# Signal integration and information transfer in an allosterically regulated network

- <sup>3</sup> Erin M. Shockley<sup>a</sup>, Carol A. Rouzer<sup>a</sup>, Lawrence J. Marnett<sup>a</sup>, Eric J.
- <sup>4</sup> Deeds<sup>c,d</sup>, and Carlos F. Lopez<sup>a,b,1</sup>
- <sup>5</sup> <sup>a</sup>Department of Biochemistry, Vanderbilt University, Nashville, TN 37212
- <sup>b</sup>Department of Biomedical Informatics, Vanderbilt University Medical Center, Nashville,
   TN 37212
- <sup>8</sup> <sup>c</sup>Center for Computational Biology, University of Kansas, Lawrence, KS 66047
- <sup>9</sup> <sup>d</sup>Department of Molecular Biosciences, University of Kansas, Lawrence, KS, 66047

# • ABSTRACT

A biological reaction network may serve multiple purposes, processing more than one input and impacting downstream processes via more than one output. These networks operate in a dynamic cellular environment in which the levels of network components may change within cells and across cells. Recent evidence suggests that protein concentration variability could explain cell fate decisions. However, systems with multiple inputs, multiple outputs, and changing input concentrations have not been studied in detail due to their complexity. Here, we take a systems biochemistry approach, combining physiochemical modeling and information theory, to investigate how cyclooxygenase-2 (COX-2) processes simultaneous input signals within a complex interaction network. We find that changes in input levels affect the amount of information transmitted by the network, as does the correlation between those inputs. This, and the allosteric regulation of COX-2 by its substrates, allows it to act as a signal integrator that is most sensitive to changes in relative input levels.

Keywords: network dynamics, allosteric regulation, systems biochemistry, Information theory, Cyclooxygenase-2

Many biological signaling networks process multiple inputs and yield multiple outputs. Examples 11 of multiple-input multiple-output (MIMO) biochemical systems include the mitogen-activated protein 12 kinase (MAPK) network, which can respond to numerous ligands and yield a range of outputs including 13 proliferation and differentiation (Santos et al., 2007); the NF- $\kappa$ B pathway, which triggers pro- and anti-14 inflammatory responses to a variety of ligands (Lawrence, 2009); and myriad metabolic networks, which 15 respond to multiple substrates and allosteric regulators by producing energy and the building blocks of 16 cellular components (Lorendeau et al., 2015). Recent work (Adlung et al., 2017; Spencer et al., 2009; Shi 17 et al., 2016; Huang, 2009; Waite et al., 2016; Mitchell et al., 2018; Chen et al., 2012) has highlighted 18 the fact that modulation of input concentrations in intracellular networks can yield markedly different 19 outcomes. Despite this clear indication that MIMO systems are crucial to biological processes, few reports 20 exist to date to explain how multiple inputs modulate reaction flux and information flow in a network to 21 allow signal processing with a range of adaptive outputs. 22

To explore the properties of MIMO systems in biology, we chose to study the dynamics of cyclooxygenase-23 2 (COX-2), a key enzyme that controls the balance between pro- and anti-inflammatory signals in mam-24 malian organisms. COX-2 lies at the interface of the eicosanoid and endocannabinoid signaling pathways 25 (Alhouayek and Muccioli, 2014; Rouzer and Marnett, 2011) and is itself the target of the widely used 26 nonsteroidal anti-inflammatory drugs (NSAIDs). Although COX-2 is a structural homodimer, it behaves 27 as a heterodimer. One subunit in the dimer harbors the catalytically active site, while the other subunit 28 contains an allosteric site that modulates the overall activity of the enzyme (Dong et al., 2013, 2011; 29 Kulmacz and Lands, 1984). An array of substrates, inhibitors, and allosteric modulators can bind to, 30 and thus compete for, either site, giving rise to highly complex reaction kinetics (Kudalkar et al., 2015; 31 Kulmacz and Lands, 1985; Mitchener et al., 2015; Rimon et al., 2010; Yuan et al., 2009; Dong et al., 32 2016a). The various products from COX-2 activity drive multiple downstream pro- and anti-inflammatory 33

processes that lead to diverse cellular fates including stress responses and apoptosis (Funk, 2001; Rouzer
 and Marnett, 2003; Smith et al., 2000).

<sup>36</sup> It is clear that COX-2 orchestrates a complex interplay between a variety of substrates (the enzyme

*inputs*), various allosteric regulators, and the concentration of downstream products (the enzyme *outputs*)

that control processes such as inflammation (Funk, 2001; Rouzer and Marnett, 2003; Smith et al., 2000).

<sup>39</sup> Previously, most studies of COX-2 function have used simplified models based on Michaelis-Menten

40 kinetics (Briggs and Haldane, 1925). Not surprisingly, these approaches have proved insufficient to

41 capture the rich complexity of the COX-2 network of reactants, intermediates and products (Mitchener

et al., 2015). We posit that a systems approach to understand COX-2 mechanism will improve inhibitor
 design to achieve desired outcomes in clinical settings.

COX-2 activity also represents an ideal model system to study the detailed dynamics of a biological 44 MIMO system. As a single enzyme, it is sufficiently simple to allow for the construction, simulation and 45 parameterization of a detailed systems biochemistry model that can capture all of the relevant transitions 46 between intermediates and products. Nonetheless, it is sufficiently complex that it represents a non-trivial 47 example of how multiple inputs lead to multiple outputs in a physiological context. We focus our study 48 on the allosteric regulation network of COX-2 by two important substrates, arachidonic acid (AA) and 49 2-arachidonoylglycerol (2-AG), which generate unusual dynamics in the COX-2 network when both are 50 present (Mitchener et al., 2015). Levels of AA and 2-AG also vary widely in vivo (Seibert et al., 1997; 51

<sup>52</sup> Monjazeb, 2006; Sugiura et al., 2006), and it is unclear how such variation would influence COX-2 signal <sup>53</sup> processing.

In this work, we analyze the execution mechanism of a biochemical reaction network with multiple 54 inputs. Our work explains how a MIMO system integrates information on the concentration and nature 55 of its substrates to yield potentially different outputs. In previous work, we developed a detailed model 56 of the COX-2 reaction network that comprises all possible biochemical enzyme states dictated by AA 57 and 2-AG occupancy of the allosteric or active sites, and all the kinetic transitions between these states 58 (Mitchener et al., 2015). The reaction rate parameters for the kinetic system were determined using a 59 Bayesian inference methodology (Shockley et al., 2017) to fit the model to experimental data on COX-2 60 kinetics. This Bayesian approach produced an ensemble of model parameters that represent the uncertainty 61 in the kinetic rates given the available data and restricts our analysis to plausible kinetic states of the 62 network (Mitchener et al., 2015; Shockley et al., 2017). To explore the COX-2 MIMO signal processing 63 mechanism, we first employed a graph-theoretic approach to enumerate all possible paths a substrate 64 can take from reactant to product molecule. We found that changing the concentration of the inputs 65 modulates not only the most dominant path that is taken by the system, but also the diversity of the paths 66 the system employs. We also used an information-theoretic approach (Shannon, 1948) to understand the 67 flow of information between network inputs, various intermediates, and the product outputs. This analysis 68 reveals that competition between AA and 2-AG for the allosteric and active site generates highly complex 69 70 concentration-dependence curves for COX-2 that are context-sensitive. In addition to providing insight into how COX-2 functions as a hub for the processing of inflammatory signals, our work suggests that 71 our systems biochemistry framework provides useful information relevant to the study of other MIMO 72 biological systems. This work also demonstrates that the extreme context-sensitivity of MIMO systems 73 must be considered when attempting to modulate their behavior through targeted interventions. 74

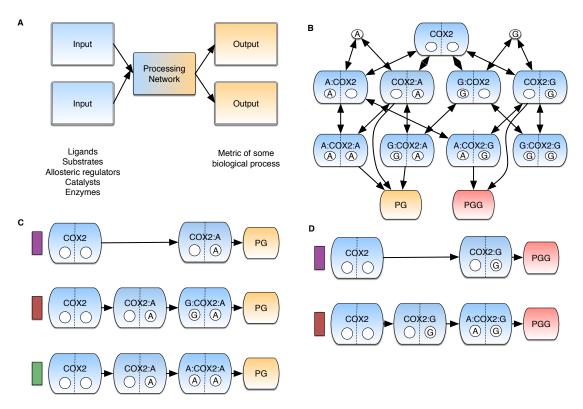
## 75 **RESULTS**

#### 76 A Mathematical Model of COX-2 Allostery and Catalysis

We built the COX-2 Reaction Model (CORM) (Fig. 1B) to understand how substrate-dependent allosteric 77 regulation affects COX-2 catalytic rates (Mitchener et al., 2015). Here, we employ this model to study 78 how multiple signals are processed in the context of a complex chemical reaction network, given a 79 range of substrate concentrations and input correlations. Briefly, CORM encodes the reaction kinetics 80 between COX-2 and two of its substrates: the fatty acid arachidonic acid (AA) and the endocannabinoid 81 2-arachidonoylglycerol (2-AG). Both AA and 2-AG can bind at the catalytic and/or allosteric site on 82 COX-2 with different affinities. At the catalytic site, AA is turned over to prostaglandin (PG) while 2-AG 83 produces prostaglandin-glycerol (PG-G). Binding of either molecule at the allosteric site modulates the 84 rate of catalysis (Mitchener et al., 2015). Although CORM includes only two substrates, the MIMO nature 85

of COX-2 kinetics results in a complex network (Fig. 1B). CORM has been calibrated to experimental

data using PyDREAM, a Bayesian parameter inference framework, to obtain the probabilistic likelihood



**Figure 1.** Network interactions within CORM. (*A*) The Multi-input Multi-output motif in a biological context. (*B*) The COX-2 Reaction Model (CORM) represents the network of interactions in the COX-2 system. The diagram depicts the possible biochemical states that the COX-2 enzyme (blue lozenges) can adopt through its allosteric (lower left circle) and catalytic (lower right circle) subunits, respectively. AA bound in either site is indicated with **A** and 2-AG with **G** within the circle. AA is turned over to produce prostaglandin (PG) and 2-AG is turned over to produce prostaglandin-glycerol (PG-G). Double-headed arrows indicate reversible reactions while single-headed arrows indicate irreversible reactions. Credible intervals for all fitted parameters are included in SI. (*C*) Dominant PG Production Paths in CORM. Colors correspond to path fluxes in Fig. 2*A*. (*D*) Dominant PG-G Production Paths in CORM. Colors correspond to path fluxes in Fig. 2*B*.

of parameters given experimental data, and information about the uncertainty in those parameter values

89 (Shockley et al., 2017). CORM is encoded in Python using PySB, which provides a flexible tool to query

<sup>90</sup> the mixture of complexes present in the system at any time point given starting concentrations. Many

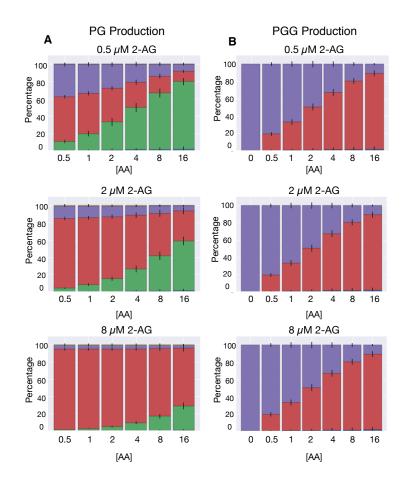
of these complexes would be costly or impossible to measure experimentally. Employing the Python

environment also facilitated the sophisticated analyses we present in this work (Lopez et al., 2013).

#### Substrate-Dependent Reaction Fluxes in Signal Execution

We first explored the net flow of reaction flux through the network using a graph theoretic approach to 94 calculate all possible paths between the unbound enzyme and each final product. Briefly, we evaluated 95 the system of ordinary differential equations (ODEs) in CORM at time intervals to extract the integrated 96 reaction flux at a given time point for each chemical reaction. We then built paths from product to reactant 97 following the reactions with net forward flux. Finally, we calculated the total chemical flux that passed 98 through a given path and used this as a measure of the probability of product formation via that path; 99 a detailed description of this procedure is given in SI Methods and Fig. S1. All fluxes were calculated 100 for the first ten seconds of catalysis after mixture with the substrates, a time chosen to match previous 101 experimental work (Mitchener et al., 2015). Path flux distributions were calculated for an ensemble of 102 calibrated parameter values to quantify path flux uncertainty arising from parameter uncertainty. 103 Our analysis indicates that there are six possible paths to produce PG (Fig. S2) and four possible paths 104

<sup>105</sup> to produce PG-G (Fig. S3) for all evaluated substrate concentration combinations. However, not all paths



**Figure 2.** Concentration-dependent PG and PG-G production paths. (*A*) Dominant Reaction paths for PG Production Vary with AA and 2-AG Concentration. Each individual plot depicts the amount of flux through each path in 1*C* for a given concentration of 2-AG across varying concentrations of AA. Colors correspond to labeled paths in Fig. 1*B*. The error bars in each plot indicates the flux variation resulting from inferred kinetic rates. (*B*) Dominant Mechanisms of PG-G Production Vary with AA Concentration. Each individual plot is at a given concentration of 2-AG. In all plots AA increases from left to right at concentrations of 0.5, 1, 2, 4, 8 and 16  $\mu$ M in *A* and 0, 0.5, 1, 2, 4, 8, and 16  $\mu$ M in *B*. Colors correspond to labeled paths in Fig. 1*C* The error bars in each plot indicates the flux variation from inferred kinetic rates.

exhibit significant reaction flux during catalysis across all the concentrations. This occurs because paths 106 in which binding of a species to the allosteric site precedes binding to the catalytic site are kinetically 107 disfavored in CORM. As shown in Fig. 1C and 1D, three paths dominate PG production and two paths 108 dominate PG-G production. The dominant PG-producing paths (Fig. 1C) include those with one or 109 two intermediates, and the allosteric site empty or occupied by AA or 2-AG. Our results show that the 110 dominant path is highly dependent on the substrate input concentrations. The presence of AA and 2-AG in 111 the allosteric site enhances the production of PG (Mitchener et al., 2015). The dominant PG-G-producing 112 paths include one or two intermediates (Fig. 1D) with the allosteric site empty or occupied by AA. The 113 presence of AA in this site reduces the rate of PG-G production Mitchener et al. (2015). Similar to PG 114 production, we also found that the flux through each dominant path for PG-G production is dependent on 115 substrate concentration (Fig. 2). 116

In the absence of 2-AG and at low  $(0.5 \ \mu M)$  AA, PG is produced without allosteric modulation (Fig. 2*A*, purple; purple-labeled path in Figure 1C, top); as the concentration of AA increases, the proportion of PG produced with AA as an allosteric modulator also increases (Fig. 2*A*, green). When 2-AG is added to the system, PG production shifts to using 2-AG as an allosteric modulator (Fig. 2*A*, red), with this path favored to a greater extent as the concentration of 2-AG increases (Fig. 2*A*, lower plots). Even in

the absence of 2-AG, about 20% of PG is produced by AA-modulated COX-2, and once even a small amount of 2-AG (0.5  $\mu$ M) is added to the system, more than half of PG production occurs via a 2-AG or

AA allosterically modulated path. In the presence of high concentrations of either modulator, as much as

<sup>125</sup> 90% of PG is produced via an allosterically modulated path.

Because 2-AG and COX-2 display substrate-dependent inhibition (Mitchener et al., 2015), the 126 production of PG-G occurs via fewer paths than are available to PG. In the absence of AA, all PG-G 127 produced is generated in the absence of an allosteric modulator (Fig. 2B, purple), because the intermediate 128 with 2-AG bound in both catalytic and allosteric sites is not turned over. As AA is added to the system, 129 the proportion of PG-G produced by the AA-modulated pathway (Fig. 2B, red) increases. Thus, in the 130 131 range of tested substrate concentrations, the dominant mechanism of PG-G production depends entirely on the amount of AA present in the system. Compared to PG, a smaller proportion of PG-G produced 132 by the system results from an allosterically regulated pathway because PG-G is only created via the 133 AA-modulated species or the allosterically unbound species. Nevertheless, at high concentrations of AA, 134 again as much as 90% of PG-G is produced by AA-modulated COX-2. For paths containing a species 135 bound in the allosteric site, binding at the catalytic site followed by binding at the allosteric site is the 136 favored mechanism. 137

We note that at any given substrate concentration, the uncertainty arising from the calibrated kinetic parameter distributions never exceeds a 20% change in the percentage of product produced by a given path (Fig. S4-S8). We find that changes in substrate levels and their relative ratios have a much larger effect on the dominant reaction paths than changes in kinetic rates within the calibrated CORM parameter distributions. Overall, these findings suggest that variation of substrate concentrations in physiologicallyrelevant ranges has a significant impact on COX-2's mechanism of catalysis.

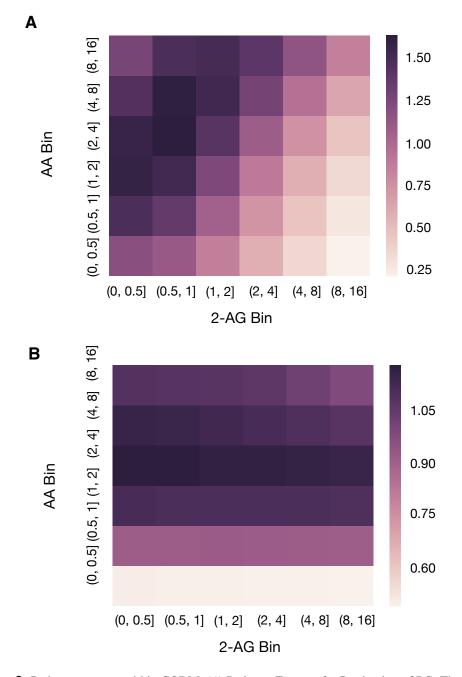
#### 144 Pathway Entropy is Dynamic Across Input Concentrations

Calculating the flux through each path allows us to obtain information about the preferred sequences of reactions that the system executes while processing AA and 2-AG. However, these measurements do not provide an estimate of how chemical traffic (i.e. the flow of chemical signals in the network) is distributed throughout the network. To explore the distribution of biochemical network traffic, we introduce the *pathway entropy* to quantify the degree to which COX-2 utilizes multiple paths at different concentrations of substrates. Our definition of entropy, originally introduced by Claude Shannon (Shannon, 1948) provides a measure of the uncertainty in a probability distribution across states as follows:

$$H = -\sum_{x=1}^{n} P(x_i) \log_2 P(x_i)$$
(1)

where *H* is entropy and  $P(x_i)$  is the probability of any state  $x_i$ . To determine the degree of uncertainty associated with product production (the pathway entropy), we considered each pathway as a state and use the fraction of flux that a given pathway contributes to the product as a measure for the probability of that state. This analysis yields a measure of how evenly distributed production is across possible paths. In general, evenly distributed fluxes across paths in a network would maximize pathway entropy for a multi-path system.

Since the dominant paths vary with substrate concentration (Fig. 2), we would expect that pathway 151 entropy would also vary. In Fig. 3 we present the pathway entropy dependence on input concentration for 152 PG (Fig. 3A) and PG-G (Fig. 3B). The pathway entropy for PG production is highest at intermediate levels 153 of AA and low levels of 2-AG, while the pathway entropy is highest for PG-G production at intermediate 154 levels of AA and any level of 2-AG. These maxima correspond to states where the reaction flux is most 155 spread across the possible paths from reactant to product (see Fig. 2A, top plot, center, and Fig. 2B, 156 top plot, center). In contrast, in the lowest entropy states - low AA and high 2-AG for PG (Fig. 2A, 157 bottom plot, far left) and low AA across the entire 2-AG spectrum for PG-G (Fig. 2B, bottom row), flux is 158 concentrated in a single or a few paths. Reaction flow is thus highly distributed in some conditions yet 159 highly concentrated in one path in other conditions. This finding suggests that MIMO networks utilize 160 multiple execution modes across input concentrations. It also suggests that approaches to modulate or 161 inhibit network activity, which focus on disrupting one or more of these paths, may need to be tailored 162 163 to specific conditions. These behaviors could have physiological relevance. For example, high-entropy conditions with highly redundant path fluxes may require multiple targets for inhibition compared to a 164 condition with low entropy. 165



**Figure 3.** Pathway entropy within CORM. (*A*) Pathway Entropy for Production of PG. The intensity indicates the pathway entropy in units of bits. (*B*) Pathway Entropy for Production of PG-G. Units are the same as in *A*.

#### 166 Input Output Behavior in CORM

The above findings on pathway entropy suggest a complex relationship between input concentrations, 167 reaction intermediates, and product concentration in CORM. To understand these relationships, we next 168 considered concentration-dependence curves derived from simulations using a fixed set of CORM kinetic 169 parameters in which PG was calculated at increasing AA concentrations in the presence of random 170 quantities of 2-AG (Fig. 4A) or PG-G was calculated at increasing 2-AG concentrations in the presence of 171 random quantities of AA (Fig. 4B). Each data point was taken at steady-state (10 seconds) for consistency 172 with experiments and previous work. Note that the presence of both substrates results in competitive 173 inhibition with suppression of product formation from either one. Thus, the highest levels of output in 174 175 each case occur when the concentration of the opposing substrate is low. These levels are similar for PG and PG-G because COX-2 utilizes the two substrates with similar catalytic efficiencies when they are 176 present individually. As the concentration of the opposing substrate increases, competitive inhibition 177 is partially balanced by positive allosteric modulation in the case of the conversion of AA to PG, but 178 exacerbated by negative allosteric modulation in the case of the conversion of 2-AG to PG-G. Therefore, 179 the suppression of PG-G formation is greater than that of AA formation as seen in the lower plateau level 180 achieved in (Fig. 4B). In addition, the range of inputs over which the output varies depends significantly on 181 which input/output pair is chosen (note the difference in that range in Fig. 4A,B). Clearly, variation of both 182 inputs (e.g. changing AA in addition to changing 2-AG in Fig. 4A), results in significant variation in the 183 outputs. Thus, while our simulations are deterministic, introducing uncertainty in the AA concentration 184 generates a type of "extrinsic noise" in the relationship between 2-AG and PG-G (Fig. 4B), and vice versa 185 for the impact of 2-AG on the relationship between AA and PG, Fig. 4A). This noise represents allosteric 186 modulation in the network due to varying input concentrations. 187

#### **Channel Capacity from Substrates to Products**

To better understand how this output variation, combined with the shape of the concentration-dependence curves, influences the COX-2 reaction network, we applied an additional concept from information theory to measure dependence between inputs and outputs, namely the Mutual Information:

$$I(X;Y) = \sum_{X} \sum_{Y} P(x,y) \log_2 \frac{P(x,y)}{P(x)P(y)}$$

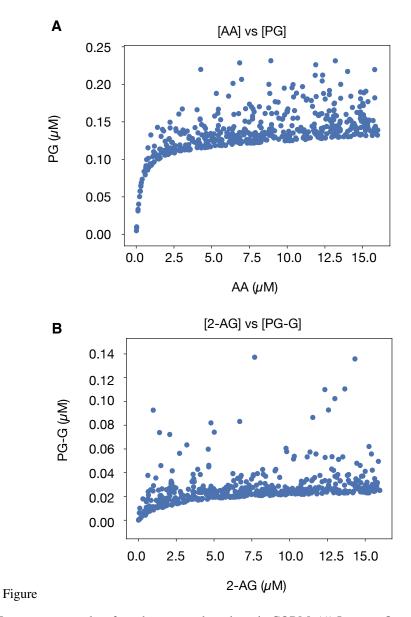
$$\tag{2}$$

where *X* represents a given signal and *Y* the response to that signal (Shannon, 1948). Mutual information quantifies the degree to which one variable provides information about a second variable. Equivalently, it is a measure of how knowledge about one variable decreases uncertainty in the value of a second variable. For biological systems, quantifying mutual information is challenging because the input distribution is generally unknown. Previous work (Cheong et al., 2011; Selimkhanov et al., 2014; Suderman et al., 2017) has focused on estimating the "channel capacity," which is the maximum information attainable across all possible input distributions:

$$C = \sup_{p_x(x)} I(X:Y) \tag{3}$$

<sup>189</sup> Note that any practical calculation provides a lower bound estimate for the channel capacity C, since only <sup>190</sup> a finite set of input distributions is used to estimate I (Suderman et al., 2017). We calculated channel <sup>191</sup> capacities using the approach and software published in Suderman *et al.* (Suderman et al., 2017), which is <sup>192</sup> similar to that used in Cheong *et al.* (Cheong et al., 2011).

We applied this estimate to two different sets of simulations. In the first set of simulations, we 193 considered a case where AA and 2-AG are perfectly correlated with each other; to do this, we sampled 194 the AA concentration from a uniform distribution on  $[0, 16 \,\mu M]$  and set the 2-AG concentration to 195 be exactly the same. In the second set, we *independently* sampled the input AA and 2-AG substrate 196 concentrations from a uniform distribution on the interval  $[0, 16 \,\mu M]$ . In each case, we sampled a total of 197 500 distinct input conditions and ran CORM simulations to 10s to agree with experiments and previous 198 work (Mitchener et al., 2015). The channel capacity was then estimated between the two different inputs 199 (either AA or 2-AG) and every possible intermediate and product. The maximum theoretical channel 200 capacity,  $\log_2(500) \approx 9$  bits, would be obtained if each of the 500 inputs yielded a distinct response. We 201 repeated the channel capacity calculation for the top 5000 most probable parameter vectors from the 202 calibrated parameter ensemble. This then allowed us to quantify the effect of kinetic parameter variation 203 on channel capacities in the system. In total the analysis required approximately 1.5M CPU hours. An 204



**Figure 4.** Input vs output plots for substrates and products in CORM. (*A*) Input vs Output plots for AA to PG. 2-AG varies randomly. All concentrations are measured at steady-state (10 seconds). (*B*) Input vs Output plots for 2-AG to PG-G. AA varies randomly. All concentrations are measured at steady-state (10 seconds).

- example of input data used for calculating channel capacities from AA to PG and 2-AG to PG-G for a
- single parameter set is shown in Fig. 4. Greater detail is provided in the SI Methods.

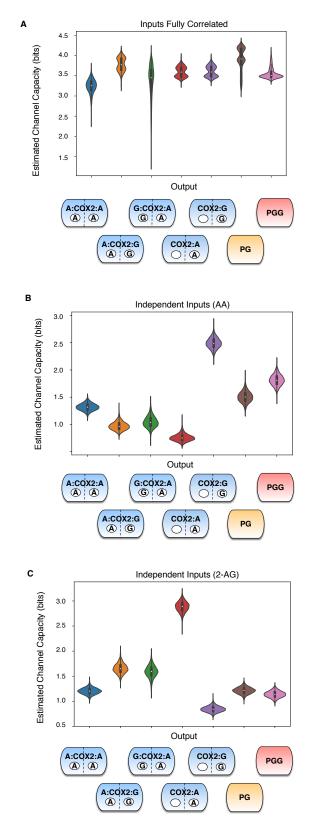
### 207 COX-2 Integrates Information from Both AA and 2-AG

For ease of visualization, we estimated kernel densities of channel capacities given variation in calibrated 208 kinetic parameters as shown in the violin plots in Fig. 5. In these plots, the data are represented by a 200 central box plot that provides the mean, interquartile range and 95% credible interval, and the surrounding 210 shape depicts the probability distribution, with wider regions indicating a higher probability. Because the 211 input-output relationship in these simulations is deterministic, deviations from the theoretical maximum 212 ( $\approx$ 9 bits) arise from the two phenomena described above: either changes in the input do not really lead to 213 significant changes in the output (*i.e.* the "flat" part of the concentration-dependence curves in Fig. 4) or 214 the independent variation in one of the substrates generates variation in the output that is not due to the 215 input being considered (*i.e.* the apparent noise in Fig. 4). 216

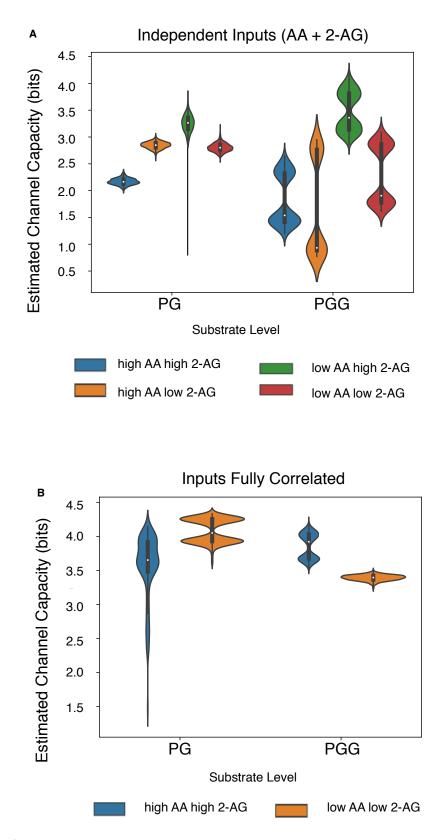
From Fig. 5, it is clear that the combination of these effects significantly reduces the observed channel 217 capacities from the theoretical maximum. The highest observed value for any of the input/output pairs 218 (AA to PG, 2-AG to PG-G, etc.) is at most half of the theoretical maximum (less than 4.5 bits). When input 219 values are perfectly correlated ([AA] = [2-AG]), Fig. 5A, the channel capacity between the (correlated) 220 inputs and the outputs is between 3 and 4.5 bits (depending on the parameters), indicating that, while not 221 perfect, the concentration-dependence curves allow for high levels of information flow between inputs 222 and outputs. It is interesting to note that the uncertainty in the kinetic parameters leads to some variation 223 in the calculated channel capacities; since the inputs here are correlated, this variation is due to changes 224 in the shape of the concentration-dependence curves between data sets. Many channel capacities in the 225 correlated case are bimodal, suggesting that two specific concentration-dependent curve shapes are most 226 likely. 227

When the inputs are varied independently, channel capacity values decrease even further (Fig. 5B228 and C). The channel capacity between AA and PG or PG-G is generally less than 2 bits, and the channel 229 capacity between 2-AG and those outputs is generally less than 1.5 bits. This could occur for two reasons. 230 First, a lack of correlation could result in less entropy in the response (*i.e.* less uncertainty in the value of 231 the product). Since the mutual information is limited by the response entropy (eq. 2, (Shannon, 1948; 232 Cheong et al., 2011; Suderman et al., 2017)), this would cause a decrease in the mutual information. 233 However, if the response entropy remains constant when there is no correlation between inputs, then 234 mutual information can only decrease if information transfer through the network is less efficient. As 235 shown in Fig. S9, the response entropy does not differ between the independent and correlated cases, 236 indicating that independent variation in one of the inputs while the other input is known has a large effect 237 on the output. In other words, COX-2 is truly an integrator of these signals, since accurate determination 238 of the substrate concentrations given the output is considerably more difficult if the two substrates are 230 independently varied. 240

Since perfect correlation and complete independence represent only the two extremes of the rela-241 tionship between AA and 2-AG concentration, we also investigated the behavior of the system when 242 the inputs exhibit moderate correlation (Pearson correlation coefficient = 0.5), and when the inputs are 243 consistently present in a 2-to-1 AA-to-2-AG ratio (Fig. S10 and Fig. S11). The behavior when input 244 ratios were fixed was similar to that for the correlated values (when the input levels were fixed equal to 245 each other); channel capacities were again higher than in the independent case and the effect of kinetic 246 parameter variation on channel capacity was higher. When the inputs are moderately correlated, the 247 system is still able to obtain high channel capacities for some kinetic parameter sets, although the overall 248 distribution of channel capacities shifts to lower values compared to when input correlation is perfect, 249 further confirming COX-2 input integration. 250



**Figure 5.** Estimated channel capacities from substrates to intermediates or products in CORM. (*A*) Estimated Channel Capacities from Input to intermediates and final products within CORM when levels of AA and 2-AG are strongly correlated (Pearson correlation coefficient = 1). Distributions in the channel capacities arise from uncertainty in the kinetic parameter values after model calibration.(*B*) Estimated Channel Capacities from AA to intermediates and final products within CORM when AA and 2-AG are varied independently. Distributions in the channel capacities arise from uncertainty in the kinetic parameter values after model calibration.(*C*) Estimated Channel Capacities from 2-AG to intermediates and final products within CORM when AA and 2-AG are varied independently. Distributions in the channel capacities from 2-AG to intermediates and final products within CORM when AA and 2-AG are varied independently. Distributions in the channel capacities from 2-AG to intermediates and final products within CORM when AA and 2-AG are varied independently. Distributions in the channel capacities from 2-AG to intermediates and final products within CORM when AA and 2-AG are varied independently. Distributions in the channel capacities arise from uncertainty in the kinetic parameter values after model calibration.



#### **Information Flow is Dictated by Substrate Concentration**

**Figure 6.** Effect of substrate level on estimated channel capacities between substrates and products in CORM. (*A*) Total Estimated Channel Capacity from AA and 2-AG combined to products across regions of substrate space. Distributions in the channel capacities arise from uncertainty in the kinetic parameter values after model calibration. (*B*) Estimated Channel Capacities from input to products when levels of AA and 2-AG are perfectly correlated across regions of substrate space. Distributions in the channel<sup>1</sup>/<sup>16</sup> capacities arise from uncertainty in the kinetic parameter values after model calibration.

We next tested whether the channel capacity between substrates and products varies with substrate level. 252 We binned the input data into four quadrants (high or low values of either substrate) and calculated the 253 channel capacity between inputs and outputs independently for each quadrant; input ranges were otherwise 254 identical to those used for the calculations described above. Low substrate values spanned 0-8  $\mu$ M and 255 high substrate values 8-16 $\mu$ M. Both independently varied inputs (Fig. 6A) and correlated inputs (Fig. 6B) 256 yielded estimated channel capacities that were significantly different between the different regions of 257 input space. In addition to differences in PG and PG-G channel capacity, we found that the distribution of 258 information that passed through different intermediates changed with substrate concentration (Fig. S13 259 and Fig. S14); certain paths to product had greater information transfer capacity at particular levels of 260 261 substrates. This echoes findings from our pathway analysis (Figs. 2 and 3), indicating that changes in substrate concentration result in significant changes in how the enzyme executes its catalytic mechanism. 262 Interestingly, we found no detectable correlation between the flux through a pathway and the mutual 263 information between an input and an intermediate in that path (Fig. S15 and Fig. S16). We leave further 264 investigation of the relationship between information transfer and actual physical reaction fluxes for future 265 work. 266

Splitting the input space into different quadrants also revealed significant variation between different parameter sets, with most distributions showing significant bimodality across parameters (Fig. 6). This suggests that both the shape of the concentration-dependence curves, and the impact of "extrinsic noise" due to variation of one substrate independent of another, varies across parameter sets. Since all of these parameter sets are equally consistent with experimental data (Mitchener et al., 2015), this suggests that multiple modes of information flow are available to the COX-2 reaction network without significant changes to the core functionality of the enzyme.

## 274 DISCUSSION

In vivo, COX-2, AA, and 2-AG concentrations vary across cells in different tissues (Seibert et al., 275 1997; Monjazeb, 2006; Sugiura et al., 2006). In most tissues, AA processed by COX-2 is released 276 from membrane phospholipids, predominantly through the action of cytosolic phospholipase A2 (Leslie, 277 2015). In some tissues, (particularly the brain) a major source of AA is hydrolysis of 2-AG (Ignatowska-278 Jankowska et al., 2014; Long et al., 2008). In turn, 2-AG is also sourced from membrane phospholipids; 279 through the sequential action of phospholipase C, which forms diacylglycerol (DAG), followed by 280 conversion of DAG to 2-AG by DAG lipase (Fezza et al., 2014). Both DAG lipase and cytosolic 281 phospholipase A2 are stimulated by increases in intracellular Ca<sup>2+</sup> (Leslie, 2015; Bisogno et al., 2003). 282 Thus, many stimuli (such as zymosan phagocytosis by macrophages (Rouzer and Marnett, 2005)) promote 283 the release of AA and 2-AG simultaneously, with concentrations of AA typically higher than those of 284 2-AG. Considering the precursor-product relationship between 2-AG and AA, however, it is conceivable 285 286 that in some cells, the levels of the two substrates may change inversely to one another, or that the level of one may change while the other remains constant. These considerations suggest that the system features 287 we find that vary with AA and 2-AG level (pathway entropy and information transfer capacity) are states 288 accessible by the true biological system with the attendant repercussions for information transfer within 289 that system. In addition, the postulated link between diet and the substrates available for COX-2 turnover 290 (Chen, 2010) suggests that the information transfer properties of the system could be modulated by fatty 291 acid intake. 292

COX-2 has significant regulatory flexibility: it is an allosteric protein, with multiple substrates and 293 multiple allosteric regulators, all of which can influence how COX-2 operates on its substrates in vivo. 294 The pathway analysis (Fig. 1B and 1C) suggests that COX-2 functions by first binding a substrate at 295 the catalytic site, followed by binding of an allosteric regulator. Allostery can be viewed as a shift 296 in the conformational free-energy landscape sampled by COX-2 through preferential binding of the 297 allosteric regulator to particular conformations (Lechtenberg et al., 2012; Nussinov and Tsai, 2013). From 298 this perspective, modulating the concentrations of allosteric regulators in the COX-2 system shifts the 299 conformational ensemble towards conformations favored by particular regulators. In the case of PG, 300 these conformations are more easily turned over to product than the unmodulated enzyme, while for 301 PG-G, the allosteric influence makes catalysis less energetically favorable (shifts the ensemble towards 302 conformations that are less active). This allows COX-2 to manage the balance between PG and PG-G 303 production in a more complex (and potentially farther-reaching) fashion than that provided by simple 304 competition between substrates. This added complexity suggests a physiological reason why the COX-2 305

system would integrate information from multiple inputs: by adding a second competitive input, the 306 system can access different responses than with a single input. Furthermore, the response dynamics 307 of COX-2 gain even greater complexity because its inputs act as allosteric modulators in addition to 308 substrates. The situation in vivo is likely far more complicated (and flexible) than considered here, as 309 COX-2 has potential substrates in addition to AA and 2-AG (Rouzer and Marnett, 2009), and some 310 nonsubstrate fatty acids that act as allosteric regulators (Dong et al., 2016b; Yuan et al., 2009; Dong et al., 311 2011, 2013, 2016a). In addition, many of the non-steroidal anti-inflammatory drugs that target COX-2 312 also may bind at either the catalytic or allosteric site. 313

One advantage of this complexity may be the significant robustness of this system to variation in 314 315 the kinetic parameters. The 5000 parameter sets we considered here all fit experimental data on PG and PG-G production equally well, despite variation of over three orders of magnitude in some of the 316 parameter values (Mitchener et al., 2015). Our results on both pathway flux (Fig. 2) and information 317 flow (Fig. 5) indicate that different parameter sets favor different distributions of paths from substrate to 318 product, and transfer information through the network in different ways. Yet the overall function of the 319 enzyme is the same despite all of this variation. In vivo, a change in the kinetic rates could correspond to 320 a mutation or a change in the level of molecular crowding for the reaction. The availability of multiple 321 "modes of execution" in this complex enzyme thus allow the system to be highly robust to such changes. 322 This complex architecture could also allow the system to be highly evolveable through a mechanism of 323 facilitated variation (Gerhart and Kirschner, 2007). We expect that future work on parameter variation 324 will reveal major insights into the evolution of robustness in enzymes like COX-2. 325

In this work we applied a systems biochemistry framework to understand chemical reaction flux, pathway entropy, and information flow in the COX-2 system and investigate how these adjust to dynamic input concentrations and correlations. The methods and approach utilized here could be applied to further probe the COX-2 system by including more inputs (its other substrates, allosteric regulators, and inhibitors), or transferred to a larger, more complex network. Given the complexity present in even the simple network considered here, we predict that a systems biochemistry approach to larger networks would provide non-intuitive insights into the dynamics of the system as a whole.

# 333 METHODS

## 334 Modeling and Model Calibration

CORM was encoded as a PySB (Lopez et al., 2013) model containing 13 distinct biochemical species and

<sup>336</sup> 29 chemical reactions. It was calibrated to experimental data consisting of PG and PG-G concentrations

at steady state across a range of substrate concentrations (Mitchener et al., 2015; Shockley et al., 2017).

## **Calculating Path Fluxes and Channel Capacities**

<sup>339</sup> The method for determining paths of production and the total flux through a path is described in detail in

SI Methods and Fig. S1. Channel capacities were calculated using the method from (Cheong et al., 2011)

<sup>341</sup> and the software of (Suderman et al., 2017). Extended detail is available in SI Methods.

The datasets generated during and/or analysed during the current study are available from the corresponding author on reasonable request.

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# **349 COMPETING INTERESTS**

<sup>350</sup> The Authors declare no competing financial or non-financial interests.

# **351 AUTHOR CONTRIBUTIONS**

<sup>352</sup> Conceptualization: EMS, CFL; Methodology: EMS, CFL, EJD; Investigation: EMS, CFL, EJD, CAR,

LJM; Resources: CFL, LJM; Analysis: CFL, EMS, EJD, CAR; Writing original draft: EMS, CFL;

Writing Review and Editing: EMS, CFL, EJD, CAR, LJM; Supervision: CFL; Funding Acquisition: CFL,
 LJM

## 356 **REFERENCES**

- Adlung, L., Kar, S., Wagner, M.-C., She, B., Chakraborty, S., Bao, J., Lattermann, S., Boerries, M., Busch,
- H., Wuchter, P., Ho, A. D., Timmer, J., Schilling, M., Höfer, T., and Klingmüller, U. (2017). Protein
- abundance of AKT and ERK pathway components governs cell type-specific regulation of proliferation.
- 360 *Molecular Systems Biology*, 13(1):904.
- Alhouayek, M. and Muccioli, G. G. (2014). COX-2-derived endocannabinoid metabolites as novel inflammatory mediators. *Trends in Pharmacological Sciences*, 35(6):284–292.
- Bisogno, T., Howell, F., Williams, G., Minassi, A., Cascio, M. G., Ligresti, A., Matias, I., Schiano Moriello, A., Paul, P., Williams, E.-J., Gangadharan, U., Hobbs, C., Di Marzo, V., and Doherty,
- P. (2003). Cloning of the first sn1-DAG lipases points to the spatial and temporal regulation of  $I_{1}$  and  $I_{2}$  and  $I_{$
- endocannabinoid signaling in the brain. *The Journal of Cell Biology*, 163(3):463–468.
- Briggs, G. E. and Haldane, J. B. (1925). A Note on the Kinetics of Enzyme Action. *Biochemical Journal*, 19(2):338–339.
- Chen, C. (2010). Lipids: COX-2's new role in inflammation. *Nature Chemical Biology*, 6(6):nchembio.375–402.
- Chen, J.-Y., Lin, J.-R., Cimprich, K. A., and Meyer, T. (2012). A two-dimensional ERK-AKT signaling code for an NGF-triggered cell-fate decision. *Molecular Cell*, 45(2):196–209.
- <sup>373</sup> Cheong, R., Rhee, A., Wang, C. J., Nemenman, I., and Levchenko, A. (2011). Information transduction <sup>374</sup> capacity of noisy biochemical signaling networks. *Science*, 334(6054):354–358.
- Dong, L., Sharma, N. P., Jurban, B. J., and Smith, W. L. (2013). Pre-existent asymmetry in the human
- cyclooxygenase-2 sequence homodimer. *The Journal of biological chemistry*, 288(40):28641–28655.
- Dong, L., Vecchio, A. J., Sharma, N. P., Jurban, B. J., Malkowski, M. G., and Smith, W. L. (2011).
- Human cyclooxygenase-2 is a sequence homodimer that functions as a conformational heterodimer.
   *The Journal of biological chemistry*, 286(21):19035–19046.
- Dong, L., Zou, H., Yuan, C., Hong, Y. H., Kuklev, D. V., and Smith, W. L. (2016a). Different Fatty Acids
- <sup>381</sup> Compete with Arachidonic Acid for Binding to the Allosteric or Catalytic Subunits of Cyclooxygenases
- to Regulate Prostanoid Synthesis. *The Journal of biological chemistry*, 291(8):4069–4078.
- Dong, L., Zou, H., Yuan, C., Hong, Y. H., Uhlson, C. L., Murphy, R. C., and Smith, W. L. (2016b).
   Interactions of 2-O-arachidonylglycerol ether and ibuprofen with the allosteric and catalytic subunits of
   human COX-2. *Journal of lipid research*, 57(6):1043–1050.
- Fezza, F., Bari, M., Florio, R., Talamonti, E., Feole, M., and Maccarrone, M. (2014). Endocannabinoids, Related Compounds and Their Metabolic Routes. *Molecules*, 19(11):17078–17106.
- Funk, C. D. (2001). Prostaglandins and leukotrienes: advances in eicosanoid biology. *Science*, 294(5548):1871–1875.
- Gerhart, J. and Kirschner, M. (2007). The theory of facilitated variation. *Proceedings of the National Academy of Sciences*, 104(suppl 1):8582–8589.
- Huang, S. (2009). Non-genetic heterogeneity of cells in development: more than just noise. *Development* (*Cambridge, England*), 136(23):3853–3862.
- <sup>394</sup> Ignatowska-Jankowska, B. M., Ghosh, S., Crowe, M. S., Kinsey, S. G., Niphakis, M. J., Abdullah, R. A.,
- Tao, Q., O' Neal, S. T., Walentiny, D. M., Wiley, J. L., Cravatt, B. F., and Lichtman, A. H. (2014). In vivocharacterization of the highly selective monoacylglycerol lipase inhibitor KML29: antinociceptive
- vivocharacterization of the highly selective monoacyiglycerol lipase inhibitor KML29: antinociceptive
   activity without cannabimimetic side effects. *British Journal of Pharmacology*, 171(6):1392–1407.
- <sup>397</sup> Kudalkar, S. N., Nikas, S. P., Kingsley, P. J., Xu, S., Galligan, J. J., Rouzer, C. A., Banerjee, S., Ji, L., Eno,
- M. R., Makriyannis, A., and Marnett, L. J. (2015). 13-Methylarachidonic Acid Is a Positive Allosteric
- Modulator of Endocannabinoid Oxygenation by Cyclooxygenase. *Journal of Biological Chemistry*,
- $_{401}$  290(12):7897–7909.
- Kulmacz, R. J. and Lands, W. E. (1984). Prostaglandin H synthase. Stoichiometry of heme cofactor.
   *Journal of Biological Chemistry*, 259(10):6358–6363.
- <sup>404</sup> Kulmacz, R. J. and Lands, W. E. (1985). Stoichiometry and kinetics of the interaction of prostaglandin H
- synthase with anti-inflammatory agents. *Journal of Biological Chemistry*, 260(23):12572–12578.
- Lawrence, T. (2009). The nuclear factor NF-kappaB pathway in inflammation. *Cold Spring Harbor Perspectives in Biology*, 1(6):a001651–a001651.

- Lechtenberg, B. C., Freund, S. M. V., and Huntington, J. A. (2012). An ensemble view of thrombin allostery. *Biological chemistry*, 393(9):889–898.
- Leslie, C. C. (2015). Cytosolic phospholipase A2: physiological function and role in disease. *Journal of lipid research*, 56(8):1386–1402.
- Long, J. Z., Li, W., Booker, L., Burston, J. J., Kinsey, S. G., Schlosburg, J. E., Pavón, F. J., Serrano,
- A. M., Selley, D. E., Parsons, L. H., Lichtman, A. H., and Cravatt, B. F. (2008). Selective blockade of
- 2-arachidonoylglycerol hydrolysis produces cannabinoid behavioral effects. *Nature Chemical Biology*,
   5(1):37–44.
- Lopez, C. F., Muhlich, J. L., Bachman, J. A., and Sorger, P. K. (2013). Programming biological models in Python using PySB. *Molecular Systems Biology*, 9(1):646–646.
- Lorendeau, D., Christen, S., Rinaldi, G., and Fendt, S.-M. (2015). Metabolic control of signalling pathways and metabolic auto-regulation. *Biology of the cell*, 107(8):251–272.
- 420 Mitchell, S., Roy, K., Zangle, T. A., and Hoffmann, A. (2018). Nongenetic origins of cell-to-cell variability
- in B lymphocyte proliferation. *Proceedings of the National Academy of Sciences of the United States* of America, 115(12):E2888–E2897.
- Mitchener, M. M., Hermanson, D. J., Shockley, E. M., Brown, H. A., Lindsley, C. W., Reese, J., Rouzer,
- 424 C. A., Lopez, C. F., and Marnett, L. J. (2015). Competition and allostery govern substrate selectivity of
- cyclooxygenase-2. Proceedings of the National Academy of Sciences of the United States of America,
   112(40):12366–12371.
- Monjazeb, A. M. (2006). Arachidonic acid-induced gene expression in colon cancer cells. *Carcinogenesis*,
   27(10):1950–1960.
- Nussinov, R. and Tsai, C.-J. (2013). Allostery in Disease and in Drug Discovery. *Cell*, 153(2):293–305.
- Rimon, G., Sidhu, R. S., Lauver, D. A., Lee, J. Y., Sharma, N. P., Yuan, C., Frieler, R. A., Trievel, R. C.,
- Lucchesi, B. R., and Smith, W. L. (2010). Coxibs interfere with the action of aspirin by binding tightly
- to one monomer of cyclooxygenase-1. *Proceedings of the National Academy of Sciences of the United States of America*, 107(1):28–33.
- Rouzer, C. A. and Marnett, L. J. (2003). Mechanism of free radical oxygenation of polyunsaturated fatty
   acids by cyclooxygenases. *Chemical Reviews*, 103(6):2239–2304.
- <sup>436</sup> Rouzer, C. A. and Marnett, L. J. (2005). Glycerylprostaglandin Synthesis by Resident Peritoneal
- Macrophages in Response to a Zymosan Stimulus. *Journal of Biological Chemistry*, 280(29):26690–
   26700.
- Rouzer, C. A. and Marnett, L. J. (2009). Cyclooxygenases: structural and functional insights. *Journal of lipid research*, 50 Suppl(Supplement):S29–34.
- <sup>441</sup> Rouzer, C. A. and Marnett, L. J. (2011). Endocannabinoid Oxygenation by Cyclooxygenases, Lipoxyge-
- nases, and Cytochromes P450: Cross-Talk between the Eicosanoid and Endocannabinoid Signaling
- <sup>443</sup> Pathways. *Chemical Reviews*, 111(10):5899–5921.
- Santos, S. D. M., Verveer, P. J., and Bastiaens, P. I. H. (2007). Growth factor-induced MAPK network
   topology shapes Erk response determining PC-12 cell fate. *Nature Cell Biology*, 9(3):324–330.
- Seibert, K., Zhang, Y., Leahy, K., Hauser, S., Masferrer, J., and Isakson, P. (1997). Distribution of Cox-1
- and Cox-2 in Normal and Inflamed Tissues. In *Eicosanoids and Other Bioactive Lipids in Cancer, Inflammation, and Radiation Injury 2*, pages 167–170. Springer US, Boston, MA.
- Selimkhanov, J., Taylor, B., Yao, J., Pilko, A., Albeck, J., Hoffmann, A., Tsimring, L., and Wollman, R.
- (2014). Systems biology. Accurate information transmission through dynamic biochemical signaling
   networks. *Science*, 346(6215):1370–1373.
- <sup>452</sup> Shannon, C. E. (1948). A Mathematical Theory of Communication. pages 1–55.
- 453 Shi, T., Niepel, M., McDermott, J. E., Gao, Y., Nicora, C. D., Chrisler, W. B., Markillie, L. M., Petyuk,
- V. A., Smith, R. D., Rodland, K. D., Sorger, P. K., Qian, W.-J., and Wiley, H. S. (2016). Conservation
   of protein abundance patterns reveals the regulatory architecture of the EGFR-MAPK pathway. *Science*
- 456 *Signaling*, 9(436):rs6–rs6.
- 457 Shockley, E. M., Vrugt, J. A., and Lopez, C. F. (2017). PyDREAM: high-dimensional parameter inference
- 458 for biological models in python. *Bioinformatics*, 18:343.
- <sup>459</sup> Smith, W. L., DeWitt, D. L., and Garavito, R. M. (2000). Cyclooxygenases: structural, cellular, and <sup>460</sup> molecular biology. *Annual review of biochemistry*, 69(1):145–182.
- <sup>461</sup> Spencer, S. L., Gaudet, S., Albeck, J. G., Burke, J. M., and Sorger, P. K. (2009). Non-genetic origins of
- cell-to-cell variability in TRAIL-induced apoptosis. *Nature*, 459(7245):428–432.

- Suderman, R., Bachman, J. A., Smith, A., Sorger, P. K., and Deeds, E. J. (2017). Fundamental trade-offs
   between information flow in single cells and cellular populations. *Proceedings of the National Academy*
- between information flow in single cells and cellular populations. *Proof Sciences of the United States of America*, 114(22):5755–5760.
- <sup>466</sup> Sugiura, T., Kishimoto, S., Oka, S., and Gokoh, M. (2006). Biochemistry, pharmacology and physiology
- <sup>467</sup> of 2-arachidonoylglycerol, an endogenous cannabinoid receptor ligand. *Progress in Lipid Research*,

- Waite, A. J., Frankel, N. W., Dufour, Y. S., Johnston, J. F., Long, J., and Emonet, T. (2016). Non-genetic
   diversity modulates population performance. *Molecular Systems Biology*, 12(12):895.
- 471 Yuan, C., Sidhu, R. S., Kuklev, D. V., Kado, Y., Wada, M., Song, I., and Smith, W. L. (2009). Cyclooxyge-
- nase Allosterism, Fatty Acid-mediated Cross-talk between Monomers of Cyclooxygenase Homodimers.
- 473 *Journal of Biological Chemistry*, 284(15):10046–10055.

<sup>468 45(5):405-446.</sup>