1 **Network organization of antibody interactions in sequence and structure space: the**
2 **RADARS model**
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4 József Prechl
5
6 Diagnosticum zrt, Attila u. 126, Budapest, Hungary
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8 Correspondence: jprechl@gmail.com

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Keywords: antibody; network; sequence; structure; clonality; B cell; systems biology;
quantitative biology, immunodominance

Abstract

Adaptive immunity in vertebrates represents a complex network of protein interactions that

develops throughout the lifetime of an individual. Based on the key molecule of humoral

adaptive immunity, the antibody, development of this system comprises molecular genetic,

cell biologic and immunologic mechanisms, and as a network the system is likely governed

and can be characterized by physical rules as well. While deep sequencing can provide vast

amounts of data related primarily to clonal relationships, functional interpretation of such

data is hampered by the inherent limitations of converting sequence to structure to function.

In this paper a novel model of antibody interaction space and network, termed radial

adjustment of system resolution, or RADARS, is proposed. The model is based on the radial

growth of resolution of molecular recognition, corresponding to increasing affinity of

immune reactivity, and the virtual infinity of directions of growth, corresponding to the

ability to respond to almost any molecular structure. Levels of interaction strength appear as

shells of the sphere representing the system, with decreasing frequencies of interactions. B-

cell development and immune responses can be interpreted in the model and quantitative

properties of the antibody network can be inferred from the physical properties of a quasi-

spherical system growing multi-radially. The thermodynamic system is described by a power-

law distribution with a network exponent of phi square, representing a scale-free network of

antibody interactions.

Thus, the RADARS model suggests that an absolute sequence space is reduced to a

thermodynamically viable structure space by means of a network of interactions.

Understanding such quantitative network properties of the system should help the

organization of sequence-derived structural data, offering the possibility to relate sequence to

function in a complex, self-organizing biological system.

1. Introduction

Appearance of complex multicellular life was accompanied by the evolution of a system that maintains cellular and molecular integrity in the host organism (1). The adaptive immune system is a complex system in the physical sense, being composed of a vast number of cells that engage in interactions, self-organize and - most impressively - adapt to the molecular and cellular environment. In fact, the host is more than an organism: a supraorganism (2,3) with microbial communities, and immunity maintains a continuity of interactions rather than simply discriminating self from non-self (4). Technological advances now allow us to measure and characterize this complexity in ever growing details, at the gene, transcript, protein and cellular levels, driving the field of systems immunology (5). The vast amount of data generated requires not only data storage and analysis capacity, but also theoretical frameworks, models that simplify data organization and systems level interpretation. Humoral adaptive immunity comprises the cells and mechanisms that lead to the production of antibodies. In human adults B-cells develop in the bone marrow throughout life and build up a system of effector and memory cells, which accumulate as a lifetime of immunological experiences. Continuously emerging naive B cells only differentiate further if selected for immunological actions based on their B-cell antigen receptor (BCR) specificity. Because this specificity is genetically coded in the individually rearranged immunoglobulin heavy and light chain sequences, it is possible to capture the antibody repertoire in a given sample of B cells. Deep sequencing or next generation sequencing (NGS) is capable of generating sequence data of antibody repertoires with varying resolution and length (6–10).

It is also possible to profile the antibody repertoire functionally, based on the identification of antibodies binding to huge sets of potential targets (11,12). This approach is biased by the fact that a priori knowledge of targets is not always possible and only those antibodies that bind to the tested antigens are identified. Antigen microarray assays are useful for the focused analysis of antibodies related to allergy, autoimmunity, infection or cancer (13–17). Such functional analyses provide a more meaningful profile in the immunological sense and if carried out from blood it is less prone to sampling error than cell-based sequencing approaches.

The relationship between antibody sequence and structure is on one hand like that of proteins in general: polypeptide chains of a given sequence fold into structures, which are responsible for function. In the enormous sequence space allowed by permutating amino acids only the thermodynamically stable structures materialize as proteins (18). Proteins capable of

interacting with molecules in a way that improves chances of survival of the host organism
will themselves survive and evolve. Unlike proteins in general, antibodies evolve within the
lifetime of the host. While thermodynamic constraints still hold, their "survival", meaning the
producing cell clone being selected into long-lived B-cell populations, is determined by
interactions with self and foreign molecules, the antigens. Importantly, because there are so
many more sequences than structures and because changing a few critical amino acids can
result in different structures, mapping sequence space to structure space in far from trivial.
The combined length of the complementarity determining regions (CDR) of heavy and light
immunoglobulin chains is around 14-50 amino acids (IMGT definition (19)). By employing
screening and selection mechanisms, coupled with cycles of random mutagenesis, targeting
primarily these amino acids, the immune system is capable of developing high-affinity
binders against most targets. Understanding these processes on the systems level preferably
requires the prediction of structures from NGS data (20) because of the complex sequence-to-
space relationship, as noted above. The architecture and functioning of complex systems can
be assessed by network science, which in the case of antibodies identifies antibody-antigen
interaction networks (21). The development of concepts of the immune system as a network
were key steps in our current perception of immunity (22,23). Efforts are now under way to
describe the immune system as a network (termed network systems immunology) using NGS
data and network science (24). Since the system is organized by structure rather than
sequence, the conceptualization of an antibody interaction network based on physical
properties should help better definition of the system.
In this paper, following a brief introduction to the sequence space of antibodies, a model for
the molecular organization of antibody structure space or interaction space is proposed. The
model builds on the generalized quantitative model of antibody homeostasis (25–27), thus
approaches antibody function from the physico-chemical perspective: antibodies are
organized into a network by binding affinity to cognate target. The model also considers the
architecture of B-cell development and hierarchy and provides a power law-based
quantitative network description of the humoral immune system.
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2. Antibody clonal network representation in sequence space

Sequence space in the biological sense is a theoretical space comprising collections of nucleic acid or protein sequences of interest. We usually talk about protein sequence space and define what protein sets are involved (proteome of a given species, cells, etc.) and whether any restrictions hold (fully random, functional, identified, etc.). An amino acid sequence with a given length 'd' and full randomization with 20 amino acids occupies a sequence space $20^{\wedge}d$ (Fig 1A). An exact sequence with no ambiguity defines an exact position in sequence space; moves in this space are discrete steps along a given dimension. As the figure suggests, it is impossible to visualize high-dimensional protein space in 2D. Exponential growth is incredibly fast, leading to the generation of vast amounts of space in high dimensions. It is accepted that only a fraction of all theoretically possible sequences are thermodynamically stable and protein evolution can be interpreted as a search for acceptable and functional structures in sequence and structure space (18). Thinking along these lines, the evolution of antibody binding surface, the paratope, is a search for the thermodynamically stable sequences and the selection from among these the ones meeting immunological criteria for B-cell survival. The set of viable antibody sequences, functional antibody sequence space, lies much below the theoretically possible (28) and close to the already observed and annotated antibody sequence space (29). Collections of antibody protein sequences obtained by translating DNA or RNA of deep sequencing data ideally span the whole variable domain of heavy (VH) and light chains (VL) and can also pair these two. In such a case the gene segments contributing to the rearrangement of VH and VL can be predicted and visualized in 3D and 2D respectively, as shown (Figure 1B). A repertoire can be represented by identifying coordinates of rearrangements identified, and symbol size or color can represent segment frequencies (30). While the use of gene segments for classification allows tremendous reduction in dimensionality, it is not best suited for functional network analysis, where the use of complete rearranged and mutated sequences is preferable (31). In a much simpler approach, heavy chain CDR3 regions only are used as an estimate of diversity. Though this region is often regarded as being most important for determining binding specificity, identical H-CDR3 sequences have been found to be present in functionally unrelated cells and therefore H-CDR3 seems insufficient for functional classification (32). Selection of the pre-BCR bearing cells depends on signals that may be triggered by ubiquitous ligands present in the bone marrow microenvironment. The presence

of uniform reactivity against such common public self-antigens may lead to the positive

selection of CDR3 with similar binding properties, and thereby similar sequences.

Sequencing of the complete heavy chain variable domains can be readily used to follow

changes in repertoire size and diversity during B-cell development and response to

immunization (33).

Whatever the depth and methodology, sequence similarity relationships can be used for the

construction of family trees, often displayed in circular forms. These trees usually start

classification with the V segment, clustering clones with common V use (34). While this

approach may be useful for classification, the use of the complete VDJ-H sequence as a first

stage classifier, followed by VJ-L use better reflects the natural development scheme of B

cells (Fig 1C).

Antibody repertoire sequencing now follows guidelines to help the integration of data (35–

37), several tools and databases devoted especially for these data have been established

(7,9,38–40).

3. Antibody interaction network representation in structure space

In contrast to this graded qualitative scheme, which may well serve the purpose of tracking

peripheral clonal expansions accompanied by affinity maturation, a quantitative scheme

should place genetic changes into structure rather than sequence space. Furthermore, because

it is not just antibody structure but also the availability of targets and the structure of those

targets that determine the development of antibody repertoire and the architecture of the

network, we shall talk about interaction space, as explained below.

3.1. Structural resolution of molecular recognition as a measure of interaction strength

While sequence can be defined with various levels of certainty of an amino acid occupying a

given position in the sequence, molecular structure can be defined at various levels of

resolution. As we are talking about antibody molecules structural resolution is on the atomic

scale, crystal structures define atomic coordinates on the Ängstrom scale. The binding site of

an antibody can also be characterized by the surface area that comes into close contact with

the antigen (41,42). Water molecules are displaced from this area as a function of the

goodness of fit. The so-called buried surface area (BSA) is therefore a good predictor of

binding energy of protein interactions (43). Another measure of goodness of fit is the

decrease of free energy of the antibody molecule upon binding. All these approaches are

correlated: higher resolution "description" of a structure by the antibody corresponds to

greater BSA and to a higher binding energy. In other words, the resolution of molecular

recognition is the goodness of fit in terms of number and strength of non-covalent bonds

forming between antibody and target and can be expressed as standard free energy change or

as equilibrium constant of binding. The advantage of using thermodynamic description for

the characterization of structural resolution is that it conveys the sense of function: higher

binding energy means higher affinity of antibody to target, which in turn means more

efficient clearance (27). Besides defining resolution of molecular recognition, which is a

general descriptor, the identification of a given interaction requires the description of target

shape, a distinct molecular structure. The higher the resolution the more information is

required for defining shape, translating into a better fit between antibody and target.

Going in the opposite direction, by decreasing the resolution of interaction, we can reach a

theoretical minimum. At this minimum all interactions are defined by a single identical

quantity of interaction strength. Let this quantity be 1, so that an equilibrium constant with

the value 1 can represent the lowest possible resolution.

As standard free energy change is defined as

$\Delta G° = -RT \ln K_A$

where R is the universal gas constant and T is thermodynamic temperature. By using RT as

the unit of energy, called nat, we obtain

$\Delta G°_{nat} = -\ln K_A$

standard free energy change expressed in mol nats, thereby simplifying further formulas.

Using $\Delta G°_{nat}$ as a measure of resolution, at the minimal resolution binding to any target is

possible and can be interpreted as minimal random contact upon collision of molecules, with

the value being 0. This minimal resolution characterizes the center of the system, represented

by the center of interaction space in Figure 2. By starting to increase resolution we shall be

able to distinguish between different shapes, the higher the resolution the more shapes

becoming distinct. Because of the structural complexity of an antibody binding surface area,

the distinction between all possible shapes at high resolution would require a

multidimensional space. Let us gradually generate a multidimensional interaction space by

considering a point of origin, the center of the system, from which a particular direction

represents a particular shape. In this representation the extent by which we leave the point of

origin corresponds to the resolution at which we can define the direction. Thus, going away

from the minimal resolution of 0 we can define shape at gradually higher resolutions,

corresponding to larger free energy decrease of the interacting molecule (Fig. 2A,B).

Different levels of resolution, that is different levels of binding energies appear in our scheme
as shells of a sphere. Theoretically the number of directions originating from a single point is
infinite, so the shapes available in this representation are also infinite if we go far enough.
The other way round, higher resolution of molecular recognition is required to distinguish
two similar antigenic structures. Practically, considering a reversible interaction, the
resolution is limited by the binding energy of reversible interactions. Beyond this limit
structure of the binding partners becomes fixed, rigid, corresponding to covalent binding.
This model of the evolution of interactions of a system we shall call 'RAdial ADjustment of
System Resolution' or RADARS in short. The abbreviation intentionally reminds of
radiolocation, where emitted electromagnetic waves interact with objects in their way and are
reflected to provide a virtual image of the surrounding. The RADARS model implies that
elements of the growing system interact with the surroundings, gaining information and
adjusting system growth accordingly.

3.2. B-cell development in interaction space

Immunological interpretation of the model requires us to fit B-cell development and antibody
network evolution into this interaction space. We shall assume that a common lymphoid
progenitor has the potential to generate any and all functional VDJ-VJ sequences and
therefore to produce via sequential differentiation and maturations steps antibody against any
and all targets. By functional VDJ-VJ sequences we mean all sequences that are physically
and biologically viable. This means thermodynamic stability (able to fold into a structure
compatible with the Ig domain), ability to pair, forming a VH-VL functional binding unit,
and ability to sustain a B-cell via delivering survival, differentiation and proliferation signals.
A differentiation step that reduces this total potential introduces restrictions in structural
space. This will appear as a step towards increased resolution of cognate target structure.
Expression of the surrogate light chain (SLC) marks the first step towards BCR formation.
These pro-B cells represent the founders of all B cells (Fig. 2C). While signaling via the SLC
may be required, it is uncertain whether binding of SLC is required for further differentiation,
therefore we assume that these cells seed the complete antibody interaction space.
Rearrangement of the heavy chain introduces a structural restriction: a particular functional
heavy chain variable domain (VH) sequence has a limited range of targets. Pre-B cells
displaying the pre-BCR composed of VH-SLC pairs will divide until and as long as ligands
(antigens) are available. Cells with different VH sequences will populate the structural space
and share this space according to the availability of target. Cells with more abundant targets
expand more, cells with less frequent targets remain in lower numbers, until optimal BCR

engagement is achieved (25). As a result, interaction space as represented at this resolution

will be filled with different pre-B cell clones according to the availability of the common

self-antigens.

The next level of interaction resolution, as well as the next level of restriction of binding

space, comes with the rearrangement of the light chain. Individual pre-B cells rearrange their

light chains independently and randomly. Therefore, all pre-B cells reserve a particular area

on the next level of structural resolution. The size of this area again will correspond to the

nature of the rearranged VL domain, with those finding more available targets expanding

more. The pool of immature B cells fills thus the outer level of resolution in the bone marrow

(Fig. 2C).

Taking a somewhat unique route of differentiation are the B1 cells. These cells seem to

generate antibodies that keep B1 cells in a continuous state of low-level activation. This may

reflect their ability to respond to soluble, highly abundant antigens (25), or an intrinsic ability

of the BCR of sustained signaling, perhaps due to structural properties (44). In any case, B1

cells represent a stable population with the highest affinity towards self and non-self, which is

achieved without affinity maturation. Meanwhile B2 cells are continuously generated but die

in a few days unless recruited as effector cells for further differentiation (Fig. 2C).

To allow for an even balance between differentiation and division we can employ a Fibonacci

branching scheme in our model: every division yields a cell that can divide further and

another one that differentiates (Fig. 2C). Assuming equal time and energy investments for

division and differentiation this scheme results in a Fibonacci series number of cells after

every time unit. In our model dividing cells remain on the same level of resolution,

differentiating cells move outwards if interaction resolution grows, in a hierarchy similar to

that proposed by Derényi (45). To maintain cell numbers in all levels of differentiation the

ratio of differentiation rates is proposed to be the average of ϕ rate expansion and no

expansion,

differentiation rate ratio $\lambda = (\phi+1)/2 = \phi^2/2$

This practically means that at a given level of differentiation for every 2 incoming cells there

are $\phi+1$ outgoing cells. The distribution of cells in interaction space will be determined by the

rate of division and differentiation involving random sequence generation pruned by

interaction-based selection events.

As implied above, selection in the bone marrow is a passive process: randomly generated

sequences find their positions in the structural space, expanding according to the availability

of fitting target structures. As a result, the emerging population of immature B cells will bear

the low-resolution antigenic signature of the bone marrow environment. This can be

interpreted both as deletion of highly self-reactive clones to prevent autoimmunity (46), and

as selection for mildly autoreactive clones to help homeostatic antibody functions and setting

a reference for recognition of non-self (47).

3.3. Immune response in interaction space

The development of cells reacting with antigens that are only temporarily present in the host

presents the risk of investing energy into clones that will become useless once that antigen

disappears. Therefore, such clonal expansions beyond the border of self only takes place

when 2nd signals inform the host of danger. This is the development of an immune response,

aided by various molecular and cellular help signals. Thymus independent and primary

thymus dependent responses expand populations of B cells without improving their affinity,

thus keeping them on the same level in the interaction space. We shall call these cells effector

B cells. Thymus dependent responses aided by helper T cells lead to the formation of

germinal centers where affinity maturation takes place. This adjustment of affinity focuses

interactions into a particular direction, shape in our model, leading to increased resolution of

interaction space only in that direction. In this region of interaction space, affinity and

corresponding resolution of target recognition is high, but once target is cleared cells go into

dormancy. These are the memory B cells that conserve the genetic information acquired

during affinity maturation but minimize their activity: no divisions, no antibody secretion;

remaining guards against future encounter with the same or similar target (Fig. 2C). Another

set of cells that remains after target has been cleared is plasma cells, which presumably arise

from high-affinity effector cells finding appropriate niche for long-term survival.

4. Characterization of the antibody interaction network

4.1 Distribution of binding energies

The cell biological aspects of the RADARS model are summarized in Figure 3A. Expansion

and differentiation of cells originating from CLPs create a cellular repertoire in the bone

marrow, then further expansions and differentiation steps increase this repertoire and

supplement it with antibody secretion. While selection starts in the bone marrow, events in

the periphery show more self-organization because interactions with the outside molecular

world begins to take control.

Further differentiation into higher resolution of structure space along $\Delta G°_{nat}$ (Fig. 3B) is

accompanied by competition between clones via antibody secretion overlapping in structure

space.

Deduction of network properties requires the knowledge of distributions of nodes and their

connectivity. We shall make two assumptions here regarding these parameters.

Universal laws governing the distribution of binding energies for biomolecular recognition

have been uncovered by Zheng and Wang (48). Based on energy landscape theory they

suggest that binding free energy ΔG follows a Gaussian distribution, while the equilibrium

constant K_A follows a log-normal distribution, accordingly. The mean interaction energy μ

corresponds to the median e^{μ} of equilibrium constant. The continuous removal of target

antigens requires the continuous production of antibodies and maintenance of a reaction

quotient Q, which we will also assume to follow a lognormal distribution. The free energy of

interactions is given by

$\Delta_r G = \ln(Q/K_A)$ $(N_A nat)$

And it follows that Q/K_A is the exponential of interaction free energy $e^{\Delta_r G}$, which then again

possesses lognormal distribution.

If B cell differentiation takes place in this interaction energy space, then network nodes will

be individual B cell clones, generated along the $\Delta G°$ radius at $\lambda = \phi^2/2$ steps. Reed (49),

Mitzenmacher (50) and Newman (51), described that the exponential sampling of lognormal

distributions produces power law distribution with two tails, called double-Pareto

distribution. If we apply their approach to our model by sampling K_A at λ rate then the

resulting power law relationship above the mean $\mu=0$, $e^{\mu}=1$

$$f(x) \approx x^{-1-\sqrt{2\lambda}} \quad , x>1$$

defines the probability density of interaction energies (Fig.3B).

To position our distribution in the dimensions of standard free energy and mean binding

energy, we shall assume a median K_A of 10^5, which is close to -30kJ/mol standard free

energy. This is the lower limit of BCR sensitivity, so it makes sense to distinguish molecular

structures above this value (52). Mean binding energy, the energy gap between native

configuration and the average unbinding states in the universal binding energy distribution

model (48), corresponds to the average binding energy of antibodies. Figure 3B suggests that

this is around 5 mol nats, which is 12.8 kJ/mol.

4.2 A scale-free network of interactions

The model presented so far follows a view of the system growing outwards, with cells

supplied from within and extending into the world of antigens. However, we can turn this

view inside out, as shown in Figure 4, interpreting the events as the immune system being

outside and developing inwards. Practically this means that we use K_D instead of K_A as a

measure for the system. Though it is more difficult to visualize a system that grows inwards,

this view helps our perception of the developing antibody network.

In the immune-side out view of the RADARS model distance from the outside boundary of

the system represents resolution of molecular recognition, which is now K_D. Directions still

correspond to theoretical targets: individual molecular shapes. If all these targets have

binding energy distributions as predicted by the universal distribution model, then our

interaction space will represent a collection of these statistical distributions.

The RADARS model suggests that the greater the resolution of structural recognition the

more restricted is the number of shapes recognized. However, with the development of high

affinity clones the ability to react with related structures also grows, a phenomenon called

cross reactivity. The further the system grows in a given direction the more focused is the

recognition of cognate target but affinity to related structures inevitably grows as well. This is

not mere polyreactivity, however, but rather organized cross-reactivity. With the supply of B-

cell precursors outside and the organization of antigen removal inside, we can best interpret

effector antibody function as an antigen sink (Fig.4). In this sink multiple sinkholes develop

as the immune system matures. The sinkholes themselves correspond to immunodominant

epitopes: structures preferred by the system as targets.

Substituting $\phi^2/2$ for λ in the double Pareto distribution we obtain the probability distribution

function of the antibody interaction network according to the RADARS model:

$$f(x) \approx k^{-1-\varphi} \qquad , k>1$$

where k is $e^{\Delta rG-\Delta rG}$, related to the energy of interaction relative to the mean interaction energy

in the system (Fig. 5). Owing to the special property of ϕ that $\phi+1=\phi^2$, the slope of the

complementary cumulative distribution and the average degree are equal to ϕ itself.

Essentially antibody interactions characterized by standard free energy above the system

mean and interaction energy above system mean constitute a scale-free network. This scale-

free network is an energy transfer system physically and an antigen transfer system

immunologically. This is an optimization of antibody differentiation in the sense that the

minimal number of high free energy antibodies (network hubs) are used for the removal of

the maximal number of antigens, covering the maximum of immunologically relevant

structure space.

The immunological implication of the RADARS model is that the naive B-cell repertoire

generates a very low affinity image of the human antigenome available in the bone marrow

environment. Once exiting the bone marrow a low affinity image of immunological self is

generated by secreted antibodies. Such an image has been called the immunological

humunculus, as an analogy to the representation of human body in the brain cortex (53).

While this property of the repertoire often leads investigators to conclude that autoreactive

antibodies are enriched in the naive and B1 repertoire, the practical use is quite obvious, as

has been suggested by Irun Cohen (47). Telling the difference between molecular structural

self and non-self can be quite easy if the difference is striking. For identifying small

differences, it is useful to have a starting repertoire that represents self and then increase

resolution only in regions where encountered dangerous structures show up in structural

space. The importance of self-recognition has also been recognized in natural antibody-

mediated physiological functions (27,54).

The generation of an antibody network, with network hubs represented by plasma cells

secreting antibodies, reveals the physical aspect of the system: all interactions of such an

antibody contribute to the clearance of many target antigens sharing structural homology but

at an ever-decreasing efficiency as we move away in structure space. A new node in the

network, a new B cell in the structure space, will preferentially attach to an existing

subnetwork as a low-affinity clone, in agreement with the preferential attachment model of

growth in scale-free networks (55). Preferential attachment may explain immunodominance

and antigenic sin, phenomena arising from the preference of the immune system for known

epitopes, which correspond to hubs in the network.

Merging sequence space to interaction space

Network theory has always been considered as a key to understand and define immunity on a

systems level. The network hypothesis of Niels Jerne (22), its modified version leading to the

concept of clonal selection (56), mathematical and computational simulations (57,58),

various re-interpretations (23), experimental approaches using NGS (24,31) or antigen

microarrays (21) all strive to describe this highly complex system as connected elements of a

network. There are two new aspects of the RADARS model that may improve our view of

this network. First, it introduces physical units, binding energy, as the measure of interactions

and as a measure of system architecture. Natural networks are formed as a result of energy

dispersal (59,60), therefore network theories should consider energy transduction in the

system. Second, it proposes a value for the power-law relationship of division rates between

levels of differentiation, and an architecture for the whole network, characterized by the

double-Pareto distribution.

The network architecture of antibody repertoires was recently computed based on high-

throughput sequencing data from more than 100.000 unique antibody sequences (24). This

study revealed that pre-B cell and naïve B-cell clones form homogenously interconnected

assortative networks, in contrast to the disassortative networks of plasma cell clones, which

covered smaller but more focused regions of sequence space. This contrasting behavior of

antigen-naïve and antigen experienced, post-germinal center B cells corresponds to the

antibody-centric view in our model. The low-affinity region with developing B-cells is

homogenously interconnected by clonal relationships and shared usage of gene segments

(Fig.2 and 3). The high affinity side of the distribution is the narrowing, focusing interaction

space of plasma cells.

Considering that our technological capability is ripe for the high-resolution determination and

comprehensive analysis of antibody sequence space, current efforts focus on the conversion

of sequence space data into datasets in interaction space. By providing a physical and

mathematical description the RADARS model may help in the final integration of data.

The model also suggests sequence-based network properties of early B-cell developmental

stages also need to be determined (24), in addition to the mature and antigen-experienced

repertoire (61), and comprehensive and selective analysis of the B1 repertoire is very

important for capturing network properties of the system.

The model presented here depicts an ideal state of the system of antibody interactions. It is

the fluctuations and disturbances in the system that we observe as immune response during

infections, and distortions are autoimmunity and allergy. Besides suggesting how antibody

sequence space fits into structural space and into an interaction network, the model may

potentially lead to the ability to model whole immune system and simulate its functioning.

Acknowledgments

The paper is dedicated to my first mentor in molecular biology and antibody cloning, István

Kurucz. The author is partly supported by VEKOP 2.1.1 grant to Diagnosticum. I wish to

thank István Csabai for reading and discussing the manuscript and anonymous referees for

their constructive criticism.

Author contributions

J.P. developed theoretical model, designed and prepared figures, wrote paper

Conflicts of interest

The author declares no conflict of interest.

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dimensions	1	2	3	n	250
values	2	2	2	x	20
system size	2^1	2^2	2^3	x^n	20^{250}

Figure 1. Sequence space and visualization of antibody combinatorial relationships
A) Theoretical diversity of a sequence is determined by its length and the number of values a particular position in the sequence can take. More than 3 dimensions are difficult to visualize in 2D. An antibody Fv region of 250 amino acids has an astronomical sequence diversity if full randomization is allowed. If the sequences are exact the positions in sequence space are discrete, but there are no structurally meaningful directions or distances in the multidimensional space.

Figure 1
B) Antibody sequences are frequently interpreted as recombined germline sequences. This approach allows the simplified display of repertoires obtained by NGS, preferably with paired heavy and light chain VD identification. Such a display of combinatorial diversity may allow the tracking of specific clonal expansions and further diversification by SHM but reveals little about the overall functional network of interactions.
C) The potential development scheme of a given antibody clone is shown with antibody sequence development along with B-cell differentiation steps. Arching arrows represent combinatorial diversification by V-D-J rearrangement and light chain paring.

A

dimensions   ~ e^r

values   ~ sphere surface ~ $r^{\wedge 2}$

system size N   ~ $e^{r^{\wedge 2}}$

B

$\ln K_A$ ~$\Delta G°$ ~BSA

r

Figure 2.

C) Systemic organization of antibody evolution.

The evolution of the system of antibodies can be interpreted as clones filling the interaction space at various levels of resolution. Along this pathway cells continually increase their specificity and affinity towards their target direction. A common lymphoid progenitor has the potential to develop antibody against any target, equivalent to a radius of ln(1)=0. Differentiation proceeds outwards from this point of origin, the center of the network. At every level of differentiation asymmetric divisions fill the level with a clone, expansion being dictated by antigen driven selection of clones with ideal receptor engagement. Accordingly, pre-B cells expand based on the ability of rearranged HVD to pair with SLC and signal for clonal expansion. The generated cells rearrange their LVD and exit bone marrow. Primary TD responses and TI responses expand B2 or B1 cells without further evolution of antibody binding. TD responses allow further directed differentiation in germinal centers. B2 cells are continuously generated and only survive if recruited for specific immune responses. B1 cells, on the contrary, survive in an activated state producing antibodies and dividing rapidly upon activation. Effector cells from clonal expnsions can establish long lived plasma cells if they arrive in the required niche.

Different colors stand for structural differences and relationships.

Figure 3. Predicted interaction properties of the humoral immune system.
A) Clonal network development of the humoral immune system, shown as a cumulative distribution function of evolving antibody clones. Self-organizing system in the bone marrow meets environment in the periphery to maintain immunological self and generate immunological antibody profile. ,r' represents the radius of the system. B) Double-Pareto distribution of antibody interaction free energies in the system. Differentiation of B cells out of the bone marrow is driven by antigen. Here antibodies with increasing standard free energy, as represented by DG°nat, bind to available targets with increasing tendency to decrease their free energy and achieve a conformation as close to the native bound form as possible. As a consequence antibodies also bind to targets in nearby structure space, a phenomenon called cross-reactivity. Cross-reactivity generates a network of interactions governed by the expansion of the immune system into this structure space. The system is thus defined by Gibbs free energy of reactions and standard free energy of interacting antibody.
*somatic hypermutations; CLP, common lymphoid progenitor; immat., immature; B2eff, effector B2 cell; Bmem, memory B cell; PC, plasma cell

Figure 4. Antibody-centric and antigen-centric views of the organization of adaptive humoral immunity.

The antibody-centric view (A) corresponds to the clonal development and expansion of B cells, with a radius of $lnKA=\Delta G°nat$. We can turn the system inside out to obtain an antigen-centric view (B), where the system grows „inwards" with a radius corresponding to $lnKD$. In this representation the development of antibodies with higher affinity pull antigen down an antigen sink with increasing efficiency.

Figure 5. Properties of the antibody interaction network.
Degree distribution of the antibody network corresponds to the relative free energy of antibody interactions and can be expressed as e^{DG}. Because of the special properties of phi, the degree exponent, the average degree, and the slope of the complementary cumulative distribution can all be xepressed using phi. Note that because of the inverse relationship between KA and KD, which determines frequency, the same scale is used as in figure 3 but with negative values.

Graphical abstract