Unsupervised Machine Learning for Analysis of Coexisting Lipid Phases

and Domain Growth in Biological Membranes

Cesar A. López.[1], Velimir V. Vesselinov[2], S. Gnanakaran[1]*, Boian S. Alexandrov[1]*.

[1]Theoretical Division, Los Alamos National Lab., Los Alamos, NM 87545

[2]Earth and Environmental Sciences Division, Los Alamos National Lab., Los Alamos, NM 87545

*Corresponding authors

E-mails: gnana@lanl.gov, boian@lanl.gov

Abstract

Phase separation in mixed lipid systems has been extensively studied both experimentally and

theoretically because of its biological importance. A detailed description of such complex systems

undoubtedly requires novel mathematical frameworks that are capable to decompose and

categorize the evolution of thousands if not millions of lipids involved in the phenomenon. The

interpretation and analysis of Molecular Dynamics (MD) simulations representing temporal and

spatial changes in such systems is still a challenging task. Here, we present a new unsupervised

machine learning approach based on Nonnegative Matrix Factorization, called NMFk, that

successfully extracts physically meaningful features from neighborhood profiles derived from

coarse-grained MD simulations of ternary lipid mixture. Our results demonstrate that leveraging

NMFk can (a) determine the role of different lipid molecules in phase separation, (b) characterize

the formation of nano-domains of lipids, (c) determine the timescales of interest and (d) extract

physically meaningful features that uniquely describe the phase separation with broad

implications.

Author Summary

Cell membranes contain mixtures of chemically diverse lipid molecules, dynamically structured,

that play a key role for cell survival. Under different conditions, lipids in the membrane can

segregate into liquid-ordered and liquid-disordered domains. It is well-known that such domains

play a critical role in cellular homeostasis. Unfortunately, the lack of molecular details hampers

the direct interpretation of the available experimental data for such lipid segregation dynamics.

Molecular Dynamics (MD) simulations can potentially fill the gap between theory and

experiments, but this task requires rigorous methods for proper analysis and description of the MD

generated trajectories. Here, we present a new unsupervised machine learning analysis based on

Nonnegative Matrix Factorization that extracts physically meaningful features from pre-processed

datasets generated by MD simulations. We simulate and analyze phase separation in a well-studied

ternary lipid mixture. Our results demonstrate that via the proposed machine learning we can: (a)

determine the role of different lipid molecules in the phase separation, (b) characterize the

formation of nano-domains in lipid bilayers, (c) determine the timescales of the formations of these

nano-domains and (d) extract physically meaningful features that uniquely describe the dynamics

of the phase separation

Introduction

Cell membranes contain mixtures of different lipid types, dynamically arranged, that play a key role in various mechanisms responsible for cell survival [1]. In the past, membranes were thought to be homogenous systems, however, new data suggests that under different stimulus, the lipids can segregate [2,3] into detergent-resistant domains commonly called "rafts". These domains are highly dynamic, varying in size and composition [4,5]. Importantly, this lateral partitioning is responsible for activation and functioning of membrane-embedded proteins [6,7].

While it is possible to experimentally visualize the structure of segregated lipid domains [2,8], a detailed description of such phases are inherently limited by the resolution of the experimental techniques. At this respect, molecular dynamics (MD) simulations provide a molecular understanding of membrane behavior. In fact, the presence of such lateral rearrangement has been studied extensively using coarse-grained (CG) MD of ternary lipid mixtures [9]. These CG simulations suggest partial segregation in large lipid systems that mimic the lipid variability of the real cell membranes [10]. MD simulations of such realistic biomolecular systems usually contain millions of particles, even when simplified models are used. When the purpose of such simulations is to gain biological or physical insights, it is challenging to identify patterns in the behavior encoded in the motion of thousands of molecules, so developing analytic tools for extracting functionally relevant features from MD generated trajectories is of great importance.

Currently, machine learning (ML) methods have shown a lot of promise in many fields [11], and recently some of them have been applied for analysis and detection of classical and

quantum phase transition data generated by simulations. Both supervised and unsupervised ML

approaches have been used for this purpose [12-19], but most of these pioneer studies used small

Ising-like systems for their investigations. ML has previously been coupled with MD simulations

of biomolecular systems in a limited context. ML techniques were reported to predict free-energy

differences when trained with MD simulation data [20], and unsupervised approaches such as PCA

[21] as well as other techniques [22,23] have been used to reduce the dimensionality of MD

generated data [24-28].

In general, the unsupervised ML methods learn relationships between elements in

uncategorized data and classify the data without human's help but by revealing its internal

structure and latent (i.e., not directly observable) features hidden in the data. The unsupervised

methods include clustering [29], classical neural networks [30], and the more contemporary blind

source separation (BSS) techniques [31]. BSS is based on *factorization* which is one of the most

powerful tools for extraction of latent features [32]. BSS include principle component analysis

(PCA) [33], singular value decomposition (SVD) [34], and more advanced methods, such as

independent component analysis, ICA [35] and nonnegative matrix factorization, NMF [36].

A limitation shared by PCA, SVD and ICA is the difficulty to relate the extracted latent

factors to physically interpretable quantities; NMF overcomes this limitation because the

nonnegativity of the extracted latent factors leads to a collection of strictly additive components

that are sparse and parts of the data and hence are amenable to a simple and meaningful

interpretation without introducing prior assumptions [37]. NMF decomposes given data matrix,

X_{LN}, into two matrices, W_{LK}, and H_{KM}, such that $X_{LN} \approx W_{LK} H_{KM}$. The factor matrices, W_{LK} and

H $_{KM}$, are both nonnegative and have one small dimension **K** that represents the number of the

latent features in the data (**Fig.** 1). A mathematically rigorous formalism is given in the later

sections. NMF ability to identify easy interpretable latent features enables discoveries of new

causal structures and unknown mechanisms hidden in the data as discussed in the literature [38].

Surprisingly, the implementation of NMF for analysis of MD simulations at the interface of

physics and biology has been lacking.

Here, we present a new unsupervised machine learning algorithm based on NMF combined

with custom k-means clustering, called NMFk, capable of analyzing phase separation in a system

of mixed lipids directly from the pre-processed trajectories derived by MD simulations. We use

CG MD simulations of a physical system that comprises a 3-component lipid mixture, commonly

accepted to mimic the behavior of a cellular plasma membrane [5]. We show that NMFk, applied

to a pre-selected data from these simulations is able to, (a) determine the molecules that play

different roles in phase separation, (b) characterize the formation of lipid nano-domains, (c) reveal

the timescales of interest, and (d) extract physically meaningful features that characterize the phase

separation.

Results

Generation of lipid mixture data sets using coarse-grained MD simulations

For MD simulations of membranes and membrane-based biological systems, the Martini coarse-

grained (CG) force field [39], considerably reduces the computational cost of calculations by

nearly three orders of magnitude compared with similar MD simulations using fully atomistic force

fields [40]. Particularly, the CG approach can capture relevant dynamics and fluctuations of larger

membrane patches, which are prohibitive with atomistic simulations. Such access to larger spatial

and temporal scales enables direct comparisons with experimental measurements [41]. Pioneering

computational studies with the Martini CG force field allowed the characterization of not only

lipid segregation and lipid phases, but also the relative partitioning of membrane proteins between

these phases [9,42-44]. More recently, Martini has been used in simulations of membranes with

lipid compositions of comparable complexity to those found in specific tissues of living cells

[45,46].

Regardless of the extensive use of the Martini force field, the building-block principle of

Martini along with the 4:1 atoms to bead mapping unavoidably reduce the accuracy due to loss of

detailed description of specific molecular chemical properties. Thus, despite the fact that many of

the current Martini lipid parameters are sufficient to guide accurate membrane simulations

[39,47,48], global lipid properties are compromised [49]. Consistent with previously published

work [42,50,51], the standard Martini V2.2 parameters for DPPC, DOPC, and CHOL do not phase

separate at 298 K, or even at 290 K in the physiologically relevant L_d/L_o coexistence region of the

phase diagram. Recently, we incorporated changes in the lipid Martini force field [52], greatly

improving the lipid segregation in line with current experimental phase diagrams [8,50].

We use the above two versions of the Martini force field, one lipid parameter set that phase

separates and the other that does not, to generate two data sets for the analysis using NMFk. The

first set considers the data from the coarse-grained MD simulations of the current Martini force

field (called "Standard"). As mentioned above, the current Martini V2.2 lipid parameters for DPPC

and DOPC are not able to properly segregate the DPPC:DOPC:CHOL mixture. It serves as the

prototype for non-phase separating homogeneous lipid mixture. The second set considers the

refined version of the Martini (called "Updated"), which has been optimized to reproduce the

experimental phase separation and domain formation for this ternary system [52]. It serves as the

prototype for phase separating lipid mixture. Using these two versions of force fields, we carried

out 20 μs long CG MD simulations. The expectation is that we should able to detect and analyze

features associated with phase separation in one case but not in the other case.

Conventional Analysis of Domains in MD Simulations of Ternary lipid Mixtures

The formation of lipid domains has been heavily studied both experimentally and computationally

[2-4,8-10,53-55] Computational observation of explicit lipid segregation at nearly atomic detail

dates back to almost 10 years ago [9] Analysis of such processes involved direct visualization of

cholesterol-rich/-poor domains, as well as physical quantification of the area per lipid, cholesterol

content, radial distribution functions and membrane thickness mismatch [9]. These analyses

brought enough details that membrane domains could be discriminated at the nanoscale. A more

sophisticated approach can be cited from the work of Baoukina et al.[51], where a Voronoi

tessellation methodology was applied in order to delineate the boundaries between

ordered/disordered domains in monolayers. This approach can be also directly combined with

automated predictive tools like Markovian based methodologies [54]. Regardless of these

published methodologies, the analysis and prediction of such fluctuating membrane domains

become inaccessible when the complexity of lipid content increases with larger size membrane

patches (e.g. plasma membrane).

A typical process of molecular lipid phase separation is depicted in **Fig. 2.** Initially, the

lipid components are randomized, mimicking the homogeneity at a high-temperature (**Fig. 2A**).

Subsequent fast quenching of the mixture to 290 K, well below the melting temperature of the

fully saturated DPPC lipid, leads to the rapid formation of nanoscale domains on a submicrosecond

time scale with the Updated Martini force field (**Fig. 2B top panel**). These nano-domains are

eventually formed over the entire surface of the membrane, but in different regions. After 0.5

microseconds, the nano-domains start to interconnect, leading to the formation of larger

cholesterol-rich regions. In agreement with the general raft hypothesis [53] and previous

computational studies [9], the ''ordered'' nano-domains contain most of the saturated lipids

together with cholesterol forming a Liquid ordered (L_o) domain, whereas the ''disordered'' nano-

domain is mainly composed of the polyunsaturated DOPC lipid segregated in a Liquid disordered

(L_d) region. Contrary to the Updated force field, the lipid mixture based on the Standard Martini

force field does not show any tendency for phase separation or domain formation (**Fig. 2B, bottom**

panel), in agreement with previously published data [52].

Following the conventional approaches to quantify the segregation tendency, we compute

the normalized total contacts between DPPC and DOPC as a function of simulation time (**Fig. 2C**).

Initially, these contacts are featured by larger values, meaning that these two lipid types are indeed

in close contact, highlighting the initial homogeneous lipid mixing of the system. However, with

the Updated Martini, lipid segregation leads to a decrease in the total number of contacts between

DPPC and DOPC (**Fig. 2C black line**). Whereas, the contacts remain unchanged in the simulations

with the standard Martini (**Fig. 2C red line**). In the case of Updated Martini, contacts decay during

the simulations and begin to plateau with increasing simulation time. We should note here that the

proper convergence to a stationary state may not be achievable within the simulation timescales

considered here, as already published [54], while significant transition towards segregation occurs

within the first 2 us (**Fig 2C insert**). We consider this time regime suitable for NMFk analysis to

extract latent features associated with the phase separation.

NMFk implementation for analysis of ternary lipid mixture simulations

To perform the NMFk analysis, we first define the primary and secondary lipid types and then

calculate the neighbor matrix at a given time t, $X_L(t)$, in terms of the number of secondary lipid

type surrounding the primary lipid type. For this study, we considered DPPC and DOPC as the

primary and secondary lipid types, respectively, although, there is no restriction of other

combinations for primary and secondary lipid types. We compute the number of closest DOPC

neighbors, $X_L(t)$, around every DPPC lipid, $L = (L_1, L_2, ..., L_M)$, within the distance corresponding

to the second peak of the DOPC-DPPC radial distribution function (**Fig. 3 blue dashed line**). The

number of neighbors within this distance serves as the order parameter for the lipid phase

separation. This neighbor data is recorded at N consecutive simulation time points, $t = (t_1, t_2, ...,$

$t_N)$, corresponding to the time evolution of the system up to first 2 us. The matrix $X_L(t)$ contains

N arrangements at N time points, presented by the columns of X, that form the matrix of the

neighbors, $X_L(t)$; $X \in M_{MN}(I_+)$, where M is the number of the rows, and each row represents the

time evolution of the closest neighbors of one specific lipid of the primary type. The I_+ denotes

the set of nonnegative integer numbers. Next, NMFk decomposes the neighbor matrix $X_L(t)$ as a

product of two matrices: $X_L(t) \approx W_{LK} * H_K(t)$, where the columns of W_{LK} are the K basis lipid

configurations describing the state of the lipid system and $H_K(t)$ contains the contributions of each

one of these configurations at time t (see **Fig. 1** where K=2).

The neighbor matrix, $X_L(t)$, contains relevant properties of the ternary lipid mixture. At

the beginning of the simulations, the lipid mixture is homogeneous and there are no distinct phases,

i.e., there is no specific structure in $X_L(t)$. Hence, $X_L(t)$ contains uniformly distributed integer

numbers that do not have any distinct features. With the Updated Martini force field, by 2 us, the

primary lipid type, DPPC, segregates into the L_o region, while the secondary lipid type, DOPC,

segregates into the L_d domain. In this case, if a concrete lipid of the primary type is located deep

in a L_o domain, the probability to have a lipid-neighbor of secondary type is small (close to zero).

In contrast, if this primary lipid is situated outside of any domain, the probability to have a neighbor

of the secondary type is much higher. Therefore, we expect the neighbor matrix to contain a

structure that tracks this phase separation and the subsequent analysis by NMFk to extract the

hidden features describing the structure and the phase separation.

The NMFk analysis, as we will see next, demonstrates exactly that: When phase separation

begins at time, $t = t_s$, for each one of the snapshots recorded at, $t > t_s$, and for each of the M lipids

of the primary type, the values of the matrix $X_L(t > t_s)$ can be represented as a linear mixing of

K basis lipid configurations presenting the probability of the given lipid of the primary type, L_i,

to have a closest neighbor-lipid of secondary type. NMFk decomposes the matrix $X_L(t)$, to a

nonnegative probability matrix, W, $W \in M_{MK}(\mathcal{R}_+)$, corresponding to these K basis lipid

configurations, blended by the weights, presented by the elements of a nonnegative matrix, H, $H \in$

$M_{KN-s}(\mathcal{R}_+)$ that reflects how these configurations are active and mix in time. Thus, for a given

arrangement of the primary lipids, X_L, at a time point $t > t_s$, we have,

$$X_L(t > t_s) \ = \ \sum_{i=1}^{K} W_k(L)H_k(t > t_s) + \varepsilon_L(t > t_s),$$

where $\varepsilon \in M_{MN-s}(\mathcal{R}_+)$ denotes the presence of a noise or unbiased error of decomposition.

Before the time point $t = t_s$, there is no trace of a phase separation and the pattern of the number

of the closest neighbors is stochastic. Therefore, there is no clear features that could be recognized

by NMFk.

The reconstruction of $X_L(t > t_s)$, via the two factor matrices, $W_k(L)$ and $H_k(t > t_s)$,

serves as a measure for the significance and quality of the extracted latent features. For the case of

Updated Martini, **Table 1** presents the Pearson correlation coefficient between the reconstructed

lipid arrangements at each time point t (obtained by NMFk) and the original arrangements at the

same time point (i.e., the corresponding column of the neighbor matrix $X_L(t)$). The K unique basis

lipid configurations (encoded in the probability matrix W), reproduced the $N-s$ lipid

arrangements forming the matrix X_{MN-s}. With the standard Martini, the NMFk was not able to

provide a set of lipid configurations that can reconstruct the simulations accurately. Indeed, and as

shown in **Table 1**, the NMFk analysis did not reproduce accurately the simulation data.

NMFk derived features associated with phase separation of ternary lipid Mixture

Here, we describe how the basis lipid configurations extracted by NMFk describe physical

properties of the phase separation, such as, time profile of which lipid molecules belongs to which

phases, the formation of nano-domain, and the spatial and temporal profiles of nucleation and

phase separation.

A typical outcome of NMFk analysis is presented on **Fig. 4**. According to our Silhouette-

Reconstruction criteria (see Methods Section), NMFk determines that the optimal number of basis

lipid configurations is 20 (**Fig. 4A**). The columns H_i of the matrix H, each of which encodes the

weights, that is, the participation of a basis lipid configuration in time, are presented on (**Fig. 4B**).

It is clear that for each H_i there is a well-defined time interval containing a number of consecutive

frames where the corresponding basis configuration W_i is active. From **Table 1**, it can be seen that

after 0.45 μs, NMFk reproduces the neighbor matrix $X_L(t)$ very well: the cross-correlation

between the neighbor matrix and the reconstructed matrix, for each time frame, is above 0.95. The

much lower cross-correlation for reconstruction of the matrix $X_L(t)$ at early times suggests a

prevalence of homogeneous lipid mixture in the first 0.45 μs. The 15 significant basis lipid

configurations that are active at consecutive time intervals after the first 0.45 μs (#6; #10; #12;

#15; #17; #19; #20; #18; #16; #14; #13; #11; #7; #2; #1) represent the evolution of the nucleation

and phase separation.

Each one of the 15 significant basis lipid configurations, extracted by NMFk, contains a

set of probabilities for the lipids of a primary type to have a close neighbor-lipid of a secondary

type. Each basis lipid configuration (i.e., the specific set of probabilities) is active at a given time

interval defined by the weight of this basis configuration at the corresponding column of the matrix

H. In each basis lipid configuration, we expect to have at least two groups of probabilities: (a) the

probabilities of primary lipids situated in the nucleation domains that have relatively small number

of neighbor-lipid of secondary type, and therefore these probabilities, on average, approach zero;

and (b) the probabilities for primary lipids outside of any nucleation domain whose number of

neighbor-lipid of secondary type is much higher. There are always transition of the primary type

of lipids in and out of the nucleation domains or at the interface of the nucleation domains: at a

certain moment, a given primary lipid could be situated outside a nucleation domain formed by

primary lipids, but after a while it could reach interfacial region and eventually get absorbed into

the nucleation domain. Alternatively, primary lipids inside the nucleation domain or at the

interfacial region may venture out into the liquid disordered region enriched of secondary lipids.

These exchanges continuously alter the probability of a given lipid of the primary type to have

neighbor-lipid of secondary type, as the phase separation proceeds which results in different basis

lipid configurations at different time points as the system goes to a phase separation. At long

timescale, when the phase separation has reached equilibrium, basis lipid configurations capture

the exchanges of the primary lipids governed by the stochasticity and diffusion.

To better characterize the above observations related to the extracted basis lipid

configurations, we applied k-means clustering on each of the 20 basis lipid configurations. We

combined the k-means clustering with Silhouette statistics to determine the most probable number

of clusters, i.e., the most probable number of groups of probabilities in each basis lipid

configuration. Specifically, we calculate consecutively the Silhouettes of the resulting clusters,

changing the number of clusters from 1 to 30 to determine the most probable groups of primary

(DPPC) lipids with similar probabilities to have a neighbor secondary (DOPC) lipid-neighbor. **Fig.**

4C shows the basis lipid configurations ordered according to the sequence of the frames

corresponding to consecutive time intervals determined by their respective weights. The k-means

clustering procedure determined that each of the extracted 20 lipid basis configurations can be

separated to two clusters: The first cluster contains the primary lipids with a low average

probability to have a DOPC lipid-neighbor and the second cluster contains the primary lipids with

more than four times higher average probability to have a DOPC lipid-neighbor. Further, we

colored differently the lipids in each of the 20 lipid basis configurations, with two clusters each, at

the time intervals where the respective lipid basis configuration is active. The color gradient in

Fig. 4C captures these two groups of primary lipids: white to grey the primary lipids within the

nucleation domains, and blue to red-the primary lipids at the interface or outside of any nucleation

domain.

Next, we use the MD simulations trajectories to visualize and rationalize the two primary

lipid groups as extracted by the clustering of basis lipid configurations derived by NMFk. We

considered lipid basis configurations, #19 and #1 corresponding to 1us and 2us time points,

respectively. All lipids contributing to those lipid basis configurations are mapped into the

trajectories at the corresponding time points in **Fig. 5**. At 2 us, approximately 70% of primary

lipids (DPPC, colored in blue) are situated in large nucleation domains which are well packed and

condensed by the high cholesterol concentration, leading to L_d phase. These primary lipids are

predominantly shielded from the secondary (DOPC, colored red) lipids which themselves are

localized to form the L_o phase. These primary lipids correspond to the first cluster identified by

NMFk and are localized in nucleation domains.

On the other hand, at 2 us, approximately 30% of the primary lipids (DPPC, colored

yellow) in the same lipid basis configuration #1 are located near the interfacial regions or deep

into the L_d regions formed by secondary lipid types. Unlike the previous set of primary lipids,

these lipids are in direct contact with the secondary lipids. The **Fig. 5 insert** shows how NMFk is

able to distinguish these lipids from all DPPC lipids available. They correspond to the second

cluster identified by NMFk. Thus, each given lipid basis configuration contains physical and

easily interpretable features that enable us to make a distinction on primary lipids depending on

their location and their contribution to the lipid segregation.

The strength of NMFk analysis is the ability to extract lipid basis configurations as a

function of time. These configurations enable us to determine the time dependence of the latent

features connected to the kinetics of phase separation without carrying out tedious multiple

analyses. A conventional analysis that seeks to probe the temporal profile would have considered

the normalized number of contacts among DPPC lipids and between DPPC and DOPC to capture

the nucleation process (**Fig. 2C**). NMFk decomposes the nucleation process in two components,

as shown in **Fig. 6,** where the distinction is made on the temporal profiles of primary lipids from

the nucleation domains from those that are still outside the nucleation domains**.** In **Fig. 6A,** the

purple bars represent the total number of primary lipids in nucleation domains at consecutive time

intervals (ordered on the x-axis), while the primary lipids outside of any nucleation domain are

presented by yellow bars. At early time, rapid growth of domains is seen which is directly

correlated to the increase of nucleation of primary lipids. After this rapid growth, a steadier

behavior is observed which continues till the end of the simulation. In **Fig. 6B** we represent the

normalized number of contacts with the secondary lipids for the primary lipids as identified from

NMFk. At early times, these contacts are high due to random encounters between lipids. This

behavior begins to change around 0.6 us and then the contacts between primary and secondary

lipids are indicative of steady growth of the number of primary lipids in the nucleation domains

and a decrease of the total number of lipids in the non-nucleating regions as the lipid mixture

system phase separates.

Furthermore, NMFk analysis extracts the temporal evolution of the primary lipids'

membership: in or out of a nucleation domain. Specifically, the membership is defined by

identifying primary lipids that join a nucleation domain and remain in that domain till the phase

separation. We ordered the 15 significant basis lipid configurations extracted by NMFk according

to the time intervals when the specific configurations are active, **Fig. 7**. We identify the primary

lipids that participate in the nucleation by keeping track of the lipids in basis lipid configurations

with low probabilities to have a secondary lipid-neighbor. In **Fig. 7A,** we present the *concrete*

primary lipids that *remain* in the same cluster with small (purple color) or high (yellow color)

probability to have a secondary lipid-neighbor at consecutive time intervals, which represents the

evolution of nucleation. The inset in **Fig. 7A** demonstrates the system at much later time (~ 20

microseconds) after the initial nucleation when the phase separation has reached equilibrium and

the primary lipids that are located in nucleation domains mostly preserve their membership in time.

Importantly, this evolution of the primary lipids can be easily mapped at their spatial coordinates.

In **Fig. 7B**, the patterns extracted by NMFk are mapped via MD trajectories to their spatial

coordinates (at each time interval), to visualize the evolution of the different groups of primary

lipids based on their membership: in nucleation domains (purple color) or outside those domains

(yellow color). This again highlights the power of the NMFk to extract physical properties and

details that can be easily visually tracked as the system undergoes localization and lipid

segregation.

Discussion

We introduce an unsupervised machine learning algorithm based on the nonnegative matrix

factorization combined with custom clustering, called NMFk, for analysis of MD simulations.

Specifically, we implement that algorithm here to detect and describe the lateral lipid segregation

in a simplistic lipid "raft" model composed of a well-characterized ternary lipid mixture. Based on

this study, we believe that the NMFk formalism can be also implemented for extracting relevant

features from a more complex biological membrane.

The DOPC:DPPC:CHOL ternary lipid mixture considered here can exist as a

homogeneously mixed mixture or exhibit two distinct phases of L_o and L_d depending on

temperature. NMFk is utilized to detect and analyze this phase separation behavior of this well-

studied system. The distinction between the two phases, L_o and L_d, is sensitive to the spatial

localization of DPPC lipids and the number of DOPC neighbors. We designate DPPC and DOPC

as primary and secondary lipids in the NMFk formalism, respectively. At the beginning of the

simulations, there are no distinct phases and the lipid mixture is homogeneous. As simulation time

progresses, lipids begin to segregate. By 0.6 us, the primary lipid type in this case, DPPC, begins

to segregate into the L_o regions, while the secondary lipid type, DOPC, begin to segregate into the

L_d domains. Thus, the number of secondary lipid neighbors around a given primary lipid should

reflect that phase separation.

Given that a neighborhood profile of lipids can track the DOPC:DPPC:CHOL mixture, we

first built a specific time-dependent data-matrix, $\boldsymbol{X_L(t)}$ (see Methods section) whose elements

represent the number of DOPC neighbors to each one of the DPPC lipids in the system, within a

specific radius, r_{cutoff} extracted from careful analysis of the radial distribution function. NMFk

decomposed the matrix $\boldsymbol{X_L(t)}$ into a product of two matrices: (i) the matrix of the basis lipid

configurations, $\boldsymbol{W_{NK}}$, whose columns present the configurations of DPPC lipids. NMFk

determines the number of basis configuration $\boldsymbol{K}$ based on the robustness of the decomposition.

Each one of the $\boldsymbol{K}$ basis lipid configurations in $\boldsymbol{W_{NK}}$ contains the probabilities of the set of the

DPPC lipids to have DOPC neighbors. The Silhouette-Reconstruction criterium was used to

estimate the optimal number of basis lipid configurations to be 20. K-means clustering of each

these 20 basis lipid configurations is demonstrating the tendency of increasing the number of

primary lipids with a neglecting probability to have a neighbor of type DOPC when the time

advances, which correspond to an increased total number of DPPC lipids located in nucleation

domains.

By relating the basis lipid configurations to MD trajectories, we were able to show details

of phase separation extracted by NMFk analysis. The NMFk discriminates lipids, depending on

whether they belong to L_o or L_d phases or interfacial regions, as they undergo phase separation.

Unlike, other analyses, basis lipid configurations provide details of lipids that take part in the

nucleation versus those that establish line tension. It tracks the complicated features of the lipid

segregation process leading to L_o and L_d phases. We identify lipids within the boundary of L_o

phase with lipid configurations basis corresponding to a signature of L_o domain where DPPC is

well packed and condensed by the high cholesterol concentration. Separately, another basis lipid

configuration captures interfacial lipids that shield the DOPC lipids from such L_o domains during

phase separation. Importantly, we demonstrate that the evolution of the nucleation process is

captured in terms of lipid membership to different basis lipid configuration active in consecutive

time intervals. NMFk identifies the lipids that take part in the initial nucleation and remains as part

of the domain towards the phase separation. Also, other lipids that join such nucleation and remain

till the phase separation are identified as the time progresses.

Conclusions

The high variability and complexity of plasma membranes is still poorly understood. Higher

resolution spectroscopy in combination with atomic detailed computer simulations are providing

new insights, however, we are not yet close to fully understand or describe the membrane processes

regulating cellular function. A detailed description of such complex systems undoubtedly requires

novel mathematical frameworks that are able to decompose and categorize the evolution of

thousands if not millions of lipids involved in the phenomenon.

Here we show the power of NMFk formalism on analyzing lipid phase separation and

providing a robust analysis of categorizing lipids according to their localization in the membrane

and elucidating the time-dependency along the nucleation process. The NMFk discriminates all

different types of lipids, part of L_o or L_d or interface, due to their particular behavior along the

trajectory and the resulting probability to have a DOPC neighbor. If there is no clear pattern in the

behavior of the lipids, for example, when MD simulations do not produce any distinct behavior

associated with phase separation, NMFk analysis does not produce false features. This is the first

demonstration of NMFk serving as a useful tool in detecting time-dependent domain formation

and lipid separation in MD simulations of complex lipid mixture systems. Even though we have

exhibited the usefulness of NMFk in the context of a well-studied ternary lipid mixture, an

extension to more complicated lipid mixtures is feasible with a tensor formalism and is currently

under consideration.

Methods
427

Membrane patch
429

An initial configuration of a CG membrane patch was obtained using the script tools provided in

the Martini force field website (http://cgmartini.nl/). Our CG lipid system contains

DPPC:DOPC:CHOL lipids in a 37:36:27 ratio respectively, which initially were randomly placed

within a XY plane. This lipid ratio has been experimentally and computationally observed to

transitioning towards a phase separated Liquid-ordered/Liquid-disordered state [54,56]. The lipids

were represented using the Martini V2.2 force field [57] with a refined set of parameters, which

has shown an improved phase separation behavior [52]. Similarly, simulation with the standard

Martini lipid model was also carried on. The total system was composed of 16366 lipids, 718830

Martini water beads (175 atomistic water molecules per lipid) and 150mM NaCl to preserve an

overall constant ionic strength. In order to avoid spontaneous freezing of the Martini water beads

(a well-known artifact previously reported in the original model [39]), 0.1% M of the water beads

were replaced by anti-freeze particles.

Molecular dynamics protocol

We followed a current update in parameters set-up for performing the CG simulations [58]. The

equations of motion were integrated every 30fs time-step. A reaction-field electrostatics algorithm

was used with a Coulomb cut-off of 1.1 nm and dielectric constants of 15 or 0 within or beyond

this cut-off, respectively. Lennard-Jones interactions were cut off at 1.1 nm, where the potential

was shifted to zero. In order to accelerate the lipid phase de-mixing, constant temperature was

maintained at 290 K via separate coupling of the solvent (water and ions) and membrane

components using a velocity-rescaling thermostat [59] with relaxation times of 1.0ps. During

equilibration, the Martini beads representing the phosphate groups of the lipid head regions were

positionally (xyz components) restraint in order to preserve the initial random positions. In this

stage, the solvent molecules (water and ions) were allowed to diffuse and the box pressure was

maintained semi-isotropically coupled at 1 bar using the Berendsen barostat [60] with relaxation

times of 12 ps and compressibilities of 3×10^{-4} bar^{-1}. After that, production runs were performed

using a Parrinello-Rahman barostats [61]. Simulations were run for 20 μs using the GROMACS

version 5.2.1 [62] and the trajectories were saved every 3 ns providing the frames for the

construction of the NMFk matrix (see later).

Generation of the contact matrix $X_N(t)$

Every frame stored within 2 us (667 frames in total) were used for generating the corresponding

matrix for NMFk analysis. We rely on the implemented GROMACS tool *gmx select* to output the

number of DOPC lipids around every DPPC molecule within 1.1 nm. This cutoff-radius

structurally corresponds to the second layer of neighbors, as estimated by the second maximum

peak of the radial distribution function g(r) (**Fig. 3**). Thus, each column of the data-matrix, $X_N(\mathbf{t})$,

corresponds to a variable number of the DOPC neighbors of a given DPPC lipid per frame, while

the rows correspond to the number of the 3038 DPPC lipids in the system. Similarly, matrix

reconstruction was carried out for 20 us collection. An example of the matrix can be found as part

of Supporting material.

Nonnegative Matrix Factorization and NMFk

Nonnegative Matrix Factorization (NMF) is a well-known unsupervised machine learning method

created for parts-based representation [36]. NMF has been successfully leveraged for decomposing

mixtures of various types nonnegative signals, i.e., for Blind Source Separation (BSS) [38]

problems. If the BSS problem is solved in a temporally discretized framework, the goal of the

NMF algorithm is to retrieve the original nonnegative signals (sources), W; $W \in M_{PK}(R_+)$ that

produced the observational records, X; $X \in M_{NP}(R_+)$, detected at a set of sensors. Here R_+

denotes the set of real nonnegative numbers, N is the number of the recording sensors, K is the

number of unknown original signals, and P is the number of discretized moments in time (time

points or frames) at which the signals are recorded at the sensors. Only the matrix X is known

initially. Thus, in a BSS problem, the recorded data, X, is formed by a linear mixing of K unknown

original signals W, blended by an unknown mixing matrix, H. Since both factor matrices W and

H are unknown, and even their size K (i.e., the number of unknown original signals) is unknown

the problem is typically under-determined. NMF can solve such kind of problems by leveraging,

for example, the multiplicative update algorithm [37] to minimize the Frobenius norm

$\frac{1}{2}||X - W * H||_F^2$. An additional advantage of NMF method is that it can work with data in which

the original signals are not independent but partially correlated [38].

One of the difficulties of the NMF algorithm is that it requires *prior* knowledge of K-the

number of the unknown original signals. Recently a new protocol called NMFk addressing this

limitation has been reported [63-65]. This protocol complements classical NMF with custom k-

means clustering and Silhouette [66] statistics, which allows simultaneous identification of the

optimal number of the unknown basis patterns. The NMFk was utilized to successfully decompose

the largest available dataset of human cancer [67] genomes, as well as for extraction of physical

pressure transients [65] and contaminants [68] originating from an unknown number of sources

that may propagate with a finite speed in nondispersive [69] or dispersive media [70] as well as

for extraction of the original crystal structures and phase diagram from X-ray spectra of material

combinatorial libraries [71].

NMFk determines the number of the unknown original signals based on the robustness and

reproducibility of the NMF solution. Specifically, it explores consecutively the possible numbers

of configurations $\tilde{K}$ ($\tilde{K}$ can go from 1 to N-1, where N is the total number of frames), by obtaining

sets of NMF minimization solutions for each $\tilde{K}$. Note that $\tilde{K}$ serves to index the different NMF

models, and it is distinct from K, which is fixed, albeit unknown number. Further, NMFk leverages

a custom clustering using the cosine similarity, in order to estimate the robustness of each set of

NMF solutions with fixed $\tilde{K}$ but derived with different initial guesses. Comparing the quality of

the derived clusters (a measure how different are the extracted signals) and the accuracy of

minimization among the sets with various $\tilde{K}$, which we call a Silhouette-Reconstruction criterium,

NMFk determines the optimal numbers of the unknown original signals. To access the quality of

the clusters obtained for each set we use their average Silhouette width, S. NMFk utilizes S to

measure how good is a particular choice of $\tilde{K}$ as an estimate for K. Specifically, the optimal

number of patterns is picked by selecting the value of $\tilde{K}$ that leads to both: (a) an acceptable

reconstruction error R of the observation matrix X, where

514
$$R = \frac{\|X - W * H\|_F}{\|X\|_F},$$

and (b) a large average Silhouette width (i.e., an average Silhouette width close to one).

The combination of these two criteria is easy to understand intuitively. For solutions with $\tilde{K}$ less

than the actual number of patterns ($\tilde{K} < K$) we expect the clustering to be good (with an average

Silhouette width close to 1), because several of the actual patterns could be combined to produce

one "super-cluster"; however, the reconstruction error will be high, due to the model being too

constrained (with too few degrees of freedom), and thus on the under-fitting side. In the opposite

limit of over-fitting, when $\tilde{K} > K$ ($\tilde{K}$ exceeds the actual number of configurations), the average

reconstruction error could be quite small - each solution reconstructs the observation matrix very

well - but the solutions will not be well-clustered (e.g., with an average Silhouette substantially

less than 0.8), since there is no unique way to reconstruct X with more than the actual number of

configurations, and no well-separated clusters will be formed.

Thus, the best estimate for the number of unknown original signals, W, corresponding to

the true number of unknown original signals K, is given by the value of $\tilde{K}$ that optimizes both of

these metrics simultaneously. Finally, after determining K, we use the centroids of the K clusters

as a final robust representation of the original signals.

NMFk minimization algorithm

Here we leveraged the multiplicative algorithm [37] based on Kullback–Leibler divergence [72]

as well as the block coordinate descent algorithm [73] based on Frobenius norm. We did not

observe any significant difference between the results obtained via these two algorithms.

NMFk clustering algorithm

NMFk creates up to N-1 sets of minimizations (called NMF runs), one for each possible number

$\tilde{K}$ of original patterns. In each of these runs, Q solutions (e.g., $Q = 200$) of the NMF

minimizations for a fixed number of patterns $\tilde{K}$ are derived. Thus, each run results in a set of

solutions $U_{\tilde{K}}$:

$$U_{\tilde{K}} = \{W_{\tilde{K}}^1, H_{\tilde{K}}^1; \, W_{\tilde{K}}^2, H_{\tilde{K}}^2; ...; W_{\tilde{K}}^Q, H_{\tilde{K}}^Q\},$$

where each of these "tuples" represents a distinct solution for the nominally same NMF

minimization: the difference is stemming from the different (random) initial guesses. Next, NMFk

performs custom clustering, assigning the $\tilde{K}$ columns/features of each $W_{\tilde{K}}^i$ of all Q solutions to

one of the $\tilde{K}$ clusters, representing $\tilde{K}$ basic patterns. This custom clustering is similar to k-means

clustering but with an additional constraint which holds the number of elements in each of the

clusters equal to the number of solutions Q. For example, with $Q = 200$ each one of the $\tilde{K}$

identified clusters must contain exactly 200 solutions. This condition has to be enforced since each

minimization (specified by a given $(W_{\tilde{K}}^i, H_{\tilde{K}}^i)$ tuple) contributes only one solution for each feature,

and accordingly supplies exactly one element to each cluster. During the clustering, the similarity

between patterns is measured using the cosine similarity.

Numerical codes, data and Supporting Information

The following files: COORD.gro with the coordinates; INPUT.mdp with the parameters set to start

the simulation with Gromacs; PARAMETERS.top with the Martini force field-based topology for

the membrane system; DPPC-DOPC-1.1nm.xvg with an example matrix generated from the MD

trajectories used for NMFk calculation, are provided as supporting information.

To extract patterns of the basis lipid configurations from the MD simulations we used the NMFk

method which is an extension of the original NMF [37] that includes a custom clustering for

determination of the number of patterns [63] . Our NMFk protocol is based on the SigProfile

software created for identification of mutational signatures in human cancer [67].

The SigProfile code is freely available at: https://www.mathworks.com/matlabcentral. To use

SigProfile an input file should be at place. In our case, the input file is the contact matrix $X_N(t)$

with size (N x M), where N is the number of the lipids in the MD simulations and M is number of

the frames. A detailed description of NMFk is available elsewhere [65]. The input file containing

the contact matrix $X_N(t)$ as well as a script, needed to run the SigProfile, are provided as

supporting information accompanied this paper.

A README file with list of the included in supporting information files, the links to publicly

available repositories along with their brief description and short instructions is also provided as

supporting information.

The simulated lipids' trajectories data (~ 100GB) is available freely, but because of its size,

upon request to gnana@lanl.gov.

Acknowledgments

This research was performed at Los Alamos National Laboratory and carried out under the

auspices of the National Nuclear Security Administration of the United States Department of

Energy. We like to acknowledge Tyler Reddy for generating synthetic data to test preliminary

results. The work was supported by LANL LDRD grant 20180060DR. This work has been

supported in part by the Joint Design of Advanced Computing Solutions for Cancer (JDACS4C)

program established by the U.S. Department of Energy (DOE) and the National Cancer Institute

(NCI) of the National Institutes of Health. This work was performed under the auspices of the U.S.

Department of Energy by Lawrence Livermore National Laboratory under Contract DE-AC52-

07NA27344, Los Alamos National Laboratory under Contract DE-AC5206NA25396, Oak Ridge

National Laboratory under Contract DE-AC05-00OR22725, and Frederick National Laboratory

for Cancer Research under Contract HHSN261200800001E. We thank the LANL Institutional

Computing for the computing resources.

Contributions

589 All authors designed the research. C. A. L. performed the MD simulations. B. S. A. performed the

590 NMFk analyses. All authors analyzed the data and wrote the manuscript.

References

1. Israelachvili J, Wennerström H (1996) Role of hydration and water structure in biological and
colloidal interactions. Nature 379: 219.
2. Nickels JD, Chatterjee S, Stanley CB, Qian S, Cheng X, et al. (2017) The in vivo structure of
biological membranes and evidence for lipid domains. PLoS Biol 15: e2002214.
3. Kraft ML (2016) Sphingolipid Organization in the Plasma Membrane and the Mechanisms
That Influence It. Front Cell Dev Biol 4: 154.
4. Rosetti CM, Mangiarotti A, Wilke N (2017) Sizes of lipid domains: What do we know from
artificial lipid membranes? What are the possible shared features with membrane rafts in
cells? Biochim Biophys Acta 1859: 789-802.
5. Levental KR, Lorent JH, Lin X, Skinkle AD, Surma MA, et al. (2016) Polyunsaturated Lipids
Regulate Membrane Domain Stability by Tuning Membrane Order. Biophys J 110: 1800-
1810.

6. Dietrich C, Volovyk ZN, Levi M, Thompson NL, Jacobson K (2001) Partitioning of Thy-1,
GM1, and cross-linked phospholipid analogs into lipid rafts reconstituted in supported
model membrane monolayers. Proceedings of the National Academy of Sciences 98:
10642-10647.
7. Van Meer G, Voelker DR, Feigenson GW (2008) Membrane lipids: where they are and how
they behave. Nature reviews Molecular cell biology 9: 112.
8. Veatch SL, Keller SL (2003) Separation of liquid phases in giant vesicles of ternary mixtures
of phospholipids and cholesterol. Biophys J 85: 3074-3083.
9. Risselada HJ, Marrink SJ (2008) The molecular face of lipid rafts in model membranes. Proc
Natl Acad Sci U S A 105: 17367-17372.
10. Ingólfsson HI, Melo MN, Van Eerden FJ, Arnarez Cm, Lopez CA, et al. (2014) Lipid
organization of the plasma membrane. Journal of the american chemical society 136:
14554-14559.
11. Michalski RS, Carbonell JG, Mitchell TM (2013) Machine learning: An artificial intelligence
approach: Springer Science & Business Media.
12. Broecker P, Carrasquilla J, Melko RG, Trebst S (2017) Machine learning quantum phases of
matter beyond the fermion sign problem. Scientific reports 7: 8823.
13. Tanaka A, Tomiya A (2017) Detection of phase transition via convolutional neural networks.
Journal of the Physical Society of Japan 86: 063001.
14. Zhang Y, Kim E-A (2017) Quantum loop topography for machine learning. Physical review
letters 118: 216401.
15. Wang L (2016) Discovering phase transitions with unsupervised learning. Physical Review B
94: 195105.
16. Carrasquilla J, Melko RG (2017) Machine learning phases of matter. Nature Physics 13: 431.
17. Zhang P, Shen H, Zhai H (2018) Machine learning topological invariants with neural
networks. Physical review letters 120: 066401.
18. Hu W, Singh RR, Scalettar RT (2017) Discovering phases, phase transitions, and crossovers
through unsupervised machine learning: A critical examination. Physical Review E 95:
062122.
19. Wetzel SJ (2017) Unsupervised learning of phase transitions: From principal component
analysis to variational autoencoders. Physical Review E 96: 022140.
20. Riniker S (2017) Molecular Dynamics Fingerprints (MDFP): Machine Learning from MD
Data To Predict Free-Energy Differences. Journal of chemical information and modeling
57: 726-741.
21. Garcia AE (1992) Large-amplitude nonlinear motions in proteins. Phys Rev Lett 68: 2696-
2699.
22. Coifman R. R., Lafon S., Lee A. B., Maggioni M. , Nadler B. , et al. (2005) Geometric
diffusions as a tool for harmonic analysis and structure definition of data: Diffusion
maps. Proceedings of the National Academy of Sciences of the United States of America
102.21 7426-7431.
23. Tenenbaum JB, de Silva V, Langford JC (2000) A global geometric framework for nonlinear
dimensionality reduction. Science 290: 2319-2323.
24. Glazer DS, Radmer RJ, Altman RB (2008) Combining molecular dynamics and machine
learning to improve protein function recognition. Biocomputing 2008: World Scientific.
pp. 332-343.

25. Karamzadeh R, Karimi-Jafari MH, Sharifi-Zarchi A, Chitsaz H, Salekdeh GH, et al. (2017)
Machine Learning and Network Analysis of Molecular Dynamics Trajectories Reveal
Two Chains of Red/Ox-specific Residue Interactions in Human Protein Disulfide
Isomerase. Scientific Reports 7: 3666.
26. Gastegger M, Behler J, Marquetand P (2017) Machine learning molecular dynamics for the
simulation of infrared spectra. Chemical science 8: 6924-6935.
27. Ash J, Fourches D (2017) Characterizing the chemical space of ERK2 kinase inhibitors using
descriptors computed from molecular dynamics trajectories. Journal of chemical
information and modeling 57: 1286-1299.
28. Sgourakis NG, Merced-Serrano M, Boutsidis C, Drineas P, Du Z, et al. (2011) Atomic-Level
Characterization of the Ensemble of the Aβ(1–42) Monomer in Water Using Unbiased
Molecular Dynamics Simulations and Spectral Algorithms. Journal of Molecular Biology
405: 570-583.
29. Hartigan JA, Wong MA (1979) Algorithm AS 136: A k-means clustering algorithm. Journal
of the Royal Statistical Society Series C (Applied Statistics) 28: 100-108.
30. Kohonen T (1998) The self-organizing map. Neurocomputing 21: 1-6.
31. Belouchrani A, Abed-Meraim K, Cardoso JF, Moulines E (1997) A blind source separation
technique using second-order statistics. IEEE Transactions on signal processing 45: 434-
444.
32. Spearman C (1904) " General Intelligence," objectively determined and measured. The
American Journal of Psychology 15: 201-292.
33. Jolliffe I (2002) Principal component analysis: Wiley Online Library.
34. Golub GH, Reinsch C (1970) Singular value decomposition and least squares solutions.
Numerische mathematik 14: 403-420.
35. Cichocki A, Yang HH (1996) A new learning algorithm for blind signal separation.
Advances in neural information processing systems 8: 757-763.
36. Paatero P, Tapper U (1994) Positive matrix factorization: A non-negative factor model with
optimal utilization of error estimates of data values. Environmetrics 5: 111-126.
37. Lee DD, Seung HS (1999) Learning the parts of objects by non-negative matrix factorization.
Nature 401: 788-791.
38. Cichocki A, Zdunek R, Phan AH, Amari S-i (2009) Nonnegative matrix and tensor
factorizations: applications to exploratory multi-way data analysis and blind source
separation: John Wiley & Sons.
39. Marrink SJ, Risselada HJ, Yefimov S, Tieleman DP, de Vries AH (2007) The MARTINI
force field: coarse grained model for biomolecular simulations. J Phys Chem B 111:
7812-7824.
40. Marrink SJ, Tieleman DP (2013) Perspective on the Martini model. Chem Soc Rev 42: 6801-
6822.
41. Vögele M, Köfinger J, Hummer G (2018) Hydrodynamics of Diffusion in Lipid Membrane
Simulations. Physical Review Letters 120: 268104.
42. Domanski J, Marrink SJ, Schafer LV (2012) Transmembrane helices can induce domain
formation in crowded model membranes. Biochim Biophys Acta 1818: 984-994.
43. Schafer LV, de Jong DH, Holt A, Rzepiela AJ, de Vries AH, et al. (2011) Lipid packing
drives the segregation of transmembrane helices into disordered lipid domains in model
membranes. Proc Natl Acad Sci U S A 108: 1343-1348.

44. Klingelhoefer JW, Carpenter T, Sansom MS (2009) Peptide nanopores and lipid bilayers:
interactions by coarse-grained molecular-dynamics simulations. Biophys J 96: 3519-
3528.
45. Ingolfsson HI, Melo MN, van Eerden FJ, Arnarez C, Lopez CA, et al. (2014) Lipid
organization of the plasma membrane. J Am Chem Soc 136: 14554-14559.
46. Ingolfsson HI, Carpenter TS, Bhatia H, Bremer PT, Marrink SJ, et al. (2017) Computational
Lipidomics of the Neuronal Plasma Membrane. Biophys J 113: 2271-2280.
47. Lopez CA, Sovova Z, van Eerden FJ, de Vries AH, Marrink SJ (2013) Martini Force Field
Parameters for Glycolipids. J Chem Theory Comput 9: 1694-1708.
48. Marrink SJ, de Vries AH, Mark AE (2004) Coarse Grained Model for Semiquantitative Lipid
Simulations. The Journal of Physical Chemistry B 108: 750-760.
49. Khelashvili G, Kollmitzer B, Heftberger P, Pabst G, Harries D (2013) Calculating the
Bending Modulus for Multicomponent Lipid Membranes in Different Thermodynamic
Phases. J Chem Theory Comput 9: 3866-3871.
50. Davis RS, Sunil Kumar PB, Sperotto MM, Laradji M (2013) Predictions of phase separation
in three-component lipid membranes by the MARTINI force field. J Phys Chem B 117:
4072-4080.
51. Baoukina S, Mendez-Villuendas E, Tieleman DP (2012) Molecular view of phase
coexistence in lipid monolayers. J Am Chem Soc 134: 17543-17553.
52. Carpenter T, López CA, Neale C, Montour C, Ingólfsson H, et al. (2018) Capturing Phase
Behavior of Ternary Lipid Mixtures with a Refined Martini Coarse-Grained Force Field.
Journal of Chemical Theory and Computation accepted.
53. Heberle FA, Feigenson GW (2011) Phase separation in lipid membranes. Cold Spring Harb
Perspect Biol 3.
54. Sodt AJ, Pastor RW, Lyman E (2015) Hexagonal Substructure and Hydrogen Bonding in
Liquid-Ordered Phases Containing Palmitoyl Sphingomyelin. Biophys J 109: 948-955.
55. Simons K, Sampaio JL (2011) Membrane organization and lipid rafts. Cold Spring Harb
Perspect Biol 3: a004697.
56. Garcia-Saez AJ, Chiantia S, Schwille P (2007) Effect of line tension on the lateral
organization of lipid membranes. J Biol Chem 282: 33537-33544.
57. Marrink SJ, Risselada HJ, Yefimov S, Tieleman DP, De Vries AH (2007) The MARTINI
force field: coarse grained model for biomolecular simulations. The journal of physical
chemistry B 111: 7812-7824.
58. de Jong DH, Baoukina S, Ingólfsson HI, Marrink SJ (2016) Martini straight: Boosting
performance using a shorter cutoff and GPUs. Computer Physics Communications 199:
1-7.
59. Bussi G, Donadio D, Parrinello M (2007) Canonical sampling through velocity rescaling. J
Chem Phys 126: 014101.
60. Berendsen HJC, Postma JPM, van Gunsteren WF, DiNola A, Haak JR (1984) Molecular
dynamics with coupling to an external bath. The Journal of Chemical Physics 81: 3684-
3690.
61. Parrinello M, Rahman A (1981) Polymorphic transitions in single crystals: A new molecular
dynamics method. Journal of Applied Physics 52: 7182-7190.
62. Abraham MJ, Murtola T, Schulz R, Páll S, Smith JC, et al. (2015) GROMACS: High
performance molecular simulations through multi-level parallelism from laptops to
supercomputers. SoftwareX 1-2: 19-25.

63. Alexandrov LB, Nik-Zainal S, Wedge DC, Campbell PJ, Stratton MR (2013) Deciphering
signatures of mutational processes operative in human cancer. Cell reports 3: 246-259.
64. Alexandrov BS, Alexandrov LB, Iliev FL, Stanev VG, Vesselinov VV (2018) Source
identification by non-negative matrix factorization combined with semi-supervised
clustering. Google Patents.
65. Alexandrov BS, Vesselinov VV (2014) Blind source separation for groundwater pressure
analysis based on nonnegative matrix factorization. Water Resources Research 50: 7332-
7347.
66. Rousseeuw PJ (1987) Silhouettes: a graphical aid to the interpretation and validation of
cluster analysis. Journal of computational and applied mathematics 20: 53-65.
67. Alexandrov LB, Nik-Zainal S, Wedge DC, Aparicio SA, Behjati S, et al. (2013) Signatures
of mutational processes in human cancer. Nature 500: 415.
68. Vesselinov VV, Alexandrov BS, O'Malley D (2017) Contaminant source identification using
semi-supervised machine learning. Journal of contaminant hydrology.
69. Iliev FL, Stanev VG, Vesselinov VV, Alexandrov BS (2018) Nonnegative Matrix
Factorization for identification of unknown number of sources emitting delayed signals.
PloS one 13: e0193974.
70. Stanev VG, Iliev FL, Hansen S, Vesselinov VV, Alexandrov BS (2018) Identification of
release sources in advection-diffusion system by machine learning combined with
Green's function inverse method. Applied Mathematical Modelling.
71. Stanev V, Vesselinov VV, Kusne AG, Antoszewski G, Takeuchi I, et al. (2018)
Unsupervised Phase Mapping of X-ray Diffraction Data by Nonnegative Matrix
Factorization Integrated with Custom Clustering. npj Computational Materials 4:43.
72. Kullback S, Leibler RA (1951) On information and sufficiency. The annals of mathematical
statistics 22: 79-86.
73. Xu Y, Yin W (2013) A block coordinate descent method for regularized multiconvex
optimization with applications to nonnegative tensor factorization and completion. SIAM
Journal on imaging sciences 6: 1758-1789.
769
770

Figure Legends

Figure 1. Illustration of a Nonnegative Matrix Factorization. The nonnegative matrix **X** is

decomposed to the product of a nonnegative matrix **W**, containing **K**=2 basis lipid configurations,

and nonnegative matrix **H**, containing the contributions of these two configurations in different

time points.

Figure 2. Corse-grained simulations of ternary lipid mixture. **(A)** Initial system setup for the CG

simulations. Lipids were initially randomly placed within the XY plane. Saturated lipid, DPPC, is

colored in green while unsaturated lipid, DOPC, is colored in red. Cholesterol is colored in white.

Water is not shown for clarity in depiction. **(B)** Lipid phase separation within 2 us simulation. The

updated CG force field shows clear phase separation into L_o (green) and L_d (red). Contrary, the

standard Martini lipid force field does not show preferential segregation in cholesterol rich

domains. **(C)** Time evolution of the normalized number of contacts between saturated and

unsaturated lipids, showing poor separation with the standard Martini force field.

Figure 3. Lateral radial distribution function for the different lipid combinations. RDF was

computing considering the center of mass of the molecules. The dashed blue line indicates the

chosen cut-off distance for profiling neighbor list needed for the NMFk matrix construction.

Figure 4. Outcome from NMFk analysis. **(A)** The Silhouette-Reconstruction criterium (see the

Methods Section). On the x-axis is denoted the number of basis lipid configurations and on the y-

axis-the average Silhouettes (right y-axis, red marking) as well as the Reconstruction (left y-axis,

the blue marking). The double arrow denotes NMFk estimates of the number of basis lipid

configurations. **(B)** Presentation of the columns H_i of the matrix H that encodes the weights of the

basis lipid configurations at given time frame. **(C)** A heatmap presenting the basis lipid

configurations ordered along x-axis according to the time interval they occurred from early time

to late as gathered from the corresponding weight-columns, H_i. The color gradient from white to

blue to red represents the increase in probability for a specific primary lipid to have a secondary

lipid neighbor within each basis lipid configurations. The increase in white and gray colors with

time is indicative of the evolution of the phase separation.

Figure 5. Visual inspection of simulations trajectories for evaluation of NMFk categorization

primary lipids according to their localization. Primary (DPPC) lipids are colored according to

NMFk output as purple (in nucleation domains) and yellow (out of nucleation domains) in MD

configurations corresponding to two time points. Secondary (DOPC) lipids are colored in red

and cholesterol in white. Insets highlight a particular region where lipids can be differentiated as

nucleating (purple) and boundary (yellow) lipids. As a comparison, the same region is

represented using the conventional way of addressing the distinction between saturated (green),

unsaturated (red) lipids, similar to Fig. 1.

Figure 6. Time dependent variation of the total number of nucleating primary (DPPC) lipids. **(A)**

The purple bars represent the total number of primary lipids in nucleation domains, as concluded

from their membership in different clusters of the corresponding basis lipid configuration, while

the primary lipids outside of any nucleation domain are presented by the yellow bars. The labels

on x-axis (the numbers) correspond to consecutive (in time) processes extracted from 0.45 us to 2

us simulation time. **(B)** The same distinction of nucleating primary lipids as in **(A)** obtained using

the normalized number of contacts of the lipids identified by NMFk. The same color scheme is

used. Black line corresponds to the normalized number of contacts using the total fraction of

saturated lipids (i.e., without making the distinction within the nucleating primary lipids).

Figure 7. Temporal description of membership profile of primary lipids as captured by NMFk

analysis. **(A)** The clear growth of nucleation domains with time, formed by primary lipids, is

extracted from the clusters containing primary lipids with low probabilities to have lipid-neighbors

of secondary type (refer **Fig. 4C**). The number of primary lipids that belong to nucleation domains

are colored in purple whereas those appear at the interface (edges of the nucleation domain) or

outside the nucleation domain are colored in yellow. The exponential growth of the number of the

primary lipids that continue to be in the same cluster demonstrated the evolution of the steady state

of the phase separation. The inset demonstrates the same process but at much later time (~ 20

microseconds) when the phase separation is in equilibrium. Here, although the minor changes still

exist, primary lipid membership numbers have stabilized. **(B)** Spatial visualization of the primary

lipid memberships extracted by NMFk analysis (between 0.45 us and 2 us). These primary lipids

were tracked using MD trajectories and rendered with the same color scheme as in **(A)** to

distinguish the primary lipids in and out of nucleation domains. Other lipids are not rendered (silver

background). The MD simulation box is represented as solid gray lines.

Table 1. The quality of reconstruction of X, estimated by the mean Pearson correlation between
the columns of X and columns of W*H.

Coarse-grained simulations of ternary lipid mixture	Time [us]	Mean Correlation Coefficient	Standard Deviation
Standard Martini	0.45 - 2	0.54	0.040
Updated Martini	0.45 - 2	0.90	0.020
	16 - 18	0.96	0.004

Figure 1