

1 The chaperone-client network subordinates cell-cycle entry to growth and stress

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13

14 Abstract

15 The precise coordination of growth and proliferation has a universal prevalence in cell homeostasis. As a
16 prominent property, cell size is modulated by the coordination between these processes in bacterial,
17 yeast and mammalian cells, but the underlying molecular mechanisms are largely unknown. Here we
18 show that multifunctional chaperone systems play a concerted and limiting role in cell-cycle entry,
19 specifically driving nuclear accumulation of the G1 Cdk-cyclin complex. Based on these findings, we
20 establish and test a molecular competition model that recapitulates cell-cycle-entry dependence on
21 growth rate. As key predictions at a single-cell level, we show that availability of the Ydj1 chaperone and
22 nuclear accumulation of the G1 cyclin Cln3 are inversely dependent on growth rate and readily respond
23 to changes in protein synthesis and stress conditions that alter protein folding requirements. Thus,
24 chaperone workload would subordinate Start to the biosynthetic machinery and dynamically adjust
25 proliferation to the growth potential of the cell.

26

27 **Keywords:** cell cycle; cell size; chaperone; cyclin; growth rate; stress, molecular competition; Start

28

29 INTRODUCTION

30 Under unperturbed conditions of growth cells maintain their size within constant limits, and different
31 pathways have concerted roles in processes leading to growth and proliferation (Cook & Tyers, 2007;
32 Marshall *et al*, 2012; Turner *et al*, 2012). Here we will use the term growth to refer to cell mass or volume
33 increase, while the term proliferation will be restricted to the increase in cell number. Cell growth is
34 dictated by many environmental factors in budding yeast, and the rate at which cells grow has profound
35 effects on their size. High rates of macromolecular synthesis promote growth and increase cell size.
36 Conversely, conditions that reduce cell growth limit macromolecular synthesis and reduce cell size. This
37 behavior is nearly universal and it has been well characterized in bacteria, yeast, diatoms, and
38 mammalian cells of different origins (Aldea *et al*, 2017). A current view sustains that cell cycle and cell
39 growth machineries should be deeply interconnected to ensure cell homeostasis and adaptation, but the
40 causal molecular mechanism is still poorly understood (Lloyd, 2013).

41 In budding yeast, cyclin Cln3 is the most upstream activator of Start (Tyers *et al*, 1993). Cln3 forms a
42 complex with Cdc28, the cell cycle Cdk in budding yeast, and activates the G1/S regulon with the
43 participation of two other G1 cyclins, Cln1 and Cln2, which contribute to phosphorylate the Whi5
44 inhibitor thus creating a positive feedback loop that provides Start with robustness and irreversibility
45 (Bertoli *et al*, 2013). The Start network in mammals offers important differences, particularly in the
46 structure and number of transcription factors, but the core of the module is strikingly similar, where
47 Cdk4,6-cyclin D complexes phosphorylate RB and activate E2F-DP transcription factors in a positive
48 feedback loop involving Cdk2-cyclin E (Bertoli *et al*, 2013).

49 As they are intrinsically unstable, G1 cyclins are thought to transmit growth information for adapting cell
50 size to environmental conditions. The Cln3 cyclin is a dose-dependent activator of Start (Sudbery *et al*,
51 1980; Nash *et al*, 1988; Cross & Blake, 1993) that accumulates in the nucleus due to a constitutive C-
52 terminal NLS (Edgington & Futcher, 2001; Miller & Cross, 2001) and the participation of Hsp70-Hsp40
53 chaperones, namely Ssa1,2 and Ydj1 (Vergés *et al*, 2007). In addition, Ssa1 and Ydj1 also regulate Cln3
54 stability (Yaglom *et al*, 1996; Truman *et al*, 2012), and play an essential role in setting the critical size as a
55 function of growth rate (Ferrezuelo *et al*, 2012). In mammalian cells cyclin D1 depends on Hsp70
56 chaperone activity to form trimeric complexes with Cdk4 and NLS-containing KIP proteins (p21, p27, p57)
57 that drive their nuclear accumulation (Diehl *et al*, 2003).

58 Molecular chaperones assist nascent proteins in acquiring their native conformation and prevent their
59 aggregation by constraining non-productive interactions. These specialized folding factors also guide

60 protein transport across membranes and modulate protein complex formation by controlling
61 conformational changes (Kampinga & Craig, 2010). Chaperones are involved in key growth-related
62 cellular processes as protein folding and membrane translocation during secretion (Kim *et al*, 2013), and
63 many chaperone-client proteins have crucial roles in the control of growth, cell division, environmental
64 adaptation and development (Gong *et al*, 2009; Taipale *et al*, 2012, 2014). Thus, since chaperones
65 required for Cdk-cyclin activation are also involved in the vast majority of processes underlying cell
66 growth, we hypothesized that competition for shared multifunctional chaperones could subordinate
67 entry into the cell cycle to the biosynthetic machinery of the cell.

68 Here we show that chaperones play a concerted and limiting role in cell-cycle entry, specifically driving
69 nuclear accumulation of the G1 Cdk-cyclin complex. Ydj1 availability is inversely dependent on growth
70 rate and, based on our findings, we have established a molecular competition model that recapitulates
71 cell-cycle entry dependence on growth rate. As key predictions of the model, we show that nuclear
72 accumulation of the G1 cyclin Cln3 is negatively affected by growth rate in a chaperone-dependent
73 manner, and rapidly responds to conditions that perturb or boost chaperone activity. Thus chaperone
74 availability would act as a G1-Cdk modulator transmitting both intrinsic and extrinsic information to
75 subordinate Start and the critical size to the growth potential of the cell.

76

77 **RESULTS**

78 **Nuclear accumulation of the G1 Cdk depends on chaperone activity**

79 Cln3 contains a bipartite nuclear localization signal at its C terminus that is essential for timely entry into
80 the cell cycle (Edgington & Futcher, 2001; Miller & Cross, 2001), and we had found that the Ydj1
81 chaperone is important for nuclear accumulation of Cln3 (Vergés *et al*, 2007) and for setting the critical
82 size as a function of growth rate (Ferrezuelo *et al*, 2012). Thus, we decided to characterize the role of
83 chaperones as regulators of the G1 Cdk during G1 progression at a single-cell level in time-lapse
84 experiments. Cln3 is too short-lived to be detected as a fluorescent-protein fusion in single cells unless
85 stabilized mutants are used (Liu *et al*, 2015; Schmoller *et al*, 2015). As previously described, mCitrine-
86 Cln3-11A displayed a distinct nuclear signal in most asynchronously growing cells, arguing against the ER
87 retention mechanism that we had proposed previously (Vergés *et al*, 2007). However, this protein is
88 much more stable compared to wild-type Cln3, and transient retention at the ER would likely be obscured
89 by accumulation of abnormally stable mCitrine-Cln3-11A in the nucleus. Thus, we decided to test whether
90 nuclear accumulation of this stabilized protein was still dependent on Ydj1 by carefully measuring nuclear

91 and cytoplasmic fluorescence levels (Fig EV1). While overall levels as determined by immunoblotting
92 were not altered, nuclear mCitrine-Cln3-11A levels strongly decreased in Ydj1-deficient cells (Fig 1A-C),
93 which confirmed previous observations obtained with 3HA-tagged wild-type Cln3 by
94 immunofluorescence (Vergés *et al*, 2007). Moreover, while nuclear levels of Cdc28-GFP in late G1 cells
95 were also negatively affected by deletion of *YDJ1*, overexpression of both Ydj1 and Ssa1 significantly
96 increased the nuclear to cytoplasmic ratio of Cdc28-GFP both in mid- and late-G1 cells (Fig 1D). Likely due
97 to the fact that Cdc28 is present at much higher levels than Cln3 (Tyers *et al*, 1993; Cross *et al*, 2002)
98 differences in the steady-state nuclear levels of Cdc28 when comparing wild-type and Ydj1-deficient or
99 overexpressing cells were only modest (Fig 1D). On the other hand, we cannot discard the effects of
100 Cln1,2 cyclins synthesized at Start by the transcriptional feedback loop. Thus, we decided to analyze
101 directly the import kinetics of Cdc28-GFP in G1 cells by nuclear FLIP (Figs 1E,F and EV2). We found that,
102 while being extremely dependent on Cln3 (Fig 1G), the nuclear import rate of Cdc28-GFP decreased in
103 Ydj1-deficient cells and was clearly impaired when chaperone function was compromised by azetidine 2-
104 carboxylic acid (AZC), a proline analog that interferes with proper protein folding (Trotter *et al*, 2001). By
105 contrast, a 2NLS-GFP control did not show significant differences in nuclear localization or import kinetics
106 in cells lacking Ydj1, Cln3 or in the presence of AZC (Fig 1C and H). These data are consistent with a
107 chaperone-dependent mechanism that drives nuclear import of the Cdc28-Cln3 complex in G1 for the
108 timely execution of Start.

109

110 **Multifunctional chaperones have a limiting role in setting cell size at budding**

111 If chaperones have a role in coordinating cell growth and Start machineries, chaperone availability ought
112 to be limiting for cell-cycle entry. Thus, we decided to test this proposition by increasing the gene dosage
113 of different chaperone sets in low-copy centromeric vectors. In addition to the Hsp70 system (Ssa1 and
114 Ydj1), we analyzed the effects of key components of the Hsp90 system (Hsc82 and Cdc37), which is
115 important for holding the Cdk in a productive conformation for binding cyclins (Vaughan *et al*, 2006), and
116 the segregase Cdc48 complex (Cdc48, Ufd1, and Npl4), which prevents degradation of ubiquitinated Cln3,
117 and concurrently stimulates its ER release and nuclear accumulation to trigger Start (Parisi *et al*, 2018).
118 Gene duplication in centromeric vectors increased chaperone gene expression by 1.5- to 2-fold in a
119 specific manner (Fig EV3A). Notably, although expression levels increased only modestly, additional
120 copies of chaperone genes caused an additive reduction of the budding volume in asynchronous cultures
121 (Fig 2A) and newborn daughter cells (Fig 2B). This effect was barely observed in large cells deficient for
122 Cln3, and was totally abolished in cells lacking Cln3 as well as Whi5 and Stb1, two key inhibitors of the

123 Start network (Fig 2B). This triple mutant displays unaltered average budding volume compared to wild
124 type (Wang *et al*, 2009), but has lost most of the dependency on growth rate (Ferrezuelo *et al*, 2012). In
125 contrast, the effect was still clear in cells lacking Whi7, an inhibitor of Start that acts at an upstream step
126 (Yahya *et al*, 2014). Finally, we observed a comparable reduction of the budding volume when genes of
127 the three chaperone systems were duplicated together in an artificial chromosome (Fig 2C). Doubling
128 times of cells with vectors expressing the different chaperone sets were not significantly different from
129 wild-type cells. Also, we had found no differences in the growth rate during G1 when comparing wild-
130 type and Ydj1/Ssa1 overexpressing cells (Ferrezuelo *et al*, 2012), which rules out indirect effects on cell
131 size by growth rate changes. In addition, protein levels and phosphorylation status of Cln3 were not
132 affected by chaperone gene dosage (Fig EV3B), pointing to a limiting role of these chaperone sets in Cdk-
133 cyclin complex activity and/or localization.

134

135 **Molecular competition for chaperones predicts cell size dependency on growth rate**

136 As they are associated with client proteins mostly in a transient manner, the level of free chaperones
137 might be inversely dependent on protein synthesis and trafficking rates, thus constituting a simple
138 mechanism to report growth kinetics to the Start network and, hence, modulate cell size as a function of
139 growth rate. To test this notion, we developed a mathematical model (Fig 3A) wherein protein synthesis
140 and G1 Cdk-cyclin complex assembly compete for limiting amounts of Ydj1, the best characterized
141 chaperone in terms of regulating Cln3. Ydj1 plays an activating role by releasing Cln3 from the ER during
142 G1 (Vergés *et al*, 2007), but is also important for efficient degradation of Cln3 by Cdc28-dependent and
143 autoactivated phosphorylation (Yaglom *et al*, 1996, 1995). Taken together, these data point to the notion
144 that Ssa1/Ydj1 chaperones contribute to both proper Cln3 folding (i.e. binding Cdc28 in a productive
145 conformation) and its release from the ER where the segregase Cdc48 plays also a key role (Parisi *et al*,
146 2018). Since these regulatory steps are likely related at the molecular level, we opted for treating them as
147 a single event in the competition model. On another point, although the specific affinity of Ydj1 for the
148 various Cln3 domains was similar to other proteins (Fig EV4), the number of client proteins being
149 synthesized at any given time is in overwhelming excess relative to those of Ydj1 (Gong *et al*, 2009) and
150 especially of Cln3, which is present at very low levels (Tyers *et al*, 1993; Cross *et al*, 2002).

151 In our model, the level of available, unbound Ydj1 (Ydj1_A) is a key variable and, since client-engaged
152 chaperones offer a reduced mobility (Lajoie *et al*, 2012; Saarikangas *et al*, 2017), we decided to use FLIP
153 and FCS to obtain a mobility index of fully functional Ydj1 and Ssa1 fusions to GFP as reporter of their

154 availability in single cells. First we tested the validity of this methodological approach by compromising
155 chaperone function with AZC, which induces misfolded protein accumulation with chaperones into
156 disperse cellular aggregates (Escusa-Toret *et al*, 2013), thus reducing levels of soluble available
157 chaperones. While GFP mobility remained unaffected, both Ssa1 and Ydj1 fusions to GFP decreased their
158 mobility upon AZC treatment (Fig EV5).

159 Individual genetically-identical cells display a large variability in multifactorial processes such as gene
160 expression and growth (Blake *et al*, 2003; Ferrezuelo *et al*, 2012) and we reasoned that, if the molecular
161 competition model is correct, endogenous variability in growth rate should have an effect on chaperone
162 availability at the single-cell level. We found that Ydj1-GFP diffusion was correlated negatively with
163 growth rate in single G1 cells by both FLIP (Fig 3C and D) and FCS (Fig 3E and F) analysis, and at a
164 population level in media sustaining different growth rates (Fig EV6A). The chaperone-competition model
165 perfectly fitted the dependence of Ydj1 availability on growth rate (Fig 3F) and, more important, it also
166 simulated very closely the increase of the budding volume with growth rate (Ferrezuelo *et al*, 2012) (Fig
167 3G). As expected from a competition framework, the fitted parameter sets produced negative
168 correlations between available Ydj1 and unfolded target proteins (Fig EV6B), and a positive correlation
169 between the level of Ydj1 in complexes with either Cln3 or all other proteins (Fig EV6C). Interestingly, the
170 competition model produced acceptable fits with parameters spanning several orders of magnitude (Fig
171 3B), which underlines the robustness of the chaperone competition design in predicting growth-rate
172 dependent chaperone availability and cell size, letting parameters to be adapted for subjugating Start to
173 cellular processes other than growth. In summary, our experimental results and modeling simulations
174 support the notion that growth rate modulates levels of available chaperones.

175

176 **Growth rate and protein synthesis modulate accumulation of Cln3 in the nucleus**

177 The molecular competition model predicted that increasing growth rate would decrease available levels
178 of free chaperones (Ydj1_A) and, hence, decrease the steady-state level of folded free Cln3 (Cln3_F) (Fig
179 EV6D and E). More precisely, the fraction of Ydj1 bound to client proteins (YP+YC) increases at higher
180 growth rates. As a consequence, the fraction of available free Ydj1 (Ydj1_A) drops and the rate at which
181 proteins can be folded is reduced, which in turn increases the fraction of unfolded proteins (Prot_U and
182 Cln3_U). Due to its intrinsic instability, folded Cln3 (Cln3_F) levels are extremely more sensitive to the effects
183 of Ydj1 compared to all other proteins. Indeed, whereas the total concentration of mCitrine-Cln3-11A in
184 G1 remained unaltered on average at different growth rates (Fig EV6G), nuclear levels of mCitrine-Cln3-

185 11A displayed a significant negative correlation ($p=2.10^{-4}$) with growth rate very similar to that predicted
186 by the model (Fig 3H). Notably, this negative correlation was totally lost in Ydj1-deficient cells (Fig 3H). In
187 summary, higher growth rates reduce the nuclear levels of Cln3 at a given volume in a chaperone-
188 dependent manner.

189 Next, with the purpose of simulating lower growth rates, we used cycloheximide (CHX) to decrease
190 protein synthesis and relieve chaperones temporarily from the load of nascent polypeptides (Fig 4A and
191 B). As expected, CHX inhibited incorporation of puromycin in cell-free extracts (Fig 4C) but it increased
192 the rate at which heat-treated luciferase was renatured and became active, indicating that both protein
193 refolding and synthesis compete for chaperones in cell extracts. Next, we tested the effects of CHX at 0.2
194 $\mu\text{g/ml}$, a sublethal concentration that does not activate the environmental stress response (Jacquet,
195 2003; Trotter *et al*, 2002), and found that the protein synthesis rate displayed a 5.9-fold decrease in live
196 cells (Fig EV7). In agreement with our model prediction (Fig 4B) this sublethal dose of CHX increased the
197 average diffusion coefficient of Ydj1-GFP as measured by FCS (Fig 4D) and FLIP (Fig 4E). Temporary
198 perturbations of chaperone availability should in turn have an effect in the nuclear accumulation of Cln3
199 (Fig 4B). In order to quantify endogenously expressed Cln3-3HA in immunofluorescence images we used a
200 semiautomated method that analyzes both cytoplasmic and nuclear compartments in fixed yeast cells
201 (Yahya *et al*, 2014). Notably, we found that relative nuclear levels of Cln3-3HA rapidly increased after
202 addition of CHX (Fig 4F and G), decreasing at later times as predicted by the model (Fig 4B), and this
203 transient increase fully depended on Ydj1. However, CHX has been shown to increase cell size at Start
204 (Jorgensen *et al*, 2004). This apparent discrepancy could originate from the different short- and long-term
205 effects of CHX, i.e. increasing Ydj1 mobility and nuclear localization of Cln3 at very short times (less than
206 one minute), but eventually decreasing G1 cyclin levels, which is what would finally result in a larger cell
207 size. In the overall, these data support the notion that chaperone availability transmits growth and
208 protein synthesis rate information to modulate the rate at which the G1 Cdk-cyclin complex is properly
209 formed and accumulates in the nucleus.

210

211 **Stress conditions that decrease chaperone availability prevent accumulation of Cln3 in the nucleus**

212 Yeast cells respond to stress conditions as diverse as high temperature, high osmolarity or abnormal
213 levels of unfolded proteins in the ER, by highly conserved transcriptional programs that increase
214 chaperone expression to protect damaged proteins from aggregation, unfold aggregated proteins, and
215 refold damaged proteins or target them for efficient degradation (De Nadal *et al*, 2011). Thus, stresses

216 are assumed to cause a temporary deficit in chaperone availability. Hsf1, the key transcriptional activator
217 of the heat shock response, is inhibited by chaperones of the Hsp70 and Hsp90 systems, and it has been
218 proposed that the accumulation of unfolded or damaged proteins would readily titrate the chaperone
219 machinery from Hsf1, allowing derepression of the transcription factor (Verghese *et al*, 2012). Supporting
220 this notion, Ydj1-assisted Ssa1 chaperone is targeted to and accumulates in protein aggregates (Mogk *et al*,
221 2018) after heat stress. A similar titration mechanism has been proposed for Kar2, the Hsp70
222 chaperone acting at the ER lumen (Gardner *et al*, 2013). On the other hand, both heat and salt stress
223 have been shown to inhibit the G1/S regulon (Rowley *et al*, 1993; Bellí *et al*, 2001; Trotter *et al*, 2001).
224 Thus, we reasoned that chaperone titration by stress could effectively reduce chaperone availability and
225 restrain nuclear accumulation of Cln3 in a temporary manner (Fig 5A). We first interrogated our model
226 and simulated a stress event by transferring different fractions of the folded protein ($Prot_F$) to the
227 unfolded population ($Prot_U$). As shown in Fig 5B, the model predicted a sharp and transient reduction in
228 available Ydj1 ($Ydj1_A$) and free Cln3 ($Cln3_F$). Notably, we found that Ydj1-GFP diffusion decreased very
229 rapidly under both heat and salt stress (Fig 5C and D), and recovered at later times to attain similar
230 steady-states to the pre-stress situation. Moreover, nuclear levels of Cln3-3HA displayed a similar and
231 transient decrease after heat and salt stress (Fig 5E and F), which did not affect overall Cln3-3HA levels as
232 measured by immunoblotting. Due to its extremely short half-life, Cln3 is thought to respond very rapidly
233 to new conditions. However, nuclear levels of Cln3 only recovered pre-stress values after 20-30 min (Fig
234 5G and H), within the same time range needed by the Ydj1 chaperone to recover pre-stress mobility (Fig
235 5C and D), thus reinforcing a functional link between chaperone availability and nuclear accumulation of
236 Cln3 under stress conditions. To test this further, we used our model to predict the behavior of Cln3
237 during stress adaptation assuming that overall protein folding and nuclear accumulation of Cln3 use
238 chaperones in independent or competing manners. As seen in Fig 5G and H, only the competition
239 scenario was able to recapitulate the Cln3 immunofluorescence data from both heat and salt stresses.

240 ER stress causes protein aggregation in the cytoplasm (Hamdan *et al*, 2017), and increases Ssa4
241 expression to levels very similar to Kar2 (Travers *et al*, 2000), suggesting that ER stress also affects Ydj1
242 availability. Moreover, ER stress also causes a G1 delay (Vai *et al*, 1987). We found that, similar to heat
243 and salt stress, addition of tunicamycin to induce irreversible ER stress in yeast cells decreased Ydj1
244 mobility and nuclear levels of Cln3-3HA (Fig EV8). Overall, these data indicate that stress conditions due
245 to very different environmental cues cause coincident decreases in Ydj1 mobility and Cln3 nuclear
246 accumulation, reinforcing the notion that chaperone availability is a key parameter that controls G1 cyclin
247 fate and adapts cell-cycle entry to growth and stress.

248 **DISCUSSION**

249 Our data show that multifunctional chaperone systems play a limiting role in driving nuclear
250 accumulation of the Cdc28-Cln3 complex during G1 progression. We also show that increased growth
251 rates, by allocating higher levels of chaperones to protein synthesis and trafficking, reduce free
252 chaperone pools and restrain nuclear accumulation of Cln3 at a given volume in G1. If Cln3 has to reach a
253 threshold concentration to execute Start (Wang *et al*, 2009; Schmoller *et al*, 2015; Liu *et al*, 2015), fast
254 growing cells would delay G1 progression to grow larger and attain the same pool of free chaperones and
255 nuclear Cln3 (Fig 6). As a consequence, the critical size would be set as a function of growth rate. Due to
256 the close molecular connection proposed here between protein synthesis and folding/release of the G1
257 cyclin, our model would allow cells to quickly adjust their size to many different intrinsic and extrinsic
258 signals as long as they modulate protein synthesis, thus acting as a common mediator of specific growth
259 signaling pathways and the Start network. This view would also explain, at least in part, why deleterious
260 mutations in nutrient sensing pathways that control ribosome biogenesis and cell growth cause a small
261 cell size phenotype (Jorgensen *et al*, 2004; Baroni *et al*, 1994; Tokiwa *et al*, 1994). A recent
262 comprehensive analysis of cell size mutants concluded that, in the majority of *whi* mutants, the small cell
263 size was due to indirect effects mostly caused by a decrease in growth rate (Soifer & Barkai, 2014).

264 The chaperone competition mechanism would only operate above a minimal translation rate to sustain
265 G1-cyclin synthesis (Schneider *et al*, 2004), and would collaborate with pathways regulating G1-cyclin
266 expression by specific nutrients (Baroni *et al*, 1994; Newcomb *et al*, 2002; Gallego *et al*, 1997; Tokiwa *et al*,
267 1994). In this respect, Cln3 synthesis is strongly downregulated at low growth rates by a uORF-
268 dependent mechanism (Polymenis & Schmidt, 1997), shifting cells from poor to rich carbon sources
269 increases Cln3 abundance but yet delays Start in terms of cell size (Johnston *et al*, 1979; Hall *et al*, 1998;
270 Tokiwa *et al*, 1994), phosphate deprivation increases degradation of Cln3 by Pho85-dependent
271 phosphorylation (Menoyo *et al*, 2013), and Rim15 counteracts Whi5 dephosphorylation in G1 to facilitate
272 cell-cycle entry in poor carbon sources (Talarek *et al*, 2017). Moreover, nutrient modulation of cell size is
273 largely independent of the core components of the Start network (Jorgensen *et al*, 2004). From this point
274 of view, modulation of the critical cell size threshold by nutrients and growth rate has remained a
275 mysterious issue during decades (Johnston *et al*, 1979; Tyson *et al*, 1979; Fantes & Nurse, 1977). Our
276 findings provide a general mechanism to modulate nuclear accumulation of Cln3 and cell-cycle entry as a
277 function of growth rate.

278 Cells deficient for Cln3 still maintain a growth-rate dependent size at Start, but with a much larger
279 variability compared to wild type cells (Yahya *et al*, 2014). Cln1 and Cln2 become essential in the absence
280 of Cln3, and cells lacking these two other G1 cyclins also display a wider range of sizes at Start as a
281 function of growth rate. Moreover, the *CLN2* mRNA has also been found enriched in Whi3 pulldowns
282 (Colomina *et al*, 2008; Holmes *et al*, 2013), suggesting that the chaperone competition mechanism would
283 also apply to Cln2, particularly in the absence of Cln3.

284 Whi5 levels have been found to decrease in rich carbon sources (Liu *et al*, 2015). If these modulation was
285 responsible for cell size adaptation, we should expect cells displaying the opposite behavior, i.e. cells
286 should be smaller in rich carbon sources. However, this observation could be interpreted as an effect,
287 rather than a causative determinant of cell size adaptation. Whi5 is synthesized in a size-independent
288 manner (Schmoller *et al*, 2015) and, also likely, in a growth-rate independent manner. As cells growing in
289 rich carbon sources are larger, this effect would produce a decrease in Whi5 concentration. Thus, while
290 Whi5 would act as a growth rate independent sizer, chaperone availability would dynamically transmit
291 growth rate information to modulate G1 Cdk activation and adjust cell size as a function of the individual
292 growth potential (Fig 6).

293 Available models of the cell cycle of budding yeast have centered their attention to different aspects of
294 the molecular machineries that execute and regulate key transitions, but the implications of growth rate
295 on cell size have been addressed only in a few occasions. Thus, a model based on intrinsic size
296 homeostasis predicts growth-rate dependence if nutrient uptake is subject to geometric constraints
297 (Spiesser *et al*, 2012, 2015). In this regard, surface to volume ratios have been recently highlighted in
298 bacteria as key parameters for setting cell size as a function of growth rate (Harris & Theriot, 2016).
299 Interestingly, an important fraction of Ydj1 is involved in post-translational protein translocation at the ER
300 (Caplan *et al*, 1992; McClellan *et al*, 1998) to fuel cell surface growth which, as a consequence, would set
301 Ydj1 demands as a function of surface-to-volume ratios. On the other hand, in a recent model of the G1/S
302 transition, it has been proposed that growth-rate dependence would be exerted, directly or indirectly, by
303 ribosome-biogenesis effects on the Cln3/Whi5 interplay (Palumbo *et al*, 2016). In agreement with this
304 idea, here we propose that chaperones act as key mediators in this pathway by modulating the ability of
305 Cln3 to accumulate in the nucleus and, hence, attain a critical Cln3/Whi5 ratio.

306 Nutrient modulation of cell size also takes place during bud growth and, as we had observed in G1, cell
307 size at birth displays a strong correlation with growth rate at a single cell level during the preceding S-G2-
308 M phases (Leitao & Kellogg, 2017). Thus, mechanisms sensing growth rate independently of the specific
309 nutritional conditions also operate during bud volume growth.

310 Finally, we show that different stress agents cause concurrent decreases in Ydj1 mobility and nuclear Cln3
311 levels, supporting the idea that chaperone availability is a key factor controlling localization of the most
312 upstream G1 cyclin and, hence, modulating G1 length under stress conditions. Heat shock transiently
313 inhibits G1/S gene expression (Rowley *et al*, 1993), but the molecular mechanism is still unknown. On the
314 other hand, osmotic shock causes a similar temporary repression of the G1/S regulon (Bellí *et al*, 2001),
315 where Hog1-mediated phosphorylation of Whi5 and Msa1 plays an important role in transcription
316 inhibition (González-Novo *et al*, 2015). However, G1/S gene expression was still repressed by salt in the
317 absence of Whi5 and Msa1, indicating the existence of additional mechanisms sufficient to inhibit the
318 G1/S regulon under osmotic shock. It has long been known that ER stress causes a G1 delay (Vai *et al*,
319 1987), but the molecular mechanisms have not been described. Our results uncover a new mechanism
320 that would explain the observed downregulation of G1/S genes by heat, salt and ER stress, whereby
321 immediate titration of chaperones would decrease available pools of Ssa1 and Ydj1 chaperones required
322 to accumulate the G1 Cdk in the nucleus for triggering Start. In this manner, stress conditions would delay
323 G1 progression until proteostasis and chaperone availability recover to normal levels (Fig 6).

324 Free chaperone levels could also report growth capability to other processes influenced by growth rate
325 (Brauer *et al*, 2008) or stressful conditions (De Nadal *et al*, 2011) through similar competition settings.
326 Furthermore, imposing a high level of free chaperones as a requirement for Start would ensure their
327 availability in highly-demanding downstream processes such as polarized growth for bud emergence or
328 nucleosome remodeling during replication.

329

330 **MATERIALS AND METHODS**

331 **Strains and plasmids**

332 Yeast strains and plasmids used are listed in Supplementary Table 1. Parental strains and methods used
333 for chromosomal gene transplacement and PCR-based directed mutagenesis have been described
334 (Gallego *et al*, 1997; Ferrezuelo *et al*, 2012). Unless stated otherwise, all gene fusions in this study were
335 expressed at endogenous levels at their respective loci. As C-terminal fusions of GFP or other tags has
336 strong deleterious effects on Ydj1 function (Saarikangas *et al*, 2017), we inserted GFP at amino acid 387,
337 between the dimerization domain and the C-terminal farnesylation sequence of Ydj1. This construct had
338 no detectable effects on growth rate or cell volume when expressed at endogenous levels. The mCitrine-
339 Cln3-11A fusion protein contains a hypoactive and hyperstable cyclin with 11 amino acid substitutions
340 (R108A, T420A, S449A, T455A, S462A, S464A, S468A, T478A, S514A, T517A, T520A) that allows its

341 detection by fluorescence microscopy with no gross effects on cell cycle progression (Schmoller *et al*,
342 2015).

343 **Growth conditions**

344 Cells were grown for 7-8 generations in SC medium with 2% glucose at 30°C before microscopy unless
345 stated otherwise. Other carbon sources used were 2% galactose, 2% raffinose and 3% ethanol. GAL1p-
346 driven gene expression was induced by addition of 2% galactose to cultures grown in 2% raffinose at
347 OD₆₀₀=0.5. When stated, 10 μM β-estradiol was used to induce the GAL1 promoter in strains expressing
348 the Gal4-hER-VP16 (GEV) transactivator (Louvion *et al*, 1993). Azetidine 2-carboxylic acid (AZC) was used
349 at 10 mM, and cycloheximide was added at a sublethal dose of 0.2 μg/ml that does not trigger stress
350 gene activation (Jacquet, 2003; Trotter *et al*, 2002). Heat and osmotic stresses were imposed by
351 transferring cells from 25°C to 37°C or adding 0.4M NaCl at 30°C, respectively. Tunicamycin was added
352 used at 1 μg/ml. Small newly-born cells were isolated from Ficoll gradients (Mitchison, 1988).

353 **Time-lapse microscopy**

354 Cells were analyzed by time-lapse microscopy in 35-mm glass-bottom culture dishes (GWST-3522, WillCo)
355 in SC-based media at 30°C essentially as described (Ferrezuelo *et al*, 2012) using a fully-motorized Leica
356 AF7000 microscope. Time-lapse images were analyzed with the aid of BudJ (Ferrezuelo *et al*, 2012), an
357 ImageJ (Wayne Rasband, NIH) plugin that can be obtained from www.ibmb.csic.es/home/maldea to
358 obtain cell dimensions and fluorescence data. Volume growth rate in G1 were obtained as described
359 (Ferrezuelo *et al*, 2012). Start was estimated at a single-cell level as the time where the nuclear to
360 cytoplasmic ratio of Whi5 had decreased below 1.5. Photobleaching during acquisition was negligible
361 (less than 0.1% per time point) and autofluorescence was always subtracted.

362 **Determination of nuclear and cellular concentrations of fluorescent fusion proteins**

363 Wide-field microscopy is able to collect the total fluorescence emitted by yeast cells and, consequently,
364 cellular concentration of fluorescent fusion proteins was obtained by dividing the integrated fluorescence
365 signal within the projected area of the cell by its volume. Regarding the quantification of nuclear levels,
366 since the signal in the nuclear projected area is influenced by both nuclear and cytoplasmic fluorescence,
367 determination of the nuclear concentration required specific calculations as described in Fig EV1A. In
368 confocal microscopy the fluorescence signal is directly proportional to the concentration of the
369 fluorescent fusion protein, and required no further calculations. The nuclear compartment was delimited
370 as described (Ferrezuelo *et al*, 2012).

371 **Chaperone mobility analysis by FLIP and FCS**

372 We used fluorescence loss in photobleaching (FLIP) and fluorescence correlation spectroscopy (FCS) to
373 analyze chaperone mobility in a Zeiss LSM780 confocal microscope. FLIP was used as a qualitative assay
374 to determine Ssa1-GFP and Ydj1-GFP mobility in the whole cell. A small circular region of the cytoplasm
375 ($3.6 \mu\text{m}^2$) was repetitively photobleached at full laser power while the cell was imaged at low intensity
376 every 0.5 sec to record fluorescence loss. After background subtraction, fluorescence data from an
377 unbleached cell region were made relative to the initial time point, and a mobility index was calculated as
378 the inverse of the fluorescence half-life obtained by fitting an exponential function to fluorescence
379 emitted as a function of time. Quantitative analysis of Ydj1-GFP diffusion by FCS was performed
380 essentially as described (Saarikangas *et al*, 2017). Specifically, FCS analysis was done at 25°C to minimize
381 signal variability in the 0.1-1 sec range, and cells were prebleached to attain count rates within the 50-
382 100 kHz range during acquisition for periods of 5 sec. FCS correlation data were fitted in the 10 μsec to
383 100 msec range of time intervals with the aid of QuickFit 3 (<http://www.dkfz.de/Macromol/quickfit/>),
384 assuming a 1-component anomalous mode of diffusion ($\alpha=0.5$) in the Levenberg-Marquardt algorithm to
385 obtain diffusion coefficients. Duplicate measurements were always taken and outliers were removed
386 from analysis if the relative standard error of the fitted coefficient of diffusion was higher than 50%, or
387 the fitted autocorrelation intersect was higher than 1.01 as a result of strong perturbations in the average
388 count rate during acquisition. In time-lapse experiments outliers were removed if the relative difference
389 to neighbor values was higher than 50%. Removed outliers were always less than 5% of measurements.

390 **Nuclear import rate determinations by FLIP**

391 To analyze nuclear import kinetics of Cdc28-GFP, a circle inscribed within the Htb2-mCherry nuclear
392 region was repetitively photobleached while the cell was imaged every 0.5 sec to record fluorescence
393 loss. After background subtraction, fluorescence data were corrected with those from a non-bleached
394 cell. Finally, fluorescence signals within nuclear and cytoplasmic areas were used to analyze import
395 kinetics as described in Fig EV2A. The export rate was assumed constant among G1 cells and obtained as
396 described in Fig EV2B.

397 **Immunofluorescence**

398 Immunofluorescence of endogenous levels of Cln3-3HA was done by a signal-amplification method
399 (Vergés *et al*, 2007) with αHA (clone 3F10, Roche) and goat- αrat and rabbit- αgoat Alexa555-labeled
400 antibodies (Molecular Probes) on methanol-pemeabilized cells. To analyze localization of Cln3-3HA we
401 used N2CJ, a plugin for ImageJ (Wayne Rasband, NIH), to perform accurate quantification in both
402 cytoplasmic and nuclear compartments of cells (Yahya *et al*, 2014).

403 Model equations

404 The model in Fig 3A was simulated with a set of non-linear differential equations.

$$\frac{d\mathbf{Prot}_U}{dt} = S_{Prot} * Vol - kb * \mathbf{Prot}_U * \frac{Ydj1_A}{Vol} - kd_{ProtU} * \mathbf{Prot}_U + kd_{Ydj1} * \mathbf{YP} \quad (1)$$

$$\frac{d\mathbf{YP}}{dt} = kb * \mathbf{Prot}_U * \frac{Ydj1_A}{Vol} - k_r * \mathbf{YP} - kd_{Ydj1} * \mathbf{YP} - kd_{ProtU} * \mathbf{YP} \quad (2)$$

$$\frac{d\mathbf{Prot}_F}{dt} = kr * \mathbf{YP} - \beta * kd_{ProtU} * \mathbf{Prot}_F \quad (3)$$

405
$$\frac{d\mathbf{Cln3}_U}{dt} = S_{Cln3} * Vol - kb * \mathbf{Cln3}_U * \frac{Ydj1_A}{Vol} - kd_{Cln3U} * \mathbf{Cln3}_U + kd_{Ydj1} * \mathbf{YC} \quad (4)$$

$$\frac{d\mathbf{YC}}{dt} = kb * \mathbf{Cln3}_U * \frac{Ydj1_A}{Vol} - kr * \mathbf{YC} - kd_{Ydj1} * \mathbf{YC} - kd_{Cln3U} * \mathbf{YC} \quad (5)$$

$$\frac{d\mathbf{Cln3}_F}{dt} = kr * \mathbf{YC} - kd_{Cln3F} * \mathbf{Cln3}_F \quad (6)$$

$$\begin{aligned} \frac{dYdj1_A}{dt} = & S_{Ydj1} * Vol - kb * \mathbf{Prot}_U * \frac{Ydj1_A}{Vol} - kb * \mathbf{Cln3}_U * \frac{Ydj1_A}{Vol} \\ & + kr * \mathbf{YP} + kr * \mathbf{YC} - kd_{Ydj1} * Ydj1_A + kd_{Cln3U} * \mathbf{YC} + kd_{ProtU} * \mathbf{YP} \quad (7) \end{aligned}$$

406 This model has seven state variables: \mathbf{Prot}_U , unfolded proteins; \mathbf{YP} , Ydj1-bound proteins; \mathbf{Prot}_F , folded
407 proteins; $\mathbf{Cln3}_U$, unfolded Cln3; \mathbf{YC} , Ydj1-bound Cln3; $\mathbf{Cln3}_F$, folded Cln3; and $Ydj1_A$, free available Ydj1.

408 Model parameters and simulations

409 In the model we define eleven parameters (Table 1). Ydj1 binding and release (kb , kr), which are assumed
410 to be the same for \mathbf{Prot}_U and $\mathbf{Cln3}_U$ (see Fig EV4), and synthesis (S_{Prot} , S_{Cln3} , S_{Ydj1}) and degradation (kd_{ProtU} ,
411 kd_{Cln3U} , kd_{Cln3F} , kd_{Ydj1}) of the different components. A scaling factor ($\beta=0.01$) is used to ensure that folded
412 protein (\mathbf{Prot}_F) has a half-life 100 times that of unfolded protein (\mathbf{Prot}_U). The state variables in the model
413 are in units of molecular number, not concentration, and therefore all 0th and 2nd order reactions are
414 explicitly scaled by cell volume (Vol). In the model, we assume that the rate of change of cell volume with
415 time is much lower than the rates of the biochemical reactions studied. This allowed us to treat the cell
416 volume as a pseudo-parameter, so the steady state of other variables with respect to cell volume and
417 growth rate (S_{ProtU}) could be analyzed more straightforwardly. The half-life of unfolded (kd_{Cln3U}) Cln3 was
418 set to be 1.8 times longer than folded (kd_{Cln3F}) Cln3 as deduced from steady-state levels of Cln3-3HA in
419 wild-type and Ydj1-deficient cells (Yaglom *et al*, 1996), while Ydj1 is a stable protein, with a half-life 20
420 times longer than folded Cln3. To reduce the degrees of freedom available for modeling, degradation
421 rates of all molecules were kept constant independent if they are in a complex or free. The underlying
422 reasoning is that molecules should be still recognized by their respective degradation machinery
423 independent of their binding partners. This should be true in our cases, since the binding of Ydj1 to its
424 targets is highly dynamic. We converted half-lives to degradation rates using the formula $\lambda = \log(2)/t_{1/2}$.

425 The remaining five parameters were used to quantitatively fit two sets of measurements: the relationship
 426 between the diffusion rate of Ydj1 and growth rate in G1 cells (Fig 3F), and the relationship between
 427 budding volume and growth rate (Fig 3G).

428 **Table 1. Model parameters**

Parameter	Definition	Type	Value	Parameter set 3114
Vol	Cell volume	Controlled	10-100 fl	
S_{ProtU}	Protein synthesis	Controlled	0.01-1 molec·sec ⁻¹ ·fl ⁻¹	
S_{Cln3}	Cln3 synthesis	Fitted	4.9·10 ⁻² -4.8 molec·sec ⁻¹ ·fl ⁻¹	0.126 molec·sec ⁻¹ ·fl ⁻¹
S_{Ydj1}	Ydj1 synthesis	Fitted	4.8·10 ⁻⁵ -6.0·10 ⁻² molec·sec ⁻¹ ·fl ⁻¹	9.19·10 ⁻⁴ molec·sec ⁻¹ ·fl ⁻¹
kd_{ProtU}	ProtU degradation	Fitted	6.4·10 ⁻³ -31.5 sec ⁻¹	7.26·10 ⁻² sec ⁻¹
kd_{ProtF}	ProtF degradation	Fitted	0.01* kd_{ProtU} sec ⁻¹	7.26·10 ⁻⁴ sec ⁻¹
kb	Binding to Ydj1	Fitted	1.4·10 ⁻² -26.7 fl·molec ⁻¹ ·sec ⁻¹	0.891 fl·molec ⁻¹ ·sec ⁻¹
kr	Release from Ydj1	Fitted	2.8·10 ⁻³ -7.7 sec ⁻¹	0.388 sec ⁻¹
kd_{Cln3U}	Cln3U degradation	Fixed	6.93·10 ⁻² sec ⁻¹	
kd_{Cln3F}	Cln3F degradation	Fixed	3.85·10 ⁻² sec ⁻¹	
kd_{Ydj1}	Ydj1 degradation	Fixed	5.77·10 ⁻³ sec ⁻¹	

429
 430 **Budding volume vs growth rate**
 431 In the model, we assume that Start is triggered by Cln3 when reaches a given critical threshold ($Cln3_F^{crit} =$
 432 25) that, together with Cdc28, is needed to phosphorylate and inactivate a fixed given amount of DNA-
 433 bound Whi5/SBF complexes (Schmoller *et al*, 2015; Wang *et al*, 2009). Our objective was then to
 434 minimize the difference between experimental measurements and simulation results by changing the five
 435 free parameters in $L1(\theta) = (Vol(s_{Vol})_{exp} - Vol(\theta | s_{Vol})_{sim})^2$, where $Vol(s_{Vol})_{exp}$ is the
 436 experimentally measured budding volume (as a proxy for the critical volume at Start) of a cell growing at
 437 rate s_{Vol} , and $Vol(\theta | s_{Vol})_{sim}$ is the volume of cells growing at rate s_{Vol} reach a steady state value
 438 where $Cln3_F$ equals the critical threshold $Cln3_F^{crit}$.

439 **Ydj1 diffusion vs growth rate**

440 We assume that Ydj1 is present in two distinct pools: a fast diffusing free fraction ($Ydj1_A$), and a slowly
 441 diffusing fraction bound to either *Prot* or *Cln3* ($YP+YC$). To compare the experimentally measured
 442 diffusion rate of Ydj1 to our simulations, we define the simulated diffusion rate of Ydj1 as the weighted
 443 average diffusion coefficient for all species of Ydj1 in our model as follows:

$$444 \quad D_{sim} = \frac{Ydj1_A}{Ydj1} * D_{free} + \frac{YP+YC}{Ydj1} * D_{bound} \quad (8)$$

445 For Ydj1-GFP we estimated that $D_{bound} = 1 \mu\text{m}^2/\text{min}$ from minimal values observed in AZC-treated cells,
 446 and $D_{free} = 30 \mu\text{m}^2/\text{min}$ from maximal values obtained with GFP and corrected by the different Stokes

447 radius. As above, we sought to minimize $L2(\theta) = (D_{exp}(s_{Vol}, Vol) - D_{sim}(\theta | s_{Vol}, Vol))^2$, where
448 $D_{exp}(s_{Vol}, Vol)$ and $D_{sim}(\theta | s_{Vol}, Vol)$ are the experimental and simulated diffusion coefficients at a
449 given growth rate and volume in G1 cells.

450 **Fitting procedures**

451 For fitting Ydj1 diffusion and budding volume as a function of growth rate we combined the respective
452 square differences to seek $\underset{\theta}{\operatorname{argmin}} L1(\theta) + L2(\theta)$. To find the optimal value of θ we used a variant of the
453 Levenberg-Marquardt algorithm with a 2nd order correction (Transtrum & Sethna, 2012). As all the
454 simulations were done at steady state, to obtain the Jacobian of the steady state with respect to the
455 parameters, we applied the implicit function theorem following the approach described here:
456 <https://arxiv.org/pdf/1602.02355.pdf>. Numerical integration of the differential equations (to obtain an
457 initial value for the steady state root finding) was done using the *SciPy routine odeint*, which automatically
458 switches between stiff and non-stiff solvers. After identifying the minima, we performed a Markov Chain
459 Monte Carlo (Goodman & Weare, 2010) exploration of the parameter space using *emcee* (Foreman-
460 Mackey *et al*, 2013). After discarding the initial 3000 draws of the MC chain as burn-in, which were too
461 close to the minima, we collected 1500 sets with good match to data and repeated all simulations using
462 this ensemble of parameters to estimate the uncertainty in parameters (Fig 3B) and simulations of
463 variables used in the initial exhaustive fitting process (Fig 3F and 3G). Simulations of other variables that
464 were experimentally tested (Fig 3H, 4B and 5B) were done with parameter set 3114 (Table 1), which gave
465 the minimal p value in the fitting process, and using a 4-fold range of values for the Ydj1-binding and
466 release constant rates (kb and kr , respectively). CHX effects were simulated by reducing $ksProt$, $ksCln3$ and
467 $ksYdj1$ 3, 4.5, 6, 9, or 12-fold to test different conditions around the experimental reduction of 5.9-fold (Fig
468 EV7). Stress effects were simulated on steady states by transferring different fractions (20-80%) of the
469 folded protein (ProtF and Cln3F) to the unfolded population (ProtU and Cln3U, respectively). To simulate
470 transient effects in Cln3F by stress, experimental data of Ydj1-GFP mobility were used to fit the model time
471 variable at different percentages of protein unfolding (Fig 5CD), resulting in 60% for salt stress and 80% for
472 heat stress. We took into account that heat, but not salt, stress increases Ydj1 mRNA levels by 2.9-fold
473 (Gasch *et al*, 2000). Then, the resulting fitted parameters were applied to the model to simulate the
474 evolution of Cln3F after stress assuming that ProtU and Cln3U compete or not for Ydj1A (Fig 5GH). The
475 model was deposited in the BioModels (Chelliah *et al*, 2015) database as MODEL1808310001 in SBML
476 format and a Copasi (Hoops *et al*, 2006) file to reproduce simulations with parameter set 3114. Code of
477 the estimation of minima in IPython Notebooks is available upon request.

478 **Parameter distributions**

479 As amply described in the literature, parameters in systems biology models are disheveled (Gutenkunst *et*
480 *al*, 2007) or structurally unidentifiable (Szederkényi *et al*, 2011). We observed this behavior as well (Fig
481 3B), with parameters consistent with the experimental data spanning several orders of magnitude.

482 **Statistical analysis**

483 We routinely show the standard error of the mean ($N < 10$) or confidence limits at $\alpha = 0.05$ ($N > 10$) to allow
484 direct evaluation of variability and differences between mean values in plots. Sample size is always
485 indicated in the figure legend and, when appropriate, t-test p values are shown in the text. For model
486 predictions the mean values and standard deviations are plotted. All experiments were done at least
487 twice with fully independent cell samples.

488 **Miscellaneous**

489 *In vitro* luciferase refolding assays have been described (Summers *et al*, 2009). Translational efficiency of
490 refolding extracts was measured by incubation with 0.1 mM puromycin. Immunoblot analysis with
491 α puromycin (clone 12D10, Sigma), α HA (clone 12CA5, Roche) and α Dpm1 (clone 5C5, Molecular Probes)
492 was as described (Georgieva *et al*, 2015). Ydj1 binding assays to GST-fusions of Cln3, luciferase and P6, a
493 selected Ydj1-target peptide (Kota *et al*, 2009) used as reference, were done with purified proteins as
494 described (Lee *et al*, 2002). Protein synthesis rates in live cells were determined by S^{35} -methionine
495 incorporation (Gallego *et al*, 1997).

496

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503

504 **AUTHOR CONTRIBUTIONS**

505 D.F.M., E.P. and G.Y. built genetic constructs and strains, and performed the experiments. F.V. and A. C.-
506 N. implemented the mathematical model and performed the informatic analysis. A. C.-N. and M.A.
507 conceived the study, designed the mathematical model, analyzed the data and wrote the manuscript.

508

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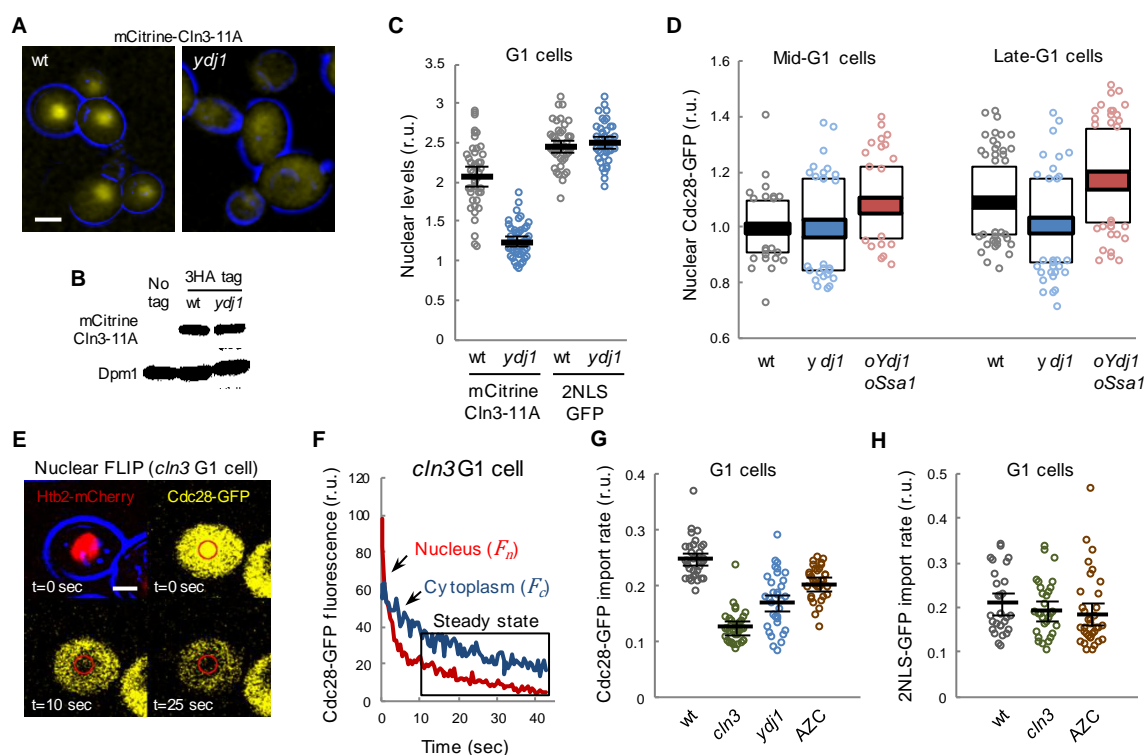
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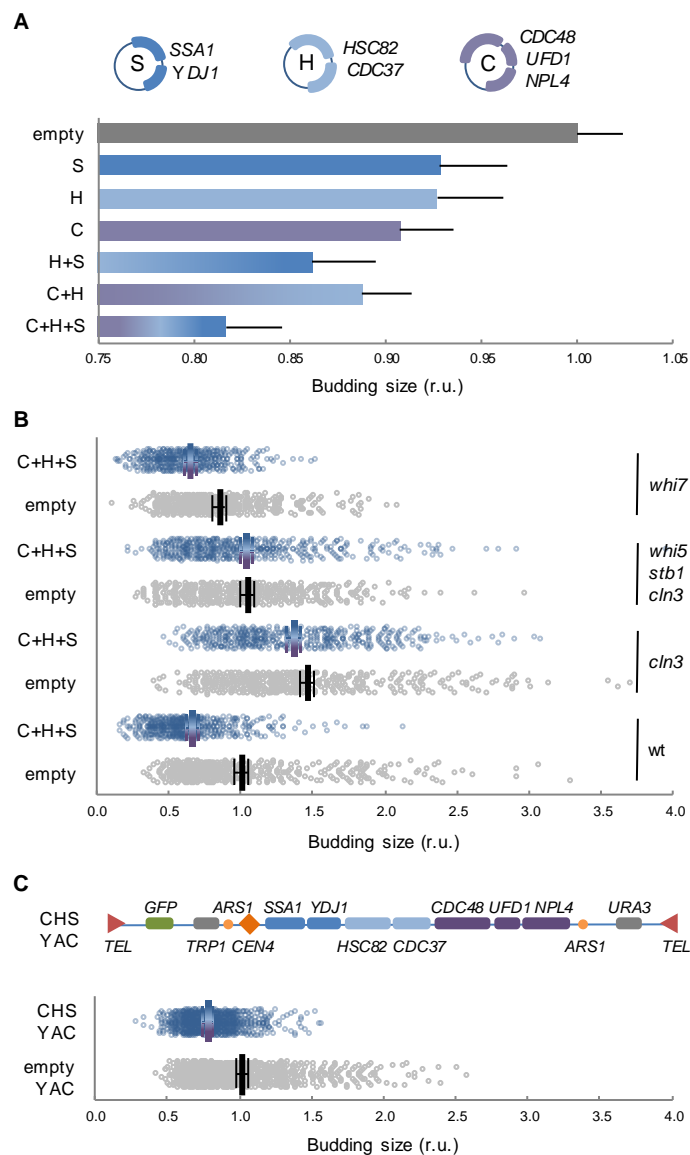
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Figure 1. Nuclear accumulation of the G1 Cdk depends on chaperone function.

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704 A Images corresponding to wild-type (wt) and Ydj1-deficient (*ydj1*) cells expressing mCitrine-Cln3-11A. Bar is 2 μ m.
705 B Immunoblotting analysis of 3HA-tagged mCitrine-Cln3-11A levels in wild-type and *ydj1* cells. Dpm1 is shown as
706 loading control.
707 C Nuclear to cytoplasmic mCitrine-Cln3-11A and 2NLS-GFP ratios for individual wild-type and *ydj1* G1 cells. Mean
708 (N=30, thick lines) and confidence limits ($\alpha=0.05$, thin lines) for the mean are also plotted.
709 D Cdc28-GFP wild-type (wt), Ydj1-deficient (*ydj1*) or overexpressing Ydj1 and Ssa1 (*oYdj1 oSsa1*) cells were analyzed by
710 time-lapse microscopy during G1 progression. Mean (N>100) nuclear to cytoplasmic Cdc28-GFP ratios are plotted
711 with respective standard deviation (white boxes) and confidence ($\alpha=0.05$, colored boxes) intervals for the mean at
712 either mid (36-45 min before Start) or late G1 (18-21 min before Start).
713 E Analysis of Cdc-28-GFP import by nuclear FLIP. A representative *cln3* cell expressing Cdc28-GFP and Htb2-mCherry at
714 different times during nuclear photobleaching is shown. Bar is 1 μ m.
715 F A representative nuclear FLIP output of Cdc28-GFP in a Cln3-deficient G1 cell showing fluorescence decay in nuclear
716 and cytoplasmic compartments.
717 G Cdc28-GFP import rates in wild-type (wt), Cln3-deficient (*cln3*), and Ydj1-deficient (*ydj1*) single cells in G1 phase.
718 Wild-type cells treated with AZC are also shown. Mean values (N>30, thick lines) with confidence limits for the mean
719 ($\alpha=0.05$, thin lines) are also plotted.
720 H 2NLS-GFP-EBD import rates in wild-type (wt) and Cln3-deficient (*cln3*) G1 single cells after in the presence of 1 μ M
721 auxin. Wild-type cells treated with AZC are also shown. Mean values (N>30, thick lines) with confidence limits for the
722 mean ($\alpha=0.05$, thin lines) are also plotted.
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Figure 2. Chaperones of the Hsp70, Hsp90 and Cdc48 systems are limiting for cell cycle entry.

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A Budding volume of yeast cells transformed with the indicated combinations of compatible centromeric vectors encoding chaperones of the Hsp70 (S, *SSA1* and *YDJ1*), Hsp90 (H, *HSC82* and *CDC37*), and Cdc48 (C, *CDC48*, *UFD1* and *NPL4*) systems. Individual budding volumes were determined and made relative to the mean value for wild-type cells transformed with the corresponding empty vectors. Mean values (N>200) and confidence limits ($\alpha=0.05$, thin vertical lines) for the mean are plotted.

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B Yeast cells with indicated genotypes were transformed with empty or compatible centromeric vectors encoding the three chaperone systems (C+H+S) and budding volumes were determined as in panel A. Individual data (N>400), mean values (thick vertical lines) and confidence limits ($\alpha=0.05$, thin vertical lines) for the mean are plotted.

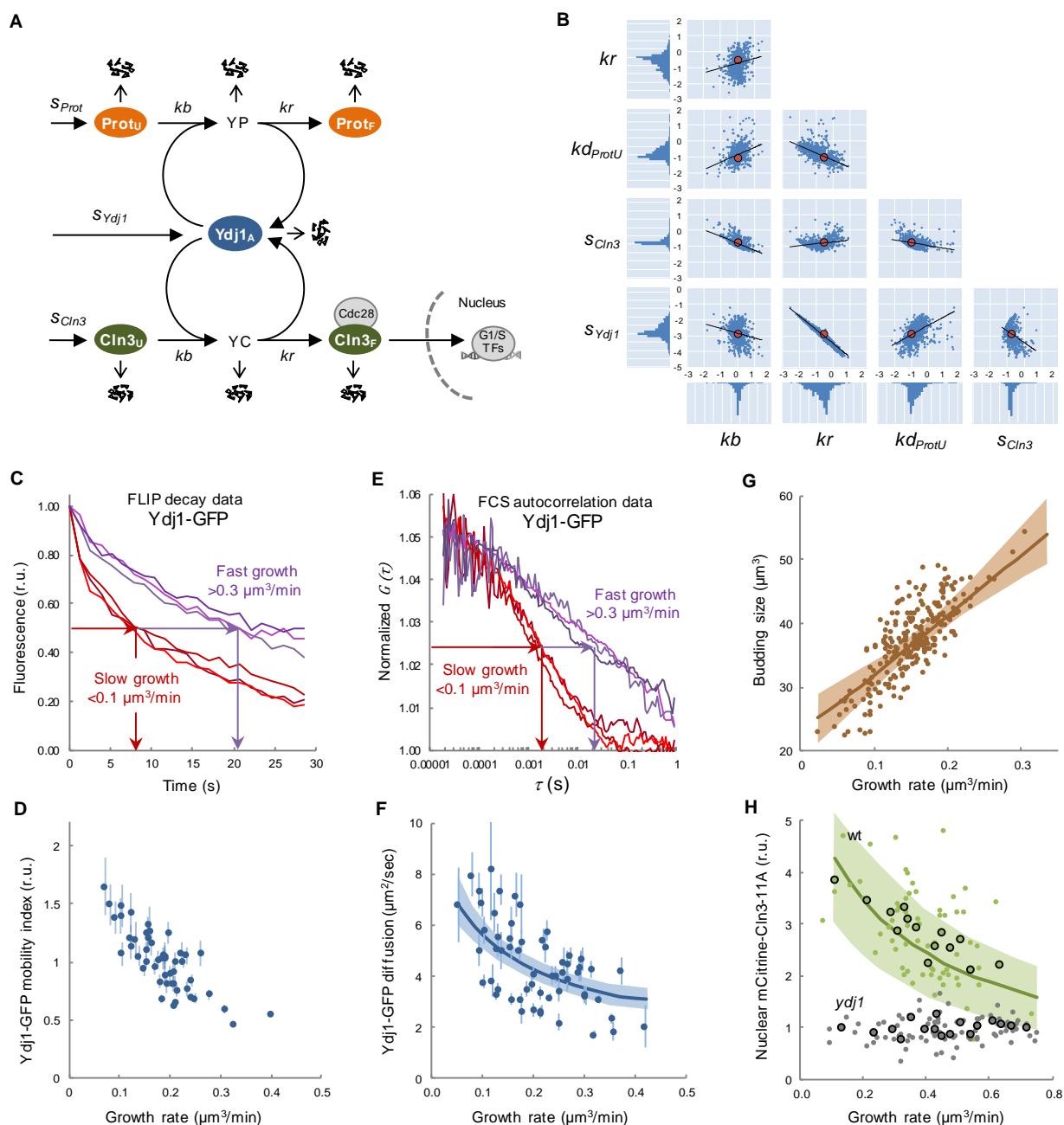
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C Budding volume of yeast cells transformed with an artificial chromosome encoding the three chaperone systems (CHS YAC) or empty vector. Budding volumes were determined as in panel A. Individual data (N<400), mean values (thick vertical lines) and confidence limits ($\alpha=0.05$, thin vertical lines) for the mean are plotted.

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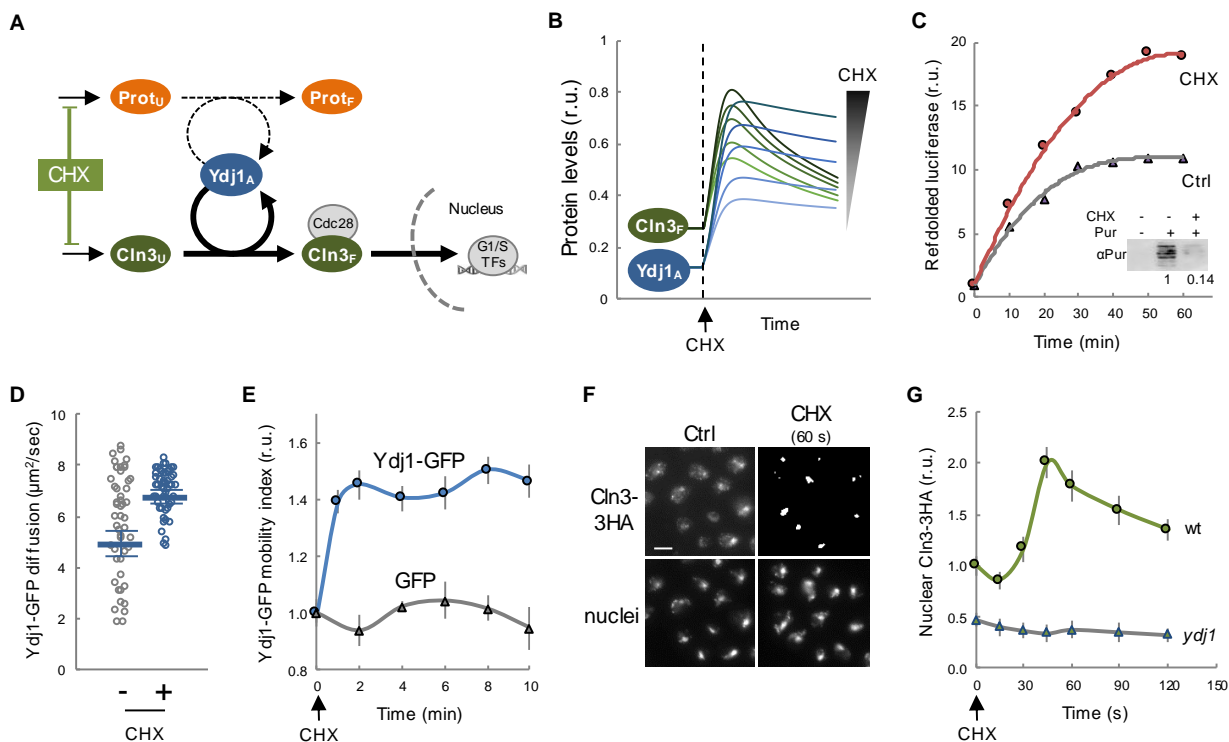
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742 **Figure 3. The molecular competition model, chaperone availability and nuclear accumulation of Cln3.**

743 **A** Scheme of the chaperone competition model connecting protein synthesis and Cln3 folding and complex
744 formation with Cdc28. Chaperones associate to the unfolded protein (Prot_U) mostly in a transient manner until
745 the properly folded protein (Prot_F) is released. Thus, protein synthesis rate would be a key determinant of the
746 level of available Ydj1 (Ydj1_A) in the free pool and, as it is essential in proper folding and release of Cln3 (Cln3_F), it
747 would in turn govern the rate of Whi5 phosphorylation in the nucleus for triggering Start. Variables and
748 parameters used in the model are indicated. All key components of the competition model are subject to specific
749 rates of degradation (open arrows) as described in Materials and Methods.

750 **B** Distribution of parameters of the model fitted to experimental data of Ydj1 diffusion and critical volume as a
751 function of growth rate. Parameter sets sampled using Markov Chain Monte Carlo (small blue circles) are plotted
752 in log₁₀ space as well as the corresponding mode values (large red circles) and regression lines. One-dimensional
753 histograms of parameter values are also plotted adjacent to the axes.

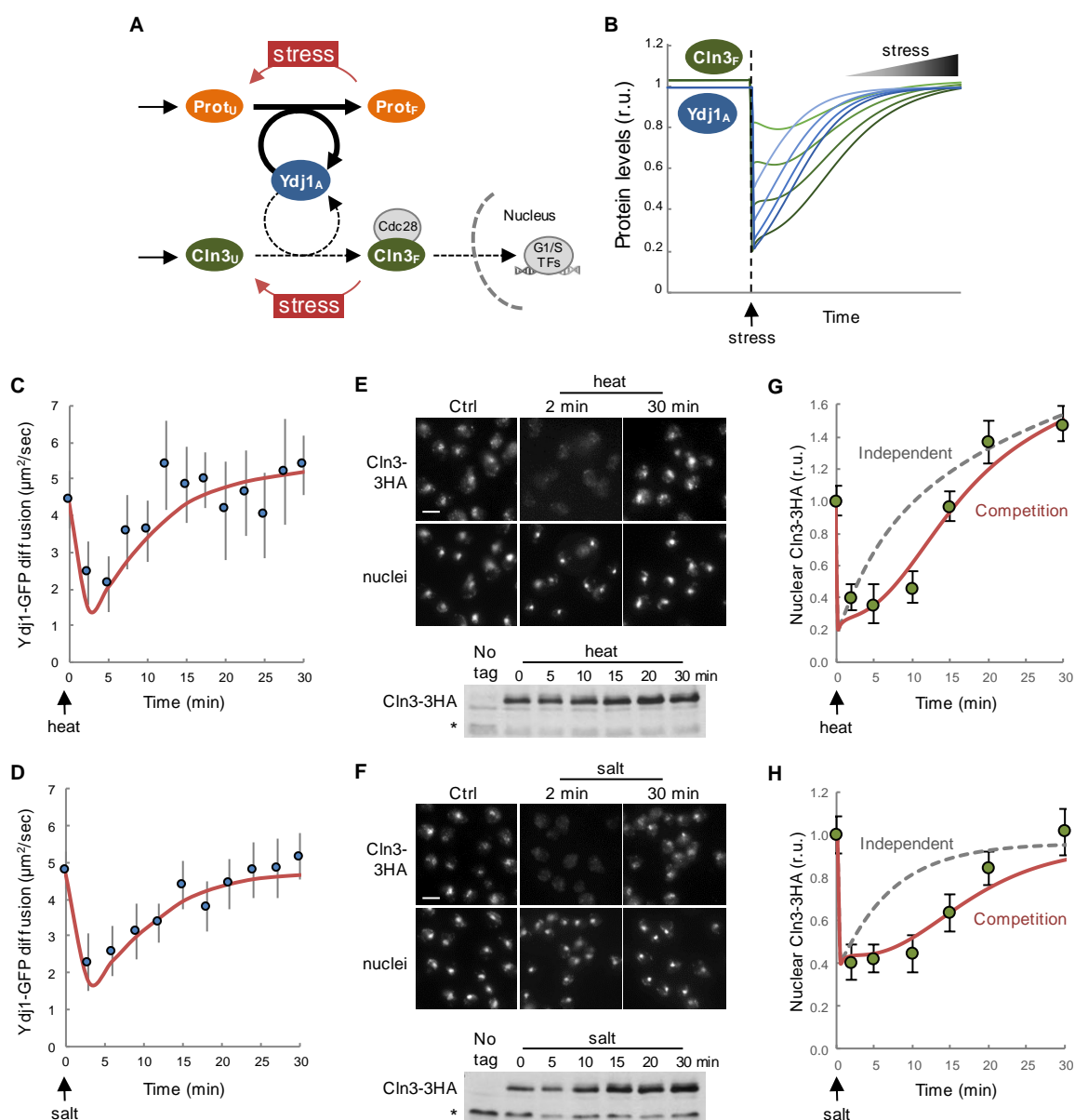
- 754 C Yeast cells expressing Ydj1-GFP were analyzed by FLIP in time-lapse experiments to determine also growth rate at
755 a single-cell level. Individual FLIP decay data are plotted for three fast ($>0.3 \mu\text{m}^3/\text{min}$, purple lines) and three slow
756 ($<0.1 \mu\text{m}^3/\text{min}$, red lines) growing cells.
- 757 D Ydj1-GFP mobility indexes (circles) were obtained from FLIP decay curves as shown in panel C and plotted as a
758 function of growth rate with the corresponding confidence limits ($\alpha=0.05$).
- 759 E Yeast cells expressing Ydj1-GFP were analyzed by FCS in time-lapse experiments to determine also growth rate at
760 a single-cell level. Individual FCS autocorrelation data are plotted for three fast ($>0.3 \mu\text{m}^3/\text{min}$, purple lines) and
761 three slow ($<0.1 \mu\text{m}^3/\text{min}$, red lines) growing cells.
- 762 F Ydj1-GFP diffusion coefficients (circles) were obtained from FCS autocorrelation functions as shown in panel E and
763 plotted as a function of growth rate with the corresponding standard error. The mean fit produced by the full
764 ensemble of parameter sets shown in panel B is plotted as a line with one standard deviation intervals.
- 765 G The chaperone competition model predicts the critical size being a function of growth rate at the single-cell level.
766 Experimental budding volumes as a function of growth rate (closed circles) and the mean fit as in panel F are
767 shown.
- 768 H Nuclear to cytoplasmic ratios for mCitrine-Cln3-11A from G1 wild-type (wt, green, N=68) and Ydj1-deficient (*ydj1*,
769 gray, N=85) cells as a function of growth rate. Mean values (large circles) and confidence limits ($\alpha=0.05$) for
770 binned (5 cells/bin) data are also shown. A simulation of Cln3F was obtained with parameter set 3114 within a 4-
771 fold range of *kd* and *kr*, and the resulting mean (green line) is plotted with one standard deviation intervals.
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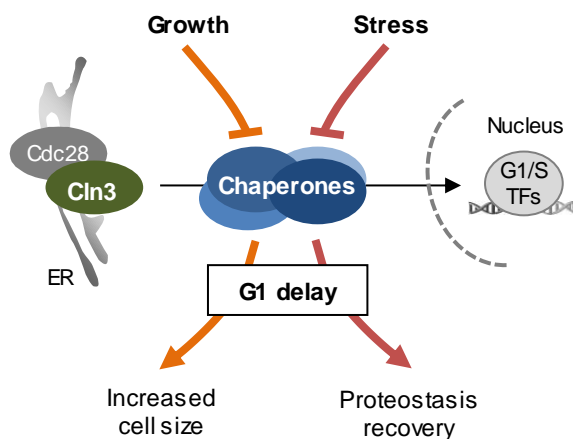
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Figure 4. Protein synthesis is a key determinant of chaperone availability and nuclear accumulation of Cln3.

- A The competition model predicts that reducing the protein synthesis rate would decrease the requirements of Ydj1 chaperone in folding of new proteins ($Prot_F$), and increase the level of available chaperone ($Ydj1_A$) and free Cln3 ($Cln3_F$).
- B Prediction of available chaperone ($Ydj1_A$) and free Cln3 ($Cln3_F$) levels as a function of time after CHX addition. Simulations were produced by using parameter set 3114 and varying (3, 4.5, 6, 9, or 12-fold) reductions in protein synthesis rates around the experimental value (Fig EV7).
- C Refolded luciferase activity as a function of time in yeast cell extracts treated or not with 20 $\mu\text{g/ml}$ CHX in the presence of an ATP-regenerating system. Inset: Immunoblot analysis of puromycin incorporation in cell-free extracts used for refolding analysis in the absence or presence of 20 $\mu\text{g/ml}$ CHX. Numbers refer to relative incorporation levels as measured by densitometric analysis.
- D Yeast cells expressing Ydj1-GFP were analyzed by FCS before (-) or 5 to 10 min after adding a sublethal dose of CHX at 0.2 $\mu\text{g/ml}$ (+). Individual protein diffusion coefficients are plotted ($N > 50$). Mean values (thick lines) and confidence limits for the mean ($\alpha = 0.05$, thin lines) are also shown.
- E Ydj1-GFP and GFP mobility assayed by FLIP at the indicated time points after CHX addition at 0.2 $\mu\text{g/ml}$. Relative mean values and confidence limits ($\alpha = 0.05$) for the mean are shown.
- F Nuclear levels of Cln3-3HA by immunofluorescence before or 60 sec after addition of CHX at 0.2 $\mu\text{g/ml}$.
- G Nuclear accumulation of Cln3-3HA in asynchronous individual wild type (wt) and Ydj1-deficient (*ydj1*) yeast cells before or at the indicated times after CHX addition as in panel F. Relative mean values ($N > 200$) and confidence limits ($\alpha = 0.05$, thin horizontal lines) for the mean are shown.



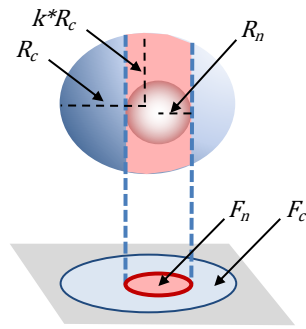
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799 **Figure 5. Stress reduces chaperone mobility and hinders nuclear accumulation of Cln3.**
800 A The competition model predicts that a sudden increase in the level of unfolded proteins ($Prot_U$) would decrease
801 the level of available chaperone ($Ydj1_A$) and, hence, reduce the level of free Cln3 ($Cln3_F$).
802 B Prediction of available chaperone ($Ydj1_A$) and free Cln3 ($Cln3_F$) levels as a function of time after stress.
803 Simulations were produced by using parameter set 3114 and transferring different fractions (20-80%) of folded
804 protein ($Prot_F$) to the unfolded population ($Prot_U$).
805 C,D Mean $Ydj1$ -GFP diffusion coefficients ($N>20$, filled circles) and confidence limits ($\alpha=0.05$, thin lines) are plotted
806 at different times during heat (C) or salt (D) stress. Model fits (see text for details) are also shown (orange lines).
807 E,F Immunofluorescence of Cln3-3HA in late-G1 cells arrested with α factor during heat (E) and salt (F) stress.
808 Bottom: Cln3-3HA levels by immunoblotting. A cross-reacting band is shown as loading control.
809 G,H Nuclear levels of Cln3-3HA quantified from cells during heat (E) and salt (F) stress as in panels E and F. Relative
810 mean values ($N>200$) and confidence limits ($\alpha=0.05$, thin horizontal lines) for the mean are shown. Model
811 simulations (see text for details) assuming that $Prot_U$ and $Cln3_U$ require $Ydj1_A$ in independent (gray dashed
812 lines) or competing (solid orange lines) scenarios are also shown.



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Figure 6. Competition for chaperones and the regulation of cell-cycle entry by growth and stress.

Chaperone-dependent Cln3 folding and release would act as a key modulator of Start to subordinate cell-cycle entry to growth and stress. By compromising higher levels of chaperones in growth processes, fast growing cells would restrain nuclear accumulation of Cln3 until a larger cell size is attained. On the other hand, stressful conditions would compromise common chaperones and delay Start until normal proteostasis conditions are restored.



$$N/C = 1 + (F_r - \frac{3}{2}k) / (R_r - F_r \cdot R_r^3)$$

$$R_r = R_n / R_c$$

$$F_r = F_n / F_c$$

N/C – Nuclear to cytoplasmic concentration ratio

F_n – Average fluorescence in nucleus projected area

F_c – Average fluorescence in cell projected area

R_n – Nuclear radius

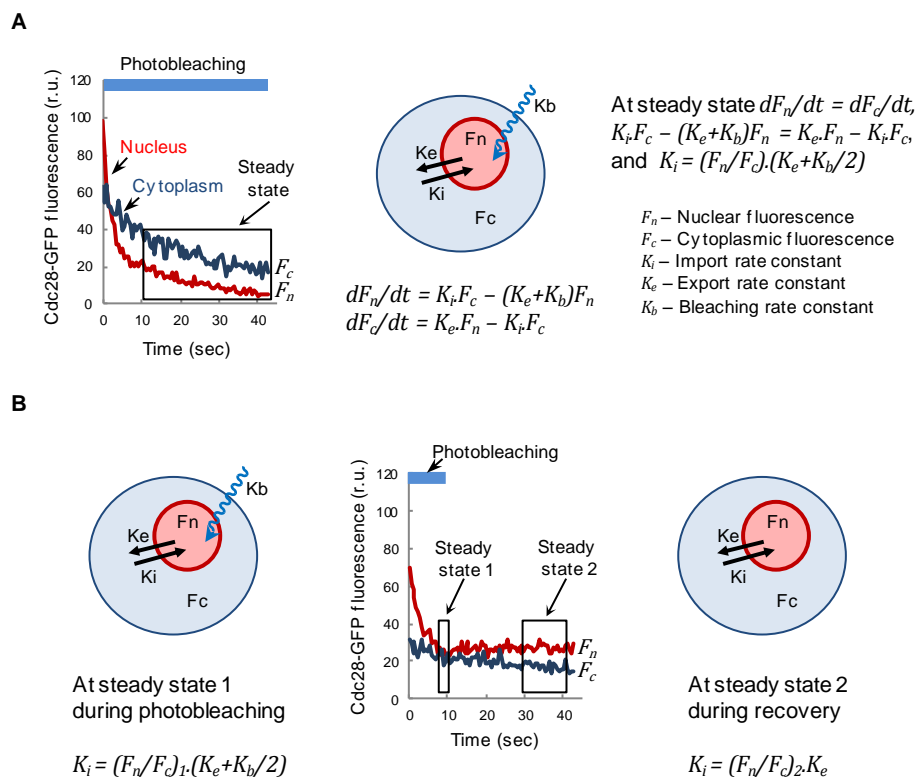
R_c – Cell radius

k – Correction factor in z axis

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824 **Figure EV1. Nuclear to cytoplasmic ratios by wide-field fluorescence microscopy.**

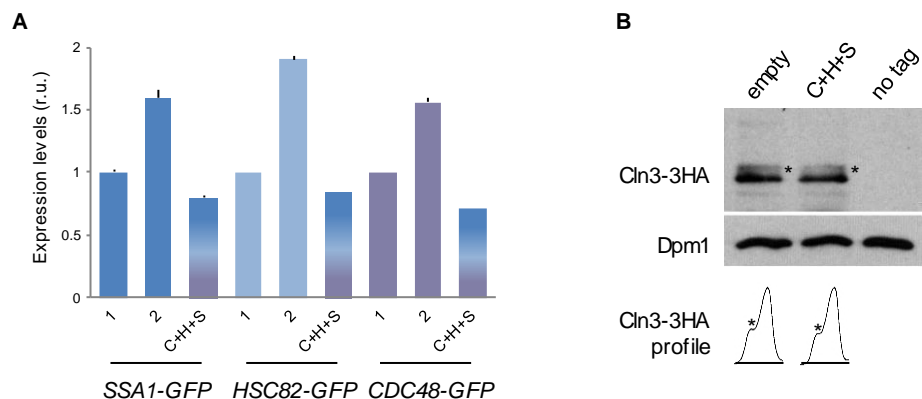
825 Fluorescence within the nuclear projected area is influenced by fluorescence levels in both nuclear and cytoplasmic
826 compartments. Briefly, the nuclear projection collects fluorescence originated from a column defined by the nuclear
827 diameter and the cell height. Total fluorescence in the column is the weighted sum of nuclear and cytoplasmic
828 concentrations of fluorophore assuming that the column is a cylinder and the nucleus a sphere with known
829 dimensions relative to the cell. Cytoplasmic fluorescence (and concentration) is obtained from cell regions outside
830 the nuclear projection, and the ratio of the nuclear to cytoplasmic concentration of the fluorescent protein is
831 calculated as $N/C = 1 + (F_r - \frac{3}{2} * k) / (R_r - F_r * R_r^3)$, where F_r is the ratio of average fluorescence signal in
832 nuclear (F_n) and cell (F_c) projected areas, R_r is the ratio of nuclear (R_n) and cell (R_c) radius, and k corrects for cell
833 radius variation in the z axis, which was experimentally obtained from GFP-expressing wild-type cells.
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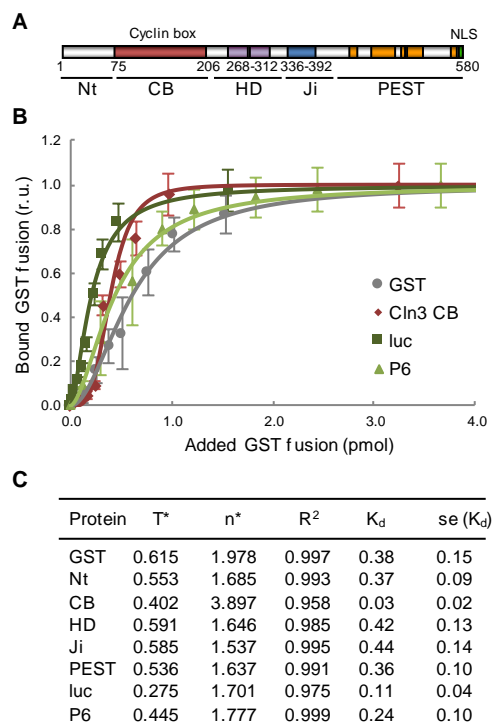
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Figure EV2. Nuclear import kinetics analysis by nuclear FLIP.

- A Schematic showing equations and parameters used to analyze Cdc28-GFP import and export kinetics as described under Materials and Methods. Fluorescence signals within nuclear (F_n) and cytoplasmic (F_c) areas were used to obtain a nuclear to cytoplasmic ratio (F_n/F_c). This ratio dropped to different extents during the first 10 sec of exposure, reflecting a population of Cdc28-GFP molecules in the nucleus not in dynamic equilibrium with the cytoplasm. After this period, however, the (F_n/F_c) ratio reached a steady state defined by $dF_n/dt = dF_c/dt$, being $dF_n/dt = K_i F_c - (K_e + K_b) F_n = K_e F_n - K_i F_c$, where K_i , K_e and K_b are the import, export and bleaching rate constants, respectively. Thus, $K_i F_c - (K_e + K_b) F_n = K_e F_n - K_i F_c$, and $K_i = (F_n/F_c) (K_e + K_b/2)$. The bleaching rate constant was obtained from Htb2-mCherry fluorescence loss in the same cell and corrected by a bleaching factor of 1.94 ± 0.09 to account for intrinsic differences in bleaching rates for GFP and mCherry, which was obtained from G1 cells (N=33) under conditions that minimize import contribution (Cln3-deficient cells).
- B Schematic showing equations and parameters used to obtain Cdc28-GFP export kinetics. In this case, the nuclear region of wild-type G1 cells (N=34) was only photobleached for 10 s and allowed to recover fluorescence by nuclear import of Cdc28-GFP. F_n/F_c ratio steady states were used to calculate import rate constants at photobleaching, $K_i = (F_n/F_c)_1 \cdot (K_e + K_b/2)$, and recovery, $K_i = (F_n/F_c)_2 \cdot K_e$, to finally obtain the export rate constant $K_e = 0.199 \pm 0.020$.



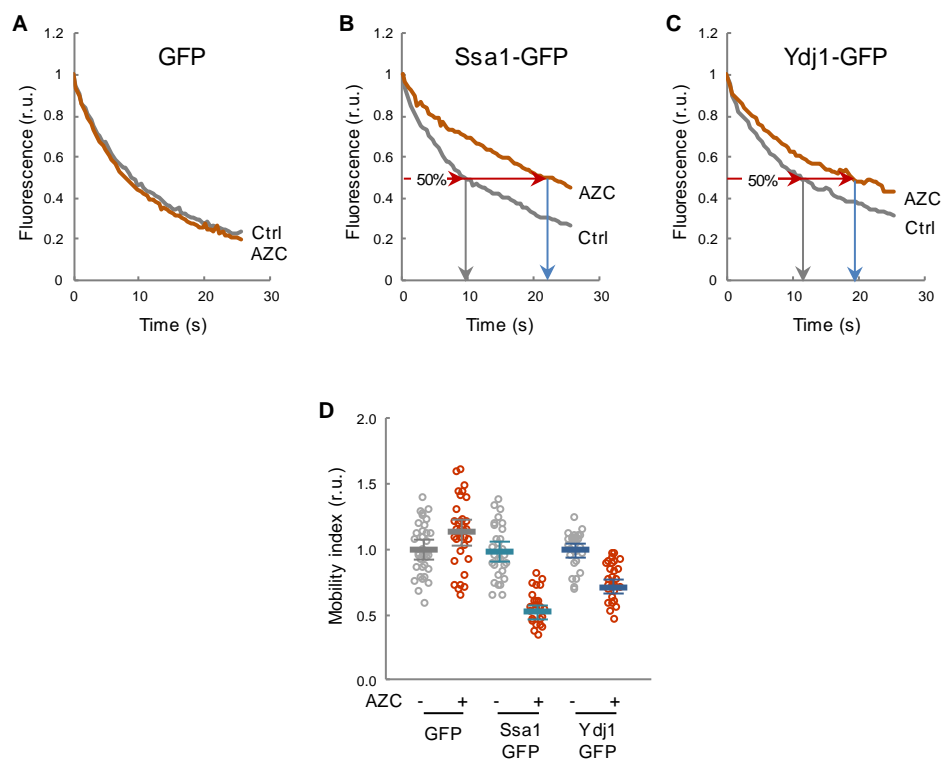
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856 **Figure EV3. Gene dosage and expression levels of GFP-fused chaperones and Cln3-3HA.**
857 A Expression levels of the indicated chaperones endogenously expressed as GFP fusions in single (1) or double (2)
858 copy, or in single copy and the presence of untagged-chaperone expressing vectors (C+H+S) as in Fig 2A.
859 Fluorescence levels were determined and made relative to the mean value for cells containing a single copy of
860 the indicated chaperone gene. Mean values (N>500) and confidence limits ($\alpha=0.05$, thin vertical lines) for the
861 mean are plotted.
862 B Immunoblot analysis of endogenously expressed Cln3-3HA levels from cells containing empty or chaperone
863 expressing vectors as in Fig 2A. A Dpm1 immunoblot is shown as loading control. Densitometric profiles of the
864 corresponding lanes are shown for direct assessment of total levels and phosphorylated (*) status.
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Figure EV4. Ydj1 binding affinity to Cln3 and reference proteins.

- A Cln3 scheme indicating the N-terminal domain (N_t), the cyclin box (CB), a hydrophobic bi-partite domain (HD), the inhibitory J domain (J_i), the C-terminal PEST rich region and the nuclear localization signal (NLS).
- B Binding efficiencies of increasing amounts (0-4 pmol) of the referred GST fusions to Ydj1 (1 pmol). Luciferase (luc) and P6, a selected Ydj1-target peptide, were used as references. Mean relative bound levels (N=3) and standard deviations are plotted.
- C Binding parameters of Ydj1 to the referred GST fusions in assays as in panel B. A simultaneous mode of binding was assumed for fitting the Hill equation, $y = x^n / (T^n + x^n)$. Obtained parameters and the resulting dissociation constant ($K_d = T^n$) are shown.

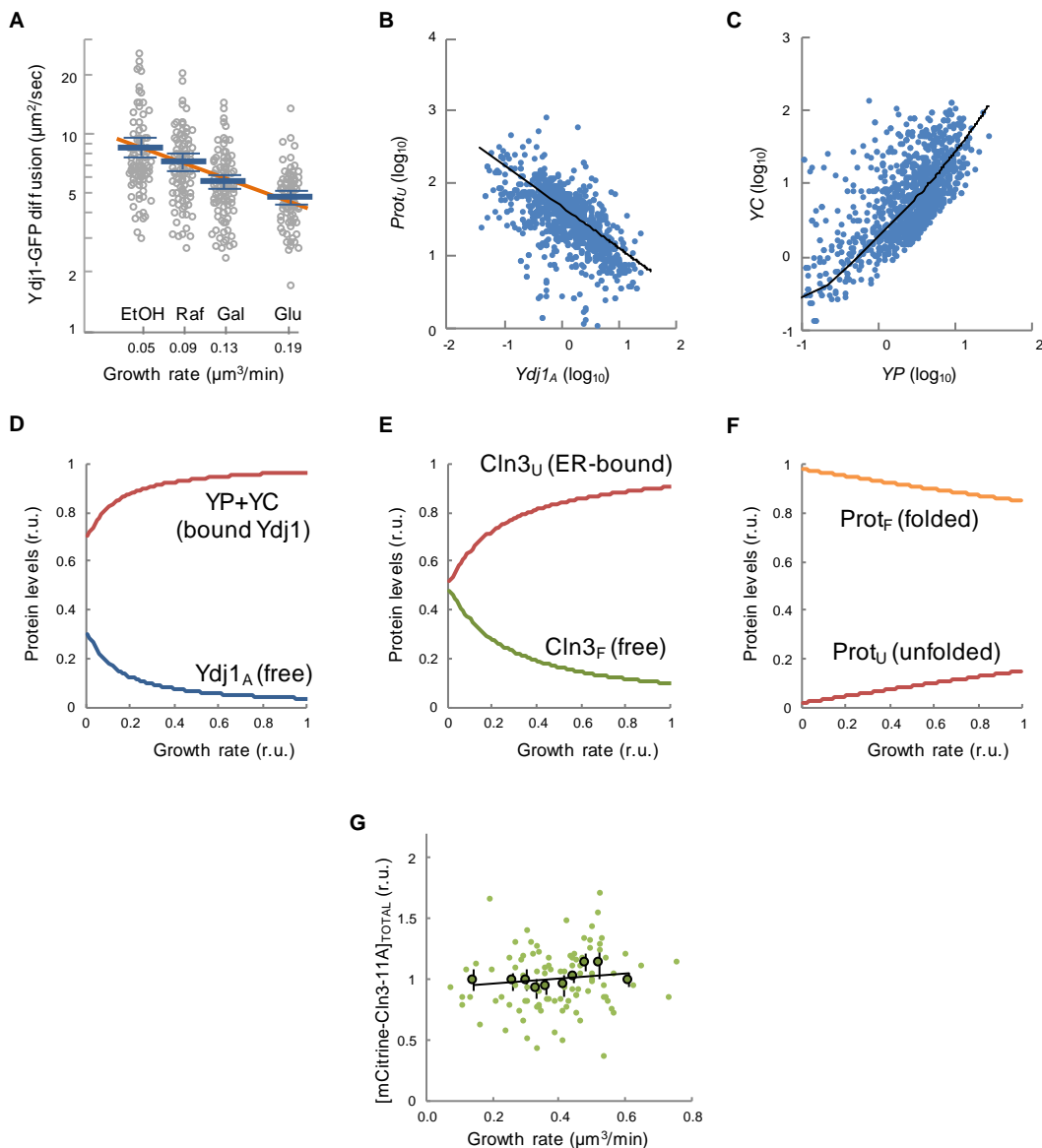


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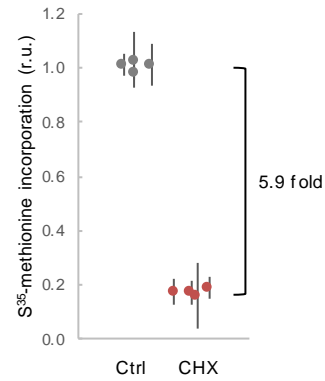
Figure EV5. Mobility of GFP-fusion proteins as a reporter of chaperone availability.

A-C Yeast cells expressing the indicated GFP fusions were analyzed by confocal microscopy to quantify intracellular mobility of Ssa1 and Ydj1 chaperones in the presence or absence of AZC. Since AZC-containing proteins accumulate with chaperones into disperse cellular aggregates (Escusa-Toret *et al*, 2013), FLIP was used to include both soluble and aggregated forms of these chaperones in the analysis. Representative fluorescence decay curves of individual cells are plotted.

D Individual protein mobility values ($N > 25$) of Ssa1- and Ydj1-GFP fusions obtained by FLIP before (-) or 15 min after adding AZC (+) are plotted. Mean values (thick lines) and confidence limits for the mean ($\alpha = 0.05$, thin lines) are also shown.



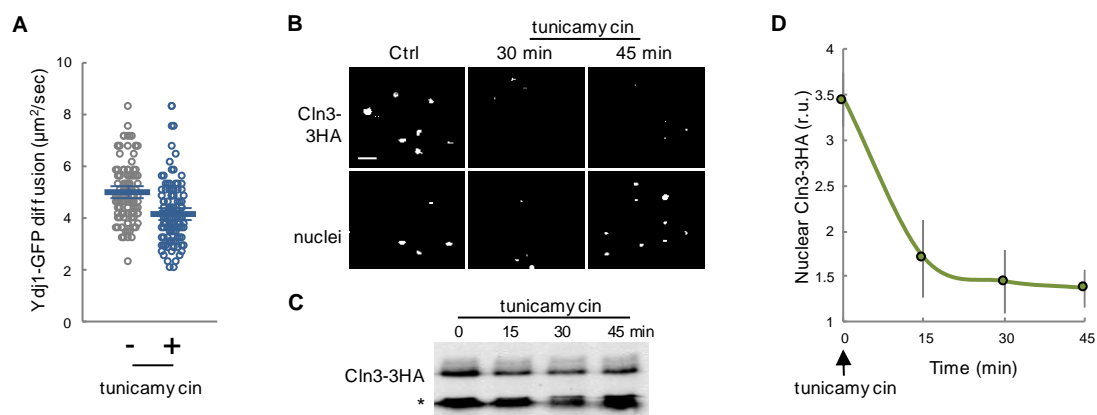
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 894 **Figure EV6. Ydj1-GFP mobility as a function of growth rate and correlation of state variables.**
 895 A Ydj1-GFP diffusion assayed by FCS in cells growing at different population growth rates in the indicated carbon
 896 sources. Individual diffusion coefficients, mean values (N=90, thick blue lines), confidence limits for the mean
 897 ($\alpha=0.05$, thin lines), and a linear fit (thick orange line) are plotted.
 898 B-C Covariation plots of $Prot_U$ vs $Ydj1_A$ (C), and YC vs YP (D) are shown. Values were obtained from parameters sets
 899 in Fig 3B and plotted in log space with the corresponding regression lines.
 900 D-F Prediction of main variables of the model as a function of growth rate. Parameter set 3114 was used to
 901 simulate relative levels of protein-bound (YC and YP) and available ($Ydj1_A$) chaperone (D), unfolded ER-bound
 902 ($Cln3_U$) and free folded ($Cln3_F$) G1 cyclin (E), and all other unfolded ($Prot_U$) and folded ($Prot_F$) proteins (F).
 903 G Cells (N=100) were analyzed to obtain the mean cellular concentration of mCitrine-Cln3-11A during G1. Single-
 904 cell (small circles) or binned data (large circles, 10 cells/bin) by growth rate are plotted. Confidence limits
 905 ($\alpha=0.05$) and a linear regression line for binned data are also plotted.
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Figure EV7. Protein synthesis effects by CHX at a sublethal dose.

Protein synthesis as measured by S^{35} -methionine incorporation in live cells in the absence or presence of 0.2 $\mu\text{g/ml}$ CHX. Relative mean values (circles) of triplicate measurements from independent cell batches ($N=4$) and confidence limits for the mean ($\alpha=0.05$, thin lines) are plotted.



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917 **Figure EV8. Effects of ER stress on Ydj1-GFP mobility and Cln3-3HA nuclear levels.**
918 A Yeast cells expressing Ydj1-GFP were analyzed by FCS 30 min after adding tunicamycin to 1 $\mu\text{g}/\text{ml}$. Individual
919 protein diffusion coefficients are plotted ($N>20$). Mean values (thick lines) and confidence limits for the mean
920 ($\alpha=0.05$, thin lines) are also shown.
921 B Immunofluorescence of Cln3-3HA in late-G1 cells arrested with α factor 30 min after 1 $\mu\text{g}/\text{ml}$ tunicamycin
922 addition. Bottom: Cln3-3HA levels by immunoblotting at different times in the presence of tunicamycin. A cross-
923 reacting band is shown as loading control.
924 C Nuclear levels of Cln3-3HA quantified from cells during treatment with tunicamycin as in panel B. Relative
925 mean values ($N>200$) and confidence limits ($\alpha=0.05$, thin horizontal lines) for the mean are shown.
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927 **Supplementary Table 1. Yeast strains and plasmids.**

Yeast strains	
CML128 (<i>MATa leu2-3,112 ura3-52 trp1-1 his4-1 can'</i>)	Gallego <i>et al</i> , 1997
CML203 (<i>CLN3-3HA::GEN</i>)	Gallego <i>et al</i> , 1997
CYC038 (<i>cln3::GEN</i>)	This study
CYC216 (<i>CDC28-sGFP::GEN tTA::LEU2</i>)	Wang <i>et al</i> , 2004
CYC228 (<i>CDC28-sGFP::GEN cln3::LEU2</i>)	Wang <i>et al</i> , 2004
MAG261 (<i>YDJ1-sGFP-FS::HIS3</i>)	This study
MAG676 (<i>SSA1-sGFP::HIS3</i>)	This study
MAG713 (<i>whi7::GEN</i>)	This study
MAG716 (<i>cln3::GEN whi5::NAT stb1::HYG</i>)	This study
MAG1086 (<i>CDC28-sGFP::GEN GAL4-ER-VP16::URA3</i>)	This study
MAG1092 (<i>CDC28-sGFP::GEN WHI5-mCherry::HYG</i>)	This study
MAG1512 (<i>TEF1_p-mCherry::NAT</i>)	This study
MAG1533 (<i>CDC28-sGFP::GEN ydj1::NAT</i>)	This study
MAG1911 (<i>TEF1_p-mCherry::NAT SSA1-sGFP::GEN</i>)	This study
MAG1913 (<i>TEF1_p-mCherry::NAT CDC48-sGFP::GEN</i>)	This study
MAG1919 (<i>TEF1_p-mCherry::NAT HSC82-sGFP::GEN</i>)	This study
KSY083-5 (<i>mCitrine-CLN3-11A::NAT</i>)	Schmoller <i>et al</i> , 2015
MAG1306 (<i>mCitrine-CLN3-11A::NAT ydj1::GEN</i>)	This study
MAG1334 (<i>mCitrine-CLN3-11A::NAT HTB2-mCherry::HYG</i>)	This study
Plasmids	
pGEX-KG (<i>tac_p-GST</i>)	ATCC77103
pMAG85 (<i>tac_p-GST-CLN3^{1-75aa}</i>)	This study
pMAG87 (<i>tac_p-GST-CLN3^{70-220aa}</i>)	This study
pMAG89 (<i>tac_p-GST-CLN3^{215-320aa}</i>)	This study
pMAG91 (<i>tac_p-GST-CLN3^{315-420aa}</i>)	This study
pMAG93 (<i>tac_p-GST-CLN3^{415-580aa}</i>)	This study
pMAG155 (<i>tac_p-GST-luc</i>)	This study
pMAG157 (<i>tac_p-GST-P6</i>)	This study
pMAG144 (<i>ARS-CEN URA3 HSC82 CDC37</i>)	This study
pMAG146 (<i>ARS-CEN LEU2 SSA1 YDJ1</i>)	This study
pMAG149 (<i>ARS-CEN TRP1 CDC48 UFD1 NPL4</i>)	This study
pMAG438 (<i>ARS-CEN 2xTEL URA3 TRP1 HSC82 CDC37 SSA1 YDJ1 CDC48 UFD1 NPL4</i>)	This study
pMAG469 (<i>ARS-CEN LEU2 GAL1_p-SSA1 GAL10_p-YDJ1</i>)	This study
pMAG1228 (<i>ARS-CEN URA3 TEF1_p-sGFP</i>)	This study
pMAG1915 (<i>ARS-CEN LEU2 SSA1-sGFP</i>)	This study
pMAG1917 (<i>ARS-CEN TRP1 CDC48-sGFP</i>)	This study
pMAG1920 (<i>ARS-CEN URA3 HSC82-sGFP</i>)	This study

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