

Calcium-driven regulation of voltage-sensing domains in BK channels

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1 **Abstract**

2 Allosteric interplays between voltage-sensing domains (VSD), Ca²⁺-binding sites, and the
3 pore domain govern the Ca²⁺- and voltage-activated K⁺ (BK) channel opening. However,
4 the functional relevance of the Ca²⁺- and voltage-sensing mechanisms crosstalk on BK
5 channel gating is still debated. We examined the energetic interaction between Ca²⁺
6 binding and VSD activation measuring and analyzing the effects of internal Ca²⁺ on BK
7 channels gating currents. Our results indicate that the Ca²⁺ sensors occupancy has a
8 strong impact on the VSD activation through a coordinated interaction mechanism in which
9 Ca²⁺ binding to a single α -subunit affects all VSDs equally. Moreover, the two distinct high-
10 affinity Ca²⁺-binding sites contained in the C-terminus domains, RCK1 and RCK2, appear
11 to contribute equally to decrease the free energy necessary to activate the VSD. We
12 conclude that voltage-dependent gating and pore opening in BK channels is modulated to
13 a great extent by the interaction between Ca²⁺ sensors and VSDs.

14 **Introduction**

15 Diverse cellular events involve calcium ions as a primary mediator in the signal
16 transduction pathways triggering, among other signaling processes, Ca²⁺-activated
17 conductances. Since the BK channels are regulated by cytosolic Ca²⁺ and depolarizing
18 voltages (Marty, 1981; Pallotta et al., 1981; Latorre et al., 1982), they are integrators of
19 physiological stimuli including intracellular Ca²⁺ elevation and membrane excitability. BK
20 channels are modular proteins where each module accomplishes a specific channel
21 function. Thus, different modules harbor voltage and Ca²⁺ sensors that communicate with
22 the channel gate allosterically (Cox et al., 1997; Horrigan and Aldrich, 1999, 2002;
23 Horrigan et al., 1999; Rothberg and Magleby, 1999, 2000; Cui and Aldrich, 2000).
24 Functional BK channels are formed by homotetramers of α -subunits (Shen et al., 1994)
25 each comprising a transmembrane voltage-sensing domain (VSD) and an intracellular
26 Ca²⁺-sensing C-terminal domain (CTD) that can independently modulate the ion
27 conduction gate in the pore domain (PD) (Latorre et al., 2017). The CTDs consist of two
28 non-identical regulators of the conductance of K⁺ domains (RCK1 and RCK2) arranged
29 into a ring-like tetrameric structure dubbed the gating ring (Wu et al., 2010; Yuan et al.,
30 2010, 2012; Hite et al., 2017; Tao et al., 2017). Each RCK domain contains distinct ligand-
31 binding sites capable of detecting Ca²⁺ in the micromolar range (Schreiber and Salkoff,
32 1997; Bao et al., 2002; Xia et al., 2002).

33 In the absence of Ca²⁺, the activation of VSD decreases the free energy necessary to fully
34 open the BK channels in an allosteric fashion (Horrigan and Aldrich, 1999; Horrigan et al.,
35 1999). Under these experimental conditions, very positive membrane potentials are
36 required to drive all voltage sensors to its activated conformation (Cui et al., 1997; Stefani
37 et al., 1997; Horrigan et al., 1999; Contreras et al., 2012), ultimately leading to a significant
38 activity of the BK channel. Hence, in cells like neurons, an appreciable open probability of

39 BK channels at physiologically relevant voltages necessarily involves the activation of Ca^{2+}
40 sensors on the gating ring. The allosteric interplays established between the functional
41 and structural modules (VSD-PD, CTD-PD, and CTD-VSD) are key in enabling BK
42 channels to operate over a dynamic wide-range of internal Ca^{2+} and voltage conditions by
43 fine-tuning the channel's gating machinery. Therefore, understanding the structure-
44 functional bases that underlie the Ca^{2+} and voltage activation mechanisms
45 interrelationship becomes essential.

46 The voltage dependence of Ca^{2+} -dependent gating ring rearrangements (Miranda et al.,
47 2013, 2018) and RCK1 site occupancy (Sweet and Cox, 2008; Savalli et al., 2012; Miranda
48 et al., 2018) as well as the perturbation of VSD movements by Ca^{2+} binding (Savalli et al.,
49 2012) support the idea that the energetic interaction between both specialized sensors
50 may be crucial to favor BK channel activation. The physical CTD-VSD interface has been
51 suggested to provide the structure capable of mediating the crosstalk between these
52 sensory modules and their synergy in activating the pore domain (Yang et al., 2007; Sun
53 et al., 2013; Tao et al., 2017; Zhang et al., 2017). However, the strength of the interaction
54 between voltage and Ca^{2+} sensors and their relevance to BK channel activation is still an
55 unresolved matter (Horrigan and Aldrich, 2002; Carrasquel-Ursulaez et al., 2015). Also,
56 the functional role that plays each of the high-affinity Ca^{2+} -binding sites on the CTD-VSD
57 allosteric interaction is an open question. The RCK1 and RCK2 Ca^{2+} -binding sites have
58 distinct functional properties conferred by their different molecular structures and relative
59 positions within the gating ring (Wu et al., 2010; Yuan et al., 2010, 2012; Hite et al., 2017;
60 Tao et al., 2017). Thus, the RCK sites differ in their Ca^{2+} binding affinities (Bao et al., 2002;
61 Xia et al., 2002; Sweet and Cox, 2008), divalent cations selectivity (Oberhauser et al.,
62 1988; Schreiber and Salkoff, 1997; Zeng et al., 2005; Zhou et al., 2012), voltage
63 dependence (Sweet and Cox, 2008; Savalli et al., 2012; Miranda et al., 2018) and in their

64 contribution to allosteric gating mechanism (Yang et al., 2010, 2015). In particular, only
65 the RCK1 site appears to be involved in communicating the Ca^{2+} -dependent
66 conformational changes towards the membrane-spanning VSD (Savalli et al., 2012;
67 Miranda et al., 2018). Recently, the *Aplysia* BK structure shows that the N-lobe of RCK1
68 domain is in a non-covalent contact with the VSD and the S4-S5 linker being this RCK1-
69 VSD interaction surface rearranged when comparing the liganded and Ca^{2+} -free
70 structures (Hite et al., 2017; Tao et al., 2017). Actually, it has been hypothesized that any
71 Ca^{2+} -induced rearrangements of the gating ring should be ultimately transmitted to the
72 pore domain via the VSD (Hite et al., 2017; Zhou et al., 2017). Thus, defining what extent
73 Ca^{2+} binding influences to VSD is crucial in determining how important is the crosstalk
74 between sensors in decreasing the free energy necessary to open the BK channel.

75 Here, we examined the Ca^{2+} -dependence of the VSD activation estimating the allosteric
76 coupling between Ca^{2+} and voltage sensors. By analyzing gating currents under
77 unliganded and Ca^{2+} -saturated conditions, we found a strong energetic influence of the
78 Ca^{2+} -binding on the voltage sensors equilibrium in an independent manner of the channel
79 opening. These findings point out that a major component in the synergistic Ca^{2+} and
80 voltage activation of BK channels can reside on the sensory domains communication. We
81 also found that the Ca^{2+} -dependent behavior of the voltage sensor activation is consistent
82 with an CTD-VSD allosteric coupling that occurs through a concerted interaction scheme
83 where each Ca^{2+} -bound to high-affinity sites affect equally all voltage sensors in the BK
84 tetramer. Notably, we found that the two distinct RCK1 and RCK2 Ca^{2+} sensors exert
85 equivalent contributions on VSD via independent allosteric pathways.

86 Results

87 Allosteric coupling between Ca²⁺-binding and voltage sensor activation is strong.

88 We characterized the effects of Ca²⁺-binding on voltage sensor activation in BK channels
89 by analyzing gating current measured on inside-out patches of *Xenopus laevis* oocyte
90 membrane. Families of gating currents (I_G) were evoked at different intracellular Ca²⁺
91 concentrations ($[Ca^{2+}]_i$) ranging from 0.1 to 100 μ M in K⁺-free solution (**Figure 1A**). For all
92 experiments, first we measured I_G in the nominal absence of Ca²⁺ (“zero Ca²⁺” condition),
93 and then we perfused the internal side with solutions containing Ca²⁺ at increasing
94 concentrations. The amount of gating charge displaced (Q_C) at each Ca²⁺ concentration
95 was obtained by fitting the initial part of the ON-gating current decay to a single exponential
96 (fast ON-gating; see *Methods*) and integrating it. In this manner, we determine only the
97 gating charge displaced before the BK channel opening.

98 The increase in internal Ca²⁺ promotes a leftward shift of the Q_C versus voltage ($Q_C(V)$)
99 curves (**Figure 1B,C**) which indicate that Ca²⁺-binding facilitates the activation of the
100 voltage sensor being more prominent as binding sites occupancy increases. Revealing a
101 strong energetic interaction between both sensors, a significant Ca²⁺-induced shift of
102 voltage sensor activation occurs ($\Delta V_H = -142.6 \pm 4.5$ mV) under Ca²⁺-saturated conditions
103 for high-affinity binding sites (100 μ M). Such large shift means that Ca²⁺-binding to the
104 RCK Ca²⁺-binding sites alters the VSD equilibrium promoting a decrease in the free energy
105 ($\Delta\Delta G_V^{Ca}$) that defines the voltage sensor resting-active (R-A) equilibrium by ~ 8 kJ/mol
106 ($\Delta\Delta G_V^{Ca} = -7.98 \pm 0.27$ kJ/mol).

107 A visual inspection of the current records indicates that the kinetics of the ON-gating
108 current is not much affected by the concentration of Ca²⁺ present in the internal solution.

109 However, it is apparent that the OFF-gating current is dramatically modified becoming
110 smaller in amplitude and with slower kinetics as the internal Ca^{2+} concentration is
111 increased (**Figure 1A** and **Figure 1—figure supplement 1A**). At least two components
112 can be resolved in the OFF gating current decay (**Figure 1—figure supplement 1B,C**),
113 and the relative contribution of the slower component increases as internal Ca^{2+}
114 augmented reflecting an increase of the open probability of channel **Figure 1—figure**
115 **supplement 1D,E**). This kinetic behavior recapitulates the effect describe on gating
116 charge displacement as a function of the depolarizing pulse duration (Horrigan and
117 Aldrich, 2002; Contreras et al., 2012; Carrasquel-Ursulaez et al., 2015), and confirm that
118 this phenomenon is associated with the time course of channel opening revealing the
119 allosteric interaction between voltage sensors and the pore gate (Horrigan and Aldrich,
120 2002).

121 **Ca^{2+} binding to single α -subunit affects the R-A voltage sensor equilibrium of all**
122 **four subunits equally.** Taking advantage of the dose-dependent effect of Ca^{2+} on voltage
123 sensor activation we investigated the underlying mechanism of the Ca^{2+} -voltage sensors
124 communication in the context of the well-established Horrigan-Aldrich (HA) allosteric
125 gating model(Horrigan and Aldrich, 2002). Two different mechanisms were proposed by
126 Horrigan and Aldrich for the interaction between the Ca^{2+} -binding sites and voltage
127 sensors. The first mechanism supposes that Ca^{2+} binding to one α -subunit affects the VSD
128 in the same subunit only (Scheme I) (**Figure 2A**), while the second mechanism assumes
129 that the Ca^{2+} binding affects the four VSD equally (Scheme II) (**Figure 2B**). It should be
130 noted that the standard HA model makes two simplifying assumptions by considering a

131 single Ca^{2+} -binding site per α -subunit and the Scheme I as the Ca^{2+} binding-VSD
132 interaction mechanism underlying BK channel gating (Horrigan and Aldrich, 2002).

133 For a better comprehension, we simulated the normalized $Q_C(V)$ curves over a wide
134 range of Ca^{2+} concentrations (from 0 to 10 mM) for each Ca^{2+} -VSD interaction scheme
135 (**Figure 2C,D**). Here we assume that the measurement of the fast gating currents captures
136 the charge displaced by R-A transitions and exclude the charge associated with the
137 transition between the activated states. This assumption is reasonable since the Ca^{2+} -
138 binding rate constant estimated for BK is about $10^8 \text{ M}^{-1}\text{s}^{-1}$ (Hou et al., 2016) implying that
139 at 10 μM internal Ca^{2+} (the highest non-saturating Ca^{2+} concentration tested) the time
140 constant of the Ca^{2+} binding is 1 ms, while the VSD activates with a time constant of ~ 30
141 μs at the higher voltage tested (see the *Supplementary Information* for details of the
142 simulations). At extreme conditions of low (0.03 to 0.1 μM) and high ($\geq 100 \mu\text{M}$) internal
143 Ca^{2+} , the VSD activation behaves in a mechanism-independent manner since all voltage
144 sensors are in the same functional state (unliganded or saturated). However, the
145 distinctive effects on $Q_C(V)$ curves at intermediate Ca^{2+} concentrations (1-10 μM) provide
146 useful signatures to distinguish between these two mechanisms. Scheme I predicts two
147 functional states of the VSD depending on occupancy status of the Ca^{2+} site (Ca^{2+} bound
148 and unbound) such that the $Q_C(V)$ curve behavior is described by the fractional
149 distribution of the unliganded and Ca^{2+} -saturated functional states like an all-or-none
150 allosteric effect (**Figure 2C; Figure 2—figure supplement 1B** and Equation 4 in
151 *Supplementary Information*). On the contrary, the Ca^{2+} -binding effect on the VSD
152 activation according to the Scheme II is characterized by a five-component Boltzmann
153 function (**Figure 2—figure supplement 1C** and Equation 6 in *Supplementary*
154 *Information*). Each component represents a single functional state determined by the
155 number of Ca^{2+} bound to the channel (from 0 to 4). In such case, the $Q_C(V)$ curves

156 resulting from a distribution of functional states behaves as an equivalent single
157 Boltzmann leftward shifted by an incremental allosteric effect (from E to E^4) as the
158 number of Ca^{2+} bound to the channel increases (**Figure 2D**).

159 To elucidate the mechanism by which Ca^{2+} and voltage sensors interact, we performed
160 fits of the $Q_C(V)$ data using the two different models represented in the Scheme I and
161 Scheme II (**Figure 3A,B**). The allosteric factor E that accounts for the coupling between
162 the Ca^{2+} -binding sites and the voltage sensors was constrained to values calculated from
163 the experimental data of the $Q_C(V)$ shift at the Ca^{2+} saturating conditions (100 μM) in
164 relation to the same curve in the absence of Ca^{2+} . The z_J , J_0 and K_D parameters obtained
165 during the fitting procedure of each model are very similar (**Figure 3C**). The fitted values
166 of the affinity constant ($K_D = 3 - 5 \mu\text{M}$) agree with previous reports (Cox et al., 1997;
167 Horrigan and Aldrich, 2002) although slightly smaller than those estimated on the closed
168 conformation of the channel ($K_D = 11 \mu\text{M}$). However, we found that the fit with the Scheme
169 II to the $Q_C(V)$ curves (**Figure 3B**) is better than the fit to the data using Scheme I (**Figure**
170 **3A**) as indicated by the Akaike model selection criteria (AIC) (Akaike, 1974). Moreover,
171 Model II generates a V_H - $\log[\text{Ca}^{2+}]$ curve (solid line) that accounts for the dose-response
172 V_H - $\log[\text{Ca}^{2+}]$ experimental data reasonable well (**Figure 3D**). Also, the behavior of
173 $Q_C(V)$ curves at intermediate Ca^{2+} concentrations (1-10 μM) is qualitatively consistent
174 with the phenotype exhibit by the Ca^{2+} -VSD scheme II (**Figure 2D and Figure 3B**). Thus,
175 the experimental dose-dependent effect of Ca^{2+} on voltage sensor activation reveals that
176 Ca^{2+} -binding to a single α -subunit of BK channels increases E -fold the equilibrium
177 constant J that defines the equilibrium between resting and active conformations of the
178 voltage sensors in all four subunits.

179 **High-affinity Ca²⁺-binding sites in RCK1 and RCK2 domains contribute equally to**
180 **the allosteric coupling between Ca²⁺ and voltage sensors.** Under physiological
181 conditions, the RCK1 and RCK2 high-affinity Ca²⁺-binding sites are responsible by all
182 calcium sensitivity of the activation of BK channel (Schreiber and Salkoff, 1997; Bao et al.,
183 2002, 2004; Xia et al., 2002). However, distinct physiological roles of the RCK1 Ca²⁺-
184 sensor and Ca²⁺ bowl may be based in their functionally and structurally distinctive
185 properties (Zeng et al., 2005; Sweet and Cox, 2008; Yang et al., 2010; Savalli et al., 2012;
186 Tao et al., 2017). Below, we asked what the energetic contribution to VSD equilibrium is
187 of the two high-affinity Ca²⁺-binding sites contained in the RCK1 and RCK2 domains.

188 To elucidate the effect of each Ca²⁺-sensor on the VSD activation we used mutations that
189 selectively and separately abolish the function of the two different RCK Ca²⁺-sites.
190 Disruption of the RCK1 Ca²⁺-sensor by the double mutant D362A/D367A (Xia et al., 2002)
191 reduces significantly (48%, ΔV_H (D362A/D367A) = -74.9 ± 4.7 mV) the leftward shift of the
192 $Q_C(V)$ curves at 100 μ M Ca²⁺ compared with the wild-type (WT) BK channel (**Figure**
193 **4A,C**). We also examined the effect of the mutant M513I (Bao et al., 2002) which have
194 been shown to eliminate the Ca²⁺ sensitivity derived from the RCK1 site (Bao et al., 2002,
195 2004; Zhang et al., 2010). In this mutant, the 100 μ M Ca²⁺-induced shift in V_H of VSD
196 activation curve is also considerably smaller relative to WT (about 54%, ΔV_H (M513I) = -
197 65.4 ± 2.6 mV) (**Figure 5**). Therefore, both mutations affect the Ca²⁺-induced
198 enhancement of activation of voltage sensor very similarly through the RCK1 site (**Figure**
199 **5C**), although their mechanisms action could be quite different. The M513 residue appears
200 to participate in the stabilization of the proper conformation RCK1 Ca²⁺-site whereas D367
201 is a key residue in the coordination of Ca²⁺ ion (Wu et al., 2010; Zhang et al., 2010; Tao
202 et al., 2017). On the other hand, neutralization of the residues forming part of the Ca²⁺
203 bowl (Schreiber and Salkoff, 1997) (5D5A mutant, see *Methods*) on the RCK2 domain

204 decreases the leftward shift of the $Q_C(V)$ curve when Ca^{2+} is increased to 100 μM by
205 approximately 54% ($\Delta V_H(5D5A) = -65.7 \pm 4.7$ mV) (**Figure 4B, D**). Surprisingly, the effect
206 of Ca^{2+} binding on ΔV_H from each high-affinity Ca^{2+} site is roughly half relative to WT
207 channels with both intact sites (**Figure 4E**). Therefore, both high-affinity Ca^{2+} -binding sites
208 contribute equally to decrease the free energy necessary to activate the VSD. Thus, the
209 change of free energy of the resting-active equilibrium of the voltage sensor in response
210 to Ca^{2+} -binding at RCK2 site is ~ -4 kJ/mol ($\Delta\Delta G_V^{Ca}(D362A/D367A) = -4.2 \pm 0.3$ kJ/mol and
211 $\Delta\Delta G_V^{Ca}(M513I) = -3.6 \pm 0.5$ kJ/mol) (**Figure 4C** and **Figure 5C**). In the same way, the
212 occupation of the RCK1 Ca^{2+} -binding site decreases the free energy necessary to activate
213 the VSD in -3.8 ± 0.4 kJ/mol ($\Delta\Delta G_V^{Ca}(5D5A)$). Remarkably, these findings reveal an additive
214 effect of Ca^{2+} -binding to the RCK1 and Ca^{2+} bowl sites on the VSD activation which
215 suggest independent allosteric pathways through which they exert their modulation on the
216 VSD.

217 Taking these results into account, we expanded the Ca^{2+} -VSD interaction model described
218 by Scheme II considering the energetic contribution of the two kinds of Ca^{2+} sensors on
219 the VSD per α -subunit ($E_{WT} = E_{S1} * E_{S2}$) (**Figure 2—figure supplement 1E**). As
220 described in the above model fittings, the allosteric factors E of each one RCK1 and RCK2
221 sites (E_{S1} and E_{S2}) were constrained to values equivalent to the Ca^{2+} -induced energetic
222 perturbations of the voltage sensor equilibrium for the 5D5A and D362A/D367A mutants,
223 respectively. However, the inclusion of the two Ca^{2+} sensors in the Ca^{2+} -VSD interaction
224 model does not produce better fits to $Q_C(V, [\text{Ca}^{2+}])$ according to the AIC criteria (**Table**
225 **1** and **Figure 3B**), the estimated K_D parameters for each Ca^{2+} -binding sites ($K_{D1} = 15.6$
226 μM and $K_{D2} = 1.9 \mu\text{M}$) by the experimental data fitting agrees very well with the apparent

227 Ca²⁺ affinities previously reported in the literature (Bao et al., 2002; Xia et al., 2002; Sweet
228 and Cox, 2008). Interestingly, modest positive cooperativity ($G = 2.6$) between the two
229 Ca²⁺-binding sites located in the same α -subunit is required to achieve a good estimation
230 of the K_D parameters (**Table 1**), where the Ca²⁺ bowl site has an affinity for Ca²⁺ about 8-
231 fold greater than does the RCK1 Ca²⁺-sensor.

232 Discussion

233 Recent insights into a major interplay between voltage- and Ca^{2+} -sensing modules in the
234 BK channel are supported by functional and structural studies (Yuan et al., 2010; Savalli
235 et al., 2012; Miranda et al., 2013, 2016, 2018; Carrasquel-Ursulaez et al., 2015; Hite et
236 al., 2017; Tao et al., 2017; Zhang et al., 2017), offering a new perspective in our
237 understanding of its multimodal gating mechanism. However, the CTD-VSD allosteric
238 coupling as well its molecular nature has yet to be firmly established since their direct
239 assessment is subject to great experimental challenges. Based on the functional
240 independence of the distinct structural domains (PD, CTD, and VSD), the energetic
241 relationship between the sensory modules can be directly defined comparing the voltage
242 sensor equilibrium change at extreme Ca^{2+} stimulus conditions limiting the status of the
243 Ca^{2+} -binding sites to two well-defined configurations: unliganded and saturated (Horrigan
244 and Aldrich, 2002).

245 Using this approach, this work straightforwardly establishes that Ca^{2+} -binding to high-
246 affinity sites make a significant and direct energetic contribution to the equilibrium of the
247 resting-activated transition (R-A) of the VSD facilitating their activation ($\Delta V_{\text{H}} = -142.6 \pm$
248 4.5 mV and $\Delta\Delta G_{\text{V}}^{\text{Ca}} = -7.98 \pm 0.27$ kJ/mol). This result resolves a previous debate
249 regarding to the magnitude of the Ca^{2+} -driven shift of the $Q_{\text{C}}(V)$ curve, because it has
250 been reported a similar leftward shift ($\Delta V_{\text{H}} = -140$ mV and $\Delta\Delta G_{\text{V}}^{\text{Ca}} = -7.9$ kJ/mol; at $[\text{Ca}^{2+}]_{\text{i}}$
251 $= 100$ μM) (Carrasquel-Ursulaez et al., 2015) and a smaller leftward shift ($\Delta V_{\text{H}} = -33$ mV
252 and $\Delta\Delta G_{\text{V}}^{\text{Ca}} = -1.9$ kJ/mol; at $[\text{Ca}^{2+}]_{\text{i}} = 70$ μM) (Horrigan and Aldrich, 2002) at saturating
253 Ca^{2+} concentration. The reason for the contradictory findings is not clear to us; since we
254 used a similar experimental approach. Even if we assumed that the calcium effect on VSD
255 is underestimated at 70 μM Ca^{2+} (Horrigan and Aldrich, 2002) compared to 100 μM as

256 saturating condition of the binding sites, we observed a significant greater effect in Ca^{2+}
257 concentrations (1, 5 and 10 μM , **Figure 1C**) where less than 50% of the Ca^{2+} sensors are
258 occupied ($K_D = 11 \mu\text{M}$ (Cox et al., 1997; Horrigan and Aldrich, 2002)).

259 Fluorescence studies that optically track the motions of the voltage sensor or gating ring
260 provide two lines of evidence that support these findings. First, conformational
261 rearrangements of the voltage sensors detected using voltage-clamp fluorometry can be
262 provoked by Ca^{2+} -binding to the high-affinity sites. The sudden rise of intracellular $[\text{Ca}^{2+}]$
263 by UV flash induced-photolysis of caged Ca^{2+} prompts a leftward shift in both
264 conductance-voltage ($G(V)$) and fluorescence-voltage ($F(V)$) relationships. These
265 results suggest that functional activation of the gating ring is propagated to VSD leading
266 to structural perturbations of voltages sensors, thereby favoring its active conformation
267 (Savalli et al., 2012). Second, the structural rearrangement of gating ring in response to
268 Ca^{2+} has a voltage dependence (Miranda et al., 2013, 2018) attributable to the voltage
269 sensor operation. The origin of these voltage-dependent motions has been recently
270 established via modifications on the voltage-sensing function of the BK channel using the
271 patch-clamp fluorometry technique (Miranda et al., 2018). Both the charged residue
272 mutations on the S4 transmembrane segment (R210, R213, and E219) and the co-
273 expression of $\beta 1$ -subunit with $\text{BK}\alpha$ channel modify the conformational changes of the
274 gating ring triggered by depolarization in correspondence to the observed $G(V)$ shift for
275 these channel constructs. In contrast, perturbations of pore opening equilibrium like the
276 F315A mutation or the assembly of $\text{BK}\alpha$ channel with $\gamma 1$ -subunit does not modify on the
277 voltage-dependent reorganization of the gating ring (Miranda et al., 2018).

278 Mechanistically and in a channel opening-independent fashion, how does the CTD-VSD
279 coupling occur? Taking into account the homotetrameric configuration of the BK channel,
280 Horrigan and Aldrich (Horrigan and Aldrich, 2002) defined the general gating scheme of

281 BK channel considering the simplest CTD-VSD interaction model in which voltage sensors
282 and Ca^{2+} -binding sites solely interact within the same subunit. However, the VSD
283 movement at non-saturating Ca^{2+} conditions which entail distinct functional states of the
284 Ca^{2+} sites (unliganded and liganded), unveiled that the standard HA model can not explain
285 the mechanistic interaction governing the allosteric coupling between the Ca^{2+} and voltage
286 sensors. Given that Ca^{2+} -binding will influence only a fraction of voltage sensors, Scheme
287 I would evidence $Q_C(V)$ curves characteristic of an all-or-none model showing two well-
288 distinguishable components Boltzmann that correspond to Ca^{2+} -affected and unaffected
289 VSD fractions (**Figure 3A**). Conversely, an energetic effect of each Ca^{2+} -site on all the
290 voltage sensors of the tetramer would lead to an equivalent functional status of each VSD,
291 so that the $Q_C(V)$ curves behaving in an incremental shifted fashion as increasing the
292 fractional occupancy of the Ca^{2+} sites. The VSD and Ca^{2+} sites interacting in such a fashion
293 (Scheme II) reproduce reasonably well the behavior of the Ca^{2+} -dependent gating charge
294 movement observed in our experiments (**Figure 3B**). This concerted CTD-VSD
295 communication may underlie a mechanism analogous to the mechanical strategy of
296 interaction between the homooctameric ring of RCK domains and the pore module
297 described for bacterial K^+ channels (Jiang et al., 2002; Ye et al., 2006; Lingle, 2007; Pau
298 et al., 2011; Smith et al., 2012, 2013). Both in MthK and BK channels, the Ca^{2+} -site
299 occupancy triggers a conformational change conveying to a symmetric overall
300 rearrangement of the cytosolic tetrameric structure that finally is propagated to the
301 transmembrane regions (TMD) via C-linker and in the BK channel also via the protein-
302 protein interfaces between the gating ring and the TMD (Jiang et al., 2002, 2003; Ye et
303 al., 2006; Yuan et al., 2010, 2012; Pau et al., 2011; Smith et al., 2012; Tao et al., 2017).
304 Consequently, we can speculate that each Ca^{2+} -binding event produces a gradual

305 conformational expansion of the gating ring affecting the four voltage sensors in each step
306 through the progressive perturbations within the protein-protein interfaces.

307 As mentioned above, the communication pathway through which the Ca^{2+} -driven
308 conformational changes are propagated to the voltage sensors appears to critically reside
309 on the CTD-VSD interface that involves non-covalent interactions between RCK1 N-lobe
310 and S0-S4 transmembrane segments (Yang et al., 2007, 2008, 2010; Sun et al., 2013;
311 Hite et al., 2017; Tao et al., 2017). Scanning mutagenesis of RCK1-N terminal subdomain
312 indicated that residues on the $\beta\text{A}-\alpha\text{C}$ region are involved into the allosteric connection of
313 the Ca^{2+} -dependent activation mediated by RCK1 site occupancy but not to the Ca^{2+} bowl
314 (Yang et al., 2010). In line with this study, the selective activation of the RCK1 domain was
315 identified to be responsible for the Ca^{2+} -induced VSD rearrangement (Savalli et al., 2012)
316 and the voltage dependence of the Ca^{2+} -driven motions of gating ring (Miranda et al.,
317 2016, 2018), suggesting that CTD-VSD allosteric coupling is primarily determined by the
318 RCK1 site. However, our results are inconsistent with this picture. The constructs
319 D362A/D367A and 5D5A (D894A-D898A) selectively impaired the Ca^{2+} -sensitivity of the
320 RCK1- and RCK2-sensors, respectively, by neutralization of residues that are involved in
321 contributing to Ca^{2+} -coordination (Zhang et al., 2010; Tao et al., 2017). Comparing the fast
322 gating charge movement at 0 Ca^{2+} and saturating Ca^{2+} conditions reflects that the
323 energetic effect of Ca^{2+} -binding on voltage sensor equilibrium is practically identical (~ -4
324 kJ/mol) for either the D362A/D367A mutations or 5D5A mutations (**Figure 4**). Thus, our
325 findings establish that the RCK2-driven contribution to CTD-VSD energetic coupling is
326 quite similar to the RCK1-driven contribution. The functional role of the RCK2-sensor on
327 Ca^{2+} -sensitivity of VSD activation was further corroborated using the M513I mutation
328 (**Figure 5**). This point mutation hinders the Ca^{2+} -dependent activation associated with the
329 RCK1-sensor presumably by disrupting the structural integrity of the binding site and the

330 transduction via through the β A- α C region (Zhang et al., 2010). Thus, another residue
331 involved in the BK Ca^{2+} -dependent activation mediated by the RCK1 Ca^{2+} -binding site but
332 not forming part of the site itself decreases the $Q_C(V)$ leftward shift almost in the same
333 amount as it does the D362A/D367A mutant.

334 Interestingly, beyond the energetic contribution of each RCK site to the voltage sensor
335 equilibrium is the same, its addition mimics the VSD Ca^{2+} -sensitivity of the fully occupied
336 sites. These findings remind us of early reports showing that each RCK site mutant shifts
337 the Ca^{2+} -dependent $G(V)$ by approximately half relative to WT channels (Bao et al., 2002;
338 Xia et al., 2002). Our results suggest an autonomy of the two RCK-sensors indicating
339 independent allosteric pathways through which they exert their modulation on the VSD but
340 does not discard some cooperativity effect between them. Indeed, various lines of
341 evidence indicate albeit modest a cooperativity between the two high-affinity Ca^{2+} -binding
342 sites although their nature is still unclear (Qian et al., 2006; Sweet and Cox, 2008; Savalli
343 et al., 2012). Intra and intersubunit structural connectivity support the putative cooperative
344 interactions between the Ca^{2+} sensors at the gating ring (Yuan et al., 2012; Hite et al.,
345 2017). Actually, a recently functional study of the intrasubunit connections between the
346 RCK1 site and Ca^{2+} bowl (R514-Y904/E902 interactions) has shown that such
347 connections are potential candidates of the structural determinants underlying to a
348 cooperative mechanism between the RCK1- and RCK2-sensor involving either to
349 preserve the integrity of RCK1 Ca^{2+} -binding site or the allosteric propagation pathway
350 towards transmembrane domains (Kshatri et al., 2018). On the basis of the cryo-EM
351 structure of *Aplysia californica* BK channel, Hite et al. (Hite et al., 2017) proposed that
352 there should be a positive cooperativity of the Ca^{2+} -binding at RCK1 site and Ca^{2+} bowl
353 since the Ca^{2+} -induced conformational change of the RCK1-N lobes from closed to open
354 configuration depends on functional state (unliganded and liganded) of both RCK sites.

355 Our analysis based on the CTD-VSD interaction model predicted a small and positive
356 cooperative relation ($G = 2.6$) among the two high-affinity Ca^{2+} sites within the same α -
357 subunit, which has been suggested by an earlier study (Qian et al., 2006). It is noteworthy
358 that K_D parameters achieved for each Ca^{2+} -binding sites ($K_{D1} = 15.6 \mu\text{M}$ and $K_{D2} = 1.9$
359 μM) by the experimental data fitting agrees very well with the apparent Ca^{2+} affinities
360 previously reported in the literature (Bao et al., 2002; Xia et al., 2002; Sweet and Cox,
361 2008). Together, all this new information recapitulate a more relevant functional role of the
362 cooperative interactions between RCK sensors within the same subunit on Ca^{2+} -
363 dependent activation of the channel (Qian et al., 2006).

364 In conclusion, our results depict a remarkable, and direct energetic direct interplay
365 between the specialized sensory modules (VSD and CTD). Our findings together with the
366 emerging structural-functional information establish a new paradigm about how the stimuli
367 integration (depolarization and intracellular Ca^{2+}) modulates the BK channel activation and
368 its relevance within a physiological context. Notable and unexpected is the equivalent role
369 of the distinct ligand-binding sites at the cytosolic domain to the allosteric regulation on
370 voltage sensing. Additional studies to discern the molecular bases underlying in the Ca^{2+}
371 and voltage propagation pathways and the cooperative interactions of the RCK1 and
372 RCK2 regulatory domains may provide new clues about the dual gating mechanism of BK
373 channel.

374 **Methods**

375 **Channel Expression.**

376 *Xenopus laevis* oocytes were used as a heterologous system to express BK channels.
377 The cDNA coding for the human BK α -subunit (U11058) was provided by L. Toro
378 (University of California, Los Angeles, CA). The cDNA coding for independent mutants of
379 each two high-affinity Ca^{2+} site from BK channel, the double mutant D362A/D367A (Xia et
380 al., 2002) and the mutant M513I (Bao et al., 2002) in the RCK1 Ca^{2+} -binding site and the
381 mutant 5D5A (Schreiber and Salkoff, 1997) (D894A/D895A/D896A/D897A/D898A) in the
382 RCK2 Ca^{2+} -binding site or calcium bowl, were kindly provided by M. Holmgren (National
383 Institutes of Health, Bethesda, MD). The cRNA was prepared by using mMMESSAGE
384 mMACHINE (Ambion) for *in vitro* transcription. *Xenopus laevis* oocytes were injected with
385 50 ng of cRNA and incubated in an ND96 solution (in mM: 96 NaCl, 2 KCl, 1.8 CaCl_2 , 1
386 MgCl_2 , 5 HEPES, pH 7.4) at 18°C for 4–8 days before electrophysiological recordings.

387 **Electrophysiological recordings.**

388 All recordings were made by using the patch-clamp technique in the inside-out
389 configuration. Data were acquired with an Axopatch 200B (Molecular Devices) amplifier
390 and the Clampex 10 (Molecular Devices) acquisition software. Gating current (I_G) records
391 were elicited by 1-ms voltage steps from -90 to 350 mV in increments of 10 mV. Both the
392 voltage command and current output were filtered at 20 kHz with 8-pole Bessel low-pass
393 filter (Frequency Devices). Current signals were sampled with a 16-bit A/D converter
394 (Digidata 1550B; Molecular Devices), using a sampling rate of 500 kHz. Linear membrane
395 capacitance and leak subtraction were performed based on a P/4 protocol (Armstrong and
396 Bezanilla, 1974).

397 Borosilicate capillary glasses (1B150F-4, World Precision Instruments) were pulled in a
398 horizontal pipette puller (Sutter Instruments). After fire-polished, pipette resistance was
399 0.5-1 M Ω . The external (pipette) solution contained (in mM): 110 tetraethylammonium
400 (TEA)-MeSO₃, 10 HEPES, 2 MgCl₂; pH was adjusted to 7.0. The internal solution (bath)
401 contained (in mM): N-methyl-D-glucamine (NMDG)-MeSO₃, 10 HEPES, and 5 EGTA for
402 “zero Ca²⁺” solution (~0.8 nM, based on the presence of ~10 μ M contaminant [Ca²⁺] (Cui
403 et al., 1997). For test solutions at different Ca²⁺ concentrations (0.1-100 μ M), CaCl₂ was
404 added to reach the desired free [Ca²⁺], and 5 mM EGTA (0.1-0.5 μ M) or HEDTA (1-10 μ M)
405 was used as calcium buffer. No Ca²⁺ chelator was used in 100 μ M free Ca²⁺ solutions.
406 Free calcium concentration was estimated using the WinMaxChelator Software and
407 checked with a Ca²⁺-electrode (Hanna Instruments). All experiments were performed at
408 room temperature (20-22 °C). To measure I_G at different Ca²⁺ concentrations in the same
409 oocyte, the patch was excised and washed with an appropriate internal solution at least
410 10 times the chamber volume.

411 **Data Analysis.**

412 All data analysis was performed using Clampfit 10 (Molecular Devices), Matlab
413 (MathWorks) and Excel 2007 (Microsoft). The first 50-100 μ s of the ON-gating currents
414 were fitted to a single exponential function and the area under the curve was integrated to
415 obtain the charge displaced between closed states (Q_C) (Horrigan and Aldrich, 1999,
416 2002; Contreras et al., 2012; Carrasquel-Ursulaez et al., 2015). $Q_C(V)$ data for each
417 [Ca²⁺]_i were fitted using a Boltzmann function: $Q_C(V) = \frac{Q_{C, \text{MAX}}}{1 + e^{\left(\frac{-z_Q F(V - V_H)}{RT}\right)}}$, where
418 $Q_{C, \text{MAX}}$ is the maximum charge, z_Q is the voltage dependency of activation, V_H is the
419 half-activation voltage, T is the absolute temperature (typically 295 K), F is the Faraday's

420 constant, and R is the universal gas constant. $Q_{C, \text{MAX}}$, V_H , and z_Q were determined
421 using least square minimization. $Q_C(V)$ curves were aligned by shifting them along the
422 voltage axis by the mean $\Delta V = (\langle V_H \rangle - V_H)$ to generate a mean curve that did not alter
423 the voltage dependence (Horrigan and Aldrich, 1999). All error estimates are SEM.

424 The Ca^{2+} -induced effect on VSD activation was quantified as the V_H shift relative to “zero”
425 Ca^{2+} condition: $\Delta V_H = V_H([\text{Ca}^{2+}]_i) - V_H(0[\text{Ca}^{2+}]_i)$. For wild-type (WT) BK channel and
426 the RCK Ca^{2+} -sensor mutants (D362A/D367A, M513I and 5D5A), the energetic
427 contribution of Ca^{2+} -binding on resting-active (R-A) equilibrium of the voltage sensor was
428 calculated as changes in Gibbs free energy of VSD activation induced by $100 \mu\text{M}$ Ca^{2+} :

$$429 \quad \Delta\Delta G_V^{Ca} = F \left(z_Q(100 \mu\text{M} [\text{Ca}^{2+}]_i) V_H(100 \mu\text{M} [\text{Ca}^{2+}]_i) - z_Q(0 [\text{Ca}^{2+}]_i) V_H(0 [\text{Ca}^{2+}]_i) \right).$$

430 **Model fitting.**

431 We fit the $Q_C(V, [\text{Ca}^{2+}])$ experimental data using two distinct interaction mechanism
432 between Ca^{2+} -binding sites and voltage sensor (see Scheme I and Scheme II in the **Figure**
433 **2A,B**) within the framework of Horrigan-Aldrich (HA) general allosteric model (Horrigan
434 and Aldrich, 2002). Assumptions and considerations for the equations that describe each
435 one of the Ca^{2+} -VSD interaction schemes are given in the *Supplementary Information*. In
436 terms of the HA allosteric mechanisms, the voltage sensor R-A equilibrium is defined by

437 the equilibrium constant J according to the relation $J = e^{\frac{z_J F(V-V_H)}{RT}} = J_0 e^{\frac{z_J FV}{RT}}$, where J_0

438 is the zero voltage equilibrium constant and z_J the gating charges displacement per
439 voltage sensor. In this fashion, the fraction of the total charge displaced essentially
440 between closed states, $(Q_C(V)/Q_{C, \text{MAX}})$ in the absence of calcium can be written as:

441 $Q_C(V)/Q_{C, \text{MAX}} (\text{Ca}^{2+} \ll K_D) = \frac{1}{1+J^{-1}}$, where K_D is the dissociation constant of the

442 high-affinity calcium-binding site with all voltage sensors at rest and the channel closed.

443 In the presence of saturating Ca^{2+} (100 μM), the equilibrium of the R-A transition J

444 becomes amplified by the allosteric factor E , which defines the coupling between Ca^{2+} -

445 binding sites and voltage sensors, being $Q_C(V)/Q_{C, \text{MAX}} (\text{Ca}^{2+} \gg K_D) = \frac{1}{1+(JE)^{-1}}$

446 and $JE = J_0 e^{\frac{RT \ln(E) + z_j FV}{RT}}$. The $Q_C(V)/Q_{C, \text{MAX}}$ measured in the presence of high

447 $[\text{Ca}^{2+}]$ and “zero Ca^{2+} ” condition at the same voltage (so that J be canceled out) but in the

448 limit where voltage where $J^{-1} \gg 1$ is :

449
$$\frac{Q_C(V)/Q_{C, \text{MAX}} (\text{Ca}^{2+} \gg K_D)}{Q_C(V)/Q_{C, \text{MAX}} (\text{Ca}^{2+} \ll K_D)} \Big|_{(\lim J^{-1} \gg 1)} = \frac{JE}{J} = E$$

450 Thus, the Gibbs free energy perturbation of the voltage sensor R-A equilibrium when the

451 high-affinity binding sites are approximately 100% occupied by Ca^{2+} (100 μM) is a

452 straightforward measure of the allosteric factor E : $E = e^{-\Delta\Delta G_V^{Ca}/RT}$.

453 Based on these conditions, the allosteric parameter E values were calculated and

454 introduced in each of the two Ca^{2+} -VSD interaction models as a fixed parameter. Once E

455 was obtained, the families of $Q_C(V, [\text{Ca}^{2+}])$ curves were simultaneously fitted to the

456 model equations (Equation 3 and Equation 6) (see *Supplementary information*) by

457 minimizing least-squares estimating the z_j , J_0 and K_D parameters for each model. To

458 select the better Ca^{2+} -VSD interaction scheme that describes the experimental data, the

459 model fits were compared according to their Akaike Information Criterion (AIC) (Akaike,

460 1974) values, calculated as $\text{AIC} = 2p - 2 \ln(L)$, where p is the number of free

461 parameters and $\ln(L)$ is the maximum log-likelihood of the model. The best model fitting
462 is that achieving the lowest AIC values. Minimum AIC values were used as model selection
463 criteria.

464 The best model fit of the Ca^{2+} -VSD interaction scheme was extended including two high-
465 affinity Ca^{2+} -binding sites per α -subunit (**Figure 2—figure supplement 2D,E**). The
466 contribution of each Ca^{2+} -binding site to the free energy of the voltage sensor equilibrium
467 may be split in two, such as $E = E_{S1} * E_{S2} = e^{-\left(\Delta\Delta G_V^{Ca(S1)} + \Delta\Delta G_V^{Ca(S2)}\right)/RT}$, where E_{S1}
468 and E_{S2} are the allosteric factor E for the RCK1 and RCK2 sites. Thus, for the global fit of
469 the $Q_C(V, [\text{Ca}^{2+}])$ curves, we constrained the allosteric parameter E_{S1} and E_{S2} obtained
470 experimentally for the RCK2 Ca^{2+} -sensor mutant (5D5A) and RCK1 Ca^{2+} -sensor mutant
471 (D362A/D367A), respectively, as described above. The rest of the parameters $z_j, J_0, K_{D1},$
472 K_{D2} , and G , where K_{D1} and K_{D2} are the dissociation constants of the RCK1 and RCK2
473 sites and G is a cooperativity factor between the two sites within the same α -subunit of
474 the BK channel, were allowed to vary freely.

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625

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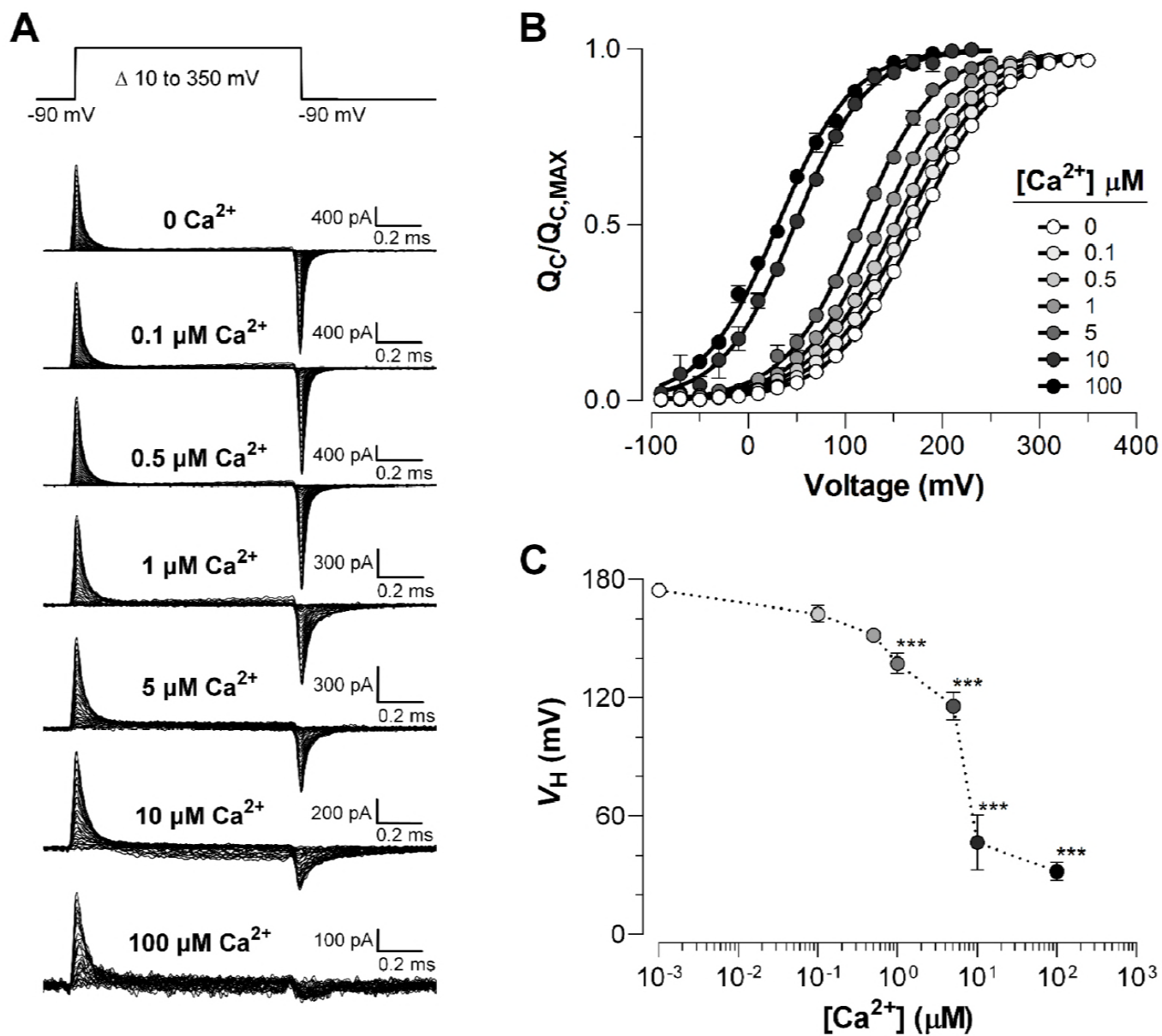
633 **Competing interests**

634 The authors declare no competing financial interests.

635

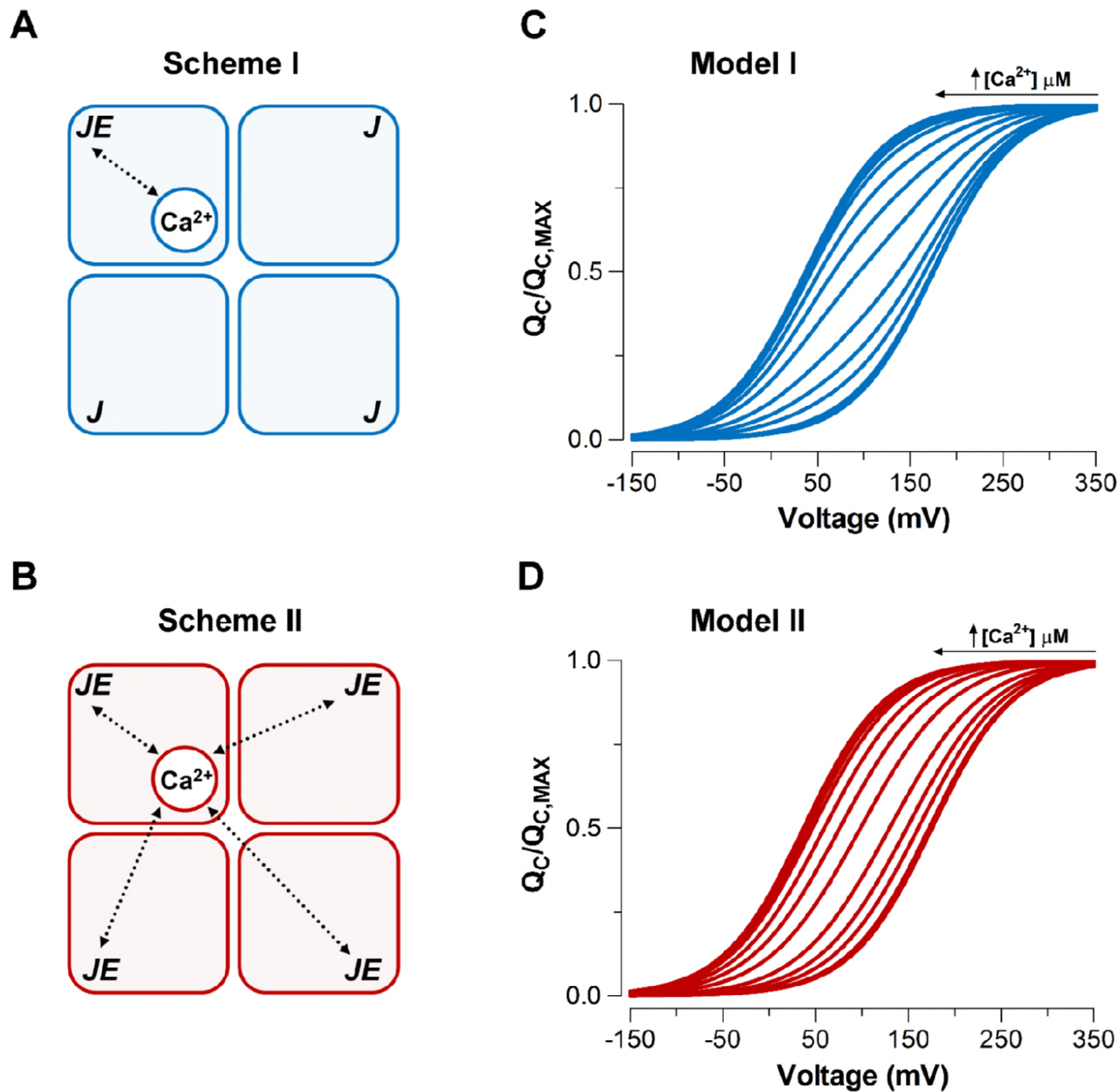
636 **Figures**

637 **Figure 1.**



638

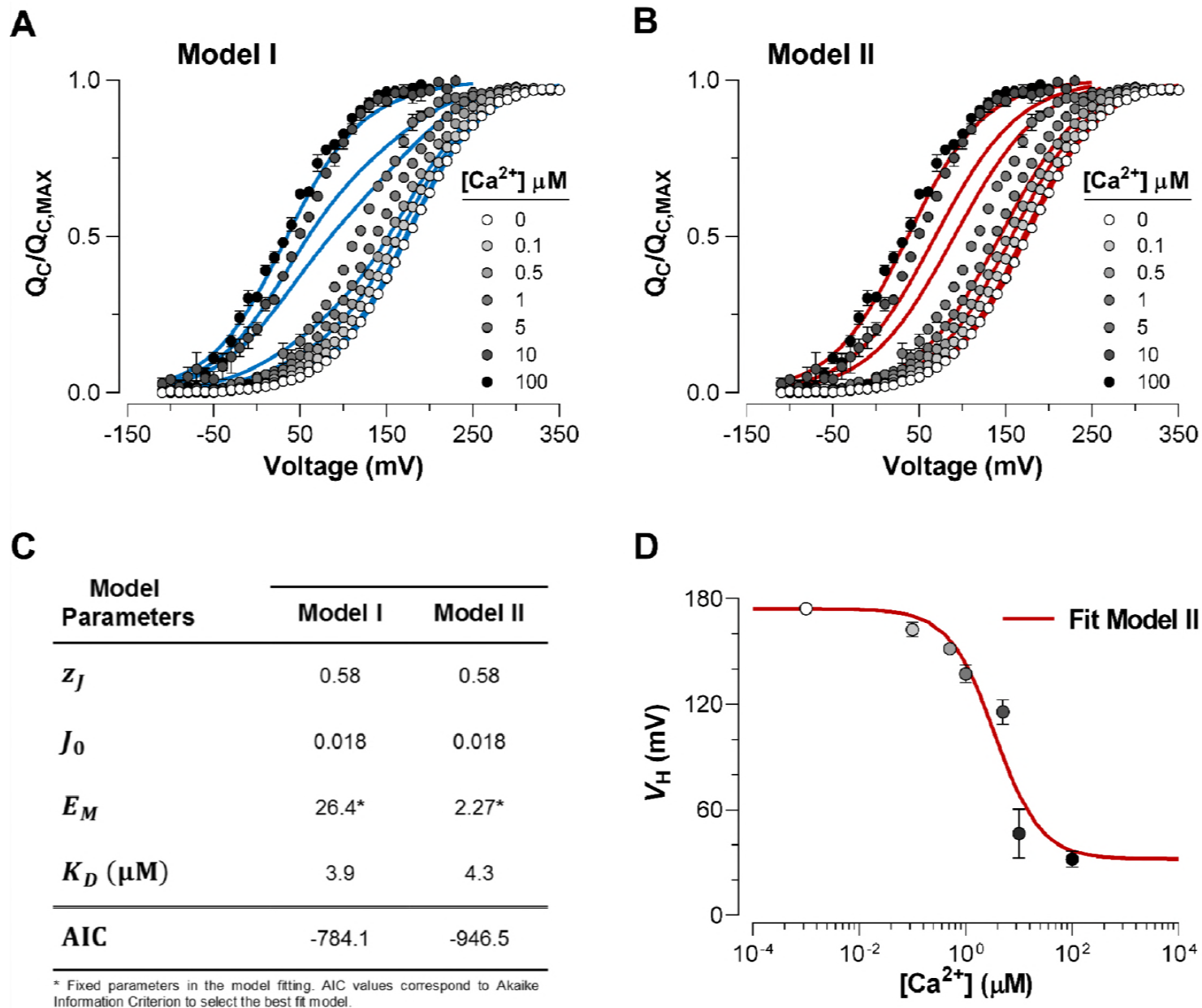
639 Figure 2.



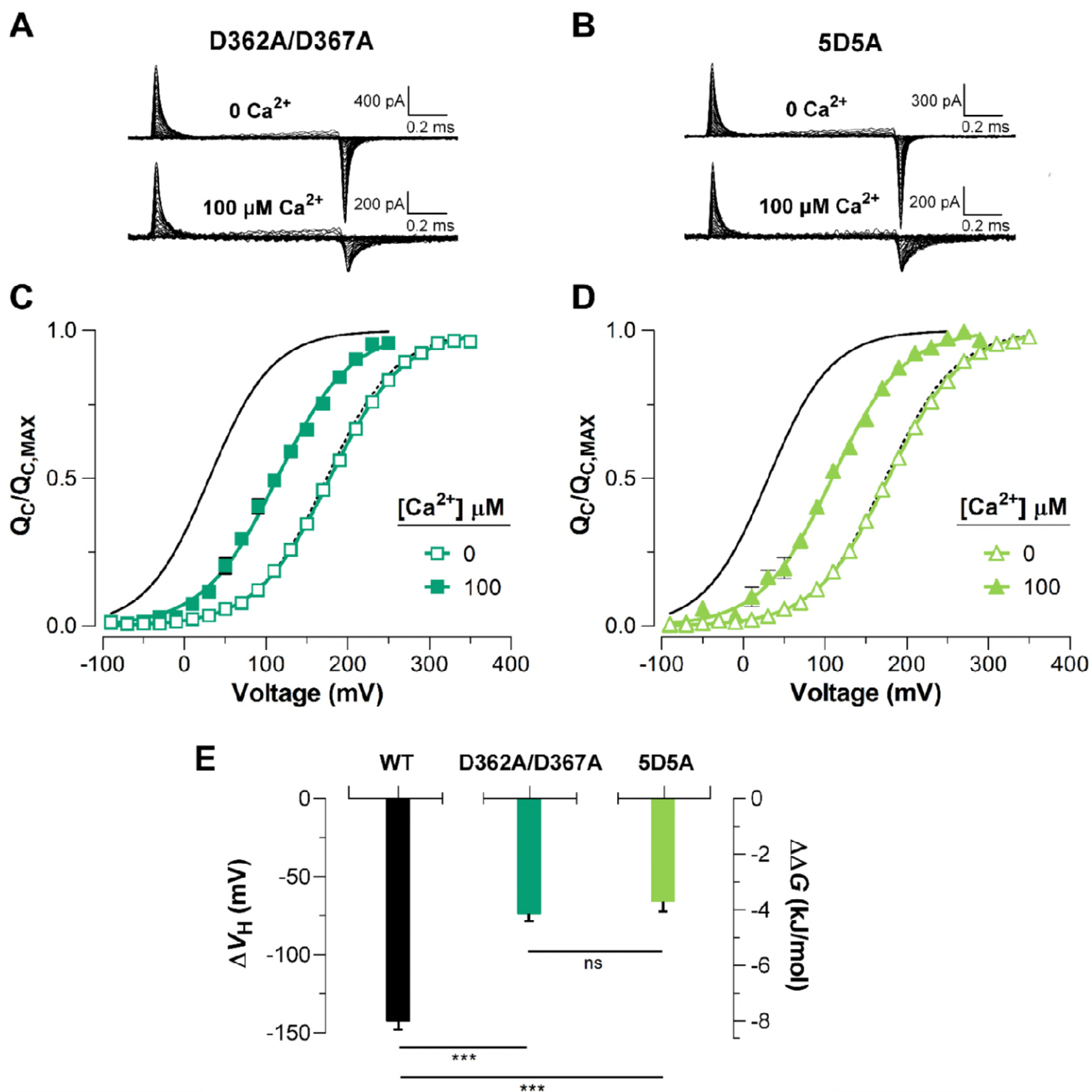
640

641 **Figure 3.**

642



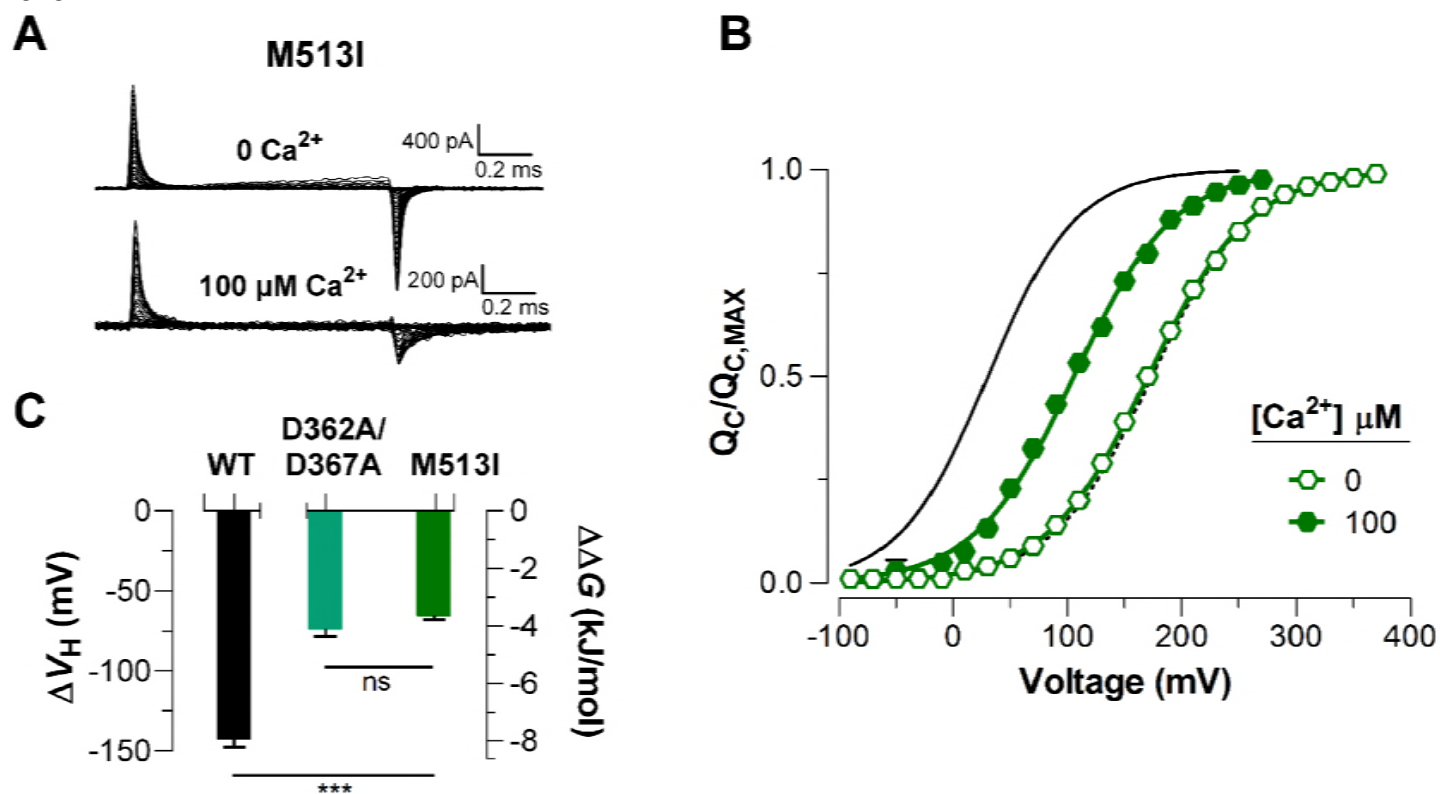
643 **Figure 4.**



644

645 **Figure 5.**

646



647 **Tables**

648 **Table 1. Parameters for the extended Ca²⁺-VSD interaction model (Model II) including**
649 **two high-affinity Ca²⁺-binding sites per α -subunit.**

650

Model Parameters	Model II	
	With cooperativity	Without cooperativity
z_J	0.58	0.59
J_0	0.018	0.018
E_{S1}		1.46*
E_{S2}		1.52*
K_{D1} (μM)	15.6	3.9
K_{D2} (μM)	1.9	2.8
G	2.6	1*
AIC	-949.9	-947.8

* Fixed parameters in the model fitting. AIC values correspond to Akaike Information Criterion to select the best fit model.

651 Legends Figures

652 **Figure 1. Effects of Ca²⁺-binding on VSD activation in BK channels.** (A) Representative
653 gating current (I_G) recordings at different internal Ca²⁺ concentrations (from 0 to 100 μ M). I_G
654 were evoked by the indicated voltage protocol of 1 ms duration. (B) Gating charge-voltage
655 relationships ($Q_C(V)$) were obtained by integrating the fast component for each ON I_G trace.
656 Normalized gating charge data ($Q_C(V)/Q_{C, MAX}$) (mean \pm SEM) were fitted using a single
657 Boltzmann function (solid lines). (C) V_H obtained from the $Q_C(V)$ curves as a function of
658 Ca²⁺ concentration (mean \pm SEM). At zero" Ca²⁺ condition $V_H(0 Ca^{2+}) = 174.5 \pm 2.4$ mV (n
659 = 25), whereas Ca²⁺ binding produce a leftward shift in V_H (ΔV_H): 0.1 μ M Ca²⁺ ($\Delta V_H = -$
660 12.1 ± 3.5 mV, $n = 5$); 0.5 μ M Ca²⁺ ($\Delta V_H = -22.9 \pm 1.8$ mV, $n = 5$); 1 μ M Ca²⁺ ($\Delta V_H = -37.1$
661 ± 3.5 mV, $n = 5$); 5 μ M Ca²⁺ ($\Delta V_H = -58.8 \pm 6.7$ mV, $n = 6$); 10 μ M Ca²⁺ ($\Delta V_H = -127.9 \pm$
662 13.9 mV, $n = 6$); 100 μ M Ca²⁺ ($\Delta V_H = -142.6 \pm 4.5$ mV, $n = 7$). The one-way ANOVA followed
663 by Dunnett's post-hoc test analysis was used to assess statistical significance of the Ca²⁺-
664 induced shifts in V_H (***) $p < 0.001$).

665 **Figure 2. Model-dependent behavior of the $Q_C(V)$ curves based on the CTD-VSD**
666 **interaction mechanisms according to the fractional occupancy of Ca²⁺-binding sites.**
667 (A-B) Cartoons representing two interaction schemes between voltage sensors and Ca²⁺-
668 binding sites (modify from Horrigan and Aldrich (2002)). The Scheme I (A) assume that Ca²⁺-
669 binding only affects the voltage sensor of one α -subunit (E_{M1}). The Scheme II (B) predicts
670 that binding of Ca²⁺ to one α -subunit affects VSD in all subunits equally, increasing the
671 voltage sensor equilibrium constants (J) E_{M2} -fold in all four subunits (E_{M2}^4 , when the four
672 Ca²⁺ sites are occupied). In both schemes, a single Ca²⁺-binding site is considered in each

673 α -subunit. **(C-D)** Predictions of $Q_C(V)$ relationships at different internal calcium
674 concentration (from 0 to 10 mM) by two distinctive interaction mechanisms between Ca^{2+} -
675 binding sites and voltage sensors (Scheme I and Scheme II), respectively. $Q_C(V)$ curves
676 were generated using Equation 4 (blue: Model I) or Equation 6 (red: Model II), and the
677 following set of parameters: $z_J = 0.58$, $J_0 = 0.018$, $K_D = 11 \mu\text{M}$ and $E_{M1} = E_{M2}^4 = 25$.

678 **Figure 3. Dose-dependent effect of Ca^{2+} on voltage sensor activation is predicted by**
679 **a Ca^{2+} -VSD interaction mechanism defining that Ca^{2+} -binding equally affects the VSD**
680 **in all four α -subunits. (A-B)** The experimental $Q_C(V)$ data were fitted with the two possible
681 allosteric interaction mechanisms between voltage and calcium sensors described by the
682 Scheme I and Scheme II. The blue and red lines represent the global fits by Model I and
683 Model II, respectively. The allosteric factor E (E_{M1} and E_{M2}) was constrained to the value
684 obtained from the individual fitting of the $Q_C(V)/Q_{C, \text{MAX}}$ curves at 0 and 100 μM Ca^{2+}
685 (experimental E (E_{exp}) equal to 26.4). The z_J , J_0 and K_D parameters were allowed to vary
686 freely. **(C)** Parameters for the best fits of the $Q_C(V)$ data. Note that the allosteric factor E
687 for Model I (E_{M1}) and Model II (E_{M2}) have different interpretations, being $E_{M2} = E_{exp}$
688 whereas $E_{M2} = \sqrt[4]{E_{exp}}$ given that the four voltage sensor will be altered in 2.3-fold ($E_{M2} =$
689 2.27) with each additional Ca^{2+} bound. Based on the Akaike Information Criterion (AIC), the
690 best model fit to the $Q_C(V, [\text{Ca}^{2+}])$ data is achieved using the Ca^{2+} -VSD interaction scheme
691 described by Model II. **(D)** The Ca^{2+} -dependence of V_H - $Q_C(V)$ curves are superimposed
692 with the predicted V_H by Model II (red line).

693 **Figure 4. The high-affinity Ca^{2+} -binding sites contribute equally to allosteric coupling**
694 **between calcium and voltage sensors in BK channels. (A-B)** Representative gating

695 current (I_G) recordings at 0 and 100 μM of $[\text{Ca}^{2+}]_i$ for the RCK1 site mutant (D362A/D367A)
696 and the RCK2 site mutant (5D5A), respectively. **(C-D)** Gating charge-voltage curves
697 ($Q_C(V)$) were obtained at 0 Ca^{2+} (open symbols) and 100 μM Ca^{2+} (filled symbols) for
698 D362A/D367A and 5D5A mutants, respectively. Boltzmann fitting to the experimental data
699 (mean \pm SEM) is indicated by solid lines ($V_{H(\text{D362A/D367A})} = 178.0 \pm 2.7$ mV, $n = 12$ and
700 $V_{H(5D5A)} = 176.4 \pm 4.6$ mV, $n = 17$ at “zero” Ca^{2+} ; $V_{H(\text{D362A/D367A})} = 104.2 \pm 7.3$ mV, $n = 7$
701 and $V_{H(5D5A)} = 110.8 \pm 6.7$ mV, $n = 6$ at 100 μM Ca^{2+}). For comparison, all $Q_C(V)$ plots
702 include the Boltzmann fit of the $Q_C(V)$ curves for WT at 0 Ca^{2+} (dashed black line) and 100
703 μM Ca^{2+} (solid black line). **(e)** Quantification of the V_H shift (ΔV_H) in the $Q_C(V)$ curves and
704 the free energy change ($\Delta\Delta G_V^{Ca}$) induced by 100 μM Ca^{2+} . The non-parametric t -test was
705 used to evaluate statistical significances between WT BK channel and the RCK sites
706 mutants (** $p < 0.001$; ns: non-significant).

707 **Figure 5. Mutations abolishing Ca^{2+} -sensing by the RCK1 binding-site reduce the**
708 **Ca^{2+} -induced effect on voltage sensors activation similarly.** **(A)** Representative gating
709 current (I_G) recordings at 0 and 100 μM of $[\text{Ca}^{2+}]_i$ for the RCK1 site mutant M513I. **(B)** Gating
710 charge-voltage curves $Q_C(V)$ were obtained at 0 Ca^{2+} and 100 μM Ca^{2+} (open and filled
711 symbols) for the M513I mutant. Boltzmann fitting to the experimental data (mean \pm SEM) is
712 indicated by solid lines ($V_{H(\text{M513I})} = 170.4 \pm 4.4$ mV, $n = 17$ at “zero” Ca^{2+} and $V_{H(\text{M513I})} =$
713 105.0 ± 6.3 mV, $n = 4$ at 100 μM Ca^{2+}). For comparison, the $Q_C(V)$ plot includes the
714 Boltzmann fit of the $Q_C(V)$ curves for WT at 0 Ca^{2+} and 100 μM Ca^{2+} (dashed and solid
715 black line). **(C)** Quantification of the V_H (ΔV_H) shift in the $Q_C(V)$ curves and the free energy
716 change induced by 100 μM Ca^{2+} ($\Delta\Delta G_V^{Ca}$). The non-parametric t -test was used to compare

717 statistical significances between WT BK channel and the RCK1-site mutants (** $p < 0.001$;
718 ns: non-significant).

719 **Supplementary Information**

720 **Assumptions and model predictions.** We assume that the four voltage sensors act
721 independently transiting between two states, resting (R) and active (A), governed by the
722 voltage-dependent equilibrium constant J . The R–A equilibrium is displaced toward the
723 active state by membrane depolarization generating a fast gating charge movement (Q_C)
724 before channels opening. Additionally, the Ca^{2+} -binding to high-affinity sites shifts the
725 voltage sensor equilibrium toward their active configuration through an allosteric coupling
726 described by the factor E (**Figure 2—figure supplement 1A**). By assuming the simplified
727 standard model for the BK channels (Horrigan and Aldrich, 2002), where each α -subunit has
728 a single Ca^{2+} -binding site, we established the possible states and their connections through
729 which each voltage sensor transit in presence of Ca^{2+} (**Figure 2—figure supplement 1B;C**)
730 following the CTD-VSD interaction mechanisms described by the Scheme I and Scheme II
731 (**Figure 2A,B**).

732 For Scheme I, in which Ca^{2+} -binding sites and voltage sensors can only interact within the
733 same α -subunit, the activation of each VSD can occur through the R_0 - A_0 or R_1 - A_1 transitions
734 according to the functional state of the Ca^{2+} site (unbound or Ca^{2+} bound). The equilibrium
735 of such transitions is governed by J or JE_{M1} , respectively (**Figure 2—figure supplement**
736 **2B**). In the case of Scheme II, in which binding of Ca^{2+} to a single α -subunit affects the four
737 voltage sensors equally, the R-A equilibrium of each VSD would be affected by the number
738 of Ca^{2+} bound in the channel (0-4) depicted in the model (Model II) as five possible R-A
739 transitions. According to this model, the J constant increase E_{M2} -fold for each occupied Ca^{2+}
740 site (**Figure 2—figure supplement 1C**). For both schemes, the horizontal transitions R-R
741 and A-A represent the Ca^{2+} -binding equilibrium (K or KE) when the VSD is in the resting or

742 active conformation, respectively. The K equilibrium constant is defined as the
743 bound/unbound probability ratio for each Ca^{2+} -binding site and depends on Ca^{2+}
744 concentration ($[\text{Ca}^{2+}]$) and the Ca^{2+} dissociation constant (K_D): $K = [\text{Ca}^{2+}]/K_D$.

745 Here, we assume that the voltage sensor movement at ON-gating currents is in equilibrium
746 relative to the binding of Ca^{2+} . The assumption is reasonable since the Ca^{2+} -binding rate
747 constant estimated for BK channel is about $10^8 \text{ M}^{-1}\text{s}^{-1}$ (Hou et al., 2016) implying that at 10
748 μM internal Ca^{2+} the association time constant is 1 ms. Thus, Ca^{2+} binding at this Ca^{2+}
749 concentration proceeds at a pace about 33-fold slower than the voltage sensor movement
750 ($\sim 30 \mu\text{s}$). Based on this consideration, the R-A transitions in the models would be
751 predominant transitions whose proportion will be determined by the $[\text{Ca}^{2+}]$ and K_D .
752 Therefore, predictions of the $Q_C(V)$ curves at different Ca^{2+} concentrations for Model I and
753 Model II were based on a given fractional occupancy of Ca^{2+} sites established by the
754 probability of Ca^{2+} bound (b) and unbound ($1 - b$) for each Ca^{2+} -sensor, and the energetic
755 contribution to VSD equilibrium.

756 Simulations of the $Q_C(V)$ curves using the Scheme I (Model I) were obtained using the
757 equation

$$758 \quad \frac{Q_C(V)}{Q_{C, \text{MAX}}} = (1 - b) \left(\frac{1}{1 + J^{-1}} \right) + b \left(\frac{1}{1 + (JE_{M1})^{-1}} \right) \quad (1);$$

759 where

$$760 \quad b = \frac{1}{1 + K^{-1}} = \frac{1}{1 + \frac{K_D}{[\text{Ca}^{2+}]}} = \frac{[\text{Ca}^{2+}]}{[\text{Ca}^{2+}] + K_D} \quad (2);$$

761 and

762
$$J = J_0 e^{\frac{z_J F V}{RT}} \quad (3)$$

763 Substituting b and J into Equation (1), the Ca^{2+} -dependent voltage sensor activation for
 764 Model I is given by the equation

765
$$\frac{Q_C(V)}{Q_{C, \text{MAX}}} = \left(\frac{K_D}{[\text{Ca}^{2+}] + K_D} \right) \left(\frac{1}{1 + \frac{e^{\frac{-z_J F V}{RT}}}{J_0}} \right) + \left(\frac{[\text{Ca}^{2+}]}{[\text{Ca}^{2+}] + K_D} \right) \left(\frac{1}{1 + \frac{e^{\frac{-z_J F V}{RT}}}{J_0 E_{M1}}} \right) \quad (4)$$

766 Thus, the $Q_C(V)$ curves are determined by the proportion of two functional VSD populations
 767 with a distinctive effect (unliganded effect or Ca^{2+} -saturated effect) Consequently, the
 768 $Q_C(V)$ curves are represented by a weighted sum of two Boltzmann functions.

769 Meanwhile, for the concerted CTD-VSD interaction Scheme II (Model II), the $Q_C(V, [\text{Ca}^{2+}])$
 770 curves would be determined using the general equation:

771
$$\frac{Q_C(V)}{Q_{C, \text{MAX}}} = \sum_{x=0}^n \binom{n}{x} (1-b)^{n-x} b^x \left(\frac{1}{1 + (J E_{M2}^x)^{-1}} \right) \quad (5)$$

772 The expression in the first bracket represents the fraction of VSD belonging to a channel
 773 with x (0 to 4) Ca^{2+} bound, according to a binomial probability distribution. Thus, the $Q_C(V)$
 774 curves result in a weighted sum of five distinct Boltzmann functions corresponding to the
 775 five possible R-A transitions (**Figure 2—figure supplement 1C**). By stating $n = 4$ because
 776 the tetrameric symmetry of the channels, and substituting b and J into the previous equation
 777 (Equation 5) we have

$$778 \quad \frac{Q_C(V)}{Q_{C, \text{MAX}}} = \sum_{x=0}^4 \binom{4}{x} \left(\frac{K_D}{[Ca^{2+}] + K_D} \right)^{4-x} \left(\frac{[Ca^{2+}]}{[Ca^{2+}] + K_D} \right)^x \left(\frac{1}{1 + \frac{e^{-zJFV/RT}}{J_0 E_{M2}^x}} \right) \quad (6)$$

779 It should be noted that at limiting Ca^{2+} conditions, both schemes become equivalent where
 780 the VSD activation is characterized by a single Boltzmann function. At zero Ca^{2+} , the $Q_C(V)$
 781 curves are described by

$$782 \quad \frac{Q_C(V)}{Q_{C, \text{MAX}}} = \left(\frac{1}{1 + \frac{e^{-zJFV/RT}}{J_0}} \right),$$

783 whereas Ca^{2+} saturating concentration J is multiply by the allosteric factor E , where $E =$
 784 $E_{M1} = E_{M2}^4$ depending on the model (Model I or Model II):

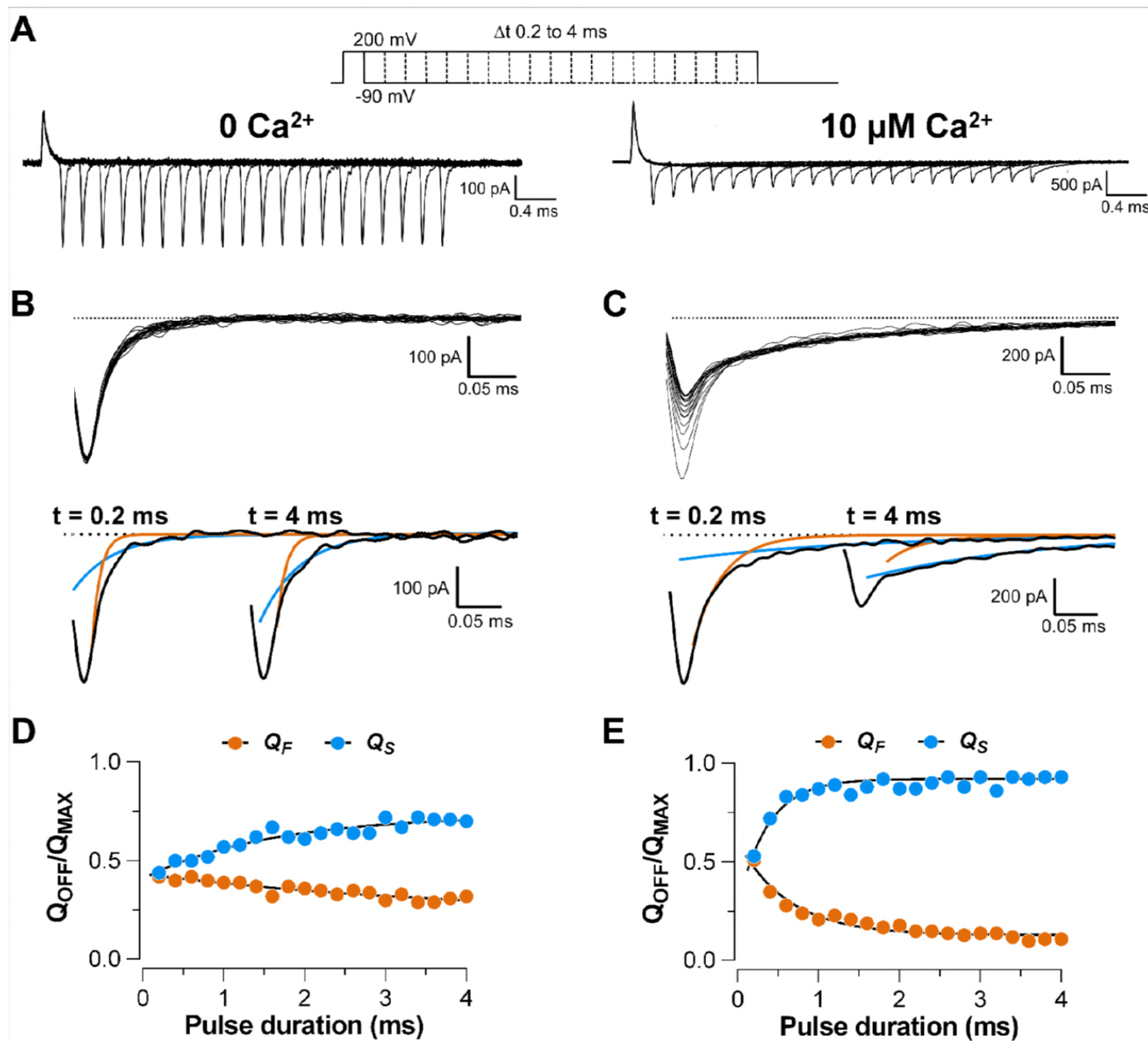
$$785 \quad \frac{Q_C(V)}{Q_{C, \text{MAX}}} = \left(\frac{1}{1 + \frac{e^{-zJFV/RT}}{J_0 E}} \right)$$

786 Given that each α -subunit has two Ca^{2+} -binding sites, we expanded the CTD-VSD
 787 interaction Scheme II (**Figure 2—figure supplement 1C**) considering the existence of two
 788 Ca^{2+} -binding sites (**Figure 2—figure supplement 1D,E**). The Model II includes the
 789 energetic contribution of RCK1 and RCK2 Ca^{2+} -sites to the VSD activation. The factor $E =$
 790 $E_{S1} * E_{S2}$ where E_{S1} and E_{S1} are the allosteric coupling between the VSD and the RCK1
 791 Ca^{2+} -site and RCK2 Ca^{2+} -site, respectively. The K_1 and K_2 constants define the
 792 bound/unbound transition for each RCK1 and RCK2 sites being $K_1 = [Ca^{2+}]/K_{D1}$ and

793 $K_2 = [Ca^{2+}] / K_{D2}$. Assuming that the Ca^{2+} sensors of distinct α -subunit do not interact,
794 we only consider intrasubunit cooperativity between the RCK1 and RCK2 sites defined by
795 the factor G . Thus, the occupancy of one RCK site will affect Ca^{2+} -binding equilibrium to the
796 other RCK site in the α -subunit (GK_1 and GK_2) (**Figure 2—figure supplement 1E**). The
797 equilibrium J of the VSD increase E_{S1} -fold and E_{S2} -fold for the each Ca^{2+} bound to RCK1
798 and RCK2 sites, respectively, reaching to $JE_{S1}^4 E_{S2}^4$ when the eight Ca^{2+} sites are occupied.

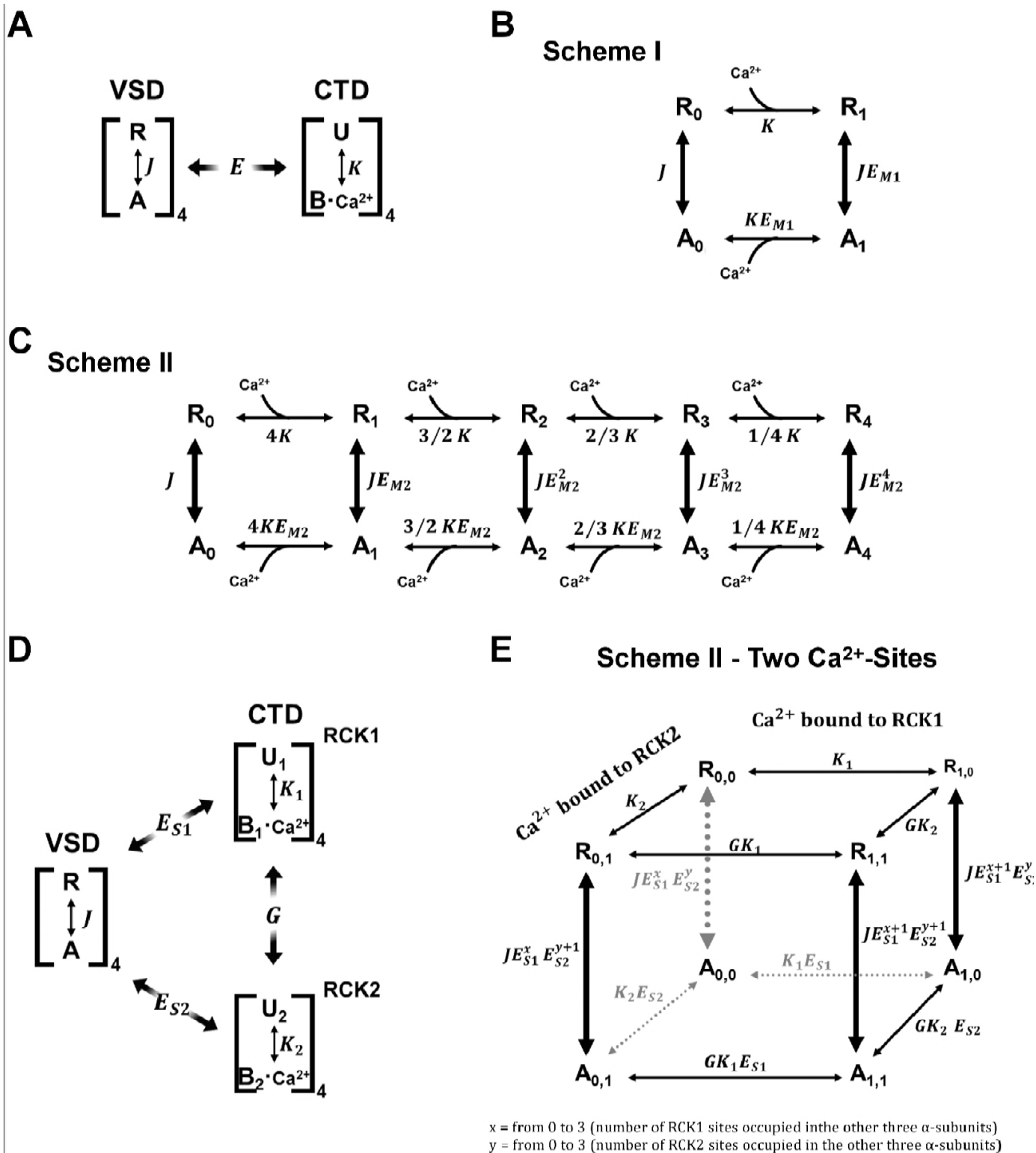
799 **Supplementary Figures**

800 **Figure 1—figure supplement 1.**



801

802 Figure 2—figure supplement 1.



803

804 Legends Supplementary Figures

805 **Figure 1—figure supplement 1. Ca²⁺ increase the slow component of the OFF gating**
806 **currents. (A)** Gating current (I_G) recordings evoked by 200 mV pulses with different
807 durations (from 0.2 to 4 ms) at 0 and 10 μM $[\text{Ca}^{2+}]$ conditions, respectively. **(B-C)** The top
808 panels show the superimposed traces of the I_G -OFF recorded at -90 mV evidencing a
809 decrease in amplitude and a slower decay of the OFF current as the duration of the pulse
810 increases at 10 μM Ca^{2+} . The dashed line represents the baseline for each experiment. I_G -
811 OFF were fitted with an exponential function of two-components (fast and slow
812 components). I_G -OFF traces at 0.2 ms and 4 ms pulse duration are displayed for each Ca^{2+}
813 condition. Orange and blue lines correspond to fast and slow components of the two-
814 exponential fits, respectively: **(B)** “zero” Ca^{2+} ($\tau_F = 10 \mu\text{s}$ and $\tau_S = 44 \mu\text{s}$) and **(C)** 10 μM Ca^{2+}
815 ($\tau_F = 25 \mu\text{s}$ and $\tau_S = 212 \mu\text{s}$). **(D-E)** The relative amplitude of the OFF-charge components,
816 the fast (Q_F) and slow (Q_S) charge components were plotted against the pulse duration and
817 fitted with an exponential function representing the time course of the opening of the
818 channel: **(D)** “zero” Ca^{2+} ($\tau_{0\text{Ca}^{2+}} = 1.8 \text{ ms}$) and **(E)** 10 μM Ca^{2+} ($\tau_{10 \mu\text{M}} = 536 \mu\text{s}$).

819 **Figure 2—figure supplement 1. Kinetic models of the VSD activation according to the**
820 **CTD-VSD interaction schemes. (A)** Sub-scheme describing calcium and voltage allosteric
821 interaction for closed channels. The VSD transit between two resting (R) and active (A)
822 configuration governed by the equilibrium constant J , whereas each Ca^{2+} site undergoes
823 unbound (U) - Ca^{2+} bound (B) transitions governed by the equilibrium constant K . The
824 allosteric factor E accounts for the coupling between the calcium and voltage sensors (CTD-
825 VSD) **(B-C)** VSD kinetic models in presence of Ca^{2+} according to CTD-VSD interaction
826 schemes I and II (**Figure 2A,B**), respectively, where the vertical transitions (R-A) represent

827 the VSD movement and the horizontal transitions (R-R and A-A) are Ca^{2+} -binding reactions
828 when the VSD is in the resting or active conformation. For the Scheme I (**B**), each VSD can
829 undergo $R_0\text{-}A_0$ or $R_1\text{-}A_1$ transitions depending on the unbound or bound state of the Ca^{2+} site
830 in the α -subunit, respectively. Thus, the $R_1\text{-}A_1$ equilibrium is defined by J increased E_{M1} -fold
831 (JE_{M1}). For the Scheme II (**C**), the $R_0\text{-}A_0$ to $R_4\text{-}A_4$ transitions represent the VSD equilibrium
832 with 0, 1, 2, 3, and 4 occupied Ca^{2+} sites in the channel. Thus, for each Ca^{2+} bound the
833 equilibrium constant J increase E_{M2} -fold reaching to JE_{M2}^4 when the four Ca^{2+} sites are
834 occupied. The thickness of the arrows indicates the probability of transitions. (**D**) General
835 sub-scheme of the CTD-VSD interaction including two Ca^{2+} sites for each CTD (RCK1 and
836 RCK2 sites). For each RCK1 and RCK2 site the unbound- Ca^{2+} bound transitions are
837 governed by the equilibrium constants K_1 and K_2 . The factor G describe the cooperativity
838 between the sites within the same α -subunit; and the E_{S1} and E_{S2} factors define the
839 allosteric coupling between the RCK1 and RCK2 sites and the VSD, respectively. (**E**)
840 Schematic representation of VSD kinetic model according to the extended version of the
841 Scheme II (**C**) accounting for both RCK1 and RCK2 Ca^{2+} -sites on each α -subunit. For sake
842 of simplicity, are only depicted the VSD transitions depending on the unbound or bound state
843 of the RCK sites within the same α -subunit: RCK1 site ($R_{1,0}\text{-}A_{1,0}$), RCK2 site ($R_{0,1}\text{-}A_{0,1}$) and
844 both sites ($R_{1,1}\text{-}A_{1,1}$).