# Nanodiamonds enable adaptive-optics enhanced, super-resolution, two-photon excitation microscopy

Graeme E. Johnstone<sup>1</sup>, Gemma S. Cairns<sup>1</sup>, and Brian R. Patton<sup>1, 🖂</sup>

<sup>1</sup>Department of Physics and SUPA, University of Strathclyde, Glasgow G4 0NG, Scotland, United Kingdom

Particles of diamond in the 5 to 100 nm size range, known as nanodiamond, have shown promise as robust fluorophores for optical imaging. We demonstrate here that, due to their photostability, they are not only suitable for two-photon imaging, but they allow significant resolution enhancement when combined with computational super-resolution techniques. We observe a resolution of 42.5 nm when processing two-photon images with the Super-Resolution Radial Fluctuations algorithm. We show manipulation of the point-spread function of the microscope using adaptive optics. This demonstrates how the photostability of nanodiamond can also be of use when characterising adaptive optics technologies or testing the resilience of super-resolution or aberration correction algorithms.

Nanodiamond | Super-resolution | Multi-photon Excitation | Adaptive Optics Correspondence: brian.patton@strath.ac.uk

#### Introduction

The biocompatibility of diamond(1), combined with the ability to make nanoscopic particles of <100 nm diameter, has led to research into the use of nanodiamond (ND) for a variety of biological applications(2), including drug delivery (3, 4) and use as a fluorescent marker for microscopy (5, 6). The surface chemistry of ND allows it to be functionalised by chemically attaching a range of different molecules to the ND surface (7, 8). Examples of functionalisation strategies include antibody (9, 10) and DNA (11) binding. The benefits arise by allowing efficient targetting of ND to subcellular features of interest, thereby allowing effective labelling for fluorescent microscopy (2).

The fluorescence of ND is due to defects in the diamond structure (12). A large number of defects are known to show fluorescent properties (8), but of particular interest is the nitrogen-vacancy (NV) defect, which occurs when two neighbouring carbon atoms are replaced by a nitrogen atom and a vacant space in the crystal lattice. This defect is most commonly found in a negatively charged state, referred to as NV-, and is efficiently imaged with a single photon excitation of 532 nm that results in emission over a wide wavelength band from 637 nm to approximately 800 nm. A particular advantage of NV- emission is that, unlike most conventional fluorophores used for microscopy, it is completely photostable, allowing imaging of individual cells labelled with ND over periods of a week or more(13). The brightness of an individual ND is a function of the number of defects it contains. This number can be increased during the production of nanodiamond, allowing for even brighter labelling, and is typically correlated with the size of the ND: particles smaller than 5 - 10 nm are unlikely to be able to support a fluorescently active NV(14, 15) without specific processing(16). By contrast, 100 nm particles may have hundreds of active NV centres. This flexbility allows a tradeoff between the intrinsic brightness of the ND (improving signal to noise for a given image acquisition rate) and the potential impact of the ND on the local biological processes (due either to physical blocking or surface chemistry effects). There have been many studies demonstrating the use of ND with standard microscopy techniques, including confocal microscopy (17) and superresolution imaging in the form of stimulated emission depletion microscopy (18, 19).

An additional driver for the interest in NV as a fluorophore relates to the quantum mechanical properties that can be accessed optically(20). By combining optical excitation and readout (as is performed when imaging in a microscope) with some pulsed microwave (≈2.88 GHz) electronic-spin manipulation, it is possible to use the NV- centre as a sensor that can detect a number of features of the local environment, such as the temperature (6, 21) and the presence of magnetic fields (22-25). Active sensing of environmental changes induced by biological processes at a sub-micron scale, with NV centres, would extend the usefulness of ND in a range of imaging applications. However, while the emission of NV- is in a wavelength range with low scattering and absorption by water, the single photon excitation wavelength of 532 nm poses problems related both to scattering and autofluorescence effects that will decrease the effective sensitivity of the ND to the signals of interest.

One alternative approach is to take advantage of two-photon excitation (TPE) microscopy, which has the ability to image at a greater depth than single photon microscopy(26) due to decreased scattering and absorption. There is also a better signal to noise ratio as the fluorescence is only generated at the excitation focus and not throughout the whole illumination cone, giving significant benefits in autofluorescent samples. It has recently been shown that NV centres in bulk diamond samples can fluoresce with TPE (27) and likewise for NV in fragments of diamond of sizes 10 -  $100 \,\mu m$  (28). Tuning the excitation wavelengths in a range from 1030 to 1310 nm allows preferential excitation of NV- or the neutral NV0 state. There have been initial reports of TPE fluoresence in nanodiamonds(29–31), showing that they are compatible

with this mode of imaging.

In this paper we further demonstrate TPE imaging of NV centres in ND and show how ND is particularly suited to computational super-resolution techniques, such as that enabled by the super-resolution radial fluctuations (SRRF) (32) While multi-photon microscopy is inherently approach. suited to imaging in optically aberrating samples, it nevertheless benefits from adaptive optical image correction (33–35). With this in mind, we also demonstrate adaptive optic control of the excitation focal volume and the resulting changes in the images obtained from single ND crystals. By combining adaptive-optics and computational super-resolution imaging, we also show that ND is a superb fluorophore with significant potential for applications in which efficient correction of aberrations deep within an aberrating medium (such as tissue) is essential.

# Experimental

Materials and sample preparation. The nanodiamonds used in these experiments were produced by Adamas Nanotechnologies. We prepared slides for imaging from a mix of two monodisperse suspensions (both 0.1% w/v) of 40 nm and 100 nm diameter ND. The 40 nm ND each contain approximately 10 NV while there are closer to 400 NV per 100 nm ND as per the manufacturers calibration information. To prepare a suspension suitable for deposition on a coverslip we first sonicated each source of NDs to break up larger aggregates before adding  $10 \,\mu l$  of each ND suspension to  $100 \,\mu l$  of distilled water. The resulting suspension was then deposited onto a microscope cover slip and allowed to dry to ensure some ND adhered to the coverslip before being mounted on to a microscope slide using a small amount of distilled water as a mountant medium and finally sealing the sample with nail polish.

**Microscope and imaging equipment.** The microscope that provided all of the imaging for this work is a custom-designed, confocal microscope. A 1.35NA oil immersion objective lens was used for imaging in an epi-flourescence geometry. We used two excitation lasers for the work presented in this paper:

- A <50 ps pulse-duration 532 nm Picoquant laser running at a repetition rate of 40 MHz. This laser was used for single photon excitation of NV- centres.
- A Coherent Fidelity 2 pulsed fibre laser with a wavelength centred on 1070 nm, a bandwidth of 70 nm and a pulse duration of 40 fs at the laser's output. A chirp compensator allows optimisation of the pulse duration at the sample by maximising the observed multiphoton signal.

The fluorescent light emitted from the sample was coupled via an optical fibre (acting as the confocal pin hole for the single photon excitation) to a single pixel detector, a Laser Components avalanche photodiode (Count-50). Images were created by raster scanning the beam across the sample using a Newport Fast Steering Mirror (FSM-300) and axial-imaging was performed by moving the objective which was mounted on a Physik Instrumente piezo positioner (P-725 PIFOC). We have chosen the detection path to have a wavelength sensitivity of 650-750 nm. This range corresponds with the peak of the emission from NV- centres. As will be discussed further in section 4, a Boston Micromachines Corporation deformable mirror (Multi-DM) with 140 actuators and  $3.5\mu m$ stroke is used for aberration correction of both the excitation and signal paths. Control of the microscope was performed by custom-written Labview software driving a National Instruments FPGA.

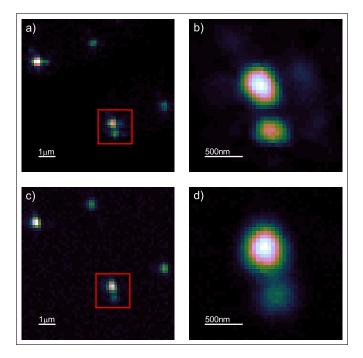
# **Two Photon Imaging**

We begin by demonstrating the effectiveness of two-photon imaging with our system. Figure 1 shows a comparison of one-photon and two-photon imaging on our mixed ND sample. We processed the data initially in Fiji(36, 37) and then generated the output figures for publication in OriginPro. We present the images using "CubeHelix"(38), a colourmap that increases linearly in perceived brightness, thereby making it suitable for colour-blind readers and reproduction in greyscale media. All unprocessed imaging data is available at the Strathelyde file sharing site along with descriptions of the file format generated by the custom software running our microscope and scripts for importing the data into Fiji.

Figure 1 shows the comparison between single-photon and multi-photon imaging of a single region of our sample. Sub-figures 1 a) and c) show that there is excellent correlation between the ND's that appear when imaging with 532 nm excitation and those present with 1070 nm excitation, respectively. To show the comparable resolution in both cases, Figs. 1 b) and d) show a higher resolution scan of the same pair of ND within the larger scan.

An advantage of multi-photon excitation is that it provides intrinsic sectioning when imaging, due to the excitation only occuring in the central volume of the excitation point-spread function (PSF). We include a video, (REF THIS), which shows multiple ND at different z-positions within the sample when imaged with the 1070 nm excitation.

While Fig. 1 demonstrates that we are seeing multi-photon excitation of the NV within our ND, we also wanted to confirm that it is a two-photon process. To confirm this, the beam was centred on a single ND and the detected photon counts were measured versus excitation power for both single- and multi-photon excitation modes. The results are shown in figure 2 for the 532 nm excitation and in figure 3 for the 1070 nm excitation. In the 532 nm excitation case, and at low input powers, the number of counts increases linearly with the power of the excitation laser. This is as expected for single photon fluorescence. For all fluorophores, as the excitation power increases further, the emitted fluorescence increases sub-linearly and starts to plateau - it saturates(39). Figure 2 shows exactly this behaviour in the single-photon excitation of ND, with saturation already apparent at  $100 \,\mu W$ incident power and an estimated peak count rate of approximately  $80,000 \,\mathrm{s}^{-1}$ . The inset of Fig. 2, plotting count rate bioRxiv preprint doi: https://doi.org/10.1101/586743; this version posted March 22, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder, who has granted bioRxiv a license to display the preprint in perpetuity. It is made available under a CC-BY 4.0 International license.



**Fig. 1.** a) Cluster of nanodiamonds imaged with single-photon excitation confocal microscopy using 532 nm laser excitation. b) A higher resolution 532 nm excitation scan of the region highlighted in a). c) The same region as a), imaged in two-photon mode with 1070 nm excitation. d) A higher resolution 1070 nm excitation scan of the region highlighted in c). The sample contains a mixture of 40 nm and 100 nm diameter nanodiamonds. The colour scale for all images is linear and normalised to the maximum and minumum pixel values of each individual image.

and power on logarithmic scales, shows a power law fit with power parameter n = 0.8 at low excitation power. That the value of n is less than one likely reflects the fact that we included points where saturation is already beginning to occur. It is worth noting here that it is often undesirable to image fluorophores in the saturation regime as it increases the probability of a photo-bleaching event due to inter-system crossings when the fluorophore is in the excited state. However, the photostability of NV centres means that it is possible to image them indefinitely even when well into the saturation regime. This is particularly relevant when seeking to use the emission properties of the NV as an environmental sensor. Knowing the relationship between excitation power and degree of saturation is useful as it allows us to maximise the photons being detected while decreasing the possibility of other phototoxicity effects from the excitation laser.

In the case of the 1070 nm excitation, Fig. 3, we see a super-linear dependence of the emission on the excitation power. For a pure two photon process the count rate should be quadratic with the excitation intensity. Performing a power law fit we recover a power parameter of  $n = 1.84 \pm 0.02$  indicating that we are seeing TPE as the mechanism for generating fluorescence at this excitation wavelength. There are two phenomena here that are worth commenting on. Firstly, we do not see saturation in the TPE power dependence. As discussed in the description of the microscope, we are limited to 12 mW power at the sample for the 1070 nm excitation laser, so this is likely a result of insufficient available laser power. The second point of note is that the TPE appears to show higher fluorescence counts than the single-photon ex-

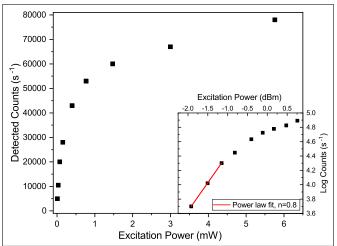
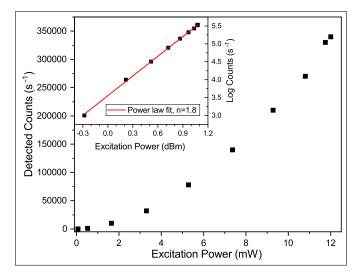


Fig. 2. Observed fluorescence count rate versus excitation power for single-photon excitation with 532 nm laser. Inset: Logarithmic power dependence showing sub-linear power law behaviour even at low excitation intensities. Scale is 1 dBm = 1 mW as measured at sample

citation at saturation. We do not currently have a full explanation for this. One contribution to the observed count rates comes from the fact that the 1070 nm laser was operated at a higher pulse repetition rate than the 532 nm laser (70 MHz vs 40 MHz). For short-duration laser pulses ( $\tau_{Pulse} < \tau_{NV-}$ ) this is equivalent to stating that each pulse results in one photon being emitted. Therefore, for repetition rates  $< 1/\tau_{NV-}$ , as is the case here, we would expect the count rate to be proportional to the laser repetition rate. Reference (28) also shows that, even with the 650 nm long pass filter in our system, there can still be significant NV0 emission leaking into the NV- channel. Furthermore, with 1070 nm excitation there is a significant cross-section for NV0 excitation. We did not have appropriate spectroscopic equipment to unambiguously determine the contribution of the NV0 to this excess count rate. However, we note that this would mainly be an issue for the use of the NV- spin properties in local field sensing. For general two-photon imaging, the apparent brightness of the ND with the excitation wavelength and power demonstrated here is beneficial. Should the application require efficient NV- only excitation, then reference (28) suggests longer wavelength excitation (>1150 nm) will improve the emission from NV-.

#### **Adaptive Optics**

Typical implementations of adaptive optics in two-photon microscopy(33) use active elements in the excitation path only and, due to the signal being generated only at the focal volume, employ wavefront sensors to directly detect the aberrations. As we are using a confocal detection scheme, the microscope used for these measurements has a deformable mirror (DM) installed in the common beam path and in such a way that it is imaged onto the back aperture of the objective. Deformations of the mirror can therefore be used to implement adaptive optical control of the PSF, with particular emphasis on correcting aberrations induced by the sample and which degrade image quality. Orthogonal control bioRxiv preprint doi: https://doi.org/10.1101/586743; this version posted March 22, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder, who has granted bioRxiv a license to display the preprint in perpetuity. It is made available under a CC-BY 4.0 International license.



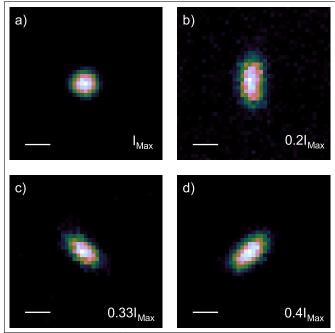
**Fig. 3.** Observed fluorescence count rate versus excitation power for multi-photon excitation with 1070 nm laser. Inset: Logarithmic power dependence showing approximately quadratic power law behaviour (exponent n = 1.8) indicating two-photon excitation. Scale is 1 dBm = 1 mW as measured at sample

modes for the DM are derived from the individual actuator influence functions as described in references (40, 41) and we use a sensorless correction procedure(34, 42) in which image-based metrics are used to measure the optimal shape of the DM. A driver for the development of efficient AO correction schemes has been the desire to minimise the photons lost to the correction process; if the sample undergoes significant photobleaching during the aberration estimation then it may call into question the use of AO in that particular sample. The lack of photobleaching of the NV centre therefore makes it an ideal candidate for implementing and testing aberration correction techniques.

In figure 4 we demonstrate control over the PSF of our twophoton confocal imaging system. All sub-figures are of the same ND, differing in the abberation applied to the DM and with a colour scale normalised to the maximum pixel value shown in the sub figure. Since aberrations are expected to decrease the peak intensity of the PSF, we also show this peak value as referenced to the peak intensity of the unaberrated PSF, Fig. 4 a). For this demonstration we have applied modes corresponding to the two primary astigmatism aberrations. Fig. 4b) shows vertical astigmatism, while Fig. 4c) and d) show positive and negative amounts of oblique astigmatism. The fidelity with the expected PSF shape is good, with little cross-talk between modes. The combination of two photon excitation microscopy, ND as a fluorophore and adaptive optics will allow deeper imaging in tissue than possible with either technique alone and we look forward to further exploring the possibilities in future work.

### Superresolution imaging of two photon excitation microscopy

The photostability of the NV defect makes it particularly suited to computational super-resolution techniques such as Super-Resolution Radial Fluctuations (SRRF) imaging. The algorithm and theory underlying the method is described in



**Fig. 4.** Experimental demonstration of deformable-mirror based control of the twophoton point-spread function (PSF). a) Optimally corrected PSF. Aberrated with: b) Vertical astigmatism c) Positive oblique astigmatism d) Negative oblique astigmatism. All scale bars are 500 nm, the colourscale is linear and ranges down from the given maximum pixel value (shown relative to the peak of a), the brightest image) to 10% of that value for each sub-figure.

Reference (32), and a plug-in module for ImageJ makes it a particularly user-friendly technique. SRRF makes use of the radial symmetry of the PSF to generate a radiality map that locates the fluorophore within the image. By then taking advantage of correlations in naturally occurring fluctuations in the radial symmetry measured over a large number images of the same object, the SRRF algorithm can extract superresolution images. In practice, a minimum of 100 standard resolution images are synthesised into a single SRRF image. It is worth noting that current versions of the SRRF algorithm do not offer any resolution enhancment along the optical axis.

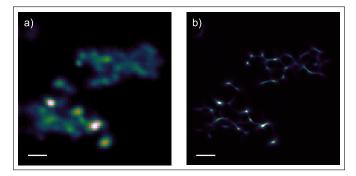


Fig. 5. Super-Resolution Radial Fluctuations (SRRF) imaging of two-photon excitation ND samples a) Drift-corrected sum of 100 acquisitions in TPE acquisition mode b) Super-resolution image derived from original image stack. Scale bar 1  $\mu$ m, linear colour scale applied to each image.

Figure 5 a) shows a pair of ND clusters imaged using two photon excitation microscopy. This image was generated by repeating 100 times and processed by correcting for in-plane sample drift, using the NanoJ-Core algorithm (43), followed

by summing the 100 frames. To generate the SRRF image shown in Fig. 5 b) we again applied the drift-correction routine before using the NanoJ-SRRF plugin with settings: Ring Radius = 0.5, Radiality Magnification = 6, Axes in Ring = 7 and Temporal Radiality Average. The resultant image shows significant increase in resolution, however there are some artefacts present; along with the lines joining individual NDs, inspection of the raw data shows sample drift along the Z axis and the presence of two distinct layers of ND separated in the Z-axis. Supplemental Movie 1 shows the results of a 3D stack of this cluster.

To better demonstrate the quality of SRRF imaging possible with ND, we performed further measurements on the upper cluster of nanodiamond imaged in Fig. 5. By keeping the pixel size approximately the same (70 nm versus 80 nm in Fig. 5) but decreasing the image boundaries, we hoped that the resulting shorter scan times would decrease the sample drift along the optical axis. Drift in this axis cannot be efficiently corrected on our hardware and has a significant deleterious effect on the SRRF processing algorithm. The results of these measurements are shown in Figure 6, with the 100 drift-corrected and summed standard resolution TPE frames shown in Fig. 6 a) and the SRRF processed image in Fig. 6 b). As is the case with the larger clusters in Fig. 5, the SRRF algorithm is able to recover significant extra resolution, and the higher quality initial imaging translates into higher SRRF resolutions. We will return to this point below. To show the enhancement in resolution, Fig. 6b) includes insets that enlarge two 250 nm square regions of interest. In the lower region we show that there is structure now visible within the brightest diffraction-limited spot within the TPE image of Fig. 6a). The lateral extent of this emitting region is of the order of 100 nm, however we do not have sufficient information to know unambiguously whether we are observing structured emission from a single 100 nm ND or emission from a small cluster of 40 nm ND. The upper region highlighted on Fig. 6 b) appears to be clearer in interpretation; there are two closely spaced emitters that the SRRF map shows as being distinguishable. To gain an initial estimation of the resolution of the SRRF image, we show a vertical slice through the left emitter of the pair along the green dashed line. Fitting this intensity profile to a Gaussian gives a 44 nm full-widthhalf-maximum (FWHM), consistent with this being a single 40 nm ND.

We have shown that sample drift can adversely affect the quality of a SRRF reconstruction. An advantage of our microscope, when combined with the lack of photobleaching of the ND, is that we can also explore the effects of optical aberrations on the SRRF process. Figure 7 shows a demonstration of how this can be put into practice. As a reference, the upper row of Fig. 7 (a) and b)) shows the unaberrated TPE and SRRF images. We then acquired further TPE image sets with identical imaging conditions apart from a known aberration being applied to the DM. For the middle row (Fig. 7 c) and d)) we applied 1 unit each of astigmatism and coma (Zernike Noll indices 6 and 7). To further quantify the effect of the aberration, we consider the effective RMS wavefront error,

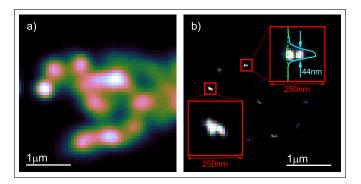


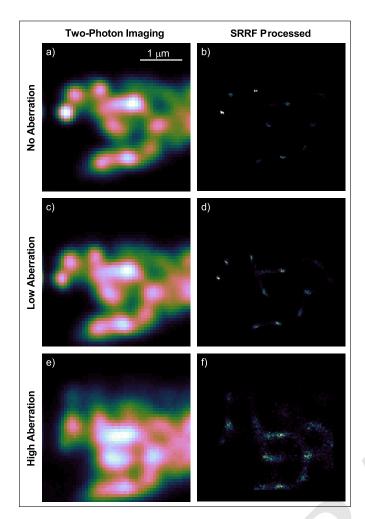
Fig. 6. Higher frame-rate imaging of upper cluster of ND from Fig. 5 a) Driftcorrected sum of 100 acquisitions in TPE acquisition mode b) Super-resolution image derived from original image stack. Insets are from two, 250 nm square regions as highlighted on main SRFF image. Upper inset also shows intensity plot along a vertical slice through one of the SRRF-resolved emitters. Indicated is the 44 nm full-width-half-maximum of a Gaussian fit to this intensity profile. 1  $\mu$ m scale bars refer to main images, linear colour scale applied to each image.

 $\sigma$ , being applied by the DM. In this case  $\sigma = 1.10$  rad. From this, we can also estimate the Strehl ratio as  $S = e^{-\sigma^2}$ , which corresponds to the ratio of the aberrated peak intensity to the unaberrated peak intensity. For  $\sigma = 1.10$  rad, this results in a Strehl ratio of 0.30. This is comparable to the Strehl ratio previously observed (44) when imaging at a depth of  $10 \,\mu m$ in cleared Drosophila melanogaster brain tissue. The resulting SRRF images show more noise, no clear structure in the features highlighted in Fig. 6b) and artefacts that appear to link previously distinct features. To demonstrate the effects of even higher aberrations,  $\sigma = 1.43, S = 0.12$ , we applied 3 units each of coma and astigmatism, with the results being shown in Fig. 7 e) and f). While SRRF still recovers some features with this level of aberration, the image is significantly degraded when compared to either of the other two aberration cases.

To better quantify the effective resolution of the SRRF images in all three cases shown in Fig. 7, we applied the Fourier Ring Correlation technique (FRC) (45). This works on a pair of images that differ only in noise: at low spatial frequencies which are dominated by the (identical) structure of the sample there is a high degree,  $FRC \approx 1$ , of correlation, which decreases with increasing spatial frequency until reaching a point at which the images are dominated entirely by uncorrelated noise. The spatial frequency at which this crossover occurs, often referred to as the FRC resolution, is a measure of the maximum spatial frequency (minimum feature size) that still contains information in the images. Figure 8 shows the FRC curves derived from each aberration case, with the FRC value plotted against inverse pixels as the unit of spatial frequency. To generate the FRC curve, we deinterleaved the odd and even frames from the original TPE image sequences and processed them in the SRRF algorithm. The resulting pair of SRRF images was then used for the FRC algorithm. Our chosen SRRF parameters resulted in a pixel size of 11.4 nm, which can be used to convert from spatial frequency to resolution.

Also shown on Fig. 8 is the threshold curve used to determine the FRC resolution. Common approaches to determine the FRC resolution use a fixed value of 1/7 as the thresh-

bioRxiv preprint doi: https://doi.org/10.1101/586743; this version posted March 22, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder, who has granted bioRxiv a license to display the preprint in perpetuity. It is made available under a CC-BY 4.0 International license.



**Fig. 7.** Demonstration of the effects of aberration on TPE and SRRF imaging. Left column: Drift-corrected sum of 100 TPE frames with no (top row), Low (middle row) and High (bottom row) amounts of applied aberration. Right column: Corresponding SRRF images. All images at same scale, with 1  $\mu$ m bar show in a) for reference. Linear colour scale applied to each image.

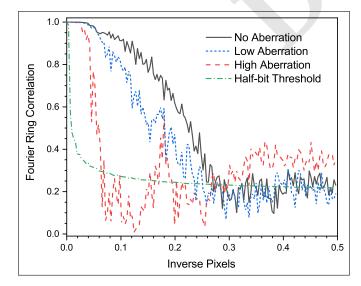


Fig. 8. Fourier-Ring Correlation curves for SRRF data in Fig. 7. Horizontal scaling is inverse pixels, with a single pixel real-space size of 11.4 nm. Also shown is a resolution threshold curve based on a half-bit of information per pixel. The FRC resolutions given in the text refer to when each curve first crosses the threshold.

old for the FRC resolution: the spatial frequency at which the FRC curve first falls under 1/7 is given as the resolution. A problem with this is that, for low spatial frequencies, the FRC curve is derived from Fourier-domain rings that contain fewer pixels than those for higher spatial frequencies. There is therefore a difference in the statistical behaviour in these two conditions (46, 47) for which a better threshold is the curve defining the FRC level at which each pixel contains half of one bit of information. We include this "Half-bit Threshold" on Fig. 8 and use it to determine the resolution for each of our images. The resulting resolutions are given in Table 1

Aberration	Strehl Ratio	FRC (Pixels <sup>-1</sup> )	FRC (nm)
None	> 0.9	0.269	42.5
Low	0.30	0.235	49
High	0.13	0.062	184

 Table 1. FRC derived resolution for SRRF images acquired under differing optical aberrations

That the FRC resolution agrees with the FWHM of the Gaussian fit in Fig. 6 b) is gratifying. What is perhaps more surprising is the robustness of the SRRF algorithm to aberrations - we see evidence of resolution enhancement even in the case of strongly aberrated images.

## Conclusion

Nanodiamond has been shown to have much promise as a fluorophore for use in biological imaging. With this study we have shown that it is not only an exceptional fluorophore in single photon imaging, but that it is also superb when used with two-photon excitation microscopes. Furthermore, we demonstate that its photostability gives it significant advantages when performing adaptive-optics or computational super-resolution images. Indeed, we saw evidence for a tenfold resolution increase when generating SRRF images from our two-photon data.

#### **Funding Information**

This work was funded under grants from the Royal Society (RGF\EA\181058 and URF\R\180017) and EPSRC (EP/M003701/1). BRP holds a Royal Society University Research Fellowship. We wish to acknowledge the loan of a Fidelity 2 laser from Coherent Inc., which was used to generate all two-photon excitation data in this paper.

#### Bibliography

- Ying Zhu, Jing Li, Wenxin Li, Yu Zhang, Xiafeng Yang, Nan Chen, Yanhong Sun, Yun Zhao, Chunhai Fan, and Qing Huang. The Biocompatibility of Nanodiamonds and Their Application in Drug Delivery Systems. *Theranostics*, 2(3):302–312, 2012. ISSN 1838-7640. doi: 10.7150/thno.3627.
- Mayeul Chipaux, Kiran J. van der Laan, Simon R. Hemelaar, Masoumeh Hasani, Tingting Zheng, and Romana Schirhagl. Nanodiamonds and Their Applications in Cells. *Small*, 14 (24):1704263, June 2018. ISSN 1613-6829. doi: 10.1002/smll.201704263.
- Basem Moosa, Karim Fhayli, Song Li, Khatchatur Julfakyan, Alaa Ezzeddine, and Niveen M. Khashab. Applications of nanodiamonds in drug delivery and catalysis. *Journal of Nanoscience and Nanotechnology*, 14(1):332–343, January 2014. ISSN 1533-4880.
- Dae Gon Lim, Racelly Ena Prim, Ki Hyun Kim, Eunah Kang, Kinam Park, and Seong Hoon Jeong. Combinatorial nanodiamond in pharmaceutical and biomedical applications. *International Journal of Pharmaceutics*, 514(1):41–51, November 2016. ISSN 1873-3476. doi: 10.1016/j.ijpharm.2016.06.004.

- Yuen Yung Hui, Wesley Wei-Wen Hsiao, Simon Haziza, Michel Simonneau, François Treussart, and Huan-Cheng Chang. Single particle tracking of fluorescent nanodiamonds in cells and organisms. *Current Opinion in Solid State and Materials Science*, 21(1):35–42, February 2017. ISSN 1359-0286. doi: 10.1016/j.cossms.2016.04.002.
- Wesley Wei-Wen Hsiao, Yuen Yung Hui, Pei-Chang Tsai, and Huan-Cheng Chang. Fluorescent Nanodiamond: A Versatile Tool for Long-Term Cell Tracking, Super-Resolution Imaging, and Nanoscale Temperature Sensing. *Accounts of Chemical Research*, 49(3): 400–407, March 2016. ISSN 0001-4842. doi: 10.1021/acs.accounts.5b00484.
- H. L. Shergold and C. J. Hartley. The surface chemistry of diamond. International Journal of Mineral Processing, 9(3):219–233, July 1982. ISSN 0301-7516. doi: 10.1016/0301-7516(82) 90029-1.
- Andreas Nagl, Simon Robert Hemelaar, and Romana Schirhagl. Improving surface and defect center chemistry of fluorescent nanodiamonds for imaging purposes—a review. Analytical and Bioanalytical Chemistry, 407(25):7521–7536, October 2015. ISSN 1618-2650. doi: 10.1007/s00216-015-8849-1.
- V. Vermeeren, L. Grieten, N. Vanden Bon, N. Bijnens, S. Wenmackers, S. D. Janssens, K. Haenen, P. Wagner, and L. Michiels. Impedimetric, diamond-based immmunosensor for the detection of C-reactive protein. *Sensors and Actuators B: Chemical*, 157(1):130–138, September 2011. ISSN 0925-4005. doi: 10.1016/j.snb.2011.03.037.
- Shabnam Siddiqui, Zhenting Dai, Courtney J. Stavis, Hongjun Zeng, Nicolaie Moldovan, Robert J. Hamers, John A. Carlisle, and Prabhu U. Arumugam. A quantitative study of detection mechanism of a label-free impedance biosensor using ultrananocrystalline diamond microelectrode array. *Biosensors and Bioelectronics*, 35(1):284–290, May 2012. ISSN 0956-5663. doi: 10.1016/j.bios.2012.03.001.
- Wensha Yang, James E. Butler, John N. Russell, and Robert J. Hamers. Interfacial Electrical Properties of DNA-Modified Diamond Thin Films: Intrinsic Response and Hybridization-Induced Field Effects. *Langmuir*, 20(16):6778–6787, August 2004. ISSN 0743-7463. doi: 10.1021/la036460y.
- A. T. Collins, G. Davies, H. Kanda, and G. S. Woods. Spectroscopic studies of carbon-13 synthetic diamond. *Journal of Physics C: Solid State Physics*, 21(8):1363, 1988. ISSN 0022-3719. doi: 10.1088/0022-3719/21/8/012.
- Tsai-Jung Wu, Yan-Kai Tzeng, Wei-Wei Chang, Chi-An Cheng, Yung Kuo, Chin-Hsiang Chien, Huan-Cheng Chang, and John Yu. Tracking the engraftment and regenerative capabilities of transplanted lung stem cells using fluorescent nanodiamonds. *Nature Nanotechnology*, 8:682, August 2013. doi: 10.1038/nnano.2013.147.
- Carlo Bradac, Torsten Gaebel, Chris I. Pakes, Jana M. Say, Andrei V. Zvyagin, and James R. Rabeau. Effect of the Nanodiamond Host on a Nitrogen-Vacancy Color-Centre Emission State. *Small*, 9(1):132–139, 2013. ISSN 1613-6829. doi: 10.1002/smll.201200574.
- Yuen Yung Hui, Chia-Liang Cheng, and Huan-Cheng Chang. Nanodiamonds for optical bioimaging. *Journal of Physics D: Applied Physics*, 43(37):374021, September 2010. ISSN 0022-3727. doi: 10.1088/0022-3727/43/37/374021.
- Shingo Sotoma, Daiki Terada, Takuya F. Segawa, Ryuji Igarashi, Yoshie Harada, and Masahiro Shirakawa. Enrichment of ODMR-active nitrogen-vacancy centres in fivenanometre-sized detonation-synthesized nanodiamonds: Nanoprobes for temperature, angle and position. *Scientific Reports*, 8(1):5463, April 2018. ISSN 2045-2322. doi: 10.1038/s41598-018-23635-5.
- S. R. Hemelaar, P. de Boer, M. Chipaux, W. Zuidema, T. Hamoh, F. Perona Martinez, A. Nagl, J. P. Hoogenboom, B. N. G. Giepmans, and R. Schirhagl. Nanodiamonds as multipurpose labels for microscopy. *Scientific Reports*, 7(1):720, April 2017. ISSN 2045-2322. doi: 10.1038/s41598-017-00797-2.
- Silvia Arroyo-Camejo, Marie-Pierre Adam, Mondher Besbes, Jean-Paul Hugonin, Vincent Jacques, Jean-Jacques Greffet, Jean-François Roch, Stefan W. Hell, and François Treussart. Stimulated emission depletion microscopy resolves individual nitrogen vacancy centers in diamond nanocrystals. ACS nano, 7(12):10912–10919, December 2013. ISSN 1936-086X. doi: 10.1021/nn404421b.
- Gregoire Laporte and Demetri Psaltis. STED imaging of green fluorescent nanodiamonds containing nitrogen-vacancy-nitrogen centers. *Biomedical Optics Express*, 7(1):34–44, December 2015. ISSN 2156-7085. doi: 10.1364/BOE.7.000034.
- Paul Delaney, James C. Greer, and J. Andreas Larsson. Spin-Polarization Mechanisms of the Nitrogen-Vacancy Center in Diamond. *Nano Letters*, 10(2):610–614, February 2010. ISSN 1530-6984. doi: 10.1021/nl903646p.
- V. M. Acosta, E. Bauch, M. P. Ledbetter, A. Waxman, L.-S. Bouchard, and D. Budker. Temperature Dependence of the Nitrogen-Vacancy Magnetic Resonance in Diamond. *Physical Review Letters*, 104(7):070801, February 2010. doi: 10.1103/PhysRevLett.104.070801.
- Sungkun Hong, Michael S. Grinolds, Linh M. Pham, David Le Sage, Lan Luan, Ronald L. Walsworth, and Amir Yacoby. Nanoscale magnetometry with NV centers in diamond. *MRS Bulletin*, 38(2):155–161, February 2013. ISSN 0883-7694, 1938-1425. doi: 10.1557/mrs. 2013.23.
- Yuzhou Wu, Fedor Jelezko, Martin B Plenio, and Tanja Weil. Diamond Quantum Devices in Biology. Angewandte Chemie International Edition, 55(23):6586–6598, June 2016. ISSN 1433-7851. doi: 10.1002/anie.201506556.
- A. Gruber, A. Dräbenstedt, C. Tietz, L. Fleury, J. Wrachtrup, and C. von Borczyskowski. Scanning Confocal Optical Microscopy and Magnetic Resonance on Single Defect Centers. *Science*, 276(5321):2012–2014, June 1997. ISSN 0036-8075, 1095-9203. doi: 10.1126/ science.276.5321.2012.
- Romana Schirhagl, Kevin Chang, Michael Loretz, and Christian L. Degen. Nitrogenvacancy centers in diamond: nanoscale sensors for physics and biology. *Annual Review of Physical Chemistry*, 65:83–105, 2014. ISSN 1545-1593. doi: 10.1146/ annurev-physchem-040513-103659.
- Fritjof Helmchen and Winfried Denk. Deep tissue two-photon microscopy. Nature Methods, 2(12):932–940, December 2005. ISSN 1548-7105. doi: 10.1038/nmeth818.
- Tse-Luen Wee, Yan-Kai Tzeng, Chau-Chung Han, Huan-Cheng Chang, Wunshain Fann, Jui-Hung Hsu, Kuan-Ming Chen, and Yueh-Chung Yu. Two-photon Excited Fluorescence of Nitrogen-Vacancy Centers in Proton-Irradiated Type Ib Diamond. *The Journal* of *Physical Chemistry A*, 111(38):9379–9386, September 2007. ISSN 1089-5639. doi: 10.1021/jp073938o.

- Peng Ji, R. Balili, J. Beaumariage, S. Mukherjee, D. Snoke, and M. V. Gurudev Dutt. Multiple-photon excitation of nitrogen vacancy centers in diamond. *Physical Review B*, 97 (13):134112, April 2018. doi: 10.1103/PhysRevB.97.134112.
- Chiara Mauriello Jimenez, Nikola Z. Knezevic, Yolanda Galàn Rubio, Sabine Szunerits, Rabah Boukherroub, Florina Teodorescu, Jonas G. Croissant, Ouahiba Hocine, Martina Seric, Laurence Raehm, Vanja Stojanovic, Dina Aggad, Marie Maynadier, Marcel Garcia, Magali Gary-Bobo, and Jean-Olivier Durand. Nanodiamond–PMO for two-photon PDT and drug delivery. *Journal of Materials Chemistry B*, 4(35):5803–5808, August 2016. ISSN 2050-7518. doi: 10.1039/C6TB01915C.
- Yuen Yung Hui, Bailin Zhang, Yuan-Chang Chang, Cheng-Chun Chang, Huan-Cheng Chang, Jui-Hung Hsu, Karen Chang, and Fu-Hsiung Chang. Two-photon fluorescence correlation spectroscopy of lipid-encapsulated fluorescent nanodiamonds in living cells. *Optics Express*, 18(6):5896–5905, March 2010. ISSN 1094-4087. doi: 10.1364/OE.18.005896.
- Yi-Ren Chang, Hsu-Yang Lee, Kowa Chen, Chun-Chieh Chang, Dung-Sheng Tsai, Chi-Cheng Fu, Tsong-Shin Lim, Yan-Kai Tzeng, Chia-Yi Fang, Chau-Chung Han, Huan-Cheng Chang, and Wunshain Fann. Mass production and dynamic imaging of fluorescent nanodiamonds. *Nature Nanotechnology*, 3(5):284–288, May 2008. ISSN 1748-3395. doi: 10.1038/nnano.2008.99.
- Siân Culley, Kalina L. Tosheva, Pedro Matos Pereira, and Ricardo Henriques. SRRF: Universal live-cell super-resolution microscopy. *The International Journal of Biochemistry & Cell Biology*, 101:74–79, August 2018. ISSN 1878-5875. doi: 10.1016/j.biocel.2018.05.014.
- Xiaodong Tao, Andrew Norton, Matthew Kissel, Oscar Azucena, and Joel Kubby. Adaptive optical two-photon microscopy using autofluorescent guide stars. *Optics Letters*, 38(23): 5075–5078, December 2013. ISSN 1539-4794. doi: 10.1364/OL.38.005075.
- Delphine Débarre, Edward J. Botcherby, Tomoko Watanabe, Shankar Srinivas, Martin J. Booth, and Tony Wilson. Image-based adaptive optics for two-photon microscopy. *Optics Letters*, 34(16):2495–2497, August 2009. ISSN 1539-4794. doi: 10.1364/OL.34.002495.
- M. a. A. Neil, R. Juškaitis, M. J. Booth, T. Wilson, T. Tanaka, and S. Kawata. Adaptive aberration correction in a two-photon microscope. *Journal of Microscopy*, 200(2):105–108, 2000. ISSN 1365-2818. doi: 10.1046/j.1365-2818.2000.00770.x.
- 36. Johannes Schindelin, Ignacio Arganda-Carreras, Erwin Frise, Verena Kaynig, Mark Longair, Tobias Pietzsch, Stephan Preibisch, Curtis Rueden, Stephan Saalfeld, Benjamin Schmid, Jean-Yves Tinevez, Daniel James White, Volker Hartenstein, Kevin Eliceiri, Pavel Tomancak, and Albert Cardona. Fiji: an open-source platform for biological-image analysis. *Nature Methods*, 9(7):676–682, June 2012. ISSN 1548-7105. doi: 10.1038/nmeth.2019.
- Curtis T. Rueden, Johannes Schindelin, Mark C. Hiner, Barry E. DeZonia, Alison E. Walter, Ellen T. Arena, and Kevin W. Eliceiri. ImageJ2: ImageJ for the next generation of scientific image data. *BMC Bioinformatics*, 18(1):529, November 2017. ISSN 1471-2105. doi: 10. 1186/s12859-017-1934-z.
- 38. D A Green. A colour scheme for the display of astronomical intensity images. page 7.
- K. Visscher, G. J. Brakenhoff, and T. D. Visser. Fluorescence saturation in confocal microscopy. *Journal of Microscopy*, 175(2):162–165, 1994. ISSN 1365-2818. doi: 10.1111/j.1365-2818.1994.tb03479.x.
- Martin Booth, Tony Wilson, Hong-Bo Sun, Taisuke Ota, and Satoshi Kawata. Methods for the characterization of deformable membrane mirrors. *Applied Optics*, 44(24):5131–5139, August 2005. ISSN 2155-3165. doi: 10.1364/AO.44.005131.
- A. Thayil and M. J. Booth. Self calibration of sensorless adaptive optical microscopes. Journal of the European Optical Society - Rapid publications, 6(0), September 2011. ISSN 1990-2573. doi: 10.2971/jeos.2011.11045.
- Martin J. Booth, Mark A. A. Neil, Rimas Juškaitis, and Tony Wilson. Adaptive aberration correction in a confocal microscope. *Proceedings of the National Academy of Sciences*, 99 (9):5788–5792, April 2002. ISSN 0027-8424, 1091-6490. doi: 10.1073/pnas.082544799.
- 43. Romain Laine, Kalina Tosheva, Nils Gustafsson, Robert D. M. Gray, Pedro Almada, David Albrecht, Gabriel T. Risa, Fredrik Hurtig, Ann-Christin Lindås, Buzz Baum, Jason Mercer, Christophe Leterrier, Pedro M. Pereira, Siân Culley, and Ricardo Henriques. Nanoj: a highperformance open-source super-resolution microscopy toolbox. *bioRxiv*, 2018. doi: 10. 1101/432674.
- Brian R. Patton, Daniel Burke, David Owald, Travis J. Gould, Joerg Bewersdorf, and Martin J. Booth. Three-dimensional STED microscopy of aberrating tissue using dual adaptive optics. *Optics Express*, 24(8):8862–8876, April 2016. ISSN 1094-4087. doi: 10.1364/OE.24.008862.
- Robert P. J. Nieuwenhuizen, Keith A. Lidke, Mark Bates, Daniela Leyton Puig, David Grünwald, Sjoerd Stallinga, and Bernd Rieger. Measuring image resolution in optical nanoscopy. *Nature Methods*, 10(6):557–562, June 2013. ISSN 1548-7105. doi: 10.1038/nmeth.2448.
- Marin van Heel and Michael Schatz. Fourier shell correlation threshold criteria. *Journal of Structural Biology*, 151(3):250–262, September 2005. ISSN 1047-8477. doi: 10.1016/j.jsb. 2005.05.009.
- Marin van Heel and Michael Schatz. REASSESSING THE REVOLUTIONS RESOLU-TIONS. *bioRxiv*, page 224402, November 2017. doi: 10.1101/224402.