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2 **Modeling enamel matrix secretion in mammalian teeth**

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17 Author Contributions: T.J.H., S.S.S. and J.J. conceived the study, T.J.H. constructed the model,
18 A. H. suggested the velocity extension scheme and provided input on the algorithms, S.S.S.,
19 I.J.C. and L.T. collected and processed the empirical data, T.J.H., S.S.S. and J.J. performed the
20 simulations, analyzed the results and wrote the paper. All authors discussed the results and
21 provided input and scientific interpretations on the manuscript.

22 **Abstract**

23 The most mineralized tissue of the mammalian body is tooth enamel. Especially in species with
24 thick enamel, three-dimensional (3D) tomography data has shown that the distribution of
25 enamel varies across the occlusal surface of the tooth crown. Differences in enamel thickness
26 among species and within the tooth crown have been used to examine taxonomic affiliations,
27 life history, and functional properties of teeth. Before becoming fully mineralized, enamel
28 matrix is secreted on the top of a dentine template, and it remains to be explored how matrix
29 thickness is spatially regulated. To provide a predictive framework to examine enamel
30 distribution, we introduce a computational model of enamel matrix secretion that maps the
31 dentine topography to the enamel surface topography. Starting from empirical enamel-dentine
32 junctions, enamel matrix deposition is modeled as a diffusion-limited free boundary problem.
33 Using laboratory microCT and synchrotron tomographic data of pig molars that have markedly
34 different dentine and enamel surface topographies, we show how diffusion-limited matrix
35 deposition accounts for both the process of matrix secretion and the final enamel distribution.
36 Simulations reveal how concave and convex dentine features have distinct effects on enamel
37 surface, thereby explaining why the enamel surface is not a straightforward extrapolation of the
38 dentine template. Human molar simulations show that even subtle variation in dentine
39 topography can be mapped to the enamel surface features. Mechanistic models of extracellular
40 matrix deposition can be used to predict occlusal morphologies of teeth.

41

42 **Introduction**

43 Most mammalian species have their teeth covered by a layer of highly mineralized enamel. The
44 thickness of the enamel layer relative to the tooth size ranges from thin to very thick. These
45 differences among species, and also increasingly within the tooth crown, have been informative
46 in studies focused on functional properties of teeth, taxonomy, and life history (1-9). Even
47 though mutations in genes required for enamel matrix secretion and maturation are known to
48 affect the enamel thickness in mammals (10), relatively little is known about the regulatory
49 changes that might underlie the variation in enamel thickness among populations or species

50 (1,11,12). Even less is known about the regulation of enamel thickness variation within the
51 tooth crown, which contrasts with the increasing availability of 3D tomography data on various
52 species. Analyses of such tomography data show that even though the enamel surface
53 topography reflects the enamel-dentine junction (EDJ) topography, the enamel surface is not a
54 simple extrapolation of the EDJ shape (13-15). Because enamel distribution is not
55 developmentally remodeled after formation, and because the internal structure of mineralized
56 enamel retains developmental information, tomography data of fully formed teeth can be used to
57 examine mechanisms underlying variation in enamel thickness. To provide mechanistic insights
58 into the regulation of enamel thickness, here we combine tomography data on enamel
59 distribution with a computational approach and introduce a model to simulate enamel matrix
60 secretion.

61

62 **Results**

63 **The Model Principles and Simulation of Artificial Shapes.** The enamel matrix is secreted by
64 specialized epithelial cells, the ameloblasts, which depart from the EDJ. The EDJ is defined by
65 the mesenchymal dentine matrix, whose secretion begins first (Fig. 1A). For empirical tests, we
66 used EDJs of real teeth as the starting point to simulate matrix secretion (Fig. 1A). Matrix
67 deposition is modeled as a diffusion-limited free boundary problem, motivated by the classical
68 Stefan problem that models phase transition of undercooled liquid by assuming that the rate of
69 phase transition from liquid to solid is limited by a diffusion process (see Methods and
70 Supplementary Information) (16,17). Here we similarly assume that the growth of the matrix
71 front is a diffusion-limited process: The advancement of the ameloblast layer departing from the
72 EDJ is assumed to be limited by the diffusion of nutrition, by which we refer communally to all
73 the factors that ameloblasts require for the secretion of the matrix (Fig. 1B). The model

74 parameters adjust the nutrition diffusion rate, the amount of nutrition required for growth, and
75 the interfacial tension or stiffness of the advancing ameloblast layer (Methods). Model
76 equations are solved using the finite element method, and the matrix interface (the ameloblast
77 layer) is tracked using the level set method (Supplementary Information). The source code of
78 the Matlab implementation of the model is freely available (Methods). For computational
79 efficiency, the model is implemented in 2D and 3D reconstructions are obtained by simulating
80 multiple sections that are combined into volumes.

81 The fundamental component of the model is the assumption that the growth of the matrix
82 requires a net influx of a diffusing nutrient substance. At the initial stage nutrition is assumed to
83 be present exterior to the dentine, and the nutrient is also replenished by a constant background
84 source (Methods). By controlling the relative amount of background production, we examine
85 two hypothetical matrix secretion processes. The primary process tested is a diffusion-limited
86 secretion in which concave surfaces are progressively exaggerated as the features protruding
87 into the nutrition-rich domain receive more nutrition than the concavities (Fig. 1C). An
88 alternative process assumes excess availability of nutrition through strong background
89 production, leading to a moving boundary of uniform thickness (Fig. 1D). This latter process in
90 fact closely approximates a simple geometric extrapolation of matrix thickness from the EDJ,
91 which we use as a null hypothesis to demonstrate the non-linearity of the matrix deposition.
92 Simulations of matrix secretion using a synthetic EDJ shape show that whereas convex EDJ
93 surfaces result in relatively linear extrapolation of the enamel surface in both simulations (Fig.
94 1C, D), concave surfaces of diffusion-limited simulations behave nonlinearly (Fig. 1C).
95 Additionally, reducing interfacial tension in the simulations increases small undulations in the
96 moving front (Fig. 1E), suggesting that lowered stiffness of the ameloblast layer may underlie
97 crenulated enamel found in taxa such as *Chiropotes* (saki monkeys) with relatively smooth EDJ
98 (14).

99 **Diffusion-Limited Simulations Predict Enamel Distribution on Pig Molar Teeth.** To
100 simulate enamel matrix secretion in real teeth, first we focused on domestic pig molar teeth that
101 exhibit substantial variation in enamel thickness and EDJ topography (Figs 1A, 2A, ref. 18).
102 EDJ and enamel surface shapes were reconstructed from microCT scans of first lower molars
103 (Fig. 2A, Methods). From the data, horizontal slices of cusps were extracted (Fig. 2A) and the
104 EDJs were used as the starting point for the simulations. The horizontal plane represents a
105 relatively synchronous front of enamel matrix secretion and captures the complex EDJ
106 morphology of the pig molars (18). The simulations show that the diffusion-limited process
107 reproduces the deep narrow furrows or fissures present on the concave sides of the real cusps
108 (Fig. 2A, B). In contrast, these features are lost when the enamel matrix is geometrically
109 extrapolated from the EDJ, or when modeling with excess background nutrition (Fig. 2C).
110 These results support the role of a diffusion-limited-like process in the regulation of enamel
111 matrix secretion, and underscore the distinct effects that the convex and concave EDJ features
112 impose on the enamel distribution. Indeed, whereas cusps of individual pigs vary in their
113 detailed cusp morphology, the overall distribution of convex and concave features is conserved
114 (Fig. S1).

115 Next we simulated the matrix secretion in a whole cusp with both convex and concave
116 features (Methods). A 3D reconstruction of these simulations show that the diffusion-limited
117 model captures the overall enamel thickness patterns in which concavities show reduced enamel
118 thickness whereas ridges show increased enamel thickness (Fig. 3, Fig. S2). A small ridge
119 present in the middle of a dentine concavity results in a local thickening of the enamel within an
120 otherwise deep fissure (arrow heads in Fig. 3A-C), a feature completely lost in geometrically
121 extrapolated surfaces (Fig. 3D).

122

123 **Diffusion-Limited Simulations Reproduce the Progression of Matrix Secretion.** In addition
124 to the distribution of enamel in fully formed tooth, the diffusion-limited simulations can be used
125 to examine the progression of the matrix secretion process itself. The successive positions of the
126 matrix-secreting front during development is recorded in teeth by incremental lines (laminations
127 or striae of Retzius, ref. 9) that are broadly analogous to growth rings in trees (19). These are
128 preserved in mature enamel and can be observed from thin sections or through phase contrast
129 synchrotron imaging (19,20). We obtained synchrotron data from a pig molar and compared the
130 positions of individual incremental lines in convex cusp ridges with the lines in cusp concavities
131 (Fig. 4A). Both the virtual incremental lines of diffusion-limited simulations and empirical
132 incremental lines show initially relatively uniform distances from the EDJ, but this uniformity
133 disappears and the differences between ridges and valleys become progressively larger as the
134 secretion accelerates in the ridges and slows down in the valleys (Fig. 4). These results are
135 suggestive that in addition to the final patterns of enamel distribution, the diffusion-limited
136 model captures aspects of the actual secretion process.

137

138 **Subtle EDJ Concavities Are Sufficient to Produce Complex Enamel Surface Features.** Pigs
139 are an example of species with relatively pointed molar cusps, allowing the simulation of matrix
140 secretion in the horizontal plane. In contrast, molars of primates with thick enamel, including
141 humans, typically have relatively low cusp relief. Therefore, to capture matrix secretion of
142 human molar morphology, we run the diffusion-limited simulations vertically. Because the
143 enamel becomes globally thinner towards the tooth neck, or lower portion of the tooth crown,
144 we implemented a nutrient sink at the base (Methods). The sink decreases the rate of matrix
145 formation towards the base of the crown, thereby approximating crown formation and the apical
146 decline in matrix secretion before the initiation of root development (ref. 9, Fig. 5A). The

147 simulations show the subtle waviness of the human EDJ, with manly concave ripple-like
148 features, is enough to produce the characteristic undulations of the enamel surface (Fig. 5B,C).
149 These features are further refined by simulations using lateral braces mimicking the presence of
150 adjacent teeth and alveolar bone (Fig. 5B), in agreement with the suggested role of the
151 surrounding tissues in the regulation of tooth shape and mineralization (21,22). Taken together,
152 these simulations indicate that even subtle EDJ features present in many hominids are important
153 for the functional surface morphology of the tooth.

154

155 **Conclusions**

156 Our diffusion-limited model suggests an objective basis for mapping the EDJ morphology to
157 enamel surface morphology. The simulations point to the critical role of convex and concave
158 EDJ surface features in the regulation of final tooth surface morphology. These results also
159 indicate that complex patterns of enamel thickness on a tooth crown can result from a single
160 developmental process, without the need to evoke specific control or explanations for individual
161 thickness features. Combined with in-depth analyses of enamel formation rates (4, 9, 18) and
162 isotope compositions (23, 24) obtainable from sections, our model should help to move studies
163 using enamel thickness towards more mechanistic and predictive science. This approach should
164 also be applicable to other systems with extracellular matrix secretion, or organs in which
165 directional tissue growth may be diffusion limited. Diffusion-limited free boundary problems
166 have a long history in mathematics (16, 17, 25), and as shown here, they can contribute to
167 solving biological problems.

168

169

170 **Materials and Methods**

171 **Diffusion-limited model.** We solve the model using a finite element method algorithm
172 presented in ref. 26. For implementation details and source code, see Supplementary
173 Information and <https://github.com/tjhakkin/biomatrix>.

174 **Dental data and processing.** Molars were extracted, stored and microCT imaged using the
175 protocols, and pig and human molar samples described in ref. 18. The voxel resolutions were 10
176 to 24 μm (pig molars) and 17 μm (human molars), and downsampled to 44 μm (pig molars) and
177 66 μm (human molars). Synchrotron data was collected at beamline ID19 of the European
178 Synchrotron Radiation Facility, with voxel resolution 2.24 μm , keV = 91, and 6000 projections
179 in 4x accumulation mode. Synchrotron data reconstruction used Paganin style single
180 propagation distance phase contrast. All the image processing steps after primary tomography
181 reconstructions were carried out with Fiji 2.0 (27). To digitize EDJs for simulations, EDJs in
182 each individual section were traced with a freehand selection, and the area was converted to a
183 line (Edit/Selection/Area to Line). The line was then interpolated with an interval of 10 pixels
184 (Edit/Selection/Interpolate), fitted to a spline (Edit/Selection/Fit spline), and adjusted manually
185 to follow the EDJ if needed. The splines were saved in ROI Manager (Analyze/Tools/ROI
186 manager/more/save). The splines were saved as XY coordinates (File/Save As/XY Coordinates)
187 that were converted to level sets using a Python script, included with the source code. During
188 the conversion the spatial node density and the relative size of the EDJ within the domain were
189 also defined. To scale different sized EDJs uniformly (e.g., when EDJs become smaller towards
190 the cusp tip), two small triangles placed in diagonally opposing corners were included in each
191 level set conversion. To enhance the visualization of the incremental lines in synchrotron
192 reconstructions, three adjacent slices were averaged.

193 **Simulations and analyses.** The main simulation parameters are listed in Table S1. Simulation
194 output for each step is an image file. The pig trigonids and talonids were simulated separately

195 (Fig. 2B). To compensate for the isolated entoconid cusp being larger (Fig. 3) than when part of
196 the talonid (Fig. 2), interfacial tension and number of iterations were decreased in the individual
197 cusp simulations. For simulations of multiple sections (Figs 3, 5C), all the sections of the
198 analyzed step were merged into a stack in Fiji. For the pig molar cusp (Fig. 3), every second
199 microCT slice (20 μm interval, 51 slices), and for the human molar (Fig. 5C), every fifth slice
200 (66 μm interval, 27 slices) was simulated. We used the basal sink to approximate developmental
201 progression in the vertical simulations. Because intercuspal regions lack the sink, vertical
202 simulations slightly exaggerate enamel thickness in valleys relative to cusp tips. Geometric
203 extrapolation of enamel thickness was obtained in Fiji by fitting a fixed sized circle along the
204 EDJ (Process/Morphology/Gray Morphology/Dilate). To visualize enamel thickness in 3D, the
205 EDJ and enamel surfaces were exported from Fiji (surfaces exported as Wavefront .obj from 3D
206 Viewer plugin) and imported into Meshlab (<http://meshlab.sourceforge.net/>). In Meshlab,
207 Hausdorff distance was used to compare distances between two surfaces (28). The distances
208 were calculated after smoothing the meshes with Laplacian smooth (3 steps). All 3D
209 visualizations use orthographic projections.

210

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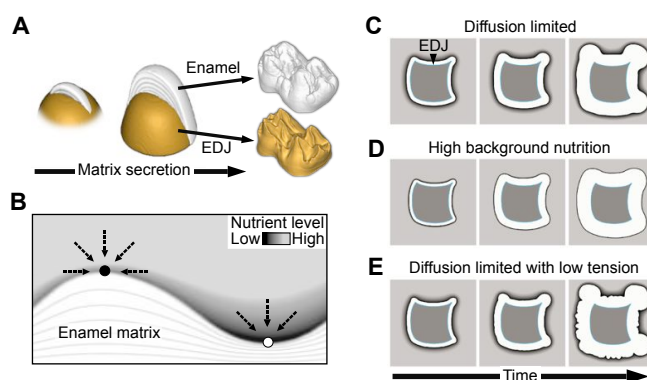
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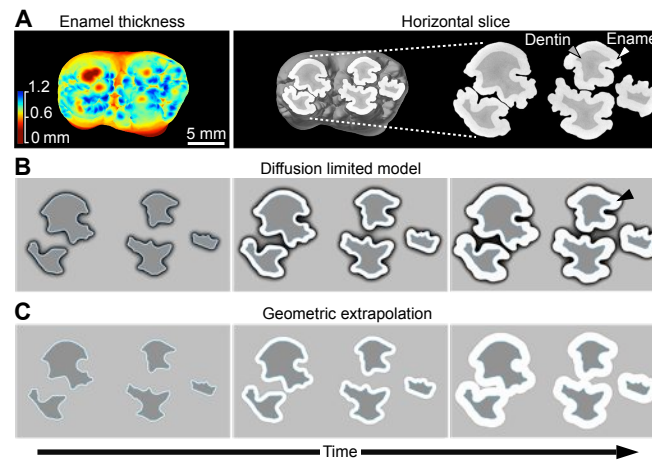


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297 **Figure 1.** Modeling tooth enamel matrix secretion. (A) A schematic illustration of a cross
298 section of enamel matrix being secreted on the top of dentine. In real teeth (a pig molar on the
299 right), the enamel surface is not a linear representation of the dentine template (EDJ). (B) In a
300 diffusion-limited model, differences in surface topography lead to ridges (black circle) receiving
301 more nutrition (dashed arrows) than valleys (white circle). (C) Starting from a synthetic EDJ
302 shape, diffusion-limited matrix deposition advances faster in convex than concave features. (D)
303 Excess production of nutrition overcomes diffusion-limited effects and produces a uniform
304 distribution of matrix. (E) Reducing surface tension of simulation in c results in crenulated
305 matrix surface. For details of the model, see Methods, and parameters used in simulation are in
306 Table S1.

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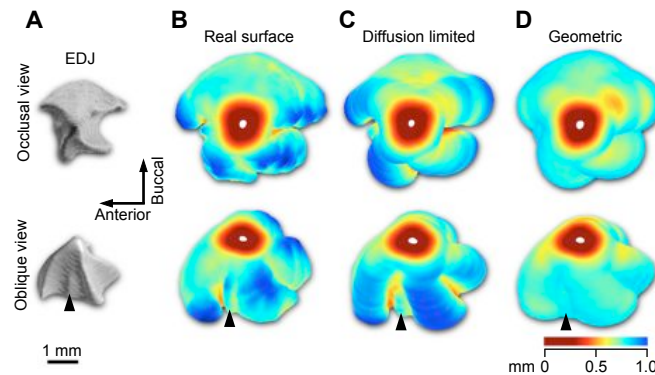
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310 **Figure 2.** Diffusion-limited simulations approximate complex patterns of enamel thickness in
311 the pig molar. (A) A heat map and a horizontal section of 3D tomography reconstruction of a
312 pig molar shows the variable enamel thickness. (B) Using a horizontal EDJ section of a pig
313 molar as an empirical template (A), diffusion-limited simulations of matrix secretion produce
314 deep fissures present in concave surfaces. (C) Geometric extrapolation shows how the fissures
315 are filled-in. In contrast, convex slopes are relatively similar between the simulations (B, C). All
316 images show or are based on occlusal views of the left lower first molar. Simulations run until
317 the lateral matrix thicknesses approximate the empirical enamel thicknesses, see Methods, and
318 for parameters Table S1. Scale bar, 5 mm.

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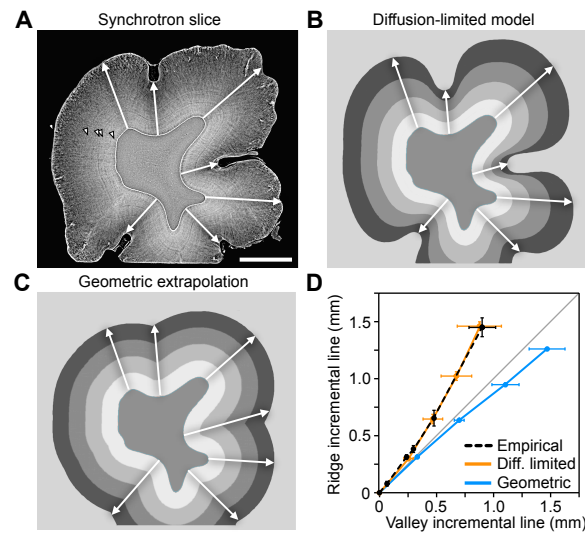
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323 **Figure 3.** 3D distribution of enamel is predicted by the diffusion-limited model. (A) The EDJ of
324 the pig entoconid cusp (arrowhead in Fig. 2B) has four ridges and only the buccal slope is
325 convex whereas the other slopes are concave. (B) The enamel surface is thickest around the
326 ridges and the EDJ concavities correspond to deep fissures with thinner enamel. The cusp tip
327 with no EDJ has been removed from the 3D data. (C) The diffusion-limited matrix simulation,
328 matched to have the enamel thickness of the convex lateral slope, captures the enamel
329 distribution patterns of the pig cusp. The small ridge present in the mesial slope of the cusp
330 (arrowhead in the oblique views) corresponds to a narrow ridge of matrix in the fissure both in
331 the diffusion-limited simulation and the empirical enamel surface. (D) Geometric extrapolation
332 from the EDJ results in relatively uniform 3D matrix thickness. The diffusion-limited
333 simulations were done from 51 individual EDJ slices using the same parameter values (Table
334 S1), and the geometric extrapolations from every slice. Enamel thickness measurements were
335 done in 3D. The thinner enamel in the lower parts of the lingual cusp ridge of the real cusp
336 (towards the bottom in occlusal view) is due to the vicinity of the adjacent hypoconid cusp, see
337 Fig 2A,B. Scale bar, 1 mm.

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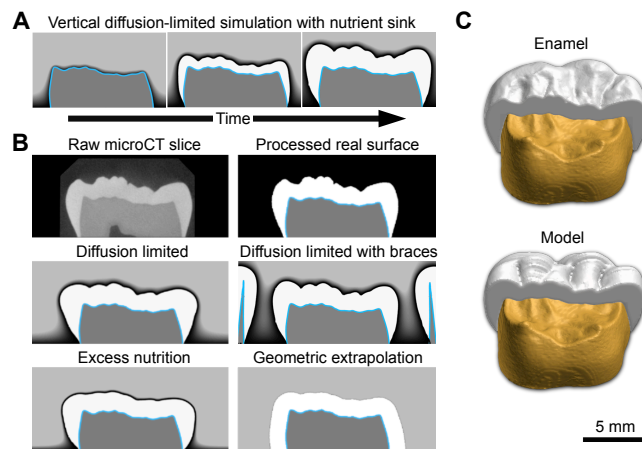


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342 **Figure 4.** Incremental lines in pig molar tooth show comparable patterns to diffusion-limited
343 matrix lines. (A) Incremental lines (arrowheads) are visible in a synchrotron imaged fully
344 formed but unerupted cusp of the second lower molar. (B) Diffusion-limited simulation and (C)
345 geometric extrapolation of matrix show contrasting patterns. The different shades of grey
346 correspond to progressive steps in simulations (every fourth) and geometric extrapolation. (D)
347 The arrows (in A,B,C) show the lines that are used to measure the progression of matrix
348 secretion in the valleys (concave EDJ regions) and ridges (convex EDJ regions). Both the
349 empirical and diffusion-limited simulations produce progressively thicker matrix in the ridges
350 relative to the valleys (mean lines shown, error bars denote s.d.). The diffusion-limited
351 simulation uses the same parameter values as the cusp in Fig 3. The border size (0.79) was set to
352 produce the empirical enamel thickness using the same number of iterations as in Fig. 3. The
353 target enamel thickness for the simulations was measured from the left side of the cusp. Because
354 the cusp was physically trimmed for synchrotron imaging, the section is missing the lower side.
355 Scale bar, 10 mm.

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358

359 **Figure 5.** The subtle EDJ topography of human molars is sufficient to produce enamel surface
360 features in diffusion-limited simulations. (A) To simulate the thick enamel of human molars that
361 also have a low cusp relief, we combined vertically oriented simulations with a basal nutritional
362 sink. The sink is used to simulate the shorter time of matrix secretion in the lower parts of the
363 crown. (B) Diffusion-limited simulations reproduce the surface features that are lost in excess
364 nutrition simulations and geometric extrapolations. Braces mimicking adjacent teeth and bone
365 constrain lateral expansion of enamel matrix. (C) Obliquely lingual views of empirical and
366 simulated enamel surfaces with a half of the EDJ (yellow) visible. The diffusion-limited
367 simulations were done from 27 individual EDJ slices using the same parameter values (Table
368 S1). The tooth shown is a human third lower molar. Scale bar, 5 mm.

369