of the two methods based on ΔRF in all model conditions and with different backbone trees containing 1/4, 1/2 and 3/4 of the species. The red tone on the x and y axes is the projection of data on both axes and represents the distribution of data on each axis.

Fig. S2. The running time of ordered placement based on size of backbone tree for very high ILS model condition and the speciation rate equal to 0.000001 (50 replicates)