Making ATP fast and slow: do yeasts play a mixed strategy to metabolise glucose?

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Abstract

The ability of some microorganisms to switch from respiration to fermentation in the presence of oxygen -the so-called Crabtree effect- has been a fascinating subject of study at the theoretical and experimental fronts. Game-theoretical approaches have been routinely used to examine and explain the way a microorganism, such as yeast, would switch between the two ATP-producing pathways, i.e., respiration and fermentation. Here we attempt to explain the switch between respiration and fermentation in yeast by constructing a simple metabolic switch. We then utilise an individual-based model, in which each individual is equipped with all the relevant chemical reactions, to see how cells equipped with such metabolic switch would behave in different conditions. We further investigate our proposed metabolic switch using the game-theoretical approach. Based on this model, we postulate that individuals play a mixed game of glucose metabolism in the population. This approach not only sheds some light in the varieties of metabolic regulations that can be utilised by the individual in the population in competition with others for a common resource, it would also allow a better understanding of the causes of the Warburg effect and similar phenomena observed in nature.

Keywords: metabolic pathways, evolutionary game theory, metabolic regulation

Introduction

The viability of an organism depends on the fit between its phenotype and the environment it inhabits; an environment that includes the abiotic and biotic factors. When discussing the characteristics of living entities, Waddington enumerated three types of temporal changes that shape a living system: evolution, development, and physiology [1]. The different strategies that a microorganism utilises to tackle the environmental needs can be explained either in terms of Waddington's first type of temporal changes (evolution) or the last type of change (physiology).

In an evolutionary explanation, a given genotype have been shaped by evolutionary processes - i.e., natural selection, drift, mutation, & recombination. The genotype would translate into the phenotype which would affect the survival strategy of the organism. The physiological response, on the other hand, should consist of an apparatus that has

been shaped by evolution but is capable of responding to the environmental cues in much shorter time spans.

The "decision-making" in λ phage is a textbook example of an apparatus - in this case, a genetic switch. The λ phage switch has been shaped by natural selection so that it would give the virus a choice between two possible strategies (lysing the host or integrating within the host's genome), thus equipping the phage to respond to the transient conditions in a timely manner [2]. The "decision-making" approach to biological phenomena has been widely used (reviewed in [3]).

The ATP-producing pathways in *Saccharomyces cerevisiae* is a perfect example of a set of strategies that can be explained differently by invoking evolution or physiology. A yeast can either convert glucose through fermentation, a process that is fast but low yields, ≈ 2 moles of ATP per 1 mole of glucose, or go down the slower path -i.e., respiration-, and produce ≈ 32 moles of ATP per 1 mole of glucose [4]. Is the strategies utilised by a yeast a fixed response hardwired in its genome by the natural selection, or is it a physiological response, a distant relative of λ phage decision-making apparatus?

The characteristics of fermentation –i.e., fast and low in yield– and respiration –i.e., slow but high in yield– can be easily reformulated using a game-theoretical approach, where fermentation is cast as the "cheater" strategy and the respiration as the "cooperative" one. If the choice of the ATP-producing pathway is a fixed behaviour, determined by the genetics, then one could assume that the "selfish" strains would follow the dictum described by Hobbes as "the war of every man against every man" [5] and simply consume the glucose as fast as possible - through fermentation - to outcompete other yeasts in the environment. The game-theoretical approach is an attempt to explain why in nature microorganisms capable of both respiration and fermentation, do not always follow the principle of the maximisation of molar yield [6].

Pfeiffer *et al.* [7] led the charge in utilising the game-theoretical framework to address why yeasts would sometimes choose to ferment and other times to respirate: if every yeast would ferment, then the pool of glucose would drain so fast that each yeast would only get few ATPs. This "tragedy of the commons" is avoidable through respiration, which is viewed through game-theoretical prism as cooperation. Others further analysed and expanded this approach to explain the trade-off between yield and rate and the dynamic nature of pay-offs for each ATP-producing strategy in yeast (e.g., see [8, 9]). Aside from the trade-off hypothesis, some suggested that the accumulation of ethanol can be utilised by certain strains of yeasts to poison less-alcohol-tolerant strains in their niche [10]. The conditions of cooperation in microorganisms have been investigated experimentally as well (e.g., [8]).

Even the game-theoretical approach described above does not distinguish between a situation where different strains play "selfish" or "cooperative", something that would require the hand of evolution to intervene, or a scenario in which each yeast has the apparatus to play selfish AND cooperative in different measures to suit its temporal needs. In fact, in reformulating the fermentation/respiration dichotomy in the mould of evolutionary game theory, the "cheaters" and "cooperators" are usually considered different strains that compete for a shared resource (e.g., [11–13]).

In our view, there is no reason to preclude the possibility that individuals do mix these two ATP-producing strategies depending on the environmental conditions. Here, we propose a simple form of such model that allow individual yeast cells to play a

mixture of fermentation and respiration. When dealing with a population of organisms showing a mixture of two strategies –e.g., 25% cheating to 75% cooperation – the population-level phenomenon can be caused by two distinct situations at the level of the individuals: a) either 25% of individuals are exclusively utilising the cheating strategy, while 75% exclusively cooperate, or b) each individual mixes cheating with cooperation in 1 to 3 ratio. The same dilemma is applicable to *S.cerevisiae*, or any other microorganism capable of fermentation and respiration.

Here, we attempt to construct a simple regulatory network which makes it possible for a microorganism to combine fermentation and respiration as a mixed strategy. We utilise two models to investigate the ramifications of this regulatory network: firstly, simulating the chemical reactions relevant to the ATP-producing pathways at individual and population levels, and secondly, using a game-theoretical approach. Our results from the population-level modelling of chemical reactions show that such regulatory network affords yeasts to utilise a mixed strategy. The results from the game-theoretical framework demonstrates the inviability of pure strategy in this system. Finally, we suggest an experimental approach to distinguish between a population of yeasts taking advantage of a mixed strategy versus a population that consists of distinct cheaters and cooperators.

Model

Metabolic regulatory network for playing a mixed strategy

For yeasts to be able to mix cheating, i.e., glycolysis, with cooperation, i.e., utilising the TCA cycle, we postulate a regulatory network that is partly supported by the experimental works conducted on *S.cerevisiae*. In the ATP-producing pathways, pyruvate kinase seems to play an interesting regulatory role: in yeast, two paralogs of pyruvate kinase (PYK) exist: *PYK1* and *PYK2*. A comprehensive study by Gruning *et al.* [14] concludes that a switch from expressing *PYK1* to *PYK2* corresponds with a shift from fermentation to respiration and the accumulation of PEP suppresses the glycolytic pathway. Boles *et al.* [15] showed that the expression of *PYK2* is suppressed by glucose. Based on these experimental observations, we constructed a regulatory network that modulates the ATP-producing pathways (figure 1). The results from the experimental evolution in yeast is in accordance with our regulatory network: Comparing the gene expression patterns between different populations of *S.cerevisiaein* shows a decrease in *PYK1* expression in the evolved lines with reduced ethanol production in comparison with the parental lines [16]. One can suspect that many interactions can be included in this network, but a simple model like this, if correct, may explain the usage of ATP-producing pathways in a cell.

Modelling respiration and fermentation

In modelling glycolysis and the TCA cycle in a digital microorganism, we condensed the myriad of reactions into a few main reactions (Table 1). To simulate the chemical reactions we used Gillespie's first-reaction methods [17]. In this approach, the time for reaction i (τ_i) is

$$\tau_i = \frac{1}{a_i}\ln(\frac{1}{r}) \quad , \tag{1}$$

where a_i is the propensity of reaction i and r is a random number drawn from a uniform distribution. The reaction with the lowest τ is picked as the reaction that

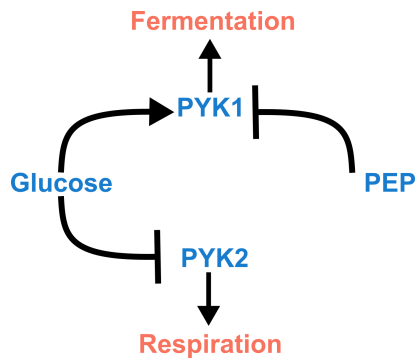

Fig 1. A simple regulatory network to explain utilising both ATP-producing pathways. Our proposed regulatory network imagines a simple switch between fermentation and respiration based on the experimental data.

occurs. Since the reaction constants are mesoscopic and dissimilar to deterministic rate constants [18], we choose values that result in biologically-reasonable behaviour in our digital microorganism.

In order to factor in the regulatory network (figure 1), in reactions #3 (fermentation) and #5 (the TCA cycle), we multiply the propensities of these reactions by the number of PYK1 and PYK2, respectively. For the activation of PYK1 (reaction #6) a Hill function is used to include the stimulating effect of glucose on PYK1 activation:

$$\theta_6 = \frac{a \times (\#GLC)^2}{b^2 + (\#GLC)^2} \quad , \tag{2}$$

where $a = 10^{-3}$ and $b = 30$. The propensity of the PYK1 inactivation reaction (reaction #8) includes a Hill function to take into account the inhibitory effect of PEP on this enzyme:

$$\theta_8 = \frac{a \times (\#PEP)^2}{b^2 + (\#PEP)^2} \quad , \tag{3}$$

where $a = 10^{-2}$ and $b = 1$. PYK2 inactivation is modelled in a similar fashion (reaction #9), where glucose exerts its inhibitory effect on PYK2 by facilitating the PYK2 inactivation reaction through a Hill function:

$$\theta_9 = \frac{a \times (\#GLC)^2}{b^2 + (\#GLC)^2} \quad , \tag{4}$$

where $a = 10^{-3}$ and $b = 30$.

In a population of cells in our model, each cell has its own set of chemical reactions (as described in Table 1). In each step of a simulation, all the first reactions in every cell is determined using Gillespie's method. Then, the cells execute their first reactions in the order of their reaction times –i.e., the first cell to execute its reaction has the lowest τ, while the last cell to proceed with its reaction has the largest τ. Afterwards, the population-level clock moves $\tau_{\max}$ forward. Each cell will undergo binary fission after accumulation of 20 ATPs. We assume that the biomass needed for division consumes all the ATP molecules in the mother cell, so after the division, daughter cells start with 0 ATPs and have to make ATPs afresh. The number of glucose molecules remain constant in the environment.

Table 1. The chemical reactions used to model respiration and fermentation.

#	Reaction	Propensity (a_i)	Parameters
1	$\mathrm{GLC} + 2\,\mathrm{NAD}^+ \longrightarrow 2\,\mathrm{PEP} + 2\,\mathrm{NADH}$	$k_1 \times \#(GLC) \times \#(NAD^+)^2$	$k_1 = 10^{-6}$
2	$\mathrm{PEP} \longrightarrow \mathrm{PYR} + \mathrm{ATP}$	$k_2 \times \#(PEP)$	$k_2 = 2$
3	$\mathrm{PYR} + \mathrm{NADH} \xrightarrow{\mathrm{PYK1}} \mathrm{EtOH} + \mathrm{NAD}^+$	$k_3 \times \#(PYR) \times \#(NADH) \times \#(PYK1)$	$k_3 = 10^{-2}$
4	$\mathrm{EtOH} + \mathrm{NAD}^+ \longrightarrow \mathrm{PYR} + \mathrm{NADH}$	$k_4 \times \#(EtOH) \times \#(NAD^+)$	$k_4 = 10^{-5}$
5	$\mathrm{PYR} \xrightarrow{\mathrm{PYK2}} 17\,\mathrm{ATP}$	$k_5 \times \#(PYR) \times \#(PYK2)$	$k_5 = 10^{-4}$
6	$\mathrm{PYK}_{\mathrm{1inactive}} \longrightarrow \mathrm{PYK}_1$	$\theta_6 \times \#(PYK1_{\mathrm{inactive}})$	See Eq. 2
7	$\mathrm{PYK}_{\mathrm{2inactive}} \longrightarrow \mathrm{PYK}_2$	$k_7 \times \#(PYK2_{\mathrm{inactive}})$	$k_6 = 10^{-3}$
8	$\mathrm{PYK}_1 \longrightarrow \mathrm{PYK}_{\mathrm{1inactive}}$	$\theta_8 \times \#(PYK1)$	See Eq. 3
9	$\mathrm{PYK}_2 \longrightarrow \mathrm{PYK}_{\mathrm{2inactive}}$	$\theta_9 \times \#(PYK2)$	See Eq. 4

* GLC: Glucose, PYR: Pyruvate, PEP: Phosphoenolpyruvate, EtOH: Ethanol, PYK: Pyruvate kinase.

Evolutionary Game-theoretical model of mixed metabolic strategy

The occurrence of respiration or fermentation pathways could be treated as a decision making process by rational players. Since they share the same resource for energy, the respiration pathway is considered as a cooperative strategy – with high yield/low rate– and the fermentation as a cheater strategy – with low yield/ high rate. Therefore, at any time, the population consists of a mixture of cooperators and cheaters. The goal in this approach is to find the evolutionary stable strategy (ESS), i.e., a set of strategies chosen by players which cannot be invaded by other strategies. In this approach, the selection criterion between these two choices for players would be based on the payoff matrix which shows the benefits gained by players as the result of their decisions. The payoffs depend on the amount of glucose as a crucial environmental factor.

The energetic benefit for a player utilising the respiration pathway is shown by V which is much more than the energetic benefit of the fermentation pathway, W. However, in each of the metabolic pathways, cells as players have to consume energy to synthesise enzymes, C and D in respiration and fermentation respectively and $C > D$.

The symmetric payoff matrix of the game (Table 2) represents the gain acquired by player 1 against player 2. According to this matrix, if two players choose the respiration pathway, the payoff –which is the gain in the respiration minus its cost– will be distributed equally between them. On the contrary, if both choose anaerobic pathway, again they should split the payoff (i.e., the gain in the fermentation case mines its enzymatic cost). However, the payoff for a cooperative strategy against a cheating strategy and vice versa, implicitly depends on the amount of glucose, as the rate of respiration and fermentation pathways are highly correlated with the glucose value. We define the ratio of the above rates with n as a nonlinear Hill function,

$$n = \frac{rate_f}{rate_r} = \alpha \frac{GLC^H}{GLC^H + K^H} \quad , \tag{5}$$

in which GLC and H indicates the glucose value and Hill exponent and K is the half

saturation value. This ratio, n, affects the off diagonal elements in the the payoff matrix (Table 2). For large amounts of glucose, n approaches its maximum value α; therefore, the payoff for a cheating strategy against a cooperation would be higher,

$$n \to \alpha \gg 1 \Rightarrow \quad n(W-D) \gg \frac{1}{n}(V-C) \approx 0 \quad . \tag{6}$$

As a result, when glucose is abundant, the fermentation/cheating would be the dominant strategy. On the contrary, in the case of glucose deficiency, n approaches zero. In this scenario, the cooperation would be reaping more benefit against cheating and would be the dominant strategy in this situation,

$$n \to 0 \Rightarrow \quad \frac{1}{n}(V-C) \gg n(W-D) \approx 0 \quad . \tag{7}$$

In a medium where the concentrations of nutrients constantly changes, the encounter between cooperation and cheating for a shared resource could be considered as a dynamic Hawk-Dove game. When the glucose is abundant, being a Hawk is the best response, in contrast, a Dove strategy will dominate the population when there is a shortage of glucose. When a moderate amount of glucose exists in the environment, neither of the strategies could invade the other one. In this range of resources, both subpopulations coexist simultaneously.

We can consider the dynamic of the strategies over time by the replicator equation. Assuming that x fraction of the population choose the strategy r with fitness f_r, and $1-x$ the f strategy, with fitness f_f, the replicator equation would be:

$$\dot{x}(t) = x(t)[f_r - \langle f \rangle] \quad , \tag{8}$$

in which $\langle f \rangle = f_r + f_f$ is the mean fitness of the population. This deterministic, nonlinear game theoretical equation, by considering the frequency dependent fitness for each strategy, calculates its frequency in the population over time. Based on the payoff matrix A in table 2, fitness of the cooperators could be defined as $f_r = Ax$, and $\langle f \rangle = x^T Ax$, where x^T is the transpose of x. We can rewrite the Eq. 8 as,

$$\begin{aligned} \dot{x}(t) = x(t)(1-x(t)) \quad & \left[\left(\tfrac{1}{2}(V-C) - n(W-D) + \tfrac{1}{n}(V-C) - \tfrac{1}{2}(W-D)\right) x(t) \right. \\ & \left. + \tfrac{1}{n}(V-C) - \tfrac{1}{2}(W-D)\right] \quad . \end{aligned} \tag{9}$$

The glucose effect is introduced through a new equation coupled with the replicator equation to reflect the consumption of glucose by cells and its influence on the payoffs:

$$\frac{dGLC}{dt} = l_1 \frac{GLC^H}{GLC^H + K^H} \left(\alpha_r x_r(t) + \alpha_f x_f(t)\right) \quad , \tag{10}$$

with K as the half saturation constant, and H the Hill exponent. The α_r and α_f, respectively, show the rate of respiration and fermentation pathways.

Results

The bias of the regulatory metabolic network in a single cell depends on the amount of glucose

While the raison d'être for the regulatory network espoused in this manuscript is to explain the metabolic behaviour of cells at the population level, it has ramifications for

Table 2. The payoff matrix of the game between respiration and fermentation strategies; the elements show the benefits to players 1 and 2 – from left to right, respectively– while the strategies in rows are selected by player 1.

		player 2	
		respiration	fermentation
player 1	respiration	$\left(\frac{1}{2}(V-C), \frac{1}{2}(V-C)\right)$	$\left(\frac{1}{n}(V-C), n(W-D)\right)$
	fermentation	$\left(n(W-D), \frac{1}{n}(V-C)\right)$	$\left(\frac{1}{2}(W-D), \frac{1}{2}(W-D)\right)$

a single cell in isolation as well. If a small number of glucose molecules are present in the environment, a cell would "choose" the respiration over fermentation (figure 2A). The low glucose means weaker activation of PYK1 and weaker repression of PYK2. Such behaviour is consistent with the yield-rate hypothesis as well, since in the absence of competition, there is no need for rapid consumption of glucose through fermentation ("cheating") and the payoff for respiration will be paramount.

Since glucose is the key regulatory element in our network, increasing the number of glucose molecules drives the regulatory networks towards fermentation (figure 2B and 2C). When the energy source in the environment is more abundant, the balance of the metabolic scale tilts towards faster energy production –i.e., fermentation– since there is no benefit to preferring the slower but more efficient path. It is worth-noting again that in our model, a cell, even in isolation, plays a "mixed" strategy and the choice between higher yield or faster rate is never binary.

The usage of ATP-producing pathways in a homogenous population depend on the population size

Interestingly, in the chemical-reactions model, the cells equipped with the regulatory metabolic network behave as one would expect within the confines of the yield-rate hypothesis. In the extreme case, where there are only two cells in a homogenous environment –i.e., an environment lacking any spatial structure– and only 2 molecules of glucose are accessible to them, the cells would opt for the "cooperative" strategy (respiration), since no "cheating" is justifiable with such a limited resource (figure 3A). Increasing the amount of accessible glucose to 100 molecules, immediately affect the behaviour of two cells: now they utilise a mixed strategy of respiration/fermentation where fermentation is dominant (figure 3B).

Increasing the number of cells to 100, with a low number of accessible glucose (5), results in a mixed strategy of respiration/fermentation. The smaller proportion of the average number of accessible glucose per cell, opting for higher yield is once again the priority (figure 3C).

Some PYK mutants can propagate in the population

In order to investigate how mutating the two key enzymes in our regulatory network, we introduced mutant strains into a population of wild-type cells. To model mutation, the rate of the activation reaction for an enzyme (reactions #6 and #7 for PYK1 and PYK2, respectively, as depicted in table 1), was multiplied by a coefficient (ζ). At the start of simulation, mutants and wild types were equal in number and each cell would duplicate after producing 20 ATPs.

If mutation results in the under-expression of PYK1 ($\zeta = 0.01$), then the mutant would dominate the population (figure 4A). The population growth, coupled with 100 accessible glucose in the environment, makes a more yield-oriented mixed strategy more suitable and the under-expression of PYK1 means that respiration will be the more dominant path in the mutant. Consequently these mutants would accumulate ATP faster and duplicate faster than the wild types. Over-expression of PYK1 ($\zeta = 100$) has the opposite effect; the mutants utilise a more rate-oriented strategy, but their wild-type rivals, which would respirate more, duplicate faster and dominate (figure 4B).

Under-expression of PYK2, results in mutants that prefer fermentation more and slightly edge out the wild-type cells (figure 4C). Over-expression of PYK2 has the opposite effect, since the wild types produce more ATPs in a shorter amount of time and duplicate faster (figure 4D). The under-expression of PYK2, simply reduces the inhibitory effect of glucose, while the over-expression of PYK2 means that the fates of these mutants are more affected by glucose as the major inhibitor.

The replicator dynamics indicates no pure strategy

Figure (5) shows the amount of glucose over time; as well, the changes in the frequency of two strategies. As it can be seen, for high value of glucose, almost all members of the population follow the cheater strategy as it has the highest payoff and does better against the other strategy, i.e. it is the ESS; however, by glucose consumption and decrease in its level, none of the strategies could invade the other one, therefore, there is not a pure strategy as the ESS. Under this circumstance, the ESS would be a mixture of the cheating and cooperation. For small amounts of glucose, the cooperative strategy has the highest payoff. As a result, it would be the dominant strategy which plays better than cheating; hence, all the population members have the tendency to this choice.

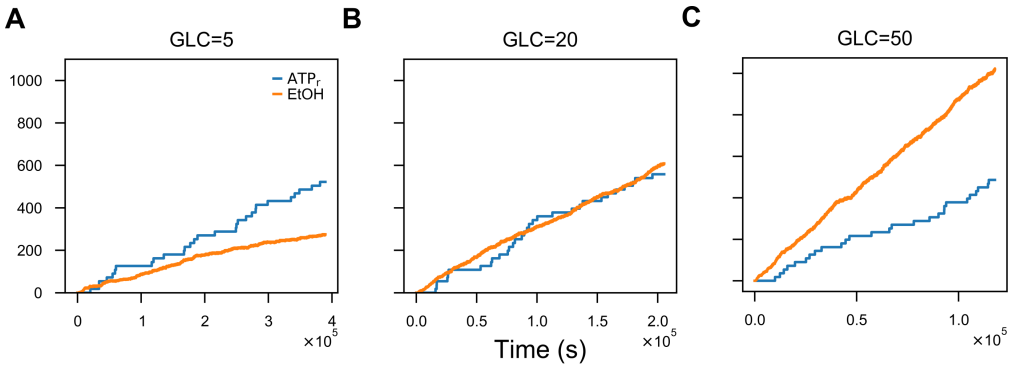

Fig 2. The effect of glucose concentration on the metabolic regulation of a single yeast cell. Each run indicates the change in the number of ATP molecules produce via the TCA cycle and the number of Ethanol molecules.

Discussion

The importance of the fermentation/respiration dichotomy in microorganisms is not a mere theoretical curiosity; the well-known tendency of cancerous cells to consume large amounts of glucose and metabolise it via fermentation, while oxygen is present in their *umwelt*, has been extensively studied since Ott Warburg observed it [19]. In spite of these studies, the biological causes of the Warburg effect have remained largely unresolved [20]. Understanding the underlying biology of the Crabtree effect -i.e., the

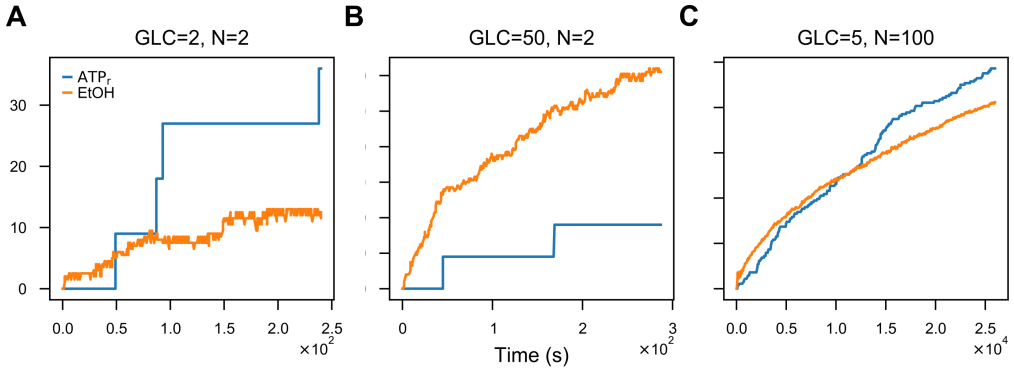

Fig 3. The population size differentially affects the metabolic regulation of a single yeast cell at different glucose concentrations. Each run indicates the change in the number of ATP molecules produce via the TCA cycle and the number of Ethanol molecules in a population of cells.

ability of microorganism to produce ethanol in the presence of oxygen is of extreme importance in the industrial endeavour to optimise ethanol production in yeast (reviewed in [21]).

Studying the alternative metabolic strategies have been a rather fruitful enterprise. Generally, different strategies are treated as distinct "strain" that do compete for a shared resource (e.g., see [22]). This approach simplifies the problem and allows to treat the problem similar to studying the invasion and fixation of mutant strain in well-mixed and structured populations. Here we propose that, alternatively, there could be no distinct cheaters and cooperators when it comes to alternative ATP-producing pathways.

Our result can provide a molecular basis for further optimisation of yeasts for ethanol production. Hitherto, environmental variables such as temperature or pH have been the focus of optimisation efforts to increase ethanol production (e.g., [23]). The manipulation of environmental conditions is a coarse-grain method based on the general effect of these conditions on the rate of chemical reactions. Our regulatory network would provide two alternative approaches: at a physiological level one can tune the concentrations of PEP and glucose so that the metabolic switch would tilt towards fermentation, or a site-directed mutagenesis targeting *PYK1* and/or *PYK2* can disable the switch such that the production of ethanol becomes an inevitability (as shown in figure 4).

The notion that cells might combine different strategies is not novel, but our results show that in the case of a microorganism equipped with alternative pathways for metabolising glucose, a simple experiment can distinguish between a population of microorganisms playing mixed strategy and a population composed of distinct respirators and fermentors. If we sample from a population where each individual respirates or ferments and measure the amount of ATP and ethanol produced in this sample, or result would vary form those of the population since by chance we could sample many more fermentors (or respirators) and thus proportion of respirators to fermentors would be different in our sample. On the contrary, if we sample from a population of mixed players, we would expect similar results from our sample compared to the population, since the proportion of respirators to fermentors observed at the population-level does not correspond to different individuals utilising different strategies,

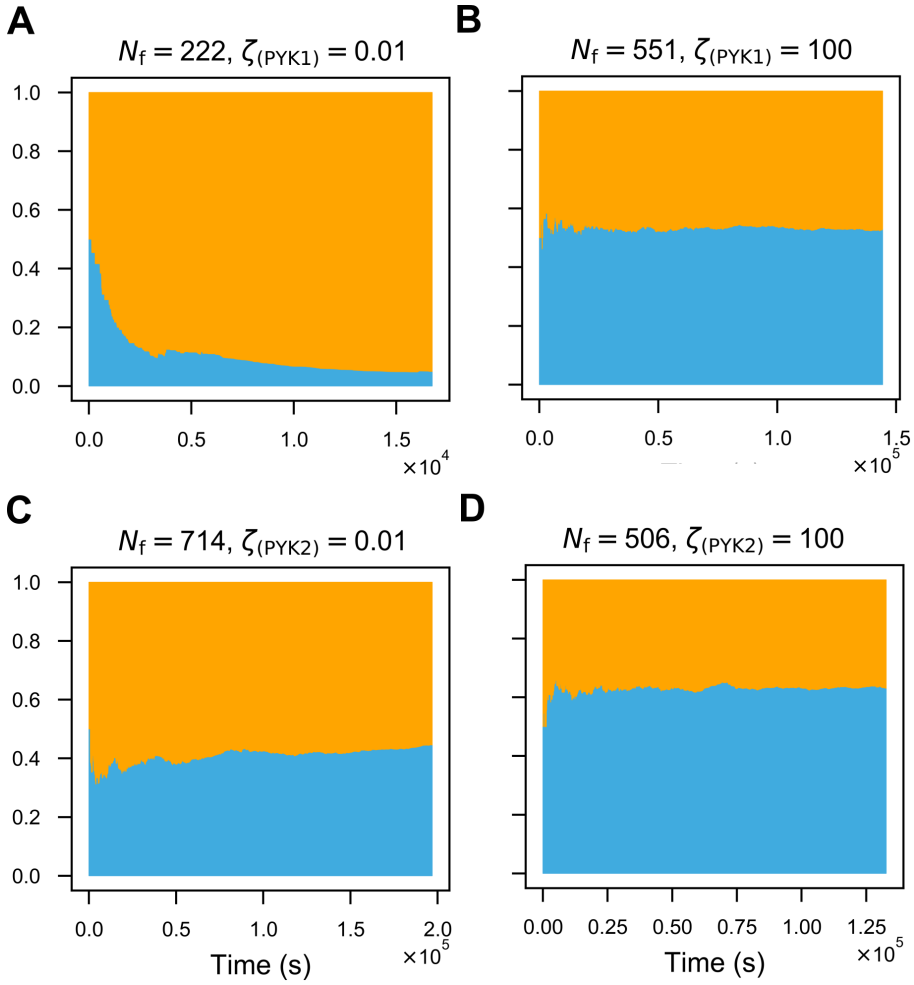

Fig 4. Investigating the effects of mutations on the regulatory functions of PYK1 and PYK2. Under-expression of PYK1 (A), over-expression of PYK1 (B), Under-expression of PYK2 (C), over-expression of PYK2 (D) are depicted here. Orange shows the frequency of the mutant strain and blue depicts the wild types. Each figure is the result of a single run of our simulation, starting from 5 wild types and 5 mutants. N_f indicates the total number of cells at the end of the simulation. ζ is a multiplied by the propensity PYK1 or PYK2 activation reaction to simulate over- or under-expression. 100 glucose molecules were present throughout the simulation.

but to individuals taking advantage of both pathways (figure 6).

It has not escaped our notice that one significant advantage of conceiving the biological details of the metabolic network is the ability to test the veracity of such regulatory scheme. The veracity of our proposed regulatory network can have significant ramification in developing anti-angiogenic drugs, given the over-reliance of cancer cells on glycolysis in place of the TCA cycle [24]. In spite of years of research on the Warburg effect, the biology of this phenomenon is still far from crystalline [20]. Unraveling the changes in the metabolic landscape of a cell as a result of cancer is an endeavour that has only recently been kickstarted [25]. Thus, little is known about the specific roles different metabolites and reactions play in driving cancerous cells to anaerobic ATP production, but our model can be an starting point to explore potential

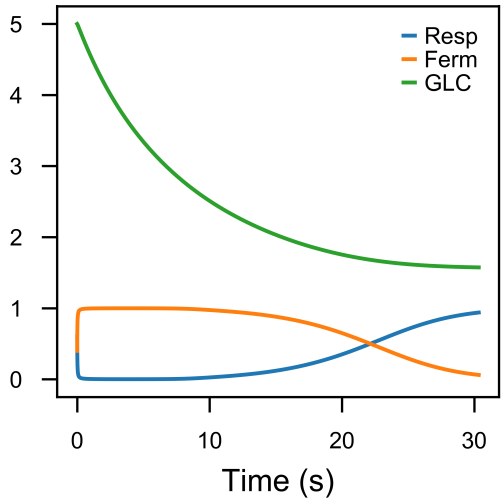

Fig 5. The frequency of two strains population over time as a function of glucose level based on the replicator equation (9). By reduction in the glucose level, cells with the respiration strategy (cooperators) invade the whole population.

targets to suppress anaerobic ATP production in malignant cells.

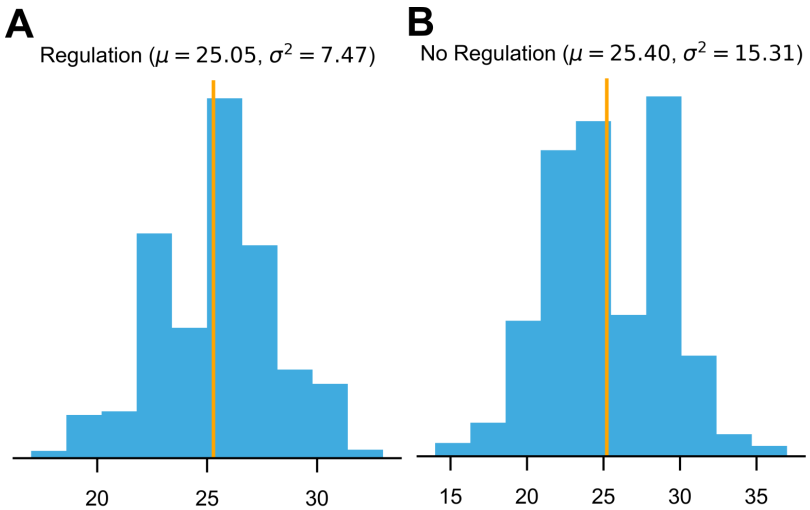

Fig 6. While average ATP productions can be identical between a population utilising a mixed strategy and a population where individuals respirate or ferment, the variances between the two would be drastically different (Bartlett's statistic= 124.16, $p - value = 7.75 \times 10^{-29}$).

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Availability of data and material

The software used to run all simulations was Python 2.7 and the scripts are available at `https://github.com/Kalirad/Making_ATP_fast_and_slow`.

Author contribution

M.S. conceived the model and helped draft the manuscript. H.S. and A.K. performed the simulations, developed the analytical calculations. A.K. drafted the manuscript. H.S. helped draft the manuscript. M.S. and H.S. critically revised the manuscript. All authors gave final approval for publication.

Ethics approval and consent to participate

Not applicable.

Consent for publication

Not applicable.

Competing interests

The authors declare that we do not have competing interests.

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