A model of ganglion axon pathways accounts for percepts elicited 1 by retinal implants

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Abstract 12

13 Degenerative retinal diseases such as retinitis pigmentosa and macular degeneration cause 14 irreversible vision loss in more than 10 million people worldwide. Retinal prostheses, now 15 implanted in more than 250 patients worldwide, electrically stimulate surviving cells in order to 16 evoke neuronal responses that are interpreted by the brain as visual percepts ('phosphenes'). 17 However, instead of seeing focal spots of light, users of current epiretinal devices perceive highly 18 distorted phosphenes, which vary in shape not just across subjects but also across electrodes, 19 resulting in distorted percepts. We characterized these distortions by asking users of the Argus 20 retinal prosthesis system (Second Sight Medical Products, Inc.) to draw percepts elicited by single-21 electrode stimulation on a touchscreen. Based on ophthalmic fundus photographs, we then 22 developed a computational model of the topographic organization of optic nerve fiber bundles in 23 each subject's retina, and used this model to successfully simulate predicted patient percepts. Our 24 model shows that activation of passing axon fibers contributes to the rich repertoire of phosphene 25 shapes reported by patients in our psychophysical measurements, successfully replicating visual 26 percepts ranging from 'blobs' to oriented 'streaks' and 'wedges' depending on the retinal location of the stimulating electrode. This model provides a first step towards future devices that 27 28 incorporate stimulation strategies tailored to each individual patient's retinal neurophysiology.

29 Impact

30 Current retinal implant users report seeing distorted and often elongated shapes rather than small

31 focal spots of light that match the shape of the implant electrodes. Here we show that the perceptual

experience of retinal implant users can be accurately predicted using a computational model that 32

- 33 simulates each individual patient's retinal ganglion axon pathways. This opens up the possibility
- 34 for future devices that incorporate stimulation strategies tailored to each individual patient's retina.

35 1. Introduction

Degenerative retinal diseases such as retinitis pigmentosa (Hartong et al., 2006) and macular 36 37 degeneration (Jager et al., 2008) lead to a loss of photoreceptor cells and subsequent remodeling of the neural circuitry in the retina (Marc and Jones, 2003; Marc et al., 2003), causing irreversible 38 blindness in more than 10 million people worldwide. Analogous to cochlear implants, the goal of 39 retinal prostheses is to help alleviate these incurable conditions by electrically stimulating 40 41 surviving cells in the retina (for a recent review, see Weiland et al., 2016). The hope is that 42 electrically evoked neuronal responses will be transmitted to the brain and interpreted by the 43 subject as visual percepts ('phosphenes').

44 Two devices are already approved for commercial use: Argus II (epiretinal, Second Sight 45 Medical Products Inc., da Cruz et al., 2016; Rizzo et al., 2014) and Alpha-IMS (subretinal, Retina Implant AG, Stingl et al., 2015), which have been shown to restore vision up to a visual acuity of 46 20/1,260 (Humayun et al., 2012) and 20/546 (Stingl et al., 2015), respectively. In addition, PRIMA 47 (subretinal, Pixium Vision, Lorach et al., 2015) has started clinical trials, with others to follow 48 49 shortly. In combination with stem cell therapy (Chader and Young, 2016; da Cruz et al., 2018) and 50 optogenetics (Gaub et al., 2015), a range of sight restoration options should be available within a 51 decade (Fine et al., 2015).

52 However, despite the increasing clinical and commercial use of these devices, the perceptual experience of retinal implant users remains poorly understood. For example, even in response to 53 54 single-electrode stimulation, the appearance of individual phosphenes is highly variable not only 55 across subjects but also across electrodes within a subject, with subjects typically reporting seeing distorted and often elongated geometric shapes that fade quickly over time (Caspi et al., 2009; 56 57 Horsager et al., 2009; Luo et al., 2016; Nanduri et al., 2008; Pérez Fornos et al., 2012; Rizzo et al., 2003; Wilke et al., 2011a; Yanai et al., 2007). Furthermore, linearly combining these 'building 58 blocks' of percepts from individual electrodes often fails to predict the combination of percepts 59 60 evoked when multiple electrodes are stimulated (Horsager et al., 2011; Horsager et al., 2010; Rizzo 61 et al., 2003; Wilke et al., 2011b). Consequently, most subjects cannot determine the orientation of 62 gratings that are used to measure visual acuity, and those who can recognize letters take more than 63 40 seconds to do so (da Cruz et al., 2013; Zrenner et al., 2011).

64 Both computational (Esler et al., 2018; Tahayori et al., 2014) and in vitro electrophysiological studies (Fried et al., 2009; Rizzo et al., 2003; Weitz et al., 2015) suggest that electrode 65 configurations similar to those implanted in patients do not achieve focal activation, but rather 66 produce significant activation of passing axon fibers, which may result in perceptual distortions in 67 patients. Here, we are the first to directly examine whether axonal stimulation contributes to the 68 69 rich repertoire of phosphene shapes reported by patients. Our computational model can account 70 for the apparent shape of phosphenes elicited by single-electrode stimulation in two generations of the Argus retinal prosthesis system (Second Sight Medical Products, Inc.). 71

72 Four subjects suffering from severe retinitis pigmentosa were chronically implanted with an 73 epiretinal prosthesis in the macular region of the retina: one subject was implanted with an Argus I 74 device (16 platinum disc electrodes arranged in a 4x4 checkerboard pattern; see Figure 1A), and 75 three subjects were implanted with Argus II device (60 platinum disc electrodes in a 6x10 76 arrangement; Figure 1B). Electrical stimulation was delivered to a number of pre-selected 77 electrodes in random order (five repetitions each) using square-wave, biphasic, cathodic-first pulse 78 trains with fixed stimulus duration, and we asked subjects to outline perceived phosphene shape 79 either on a grid screen (Argus I; Figure 1B, C) or a computer touch screen (Argus II; Figure 1E, F) (see Methods). We then used a computational model to generate predictions about the apparent 80 81 shape of the expected visual percepts, and compared the predicted images to patient phosphene 82 drawings. The model assumed that distortions are due to activation of ganglion axon pathways, having estimated the spatial layout of these pathways using traced nerve fiber bundle trajectories 83 84 extracted from ophthalmic fundus photographs of 55 human eyes (Jansonius et al., 2009).

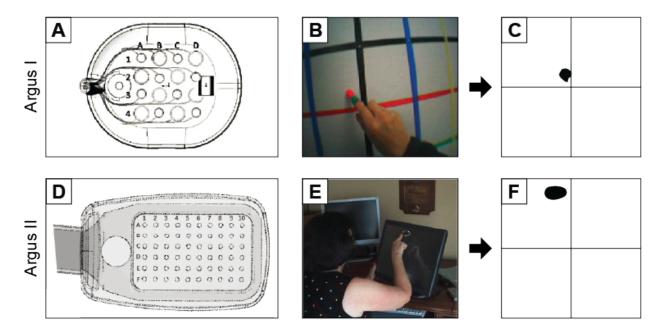


Figure 1: Retinal implants used for the drawing task. (A) Argus I electrode array (4x4 electrodes of 260 μ m or 520 μ m diameter arranged in a checkerboard pattern). (B) Argus I subject drawings on a grid screen were captured by an external camera and recorded to a video file. (C) Video files were analyzed offline by tracking the location of the fingertip frame-by-frame and by translating the drawings to a binary image. (D) Argus II electrode array (6x10 electrodes of 200 μ m diameter). (E) Argus II subject drawings were recorded by a touch screen monitor. (F) Subject drawings were translated to a binary image. Shapes were closed by automatically connecting the first and last tracked fingertip location, after which a floodfill was applied.

85 2. Results

86 2.1 Phosphene drawings vary across electrodes, but are relatively consistent for a given

87 electrode

All subjects consistently reported seeing phosphenes upon electrical stimulation of the retina. Phosphenes appeared light gray, white, or yellowish in color. However, phosphene drawings varied greatly across subjects and electrodes; representative drawings for each subject are shown

- 91 in **Figure 2**. Whereas stimulation of some electrodes elicited consistent percepts across trials (top
- 92 row of panels in each subplot), stimulation of other electrodes led to percepts that varied in both
- 92 now of panels in each subplot), summation of other electrodes fed to percepts that varied in ooth 93 size and shape across trials (bottom row of panels in each subplot). Subjects occasionally but rarely

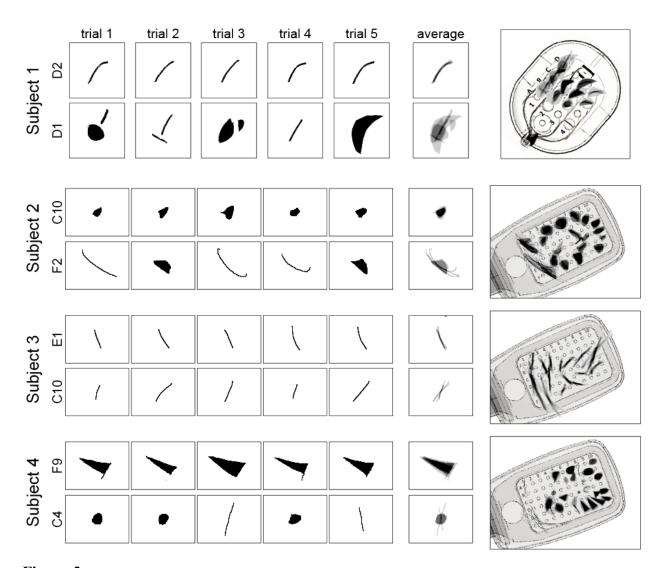


Figure 2: Phosphene drawings vary across electrodes. Drawings from individual trials are shown for the most consistent (top row in each panel) and least consistent electrodes (bottom row in each panel) for Subjects 1–4. Mean images (labeled 'average') were obtained by averaging drawings from individual trials aligned at their center of mass. These averaged drawings were then overlaid over the corresponding electrode in a schematic of each subject's implant (rightmost column).

reported seeing two distinct shapes (e.g., Subject 1, Electrode D1). Mean images for each electrode
were obtained by averaging the drawings across the five stimulation trials, aligned by their centers
of mass (column 'average'). Mean images were then centered over the corresponding electrode in
a schematic of the subject's implant to reveal the rich repertoire of elicited percepts across
electrodes (large, rightmost panel in each subplot).

As is evident from these data, only a small number of phosphenes could be described as focal spots of light. Subject 1 drew percepts as either curved or straight lines, wedges, or relatively round spots. Subject 2 drew most percepts as ovals or relatively round spots with only a few curved or straight lines of varying thickness, whereas Subject 3 drew all phosphenes as slightly curved or straight, thin lines. Subject 4 predominantly drew ovals, wedges, and triangles, with only few curved or straight lines.

Interestingly, for Subjects 2–4 the percepts produced by electrodes in the first two rows of the array (i.e., Electrodes A1–F1, A2–F2) were much thinner and longer than for other electrodes (Beyeler, 2018; Mueller and Grill, 2013). It is possible that these electrodes were the ones that were closest to the retinal surface, since the surgical tack used to attach the implant to the retina was located next to the first row of electrodes. However, we did not have access to optical coherence tomography data, which would have allowed us to directly measure electrode-retina distance.

To quantify the similarity and variability of individual phosphene drawings, we calculated three shape descriptors for each collected drawing: phosphene *area*, *orientation*, and *elongation* (see Methods). These parameter-free metrics were based on a set of statistical quantities known as 'image moments'; that is, particular weighted averages of pixel intensities across an image (Equation 1). Phosphene orientation and elongation were calculated from the eigenvalues and eigenvectors of each drawing's covariance matrix (Equations 2 - 4).

The upper panels of **Figure 3** show distributions of phosphene *area* (**Figure 3A**), *orientation* (**Figure 3B**), and *elongation* (**Figure 3C**) for each subject, across all tested electrodes. The lower panel (**Figure 3D–F**) boxplots depicts trial-to-trial variability for each shape descriptor of a given electrode, measured as the standard error of the mean (SEM) calculated across drawings.

122 To assess whether observed SEM values were smaller than would be predicted from a random 123 sample of phosphene drawings we performed a resampling analysis (1000 iterations). We began 124 by calculating the SEM across all five drawings for each electrode. To assess whether, for an 125 individual subject, drawings were more similar for an individual electrode then across other 126 electrodes in that particular subjects' array, resampling was done by randomly sampling (with 127 replacement) phosphene drawings across all the electrodes of that subject. Probability values were 128 estimated by comparing the mean SEM across electrodes of the real distribution to the 1-tailed 129 confidence interval generated by resampling. Detailed results for each shape descriptor are given 130 below.

131 2.1.1 Phosphene area estimates show consistent variation across electrodes

- 132 Phosphene *area* was calculated as the number of nonzero pixels in the drawing. We report data in 133 terms of pixels because the relationship between drawing area and the size of the phosphene in
- terms of visual angle should be interpreted with caution. Based on each subject's viewing distance,
- 135 the touchscreen should have subtended $73.8 \times 73.8^{\circ}$ of visual angle for Subject 1, $60 \times 45^{\circ}$ for
- 136 Subject 2, $65 \times 48.8^{\circ}$ for Subject 3, and $64 \times 48^{\circ}$ for Subject 4. Although we asked subjects to
- 137 draw phosphenes 'as if they appeared at arm's length' (see Methods), subjects qualitatively
- 138 reported that phosphenes could appear as close as 'in front of their face' to 'at arm's length'. As
- 139 can be seen by the variability in the boxplots in **Figure 3D**, estimates of area varied widely across
- 140 both subjects and electrodes. However, despite the lack of a reference plane in depth, for all but
- 141 S1 (marginally significant) the observed SEM values for phosphene area were significantly smaller
- 142 than SEM values from randomly chosen electrodes (S1: p < 0.06, S2: p < 0.01, S3: p < 0.001,
- 143 S4: p < 0.001). S1 had particularly small percepts, so areal variability may have been more
- 144 heavily influenced by drawing error.

145 **2.1.2** Phosphene orientation is more consistent within than across electrodes

- 146 Phosphene *orientation* was calculated as the angle of the principal eigenvector (in the range [-90°,
- 147 90°]). For all subjects, mean SEM values for phosphene orientation were significantly smaller than
- 148 mean SEM values for our bootstrapped null model (S1: p < 0.001, S2: p < 0.001, S3: p < 0.001,

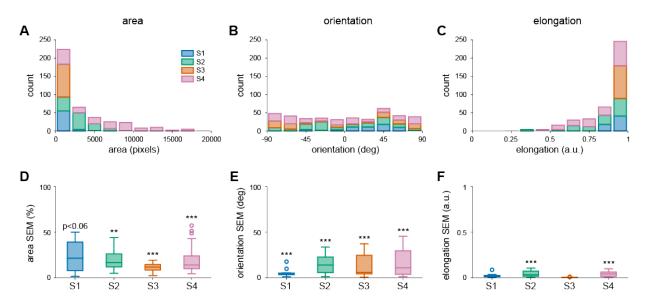


Figure 3: (A-C) Distribution of phosphene area, orientation, and elongation for each subject (Subject 1: 60 drawings, Subject 2: 110 drawings, Subject 3: 90 drawings, Subject 4: 140 drawings). (D–F) Distribution of the variability of shape descriptors for each subject, measured as the standard error of the mean (SEM) across trials for every electrode. Each box extended from the lower to upper quartile values of the data, with a line at the median. Whiskers extended from the fifth to ninety-fifth percentiles, with data points outside that range considered outliers ('o'). Area SEM for every electrode was normalized by the mean area of all drawings for that particular electrode.

- 149 S4: p < 0.001), showing that the variation in phosphene orientation within an individual electrode
- 150 is less than the variation across electrodes (**Figure 3E**).

151 **2.1.3** Phosphene elongation is more consistent within than across electrodes

Phosphene *elongation* was calculated as the relative difference in magnitude of the eigenvalues and normalized to [0, 1], with 0 representing a circle, and 1 representing an infinitesimally thin line. The distribution of elongation values indicates that subjects consistently saw elongated percepts instead of focal spots of light, indeed Subject 3 reported exclusively seeing thin curved and straight lines. These results are in stark contrast to the prevailing assumption in the field that stimulating a single electrode should generate the percept of a small focal spot of light (Chen et al., 2009; Dagnelie et al., 2007; Freeman et al., 2011; Hayes et al., 2003; Thompson et al., 2003).

- 159 For Subjects S2 and S4, observed SEM values for phosphene elongation were significantly
- smaller than of our bootstrapped null model (S2: p < 0.001, S4: p < 0.001). For Subjects S1 and
- 161 S3 results were not significant; percepts were heavily elongated for every electrode, providing
- 162 little variability in the dataset (**Figure 3F**).

163 **2.1.4 Drawing accuracy**

Our subjects had been lacking tactile-visual feedback for many years. This motivated a control experiment, where we asked subjects to explore various tactile targets (made of felt with a cardboard background) with their hands, and to draw the targets on a touch screen (**Figure S1**). Drawing errors in the tactile experiments were similar to those in our phosphene drawing experiments (**Figure S2**).

169 **2.2** Phosphene orientation is aligned with retinal nerve fiber bundles

As described above, computational models and electrophysiological evidence from in vitro 170 171 preparations of rat and rabbit retina suggest that retinal implants may stimulate passing axon fibers 172 (Fried et al., 2009; Rizzo et al., 2003; Weitz et al., 2015). Retinal ganglion cells send their axons 173 on highly stereotyped pathways en route to the optic nerve (Figure 4A-C). Because of this 174 topographic organization, an electrode that stimulates nearby axonal fibers would be expected to 175 antidromically activate cell bodies located peripheral to the point of stimulation. Perceptually, 176 activating an axon fiber that passes under a stimulating electrode is indistinguishable from the 177 percept that would be elicited by activating the corresponding ganglion cell body. The visual percept should appear in the spatial location in visual space for which the corresponding ganglion 178 179 cell encodes information, which could be hundreds of microns away from the stimulation site (Fine 180 and Boynton, 2015). Consequently, percepts elicited from axonal stimulation would be expected to appear elongated in the direction of the underlying nerve bundle trajectory (Figure 4C). 181

182 To test whether the orientation of phosphene drawings were aligned with the underlying nerve 183 fiber bundles, we estimated the relative location and orientation of each subject's implant with 184 respect to the fovea and the optic disc, using ophthalmic fundus photographs (Figure 4D; here 185 shown for Subject 4). While yellow screening pigments allow for visualization of macular extent 186 in normal eyes, it is difficult to discriminate the macula-periphery boundary in our subjects because 187 of the characteristic pigmentary deposits associated with retinitis pigmentosa (Hartong et al., 2006). We therefore had a retina specialist mark the fovea on a fundus image obtained before 188 surgery (Figure 4D, top), and subsequently used computer vision techniques (see Methods) to 189 190 align the presurgery image with a second fundus image obtained after surgery (Figure 4D, bottom), showing the implant relative to the optic nerve head. This allowed us to estimate the array 191 192 center with respect to the fovea, the array rotation with respect to the horizontal raphe, and the 193 retinal distance between the fovea and the optic nerve head for each subject (Figure 4E). The

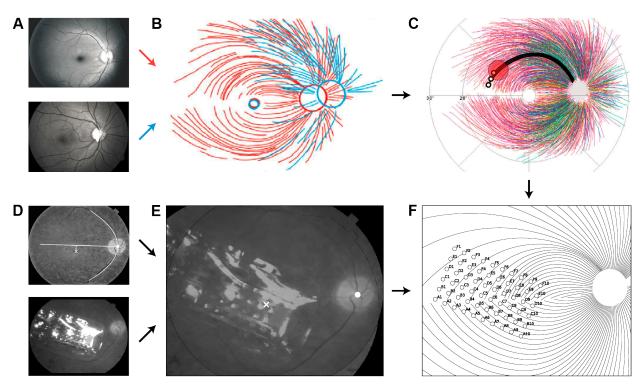


Figure 4: (**A**–**C**) The topographic organization of optic nerve fiber bundles is highly stereotyped in the human retina (adapted from Jansonius et al., 2009). Fundus images from 55 human eyes (**A**) were superimposed by translation in order to center the foveola (**B**), followed by rotation and zooming to align the centers of the optic disc (**C**). Electrical stimulation (red circle) of a nerve fiber bundle could antidromically activate ganglion cell bodies peripheral to the point of stimulation (small black circles), leading to percepts that appear elongated in the direction of the underlying nerve bundle trajectory. (**D**–**E**) The location and orientation of each subject's implant (Subject 4 shown here) was estimated by combining their postsurgical fundus photograph (**D**, bottom) with a baseline presurgical image in which the fovea had been identified (**D**, top) to produce a registered image (**E**; x: foveal pit, o: optic disc). The horizontal raphe (**D**, white line) was approximated by fitting a parabola to the main vascular arcade and finding the tangent to the parabola inflexion point. (**F**) The extracted landmarks were then used to place a simulated array on a simulated map of nerve fiber bundles.

resulting topographic measurements were then used to simulate a map of the ganglion axon
pathways (Jansonius et al., 2009) that was tailored to each subject's retinal dimensions (Figure
4F).

197 Remarkably, we found that for all subjects, phosphene orientation was well aligned with the 198 tangent line of the nerve fiber bundle directly below the stimulating electrode (**Figure 5**). Here, 199 insets show mean drawings for representative electrodes, from which phosphene orientation was 200 calculated. This was not only true for line phosphenes, which resembled carbon copies of the 201 underlying fiber bundle topography (e.g., Subject 1: D2, Subject 4: F2), but also for more compact 202 phosphenes, which still tended to be elongated in the direction of the local fiber bundle trajectory 203 (e.g., Subject 2: B9, Subject 4: C10).

To assess whether these angular errors were smaller than would be predicted from a random placement of the array on the retina, we performed a resampling analysis. First, we calculated the mean absolute angle between the five drawings corresponding to a single electrode and the tangent line of the closest nerve fiber bundle. We repeated this procedure for all electrodes in the array to produce a distribution of mean angular errors (box plots in **Figure 5**). Our resampled distribution (1000 iterations) was generated by randomly placing the array on the retina (array center

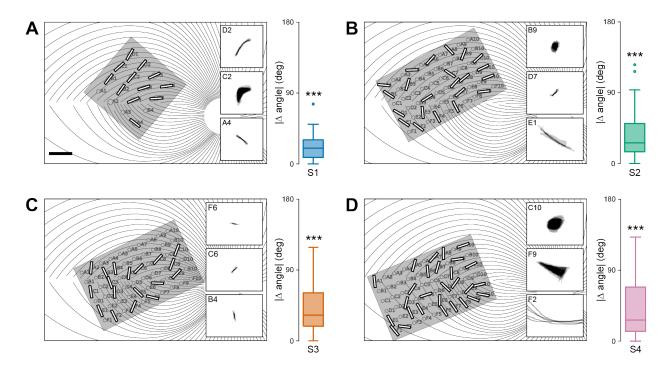


Figure 5: Phosphene orientations are aligned with retinal nerve fiber bundles. (**A**–**D**) Simulated map of nerve fiber bundles for Subjects 1–4 (scale bar: 1 mm). Phosphene orientation is indicated as oriented bars, overlaid over the corresponding electrode in the array. Insets show example percepts. Note that the maps are flipped upside down so that the upper image half corresponds to the upper visual field (inferior retina). Box plots indicate the distribution of mean absolute angular errors between phosphene orientation and the tangent line of the ganglion axon pathway nearest to the corresponding electrode. For all subjects, angular errors were significantly better than would be expected from random array placement.

- 210 coordinates: $x \in [-30, 30]^\circ$, $y \in [-15, 15]^\circ$. Probability values were estimated by comparing the
- 211 mean angular error of the real distribution to the 1-tailed confidence interval of values from the
- 212 resampled null model. Angular errors were significantly smaller than predicted by the null model
- 213 in all four subjects (S1: p < 0.001, S2: p < 0.001, S3: p < 0.001, S4: p < 0.001).

214 **2.3** Predicting phosphene shape based on a simulated map of ganglion axon pathways

215 We then tested whether the spatial layout of ganglion axon pathways could account for phosphene shape as well as orientation. We assumed that the activation of an axon elicited a percept centered 216 217 over the receptive field location of that axon's cell body. The activation sensitivity of a passing axon fiber was assumed to decay exponentially with retinal distance from the stimulation site, with 218 219 each subject's data being fit with two parameters: a decay constant λ , which described activation 220 sensitivity along the axon, and a decay constant ρ , which described sensitivity orthogonal to the 221 axon (see Methods). This allowed us to generate a tissue activation map for each stimulating 222 electrode, which we thresholded to arrive at a binary image that could serve as a prediction of a 223 phosphene drawing (small schematic in the center column of Figure 6).

224 Alternatively, we considered a simpler but widely used model that treated each electrode in 225 an array as a 'pixel' in an image, thus assuming that stimulating a grid of electrodes on the retina would result in the percept of a grid of isolated, focal spots of light (Chen et al., 2009; Dagnelie et 226 227 al., 2007; Freeman et al., 2011; Hayes et al., 2003; Thompson et al., 2003). We refer to this model 228 as the 'scoreboard model', because much like the large scoreboards found in sports stadiums, an 229 image is created by an array of individual light sources that can be turned off or on. To implement 230 the scoreboard model, we assumed that an electrode would lead to the percept of a Gaussian blob 231 (with spatial decay constant ρ). The resulting intensity profile was again thresholded to obtain a binary image, which was compared to real phosphene drawings (small schematic in the right 232 233 column of Figure 6).

234 To find the parameter values under each model that best predicted phosphene shape, we 235 constructed a cost function from the difference between predicted and observed phosphene area, 236 orientation, and elongation, which we minimized using particle swarm optimization (see Methods). Because scoreboard and axon map models had a different number of parameters 237 238 (scoreboard model: ρ ; axon map model: ρ , λ), we used leave-one-electrode-out cross-validation to 239 allow for fair model comparison, where we repeatedly fit each model to the drawings from all but one electrode in the array. Fitted parameter values were then used to predict the phosphene shapes 240 241 of the held-out drawings. Note that a single value of ρ and λ was used to describe the drawings of 242 all electrodes in that subject's array.

The result of this cross-validation procedure is shown in **Figure 6**. Here, ground-truth drawings are shown in the left column, and predicted phosphenes (on the test-fold of the crossvalidation procedure) are shown in center and right columns. Thus, predicted phosphene shapes represent each model's ability to generalize to new electrodes. Whereas the axon map model was able to generate both compact and elongated phosphenes that span a range of geometrical shapes such as 'blobs', 'lines', and 'wedges', the scoreboard model exclusively predicted round phosphenes of various size.

250 The best fitting, cross-validated parameter values are given in **Table 1** (averaged across folds).

251 Even though phosphene shape often varied drastically across electrodes, the axon map model

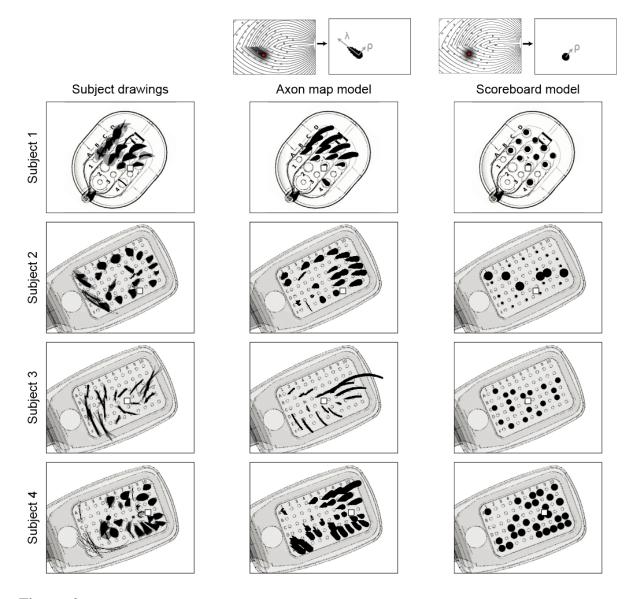


Figure 6: Phosphene drawings (left columns) contrasted against cross-validated phosphene predictions of the axon map model (center column) and the scoreboard model (right column), overlaid over a schematic of each subject's implant. Each predicted phosphene is from the test fold of a leave-one-electrode-out cross-validation.

recovered similar values for ρ and λ across different folds for a given subject, as indicated by relatively small SEMs. Without adjusting for drawing bias, these results suggest that electrical stimulation influences ganglion cells whose cell bodies are at a distance of approximately ρ =437 µm (corresponding to ~1.5° of visual angle) orthogonal to the direction of the axon fiber bundle, but as far as λ =1,420 µm (corresponding to ~5° of visual angle) along a direction parallel to the axon fiber.

258

| | Axon m | Scoreboard model | |
|------------|--------------|------------------|-------------|
| Subject ID | ρ (μm) | λ (μm) | ρ (μm) |
| 1 | 410 ± 5 | 1190 ± 157 | 533 ± 11 |
| 2 | 315 ± 17 | 500 ± 142 | 244 ± 34 |
| 3 | 86 ± 3 | 992 ± 150 | 170 ± 1 |
| 4 | 437 ± 6 | 1420 ± 42 | 175 ± 1 |

Table 1: Cross-validated model parameter values, averaged across folds ± uncorrected SE.

261 To further quantify model performance, we compared cross-validated prediction errors 262 (Equation 13) across axon map and scoreboard models, Figure 7. Here, each data point in the 263 scatter plots corresponds to the cross-validated prediction error (averaged across every drawing in 264 that fold) for each electrode. Data point almost always lie below the diagonal, indicating that the 265 axon map model was more accurate than the scoreboard model. Indeed, the axon map model often improved cross-validated log prediction error by an order of magnitude (see insets), simply by 266 267 adding a single parameter λ that accounted for the current spread along axons of passage in the 268 optic nerve fiber layer of the retina.

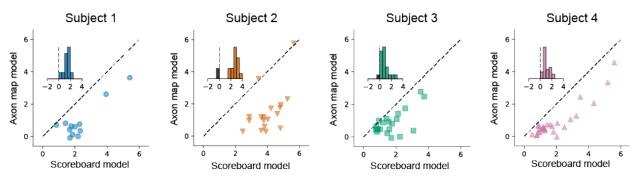


Figure 7: Comparison of log mean prediction error for the two models. Prediction error was based on the sum of differences between predicted and observed phosphene area, orientation, and elongation (see Equation 13). Each data point in the scatter plots corresponds to the cross-validated prediction error of all drawings associated with a particular held-out electrode. Prediction error was significantly higher for the scoreboard model compared to the axon map model (Subject 1: p<0.001, N=12; Subject 2: p<0.001, N=22; Subject 3: p<0.001, N=18; Subject 4: p<0.001, N=28; 2-tailed Wilcoxon signed-rank test). Insets in each panel show the histogram of pair-wise differences in log prediction error.

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270 **3. Discussion**

We show here that the elicited percepts of patients with retinal implants can be accurately predicted 271 272 using the spatial layout of ganglion axon pathways in the human retina. Model fits to behavioral 273 data suggest that sensitivity to electrical stimulation is not confined to the axon initial segment 274 (Fried et al., 2009), but can be modeled as falling off with different decay constants along the axon 275 (with λ ranging from 500–1,420 µm) and orthogonally from the axon (with ρ ranging from 86– 276 437 µm), resulting in visual percepts ranging from 'blobs' to 'streaks' and 'wedges' depending on 277 both the relative values of λ and ρ , and the retinal location of the stimulating electrode. These 278 results are in agreement with theoretical work suggesting an anisotropic spread of current in the 279 retinal tissue (Esler et al., 2018) as well as previous animal literature demonstrating that epiretinal 280 stimulation leads to activation of passing axon fibers (Fried et al., 2009; Grosberg et al., 2017; 281 Rizzo et al., 2003; Weitz et al., 2015), which can severely distort the quality of the generated visual experience (Beyeler et al., 2017b; Fine and Boynton, 2015; Nanduri et al., 2008; Rattay and Resatz, 282 283 2004; Rizzo et al., 2003). Our findings suggest that the spatial distortions reported by patients are 284 not arbitrary, but rather depend on the topographic organization of optic nerve fiber bundles in 285 each subject's retina, which can be captured by a computational model. Having an accurate model 286 that generalizes across patients is crucial for retinal prostheses to be able to generate more complex, perceptually intelligible percepts. Our results therefore open up the possibility for future devices 287 to incorporate stimulation strategies that are tailored to the predicted perceptual experience of each 288 289 individual patient, relying on the known surgical placement of the device and empirical estimates 290 of ρ and λ .

291 **3.1** A rich repertoire of phosphene shapes

The phosphenes elicited by single-electrode stimulation vary dramatically across subjects and electrodes (**Figure 2**, **Figure 3A–C**), despite relatively small drawing errors and consistency in drawings within a given electrode (**Figure 3D–F**). These results are in agreement with the previous literature that has reported that patients subjectively report a variety of percept shapes (de Balthasar et al., 2008; Greenwald et al., 2009; Horsager et al., 2009; Nanduri et al., 2012), of which only a small fraction could be described as focal spots of light.

298 The variability in phosphene shape across subjects that we report (captured by variation in λ 299 and ρ across patients), might be due to a number of factors, a few of which are outlined below. 300 First, diseases such as retinitis pigmentosa and macular degeneration are characterized by a progressive degeneration of photoreceptors, gradually affecting other layers of the retina 301 (Humayun et al., 1999; Jones et al., 2003; Marc et al., 2003; Mazzoni et al., 2008). In severe end-302 303 stage retinitis pigmentosa, roughly 95% of photoreceptors, 20% of bipolar cells, and 70% of 304 ganglion cells degenerate (Santos et al., 1997), so that little or no useful vision is retained. Disease 305 progression therefore influences the relative proportion of surviving bipolar and ganglion cell 306 types, which in turn is likely to influence phosphene shape.

307 Second, with a diameter of 200 μ m, each electrode in the Argus II array encompasses the 308 equivalent area of hundreds of photoreceptors. A single electrode therefore inevitably leads to 309 activation of a wide variety of morphologically and functionally distinct retinal cells (Dacey, 2004; 310 Field and Chichilnisky, 2007), including simultaneous activation of both ON and OFF pathways. 311 This is in contrast to natural stimulation, which precisely activates a number of specialized, 312 functionally complementary, parallel processing pathways in the retina (for a recent review see 313 Nassi and Callaway, 2009). Although epiretinal stimulation with relatively short pulses might 314 primarily activate ganglion cells rather than bipolar cells (Freeman et al., 2010; Fried et al., 2006; Greenberg, 1998; Sekirnjak et al., 2006, 2008), there is still much to be learned about how the 315 information from these different retinal representations are combined at later stages of processing 316 317 to form a conscious percept.

Third, the mapping of retinal eccentricity to visual field coordinates is nonlinear. Because the foveola contains only photoreceptors, ganglion cell bodies are displaced centrifugally from their cone inputs by several degrees; an effect that extends out as far as 17° (Curcio and Allen, 1990; Watson, 2014).

322 Finally, phosphene size might be influenced by ganglion cell density and receptive field size. 323 Whereas the receptive field size of retinal ganglion cells only gradually increases with eccentricity 324 (Peichl and Wassle, 1979), ganglion cell density decreases rapidly (Curcio and Allen, 1990). 325 Furthermore, retinal degeneration in retinitis pigmentosa tends to progress from the periphery to 326 the macula, thereby having a greater effect on ganglion cell density in the periphery (Humayun et 327 al., 1999; Santos et al., 1997; Stone et al., 1992). As a consequence, more peripheral electrodes 328 would typically stimulate cells with only slightly larger receptive fields, but in much smaller 329 numbers than in the fovea. These two conflicting effects may contribute to our finding of no 330 correlation between phosphene area and retinal eccentricity (data not shown).

331 3.2 Phosphene shape is mediated by axonal stimulation

Despite the variability in phosphene shape, all subjects reported seeing elongated phosphenes on at least a subset of electrodes (**Figure 3C**). Although the electric field generated by a disk electrode is radially symmetric, the neural tissue induces anisotropies in the electric field, and stimulation of axon fibers produces even more striking anisotropies in patterns of neural activation within the retina (Esler et al., 2018). It has long been known that external stimulation of an axon induces an action potential that travels both backward to the cell body and forward to the synaptic terminals (Bishop et al., 1962; Lemon, 1984).

A number of studies have previously hypothesized that axonal stimulation could lead to phosphenes that are elongated in shape and poorly localized (e.g., Fine and Boynton, 2015). However, this idea has never been explicitly tested. In the present study we demonstrate that axonal stimulation in the retina leads to predictable distortions of shape in human patients, which can be captured by a computational model (**Figures 5–7**).

344 Axonal stimulation is a concern for other implant technologies as well. Although subretinal 345 prostheses such as Alpha-IMS (Stingl et al., 2015) have electrodes in close proximity to bipolar 346 cells, *in vitro* animal studies have found that subretinal stimulation with 1 ms pulses also directly 347 activates retinal ganglion cells at thresholds statistically similar to those of inner retinal cells 348 (Boinagrov et al., 2014; Eickenscheidt et al., 2012; Tsai et al., 2009). Similarly, axonal stimulation 349 is expected to be an issue for cortical implants, since passing axons from neurons located in distant 350 parts of the brain have been shown to be highly sensitive to electrical stimulation (Histed et al., 351 2009; Lee et al., 2016; Ranck, 1975).

352 Several recent studies have tried to identify stimulation protocols that minimize axonal 353 activation, with mixed results. Whereas one *in vitro* study suggested using short-duration pulses 354 (< 100 µs) to avoid axonal stimulation (Jensen et al., 2005), another study did not see any benefits of short pulses, and instead suggested using long-duration pulses (>25 ms) or low-frequency 355 356 (< 25 Hz) sinusoidal stimulation (Weitz et al., 2015). One difficulty with these approaches is that 357 they are likely to limit stimulation to a highly restricted amplitude and/or frequency range, 358 potentially limiting the dynamic range available for the encoding of brightness (Greenwald et al., 359 2009; Nanduri et al., 2012).

We show here that percepts are highly consistent over time and can potentially be described using an anatomically detailed computational model with a small number of parameters. Thus, an alternative strategy might be to move away from thinking about artificial sight as a linear combination of 'pixels', and instead accept the perceptual distortions resulting from axonal stimulation as the fundamental building blocks of prosthetic vision.

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374 **5.** Author contributions

- J.W., A.R., G.M.B., and I.F. designed the study. D.N. collected the data. M.B. and A.R. analyzed
- the data. M.B. wrote the software. M.B., D.N., and I.F. wrote the manuscript.

377 6. Declaration of interests

- 378 Authors M.B., JDW, A.R., G.M.B. and I.F. are collaborators with Second Sight Medical Products
- 379 Inc., who develops, manufactures, and markets the Argus II Retinal Prosthesis System referenced
- 380 within this article.

381 7. Methods

382 7.1 Subjects

383 Participants were four blind subjects (one female and three male) with severe retinitis pigmentosa, 384 ranging from 45 to 70 years in age (Table 2). Subjects were chronically implanted with an epiretinal prosthesis as part of an FDA approved clinical trial (clinicaltrials.gov identifier for 385 386 Subject 1: NCT00279500, completed; Subjects 2-4: NCT00407602, active). Surgeries were 387 performed at the Doheny Eye Institute at the University of Southern California (Los Angeles, CA; Subject 1), at the Wilmer Eye Institute at Johns Hopkins School of Medicine (Baltimore, MD; 388 389 Subject 2), at the Moorfields Eye Hospital (London, UK; Subject 3), and at the Royal Eye Hospital (Manchester, UK; Subject 4). None of the subjects had a recordable visual acuity prior to surgery, 390 391 scoring worse than 2.9 logMAR (worse than 20/15,887) on a four-alternative forced-choice 392 square-wave grating test (Ahuja et al., 2013; Caspi et al., 2009).

393 Due to their geographic location, Subjects 2 - 4 were not directly examined by the authors of 394 this study. Instead, initial experimental procedures were sent to the clinical site, and trained field 395 clinical engineers performed the experiments as specified. Raw collected data was then sent to the 396 authors for subsequent analysis.

All tests were performed after obtaining informed consent under a protocol approved by the
 Institutional Review Board (IRB) at each subject's location and under the principles of the
 Declaration of Helsinki.

400

| Subject | Second | Clinical site | Gender | Preoperative | Age at | Years |
|---------|----------|------------------------------|--------|--------------|--------------|-------|
| ID | Sight ID | | | VA | implantation | blind |
| 1 | TB | Doheny Eye Institute, | М | NLP | 55 | 11 |
| | | University of Southern | | | | |
| | | California (Los Angeles, CA) | | | | |
| 2 | 12-005 | Wilmer Eye Institute, Johns | М | NLP | 70 | ? |
| | | Hopkins School of Medicine | | | | |
| | | (Baltimore, MD) | | | | |
| 3 | 51-009 | Moorfields Eye Hospital | F | NLP | 45 | 15 |
| | | (London, UK) | | | | |
| 4 | 52-001 | Royal Eye Hospital | М | BLP | 50 | 21 |
| | | (Manchester, UK) | | | | |

401 **Table 1**: Subject details. Columns 3-7 indicate the implant site, gender, preoperative visual acuity (VA) categorized

402 as either bare light perception (BLP) or no light perception (NLP), the age at implantation, and the number of years

403 participants had been blind prior to implantation (self-reported). Years blind for Subject 2 is unknown due to gradual

404 loss of vision.

406 7.2 Implant specification

- Subject 1 was implanted with a 16-channel microelectrode array (Argus I; Second Sight Medical Products, Inc., Sylmar, CA) consisting of 260 and 520 μ m diameter platinum disc electrodes, subtending 0.9° and 1.8° of visual angle, respectively. Electrodes were spaced 800 μ m apart, and arranged in a 4x4 alternating checkerboard pattern (**Figure 1A**). Subjects 2 – 4 were implanted with a 60-channel microelectrode array (Argus II; Second Sight Medical Products, Inc., Sylmar, CA) consisting of 200 μ m diameter platinum disc electrodes, each subtending 0.7° of visual angle. Electrodes were spaced 525 μ m apart, and arranged in a 6x10 grid (**Figure 1B**).
- All stimuli described in this study were presented in 'direct stimulation' mode. Stimuli were programmed in Matlab using custom software, and pulse train parameters (the electrode(s) to be stimulated, current amplitude, pulse width, individual pulse duration, inter-pulse interval, and pulse train duration) were sent directly to an external visual processing unit (VPU), which was used to send stimulus commands to the internal portion of the implant using an inductive coil link ('camera' mode). The implanted receiver wirelessly received these data and sent the signals to the electrode array via a small cable.
- In day-to-day use, an external unit consisting of a small camera and transmitter mounted on a
 pair of glasses is worn by the user. The camera captured video and sends the information to the
 VPU which converts it into pulse trains using pre-specified image processing techniques.

424 **7.3** Psychophysical methods

- 425 Perceptual thresholds for individual electrodes were measured using an adaptive yes/no procedure 426 implemented using custom software (see Supplemental Information). All presented stimuli were 427 charge-balanced, square-wave, biphasic, cathodic-first pulse trains with fixed stimulus duration 428 (Argus I: 500 ms, Argus II: 250 ms), current amplitude (set at 2x threshold), stimulus frequency 429 (20 Hz) and pulse duration (0.45 ms/phase, no interphase delay).
- Subjects were asked to perform a drawing task with a tactile target (Supplemental Information) or when their retina was electrically stimulated (**Figure 1**). In a given experimental run, a total of n stimulus conditions (either tactile or retinal stimulation) were tested. Each condition was repeated for m trials (for a total of mn trials per experimental run). Repeated trials of the same condition were randomized amongst other stimuli to confirm reproducibility of results.
- 435 Head movement of the Argus I subject was minimized with a chin rest. After each stimulus 436 presentation, the subject traced the shape on a grid screen (containing 6 inch horizontal and vertical 437 grid lines) with a center location aligned horizontally and vertically with the subject's head. 438 Drawing was carried out with a pen whose cap was a different color than its body. A head-mounted 439 camera (Misumi CMOS S588-3T), located on the subject's glasses, was used to record the trials 440 to digital video recorder (DVR). Video files were analyzed off-line to extract shape data using 441 custom built tracking software. In the first stage of processing, the entire image was rotated appropriately using the grid screen background as a reference. In the second stage, vertical and 442

horizontal gridlines, and the distance from the subject to screen were used to set a new coordinate
system in visual angle coordinates (since the subject was 16 inches / 40.6 cm from the screen, 4
gridlines = 70.0 cm corresponded to 73.8 degrees visual angle). In the third stage, the location of
the pen cap was tracked (based on its color) across each frame of the video file. Finally, a binary
shape data file was built from pen cap coordinate locations across all frames.

Argus II subjects were placed in a chair at a comfortable distance from a touch screen monitor 448 with its center location aligned horizontally with the subject's head. The distance from each 449 450 subject's eyes to the screen was recorded. After each stimulus presentation, the subject traced the 451 shape on the monitor and the experimenter advanced to the next trial. Touch screen data were 452 instantly recorded by custom software in 2D coordinates to a text file. Text files were analyzed 453 offline to translate vector coordinates to a binary shape data file. The distance recorded from the subject to screen was used to set a new coordinate system in visual angle. Since Subjects 2-4454 were 33, 30.0, and 30.5 inches from the screen, this corresponded to a display size of 60, 65 and 455 456 64 degrees of visual angle (horizontal screen length), respectively. After translating to the final 457 visual angle coordinate system, the binary image was used in subsequent shape analyses.

458 **7.4 Computational methods**

459 **7.4.1 Phosphene shape descriptors**

460 Phosphene shape was quantified using three parameter-free shape descriptors commonly used in 461 image processing: area, orientation, and elongation (Van der Walt et al., 2014). (Elongation is 462 sometimes also referred to as eccentricity in the literature. We avoid that usage here to prevent 463 confusion with retinal eccentricity). These descriptors are based on a set of statistical quantities 464 known as 'image moments'. For an $X \times Y$ pixel grayscale image, I(x, y), where $x \in [1, X]$ and 465 $y \in [1, Y]$, the raw image moments M_{ij} were calculated as:

$$M_{ij} = \sum_{x} \sum_{y} x^{i} y^{j} I(x, y) \,. \tag{1}$$

466 Raw image moments were used to compute area $(A = M_{00})$ and the center of mass $(\bar{x}, \bar{y}) =$

467 $(M_{10}/M_{00}, M_{01}/M_{00})$ of each phosphene.

468 Phosphene orientation was calculated from the covariance matrix of an image:

$$\operatorname{cov}[I(x,y)] = \begin{bmatrix} \mu'_{20} & \mu'_{11} \\ \mu'_{11} & \mu'_{02} \end{bmatrix},$$
(2)

469 where $\mu'_{20} = M_{20}/M_{00} - \bar{x}^2$, $\mu'_{11} = M_{11}/M_{00} - \bar{x}\bar{y}$, and $\mu'_{02} = M_{02}/M_{00} - \bar{y}^2$. The eigenvectors 470 of this matrix corresponded to the major and minor axes of the image intensity. Orientation (θ) 471 could thus be extracted from the angle of the eigenvector associated with the largest eigenvalue 472 towards the axis closest to this eigenvector:

$$\theta = \frac{1}{2} \arctan\left(\frac{2\mu'_{11}}{\mu'_{20} - \mu'_{02}}\right),\tag{3}$$

- 473 which was valid as long as $\mu'_{20} \neq \mu'_{02}$, with $\theta \in \{-\pi/2, \pi/2\}$. To avoid division by zero, we
- 474 manually assigned an angle of $\theta = 0$ whenever μ'_{20} was equal to μ'_{02} .
- 475 Phosphene elongation (E) was calculated from the eigenvectors of the covariance matrix of 476 Equation (2):

$$E = \sqrt{1 - \frac{\lambda_2}{\lambda_1}},\tag{4}$$

477 where $\lambda_{1,2} = (\mu'_{20} + \mu'_{02})/2 \pm \sqrt{4{\mu'_{11}}^2 + (\mu'_{20} - \mu'_{02})^2/2}$, and $E \in [0, 1]$. An elongation of E = 470

478 1 represents a circle, and E = 0 represents an infinitesimally thin line.

479 **7.4.2** Determination of implant location using fundus photography

- 480 Implant location was estimated by analyzing stereoscopic color fundus photographs obtained using
- 481 systems available at each clinical site. For each subject, we performed the following procedure:
- 482 1. Extract landmarks: On a baseline fundus photograph (before surgery), a retina specialist
 483 marked the foveal pit and the center of the optic nerve head. On the most recent fundus
 484 photograph (after surgery), we marked the center of the implant.
- 2. Combine baseline image with implant image: We performed image registration using featurematching to bring the two images into the same coordinate system.
- 487 3. Adjust for magnification: Pixel distances were converted to retinal distances by using the
 488 known electrode-electrode spacing (Argus I: 800 μm, Argus II: 525 μm).
- 489 4. Adjust for rotation: We approximated the horizontal raphe by fitting a parabola to the main
 490 vascular arcade, assuming that the center of the optic nerve head lied at the vertex of the
 491 parabola, and that the raphe was parallel to the parabola's axis of symmetry (Chin et al., 2013;
 492 Tobin et al., 2007).
- 5. Coordinate transform: The registered image was rotated so that the horizontal raphe came to
 lie on the abscissa, and the foveal pit at the origin of the new coordinate system. We located
 the coordinates of the center of the optic nerve head as well as the center of the array (from
 Step 1) in this new coordinate system. Retinal distances (µm) were related to eccentricity (deg)
 using a formula that computes the relationship between retinal arc lengths and visual angles
 from based on the optic axis (Watson, 2014).
- 6. The extracted landmarks were then used to place a simulated array on a simulated map ofganglion axon pathways using the pulse2percept software (Beyeler et al., 2017a).
- 501 This procedure allowed us to estimate each subject's array location and orientation with respect to
- 502 the fovea (**Table 3**). Based on fundus photographs of 104 sighted humans (Rohrschneider, 2004),
- 503 the center of the optic disc was expected to be located at $15.5^{\circ} \pm 1.1^{\circ}$ nasal, $1.5^{\circ} \pm 0.9^{\circ}$ superior
- 504 with respect to the fovea. For all four subjects, the estimated center of the optic disk was within
- 505 two standard deviations of these expected values.

| Subject ID | Array center (x, y; μm) | Array rotation (deg) | Optic disc center (x, y; deg) |
|------------|-------------------------|----------------------|-------------------------------|
| 1 | (-651, -707) | -49.3 | (14.0, 2.40) |
| 2 | (-1331, -850) | -28.4 | (16.2, 1.38) |
| 3 | (-467, 206) | -25.8 | (14.0, 1.24) |
| 4 | (-1807, 401) | -22.1 | (16.3, 2.37) |

506 **Table 2**: Estimated locations of the implant and optic disc with respect to the fovea located at (0, 0) using fundus 507 photography. Array rotation was measured with respect to the horizontal raphe.

508

509 7.4.3 Scoreboard model

510 The scoreboard model assumed that electrical stimulation led to the percept of focal dots of light,

511 centered over the visual field location associated with the stimulated retinal field 512 location (x_{stim}, y_{stim}), whose spatial intensity profile decayed with a Gaussian profile (Hayes et

513 al., 2003; Thompson et al., 2003):

$$I_{\text{score}}(x, y; \rho) = \exp\left(-\frac{(x - x_{\text{stim}})^2 + (y - y_{\text{stim}})^2}{2\rho^2}\right),$$
(5)

514 where ρ was the spatial decay constant.

515 The resulting intensity profile $I_{\text{score}}(x, y; \rho)$ was then thresholded to obtain a binary image. 516 The threshold was chosen as $1/\sqrt{e}$, such that points closer than ρ to $(x_{\text{stim}}, y_{\text{stim}})$ were assigned 517 a value of 1, and all other points were assigned a value of 0.

518 **7.4.4** Axon map model

519 Following Jansonius et al. (2009), we assumed that the trajectories of the optic nerve fibers could

be described in a modified polar coordinate system (r, ϕ) with its origin located in the center of

521 the optic disc. A nerve fiber was modeled as a spiral:

$$\phi(r,\phi_0) = \phi_0 + b(r,\phi_0)(r-r_0)^{c(r,\phi_0)},\tag{6}$$

522 where $\phi_0 = \phi(r = r_0)$ is the angular position of the trajectory at its starting point at a circle with

radius r_0 around the center of the optic disc, b a real number describing the curvature of the spiral,

$$b(\phi_0, r) = \begin{cases} \exp\left(-1.9 + 3.9 \tanh\left(\frac{-(\phi_0 - 121)}{14}\right)\right), r \ge 0 \\ -\exp\left(0.7 + 1.5 \tanh\left(\frac{-(-\phi_0 - 90)}{25}\right)\right), r < 0, \end{cases}$$
(7)

and c a positive real number describing the location of the point of maximal curvature,

$$c(\phi_0, r) = \begin{cases} 1.9 + 1.4 \tanh\left(\frac{\phi_0 - 121}{14}\right), r \ge 0\\ 1.0 + 0.5 \tanh\left(\frac{-\phi_0 - 90}{25}\right), r < 0. \end{cases}$$
(8)

Jansonius and colleagues determined parameter values by fitting Equations (6–8) to the topographical layout of 55 eyes from 55 human subjects (for details see Jansonius et al., 2009).

- 527 The attentive reader might notice that Equation (8) above fixes a typo in Equation (3) of Jansonius
- 528 et al. (2009): The tanh numerator should indeed read $\phi_0 121$, not $-(\phi_0 121)$.
- 529 To apply the axon map to the eyes of our subjects, we first transformed the original coordinate
- 530 system (r, ϕ) to Cartesian coordinates (x, y) with the foveal pit located at (0, 0), and then set the
- 531 coordinates of the optic disc (x_{od}, y_{od}) to the values estimated from fundus photography (**Table**

532 3). The resulting axon maps for each subject can be seen in Figure 4.

533 An axon's sensitivity to electrical stimulation was assumed to decay exponentially with 534 distance from the soma (x_{soma}, y_{soma}) :

$$I_{\text{axon}}(x, y; \rho, \lambda) = I_{\text{score}}(x, y; \rho) \exp\left(-\frac{(x - x_{\text{soma}})^2 + (y - y_{\text{soma}})^2}{2\lambda^2}\right),\tag{9}$$

- 535 where λ was the spatial decay constant along the axon. $I_{score}(x, y; \rho)$ is the same as in Equation
- 536 (5) and is parameterized by a single parameter, ρ . As in the scoreboard model, the resulting 537 intensity profile $I_{axon}(x, y; \rho, \lambda)$ was thresholded to obtain a binary image.

538 7.4.5 Model fitting and evaluation

- 539 To fit the scoreboard and axon map models to subject drawings, we first calculated the coefficient
- of determination (R^2) from the predicted binary images and the corresponding ground-truth subject
- 541 drawings. R^2 was calculated from the ratio of the residual sum of squares (SS_{res}) and the total sum
- of squares (SS_{tot}) for each shape descriptor (area, orientation, or elongation):

$$R^2 = 1 - \frac{SS_{\rm res}}{SS_{\rm tot}},\tag{10}$$

$$SS_{res} = \sum_{i} (s_i - \hat{s}_i)^2,$$
 (11)

$$SS_{tot} = \sum_{i}^{r} (s_i - s)^2,$$
 (12)

- 543 where s_i was the shape descriptor for the *i*-th ground-truth image, \hat{s}_i was the shape descriptor for
- the *i*-th predicted image, and \bar{s} was the mean of the shape descriptor averaged over all images. The three quantities R_{area}^2 , $R_{\text{orientation}}^2$, and $R_{\text{elongation}}^2$ resulting from this procedure were then combined to construct a cost function that could be iteratively minimized:

$$c = \sum_{d} 1 - R_d^2, \tag{13}$$

where d = {area, orientation, elongation}. Due to the nonconvexity of this optimization problem,
we minimized the cost function using particle swarm optimization (Kennedy and Eberhart, 1995).
We set the swarm size at ten times the number of parameters (Storn, 1996). We ran every fitting
procedure five times with different, randomly chosen initial conditions, and then chose the best
run in subsequent analyses.

552 To allow for a fair performance comparison despite the scoreboard and axon map models 553 having different numbers of parameters, we implemented a leave-one-electrode-out cross-554 validation procedure, where we repeatedly fit each model to the drawings from all but one 555 electrode in the array. This is equivalent to calculating the Akaike Information Criterion that takes 556 into account the difference in number of parameters (Stone, 1977). The fitted parameter values 557 were then used to predict the shape descriptors of the held-out drawings (Figure 13). Note that a 558 single value of ρ and λ was fitted for each subjects, and then used for all electrodes in that subject's 559 array.

560 **7.5 Data and software availability**

561 Data are available on the Open Science Framework (doi:10.17605/osf.io/dw9nz). The software

used for analyses was based on the pulse2percept Python package (Beyeler et al., 2017a). Scripts

used to fit the scoreboard and axon map models, to analyze the data, and to produce the figures in

the paper are available on GitHub (https://github.com/VisCog/ArgusShapes.git, v0.1).

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