synder: inferring genomic orthologs from synteny maps

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¹ Abstract

Ortholog inference is a key step in understanding the evolution and function of a gene or 2 other genomic feature. Yet often no similar sequence can be identified, or the true ortholog 3 is hidden among false positives. A solution is to consider the sequence's genomic context. Δ We present the generic program, synder, for tracing features of interest between genomes 5 based on a synteny map. This approach narrows genomic search-space independently of 6 the sequence of the feature of interest. We illustrate the utility of synder by finding 7 orthologs for the Arabidopsis thaliana 13-member gene family of Nuclear Factor YC 8 transcription factor across the Brassicaceae clade. 9

10 1 Introduction

A powerful first step in understanding the evolution and function of a genomic feature is 11 resolving its genomic context, that is, comparing the feature to orthologous features in 12 other species. Comparing multiple orthologous features across species allows evolutionary 13 patterns to be uncovered. These patterns may include evidence of purifying selection, which 14 implies the feature is important to the survival of the species; positive selection, implying 15 the feature is rapidly evolving along one lineage; and functional dependencies between sites 16 (for example, amino acids in an enzyme reaction site) [1]. These evolutionary trends have 17 direct application in fields such as rational protein design [2]. Distinguishing between 18 orthologs (homologous features arising through speciation) and paralogs (homologous 19 features arising through gene duplication) is foundational to understanding the history of a 20 feature. Genomic context is also critical for discerning the origins of the often large 21 numbers of species-specific "orphan" genes that are found in most genome projects [3–6]. 22 Identifying orthologs is not easy. A simple sequence similarity search of a query feature 23 (e.g., a gene, transposon, miRNA, or any sequence interval) against a genome or proteome 24 of a target species may obtain thousands of hits in a swooping continuum; these could 25 include: the true ortholog, related family members (paralogs), and non-specific hits. 26 Therefore, methods for winnowing the search results have been developed to identify the 27 true orthologs. A straightforward approach to identify orthologs of protein-coding genes is 28 reciprocal best hits [7]. In this technique, a protein encoded by a gene from the focal species 29 is searched (e.g. with BLAST) against the target proteome. The highest scoring gene is 30 then searched back against the proteome of the focal species. If the top scoring hit of the 31 second search is the original query gene, then the two genes are accepted as orthologs. 32 There are also methods that build on reciprocal best hits, such as the reciprocal smallest 33 distance method that considers evolutionary distance in addition to similarity score [8]. 34 Little or no significant sequence similarity is expected across species for some classes of 35

features. A lack of significant similarity may stem from sequences being very short (e.g., a 36 single promoter element or an miRNA) or it could result from very rapid mutation rates in 37 the feature (e.g., intragenic intervals that are under little or no purifying selection). 38 Orphan genes, which by definition have no protein homolog in related species, are an 39 example of a feature for which sequence comparisons alone cannot delineate the region in 40 the target genome from which the orphan gene arose [4]. These genes are often both short 41 and rapidly evolving, making it very difficult to find orthologous genomic regions (possibly 42 non-coding) even in closely-related target species. Without an ability to identify 43 orthologous genomic intervals, the pathway of evolution of an orphan cannot be 44 determined; for example, orphans of *de novo* origin cannot be distinguished from those 45 orphans that stem from rapid mutation [3]. 46

Purely sequence-based methods are also problematic if the true ortholog of a query gene is duplicated in the target species. In this case, the target species contains two genes that are true orthologs of the query gene. The co-evolution of duplicate genes relative to their singleton ortholog, is of interest in theoretical evolution [9]. One of the copies may rapidly evolve to gain a new function or it may become a pseudogene [10]. In either case, the reciprocal best hits method would find only the conserved copy.

A different approach to ortholog identification, one which does not depend on the genome-wide sequence similarity of the query features themselves and that does handles duplication events, is to consider the genomic context of the query, i.e., synteny [11]. Genomic synteny is the conservation of the order of genomic features between two genomes [12].

The most obvious approach to a context-based search is to include the flanking regions of a query feature of interest when searching for an ortholog in the target genome. This approach is used by MicroSyn [13] for finding orthologs of features, such as miRNAs, that are too short and numerous to be easily searched by their sequence alone. While this

approach works well for an individual query feature, extending it to a high-throughput
analysis is problematic, since no single cutoff for flank length will work well for all cases.
For instance, a sequence residing within a highly repetitive centromere might require flanks
of megabases.

An alternative to looking at the flanking sequence of each query feature individually is 66 to reference a genome-wide synteny map. Rather than searching for the feature directly, 67 orthologs of flanking syntenic regions (blocks) can be identified, and a potential ortholog of 68 the query feature can be identified in the target genome by searching within the syntenic 69 region. This strategy has been applied to study the genomic origin of orphan genes [14] 70 (and the method refined in [15]) where a map of one-to-one orthologous genes was used to 71 infer the orthologous genomic intervals where the non-genic sequence corresponding to the 72 orphan genes is expected to reside. The one-to-one map made the computational problem 73 very easy, and could effectively identify a sub-set of the genes of *de novo* origin, but the 74 map was very coarse, especially in regions of low gene density, so no information is 75 obtained for other orphan genes. 76

There are many programs designed to build synteny maps. Some programs build sparse
synteny maps from given sets of orthologous genes (e.g., OrthoClusterDB [16]). Others
perform full genome alignments. Of these, some focus on large scale (megabase range)
syntenic blocks that are conserved across great evolutionary distances (e.g.,

DiagHunter [17]), while others focus on micro-synteny, producing maps of many small
syntenic blocks that capture local inversions, duplications and deletions (e.g., BLASTZ [18],
MUMmer4 [19], and Satsuma [20]). These micro-synteny programs are of greatest interest in
this paper.

The diverse synteny mapping tools, though highly variable in granularity and accuracy [11,21], provide powerful approaches to enable the study of comparative genome evolution [12,22–24] and to glean novel information about the origin of *de novo* orphan

genes [14, 15, 25–27]. However, the use of these maps as a tool for orthology has been generally limited to either manual inspection, or to considering only those query features that overlap syntenic blocks.

synder is designed to infer orthologous regions in the target genome, even when the 91 orthologs are *between* syntenic blocks, and to assess the quality of the inferences. To do 92 this, it traces query features from a focal genome to a target genome using a whole-genome 93 map. synder is a high-performance program with a core written in C++ and an R 94 wrapper for integration into R workflows. It will work with any synteny map, but was 95 designed for fine-grain micro-synteny maps that capture local inversions and transpositions. 96 It assembles collinear sets of syntenic blocks from the map and uses them to infer tight 97 search intervals for each query on the target genome, naturally handling duplication events 98 and inversions. synder also provides detailed information about the quality of the search 99 result. The only input required is a whole-genome synteny map and a set of features of 100 interest in the focal genome. Thereby, synder automates the use of syntenic information to 101 study orthologs across any pair of species with sufficiently conserved synteny. 102

103 2 Algorithm

The primary function of synder is to map a user-designated set of query features in the focal genome to a set of search intervals in a target genome (see **Table 1** for terminology and **Figure 1** for overview). To do this, synder contextualizes the query features based on a user-provided synteny map for the focal and target genomes. Query features of the focal genome are mapped to an associated synteny-based search interval on the target genome; this search interval delineates the region of the target genome where the query feature is predicted to be located.

Algorithm 1 is an overview of the synder's search algorithm. Each of the functions in

	Table 1: Terminology
focal genome:	The genome that contains the query features.
target genome:	The genome in which search intervals are found for each feature of
	interest.
query feature:	The sequence interval delineating any feature of interest in the focal
	genome. This could be a protein-coding gene, an miRNA, an intron,
	a transposon, a nucleotide repeat, an lncRNA or any other genomic
	feature
blocks:	Focal and target genome intervals that are inferred to be orthologs
	by an outside synteny program.
synteny map:	A set of blocks for a pair of genomes.
syntenic interval:	A single interval on one side of a synteny map.
adjacent intervals:	Two syntenic intervals on the same scaffold with no syntenic interval
	located entirely between them.
collinear blocks:	Two blocks where both the focal and target syntenic intervals are
	adjacent and in the same orientation.
collinear block set:	An ordered set of blocks where block i is collinear to block $i + 1$.
query context:	All blocks that overlap or are adjacent to the query interval.
search interval:	An expected location of an ortholog of a query feature in the target
	genome.
search space:	The union of search intervals for a given query interval.
synteny score:	A score for a syntenic block produced by the outside synteny pro-
	gram.
synder score:	A score for the relative reliability of a search interval (see Figure 5).

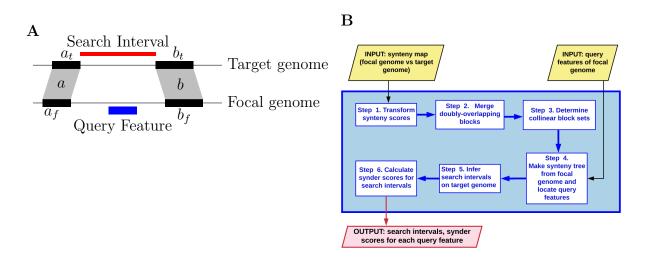


Figure 1: The synder algorithm identifies search intervals for query features based on synteny. (A) Diagram of a very simple syntenic relationship across focal and target genomes. a_f, a_t, b_f , and b_t are four syntenic intervals that comprise block a (a_f, a_t) and b (b_f, b_t) . Blocks a and b are collinear and provide landmarks for associating the query feature in the focal genome with its search interval in the target genome. (B) Flow chart of the steps in the synder algorithm. synder: 1) transforms the synteny scores for each of the blocks in an input synteny map, such that scores are additive; 2) merges doubly-overlapping blocks; 3) assigns each block in the synteny map to exactly one collinear set of blocks; 4) finds the overlapping or nearest flanking syntenic intervals for each query feature in the focal genome (e.g., a_f and b_f in A); 5) for each query feature (i.e. the interval corresponding to a feature of interest on the focal genome) finds all collinear block sets that contain at least one of the blocks that flank or overlap the query feature, and then relative to each of these collinear block sets, maps the query interval to a search interval in the target genome; and 6) calculates search interval scores for each query feature relative to the search interval of each collinear set. The final output provides the query features with their corresponding hits in the target genome and a composite score for each hit.

¹¹² this algorithm is defined in detail in the subsequent sections.

```
1 function synderSearch(\vec{q}, M, r, k, t):
         \vec{s} = \texttt{transformScores}(M, t)
 \mathbf{2}
         M' = mergeOverlapping(M, \vec{s})
 3
        C = \text{collinearSets}(M', k)
 \mathbf{4}
        T = \text{buildTree}(M')
 5
        foreach q in \vec{q} do
 6
             \vec{a} = \operatorname{anchors}(q, T)
 \mathbf{7}
             \vec{c} = \text{searchSets}(\vec{a}, C)
 8
             for
each c in \vec{c} do
 9
                  (i, b) = \texttt{searchInterval}(q, c)
10
                  s = \texttt{score}(q, c, r)
11
                  recordRow(q, i, s, b)
12
13
             end
         end
\mathbf{14}
```

Algorithm 1: A high-level overview of the core synder search algorithm. \vec{q} , list of query features; M, synteny map; r, search interval score decay rate (see Figure 5); k, number of interrupting blocks that is tolerated; t, type of synteny score; \vec{s} , vector of transformed, additive scores used in assigning final scores to each search interval. synder transforms scores and merges overlapping blocks to yield a processed, reduced synteny map, M'. Sequential syntenic blocks, C, are determined from M'. T, the interval tree data structure, is then used to find the syntenic context (i.e., the anchors, \vec{a}) on the focal genome for each query feature, q. Next, query features are mapped to one or more collinear set of blocks, \vec{c} . For each block, the associated search interval, i, is identified and the type of boundary, b, is determined. Each search interval is given a synder score, s. Finally, each search interval is recorded in the output table as a single row including the query feature (q), search interval (i), synder score (s), and search interval type (b).

¹¹³ 2.1 Input Synteny Map

The primary raw input to synder is a synteny map that is provided as a table where each row describes one block. Each block consists of: an interval in the focal genome; an inferred syntenic interval in the target genome; a synteny score representing some metric of the confidence that the pair of intervals is orthologous; and, the relative orientation of the intervals. The focal and target intervals are each described by a chromosome/scaffold name and a start and stop position. The synteny score for each block is some measure of quality/certainty (e.g., percent identity or p-value) that is specific to the tool that used to generate the map. The orientation of the block is the strand in the target genome relative to the query, with '+' indicating the same strand and '-' indicating the inversion.

¹²³ 2.2 Step 1. Transform syntemy scores

The synteny scores for the blocks in a synteny map may be expressed in a variety of ways 124 by the various synteny programs. Strong similarity may be represented by low numbers 125 (e.g., if scores are e-values) or high numbers (e.g., if scores are bitscores). Scores may be 126 additive (e.g., bitscores) or averaged (e.g., percent similarity). The user must specify the 127 type of the input synteny scores. Internally, the synder algorithm transforms these scores 128 so that they are additive. More specifically, synder assumes S(a + b) = S(a) + S(b), that 129 is, if the blocks a and b are concatenated, then the syntemy score should be equal to the 130 sums of the scores for blocks a and b. synder transforms the synteny map scores to an 131 additive score using one of the transforms below: 132

$$\operatorname{transformScore}(s,l) = \begin{cases} \operatorname{score \ density} & l * s \\ \operatorname{percent \ identity} & l * s/100 \\ \operatorname{e-value \ or \ p-value} & -log(s) \\ \operatorname{otherwise} & s \end{cases}$$
(1)

133

Where s is the input synteny score and l is the interval length. synder transforms the scores when it loads a synteny file, updates them as needed in Step 2, and ultimately uses them in Step 6 to generate scores for the final search intervals.

¹³⁷ 2.3 Step 2. Merge doubly-overlapping blocks

In a "perfect" synteny map, blocks would not overlap on both the focal and target sides. In practice, however, synteny algorithms occasionally produce overlapping blocks. These cases would produce multiple collinear block sets that have the same orientation and cover the same region. To avoid this, **synder** merges any blocks that overlap on both the focal and target sides. The interval of the merged blocks is the union of the overlapping block intervals. The **synder** score of the merged blocks is calculated by summing the non-overlapping interval scores with the maximum of the overlapping intervals:

$$S_{ab} = d_a(l_{a_f} - l_o) + d_b(l_{b_f} - l_o) + l_o \max(d_a, d_b)$$
⁽²⁾

Where d_a and d_b are the score densities of blocks a and b (density is the synteny score for a block divided by the length of the syntenic interval on the focal genome); and where l_{a_f} , l_{b_f} and l_o are the lengths of a, b, and their overlap, respectively.

A potential downside of this approach is that, when more than two intervals are 148 doubly-overlapping, the order in which the scores are merged matters, with blocks merged 149 later having a stronger influence. A second issue is that the merged score is calculated 150 based on the intervals on just one side of the synteny map. The length of each interval, and 151 the length of the overlap between the intervals, may vary between the two sides of the 152 synteny map. For now, we do not address either of these issues, since doing so would 153 complicate the algorithm and probably have little effect on any biological dataset (since 154 doubly-overlapping intervals are uncommon). 155

156

The output of Step 2 is a processed synteny map without doubly-overlapping blocks.

¹⁵⁷ 2.4 Step 3. Determine collinear block sets

¹⁵⁸ synder assigns each block in a synteny map to exactly one set of collinear syntenic blocks

(Figure 2). Each collinear block set consists of adjacent blocks that are ordered on the 159 query and target sides. synder considers two syntenic intervals "adjacent" if they are on 160 the same scaffold and no syntenic interval is contained entirely between them. Adjacency 161 on the target-side further requires that the intervals have the same orientation (+/-)162 relative to the focal genome. Two blocks are collinear if the syntenic intervals on the 163 focal-genome and target-genome are adjacent. The collinear block sets may be inverted 164 and/or may overlap other collinear block sets on either the focal or target side (e.g., for 165 duplicated sequences). The individual blocks that make up the collinear set are used in 166 Steps 4 and 5 to delimit the search intervals on the target genome relative to each query 167 feature of the focal genome. 168

This approach can be overly strict, resulting in many small collinear block sets. Tracing 169 blocks across whole genome duplication, and subsequent genome alterations [28], is 170 particularly challenging, since intervals in the homologous chromosomes could randomly 171 diverge, resulting in a synteny map that alternates between mapping to one chromosome 172 and the homologous chromosome. This is especially problematic in plants, where whole 173 genome duplications are common [29]. To reduce this potential complication, synder 174 provides the user an option to relax the adjacency restriction by allowing k syntenic 175 intervals that map to alternative target scaffolds to interrupt a pair of query-side intervals 176 in a collinear set. 177

The output of Step 3 is the set of blocks that are non-overlapping and adjacent. Each block is assigned to exactly one collinear block set.

2.5 Step 4: Find the contextual anchors on the focal genome for each query feature

The next step is to find the blocks that contain, overlap, or are adjacent to each query feature on the focal genome. These blocks will provide "anchors" that will be used in Step 5 to map the query feature to one or more collinear sets of blocks in the target genome and hence to identify the search interval(s) in the target species.

¹⁸⁶ The user provides the query features as a Gene Feature Format (GFF) file that

¹⁸⁷ describes the genomic intervals on the focal genome corresponding to the query features of

¹⁸⁸ interest. A modification is to provide the GFF file along with BLAST or other

¹⁸⁹ whole-genome similarity scores; this modification was used as input for the case study on

¹⁹⁰ the NF-YC gene family (see RESULTS section).

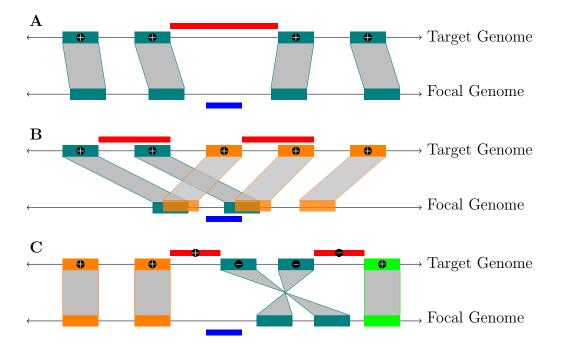


Figure 2: Collinear block set construction with focal-genome "anchors" to infer search intervals on the target genome. The **blue bars** below each focal genome are the query features. Genome-wide collinear block sets (colored orange, teal or green) are identified in Step 3, and are used to identify the focal-side anchors for each query feature in Step 4. The **red bars** above the target genome are the search intervals inferred by **synder** in Step 5. (A) a simple case where the query feature does not overlap a syntenic interval and is bound between syntenic intervals in a collinear set of blocks. (B) a tandem duplication where **synder** resolves the blocks into two collinear block sets (teal and orange) and infers search intervals for each. (C) a query feature that is **unbound** on each side (see **Figure 4**) resulting in one search interval relative to the inverted teal block collinear set (red bar on right). (+/-) signs in the target search intervals represent their strand orientation relative to the query ('-' is an inversion).

synder uses a modified interval tree algorithm to locate the syntenic intervals on the focal genome that "anchor" the query feature. Building the interval tree is an $O(n \log(n))$ operation (see Algorithm 2) and searching for a given interval is $O(\log(n) + m)$, where mis the number of overlapping intervals returned and n is the size of the synteny map (see Algorithm 3). We modified an algorithm that returns only directly overlapping intervals [30], to enable synder to find the flanking intervals (upstream and downstream intervals) when no overlapping intervals are found (see Figure 3).

```
1 function buildTree(\vec{q}):
```

```
2 | if length(\vec{q}) == 0 then
3 | return Null
```

```
\begin{array}{c|c} \mathbf{4} & \mathbf{end} \\ \mathbf{5} & c = \operatorname{midpoint}(\vec{q}) \\ \mathbf{6} & \vec{v}_{left} = \operatorname{filter}(\vec{q}, \, \boldsymbol{\lambda} \; q \rightarrow c < q_1) \\ \mathbf{7} & \vec{v}_{mid} = \operatorname{filter}(\vec{q}, \, \boldsymbol{\lambda} \; q \rightarrow q_1 \le c \le q_2) \\ \mathbf{8} & \vec{v}_{right} = \operatorname{filter}(\vec{q}, \, \boldsymbol{\lambda} \; q \rightarrow q_1 < c) \\ \mathbf{9} & T_{left} = \operatorname{buildTree}(\vec{v}_{left}) \end{array}
```

```
10 T_{right} = \text{buildTree}(\vec{v}_{right})
```

11 return Tree($c, \vec{v}_{mid}, T_{left}, T_{right}$)

Algorithm 2: Build a synteny interval tree. buildTree takes a vector of intervals, \vec{q} , on a given scaffold/chromosome of the focal genome and returns an interval tree data structure. The midpoint c is an integer equal to the middle position in the interval in the middle of the vector of intervals (by index). If the input vector is sorted, then the midpoint will tend to be near the center of the scaffold. filter(\vec{q} , f) selects the subset of intervals in \vec{q} for which the condition f(q) is true. The filters in lines 6-8 partition each element in \vec{q} into one of three sets: intervals on the left of the midpoint c, intervals overlapping the midpoint c, and intervals on the right of the midpoint c. New trees are created recursively for the left (less than) and right (greater than) sets of intervals. buildTree returns a new syntenic interval Tree object, (T), that stores the midpoint c, all overlapping syntenic intervals (\vec{v}_{mid}), and the left and right child trees. The Tree will be used in Algorithm 3 to identify the anchors for each query feature.

```
1 function search(T, t, q):
        if t = Null then
 \mathbf{2}
             return Empty
 3
        end
 \mathbf{4}
        \vec{r} = []
 \mathbf{5}
        if t_{midpoint} < q_1 then
 6
             for each i in stopSorted(t) do
 7
                  if q_1 \leq i_2 then
 8
                     \vec{r}.add(i)
 9
                  end
10
             end
11
             if t_{right} = Null and length(r) = \theta then
12
                 \vec{r}.add(opposite(T, t))
\mathbf{13}
             end
14
             \vec{r}.add(search(T, t_{right}, q))
\mathbf{15}
        end
16
        else if t_{midpoint} > q_2 then
\mathbf{17}
             for each i in startSorted(t) do
\mathbf{18}
                  if q_2 \geq i_1 then
19
                      \vec{r}.add(i)
\mathbf{20}
                  end
\mathbf{21}
             end
22
             if t_{left} = Null and length(r) = 0 then
23
                  \vec{r}.add(opposite(T, t))
24
             end
25
             \vec{r}.add(search(T, t_{left}, q))
26
        end
\mathbf{27}
        else
\mathbf{28}
             foreach i in startSorted(t) do
29
30
                  \vec{r}.add(i)
             end
31
             \vec{r}.add(search(T, t_{left}, q))
\mathbf{32}
             \vec{r}.add(search(T, t_{right}, q))
33
        end
34
        return \vec{r}
35
```

Algorithm 3: Given the input of a syntenic interval tree (T), the current node in the tree (t), and a query feature (q), find all syntenic intervals in the focal genome that overlap the query feature. \vec{r} . add (\vec{x}) means intervals \vec{x} are added to the search result \vec{r} . q_1 and q_2 represent the left- and right-hand edges of the query feature. i is an interval in the interval tree. $t_{midpoint}$ is the midpoint of the current node in the tree. t_{left} and t_{right} and the left- and right-hand subtrees. If no intervals are found, the opposite function returns the nearest blocks on each side of q (see Figure 3).

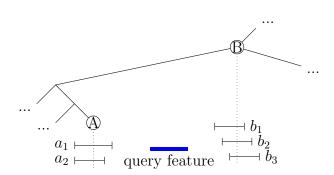


Figure 3: Identification of the syntenic intervals that anchor a query feature on the interval tree from the focal genome. A and B are nodes in the interval tree. A stores the overlapping syntenic intervals a_1 and a_2 . B stores the overlapping intervals b_1 , b_2 and b_3 . The query feature falls between the syntenic intervals stored in nodes A and B. The interval tree algorithm first makes the tree, and then finds the nearest node to the query. If the closest node found is A, and the nearest syntenic interval (a_1) detected is on the left side of the query feature, then the algorithm will trace the tree until it finds the first node to the right of the query feature (i.e., node B). Conversely, if the closest node found is to the right of the query feature (node B), then the tree is traced one branch to the left, and then as many branches to the right as possible (i.e., until node A is found). In either case, all overlapping nodes in A and B are returned as the anchors for this query sequence.

¹⁹⁸ 2.6 Step 5. Map query features and infer search intervals on the

199

target genome

Each query feature is mapped to a search interval that is created with respect to each 200 associated collinear block set (Figure 2). To do this, synder first classifies each edge of 201 the query feature relative to its relationship to an associated collinear set of blocks (Figure 202 4), where each query feature edge may fall: 1) between two collinear sets of blocks 203 (unbound); 2) inside a block (inblock); 3) between blocks comprising a collinear block set 204 (bound); or 4) beyond all blocks, i.e., near the beginning or end of the scaffold (extreme). 205 synder sets each boundary of the target genome search interval to the nearest edge of a 206 block in the collinear set if the edge is **inblock** or **bound**; to the nearest syntenic interval 207 beyond the collinear set if the edge is **unbound**; or to the end of the scaffold if the edge is 208 extreme (see Figure 4). 209

If a search interval is bound by two blocks, a and b, which define the two bounding

intervals, $[a_1, a_2]$ and $[b_1, b_2]$, then the search interval be the inclusive interval $[a_2, b_1]$. We use an inclusive interval, rather than the exclusive interval from $(a_2 + 1)$ to $(b_1 - 1)$, to avoid negative length intervals that would occur when $b_1 = a_1 + 1$ (as would occur if there is a deletion in the target genome).

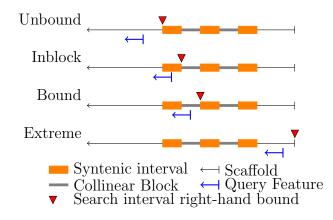


Figure 4: Snapping rules to define the location of the search interval edges on the target genome. 1) The left and right edges of the query feature are used to define the search interval relative to a given collinear block. Only the target genomes and the right edge of the query featured (represented by perpendicular line on query feature) are shown. 2) The right-hand edge of the search interval is then assigned (red triangles) (Rules are the same for the left edge). Unbound: the edge does not overlap the collinear block set. Inblock: the edge is inside a syntenic interval. Bound: the edge is between intervals in a collinear block set. Extreme: the edge is beyond any syntenic interval (near end of scaffold).

215 2.7 Step 6. Calculate scores for each collinear set relative to each overlapping query feature

synder calculates the synder score for each input query feature relative to each associated collinear block set (Figure 5). The score reflects the intuitive ideas that: 1) query features are more reliable if a greater proportion of their sequence overlaps blocks in a collinear set; and, 2) query features are more reliable if they are within collinear block sets that are densely packed. In cases where many possible search intervals are identified for a given query feature, the synder scores can be used to compare the relative quality of the search

intervals. The synder score is especially important when k (the number of interrupting blocks that is tolerated) is high, since a large k allows large gaps between blocks in the collinear block sets. The pseudocode for synder's scoring algorithm is shown in Algorithm 4. Note that input scores for syntenic blocks have been transformed to be additive (Equation 2.2 (Step 1)).

```
1 function score(q, \vec{b}, r):
          s = 0
 2
          foreach b in \vec{b} do
 3
                o = \operatorname{overlap}(q, b)
 4
                d = b_{score}/(b_2 - b_1 + 1)
 \mathbf{5}
                s += d * (o_2 - o_1 + 1)
 6
                if b_1 < q_1 then

| s += d \int_{q_1-b_1}^{\max(0,q_1-b_2)} e^{rx} dx
 \mathbf{7}
 8
                end
 9
                if b_2 > q_2 then

| s += d \int_{b_2-q_2}^{\max(0,b_1-q_2)} e^{rx} dx
10
11
                end
12
           end
13
           return s
\mathbf{14}
```

Algorithm 4: Calculating the synder score (s) for a query feature and the set of collinear blocks from the target genome to which it is anchored. q is the query feature, b is a focal genome-side syntenic interval within collinear block set \vec{b} , and o is the intersection (of zero length or greater) between q and b. The start and end points (edges) of the query feature q are q_1 and q_2 (as for edges of b and o). b_{score} is the syntemy score associated with syntenic interval b. r is an adjustable parameter, the decay rate.

In Algorithm 4, each block in the collinear block set can contribute to the total synder score (Figure 5). The score decay rate is controlled by the adjustable parameter r. For the default settings, the weight of the scores of blocks that neither overlap nor partially overlap the query feature decays exponentially with the absolute distance from the nearest query feature bound on the focal side. If the user sets r to be a low positive number, the weight at a given position will fall slowly with distance from the query interval (e.g., when r = 0.001 the weight will fall by half by 1000 bases from the nearest query feature bound);

thus, all blocks in the collinear set will contribute to the score, but they matter less with distance (Figure 5, r > 0). r = 0 would give equal weight to all blocks in the collinear set, in that case, the density of the map will not affect the score, and the score would simply be equal to the sums of the total scores for all the syntenic blocks. A high value, such as r = 100, would completely ignore genomic context, basing the query feature score only on the portions of syntenic blocks that overlap the query feature. With this r setting, the synder score would be 0 if the query feature does not overlap any syntenic block.

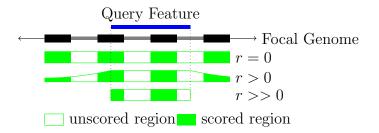


Figure 5: Calculation of synder score for a query feature relative to a collinear block set. **Black bars:** the collinear set of syntenic blocks that anchor the focal genome to the target genomes. (Only depicted on focal genome.) The total score of the search interval is the sum of the scores for each block. The score for each block, relative to the query feature (blue bar), is equal to the syntemy score for the block times the "weight" of the block (determine by the adjustable parameter, r). Three values for r are depicted. The weight of each block is the area represented by the **solid green**. The intervals between blocks (**empty green**) do not contribute to the score.

242 3 RESULTS AND DISCUSSION

Mapping genes in a gene family in one species to their orthologs in a related species is a
major usage case for synder. To demonstrate the use of synder, we identify orthologs of
the A. thaliana NF-YC family genes across several species in Brassicaceae (Figure 6).
The canonical NF-Y is a heterotrimeric, eukaryotic transcription factor that is
comprised of subunits NF-YA, NF-YB and NF-YC [31]. NF-Y has been associated with

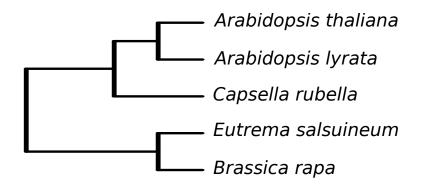


Figure 6: The species tree of the Brassicaceae used in this study. A. thaliana is the focal species.

spectrum disease resistance [36], and carbon and nitrogen partitioning [37]. In animals and 240 fungi, a single gene encodes each of the three NF-Y subunits. In contrast, the NF-Y 250 subunits in plants are each encoded by gene families of 10-15 genes [34, 38, 39]. The 251 combinatorial complexity of the potential plant NF-Y complexes that could be formed 252 from the three NF-Y subunits has obfuscated the role of each individual family member, 253 although progress is being made. For example, NF-YA1 of alfalfa controls successful 254 symbiosis between rhizobia and plant, and is required for the persistence of the nodule 255 meristem [40, 41]. 256

Compounding the complexity of the action of NF-Y subunits in the cannonical 257 heterotrimer, specific family members of at least two of the subunits, NF-YC and NF-YB, 258 can also form associations with a variety of other nuclear proteins [37, 42, 43]. One of three 259 NF-YC proteins can interact with one of two NF-YB proteins to enable 260 CONSTANS-promoted photoperiod-induced flowering [44, 45]. NF-YC4 of A. thaliana 261 interacts with the protein of the orphan gene QQS to modulate carbon and nitrogen 262 partitioning [37]. Several NF-YC family members interact with histone deacetylase 15 263 (HDA15) in the light to reduce histone acetylation, which in turn decreases hypocotyl 264 elongation [42]. 265



the relationships among orthology and function in evolution of this gene family. In practice, ortholog identification is often based only on sequence similarity scores. The highest scoring match, however, may not be the true ortholog. **synder** allows more reliable ortholog inference by finding the similarity matches that overlap the inferred syntenic regions. In this way, **synder** may serve as a syntenic filter downstream of the similarity search.

3.1 NF-YC orthologs: Arabidopsis thaliana compared to Arabidopsis lyrata

The specific case of determining the A. thaliana NF-YC orthologs in its sister species, 274 A. lyrata, illustrates the use of synder in resolving orthologs. Since NF-Y is a large family, 275 the paralogous NF-YC family members must be distinguished from the true orthologs. 276 The genomic relationship between the two species further challenges analysis. While the 277 species diverged only about 8.8 million years ago [46], A. lyrata has undergone a whole 278 genome duplication since splitting from the common ancestor it shares with A. thaliana. 279 This complicates orthology inference, since each A. thaliana gene is expected to have two 280 orthologs in A. lyrata. Only one of each duplicate A. lyrata ortholog may have preserved a 281 function. Its sister ortholog may have been deleted or become a pseudogene through 282 genome fractionation [28,47]. Alternatively, a sister ortholog may have undergone selection 283 for a completely new molecular function [48,49]. A third possibility is that the molecular 284 function of each sister ortholog was preserved through the neutral process of 285 subfunctionalization [48]. 286

In this analysis, we built a synteny map with Satsuma [20] using default parameters that yielded 229,562 syntenic blocks with a median length of 163 nt (1st quantile = 33 bases, 3rd quantile = 365 bases). This is a very dense map: the *A. thaliana* genome is about 120M in length, thus there are an average of around 1900 syntenic blocks per megabase. A synder search mapped 12 of the 13 query NF-YC family member genes to a search

interval in A. lyrata that also contained the top BLAST hit (see Hits worksheet in 292 supplementary) (Figure 7). Further, synder uniquely mapped 11 of the 13 query genes to 293 a single A. lyrata gene. NF-YC5 and NF-YC10 are mapped by synder to two genes in 294 A. lyrata, potentially reflecting that the genome duplication of A. lyrata was syntenically 295 conserved. In contrast, a BLAST search yielded a nearly fully connected graph between 296 NF-YC members in the two species. In the case of NF-YC8, synder identified orthologs 297 that were located in the same syntenic region of the two genomes; however, the whole 298 genome BLAST did not identify these likely orthologs, but rather other sequences were 299 among the top hits. synder and BLAST identified the same gene as having the highest 300 score. A second NF-YC12 ortholog was identified by synder that was not selected by 301 BLAST. 302

If each pair of orthologs in *A. lyrata* had undergone only minimal sequence divergence and if synteny was maintained in each case, a **synder** analysis might uniquely identify two *A. lyrata* orthologs for each of the 13 NF-YCs of *A. thaliana*. Indeed, **synder** identified two hits for three of the family member: NF-YC5, NF-YC10 and NF-YC12. The BLAST results cannot reveal whether the second top BLAST hit is an ortholog or not.

³⁰⁸ 3.2 NF-YC orthologs across the Brassicaceae family

This approach can be easily extended across the Brassicaceae family. We consider the 309 species in **Figure 6**. In each species, tBLASTn alone links each NF-YC gene to nearly all 310 of the other NF-YC genes; in contrast, synder identifies unique mappings to orthologs, 311 many of which differ from the highest BLAST hit. As syntenic distance increases, the 312 orthologs become more difficult to identify through syntenic methods (Figure 7). 313 However, for those genes located in syntenically-conserved regions, synder would more 314 reliably identify the ortholog. For example, in *B. rapa*, synder identifies an NF-YC 315 ortholog within the syntenic search space for NF-YC3, NF-YC5, NF-YC7, and NF-YC8 316

that does not correspond to the top BLAST hit (Figure 7). synder identified a syntenic ortholog of NF-YC6 that is only a weak BLAST hit. For NF-YC2, the ortholog identified by synder is not annotated at all in *B. rapa*. It may or may not be an expressed gene, but it is most likely an ortholog. Thus, synder can be used to augment whole-genome similarity inferences with syntenic context information.

322 4 CONCLUSION

synder provides a flexible, reproducible method to track specific genetic events. It also 323 provides a pathway to evaluate broad biological concepts, including the evolution and 324 diversification of gene families; the predominant mechanisms of diversification across 325 lineages of eukaryotes and prokaryotes; the effects of genome duplication; and the 326 relationship of different features to genomic instability. These types of analyses can 327 ultimately reveal those genetic events that might be associated with particular evolutionary 328 consequences, such as rapid evolution, horizontal transfer, de novo emergence of genes, 329 transposition, or duplication. 330

331 5 IMPLEMENTATION

synder is a C++ program wrapped in an R package via Rcpp [50]. It is designed to be
compatible with Bioconductor, an R-based bioinformatics ecosystem [51].

334 6 AVAILABILITY

As an R package, synder should work on any system. It is distributed under a GPL-3 open source license and the source code is available at https://github.com/arendsee/synder. All code required to run the case study is available at

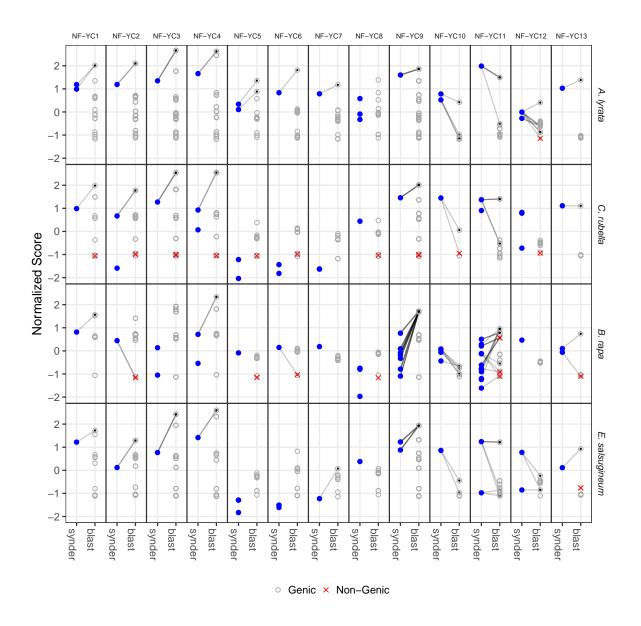


Figure 7: Comparison of orthologs inferred by synder and BLAST for the 13 *A. thaliana* NF-YC family members across genomes of four target species from Brassicaceae. Each row represents predicted orthologs in a target species. The x-axis for each box compares synder and tBLASTn scores. Blue dots, search intervals on the target genome that overlap a gene; gray circles, tBLASTn hits (E-value<0.001) on the target genome; red X's, tBLASTn hits on the target genome that do *not* overlap any annotated gene. The normalized Score (y-axis) is the score for synder search intervals and tBLASTn hits; synder scores were logged, and tBLASTn E-values were transformed with a negated, base10 log. Values were normalized by subtracting the means and dividing by the standard deviation. Gray lines, overlap between the tBLASTn hit interval and the synder search interval, i.e., tBLASTn finds a hit on the expected strand within the synder-inferred search interval.

- ³³⁸ https://github.com/arendsee/synder-case-study and the required input data is on
- 339 DataHub at https://datahub.io/arendsee/synder-nfyc.

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342 8 AUTHORS' CONTRIBUTIONS

³⁴³ ZA conceived of the project and ZA and AW implemented the software. MH reviewed the ³⁴⁴ software and offered helpful feedback. US and LJ tested the software and helped with the ³⁴⁵ case studies. ZA and ESW wrote the initial drafts and final version. All authors ³⁴⁶ participated in the writing of the manuscript, and read and approved the final manuscript.

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