TITLE:

Inference of recombination maps from a single pair of genomes and its application to archaic samples

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ABSTRACT:

Understanding the causes and consequences of recombination rate evolution is a fundamental goal in genetics that requires recombination maps from across the tree of life. Since statistical inference of recombination maps typically depends on large samples, reaching out studies to non-model organisms requires alternative tools. Here we extend the sequentially Markovian coalescent model to jointly infer demography and the variation in recombination along a pair of genomes. Using extensive simulations and sequence data from humans, fruit-flies and a fungal pathogen, we demonstrate that iSMC accurately infers recombination maps under a wide range of scenarios – remarkably, even from a single pair of unphased genomes. We exploit this possibility and reconstruct the recombination maps of archaic hominids. We report that the evolution of the recombination landscape follows the established phylogeny of Neandertals, Denisovans and modern human populations, as expected if the genomic distribution of cross-overs in hominids is largely neutral.

Meiotic recombination is a major driver of the evolution of sexually-reproducing species[1]. The

crossing-over of homologous chromosomes creates new haplotypes and breaks down linkage

between neighbouring loci, thereby impacting natural selection[2,3] and consequently the genome-

wide distribution of diversity[4]. The distribution of such cross-over events is heterogeneous within

and among chromosomes[5,6], and commonly referred to as the recombination landscape – a

picture of how often genetic variation is shuffled in different parts of the genome. Interestingly,

this picture is not static, but instead is an evolving trait that varies between populations[7,8] and

species[9]. Moreover, the proximate mechanisms responsible for shaping the recombination

landscape vary among *taxa*. For example, among primates (where the PRDM9 gene is a key

player determining the location of so-called recombination hotspots[10]) the landscape is conserved

at the mega-base (Mb) scale, but not at the kilo-base (kb) scale[11]. In birds, which lack PRDM9,

the hotspots are found near transcription start sites in the species that have been studied so far[8,12].

In *Drosophila* (where clear hotspots appear to be absent[13]), inter-specific changes are associated

with mei-218 variants[14], a gene involved in the positioning of double-strand breaks[15]. The

molecular machinery influencing the distribution of cross-over events is still poorly understood

in many other groups, where a picture of the recombination landscape in closely related species

is lacking.

Aside from their intrinsic value in genetics, accurate recombination maps are needed to interpret

the distribution of diversity along the genome. Since the rate of recombination determines the

extent to which linked loci share a common evolutionary history[16], inferring selection[17–19],

introgression[18,20] and identifying causal loci in association studies requires knowledge of the

degree of linkage between sites[21]. Furthermore, recombination can cause GC-biased gene

conversion[22,23], which can mimic the effect of selection[24] or interfere with it[25]. Obtaining

recombination maps, however, remains a challenging task. Due to the typically low density of

markers, experimental approaches provide broad-scale estimates and are limited in the number of

amenable *taxa*. Conversely, population genomic approaches based on coalescent theory[26,27] have

proved instrumental in inferring recombination rates from polymorphism data.

Traditionally, population genomic methods infer recombination maps from variation in linkage

disequilibrium (LD) between pairs of single nucleotide polymorphisms (SNPs)[28–30]. However,

since "LD-based" methods typically require large sample sizes per population (from a dozen

individuals[31]), their application is restricted to a few model organisms where such sequencing

effort could be afforded. Moreover, because computation of the exact likelihood is intractable for

long sequences, the underlying model only accounts for pairs of SNPs[32], multiple pairs being

considered independent and combined using a composite likelihood approach. To avoid over-

fitting due to the high number of parameters, smoothness in the landscape is enforced by using

heuristic corrections that have been fine-tuned for humans[28] or fruit-flies[30]. Application of these

methods to systems with distinct genomic architectures therefore requires extra-benchmarking

(see for instance Stukenbrock and Dutheil[31]).

Here we introduce a new modeling framework (iSMC) to infer the variation in the recombination

rate along the genome, using a single pair of unphased genomes. Using simulations, we show

that iSMC is able to accurately recover the recombination landscape under diverse scenarios. We

further demonstrate its efficacy with case studies in Humans, Fruit-flies and the fungal pathogen

Zymoseptoria tritici, where experimental genetic maps are available. Finally, we exploit our new

method to investigate the recombination landscape of archaic hominid samples: Ust'Ishim, the

Vindija Neandertal, the Altai Neandertal and the Denisovan. Because it allows inference from

datasets for which sample size is intrinsically limited, such as ancient DNA samples, our method

opens a new window in the study of the recombination landscape evolution.

RESULTS:

Overview of iSMC

Besides its common interpretation as a backwards-in-time process, the coalescent with

recombination[33,34] can also be modelled as unfolding spatially along chromosomes[35]. Starting

from a genealogy at the first position of the alignment, the process moves along the chromosome

sequence, adding recombination and coalescence events to the ensuing ancestral recombination

graph (ARG)[36,37] (**Figure 1a**). Due to long-range correlations imposed by rare recombination

events that happen outside the ancestry of the sample (in so-called trapped non-ancestral

material[38]), the genealogy after a recombination event cannot be entirely deduced from the

genealogy before, rendering the process non-Markovian. The sequentially Markovian coalescent

process (SMC)[39,40] ignores such recombination events, but captures most of the properties of the

original coalescent[41] while being computationally tractable. It is the foundation of recent models

for demographic inference[42–44] and has been used to infer the broad-scale recombination map of

the human-chimpanzee ancestor based on patterns of incomplete lineage sorting[45,46]. In the SMC,

transition probabilities between genealogies are functions of ancestral coalescence rates and – of

key relevance to this study – the population recombination rate ($\rho = 4.Ne.r$)[43,44]. Thus,

heterogeneous recombination landscapes affect the SMC by modulating the frequency of

genealogy transitions: genomic regions with higher recombination rate are expected to harbour

relatively more genealogies than regions with smaller recombination rate (**Figure 1**). We

leverage this information by extending the SMC to accommodate spatial heterogeneity in ρ (see

Methods). In brief, our new model combines the discretised distribution of times to the most

recent common ancestor (TMRCAs) of the pairwise SMC[43] with a discretised distribution of ρ to

jointly model their variation along the genome. Since we model the transition between

discretised ρ categories as a spatially Markovian process along the genome, combining the SMC

with the Markov model of recombination variation leads to a Markov-modulated Markov model.

We cast it as a hidden Markov model[47,48] (HMM) to generate a likelihood function, where the

observed states are orthologous nucleotides and the hidden states are {TMRCA, ρ-category}

pairs (**Figure 1c**). We name our new approach "integrative sequentially Markov coalescent

(iSMC)", as it enables jointly capturing the effect of time and space in the Coalescent. This

framework explicitly connects the genealogical process with the classical definition of LD as the

non-random association of alleles at different loci[49], which has been formulated in terms of

covariances in coalescence times[50]. Henceforth, we restrict the use of the term LD to its

"topological" interpretation[51].

iSMC models spatial variation in the recombination rate using a single discrete distribution

(**Figure 1b**), which can be accommodated to various models of recombination rate variation (see

Methods). After fitting the alternative distributions to sequence data, Akaike's Information

Criterium (AIC)[52] is employed as a mean of model selection. If AIC favours a spatially

heterogeneous model over the null model where ρ is constant along the genome, iSMC then

estimates a recombination landscape of single-nucleotide resolution by weighting the discretised

values of the selected distribution with their local posterior probabilities. In the following

section, we benchmark our model on different simulated scenarios. The correlations between

simulated and inferred maps reported therein were computed after binning the inferred

landscapes into windows of 50 kb, 200 kb, 500 kb and 1 Mb.

Simulation study

To assess iSMC's overall performance, we used SCRM[53] to simulate five recombination

landscapes corresponding to different patterns of magnitude and frequency of change in ρ and a

"null" scenario with constant recombination rate along the genome (see Methods). For each

landscape, we simulated 10 ARGs, each describing the ancestry of 2 haploid chromosomes. We

tested two discretisation schemes for the joint distribution of TMRCAs and recombination rates:

the first with 40 time intervals, five ρ categories; the second with 20 time intervals, 10 ρ

categories, leading to a total of 200 hidden states in both configurations (**Supplemental Note**).

Model selection based on AIC favours the correct model in 45 of the 50 datasets (**Table S1**),

with the five exceptions belonging to the scenario where changes are frequent and of small

magnitude. In this regime, transitions to regions of slightly different recombination rates do not

significantly skew the distribution of genealogies, and the short length of blocks with constant ρ

leaves little signal in the data. Nevertheless, correlations between simulated and inferred maps

are highly significant (ranging from 0.385 to 0.563 in the five identifiable replicates with

frequent changes of low magnitude, and from 0.682 to 0.928 in the others, **Tables S2, S3**).

Overall, the results are consistent between replicates and robust to the choice of discretisation

(**Figure 2b**). We use the configuration with 40 time intervals and five ρ categories, as it

implements a finer discretisation of time that is more adequate to capture the effect of ancestral

demography. In the following, as we introduce new simulated scenarios, we focus on the

recombination landscape with frequent changes of large magnitude.

Demographic history. The random sampling of haplotypes during population bottlenecks and

expansions affects LD between SNPs, thus creating spurious signals of variation in ρ[54–56]. To test

whether iSMC could capture the effect of demography on the inference of recombination maps,

we simulated a heterogeneous recombination landscape coupled with either a recent 20-fold

increase, or ancient 20-fold decrease in population size. We then fit our model twice for each

scenario: first, erroneously assuming a flat demographic history; second, allowing iSMC to infer

piecewise constant coalescence rates in order to accommodate population size changes. The

correlation coefficients are all highly significant (**Figure 3**), showing that the inferred

recombination landscape is relatively robust to misspecification of the demographic scenario, but

are systematically higher when demography is jointly inferred (**Figure 2c-d, Table S4, S5**). The

difference is stronger at the fine scale, where, in the presence of complex demography the

distribution of genealogies can get locally confined to a time period, and ignorance about

differential coalescence rates reflects poorly on local ρ estimates. We conclude that the joint-

inference approach of iSMC can disentangle the signal that variable recombination and

fluctuating population sizes leave on the distribution of SNPs.

Introgression events. Recent studies suggested that introgression is a frequent phenomenon in

nature[57,58]. The influx of a subset of chromosomes from a source population into another, target

population (in a process analogous to a genetic bottleneck) introduces long stretches of SNPs in

strong LD. Past introgression events will thus affect runs of homozygosity, potentially biasing

the distribution of genealogies. To test the robustness of iSMC to the confounding effect of

introgression, we simulated two scenarios of admixture which differ in their time of secondary

contact between populations. The correlations between simulated and inferred recombination

maps remain highly significant (ranging from 0.631 to 0.834, **Figure 2e**, **Table S6, S7**) and

depend on the time when introgression occurred. Recombination maps are less accurately

recovered in case of recent introgression, because in such case there has been less time for

recombination to break SNP associations that do not reflect local ρ in the target, sampled

population.

Variation in mutation rate. The rate of *de novo* mutations varies along the genome of many

species. For example, CpG di-nucleotides experience an increase in mutation rate (μ) as a result

of methylation followed by deamination into thymine, whereas the efficiency of the molecular

repair machinery is negatively correlated with the distance from the DNA replication origin,

causing μ to vary accordingly[59]. Such heterogeneity could bias iSMC's estimates because the

transition into a region of higher μ mimics the transition to a genealogy with a more ancient

common ancestor, since in both cases the outcome is locally increased genetic diversity. To

assess the impact of variation of mutation rate on the estimation of recombination rate, we

simulated two scenarios of variation of $\theta = 4.Ne.\mu$ along the genome, corresponding to low and

high frequency of change, relative to the frequency of change in the recombination rate. We

report that transitions to different mutation rates along the genome globally do not introduce

substantial biases in our estimates (correlations range from 0.655 to 0.844, **Figure 2f**, **Table S8,**

S9). There is, however, an effect of the local ratio θ / ρ at the fine-scale: regions with a ratio < 1

tend to have their local ρ underestimated because the relatively small number of mutations render

some recombination events undetectable (**Figure S1a**). Importantly, this effect is a consequence

of the magnitude of μ, and is not expected as a result of the local reduction in diversity caused by

selection, since in the latter case there is a linear scaling of both θ and ρ (due to a decrease in the

local effective population size, Ne), keeping their ratio constant. Furthermore, the bias is reduced

when site-specific recombination estimates are binned into larger windows (**Figure S1b**).

Application to a fungal pathogen, fruit-flies and humans

We benchmarked iSMC on model organisms with contrasting genomic architectures and

evolutionary histories. The leaf blotch *Zymoseptoria tritici* is a highly polymorphic fungal

pathogen with a compact genome (40 Mb) that is under widespread selection[60] and exhibits an

extremely rugged recombination landscape[31,61]. In this species, AIC favours a heterogeneous

model with the presence of recombination hotspots in all three pairs of genomes analysed (**Table**

1, see Methods). Under this model, correlations between iSMC maps and a previously published

genetic map[61] are highly significant (**Table S10**) at the 20 kb scale (0.279, 0.287 and 0.308) and

increase at the 100 kb scale (0.393, 0.476 and 0.499). In sharp contrast to *Z. tritici*, the

recombination landscape in *Drosophila* is notably smooth[13], and AIC favours a heterogeneous

model based on a Gamma distribution. Under this model, correlations between iSMC maps and a

genetic map of this species are highly significant (**Table S10**) at the 100 kb scale (0.334, 0.342

and 0.363), and increase at the 1 Mb scale (0.549, 0.613 and 0.644). Like in *Zymoseptoria tritici*,

model fitting in humans favours a heterogeneous distribution of recombination rates with the

presence of hotspots (**Table 1**). We inferred recombination maps under this model for each of the

three Yoruban (African), three Dai Chinese (Asian) and three Finnish (European) genomes

available in the Simons Genome Diversity Project[62], and correlated them to the sex-averaged

genetic map from DECODE[7], after binning into windows of 50 kb, 200 kb, 500 kb, and 1 Mb

(**Table 2, Table S11**). Correlations between the DECODE map and iSMC maps from the

African individuals(range from 0.116 to 0.388 depending on window size) are lower than when

individual maps from either Asia (0.177 to 0.457) or Europe (0.179 to 0.455) are compared. This

was expected since the DECODE map was estimated from a pedigree study of the Icelandic

population. The correlations increase if we use consensus maps (defined here as the average

maps among three diploids) from each population (from 0.177 to 0.431 according to window size

for Africans, 0.251 to 0.508 for Asians and 0.253 to 0.521 for Europeans). Taken together these

results show that iSMC can infer recombination maps from species with extremely different

recombination profiles.

Application to archaic samples

At the fine scale, the location of cross-over events in great apes is strongly influenced by the

sequence of the PRDM9 gene[6,10,63]. Recombination hotspots determined by PRDM9 tend to erode

over time, being replaced somewhere else in the genome with the rise of new PRDM9 alleles.

Such turn-over of hotspot locations leads to rapid evolution of the recombination landscape[64,65],

therefore, if the location of hotspots is selectively neutral, recombination maps should become

more dissimilar with increasing divergence between populations and species. This hypothesis has

been corroborated by two lines of evidence. First, comparisons between recombination maps of

extant great ape species show no overlap of hotspots at the fine scale, but correlations increase

with window size. While this observation suggests that molecular players other than PRDM9

shape the landscape at the large scale, such positive relationship could be an artefact of reduced

variance when recombination estimates are averaged in larger windows (e.g., correlations

increase with window size in our simulations, despite recombination landscape being static over

time, **Table S1-2**). Second, *in silico* prediction of PRDM9 binding sites in the Denisovan

genome has shown no overlap of hotspots with modern humans[66]. iSMC's unique ability to

extract information from single diploids allowed for an alternative test of this hypothesis through

the analyses of four archaic samples[67]: the Altai Neandertal[68], the Vindija Neandertal[69], the

Denisovan[70] and the Ust'Ishim individual[71], a 45,000-year-old modern human from Siberia. Pair-

wise correlations between individual maps at the fine (50 kb) scale reveals that the evolution of

the recombination landscape recapitulates the evolutionary history of hominids: Asians and

Europeans form a distinct cluster; the 45,000 year-old Ust'Ishim is a long branch, sister to this

clade, depicting similarities in the recombination landscape that have been frozen by his demise

soon after the out-of-Africa migration; and all modern humans are highly diverged from the

monophyletic Neandertal-Denisovan group (**Figure 4a**). The tree has high bootstrap support for

its branches and is corroborated by principal component analysis (**Figure 4b**). Overall, the

topology is consistent at larger scales (**Figure S2**), with the notable exception of Ust'Ishim

forming a highly supported cluster with the Altai Neandertal. Interestingly, introgression from

Neandertals is estimated to have occurred into the population ancestral to this ancient *Homo*

sapiens, 232-430 generations before his lifetime. His DNA carries segments of Neandertal

ancestry that are longer and more abundant than those in contemporary modern humans[71]. It is

thus tempting to interpret this result as a consequence of the hybridisation event. Besides similar

LD in the longer introgressed regions, a non-exclusive possibility is that the recombination

landscape of Ust'Ishim was influenced by trans-acting alleles inherited from Neandertals,

presumably acting at a larger scale than PRDM9. This could explain the discrepancy between

recombination-based trees at the large *versus* fine scale (where rapid evolution of PRDM9 would

quickly erode the signal of introgression), although further investigation is needed to test this

hypothesis – ideally, as the number of high-quality archaic genomes continues to increase in the

next years. Concretely, these results show that 1) iSMC can be used to extract information from

archaic genomes; 2) hotspot turn-over driven by PRDM9 not only is responsible for short time-

scale differences in the location of cross-over events, but the accumulation of such differences is

fast enough to have already impacted the landscape of *historical* recombination along the human

lineage; and 3) in hominids, the spatial distribution of cross-over events changes at a reasonably

constant rate, indicating that it evolves – to a large extent – neutrally.

269 **DISCUSSION:**

Our analyses have shown that iSMC is able to infer accurate recombination maps from single

pairs of genomes. Nevertheless, the correlations between statistical and experimental maps for

the three species are consistently lower than the correlations obtained during simulations. While

this difference can be partly explained by technical noise (e.g., sequencing or SNP calling

errors), there are alternative – and conceptually engaging – explanations for it. First, the different

types of data used by experimental and statistical methods imply that they measure different

facets of recombination. While experimental maps reflect the average cross-over rate (r) between

markers (i.e., a snapshot of the landscape at present-day generation), the population rate ρ

($4.Ne.r$) estimated by iSMC depends on ancestral population sizes as well as on the variation of

Ne along the genome, and reflects the time-average of the historical recombination rate r. Since

regions of high r tend to erode quickly[64,65], the evolution of the recombination landscape over

time implies that ρ may be quite different from r (and more meaningful than r in the context of

population genomics[57]). Second, biological processes that affect Ne locally (therefore distorting

the distribution of genealogies) but are unaccounted for by our model will affect LD without

reflecting the recombination rate. Among these, introgression and selective sweeps (through the

rapid increase of the frequency of advantageous haplotypes) can introduce a substantial bias if

prevalent along the genome. In a similar vein, background selection distorts the distribution of

genealogies towards lower TMRCAs[72], and should be common near regions under purifying

selection such as coding regions.

In order to study processes such as population structure[62] and speciation[57,73], population

genomics generates high quality whole-genome sequences, with a small number of individuals

representing each of several sub-populations[73–76]. Due to the importance of linkage in ancestral

inference, recombination maps are key to analysing these data – and because of its power with

restricted sample sizes, iSMC is well suited for the task. We have demonstrated its accuracy in

species with contrasting levels of diversity, demographic histories and selective pressures, and

posit that it will be useful for investigation in other species. Not only will such maps aid the

interpretation of diversity in non-model organisms, but a picture of the recombination landscape

in different groups will tell us about the nature of recombination itself[77]. Open questions include

whether the recombination landscape is associated with large-scale genome architecture and how

variation in the recombination landscape relates to life history and ecological traits. Finally, as

ancient DNA samples become more common (including species other than humans[78]), it will be

possible to obtain maps from extinct *taxa*, granting the opportunity to study the evolution of the

recombination landscape with unprecedented resolution[45,79].

METHODS:

306 **The Markov-modulated Hidden Markov Model framework**

307 SMC models discretise a distribution of coalescence times into t intervals to implement a discrete

308 space Hidden Markov Model (HMM) with t x t transition matrix:

310
$$\boldsymbol{Q}(\rho)_{smc} = \begin{bmatrix} G_{11} & G_{12} & \cdots & G_{1t} \\ G_{21} & & & G_{2t} \\ \vdots & & & \vdots \\ G_{t1} & G_{t2} & \cdots & G_{tt} \end{bmatrix}$$

where G_{ij} (the transition probabilities between genealogies i and j) is a function of ancestral

coalescence rates and the global parameter ρ, which is assumed to be constant along the

genome[40,44]. The key innovation in iSMC is to relieve this assumption by letting ρ vary along the

genome, following its own Markov process, where values drawn from an a priori distribution are

used to compute the transition probabilities between genealogies. Let R be any strictly positive

probability distribution with mean = 1.0 describing the variation in recombination along the

genome. If R is discretised into k categories of equal density, the possible values that ρ can

assume in the Markov-modulated process are all $r_{j} * \rho_0$, where r_j is the jth R category and ρ_0 is the

genome-wide average recombination rate. Our Markov model (inspired by the observation that

the distribution of cross-over events is not random, but clustered in regions of similar values)

states that the probability distribution of R at position $x + 1$ only depends on the the distribution

at position x. We consider the case where the transition probability between any two R categories

(P_{ij}) is identical and equivalent to one auto-correlation parameter (δ). The transition matrix of

this Markovian process is simply:

327
$$
\mathbf{Q}_{\rho} = \begin{bmatrix} P_{11} & P_{12} & \cdots & P_{1k} \\ P_{21} & & & P_{2k} \\ \vdots & & & \vdots \\ P_{kl} & P_{k2} & \cdots & P_{kk} \end{bmatrix} = \begin{bmatrix} 1-\delta & \frac{\delta}{k-1} & \cdots & \frac{\delta}{k-1} \\ \frac{\delta}{k-1} & 1-\delta & & \frac{\delta}{k-1} \\ \vdots & & & \vdots \\ \frac{\delta}{k-1} & \frac{\delta}{k-1} & \cdots & 1-\delta \end{bmatrix}
$$

Because ρ is a parameter of the SMC, variation in the recombination rate affects the transition

probabilities between genealogies ($\mathbf{Q}_{SMC}$). Since spatial variation in ρ is modeled as a Markovian

process, the combined process is said to be Markov-modulated by ρ, leading to a Markov-

modulated HMM. If t is the number of discrete genealogies of the SMC, and k is the number of

discretised ρ categories, then the Markov-modulated HMM is a HMM with $n = t \times k$ hidden

states (**Figure 1**). We further disallow transitions between hidden states where both the

genealogies and ρ values change simultaneously. In this case, the transition matrix of the

Markov-modulated process, $\mathbf{Q}_{iSMC}$, is given by:

$$338 \qquad diag(Q_p) \otimes Q_{SMC} + (Q_p - diag(Q_p)) \otimes I_t$$

340   where û denotes the Kronecker product and $\mathbf{I_t}$ the identity matrix of dimension t. Since many of

341   its elements are reduced to zero, the matrix can be transversed efficiently:

343
$$\mathbf{Q_{iSMC}} = \begin{bmatrix} P_{11} \cdot Q(\rho_1)_{SMC} & P_{12} \cdot I_t & \cdots & P_{1k} \cdot I_t \\ P_{21} \cdot I_t & P_{22} \cdot Q(\rho_{22})_{SMC} & & P_{2k} \cdot I_t \\ \vdots & & & \vdots \\ P_{k1} \cdot I_t & P_{k2} \cdot I_t & \cdots & P_{kk} \cdot Q(\rho_k)_{SMC} \end{bmatrix}$$

In other words, $\mathbf{Q_{iSMC}}$ is a composition of k^2 square sub-matrices of dimension t. The main

diagonal sub-matrices are $\mathbf{Q_{SMC}}$ assembled using the corresponding ρ value for category k (and

scaled by $1 - \delta$), while the off-diagonal sub-matrices are identity matrices which have δ as main

diagonal elements.

Modelling spatial variation in recombination rates

iSMC implements three models of spatial variation in the recombination rate. We first use a

Gamma probability density function with a single parameter (α = beta), which constrains it to

have a mean equal to 1.0. After discretisation into k categories of equal density, the mean value

inside each category is drawn to scale the genome-wide average ρ during integration over all

recombination rates in the forward recursion (**equation 1**). In our simulation study, since we

used a continuous Gamma distribution to draw values of the recombination landscape, we used

this model to infer recombination maps. In the second model, we extend the gamma distribution

by adding a category that represents the intensity of the recombination rate in sharp hotspots

(parameter H). Since hotspots are narrow relative to the extension of the background

recombination rate, we use extra parameters to accommodate this effect. As before, δ is the

transition probability between gamma categories, and we introduce u as the transition probability

from any gamma category to H, and v as the transition probability from H to any gamma

category. The third model is obtained by letting the number of discretised categories of the

Gamma distribution equal to 1, such that it becomes a probability mass function of two

categories (**Supplemental Note**).

Model selection and computation of the posterior recombination landscape

iSMC works in two steps: (1) fitting models of recombination rate variation and (2) inferring

recombination maps based on the selected model. During step 1, the model parameters are

optimized by maximizing the likelihood using the Powell multi-dimensions procedure[80], which is

computed for the entire sequence by applying the forward recursion of the HMM[48] at every

position x of the alignment:

equation 1 $F_{S_x, G_u}(\rho_l) = \left(\sum_k \left(\sum_t F_{S_{(x-1)}, G_t}(\rho_k) \cdot Pr(G_t \rightarrow G_u | \rho_k) \cdot Pr(\rho_k \rightarrow \rho_l) \right) \right) \cdot Pr(G_u \rightarrow S_x)$

where we integrate over all k discretized values of ρ and over all t TMRCA intervals. The

transition between genealogies ($G_t \rightarrow G_u$) is a function of both the focal recombination rate

(ρ_k) and the ancestral coalescence rates, and $G_u \rightarrow S_x$ represents the emission probability from

G_u to the observed binary state at position x (**Supplemental Note**). In case AIC favours one of

the heterogeneous models, in step 2 iSMC uses the estimated parameters to estimate the posterior

average ρ for all sites in the genome. To this end, it first uses the so-called posterior decoding

method[48] as implemented in zipHMMlib[81] to compute the posterior probability of every hidden

state at each position in the sequence. Since in the Markov-modulated HMM the hidden states

are pairs of ρ categories and TMRCA intervals, this results in joint probability distributions of

recombination values and coalescence times, for all sites in the genome. Thus, prior to

computing the posteror average, iSMC obtains the marginal distribution over recombination

rates: if ${}^n\mathbf{Y}_x$ is the n-dimensional vector containing posterior probabilities for all n hidden states

at position *x*, where *n* is the product of *t* TMRCA intervals and *k* ρ categories, iSMC obtains the

k-dimensional vector $^k\mathbf{Z}_x$ by summing, for all *k*, the posterior probabilities of every hidden state *n*

matching ρ category *k*. Finally, iSMC uses $^k\mathbf{Z}_x$ to scale the corresponding values of the discretized

distribution of ρ, such that the posterior average ρ for position *x* is $(\overline{\rho_x}) = \sum_k {}^k Z_x \cdot \rho_k$.

Modelling complex demographic histories

The original HMM implementation of the SMC[43] uses the expectation-maximisation algorithm to

optimise transition probabilities, where the actual targets of inference – the coalescence rates at

each time interval – are hyper-parameters of the model. Here we use cubic spline interpolation[42]

to map coalescence rates at time boundaries, which are then assumed to be piecewise constant

for the duration of each interval. Because we use three internal splines knots (i.e., the

demographic history is divided into four epochs wherein a cubic curve is fitted), the number of

parameters is substantially reduced in our model – in particular when a fine discretisation of

TMRCA is employed.

Simulation study

Four scenarios of spatial variation in ρ. We simulated a piecewise constant recombination rate

along the genome by drawing values from a gamma distribution with parameters α and β, and

segment lengths from a geometric distribution with mean length g. We considered four possible

scenarios where α = β = 0.5 or 5.0, and g = 100 kb or 1 Mb. For each of the four combinations,

we simulated 10 independent pairs of two 30 Mb haploid chromosomes under a constant

population size model, assuming θ = 0.003 and ρ = 0.0012. For each of the following simulated

scenarios, we focus on the landscape with α = 0.5 and g = 100 kb. All scenarios share base

parameters values (θ, ρ, sequence length and sample size).

Demographic history. We simulated two demographic scenarios. First, a 20-fold population

expansion 0.01 coalescent time units ago; second, a 20-fold population bottleneck 0.5 coalescent

time units ago. Translating these coalescent times based on effective population sizes, the

expansion happened 600 generations ago, and the bottleneck happened 30,000 generations ago.

Introgression events. We simulated two introgression scenarios where a source population

introduces a pulse of genetic material into a target population. In both scenarios, the split

between source and target populations happened 2.0 coalescent time units ago, and the source

replaces 10% of the genetic pool of the target. In the first scenario, secondary contact happened

0.125 coalescent time units ago; in the second, it happened 0.25 coalescent time units ago.

Translating these coalescent times based on effective population sizes, the split between

population happened 120,000 generations ago, and the introgression events happened 7,500 and

15,000 generations ago, respectively.

Variation in the mutation rate. We simulated a piecewise constant mutation rate along the

genome by drawing rate values from a uniform distribution and segment lengths from a

geometric distribution with mean length f, where f is either 20 kb or 500 kb. The uniform

distribution generating scaling factors of θ has mean = 5.05 instead of 1.0. In this case, the

expected genome-wide average θ = 0.015. The reason for that is our focus on the spatial

distribution of θ itself. If the landscape had mean = 0.003, its highly heterogeneous nature would

scale θ down to values well below ρ (0.0012) too often along the 30 Mb sequence. The ensuing

loss of signal (due to low SNP density) would result in poorly inferred maps that display low

correlations with the simulations, not because of spatial *heterogeneity* in θ (local transitions), but

instead because the ratio θ / ρ would be too low in many windows across the chromosome.

Code availability

Source code for iSMC, as well as executable files with an example dataset, can be obtained at

[github repository will be made public upon publication]. R scripts used both for simulations and

data analyses are available in **Supplemental Data 1**.

Data analysis

Model selection followed by inference of recombination maps in the three species studied (**Table**

1) was performed using publicly available sequences (chromosome 2L from haploid pairs

ZI161 / ZI170, ZI179 / ZI191 and ZI129 / ZI138 in the Drosophila Population Genomics Project

Phase 3[82]; chromosome 1 from haploid pairs Zt09 / Zt150, Zt154 / Zt155 and Zt05 / Zt07 for

Zymoseptoria tritici[31]; chromosome 10 from three Finnish individuals (LP6005442-DNA_C10,

LP6005442-DNA_D10, LP6005592-DNA_A02) available in the Simons Genome Diversity

Project[62] for humans). In the first two species, gaps and unknown nucleotides in the sequences

(in FASTA format) were assigned as missing data, whereas in Humans the available strict mask

for the dataset was applied after parsing the VCF files.

iSMC was fitted four times to each pair of genomes of the three species: 1) with 40 discretised

time intervals and a model of variation in ρ based on a Gamma distribution with five discretised

categories; 2) with 40 discretised time intervals and a model of variation in ρ based on an

extended Gamma distribution with four discretised categories and an additional "Hotspot"

category; 3) with 40 discretised time intervals and a model of variation in ρ based on a

probability mass function of two categories; 4) with 100 discretised time intervals and a model of

variation in ρ based on a probability mass function of two categories. In each case, Kendall

correlation of ranks was computed between the resulting recombination landscape and available

genetic maps both at the fine scale (100 kb for *Drosophila*, 20 kb for *Zymoseptoria tritici* and 50

kb for Humans) and at the large scale (1 Mb for *Drosophila*, 200 kb for *Zymoseptoria tritici* and 1

Mb for Humans).

Whole-genome sequence data were used for in-depth analyses of the recombination landscape in

the hominid clade. Model fit (based on the "Hotspot" distribution) and inference of

recombination maps was performed independently on each chromosome. The individual IDs

within the Simons Genome Diversity Project[62] and corresponding population of origin of the nine

contemporary modern humans are as follows: African (Yoruban): LP6005442-DNA_A02,

LP6005442-DNA_B02 and SS6004475; Asian (Dai Chinese): LP6005441-DNA_D04,

LP6005443-DNA_B01 and LP6005592-DNA_D03; European (Finnish): LP6005442-

DNA_C10, LP6005442-DNA_D10, LP6005592-DNA_A02. The available strict mask for the

dataset was applied to assign low-quality positions as missing data. The four ancient DNA

samples were downloaded from the server at the Max Planck Institute for Evolutionary

Anthropology in Leipzig (http://cdna.eva.mpg.de/neandertal/Vindija/VCF/) in May 2018. Since

these are complete VCF files where all callable positions are reported, no mask was used and

absent positions were assigned as missing data.

The analyses of modern and archaic datasets was performed considering only positions present

in the DECODE genetic map. The dendogram presented in **Figure 4** was obtained by

hierarchical clustering (using complete linkage) of pair-wise distances computed from $1 - \tau$,

where τ is the Kendall correlation of ranks between two individual recombination maps.

Recombination maps for the entire archaic sequences are available as a resource in

Supplemental Data 2.

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Author Contributions

JYD and GVB conceived and designed the study, analysed the datasets and wrote the

manuscript. GVB developed the software. GVB and NP performed the simulation study.

The authors declare that there are no conflict of interest regarding the publication of this article.

Table 1: Performance of iSMC in three distantly related species. AIC and Kendall correlations between individual recombination maps and a genetic map from each species.

	Configuration	Drosophila (chr 2L) 100-kb / 1-Mb			Zymoseptoria (chr 1) 20-kb / 200-kb			Humans (chr 10) 50-kb / 1-Mb		
		Sample 1	Sample 2	Sample 3	Sample 1	Sample 2	Sample 3	Sample 1	Sample 2	Sample 3
AIC	40x5	**2240174.6**	**2247931.8**	**2207295.4**	572264.6	589366.4	589410.5	1399031.9	1374656.2	1434109.5
	40x(4+1)	2240269.1	2247937.7	2207417.0	572101.7	589772.2	589614.0	1399099.2	1374692.4	1434148.8
	40x2	2240267.8	2248028.2	2207415.9	571974.0	589392.2	589509.4	1399096.3	1374690.3	1434146.9
	100x2	2240359.0	2247948.0	2207537.0	**571756.1**	**588792.1**	**588748.8**	**1398867.6**	**1374403.8**	**1433950.9**
Cor. fine-scale	40x5	**0.363***	**0.334***	**0.342***	0.041	0.118**	0.245***	0.189***	0.196***	0.192***
	40x(4+1)	0.294***	0.267***	0.300***	0.216***	0.272***	0.282***	0.196***	0.191***	0.179***
	40x2	0.293***	0.261***	0.300	0.217***	0.225***	0.223***	0.198***	0.192***	0.180***
	100x2	0.289***	0.265***	0.298***	**0.287***	**0.279***	**0.308***	**0.211***	**0.190***	**0.179***
Cor. large-scale	40x5	**0.613***	**0.549***	**0.644***	-0.306*	-0.007	0.191	0.445***	0.436***	0.460***
	40x(4+1)	0.502***	0.455**	0.494***	0.421***	0.471***	0.499***	0.449***	0.445***	0.452***
	40x2	0.510***	0.423**	0.494***	0.398**	0.476***	0.421***	0.448***	0.449***	0.450***
	100x2	0.494***	0.439**	0.486***	**0.499***	**0.393**	**0.476***	**0.455***	**0.445***	**0.446***

* p-value < 0.05; ** p-value < 0.01; *** p-value < 0.001

505 **Table 2: Performance of iSMC in distinct human populations.** Kendall correlations between
506 individually inferred recombination maps for each of three human populations and the DECODE
507 genetic map. All values are significant with p-value < 0.001.

	Bin Size	Sample 1	Sample 2	Sample 3	Consensus
African (Yoruba)	50kb	0.116	0.154	0.148	0.177
	200kb	0.171	0.236	0.219	0.267
	500kb	0.235	0.309	0.271	0.319
	1mb	0.309	0.388	0.338	0.431
Asian (Dai Chinese)	50kb	0.185	0.177	0.191	0.251
	200kb	0.312	0.273	0.261	0.348
	500kb	0.397	0.406	0.369	0.464
	1mb	0.473	0.457	0.436	0.508
European (Finnish)	50kb	0.211	0.190	0.179	0.253
	200kb	0.277	0.295	0.283	0.356
	500kb	0.397	0.366	0.363	0.447
	1mb	0.455	0.445	0.446	0.521

 FIGURES

 Figure 1. Schematic representation of iSMC for one pair of genomes, with five time

 intervals and three recombination rate categories. A, In the SMC process, the spatial

 distribution of TMRCAs can be described by a matrix of transition probabilities that depend on

 local population recombination rate ρ and the ancestral coalescence rates. **B**, variation in ρ along

 the genome, modelled as a Markovian process and described by a matrix of transition

 probabilities. **C**, the combination of both Markovian processes leads to a Markov-modulated

 Markovian process. The hidden states of the resulting hidden Markov model are all pairwise

 combinations of discretized classes in **A** and **B**.

Figure 2. Distribution of correlation coefficients in the simulation study. Center line,

median; box limits, upper and lower quartiles; whiskers, 1.5x interquartile range; points, outliers.

A, four scenarios of spatial variation in the recombination rate, corresponding to different

combinations of parameters (colour). **B**, the respective comparison between two discretisation

schemes in the four recombination landscapes. **C-D**, comparison between a model where

demography is mis-specified and another where it is jointly inferred (colour), in scenarios of

recent growth (**C**) or ancient bottleneck (**D**). **E**, two scenarios of introgression, varying the time

of gene-flow (colour). **F**, two scenarios of spatial variation in the mutation rate, varying its

frequency of change (colour).

   Figure 3. Inference of recombination maps in the presence of recent population growth.

   Each column represents a bin size (50 kb, 200 kb, 500 kb and 1 Mb). **A-D**, Simulated (black) and

   inferred (orange) recombination maps. **E-H**, scatter-plots of the same data. Red lines represent y

   = x, blue lines represent loess smoothing curve.

   Figure 4. Evolution of the fine-scale recombination landscape in hominids. A, Dendogram

   based on pair-wise correlations between whole-genome recombination maps at the 50 kb scale. **B**,

   principal component analysis of the same data.

SUPPLEMENTAL FIGURE LEGENDS

Figure S1. Inference of recombination maps in the presence of a heterogeneous mutation landscape. Points are coloured as a function of the local ratio θ / ρ (>= 1 green, < 1 pink). Magenta dashed line represents y = x. **A**, both ρ and θ are binned into 50 kb windows. Solid lines represent loess smoothing curves fitted to each class of θ / ρ, with 95% confidence intervals aroung them (shaded). **B**, both ρ and θ were binned into 500 kb windows.

Figure S2. **Evolution of the large-scale recombination landscape in hominids. A-C**, Dendogram based on pair-wise correlations between whole-genome recombination maps at the 50 kb, 200 kb and 1 Mb scales. **D-F**, principal component analysis of the same data.

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