Random Tanglegram Partitions (Random TaPas): An Alexandrian Approach to

the Cophylogenetic Gordian Knot

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Abstract

Symbiosis is a key driver of evolutionary novelty and ecological diversity, but our

understanding of how macroevolutionary processes originate extant symbiotic associations is

still very incomplete. In this context, cophylogenetic tools are used to assess the congruence

between the phylogenies of two groups of organisms related by extant associations. If

phylogenetic congruence is higher than expected by chance, we conclude that there is

cophylogenetic signal in the system under study. However, none of the current cophylogenetic

methods quantifies the degree of cophylogenetic signal satisfactorily. We present a novel

approach, Random Tanglegram Partitions (Random TaPas) that applies a given global-fit

method to random partial tanglegrams of a fixed size to identify the associations, terminals and

nodes that maximize phylogenetic congruence. By means of simulations, we show that the

output value produced is inversely proportional to the number of cospeciation events employed

to build simulated tanglegrams. In addition, with time-calibrated trees, Random TaPas is also

efficient at distinguishing cospeciation from pseudocospeciation. Random TaPas can handle

large tanglegrams in affordable computational time and incorporates phylogenetic uncertainty in

the analyses. We demonstrate its application with two real examples. In both systems, Random

TaPas revealed low cophylogenetic signal, but mapping its variation onto the tanglegram

pointed two different coevolutionary processes accounting for this result. Finally, we suggest

that the recursive partitioning of the tanglegram buffers the effect of phylogenetic

nonindependence occurring in current global-fit methods and therefore Random TaPas is more

reliable to identify host-symbiont associations that contribute most to cophylogenetic signal

than regular global-fit methods. Random TaPas can be implemented in the public-domain

statistical software R with scripts provided herein.

Keywords: Symbiosis, Coevolution, Codiversification, Cophylogenetic Signal.

INTRODUCTION

Symbiosis is widespread throughout the tree of life and is considered as a key driver of

evolutionary novelty and ecological diversity (Moran 2006; Zook 2015). Because organisms do

not evolve in isolation, the evolutionary fate of symbiotic partners is intertwined at ecological

and evolutionary levels, but despite the centrality of symbiosis in evolutionary biology, our

understanding of how macroevolutionary processes originate extant symbiotic associations is

still very incomplete (Weber et al. 2017). However, the recent emergence of robust comparative

phylogenetic methods has expanded and facilitated research in this area (Hutchinson et al.

2017a). Cophylogeny, in particular, provides a quantitative framework to evaluate the

dependency of two evolutionary histories (Hutchinson et al. 2017b). This approach involves

some assessment of the congruence between the phylogenies of two groups of species or taxa

related by extant associations, where congruence quantifies the degree of both topological and

branch-length similarity (Page 2003). If such congruence is higher than expected by chance, it

is concluded that there is cophylogenetic signal in the system studied (Mendlová et al. 2012).

Although cophylogenetic signal was initially interpreted as evidence of high level of

cospeciation, it has been shown that other mechanisms can account for some degree of

topological congruence. Particularly, complete host-switching events (i.e., colonization of a new

host species followed by speciation) among closely related hosts can result in symbiont

diversification mimicking the tree topology of the host, a process that has been termed

pseudocospeciation (de Vienne et al. 2013). In any case, even if its causality cannot not be

determined, detecting cophylogenetic signal is highly relevant because it implies that

contemporary ecological associations among species have been the product of a coupled

evolutionary history such that ancestral forms of each species experienced and responded to

shared selection pressures (Hutchinson et al. 2017b).

The wide range of cophylogenetic methods currently available can be roughly

categorized as either event-based or global-fit (Hutchinson et al. 2017a), but none of them deal

with cophylogenetic signal satisfactorily. Event-based methods attempt to reconstruct the

coevolutionary history of the organisms involved by assigning costs to each type of event and

heuristically search for the solution(s) that minimize(s) the overall sum of costs (Charleston and

Libeskind-Hadas 2014). The problem is that cophylogenetic signal can be easily overestimated

because the default cost of cospeciation is assumed to be zero, which is often at odds with

empirical evidence (de Vienne et al. 2013). In addition, with large datasets, the approach

becomes computationally prohibitive and the influence of phylogenetic uncertainty is not

explicitly considered (i.e., the single input phylogenetic trees of host and symbionts are assumed

to represent the actual evolutionary relationships), which may lead to erroneous conclusions if

not all clades are well supported. Global-fit methods, for their part, assess the degree of

congruence between two phylogenies and can also identify the specific interactions that

contribute most to overall congruence (Balbuena et al. 2013). They can handle large datasets

economically in terms of computational time, and the effect of phylogenetic uncertainty can be

assessed (Pérez-Escobar et al. 2016). However, current methods such as PACo (Balbuena et al.

2013) or ParaFit (Legendre et al. 2002), provide statistical evidence of cophylogenetic signal,

but produce no directly interpretable statistic as for its strength and no explicit links with

coevolutionary events are made.

Therefore, additional work remains to be done in this domain. Particularly, the recent,

spectacular expansion of DNA sequencing and phylogenetic reconstruction is leading to

increasingly common scenarios involving species-rich trees and complex host-symbiont

interactions (e.g., Hutchinson et al. 2017b). Equating these elaborate systems to evolutionary

Gordian knots, we present herein an Alexandrian approach to cophylogenetic signal assessment.

Random Tanglegram Partitions (Random TaPas) applies a given global-fit method to random

partial tanglegrams of a fixed size to identify the associations, terminals and nodes that

maximize phylogenetic congruence. By means of simulations, we show that the output value

produced by Random TaPas is inversely proportional to the number of cospeciation events

employed to build the tanglegrams. In addition, with time-calibrated trees, Random TaPas is

also efficient at distinguishing cospeciation from pseudocospeciation. The method is also useful

to identify what host-symbiont associations contribute most to phylogenetic congruence because

the variation in cophylogenetic signal can be mapped onto the tanglegram. We illustrate its

application with two real datasets and show how it can incorporate phylogenetic uncertainty in

the analyses. R scripts (R Core Team 2018) to perform Random TaPas and a user's guide are

also provided.

MATERIALS AND METHODS

The Random-TaPas algorithm

The starting point is a triple (H, S, $\mathbf{A}$), where H and S represent the phylogenies of hosts and

symbionts, and $\mathbf{A}$ is a binary matrix with rows and columns corresponding to terminals in H and

S, respectively, in which extant associations between each terminal are coded as 1 and no

associations as 0. The triple is often represented graphically as a tanglegram (Fig. 1), in which H

and S usually are displayed face to face and their terminals are connected by lines reflecting the

associations encapsulated in $\mathbf{A}$. Figure 1 provides a complete overview of the Random TaPas

algorithm. In short, for a large number of times (N), it selects n random unique one-to-one

associations, so that each taxon in H is associated to one, and only one, taxon in S, and vice

versa. (Since the aim is to find associations that maximize congruence, this is a condition to be

met by any perfect host-symbiont cospeciation scenario). Then a global-fit method is applied to

the partial tanglegram defined by the n associations and the statistic produced is saved. Finally,

a percentile p of the distribution of the N statistics generated is set and the frequency of

occurrence of each host-symbiont association of $\mathbf{A}$ included in p is computed.

The output of Random TaPas is a frequency distribution of host-symbiont associations

in which each value is expected to be directly proportional to the contribution of the host-

parasite association to the global pattern of phylogenetic congruence (Figure 1). The shape of

this distribution can be characterized by computing the variance to mean ratio (VMR) of the

frequencies, whose value is biologically informative. In a perfect cospeciation scenario, VMR

= 0 is expected because each host-symbiont association would contribute equally to the global

fit, yielding a uniform frequency distribution. Thus, cophylogenetic signal would be significant

and maximal. If the association between H and S were completely random, the frequency

distribution would follow a Poisson distribution with VMR = 1 and cophylogenetic signal

would be not significant. Finally, unequal contributions of the host-symbiont associations would

lead to skewed frequency distributions with VMR >> 1 and, if significant, VMR would be

inversely proportional to cophylogenetic signal.

Global-fit methods

Random TaPas can be applied in conjunction with any global-fit method. For the sake of

demonstration, we chose here two very different approaches: Procrustes Approach to

Cophylogeny (PACo) (Balbuena et al. 2013) and geodesic distances (GD) in tree space (Schardl

et al. 2008). PACo uses Procrustean superimposition of Euclidean embeddings of the

phylogenetic trees to assess phylogenetic congruence (Balbuena et al. 2013). The second

approach entails computing pairwise GDs between the partial phylogenies defined by n. Most

global-fit methods translate matrices of evolutionary distances into Euclidean space whose

dimensionality is higher than that of tree space (Holmes 2005). So the advantage of this

approach is that it skips the potential effect of this dimensional mismatch. In both methods, the

value of the statistic produced is inversely proportional to statistical congruence.

PACo was performed with package paco (Hutchinson et al. 2017b) employing patristic

distances as input. Its use with Random TaPas is aimed at finding the set of partial tanglegrams

that minimize the square sum of residuals (m^2_{XY}) of the Procrustes superposition of host and

symbiont spatial configurations in p. The use of GDs with Random TaPas attempts to find the

set of partial tanglegrams in p with minimal pairwise distances in tree space. These distances

were computed with function dist.multiPhylo of package distory in R (Chakerian and Holmes

2010).

Synthetic data

The operation of Random TaPas depends on three parameters: N, n and p (Fig. 1). We assessed

performance with different parameter combinations and the two aforementioned global fit

methods with 200 synthetic tanglegrams generated with CoRe-Gen (Keller-Schmidt et al. 2011).

For a given set of input parameters, the program provides a pair of resulting ultrametric trees, a

list of associations between the terminals and the number of coevolutionary events

(cospeciation, duplication, sorting, and complete host-switching) involved in the construction of

the tanglegram. Since it is not possible to accurately control a priori the output based on the

input parameters, we first generated a library of 1,000 tanglegrams. The trees were built

following a pure-speciation (Yule) model, which has been shown to describe adequately

empirical phylogenetic trees (Hagen et al., 2015). For each host-symbiont pair, we specified a

different random combination of input parameters sampled from a uniform distribution. The

parameters and sampling ranges were: number of generations (100-200), probability of

cospeciation event (0.2-1.0), probability of host-switching event (0.2-0.8) and probability of

choosing a host for speciation instead of a parasite (0.7-1.0). Because our method is intended for

a wider range of settings than those considered by Keller-Schmidt et al. (2011), the parameter

ranges are broader than those used originally. Thus, our resulting tanglegrams included

scenarios where cospeciation events ranged from very rare to very common. Since some

combinations of parameters yielded trees with few terminals (≤ 15) or numbers of host parasite

associations (≤ 20), we ran CoRe-Gen 1,274 times to obtain a set of 1,000 workable

tanglegrams.

Given that Random TaPas is specially intended for large tanglegrams, we chose for

subsequent analyses two sets of 100 tanglegrams each involving approximately 50 (mean =

50.5, median = 51, range: 47-54) and 100 (mean = 99.7, median = 100, range: 93-107) host-

symbiont associations, respectively. For convenience, these subsets will be henceforth referred

to as Set50 and Set100, respectively. Since some trees included terminal polytomies and GD

requires fully resolved trees, we added 0.01 arbitrary units of time to all terminal branches. A

limitation of Core-gen is that it only generates coevolutionary systems in which each symbiont

can be associated with only a single host. Given that many real-world scenarios do not conform

to this scenario (e.g., Example 2 below), we modeled the occurrence of colonization (aka host-

sharing) by a given symbiont of several hosts following Drinkwater et al. (2016). For each

triple, a rate of host sharing of 0%, 10% or 20% of the total available host species was set

randomly. Then colonization was simulated by selecting each terminal in S and allowing the

corresponding symbiont to colonize a random number x of additional hosts, $\{x \in \mathbb{Z} \mid 0 \leq x \leq R$

$\times N_h\}$, where R represents the rate of host sharing for the given tanglegram and N_h the total

number of host terminals.

Since additive trees (i.e., phylograms) estimated from molecular sequence data are

commonly used in cophylogenetic analyses, we ran the simulations with the original ultrametric

trees and phylograms derived from them. The transformation of the ultrametric trees into

phylograms was done by multiplying their branch lengths by varying rates of molecular

substitution (Brown and Yang 2011; Paradis 2014), sampled from a log-normal distribution

with mean 0.01 substitutions/site/time unit (Brown and Yang 2011).

Simulations

We applied Random TaPas to Set50 and Set100 (both additive and ultrametric trees) using both

PACo and GD with all combinations of the following parameter values: $N=10^4$, $n=5$, 10 and 20

(Set50), and $n=10$, 20 and 40 (Set100) (i.e., n representing about 10%, 20% and 40% of the total

associations), and $p=1\%$ and 5%. In preliminary analyses, $N=10^5$ was also tested with additive

trees in combination with the same arrays of n and p values but the results were very similar to

those obtained with $N=10^4$ (Supplementary Figures S1 and S2 in Supplementary Material).

Since the increased computing time resulting from using a larger N did not result in a detectable

improvement in performance of the method, $N=10^5$ was not further considered. In simulations

involving additive trees, prior to running PACo the patristic distances were rendered Euclidean

by taking the element-wise square root of each cell in order to minimize geometric distortion

and avoid negative eigenvalues (de Vienne et al. 2011).

For each simulation, the VMR of the frequency distribution of host-symbiont

associations produced by Random TaPas was computed. We assessed the relationship between

the VMRs of each set of simulations and the number of coevolutionary events (cospeciation,

duplication, sorting, host-switching and colonization) associated to each tanglegram in two

ways. First, regression trees were built with a recursive-partitioning function of package rpart in

R (Therneau and Atkinson 2018). This approach is indicated to provide a general picture of the

structure of the data and reveal complex interactions between variables (Crawley 2013). The

importance of each coevolutionary event in each tree model (scaled to sum 1) was computed

according to Therneau and Atkinson (2018). In addition, the coefficient of determination of

each model (R^2) was computed as the 1–relative error at the last split (Therneau and Atkinson

2018). Second, we computed the correlation coefficients between VMR of frequency

distributions and the numbers of each of the coevolutionary events.

Pseudocospeciation experiment

In order to assess the ability of Random TaPas to distinguish between cospeciation and

pseudocospeciation (de Vienne et al. 2007), we selected a triple (#63) in Set50 with high

cospeciation signal. This simulated host-symbiont system resulted from 50 cospeciations, 1

sorting, 2 duplications, 1 complete host-switching and 0 colonization events. We arbitrarily

selected a clade of 17 terminals to simulate rapid colonization and speciation of the symbiont

lineage (de Vienne et al. 2007). In both the ultrametric and additive trees versions of the

tanglegram, the branch lengths of the clade were shortened to half their original length, whereas

its basal branch was lengthened to keep the original height of the clade. We applied Random

TaPas to the original and modified tanglegrams using GD, $N = 10^4$, $p = 5\%$ and $n = 5, 10$ and

20. The ability of Random TaPas to distinguish cospeciation from pseudocospeciation was

assessed by plotting as a heatmap on the tanglegram, the frequency of occurrence of each host-

symbiont link and the average frequency of occurrence of each terminal in p.

Biological Examples

To gain further insight on its performance and provide further guidance to prospective users, we

demonstrate the application of Random TaPas to two real-world examples. The trees,

association matrices and R scripts used with each example are available at

https://github.com/Ligophorus/RandomTaPas.

Example 1: Neotropical orchids and their euglossine pollinators.— We used the association

data and published chronograms of pollinated orchids and their corresponding bee pollinators

(Ramírez et al. 2011). The posterior probability trees of orchids and euglossine bees to build the

consensus were kindly supplied by Santiago Ramírez, University of California Davis.

Random TaPas was run with GD and PACo, $N = 10^4$, $n = 29$ and $p= 5\%$. This example

involves 129 bee-orchid associations. The n value chosen was the maximum number of one-to-

one associations that could be formed over the 10^4 runs, and it is close to the 20% we

recommend based on results of the preceding simulations. In order to account for taxonomic

uncertainty, we computed 95% confidence intervals of the host-symbiont frequencies of each

association using a random sample (excluding the burn-in set) of 1,000 pairs of the posterior-

probability trees used to build the consensus trees of euglossine bees and orchids. Random

TaPas was run for each tree pair as specified above and the 2.5% and 97.25% percentiles of

each host-symbiont association frequency were computed.

We also assessed the different contribution of each host-symbiont association to the

global cospeciation signal by displaying as heatmap on the tanglegram their frequency of

occurrence and the average frequency of occurrence of each terminal occurring in p. Taking the

latter as a continuous trait, fast maximum likelihood estimators of ancestral states were

computed with fastAnc of package phytools in R (Revell 2012), and their values were displayed

on the nodes of the phylogeny as a color scale. We adopted this approach only to assess

different levels of cophylogenetic signal across the tanglegram and by no means imply that we

consider these estimators to reflect actual ancestral states of host-symbiont associations. In

addition, we used negative binomial regressions (glm.nb function from the MASS package in R,

Venables and Ripley 2002) to test for differences in average frequency of occurrence of each

terminal in *p* among three main clades that represent each an orchid subtribe.

Example 2: Coitocaecum parvum *and its amphipod host.—* Data of mitochondrial haplotypes of

the cytochrome oxidase subunit 1 of the trematode, *Coitocaecum parvum* (Crowcroft, 1945),

and those of its amphipod host, *Paracalliope fluviatilis* (Thomson, 1879), in seven locations in

South Island, New Zealand from Lagrue et al. (2016). This example is worked out in the

Random TaPas User's Guide (available at https://github.com/Ligophorus/RandomTaPas).

251   Random TaPas was run with GD and PACo, $N = 10^4$, $n = 8$ and $p = 5\%$ to evaluate the

extent to which genetic differentiation among populations was coupled with local adaptation

patterns (Lagrue et al. 2016). We chose $n = 8$ because it is a good compromise between the

number of unique combinations of unique one-to-one associations that can be evaluated over

10^4 runs and the fraction of total number of host-symbiont associations (8 of 75, i.e., $\approx 10\%$).

(The accompanying R script and the user's guide demonstrates the strategy followed to choose

the best *n* for this example). PACo by default assumes dependency of one phylogeny upon the

other. Since in this case codivergence between host and parasite lineages was assumed to be

reciprocal, PACo was run in symmetric mode (Hutchinson et al. 2017a). Estimation of

confidence intervals of the host-symbiont frequencies and mapping of results on the tanglegram

was performed as in Example 1.

RESULTS

Simulations

Not all simulations could be performed because, in some tanglegrams, the number of possible

unique one-to-one associations between terminals was less than the number *n* set in simulations.

So the number of tanglegrams produced in Set50 with $n = 20$, was 79; and those in Set100 with

$n = 20$ and $n = 40$ was 99 and 63, respectively.

268   Forty-eight regression tree models describing the relationship between VMR of host-

symbiont frequency distributions and the number of evolutionary events of tanglegrams

involving the additive and the original ultrametric trees with all combinations of *n* and *p* and

global-fit method employed were produced. The average and range of VMRs corresponding to

each parameter combination are given in Table 1. Figure 2 shows the regression trees

corresponding to Set50, additive trees, applying GD with all combinations of p and n. In

general, the patterns were similar to those obtained with PACo and with other parameter

combinations (Supplementary Figures S3-S9) and the R^2 values suggest good agreement of the

models with the data. The number of cospeciation events determined the first node in 43 of the

models, but the placement of evolutionary events at subsequent nodes was very variable. In the

remaining models, the number of sorting (4 instances) or duplication events (1 instance)

determined the first split. These five models involved simulations in which $n \approx 10\%$ of the total

number of host-symbiont associations (Supplementary Figures S5, S8, S9). Figure 3 shows the

relative importance of each evolutionary event in building the regression tree models. In 42

instances, the number of cospeciation events was the most important predictor of VMR,

accounting for > 40% of the total in 38 cases. In six models, the number of cospeciation events

was ranked as the second (5 cases) or third variable (1 case) in importance. These six cases

involved models in which n represented $\approx 10\%$ of the host-symbiont associations. Two and four

of these were produced with GD and PACo, respectively. Five of the six cases were produced

by models based on ultrametric trees and four were produced with Set100.

The correlation with the number of cospeciation events was significant ($P < 0.01$) in all

simulations, ranging between -0.31 and -0.74. In 38 of 48 parameter combinations (16 of Set50

and 22 of Set100), the highest absolute correlations of VMR with the number of evolutionary

events involved those with the number of cospeciations (Fig. 4). In the 10 remaining parameter

combinations, the absolute value of the correlation coefficient with the number of cospeciation

events was ranked second, but was very close to those of the first (duplications) and involved

five cases each produced with GD and PACo. Eight of those cases involved simulations with

additive trees and four cases represented simulations in which $n \approx 10\%$ of the associations.

Pseudocospeciation experiment

In the additive trees, host-symbiont associations involving the modified clade were marked as highly congruent, showing similar values to those in the original tanglegram, independently of the n value chosen (Fig. 5). In contrast, the counterpart associations in the ultrametric trees were marked as incongruent with $n = 5$ and 10, but not with $n = 20$ (Fig. 6).

Example 1: Neotropical orchids and their euglossine bee pollinators

The frequency distributions of pollinator-orchid associations produced by Random TaPas with GD and PACo were highly skewed (Fig. 7a, b). The VMR of these frequencies obtained with the consensus trees were 30.03 and 30.29 for Random TaPas run with GD and PACo, respectively. Similar VMR values were obtained with the 1,000 pairs of trees used to compute the confidence intervals of the frequencies (Fig. 7c). Both GD and PACo revealed that nine pollinator-orchid associations were highly congruent, as they occurred in 100% of cases (Fig. 7). These associations were unrelated since involved orchids species of the three subtribes represented: Catasetinae (1 *Galeandra*, 1 *Catasetum* species), Zygopetalinae (1 *Chondrorhyncha* species) and Stanhopeinae (2 *Coryanthes*, 1 *Gongora*, and 2 *Soterosanthus* species) (Fig. 8). There were no significant differences among the orchid subtribes in the average frequency of occurrence of their terminals in p (negative binomial regression, $P > 0.40$ using both GD and PACo).

Example 2: Coitocaecum parvum *and its amphipod host*

The frequency distributions of the associations between haplotypes produced by Random TaPas were highly skewed (Fig. 9). The wide confidence intervals associated with many host-symbiont associations (Fig. 9a, b) indicate the relatively high uncertainty about the placement of some nodes, but the VMRs were consistently high (> 20) (Fig. 9c). The frequencies plotted on terminals and nodes of the tanglegram indicate a higher signal between two early-branching clades of both phylogenies (Fig. 10). These represent host haplotypes from the Waikouaiti and Waitaki Rivers associated with parasite haplotypes of the latter.

DISCUSSION

Herein we have developed Random TaPas that uses a given global-fit method for analysis of

large tanglegrams and produces an index (VMR) that quantifies cophylogenetic signal in the

data. In fact, the simulations indicated that VMR is inversely proportional to the number of

cospeciation events used to build the evolutionary histories of hosts and symbionts. This is

consistently shown with most parameter combination tested (particularly when $n \geq 20\%$ of the

total number of host-symbiont associations) and global-fit method used. When $n \approx 40\%$ the

correlation between VMR and number of cospeciation events tend to be higher, but note that not

all simulations could be executed and those excluded represented cases with low number of

cospeciation events. This is because the highest possible n of a given host-symbiont system

conveys the maximum quantity of unique host-symbiont associations and its value is

constrained by the nature of the joint evolutionary history. Thus this upper limit is informative

of the amount of cophylogenetic signal in the system. For instance, in Example 2, out of 75

host-symbiont associations the highest possible n was 5 or 6 (depending on the randomization)

over 10^4 trials, anticipating the low cospeciation signal detected. If possible, we recommend

setting n at least 10%, and ideally around 20%, of the total number of associations because the

simulation results suggest that the relationship with the number of cospeciation events becomes

stronger. In addition, with ultrametric trees, $n \approx 20\%$ seems to provide a good balance between

capturing cophylogenetic signal and detecting potential pseudocospeciation events.

The choice of p and global-fit method seems secondary to that of n, but note that $p = 1\%$

tended to produce more skewed distributions than $p = 5\%$ (Table 1). Random TaPas has been

developed with two very different global-fit approaches. As noted above a potential of GD over

PACo, and most other global-fit methods, is that it skips the potential effect of the dimensional

mismatch between Euclidean and tree spaces (Holmes 2005). However, GD performed only

marginally better than PACo in terms of relationship between VMR and number of cospeciation

events, and overall results were very similar. This evidence points to robustness of Random

TaPas to parameters and method utilized. In fact, the algorithm can be readily adapted to other

global-fit methods. In a preliminary analysis, we ran it with ParaFit (Legendre et al. 2002),

Set50, $n = 20$, yielding very similar results to those presented here in terms of relationship with

the number of cospeciation events (unpublished data).

Although VMR can be related with the amount of cophylogenetic signal in the system, a

current limitation is that it has no upper bound, and its value seems to depend on variables such

as p and tanglegram size (Table 1), which makes it difficult to compare the degree of

cophylogenetic signal among different data sets. So further work is needed on standardization or

normalization of metrics of cophylogenetic signal. However, the results of the present or future

simulations could be used as a benchmark to assess the degree of cophylogenetic signal in a

given host-symbiont system. This is particularly valuable because current global-fit methods

test for congruence between phylogenies, but do not quantify in a meaningful way the strength

of the relationship. For instance, in Example 2, Lagrue et al. (2016) applied PACo and ParaFit

to their data and reported highly significant ($P < 0.001$) evidence for cophylogenetic signal.

Likewise, applying the same analyses to Example 1 leads to a similar conclusion (PACo: $m^2_{XY} =$

$1.52 \cdot 10^5$, $P < 0.0001$; ParaFit: ParaFitGlobal $= 1.18 \cdot 10^9$, $P < 0.0001$). However, in both

examples the estimated VMR values were around 30 which falls above the ranges computed in

the simulated tanglegrams, particularly the large ones (Set100) (Table 1), which strongly

suggests that cospeciation (Example 1) or codiversification (Example 2) did not play a

prominent role in the evolutionary history of these systems. In Example 1, the most congruent

associations were scattered in the tanglegram, which agrees with the hypothesis that preexisting

traits in the euglossine bees (i.e., collection of aromatic compounds), rather than cospeciation,

drove floral adaptation and diversification in euglossine-bee pollinated orchids (Ramírez et al.

2011; Pérez-Escobar et al. 2017). By contrast, in Example 2, cophylogenetic signal was

unevenly distributed being stronger in the early-divergent lineages of both phylogenies. This

would account for the mismatch between the genetic differentiation and local adaptation

patterns that Lagrue et al. (2016) found it difficult to account for, and supports a scenario of

geographically structured differences in codiversification proposed by these authors.

A problem with global-fit methods is that they do not correct for phylogenetic

nonindependence, so that comparison of pairwise distance matrices derived from host and

symbiont phylogenies gives greater weight to pairs that include deeper most recent common

ancestors (MRCAs) than those involving shallower ones (Schardl et al. 2008; de Vienne et al.

2013). To deal with this issue, Schardl et al. (2008) proposed selecting a single pairwise

distance per MRCA prior to evaluation of congruence between two phylogenies globally.

However, this approach is not immediately applicable to assess the contribution of individual

host-symbiont associations to the global fit.

Without correction for nonindependence, phylogenetic congruence between old MRCAs

is expected to be propagated towards the descendent terminals. So associations between them

would tend to be identified as congruent even if the placement of their more recent MRCAs is

not. In Example 2, for instance, ParaFit indicated that all except two associations contributed

significantly ($P<0.05$) to congruence, whereas PACo rendered 45 associations in which the

confidence intervals of their associated squared residuals fell below the median squared residual

value (Lagrue et al. 2016). In contrast, Random TaPas identified only seven (GD) or eight

(PACo) trematode-amphipod associations whose confidence intervals of their frequency of

occurrence in p was above the expected frequency of a uniform distribution (perfect

codiversification scenario). This restricted number of supposedly congruent associations agrees

better with the low cophylogenetic signal detected. So although further work is needed to clarify

this issue, we suggest that, although nonindependence is not completely accounted for in the

partial tanglegrams, the evaluation of a limited set of associations over a large N seems to buffer

the effect of phylogenetic nonindependence. So Random TaPas would represent a better way to

determine which host-symbiont associations contribute most to cophylogenetic signal than

current global-fit methods. In any case, we find that the mapping of cophylogenetic signal on

the tanglegram is an extremely useful new tool for the analysis of coevolutionary histories as it

allows evaluating variation in cophylogenetic signal and testing specific hypotheses, such as

differences among taxa as illustrated in Example 1.

A final word of caution is that the effects of cospeciation and pseudospeciation on

cophylogenetic signal can be difficult to tease apart, especially if the trees are not dated.

However, one would expect pseudocospeciation to be more prevalent if host trees are clustered

in few large clades and in those with rapid species turnover (rapid adaptive radiations),

particulary if symbionts are highly specific (Engelstädter and Fortuna 2018). With dated trees,

our results suggest that marked differences in frequency of host-symbiont associations with

varying *n* can give clues about the presence of pseudocospeciation in the system.

In summary, Random TaPas represents a new tool for cophylogenetic analysis that

provides a framework to assess cophylogenetic signal in a given host-symbiont system. In

addition, it facilitates data interpretation by mapping the extent of cophylogenetic signal on the

tanglegram. The method can handle large tanglegrams in affordable computational time,

incorporates phylogenetic uncertainty, makes a more explicit links with cospeciation, and is

more reliable to identify host-symbiont associations that contribute most to cophylogenetic

signal than regular global-fit methods. For greater usability, Random TaPas is implemented in

the public-domain statistical software R.

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REFERENCES

Balbuena J.A., Míguez-Lozano R., Blasco-Costa I. 2013. PACo: A novel Procrustes application

to cophylogenetic analysis. PLoS ONE 8:e61048.

Brown R.P., Yang Z. 2011. Rate variation and estimation of divergence times using strict and

relaxed clocks. BMC Evol. Biol. 11:271.

Chakerian J., Holmes S. 2010. Computational tools for evaluating phylogenetic and hierarchical

clustering trees. arXiv:1006.1015

Charleston M.A., Libeskind-Hadas R. 2014. Event-based cophylogenetic comparative analysis.

In: Garamszegi L.Z., editor. Modern phylogenetic comparative methods and their

application in evolutionary biology. Berlin, Heidelberg: Springer. p. 465–480.

Crawley M.J. 2013. The R book. Chichester: Wiley.

de Vienne D.M., Aguileta G., Ollier S. 2011. Euclidean nature of phylogenetic distance

matrices. Syst. Biol. 60:826–832.

de Vienne D.M., Giraud, D T., Shykoff J.A. 2007. When can host shifts produce congruent host

and parasite phylogenies? A simulation approach. J. Evol. Biol. 20:1428–1438.

de Vienne D.M., Refrégier G., López-Villavicencio M., Tellier A., Hood M.E., Giraud T. 2013.

Cospeciation vs host-shift speciation: Methods for testing, evidence from natural

associations and relation to coevolution. New Phytol. 198:347–385.

Drinkwater B., Qiao A., Charleston M.A. 2016. WiSPA: A new approach for dealing with

widespread parasitism. arXiv:1603.09415

Engelstädter J., Fortuna N.Z. 2018. The dynamics of preferential host switching: host phylogeny

as a key predictor of parasite prevalence and distribution. bioRxiv 209254.

Hagen O., Hartmann K., Steel M., Stadler T. 2015. Age-dependent speciation can explain the

shape of empirical phylogenies. Syst. Biol. 64:432–440.

Holmes S. 2005. Statistical approach to tests involving phylogenies. In: Gascuel O., editor.

Mathematics of Evolution and Phylogeny. Oxford: Oxford University Press. p. 91–120.

Hutchinson M.C., Cagua E.F., Balbuena J.A., Stouffer D.B., Poisot T. 2017a. paco:

implementing Procrustean Approach to Cophylogeny in R. Meth. Ecol. Evol. 8:932–940.

Hutchinson M.C., Cagua E.F., Stouffer D.B. 2017b. Cophylogenetic signal is detectable in

pollination interactions across ecological scales. Ecology. 98:2640–2652.

Keller-Schmidt S., Wieseke N., Klemm K., Middendorf M. 2011. Evaluation of host parasite

reconciliation methods using a new approach for cophylogeny generation. Technical

Report, Bioinformatics Leipzig. Available at http://www.bioinformatik.uni-

leipzig.de/Publications/PREPRINTS/11-013.pdf

Lagrue C., Joannes A., Poulin R., Blasco-Costa I. 2016. Genetic structure and host-parasite co-

divergence: evidence for trait-specific local adaptation. Biol. J. Linn. Soc. 118:344–358.

Legendre P., Desdevises Y., Bazin E. 2002. A statistical test for host-parasite coevolution. Syst.

Biol. 51:217–234.

Mendlová M., Desdevises Y., Civáňová K., Pariselle A., Šimková A. 2012. Monogeneans of

West African cichlid fish: evolution and cophylogenetic interactions. PLoS ONE 7:e37268.

Moran N.A. 2006. Symbiosis. Current Biol. 16:R866–R871.

Page R.D.M. 2003. Introduction. In: Page R.D.M., editor. Tangled trees: phylogeny,

cospeciation and coevolution. Chicago: Chicago University Press. p. 1–22.

Paradis E. 2014. Simulation of phylogenetic data. In: Garamszegi L.Z., editor. Modern

phylogenetic comparative methods and their application in evolutionary biology. Berlin,

Heidelberg: Springer Verlag. p. 335–350.

Pérez-Escobar O.A., Balbuena J.A., Gottschling M. 2016. Rumbling orchids: How to assess

divergent evolution between chloroplast endosymbionts and the nuclear host. Syst. Biol.

65:51–65.

Pérez-Escobar O.A., Chomicki G., Condamine F.L., Karremans A., Bogarin D., Matzke N.J.,

Silvestro D, Antonelli A. 2017. Recent origin and rapid speciation of Neotropical orchids in

the world's richest plant biodiversity hotspot. New Phytol. 215:891–905.

R Core Team. 2018. R: A language and environment for statistical computing. R Foundation for

Statistical Computing, Vienna, Austria.

Ramírez S.R., Eltz T., Fujiwara M.K., Gerlach G., Goldman-Huertas B., Tsutsui N.D., Pierce

N.E. 2011. Asynchronous diversification in a specialized plant-pollinator mutualism.

Science 333:1742–1746.

Revell L.J. 2012. phytools: An R package for phylogenetic comparative biology (and other

things). Meth. Ecol. Evol. 3:217–223.

Schardl C.L., Craven K.D., Speakman S., Stromberg A., Lindstrom A., Yoshida R. 2008. A

novel test for host-symbiont codivergence indicates ancient origin of fungal endophytes in

grasses. Syst. Biol. 57:483–498.

Therneau T.M., Atkinson E.J. 2018. An introduction to recursive partitioning using the RPART

routines. R package. https://cran.r-project.org/web/packages/rpart/vignettes/longintro.pdf,

accessed November 26, 2018.

Venables W.N., Ripley B.D. 2002. Modern applied statistics with S. New York: Springer.

Weber M.G., Wagner C.E., Best R.J., Harmon L.J., Matthews B. 2017. Evolution in a

community context: On integrating ecological interactions and macroevolution. Trends

Ecol. Evol. 32:291–304.

Zook D. 2015. Symbiosis – evolution's co-author. In: Gontier N., editor. Reticulate evolution.

Cham, Switzerland: Springer. p. 41–80.

Table 1. Mean and range of variance to mean ratios of frequency distributions of host-symbiont (h-s) associations produced by Random TaPas applied in conjunction to two global-fit (GF) methods, Geodesic Distances (GD) and Procrustes Approach to Cophylogeny (PACo) to two sets of 100 simulated tanglegrams each: Set50 and Set100 involving $\approx$ 50 and 100 h-s associations, respectively. Random TaPas was evaluated with both additive and ultrametric trees over 10^4 runs with a fixed number of unique h-s associations (n) $\approx$ 10%, 20% and 40% of the total number of h-s associations and percentiles (p) = 1% and 5%. (See Fig. 1 for definitions of n and p).

$n\approx10\%$	Set50 - Additive trees		Set50 - Ultrametric trees		Set100 - Additive trees		Set100 - Ultrametric trees	
GF method	Mean	Range	Mean	Range	Mean	Range	Mean	Range
GD, p=1%	16.5	7.6 – 30.4	13.1	0.1 – 31.1	10.0	3.4 – 16.5	9.0	0.6 – 17.6
GD, p=5%	10.8	5.0 – 22.3	9.3	0.1 – 19.5	7.1	1.7 – 12.0	7.0	0.6 – 13.9
PACo, p=1%	13.2	5.6 – 25.3	12.8	0.4 – 28.3	9.9	3.4 – 17.3	9.4	1.0 – 18.5
PACo, p=5%	9.4	3.9 – 20.3	8.9	0.4 – 16.6	7.1	2.3 – 13.1	7.1	0.6 – 13.9
$n\approx20\%$								
GD, p=1%	16.8	8.1 – 31.4	15.4	0.2 – 29.4	11.9	3.0 – 21.0	11.6	1.2 – 22.4
GD, p=5%	12.9	5.4 – 27.5	11.9	0.2 – 26.3	9.6	2.4 – 19.6	9.6	1.2 – 19.1
PACo, p=1%	16.7	8.4 – 31.1	15.6	0.6 – 26.1	12.3	1.9 – 22.4	12.2	1.4 – 22.4
PACo, p=5%	12.7	5.3 – 25.9	12.1	0.4 – 23.4	9.9	1.3 – 20.0	10.1	1.2 – 19.9
$n\approx40\%$								
GD, p=1%	18.9	8.1 – 28.7	18.0	0.4 – 27.1	15.6	5.9 – 25.6	15.8	2.4 – 26.4
GD, p=5%	16.2	4.8 – 24.5	15.9	0.4 – 25.3	13.9	4.1 – 25.3	14.3	2.4 – 25.0
PACo, p=1%	19.1	8.1 – 28.0	18.3	1.2 – 27.9	16.3	5.1 – 26.6	16.6	2.7 – 26.3
PACo, p=5%	16.4	5.3 – 25.2	16.1	0.6 – 24.6	14.6	4.3 – 25.4	14.9	2.5 – 25.2

Figure 1. The Random TaPas algorithm. Given a triple (H, S, **A**), where H and S represent the phylogenies of hosts and symbionts, and **A** is a binary matrix that codes the associations between terminals in H and S: **1.** Set a number n less than the total number of host-symbiont associations. **2.** For i from 1 to N times (where N is sufficiently large, typically $\geq 10^4$) do **2.1.** Randomly choose n unique associations in **A**, so that each terminal in H is associated to one, and only one, terminal in S, and vice versa. (This is a prerequisite for a perfect host-symbiont cospeciation scenario); **2.2.** Produce a partial tanglegram that includes only the n associations chosen at step 2.1 by trimming **A** and pruning H and S; **2.3.** Run a global-fit test with the partial triple and **2.4.** Save the resulting statistic z_i and the set of n host-symbiont associations selected at 2.1. **3.** Render the frequency distribution of the z_i's and set a small percentile p where the highest cophylogenetic congruence is expected. **4.** Determine how many times each host-symbiont associations occurs in p, and return their frequency distribution.

Figure 2. Regression trees relating the variance to mean ratio (VMR) of the frequency distribution of host-symbiont associations produced by Random TaPas with the number of evolutionary events in 100 simulated tanglegrams of ≈50 host-symbiont associations each, applying geodesic distances as global-fit method to phylograms. Expressions on nodes indicate the split criterion that shows the threshold value of the evolutionary event that was used to create the split. Branches to the left include cases that fulfill the criterion. Numbers at tips represent the average VMR of the group. Parameter combinations were as follows: (a) $n = 5$, $p = 1\%$; (b) $n = 5$, $p = 5\%$; (c) $n = 10$, $p = 1\%$; (d) $n = 10$, $p = 5\%$; (e) $n = 20$, $p = 1\%$; (f) $n = 20$, $p = 5\%$. Event abbreviations: csp = cospeciation, sor = sorting, dup =duplication, hsw = complete host-switching, col = colonization of new host without speciation.

Figure 3. Relative importance of evolutionary events to explain the variance-to-mean ratio of the frequency distribution of host-symbiont associations produced by Random TaPas with regression trees in two sets of 100 simulated tanglegrams each involving approximately 50 (a-d) and 100 (e-h) host-symbiont associations, respectively. Regression tree models were run with both additive (a, b, e, f) and ultrametric trees (c, d, g, h) applying Random TaPas with geodesic distances (a, c, e, g) and PACo (b, d, f, h) with a varying number of host-symbiont associations (*n*) and two percentile values (*p*). Event abbreviations: csp = cospeciation, sor = sorting, dup =duplication, hsw = complete host-switching, col = colonization of new host without speciation.

Figure 4. Correlation coefficients of the variance-to-mean ratio of the frequency distribution of host-symbiont associations produced by Random TaPas with the number of cospeciation events in two sets of 100 simulated tanglegrams each involving approximately 50 (a-d) and 100 (e-h) host-symbiont associations, respectively, and both additive (a, b, e, f) and ultrametric (c, d, g, h) trees applying Random TaPas with geodesic distances (a, c, e, g) and PACo (b, d, f, h) with a varying number of host-symbiont associations (*n*) and two percentile values (*p*). Event abbreviations: csp = cospeciation, sor = sorting, dup =duplication, hsw = complete host-switching, col = colonization of new host without speciation.

Figure 5. Results of the pseudocospeciation experiment with one simulated tanglegram of ≈50 host-symbiont associations relating two additive trees. Random TaPas was applied with geodesic distances, *p* = 5% and *n* = 5 (a), *n* = 10 (b) and *n* = 20 (c) to the original (left) and modified (right) tanglegrams. In the latter, the branch lengths of one clade (arrow) were reduced to one half, whereas its basal branch was lengthened to keep the original height of the clade. The frequency of occurrence of each host-symbiont association in the percentile *p* retrieved by Random TaPas (see Fig. 1) is coded in a color scale, where red and blue denote low and high values, respectively. The points at terminals are also coded on the same scale and represent the average frequency of host-symbiont association in which the terminal is involved.

Figure 6. Results of the pseudocospeciation experiment with one simulated tanglegram of ≈100 host-symbiont associations relating two ultrametric trees. Random TaPas was applied with geodesic distances, $p = 5\%$ and $n = 5$ (a), $n = 10$ (b) and $n = 20$ (c) to the original (left) and modified (right) tanglegrams. In the latter, the branch lengths of one clade (arrow) were reduced to one half, whereas its basal branch was lengthened to keep the original height of the clade. The frequency of occurrence of each host-symbiont association in the percentile p retrieved by Random TaPas (see Fig. 1) is coded in a color scale, where red and blue denote low and high values, respectively. The points at terminals are also coded on the same scale and represent the average frequency of host-symbiont association in which the terminal is involved.

Figure 7. Results of Random TaPas applied to data of Neotropical orchids and their euglossine bee pollinators. The frequency distributions of pollinator-orchid associations were obtained with $N = 10^4$, $n = 29$, and $p = 5\%$ with GD (a) and PACo (b). Vertical lines represent 95% confidence intervals of the frequencies computed with 1,000 randomly chosen pairs of posterior probability trees used to build the consensus trees of bees and orchids. Horizontal lines represent the expected mean if all associations were contributing equally to cophylogenetic signal. (c) Variance to mean ratio (VMR) of the respective frequency distributions (asterisks) and boxplots of VMRs produced with the pairs of posterior probability trees generated with GD and PACo.

Figure 8. Tanglegram representing the association between Neotropical orchids and their euglossine bee pollinators. The frequency corresponding to each pollinator-orchid association shown in Fig. 7 is mapped using a color scale ranging from dark blue (highest) to dark red (lowest). The average frequency of occurrence of each terminal and fast maximum likelihood estimators of ancestral states of each node are also mapped according to the same scale.

Figure 9. Results of Random TaPas applied to study the association between haplotypes of the trematode *Coitocaecum parvum* with those of its amphipod host, *Paracalliope fluviatilis*. The frequency distributions of host-symbiont associations were obtained with GD (a) and PACo (b), $N = 10^4$, $n = 8$ and $p = 5\%$. Vertical lines represent 95% confidence intervals of the frequencies computed with 1,000 randomly chosen pairs posterior probability trees used to build the consensus trees of trematode and amphipod haplotypes. Horizontal lines represent the expected mean if all associations were contributing equally to cophylogenetic signal. (c) Variance to mean ratio (VMR) of the respective frequency distributions (asterisks) and boxplots of VMRs produced with the pairs of posterior probability trees generated with GD and PACo.

Figure 10. Tanglegram representing the association between haplotypes of the trematode *Coitocaecum parvum* with those of its amphipod host, *Paracalliope fluviatilis*. The frequency corresponding to each trematode-amphipod association shown in Fig. 7 is mapped using a color scale ranging from dark blue (highest) to dark red (lowest). The average frequency of occurrence of each terminal and fast maximum likelihood estimators of ancestral states of each node are also mapped according to the same scale.