Contingent Convergence: The ability to detect convergent genomic evolution is dependent on demographic similarity

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ABSTRACT

Outlier scans, in which the genome is scanned for signatures of selection, have become a prominent tool in studies of local adaptation, and more recently studies of genetic convergence in natural populations. However, these methods have the potential to be confounded by features of demographic history, which are considerably variable across natural populations. In this study, we use forward-simulations to investigate and illustrate how several measures of genetic differentiation commonly used in outlier scans (F_{ST}, D_{XY} and $\Delta\pi$) are influenced by demographic variation across multiple sampling time points. In a factorial design with 32 treatments, we manipulate the strength of bottlenecks (N of founding individuals), contractions (proportional size of derived population) and migration rate between an ancestral population and a derived population. Our results illustrate known constraints of individual measures associated with strong contractions and a lack of gene-flow, but notably we demonstrate how relationships between measures are similarly dependent on demography. We find that false-positive signals of convergent evolution (the same simulated genes marked as outliers in independent treatments) are attainable as a product of similar demographic treatment, and that outliers across different measures (particularly F_{ST} and D_{XY}) can occur with little influence of selection. Taken together, we show how underappreciated, yet quantifiable measures of demographic history can influence commonly employed methods for detecting selection.

KEYWORDS

Outlier scans, demographic history, F_{ST}, D_{XY}, false-positives, convergence

INTRODUCTION

Big-data studies of adaptation and evolution across the genome are increasing in popularity with the

availability of modern sequencing technologies. These studies often centre around quantifying

patterns of variation in genome-wide SNPs, which can be used to highlight regions or genes having

experienced selection relative to the neutral backdrop of the rest of the genome. These analyses,

which we refer to here as outlier scans, have become a common tool in population genetics and

have seen great success across diverse, natural systems in identifying candidate genes associated

with the evolution of a range of adaptive traits (reviewed recently by (Ahrens et al. 2018)). More

recently, the method of overlapping outlier scans across independent lineages has been employed

to test whether the same regions are involved in independent adaptation events (i.e. genetic

convergent evolution). This study seeks to investigate how different outlier scan methods are

influenced by demographic variation in natural populations, and how this may lead to overlapping

false-positives.

Recent discussions have highlighted the propensity of outlier scans to yield false-positives, given that

outliers caused by heterogeneous genomic landscapes are commonplace irrespective of selection

(Ellegren and Wolf 2017). Specifically, background selection (BGS), whereby linkage between neutral

and deleterious variants reduces local diversity (B. Charlesworth, Morgan, and Charlesworth 1993;

Bank et al. 2014; Burri 2017), has been invoked to offer alternative explanations for patterns at first

attributed to directional selection (Cruickshank and Hahn 2014). Furthermore, the influence of

neutral processes such as genetic drift can similarly produce false-positive signatures of selection

(Kimura 1983).

The strength of these processes are dependent on demography. For example, the influence of

neutral processes and BGS should be more pronounced in smaller populations (low N_e) (D.

Charlesworth, Charlesworth, and Morgan 1995; Cutter and Payseur 2013; B. Charlesworth 2009;

Yeaman and Otto 2011); as has been demonstrated in humans (Torres, Szpiech, and Hernandez

2018) and *Drosophila* (Sella et al. 2009; B. Charlesworth 1996). This relationship, however, may not

be simply linear, with additional simulation evidence suggesting the effects of BGS are strongest at

intermediate-low N_e, with effects becoming weaker again at very low N_e (Zeng 2013).

Lack of connectivity among populations may also elevate measures of genetic differentiation, if a

large global population is composed of smaller, isolated, sub-divided populations that each

experience the effects of reduced N_e (B. Charlesworth, Nordborg, and Charlesworth 1997; Hoban et

al. 2016). In an attempt to mitigate the likelihood of false-positives, some have advocated using

multiple measures of population differentiation and divergence to identify regions of the genome

likely to be under selection (B. Charlesworth 1998; Cruickshank and Hahn 2014). However, how

these measures are correlated with each other and with selection under different demographic

scenarios has not been explored.

A diverse array of measures of genetic differentiation and divergence have been employed for

outlier scans, but here we focus on two of the most common measures of relative differentiation (F_{ST}

and π) and a third measure of absolute divergence (D_{XY}). The most commonly used measure in

outlier scans is the fixation-index F_{ST} (Weir and Cockerham 1984; Hudson, Slatkin, and Maddison

1992), which measures the relative importance of within- and between-population variance. This

measure is thus maximised when genomic regions exhibit the lowest within- and highest between-

population variance. F_{ST} outliers at the right-tail of the distribution are considered candidates for

adaptation because they reflect regions with large differences in allele frequencies or high

substitution rate (large between-population variance) and/or low nucleotide variation (low within-

population variance) relative to the rest of the genome. Changes in nucleotide diversity (π) are

another indicator of adaptation, as selection on a beneficial allele limits variation within a population

resulting in selective sweeps (Smith and Haigh 1974). Comparisons of the ratio of π between

diverging populations reveal regions under selection as local π is reduced in one population in

comparison to the other. Whilst similar to F_{ST}, changes in π ($\Delta\pi$) do not discriminate between which

copy of a polymorphism is fixed, such that a substitution between populations is equivalent to a

common non-polymorphic site. $\Delta\pi$ outliers therefore represent regions of the genome with reduced

π in either population relative to the rest of the genome. As a measure of absolute genetic

divergence, D_{XY} (Nei 1987) does not consider the relative frequencies of polymorphisms within

populations (B. Charlesworth 1998; Cruickshank and Hahn 2014). D_{XY} can be quantified as the

average number of pairwise differences between sequence comparisons between two populations.

This measure is therefore influenced by ancestral π and the substitution rate, so outliers highlight

regions that are highly variable ancestrally, or in either population (large π), or exhibit many

substitutions and thus increased sequence divergence.

Because each measure of differentiation quantifies genetic variation between populations in a

slightly different way (Cruickshank and Hahn 2014; Matthey-Doret and Whitlock 2018; Whitlock and

Lotterhos 2015), each has a unique relationship with demography. Whilst we can predict how

individual measures are influenced by demography, and subsequently neutral processes, we know

little about how the relationships between measures are affected. Therefore their combined power

to detect selection should also vary with demography, suggesting that combining measures may

provide unwarranted confidence in results.

This complex interplay between selection measures and demography may be further exacerbated

where studies compare scans from multiple populations to identify convergent genomic evolution.

Here, researchers use measures of population divergence across independent pairs of evolutionary

replicates with 'outlier' loci compared across results. This strategy has been employed extensively

across diverse taxa, including: birds (Cooper and Uy 2017), fish (Hohenlohe et al. 2010; Jones, Chan,

et al. 2012; Rougemont et al. 2017; Fraser et al. 2015; Reid et al. 2016; Meier et al. 2018), insects

(Soria-Carrasco et al. 2014; Van Belleghem et al. 2018), mammals (Waterhouse et al. 2018), molluscs

(Ravinet et al. 2016; Westram et al. 2014) and plants (Trucchi et al. 2017; Roda et al. 2013).

However, different demographic histories within independent scans, and the subsequent effects on

measures of population divergence, have rarely been considered in how they affect our ability to

detect convergent genetic evolution.

Here, we used forward-simulations to investigate the effects of different demographic histories on

the relationships between measures of divergence with selection. We focus on examining SNP

variation between ancestral and derived populations, although other methods are employed in the

literature (e.g. replicated clines, phylogenomics, single population measures e.g. Tajima's D). We

varied demography through manipulating the number of founding individuals (bottlenecks), the

population size of the derived population (contractions) and the presence/absence of migration. We

simulated the effects of selection on realistic genes designed from features taken from the guppy

genome assembly, a prominent model system for studies of convergent evolution (Fraser et al.

2015; Reznick and Endler 1982). Moreover, we measured genetic divergence at four set time points

through F_{ST}, D_{XY} and $\Delta\pi$ between an ancestral population and derived population to examine

temporal relationships. Our aim was to investigate the significance of demographic history when

employing outlier scans and highlight demographic scenarios that are susceptible to false-positives.

We also aimed to test when common outliers across measures occur, and whether overlapping

outliers are consistently good indicators of selection. We sought to answer the following questions:

1) How do demographic factors influence measures of divergence through time? 2) How well do

measures of divergence identify regions of the genome under strong selection through time and

across demographic factors? 3) How are the different measures of divergence related through time

and across demographic factors? 4) Where do we detect the strongest signals of convergence (i.e.

overlapping outliers using single or multiple measures), and are these consistent with selection?

METHODS

The forward-simulation software SLiM 3.0 (Haller and Messer 2019) was used to simulate population

divergence under contrasting demographic treatments in a fully factorial design across an ancestral

population of N = 1000 with a mutation rate based on the guppy genome (Künstner et al. 2016) and

scaled 100-fold over three raw mutation rates ($4.89e^{-5}$, $4.89e^{-6}$, $4.89e^{-7}$) to ensure robustness of

results across different, realistic values of θ ($4N_e\mu$). SLiM employs a classic Wright-Fisher model to

simulate populations, in which a population of diploid hermaphrodites proceeds through

generations such that an individual's contribution towards the next generation is proportional to its

relative fitness.

Demographic treatments included varying degrees of population contraction relative to the

ancestral population size (N = 1000) (0.01, 0.1, 0.5, 1.0), migration as a proportion of individuals

exchanged between populations (0.0, 0.002) and founding bottlenecks as a number of individuals (2,

20, 100, 1000). For example, a demographic history with bottleneck = 2, contraction = 0.01, and

migration = 0.002 would represent the following scenario: 1) 2 individuals are sampled from the

ancestral population of 1000 to form the derived population; 2) At the next generation (and for the

remainder of the simulation), the derived population's size reflects the contraction treatment, in this

case 10 (0.01 of 1000); 3) The ancestral and derived population experience migration in both

directions. Thus, each of our treatments can be thought of as a manipulation of the following:

'Bottlenecks' limit the amount of variation within the ancestral population that is transferred to the

derived population; 'Contractions' limit the size of the derived population; and 'Migration' dictates

the presence of gene flow between the ancestral and derived (Figure 1). Combining these treatment

levels in a fully factorial experimental design generated a total of 32 different independent

demographic histories that all genes experienced.

SLiM runs were performed over simulated genes of varying length (in order to ensure robustness

across different genomic elements); with exon number (max = 10), exon lengths, and intron lengths

drawn at random from the guppy genome gene annotation file (gff). Genes were also given 1kb

flanking regions and a divergence selection coefficient (S_σ) drawn at random.

Selection in our model was represented as the fitness consequences incurred through distance from

a phenotypic optimum in a one-dimensional landscape. These phenotypic were maintained across

the course of simulations; thus, selection was constant throughout. This setup can be considered as

analogous to representing two environments with contrasting optimum trait values for a single trait.

Intensity of selection was manipulated by modifying the standard deviation (σ) of the normal

distribution curve from which the density distribution was calculated through the "dnorm" function

in SLiM. Standard deviations for fitness distributions (S_σ) were 0.1, 0.5, 1.0, 5.0, and 10.0, with 0.1

representing the steepest fitness peak and 10.0 the shallowest. All subsequent analyses' standard

deviations were 1/x-transformed so that $S_{1/\sigma}$ = 10 represented the strongest selection treatment

(Figure 1A). Phenotypes were calculated per individual as the additive phenotypic effects of exonic

non-synonymous mutations, which appeared at a rate of 7/3 relative to synonymous mutations

(assuming that most mutations in the third base of a codon do not alter the amino acid). Effect sizes

for mutations with phenotypic effects were drawn from a Gaussian distribution with mean = 0 and σ

= 1. The remaining synonymous exon mutations, and those in introns and flanks, had no effect on

fitness. Recombination rate was set at a constant of $1e^{-8}$ across all genomic elements.

Figure 1: Experimental design for simulations. **A)** Selection treatments assigned to genes, illustrated
as the relationship between relative fitness of an individual and its phenotype. Each facet represents
a different fitness landscape modified through editing the standard deviation of the normal
distribution of fitness consequences in the derived (blue, dashed) population. Facet labels constitute
1/standard deviation applied. The x-axes represent phenotype as calculated through non-
synonymous mutations and the y-axes represent relative fitness of individuals. The phenotype of the
ancestral population (red, solid) is the same in all treatments (mean = 0, sd = 1), whilst derived
populations have a diverged phenotypic optimum (mean = 10, sd = S_σ). **B)** Demographic
representation of treatment factors. **C)** Representation of simulation timeline for treatments,
illustrating that all treatments share an ancestral burn-in population before splitting into 32
replicated "ancestral" (solid) and "derived" (dotted) population pairs. Red, dashed lines denote
sampling generations at which F_{ST}, D_{XY} and $\Delta\pi$ are calculated and averaged across the preceding 50
generations. The purpose of this averaging was to achieve a general sense of population
differentiation at four discrete sampling points, such that values represent stable patterns rather
than more stochastic generation to generation variation.

For each simulation, populations were seeded with 1000 individuals and allowed to proceed for a

burn-in period of 5*2N (10,000) generations to develop stable levels of natural variation under

stabilising selection. During this period, burn-in populations evolved towards a phenotypic optimum

of 0, defined as a normal distribution with mean = 0 and σ = 1.0 (Figure 1A). Burn-in populations

were then subjected to each demographic treatment to simulate the founding of multiple

populations from a shared ancestral state. During this 'divergence period', the ancestral population

continued to evolve around a phenotypic optimum of 0, whilst the derived population's phenotypic

optimum was centred around 10, with fitness consequences defined according to the selection

treatment. Individuals also experienced fitness costs associated with phenotypic proximity to other

individuals within the population as a proxy for competition and to ensure a realistic amount of

phenotypic variation persisted within populations. Fitness costs due to competitive proximity were

drawn from a Gaussian distribution with mean = 1, σ = 0.4 and occurred reciprocally between local

individuals with phenotypes with a difference of ≥ 1.2 (3 * 0.4).

Each gene was then run across all demographic treatment levels in parallel. Simulations were

sampled at 0.05*2N (100), 0.158*2N (316), 1.581*2N (3162) and 5*2N (10,000) generations (Figure

1C). At each sampling point, F_{ST} (calculated according to Hudson, Slatkin and Maddison (1992)), D_{XY}

(calculated according to Nei (1987)), and mean heterozygosity (π) of each population were

calculated as the average across the preceding 50 generations. Averaging was performed such that

measures would not be dramatically biased by events occurring within individual generations. The

change in mean heterozygosity between the ancestral and derived population ($\Delta\pi$) was calculated at

each sampling point as the $\log_{10}$-transformed ratio of ancestral π to derived π, such that reduced

diversity in the derived population increases the value of $\Delta\pi$. Statistics were calculated over all sites

of the gene.

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$$F_{ST} = 1 - \frac{H_S}{H_T}$$

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$$D_{XY} = \sum_{ij} x_i y_j d_{ij}$$

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$$\Delta\pi = \log_{10} \frac{\pi_{ancestral}}{\pi_{diverged}}$$

In total, ~1,000 genes were simulated across 32 demographic treatments across three mutation

rates. In addition, a fourth set of simulations was performed in which the phenotypic optimum for

both populations was kept at 0 (Pheno$_{Null}$). This dataset was used to assess whether patterns

associated with selection were driven by phenotypic divergence or variable stabilising selection

within populations. Sets of genes were generated randomly for each mutation rate. Outliers for gene

sets were taken as upper quantiles (either the upper 1% or 5% depending on analysis).

All data analysis was performed in R (3.5) (R Core Team 2016). To assess relationships between

divergence measures and selection, we subsetted our data within each treatment level for each

demographic factor (e.g. subsetting contraction groups of 0.01, 0.1, 0.5 and 1.0) and calculated

Pearson's correlation coefficients across each subset. For example, for each population contraction

level, 8 treatment groups were subsetted together and averaged over. To compare the proportions

of outliers of different selection treatments from random expectations we applied chi-squared tests.

When assessing overlap of outliers across treatment groups, we downsampled the dataset such that

we retained a random 10% of $S_{1/\sigma}$ = 10 and a random 50% of $S_{1/\sigma}$ = 2 genes per iteration. This step

was taken to try to reduce the proportions of genes under the strongest selection treatment within

the dataset from their initial ~20% proportions to a more realistic ~2% and ~10% respectively.

Downsampling was bootstrapped 100 times, with the proportional overlap between demographic

treatments recorded per iteration and averaged across all runs. Following downsampling, we

examined proportional overlap of the two 95% outlier sets with an expected proportional overlap of

0.05 under a null hypothesis. To examine how simulated gene features influenced patterns of

genetic divergence, we used random forests of 100 trees with the R package *randomForest* and

calculated relative importance of each feature. Gene features considered were: within-population π

of the derived population, number of exons (Exon N), gene size, the proportion of gene that is

coding (Target Proportion). Also included were the selection ($S_{1/\sigma}$) imposed on the gene and the

generation at which the optimum phenotype was reached (Pheno Gen).

RESULTS

Demography modifies measures of divergence

Bottlenecks, simulated by modifying the number of founding individuals, had little effect on F_{ST} and

D_{XY}, producing minimal variance between treatments over all sampling points (Figure 2A).

Conversely, there was a relatively pronounced effect on $\Delta\pi$ that persisted for several hundred

generations. Genes that were simulated with the most extreme bottlenecks displayed inflated

measures of divergence in $\Delta\pi$ because of a sharp reduction in π in the derived population.

Contractions, simulated by modifying the stable number of individuals within the derived

population, had pronounced and variable effects on all measures. F_{ST} was negatively associated with

contractions, with values increasing with a reduction in derived population size. This effect was

generally consistent through time, however early sampling points exhibited the largest variance

between the most extreme contraction treatments, whereas later on the strongest variance was

observed between weaker treatments (Figure 2B). A similar effect was observed for $\Delta\pi$; however,

this measure was particularly susceptible to inflation under the most extreme contraction scenarios,

with substantially more elevated values observed between contraction proportions of 0.01 and 0.1

compared with 0.1 and either 0.5 or 1.0. Whilst this pattern was broadly consistent through

sampling points, variance among the different contraction levels for $\Delta\pi$ was most pronounced at the

initial (100 generations) and final sampling points (10,000 generations). Such observations are

unsurprising given that both F_{ST} and $\Delta\pi$ increase with processes that reduce within-population

genetic variance. D_{XY} was largely unaffected by contraction treatments up until the third sampling

point (3162 generations). Following this, in contrast to F_{ST} and $\Delta\pi$, D_{XY} decreased when derived

population sizes were reduced (Figure 2B).

The inclusion of migration reduced absolute values of all measures of divergence. For F_{ST} and D_{XY},

variance between migration treatments increased across the simulation, however D_{XY} was generally

more consistent across migration treatments. $\Delta\pi$ was also reduced in the presence of migration,

although the effect of migration on $\Delta\pi$ was generally consistent across all generations and did not

increase through time, as was the case for F_{ST} and D_{XY}.

Unsurprisingly, there was a consistent trend regardless of demographic treatment for F_{ST} and D_{XY} to

increase generally over time, however this was not the case for $\Delta\pi$, which was generally constant

through time whilst marginally declining. The majority of these patterns were apparent in the

Pheno$_{Null}$ simulations (Figure S3), however genetic differentiation for all measures was reduced by

the removal of derived phenotypes when gene flow was present.

Figure 2: Effects of demographic treatments on measures of genetic divergence across all sampling
generations. Point colour and shape denote treatment groups for bottlenecks (**A**), population

contraction (**B**) and migration (**C**). Each point represents values of divergence averaged across all
genes, and all other treatment levels beyond those of the treatment group of interest.
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Demography moderates the association between measures of divergence and selection

Bottlenecks had a minimal effect on the correlations observed between strength of selection and

measures of divergence with minimal variance observed between bottleneck treatments in all

comparisons (Figure 3A).

Population contractions had substantial effects on relative (F_{ST} and $\Delta\pi$) measures and marginal

effects on absolute (D_{XY}) measures of divergence (Figure 3B). Relative measures in smaller derived

populations (0.01, 0.1) were less correlated, and indeed largely uncorrelated with selection than

those observed in treatments with minimal (0.5) or no (1.0) contractions (Table 1). For F_{ST} the

variance in correlation coefficients between contraction treatment groups generally increased

across time whereas variance between treatments for $\Delta\pi$ peaked at 3,162 generations. For D_{XY},

correlations with selection were broadly consistent across contraction treatments up until 10,000

generations, in which associations with selection were reduced by stronger contractions (Figure 3B).

Expectedly, the absence of migration largely precluded the ability of measures of divergence to

predict strength of selection, with notable variance observed between no migration (M= 0.0) and

minimal migration (M = 0.002) treatments by 3,162 generations for all divergence measures (Figure

3C) (Table 1). Both F_{ST} and D_{XY} variance between migration treatments was greatest at the 10,000

generations sampling point, whereas similar variance was observed between migration treatments

for $\Delta\pi$ at both 3,162 and 10,000 generations. This observation again highlights the significance of

temporal differences between measures.

Pheno$_{Null}$ simulations resulted in weaker correlations with $S_{1/\sigma}$ for F_{ST}, whilst D_{XY} became negatively

correlated with $S_{1/\sigma}$ over time (Figure S6B) rather than positively correlated. $\Delta\pi$, however, became

more positively correlated with $S_{1/\sigma}$ over time for all demographic treatments (Figure S6C). These

results demonstrate that increases in F_{ST} are partly dependent on divergent selection, increases in

D_{XY} are exclusively dependent on divergent selection (and adaptive substitutions), and $\Delta\pi$ increases

are less indicative of divergent selection and more of stabilising selection and within-population

variance.

Table 1: Correlation coefficients between measures of divergence and selection, separated according to individual treatment levels across all sampling generations. For each measure, the largest correlation coefficient is highlighted in bold.

Treatment	Level	F_{ST}				D_{XY}				$\Delta\pi$			
		100	316	3,162	10,000	100	316	3,162	10,000	100	316	3,162	10,000
Bottleneck	2	-0.006	0.040	0.129	0.169	0.016	0.019	0.033	0.095	0.006	0.083	0.148	0.072
	20	0.013	0.051	0.140	0.165	0.031	0.026	0.043	0.093	0.010	0.097	0.137	0.071
	100	0.010	0.043	0.147	0.177	0.024	0.022	0.050	0.102	0.009	0.084	0.138	0.074
	1000	0.007	0.040	0.133	0.165	0.020	0.021	0.041	0.097	0.019	0.079	0.149	0.070
Contraction	0.01	0.015	0.019	0.033	0.053	0.030	0.034	0.039	0.052	0.004	0.008	0.006	-0.024
	0.1	0.000	-0.001	0.087	0.157	0.015	0.006	0.020	0.110	0.034	0.040	0.189	0.122
	0.5	0.009	0.078	0.269	0.304	0.025	0.027	0.063	0.147	0.013	0.168	0.378	0.214
	1	0.000	0.136	0.306	0.355	0.022	0.020	0.051	0.138	0.031	0.260	**0.406**	0.245
Migration	0	0.003	0.029	0.074	0.062	0.020	0.014	0.006	-0.015	0.018	0.081	0.094	0.007
	0.002	0.012	0.101	0.335	**0.429**	0.027	0.033	0.092	**0.223**	0.003	0.105	0.241	0.191

Figure 3: Effects of demographic treatments on the relationship between selection ($S_{1/\sigma}$) and
measures of genetic divergence across all sampling generations. Point colour and shape denote
treatment groups for bottlenecks (**A**), population contraction (**B**) and migration (**C**). Each point
represents correlation coefficients averaged across all genes, and all other treatment levels beyond
those of the treatment group of interest.

By examining the correlation coefficients of all 32 unique demographic histories, we can investigate

the combined effect of migration and contraction and directly compare effectiveness of individual

measures across time (Figure 4). F_{ST} consistently outperforms D_{XY} in terms of associating with $S_{1/\sigma}$

under most demographic treatments, particularly when contractions are weak and migration is

present. By 10,000 generations however, the relative dominance of F_{ST} appears to marginally

subside, with the trend through time suggesting a relative improvement in D_{XY} in treatments with

gene flow (Figure 4). $\Delta\pi$ is similarly more informative than D_{XY} across sampling generations under

most demographic treatments. Interestingly, at sampling points 316 and 3,162 contractions produce

the biggest bias towards $\Delta\pi$, however by 10,000 generations zero migration produces the largest

deviance away from the y=x relationship (Figure 4). The resilience of $\Delta\pi$ under no-migration

treatments is also apparent in F_{ST} - $\Delta\pi$ comparisons, such that at 316 and 3,162 generations $\Delta\pi$ is

more informative than F_{ST} in the absence of migration. By 10,000 generations however F_{ST}

outperforms $\Delta\pi$ under most scenarios, indicative of the decaying association between $\Delta\pi$ and $S_{1/\sigma}$

discussed previously.

Figure 4: Pairwise comparisons between the correlation coefficients of $S_{1/\sigma}$ with F_{ST}, D_{XY} and $\Delta\pi$
across all sampling points. Each data point represents a unique demographic treatment with points
coloured according to contraction level and shaped according to migration level. Correlation 1 refers
to the first measure listed in the comparison and Correlation 2 to the second. The y=x line is plotted
within each facet to illustrate biases towards one measure. Points below the line are biased towards
Correlation 1, whilst points above the line are biased towards Correlation 2.

Demography moderates the tail end of divergence distributions

Ultimately, outlier tests are concerned with the extreme tail end of the distribution, and as such

correlation coefficients across the whole dataset may fail to reflect consistent outliers. To counteract

this, we asked at each sampling point what the relative proportions of outliers above the 99th

quantile were per $S_{1/\sigma}$ treatment, and how these proportions varied according to individual

demographic treatments (Figure 5) and collectively (Figure 6) after 10,000 generations (results for

other sampling points and mutation rates Figure S10-20). Each simulated 'genome' consisted of

~1000 genes evenly distributed across the 5 treatment levels of $S_{1/\sigma}$, meaning expected null

proportions of each $S_{1/\sigma}$ value are 0.2. This analysis assumes that if measures of differentiation are

good at highlighting genes under the strongest selection coefficients, genes within the upper 1% of

the distribution should be disproportionately associated with stronger selection ($S_{1/\sigma}$ = 2 or 10).

We found that migration and contraction treatments influenced the relative proportions of $S_{1/\sigma}$

treatments in the upper F_{ST} quantile. Under the weakest contraction treatment, the proportion of

$S_{1/\sigma}$ = 10 outliers increased from 0.19 (contraction = 0.01) to 0.33 (contraction = 1.0) (null

expectation of 0.20 given 5 selection treatments). Migration also dramatically increased the

proportion of genes under the strongest selection from 0.19 to 0.63. The extreme effect of migration

is evident when combining contraction and migration treatments (Figure 6). Whilst weaker

contractions yield a greater proportion of strong selection outliers (moving left to right in the figure),

migration is the dominant factor given that the treatment with the most extreme contraction (0.01)

and migration present has a stronger selection bias than the treatment with no contraction and

migration absent (Figure 6).

The upper quantile of D_{XY} outliers was unaffected by bottlenecks and contractions but was heavily

biased towards $S_{1/\sigma}$ = 10 genes in the presence of migration (Figure 5). Proportions of $S_{1/\sigma}$ = 10

outliers doubled in the presence of migration from 0.27 to 0.54. Proportions across the 16 unique

contraction/migration patterns produced results analogous to F_{ST}, with migration the dominant

factor in biasing proportions towards strong selection genes (Figure 6).

Except for the most extreme population contraction, Δπ outlier proportions were strongly indicative

of genes under strong selection, yielding outlier proportions for $S_{1/\sigma}$ = 10 genes of 0.72 (contraction =

0.1), 0.61 (contraction = 0.5) and 0.58 (contraction = 1.0) at sampling generation 10,000. Effects of

contractions were visible for Δπ outliers by generation 100 at the most extreme treatments (Figure

S10) and clear across all 3 weaker contraction treatments by 3162 generations (Figure S12).

Migration had a more modest effect on outlier proportions relative to contractions, increasing the

proportion of genes under the strongest selection from 0.16 to 0.41 at sampling generation 10,000.

The effect of migration was not as persistent through time however, emerging only by generation

3,162 with $S_{1/\sigma}$ =10 proportions of 0.18 (migration = 0) and 0.24 (migration = 0.002). These results

are corroborated across the 16 contraction/migration treatments, as proportions acquired from

treatments with extreme contractions (contraction = 0.01) are relatively uniform with only a small

biasing effect of migration (Figure 6). For all other treatments, outliers are heavily biased towards

strong selection genes.

Taken together, these results highlight that outlier detection using F_{ST} and D_{XY} are heavily dependent

on the presence of migration, and to a lesser extent the absence or minimising of population

contractions for F_{ST}. Δπ outliers appear rapidly and are generally robust in relation to population

contractions up until the most extreme treatment. Whilst migration also influences Δπ, the biasing

of outliers towards genes under the strongest selection treatment is less extreme.

Removing divergent selection (Pheno$_{Null}$) moderated outlier proportions in line with expectations

given correlations with $S_{1/\sigma}$ (Figures S21-24). Interestingly, over time both F_{ST} and Δπ outliers were

skewed further towards stronger selection treatments when migration was absent (stronger

patterns of reduced within-population variance) in comparison to simulations with phenotypic

divergence, whilst D_{XY} outliers became biased towards weaker selection treatments in the presence

of gene flow.

Figure 5: The effect of demography on representation of genes under different selection treatments
as a proportion of outliers above the 99% quantile. Colour of bars within stacks denotes different
selection treatments. Vertical facets represent different demographic treatments and horizontal
facets show effect per measure of genetic divergence. Results shown are from sampling generation
10,000. Results for other sampling points can be found in Figures S10-12.

Figure 6: The combined effects of contractions (proportion relative to ancestral population size = 1,000) and migration in 16 unique demographic treatments (all combinations of contraction and migration treatments) on representation of genes under different selection treatments as a proportion of outliers above the 99% quantile. Full information regarding demographic treatment is described on the x-axis. Colour of bars within stacks denotes different selection treatments. Horizontal facets show effect per measure of genetic divergence. Results shown are from sampling generation 10,000.

Demography moderates associations between measures of divergence

Given F_{ST}, D_{XY} and $\Delta\pi$ are all measures of population genetic divergence, there is an assumption that

positive associations should exist between them. We employed the same analysis as above for

correlations with $S_{1/\sigma}$, but instead examined correlations between individual measures. Bottlenecks

had minor effects on the correlations observed between measures of divergence (Figure 7A).

Expectedly, effects were strongest at the first sampling point, with the most extreme bottlenecks

increasing the correlation coefficients between F_{ST} & D_{XY} and D_{XY} & $\Delta\pi$ and decreasing the correlation

coefficient between F_{ST} & $\Delta\pi$. Variation in correlation coefficients was generally minimal however

compared to the effects of other demographic treatments.

F_{ST} & D_{XY} were positively associated irrespective of demography, but smaller population sizes

generally increased the association (Figure 7B) with variance between treatments generally

decreasing through time. Similarly, F_{ST} & $\Delta\pi$ were typically positively associated, however

contractions had a more pronounced effect on the association. Extreme contractions increased the

association between F_{ST} & $\Delta\pi$, with contraction-induced variance increasing across sampling points

(Figure 7B). At 10,000 generations when variance was largest, F_{ST} & $\Delta\pi$ ranged from being generally

well associated under extreme contractions (R^2 = 0.60) to unassociated when populations were

equally sized (R^2 = 0.08). D_{XY} & $\Delta\pi$ correlations were initially weak early in the simulations, however

increased generally over time, with populations contractions similarly inflating associations between

measures. Interestingly, associations with D_{XY} and both F_{ST} and $\Delta\pi$ appear to peak for weak

contraction treatments at 3,162 generations, suggesting a probable temporal factor within the

simulations driving positive associations with D_{XY} at some point between 316 and 3,162 generations.

Migration induced substantial variance between correlations of divergence measures, with effects

dependent on sampling point (Figure 7C). In the absence of migration, F_{ST} & D_{XY} were strongly

associated at 100 and 316 generations, whilst associations were weaker in migration-present

treatments. However, by 3,162 generations F_{ST} & D_{XY} associations increased substantially in the

presence of migration, and by 10,000 generations the effect of migration had reversed entirely. F_{ST} &

$\Delta\pi$ associations were strong initially, but migration weakened the association over time so

migration-present associations ranged from R^2 = 0.67 (100 gens) to R^2 = 0.14 (10,000 gens). In

contrast, in the absence of migration positive associations between F_{ST} & $\Delta\pi$ were relatively stable

(R^2 = 0.55 – 0.51 over the same time period). Interestingly, without migration D_{XY} & $\Delta\pi$ were largely

unassociated, but migration-present treatments induced a negative association between D_{XY} & $\Delta\pi$

over time from R^2 = -0.04 (100 gens) to R^2 = -0.28 (1000 gens).

Contextualised by our previous demonstrations of associations with selection, these results highlight

that selection can induce positive associations between measures. Namely, F_{ST} & D_{XY} become

strongly associated by generation 10,000 with migration present, which we know is when F_{ST} and D_{XY}

are most strongly linked to selection. Crucially, however this relationship only emerges after several

thousand generations, before which we observe positive associations in migration-absent

treatments when associations with selection are weak for both measures. Extreme contractions also

induce positive associations between F_{ST} & D_{XY} that are likely indicative of false-positives given the

poor association with selection in these treatments. These results highlight that positive associations

between statistics are also achievable under neutrality. It is also interesting to note the decay of

associations with $\Delta\pi$ and both F_{ST} and D_{XY} under demographies in which selection should be

effective. These observations are most likely driven by the substitution rate. Substitution rates are

increased under stronger selection (Lanfear, Kokko, and Eyre-Walker 2014) and drive increased F_{ST}

and D_{XY} but not $\Delta\pi$.

Figure 7: Effects of demographic treatments on the relationship between measures of genetic divergence across all sampling generations. Point colour and shape denote treatment groups for bottlenecks (**A**), population contraction (**B**) and migration (**C**). Each point represents correlation coefficients averaged across all genes, and all other treatment levels beyond those of the treatment group of interest.

In Pheno$_{Null}$ simulations the influence of bottleneck treatments and contraction treatments was

broadly unchanged, however the notable emergence of a correlation between measures of F_{ST} and

D_{XY} in simulations with gene flow failed to emerge by generation 10,000 (Figure S27). This

demonstrates that this positive correlation is driven by divergently adaptive allele frequency shifts

and substitutions. In addition, the decay of the relationship between F_{ST} and $\Delta\pi$ in the face of

migration did not occur without divergent selection. Rather, this relationship remained strongly

positive ($R^2 > 0.5$) up to 10,000 generations regardless of migration treatment (Figure S27C).

To examine the overlap of outliers across measures of divergence, we again sub-divided our

treatments into treatment-specific levels and compared the three-way and all pairwise upper 95%

quantile gene overlaps across measures of divergence at sampling point 10,000. Three-way

agreement was generally greater than expected by-chance under most conditions, with the largest

overlap observed under extreme contractions (Figure 8). Our results demonstrate large overlap

between F_{ST} and D_{XY} outliers across all treatments, which was marginally increased by contraction

treatments that favour the effectiveness of selection. This association suggests stronger selection

may improve the positive association between F_{ST} and D_{XY}, however a causative effect is not clear.

Whilst overlap increased by selection-favouring conditions, all treatment levels exhibited above-

expected levels of F_{ST} - D_{XY} overlap, suggesting a strong potential for false-positives. Overlap

between $\Delta\pi$ and both F_{ST} and D_{XY} was substantially less but had contrary associations with

contractions. More extreme contractions tended to increase the overlap between $\Delta\pi$ and F_{ST}

outliers, suggesting a shared risk of false-positives. In contrast, $\Delta\pi$ and D_{XY} outlier overlap tended to

increase under weaker contractions, suggesting a beneficial effect of combining these measures to

remove false-positives. Migration increased outlier overlap between $\Delta\pi$ and both F_{ST} and D_{XY}.

Figure 8: Proportional overlap of 95% outliers across measures of divergence, separated according to treatment levels of bottlenecks (**A**), contractions (**B**) and migration (**C**).

Demography drives signals of convergence irrespective of selection

By sampling generation 10,000, significant overlap in outlier genes was apparent in F_{ST} results across

all demographic treatments that had no migration (Figure 9). Within this cluster, the average overlap

of downsampled outliers above the 95% ranged between 0.07 and 0.32, suggesting a 1.4- to 6.4-fold

enrichment above the null expectation (0.05). These minimum and maximum values were observed

between extremes of contraction (minimum) or when contractions were absent (maximum). Given

the poor association between F_{ST} and selection in the absence of migration, convergent F_{ST} outliers

here are likely driven by neutral processes and would constitute a false-positive signal. Outside of

this cluster, there was also reasonable clustering of results across treatments that included

migration and weaker contractions (0.1, 0.5 or 1.0). Here, overlap of outliers ranged between 0.08

and 0.26, representing a 1.6- to 5.2-fold enrichment above the expected. In the presence of

migration and minimal contractions F_{ST} is a good predictor of selection in our dataset, suggesting this

convergence may be driven by inferred selection. Beyond these clusters, overlap between

treatments of contrasting migration treatment failed to exceed 0.18. Interestingly, the clustering of

F_{ST} outliers in the presence of migration was heavily reduced when divergent selection was removed

(Pheno$_{Null}$) but clustering of outliers in the absence of migration was still strong (Figure S39).

Figure 9: The proportional overlap of outliers above the 95% quantile for F_{ST} values, averaged across 100 randomly downsampled datasets for each of the 32 demographic treatments. Colouring of axis labels denotes migration treatment level. Axis orderings were determined through hierarchical clustering

Clustering of D_{XY} outliers followed a broadly similar pattern to F_{ST} with migration treatments

dominating the clustering and inducing proportional overlaps of 0.11-0.34 (2.2- to 6.8-fold

enrichment) in the absence of migration (Figure S31). In general, proportional overlap of Δπ outliers

was lower than for F_{ST} and D_{XY}, with a maximum overlap observed of 0.21 (fold-enrichment 4.2)

(Figure S32). This value was observed in two treatments with minimal contractions (0.5-1.0) and

migration present. Generally, however, clustering by demography was weaker in Δπ than for F_{ST} and

D_{XY}, corroborating previous results suggesting Δπ may be less susceptible to variation in migration

and contraction (with the exception of extreme contraction).

Because migration was the dominant factor in clustering of treatments with convergent overlaps, we

sought to investigate what features of simulated genes drove variance in measures of divergence

with treatments separated by migration factor using a Random Forest approach (Figure 10). For F_{ST},

we observe that the best predictor of variance in the absence of migration is diversity (π) of the

derived population whilst treatments with migration are most strongly influenced by $S_{1/\sigma}$. This is

consistent with the notion of F_{ST} relying on within-population genetic variance in the absence of

efficient selection. In contrast, D_{XY} in the absence of migration is most strongly driven by gene

features, predominantly the proportion of simulated gene that is coding and by the length of the

simulated gene. With migration, D_{XY} variance is driven by selection and derived π. Unsurprisingly, Δπ

is also strongly influenced by derived π (the denominator in its calculation), but we can see a

secondary role for selection in treatments with migration and little influence of gene features.

Removing divergent selection (Pheno$_{Null}$) did not modify the relative importance of any features of

simulations for F_{ST}, but did affect D_{XY} and Δπ (Figure S44). With migration, the relative importance

for derived population π in explaining D_{XY} variance increased substantially. For Δπ, selection was as

important as derived population π in explaining variance.

Figure 10: The relative importance of simulated gene features in eliciting variance in measures of genetic variance. Boxplots denote the relative importance of each explanatory variable across 16 individual treatments with/without migration taken at sampling generation 10,000. Variables considered are within-population π of the derived population and gene features including: Number of Exons (Exon N), Gene Size, and the proportion of gene that is coding (Target Proportion). Also included are the selection ($S_{1/\sigma}$) imposed on the gene and the generation at which the optimum phenotype is reached (Pheno Gen).

DISCUSSION

Summary of results

Here, we show that differing demography can have dramatic effects on how measures of population

divergence identify regions of the genome under selection. Effects are also strongly time-dependent.

Using simulated populations, we have demonstrated the relative influences of founding bottlenecks,

population contractions, and migration on three commonly used measures of genetic divergence

(F_{ST}, D_{XY}, $\Delta\pi$), whilst demonstrating the relative usefulness of each measure for informing on

selection under different demographic conditions.

We find that founding bottlenecks have little effect on population divergence measures, with only

minor influence over differences in nucleotide diversity ($\Delta\pi$) shortly after founding. Population

contractions (size of diverging population), however, artificially inflate F_{ST} and $\Delta\pi$ but reduce D_{XY}, and

can erase the relationship of F_{ST} and D_{XY} with selection under the most extreme contractions. These

results can be explained in part due to the relationship between founding population size and

relative (F_{ST} and $\Delta\pi$) and absolute (D_{xy}) divergence measures. Relative measures are, in part, driven

by intra-population changes in allele frequency, which become exaggerated in smaller populations

as a product of drift (B. Charlesworth 2009; Ellegren and Galtier 2016). As a consequence, we

observe inflated measures of relative divergence as allele frequencies drift in our smaller derived

population.

D_{xy} in contrast increases under weaker population contractions as a product of the relationship

between the number of segregating sites and the population-level mutation rate ($4N_e\mu$) (Hartl, Clark,

and Clark 1997). D_{xy} is a measure of sequence divergence and is averaged across all sites (although

averaging across all segregating sites is possible), which results in higher D_{XY} as segregating sites are

introduced into either population at rate of $4N_e\mu$. This relationship with the number of segregating

sites can be observed by examining the positive relationships between D_{xy} and π in our derived

population (Figure S45). Overall, the relationship between D_{xy} and selection is less affected by

population contractions than F_{ST} and $\Delta\pi$, likely due to the lack of allele frequency relevance.

Consider for example, two SNPs with minor allele frequencies of 0/0.5 (SNP 1) and 0.5/0.5 (SNP 2) in

the ancestral/derived population. Each locus contributes equally towards D_{xy} (SNP 1 = [0 x 0.5] + [1 x

0.5] = 0.5; SNP 2 = [0.5 x 0.5] + [0.5 x 0.5] = 0.5), whereas the reduction of within-population

variance observed for SNP 1 inflates F_{ST} and $\Delta\pi$.

Migration, even at the relatively modest rate of 0.2% employed here, reduced absolute values for all

measures of divergence substantially. However, whilst absolute values were reduced, their

informativeness of selection coefficients increased dramatically (both in terms of their overall

relationship with selection and in identifying outliers). Such a result is expected given the role of

gene-flow in homogenising neutral loci (reducing measures of divergence), whilst retaining

population divergence around adaptive loci (increasing informativeness). The well-known 'genomic

islands of divergence' model is often invoked to explain this pattern of heterogenous genomic

divergence in studies of speciation-with-gene-flow (Nosil, Funk, and Ortiz-Barrientos 2009; Turner,

Hahn, and Nuzhdin 2005).

Migration also exhibited interesting temporal patterns that are useful for discussing the

discrepancies observed between $\Delta\pi$ and both F_{ST} and D_{xy}. Of the measures we considered, $\Delta\pi$

uniquely disregards SNP substitutions in its calculation, as fixed substitutions have no influence on

intra-population heterozygosity beyond reducing the heterozygosity of proximate SNPs in the

aftermath of a hard sweep. This characteristic explains why $\Delta\pi$ responds to selection more rapidly

than F_{ST} and D_{xy} and is influenced by migration in a constant manner across time. In addition, the

inability of $\Delta\pi$ to account for adaptive substitutions is likely why $\Delta\pi$ informativeness peaked at 3,162

generations and decayed by 10,000 generations. In contrast, the contributions of adaptive

substitutions to F_{ST} and D_{xy} over time increases their predictive power. This temporal observation

has important implications for studies of rapid adaptation on the scale of 10s to 100s of generations,

in which our simulations suggest Δπ may be the most informative measure of divergence, whilst D_{xy}

was largely uninformative until > 3,162 generations.

Examining the effects of demographic variation on the associations between measures of divergence

themselves is a novel element to this study. The relative weaknesses of individual measures of

divergences has prompted a recent movement within the literature to employ multiple measures of

divergence to avoid false-positives. Our results provide some support for this strategy, with outlier

overlap across measures generally increasing under conditions that favour informativeness of

selection, suggesting their combined use may be useful in removing false-positives. Importantly,

however, we also find that F_{ST} and D_{xy} (and to a lesser extent F_{ST} and Δπ) have overlapping outliers

across demographic treatments with ineffective selection.

Cruickshank and Hahn (2014) suggested that a disagreement between F_{ST} and D_{xy} outliers in

genomic-islands-of-divergence tests highlighted a particular susceptibility of F_{ST} to BGS (although see

(Matthey-Doret and Whitlock 2018)). Our results are in line with the notion that D_{xy} is more resistant

to false positives due to BGS, given that contraction treatment levels resulted in minimal variance in

D_{xy} (assuming treatment levels of population contraction are analogous to different rates of BGS

across the genome in exhibiting reduced N_e). We also showed that F_{ST} and D_{XY} are positively

correlated under several demographic scenarios, but this strong association only reflects selection

when gene-flow is present and only after several thousand generations, consistent with previous

simulation work (Ravinet et al. 2017). When migration is absent, and selection ineffective, F_{ST} and D_{XY}

are also positively correlated; but this relationship decays over time (Figure 7C), with empirical

evidence (see below) suggesting a negative relationship is likely to emerge without gene flow. No-

migration treatments are consistent with Isolation-By-Distance demographic histories and, similarly,

inter-specific comparisons. Indeed, negative correlations between F_{ST} and D_{XY} within and between

clades of birds (Vijay et al. 2017; Irwin et al. 2016), within a radiation of monkeyflowers (Stankowski

et al. 2018) and between speciating orca populations (Foote et al. 2016) support a declining

relationship between these measures over long periods of time in isolation. This negative

association between measures in the absence of effective selection is also predicted, given F_{ST} is

negatively associated with within-population π (increases within-population variance), D_{XY} is

positively associated with local π (reduces likelihood of common sequence) and π is generally well-

conserved in stable populations even across long time periods (Romiguier et al. 2014; Van Doren et

al. 2017; Dutoit et al. 2017).

Similarly, we found F_{ST} – Δπ outliers under most demographic scenarios and overlapping outliers

marginally increased under extreme contractions. These results, again, support the notion that using

multiple measures may be useful in reducing false-positives under demographic scenarios with

effective selection, but there exists a risk of false-positives occurring across populations with

ineffective selection.

In comparing our results to a second dataset that lacked divergent selection (Pheno$_{Null}$), we found

consistent support that associations between D_{XY} and selection are strongly dependent on the

inclusion of a divergent phenotype; F_{ST} patterns are attainable with stabilising selection (but are

weaker than when divergent selection is included); and Δπ patterns are primarily driven by variable

stabilising selection and made weaker by the inclusion of phenotypic divergence. These comparisons

are useful in highlighting the relative roles of adaptive allele frequency changes and substitutions in

driving patterns of genetic differentiation. It is also of interest to note that overlapping outliers are

readily attainable across no-migration treatments in Pheno$_{Null}$ simulations, but not for treatments

with gene-flow (Figure S39). This confirms that overlapping outliers in no-migration treatments

occur due to common neutral processes within genes, whereas overlapping outliers in treatments

with migration are driven by the effects of divergent selection. The discrepancies between our

Pheno$_{Null}$ and other simulated datasets highlight the necessity in quantifying phenotypic differences

or environmental selection pressure when interpreting patterns of variation across the genome.

Detecting genetic convergence

In addition to understanding how outlier detection in individual pairs were affected by demography,

we also wanted to explore how studies looking at overlapping outliers in multiple pairs (i.e. genetic

convergence) were affected by demography. Our simulation design, in which an ancestral burn-in

population is used to found 32 independent pairs of ancestral – derived populations is analogous to

replicated ecotype population pairs in model systems, such as various ecotype pairs of the three-

spined stickleback, *Gasterosteus aculeatus* (Hohenlohe et al. 2010; Jones, Chan, et al. 2012);

high/low predation Trinidadian guppies, *Poecilia reticulata* (Fraser et al. 2015); crab/wave ecotype

periwinkles, *Littorina saxitilis* (Ravinet et al. 2016; Kess, Galindo, and Boulding 2018; Westram et al.

2014), and alpine/montane ecotypes of *Heliosperma pusillum* (Trucchi et al. 2017). We found

overlapping outliers between demographic treatments (proportions above a random null

expectation), and therefore that signals of convergent genes are attainable for both F_{ST} and D_{XY}.

Clustering of outliers was predominantly driven by the presence or absence of migration (with

minimal overlap beyond expectations between clusters).

Given that within our simulations, selection is expectedly ineffective when migration is absent,

overlap of outliers across migration-free treatments suggests a different subset of genes, which are

not under strong selection, are repeatedly reporting the strongest signals of genetic divergence for

both F_{ST} and D_{XY}. In seeking to explain this, we took a random forest approach to explain how

different features of our simulated genes may explain variance in measures of divergence. F_{ST} was

heavily influenced (negative association) by within-population genetic diversity (π), and to a lesser

extent gene features such as gene length (negative) and the generation at which the new

phenotypic optimum was reached ("Pheno Gen", positive), in the absence of migration. This is

consistent with previous theoretical and empirical work highlighting the susceptibility of F_{ST} to

processes that reduce within-population diversity in the absence of selection, such as heterogeneity

in recombination landscape (Cutter and Payseur 2013; Ravinet et al. 2017), structural variation

(Kirkpatrick and Barton 2006), and gene density (Enard, Messer, and Petrov 2014; Cutter and

Payseur 2013). Without migration, D_{XY} outliers were categorised through features of simulated

genes, predominantly length of gene (positive) and proportion of gene that was coding (positive).

Such an effect may be explained by reduced neutrality of mutations within coding regions, and

therefore genes with increased coding content tend to exhibit reduced neutral polymorphism

(across both the ancestral and derived population) and lower D_{XY} as a result across multiple

demographic treatments. The secondary effect of gene length is less clear, given that D_{XY} is averaged

across all sites, but may stem from potentially lower linkage in larger genes (Ellegren and Galtier

2016) or the increased accumulation of segregating sites in larger genes (given mutation occurs with

a fixed probability per site). With effective selection in the presence of migration, we observed the

expected effect of simulated $S_{1/\sigma}$ in producing overlapping D_{XY} outliers. Interestingly however, we

also observed an effect of derived population π that hints towards a susceptibility to BGS even in the

presence of effective selection. This dependence on the efficacy of selection in detecting

overlapping outliers may explain the discrepancies within the literature regarding the susceptibility

to BGS of both F_{ST} (B. Charlesworth, Nordborg, and Charlesworth 1997; Noor and Bennett 2009;

Cruickshank and Hahn 2014) and D_{XY} (Matthey-Doret and Whitlock 2018).

It is perhaps surprising that population contractions (with the exception of the most extreme factor

level) did not have a dominant influence in detecting genetic convergence, given the strong effect on

population contractions on the relationship between population divergence and selection. However,

this is consistent with the increased influence of random drift in populations with reduced N_e,

thereby limiting repeatability of outliers.

Limitations of simulations

In our analyses, we grouped genes within 32 unique demographic treatments, assuming the effects

of contraction and migration are equivalent for all genes. This may be unrepresentative of genomes

sampled from the wild, in which gene flow and effective population size can vary across genomic

regions through structural variation, variable recombination rate and BGS (Gossmann, Woolfit, and

Eyre-Walker 2011). A prominent example of such a mechanism is the well-characterised

consequence of reduced gene-flow within inversions that carry locally adapted alleles. Assuming

inversion variants are fixed between populations, migration across the locus is limited by the

prevention of recombinant haplotypes and resistance to introgression (Kirkpatrick and Barton 2006;

Ravinet et al. 2017). Recent genome scan studies have highlighted convergent outliers within

inversions (Jones, Grabherr, et al. 2012; Nishikawa et al. 2015; Morales et al. 2018), confirming

theoretical models regarding their role in shielding adaptive haplotypes from introgression during

the adaptation process. Our simulations highlight that genes with reduced migration, and reduced

N_e as a consequence, will have inflated measures of divergence and differentiation relative to other

genomic regions. Therefore, we predict this to lead to their over-representation in genome scan

outliers, thus caution should be taken regarding the adaptive significance of these outliers relative to

absolutely lower values of genetic divergence attained from regions outside of chromosomal

rearrangements.

By choosing to use a factorial design here, we have increased our understanding in the interplay

between individual features of demographic history and multiple measures of population

divergence. However, computational limitations constrained absolute population sizes to a

maximum of 1,000 individuals and generations to a maximum of 10,000. To mitigate these

constraints, we repeated the analysis over multiple mutation rates to illustrate patterns over 100-

fold variation of θ. In general, most trends were consistent, suggesting that results should be

consistent across taxa of variable effective population size. However certain patterns were

exaggerated or dampened with increased or decreased mutation rate respectively, for instance it is

clear that the time lag on informativeness of D_{XY} on selection is shortest when θ is largest, which

results in stronger positive associations between F_{ST} and D_{XY} by generation 10,000. It is well-

documented that both N_e (Frankham 1995) and mutation rate (μ) (Hodgkinson and Eyre-Walker

2011) are highly variable across taxa, which suggests that applying knowledge of the relationships

between measures of population differentiation will vary by system.

Furthermore, temporal variation within our simulations is confounded by the time at which there

was a major shift in the derived population's phenotype (Figure S46-49), and by extension when

selective sweeps occur. This variation in timing is random with respect to adaptive mutations arising

de novo, but is also influenced by demography (Figure S50). For example, treatments that are

founded with strong bottlenecks are less likely to evolve using variation in the founder, increasing

dependence on *de novo* mutations. Additionally, variation in our population contraction parameter

modifies the per population number of new mutations per generation. This is also true for features

of simulated genes, such as absolute length of coding sequence. Predictable temporal variation in

the time at which adaptation is likely to occur is a probable source of variance between measures of

differentiation and is particularly clear for $\Delta\pi$.

Concluding remarks

We have used forward-in-time simulations to perform a factorial experiment in which we explored

the relationships between three measures of genetic differentiation, selection, and features of

demographic history that are commonly variable in natural populations. In agreement with previous

theoretical work, we found the reliance of measures of genetic divergence to indicate regions under

selection are dependent on demography and variable through time, with a notable lag in D_{XY}.

Furthermore, we provided novel comparisons between measures of genetic differentiation that call

into question the use of multiple measures of genetic differentiation to rule out false-positives. We

also demonstrated that signals of convergent evolution across independent replicates can be driven

by similar demographic histories with minimal influences of selection. Therefore, we strongly advise

those using overlapping outlier scans to carefully consider the demographic context of their system

to avoid false-positives. It is tempting to assume that replication in study design or analysis in the

form of taking multiple measures of genetic divergence can reduce the risk of attaining false-

positives. We hope to emphasise in this study that this is not the case, as false-positives (i.e. genome

scan outliers that are not associated with regions under natural selection) can be driven by non-

random genomic or common demographic features that cannot be bypassed through replication.

Moreover, many of the patterns we observe are variable through time, such that the relevant pitfalls

of analyses will depend on the age of the populations being considered.

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AUTHOR CONTRIBUTIONS

JRW and BAF conceived the project, developed the experimental design and contributed towards

the writing of the manuscript. JRW wrote and implemented the pipeline for simulations and analysis.

DATA ACCESSIBILITY

A full pipeline including all bash, Eidos and R scripts necessary to repeat this analysis can be

downloaded from github (https://github.com/JimWhiting91/Contingent_Convergence_Pipeline).

Supplementary figures (S1-50) have been uploaded through the GSA figshare portal. Supplementary

figures include results for different mutation rates and Pheno$_{Null}$ data across sampling generations

along with additional figures.

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CONFLICTS OF INTEREST

The authors declare no conflicts of interest

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