Insights from Fisher's geometric model on the likelihood of speciation under
different histories of environmental change

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Abstract

The formation of new species via the accumulation of incompatible genetic changes is

thought to result either from ecologically-based divergent natural selection or the order

by which mutations happen to arise, leading to different evolutionary trajectories even

under similar selection pressures. There is growing evidence in support of both ecological

speciation and mutation-order speciation, but how different environmental scenarios

affect the rate of species formation remains underexplored. We use a simple model of

optimizing selection on multiple traits ("Fisher's geometric model") to determine the

conditions that generate genetic incompatibilities in a changing environment. We find that

incompatibilities are likely to accumulate in isolated populations adapting to different

environments, consistent with ecological speciation. Incompatibilities also arise when

isolated populations face a similar novel environment; these cases of mutation-order

speciation are particularly likely when the environment changes rapidly and favors the

accumulation of large-effect mutations. In addition, we find that homoploid hybrid

speciation is likely to occur either when new environments arise in between the parental

environments or when parental populations have accumulated large-effect mutations

following a period of rapid adaptation. Our results indicate that periods of rapid

environmental change are particularly conducive to speciation, especially mutation-order

or hybrid speciation.

Keywords

Ecological speciation, mutation-order speciation, homoploid hybrid speciation, Fisher's

geometric model.

Introduction

According to the ecological theory of speciation, populations diverge when exposed to different environmental conditions (Schluter 2000). Metaphorically, populations in different environments are thought to evolve phenotypically across different fitness landscapes, diverging over time as they approach different fitness peaks. This theory can be tested using reciprocal transplant experiments in which the performance of phenotypically divergent populations and their hybrid progeny are measured in both parental environments. The results of such studies often indicate that the environment matters, with phenotypic differentiation and the performance of hybrids depending on the environment (Table 5.1 in Schluter 2000).

An alternative theory of speciation – "mutation-order speciation" – proposes that populations diverging under similar selection pressures may ultimately become reproductively isolated because they accumulate different sets of mutations, some of which are incompatible with one another (Mani and Clarke 1990; Schluter 2009; Schluter and Conte 2009; Mendelson *et al.* 2014). The focus here is on the reduction in fitness caused by combining genes that have independently spread in different populations, so-called "Bateson-Dobzhansky-Muller" incompatibilities (BDMI), regardless of the environment in which hybrids are assayed.

Empirical studies have suggested that both divergent selection and parallel selection are relatively common (Table 5.2 in Schluter 2000), suggesting that both ecological and mutation-order speciation may underlie the formation of new species in nature. Ecological speciation is often inferred based on local adaptation of parental populations to different abiotic (e.g., soil chemistry) or biotic conditions (e.g., pollinator communities) (see Waser and Campbell 2004 for a review of evidence in plants). While such data provides evidence for ecology-dependent selection, it does not prove that ecological differences underly reproductive isolation, rather than intrinsic genetic incompatibilities (BDMIs). Additional evidence for ecological speciation comes from reciprocal transplant experiments where hybrids formed by backcrossing to the foreign parent are less fit than backcrosses to the local parent (Rundle and Whitlock 2001), as seen in sticklebacks (Rundle 2002). Alternative evidence for ecological speciation is provided when populations that have independently adapted to a novel environment and that are isolated from their ancestral populations remain interfertile with other such populations from similar environments (Schluter 2000). Such "parallel ecological

speciation" has been found in a number of animal taxa, including sticklebacks and other

fish, walking-stick insects, and *Littorina* snails, but evidence in plants remains weak

(Ostevik *et al.* 2012).

Empirical evidence for mutation-order speciation includes cases of reciprocal

gene loss of duplicated genes in *Drosophila*, *Arabidopsis*, and yeast, where the loss of

one gene copy or the other is thought to have occurred under similar selection pressures,

reducing fitness in hybrids that lack the gene (see discussion and review of evidence by

Muir and Hahn 2015). Genetic conflict, such as meiotic drive or cytonuclear conflicts,

has also been shown to generate reproductive isolation in a manner consistent with

mutation-order speciation in a wide variety of animal and plant species (Crespi and

Nosil 2013).

Experimental evolution studies in the lab have also provided evidence for both

ecological speciation and mutation-order speciation. In such studies, multiple

independent cultures of organisms are allowed to evolve under either different

environmental conditions or identical conditions, following which genetic

incompatibilities are measured between the replicate populations. Evidence for ecological

speciation has been obtained in studies that have adapted lines to different conditions. For

example, Dettman *et al*. (2007) evolved multiple populations of the yeast *Saccharomyces*

cerevisiae in either rich media with high salt or in minimal media with low glucose. In

most replicates, hybrid diploids performed significantly worse than the strain that had

adapted to a particular local environment. Similarly, Dettman *et al*. (2008) adapted

Neurospora crassa to either high salinity or low temperature conditions, finding evidence

for the first stages of parallel ecological speciation. When crossed, reproductive success

was lower among hybrids formed from strains adapted to different environments than

among hybrids from strains adapted to the current environment being tested.

Evidence for mutation-order speciation includes an experimental evolution

study by Kvitek and Sherlock (2011) in *S. cerevisiae* involving multiple replicate

populations propagated under glucose limitation. Genomic sequencing revealed that

mutations in two genes (MTH1 and HXT6/HXT7) arose repeatedly in different lines but

were never found together. Subsequent crosses established that adaptive mutations at each

of these two genes were deleterious when combined, reducing the fitness of hybrids.

Similarly, a study of *S. cerevisiae* adapting in the presence of the fungicide nystatin found

that even the first-step mutations that arise during adaptation can be incompatible (Ono

et al. 2017). When lines that had accumulated different resistance mutations were crossed, the double mutants performed less well than single mutants in many cases ("sign epistasis"). Sign epistasis was also observed in an experiment with the bacterium, *Methylobacterium extorquens*, evolving to tolerate a genetically-engineered change to how formaldehyde is oxidized (Chou *et al.* 2014). Again, adaptive mutations tended to work poorly when combined.

Previous theoretical studies have modeled the fitness of recombinant hybrids under divergent and parallel adaptation following a period of adaptation with *de novo* mutations (Barton 2001; Chevin *et al.* 2014; Fraïsse *et al.* 2016). These models have clarified how segregation of different adaptive alleles reduces hybrid fitness ("segregation load"), via the separation of coadapted alleles. Using Fisher's geometric model to track fitness variability among hybrids between independently adapting populations, Chevin *et al.* (2014) found that segregation load (isolated from extrinsic, environment-dependent, fitness effects) is insensitive to whether adaptation occurred to the same or to different environmental optima (e.g., Figure 2 in Chevin *et al.* 2014). This work is a launching point for the current study, where we explore how the distribution of potential mutations and the speed of adaptation influence the mean fitness of hybrids, combining the segregation load and the mismatch to the environment in which hybrid and parental fitnesses are measured (i.e., both intrinsic and extrinsic incompatibilities; their Equation 1, see also Equation 3 of Barton 2001). Fraïsse *et al.* (2016) further found that Fisher's geometric model can generate many of the empirical patterns of speciation studies, from Haldane's rule to asymmetrical introgression.

As noted in these two studies, large-effect mutations are more likely to contribute to genetic incompatibilities. This prediction is consistent with the observation that incompatibilities arise often in short-term experimental evolution studies, because those studies typically induce strong selection favoring large-effect mutations. Large-effect mutations are more likely to cause hybrid breakdown both because large-effect mutations can have large pleiotropic side effects and because combining such mutants can overshoot the optimal fitness (Figure 1). Our work thus aims to explore the environmental conditions that allow such strong genetic incompatibilities to arise, measuring how overall reproductive isolation, including both intrinsic and extrinsic isolation, depends on the speed and direction of environmental change, as well as the average effect size of new mutations.

In another recent study, Simon *et al.* (2018) looked not at the processes
generating divergence between parental populations but at the fitness relationships
between different hybrid genotypes. Given a set of divergent alleles between the parents,
hybrid fitness depends on two main quantities, the hybrid index, H (the total proportion
of alleles from one parent), and heterozygosity, p_{12} (the proportion of divergent sites that
carry one allele from each parent population). Using a Brownian bridge approximation to
walk from hybrids with only alleles from one parent ($H = 0$) to hybrids with only alleles
from the other parent ($H = 1$) and using Fisher's geometrical model to describe fitness,
the authors predict the average fitness of all hybrid combinations (H, p_{12}) given
remarkably few summary statistics (the breakdown scores of the two parents and one
additional fitted parameter; see their Equation 6), matching empirical data sets well.
Importantly, Simon *et al.* (2018) take the divergence between the parents as a given (the
number of diverged sites and the average trait variance contributed by each site). By
contrast, we focus here on how the history of environmental change influences the genetic
differences observed between the parents and the amount of hybrid breakdown (i.e., the
fitted parameter in Simon *et al*. (2018)). In particular, we explore the conditions under
which large effect mutations are likely to accumulate, leading to greater trait variance per
locus and greater hybrid breakdown, even among parental populations experiencing the
same environments. We then use the Brownian bridge approximation of Simon *et al.*
(2018) to fit fitness data from a variety of hybrid types.

Specifically, using simulations, we assess how the history of adaptation to
environmental change and the degree of environmental similarity between two
populations impact the mean fitness of a variety of hybrid crosses (e.g., F_1, F_2, backcross
to local, backcross to foreign parents) for both haploid and diploid species. We illustrate
how the degree of reproductive isolation depends on the history of adaptation, the mean
mutational size, and the cross considered. Our results emphasize how the nature of past
selection – both the direction and the speed of selection in each population – has a
substantial effect on the amount of hybrid breakdown predicted.

We also consider how the modularity of the genotype-phenotype relationship
impacts the development of reproductive isolation under mutation-order speciation.
Modularity refers to the observation that genes cluster according to which traits are
affected by genetic perturbations. Such clustering is common, for example in the
genotype-phenotype maps measured using large gene deletion collections in yeast,

nematodes, and mice (Wang *et al*. 2010). Modularity may arise when genes in the same

module are subject to similar regulatory networks or have phenotypic effects that are

spatially or temporally confined within a particular tissue or cellular component. To vary

modularity, we investigate a generalized form of Fisher's geometric model (FGM), in

which the level of pleiotropy can be tuned. The original FGM assumes that a mutation

affects all traits under consideration (i.e., universal pleiotropy; fitness landscape is a

single hypersphere). Here, we also consider a "multi-sphere model," where each mutation

affects only one module or cluster of traits (modular pleiotropy, Welch and Waxman 2003;

Chevin *et al*. 2010; Wagner and Zhang 2011; Hill and Zhang 2012; Martin 2014). Given

that we simulate a changing environment affecting the optimum in only one sphere, we

predicted that there would be a higher fraction of compatible genetic changes in

organisms with greater modularity, because the pleiotropic effects of adaptive mutations

and any compensatory mutations would be restricted to the same subset of traits. Thus,

we expected a higher degree of parallel evolution, leading to less reproductive isolation,

in cases where the environmental change affected the same module. Unexpectedly we

found a non-monotonic relationship between the extent of reproductive isolation and the

degree of modularity, which we were able to ascribe to a counteracting tendency for

mutations to arise more often in different modules, especially late in the divergence

process when there are many modules.

Finally, we explore the potential for hybrids to colonize new sites beyond the

range of the parental species. Crosses between individuals from two adapted populations

can produce a wide variety of hybrid genotypes, potentially allowing hybrids to survive

beyond the environmental conditions in which parental genotypes can survive (Albertson

and Kocher 2005). We thus explored the range of environments in which hybrids were

more likely to establish than parental individuals, potentially contributing to hybrid

speciation (i.e., without a change in ploidy: "homoploid hybrid speciation"; Rieseberg

1997).

Overall, our work explores how the nature of environmental change and the

modularity of the genetic architecture influence the development of reproductive isolation

and the potential for hybrid speciation.

Model

We first describe the fitness landscape in our model and then describe how we simulate

the evolution of reproductive isolation.

Fitness landscape

Fisher's model assumes multivariate stabilizing selection around a single optimum. We

extend this model by defining an individual's phenotype as *m* sets of *n*-dimensional

vectors, where *m* is the number of spheres and *n* is the number of traits in each sphere.

Specifically, the phenotype of an individual in the *i*th sphere is $\mathbf{z}_i = \left\{ z_{i,1}, z_{i,2}, ..., z_{i,n} \right\}$,

whose components $z_{i,j}$ are the phenotypic values for trait *j*; we denote the individual's

phenotype across all spheres as $\mathbf{Z} = \{\mathbf{z_1}, \mathbf{z_2}, ..., \mathbf{z_m}\}$.

213   The fitness component based on the set of traits described by the *i*th sphere

depends on the distance of the phenotype from the optimum $\mathbf{o}_i = \left\{ o_{i,1}, o_{i,2}, ..., o_{i,n} \right\}$,

measured as the Euclidean distance $\left\| \mathbf{z}_i - \mathbf{o}_i \right\| \equiv \sqrt{\sum_{j=1}^{n} \left(z_{i,j} - o_{i,j} \right)^2}$. Assuming that an

individual's relative fitness is calculated by considering fitness across all spheres in a

multiplicative fashion, fitness is given by:

$$w(\mathbf{Z}) = \exp(-q \sum_{i=1}^{m} \|\mathbf{z}_i - \mathbf{o}_i\|^k), \qquad \text{(Eq. 1)}$$

where *q* sets the overall strength of selection and *k* determines the curvature of the fitness

function. The parameter *k* corresponds to the degree of epistasis (Tenaillon 2014).

Throughout, we assume that fitness declines from a peak height at the optimum,

according to a Gaussian fitness surface ($k = 2$). It is worth noting that selection is assumed

independent and equally strong on all $m \times n$ traits, for a given distance to the optimum

(isotropic selection).

225   Each mutation additively shifts the phenotypic value relative to its present value.

While each mutation has an additive effect on the phenotype, the effect on fitness is not

additive but depends on the height of the fitness function for those phenotypes (Eq. 1). In

the multi-sphere model, we assume that a mutation affects one, and only one, sphere,

chosen at random. Once a sphere is chosen, the mutation affects all of the *n* traits in the

sphere under consideration, in a random direction (isotropic mutation). While the trait

axes can be defined to allow isotropy with respect to either selection or mutation

(assuming a single optimum), it is not possible to do so for both. Nevertheless, previous

work exploring a non-isotropic FGM model has shown that the isotropic FGM serves as

a good approximation, in many cases, if we consider n to be an effective number of

dimensions (Waxman and Welch 2005; Martin and Lenormand 2006).

236   For both haploids and homozygous diploids, we denote the effect of a mutation

occurring within sphere i by $\Delta \mathbf{z}_i = \left\{ \Delta z_{i,1}, \Delta z_{i,2}, ..., \Delta z_{i,n} \right\}$, with $\Delta z_{i,j}$ describing the

effect on trait j within that sphere. We assume that a mutation affects each trait within the

sphere independently, with $\Delta z_{i,j}$ proportional to a draw from a standard normal

distribution, denoted as ξ_j (Hartl and Taubes 1998; Fraïsse $et\ al.$ 2016). The total effect

size of the mutation was then set to r, drawn from an exponential distribution with mean

λ, adjusting the mutational effect on each component trait j according to $\Delta z_{i,j} =$

$r \xi_j / \sqrt{\sum_{l=1}^{n} \xi_l^2}$ (for alternative distributions, see discussion in Poon & Otto 2000). The

phenotypic value of the mutant individual was then set to $z_{i,j} + \Delta z_{i,j}$ for all traits j

within sphere i and left unchanged for traits in other modules. Denoting the resulting

mutant phenotypic vector as $\mathbf{Z} + \Delta \mathbf{Z}$, the selection coefficient of the mutation is

$s \equiv \dfrac{w(\mathbf{Z} + \Delta \mathbf{Z})}{w(\mathbf{Z})} - 1$. In diploids, the above describes the properties of homozygous

mutations. Heterozygous diploids are assumed to be shifted half as far in phenotype space,

$\Delta \mathbf{Z}/2$ (i.e., we assume additivity on a phenotypic scale). The dominance coefficient for

fitness is then defined as $h \equiv \left(\dfrac{w(\mathbf{Z} + \Delta \mathbf{Z}/2)}{w(\mathbf{Z})} - 1 \right) \Big/ s$.

Simulation methods

We consider a species that is sexually reproducing with non-overlapping generations. The

species is sub-divided into two finite populations, each comprising N hermaphrodites

with no migration between them (i.e., allopatry). Initially, these populations are

genetically identical, having just separated geographically. Genomes may be haploid or

diploid and are assumed to be large enough for each mutation to occur at a unique site,

with free recombination among sites (i.e., assuming an infinite sites model).

259   Mutations that affect fitness occur stochastically every generation, but we

assume that the mutation rate is quite low to keep the product of the rate and population

size much smaller than one. This condition allows us to assume that a population is

monomorphic most of the time (Kimura and Ohta 1969; Taylor $et\ al.$ 2006). Thus, we

consider the fate of mutations one at a time (Orr 1998; Chevin $et\ al.$ 2014). Each mutation

that arises reaches fixation within a single population with probability $\dfrac{1-\exp(-2s)}{1-\exp(-2Ns)}$

in haploids and $\dfrac{\int_0^{\frac{1}{2N}} e^{-2Ns(2h-1)x(1-x)-2Nsx}dx}{\int_0^1 e^{-2Ns(2h-1)x(1-x)-2Nsx}dx}$ in diploids (Crow and Kimura 1970). Note that

overdominance naturally arises, at least transiently, in diploid models of adaptation to a

new optimum (Sellis *et al*. 2011). We assume that the population size is small enough that

polymorphisms are sufficiently transient to be ignored, although this assumption is more

tenuous in diploids with overdominance. To simplify the simulations, we track time in

units of fixation events, where we randomly choose mutations and assign them to one or

the other population.

As the two populations accumulate mutations, they independently traverse the

fitness landscapes in the two patches. While this necessarily leads to genetic divergence,

the populations may remain similar phenotypically or may diverge initially and

subsequently converge (or vice versa), depending on the optima in the two patches. To

explore the impact of parallel versus divergent selection on reproductive isolation, we

study the following two environmental scenarios:

(1) Adaptation to a common optimum, shifted from the position of the initial population,

(to investigate mutation-order speciation).

(2) Adaptation to different optima (to investigate ecological speciation).

For each of these scenarios, we explore how the extent of reproductive isolation depends

on whether the environment shifts rapidly (in one step) or gradually (in multiple steps).

Specifically, we define the vector of optima across all spheres as $\mathbf{O}=\{\mathbf{o}_1,\mathbf{o}_2,...,\mathbf{o}_m\}$. By

assumption, the initial phenotype $\mathbf{Z}_0$ and the initial optimum, $\mathbf{O}_0$, are the same in the

two populations and set to the origin in all *m* spheres. We then allow environmental

change by shifting the optimum phenotype, which induces directional selection until the

population approaches the new optimum, at which point the population experiences

stabilizing selection. Under scenario (1), the optimum starts at $\mathbf{O}_0$ and moves to a final

optimum of $\mathbf{O}_E$, either in one step (rapid environmental change) or in τ time steps,

with each step occurring after a fixation event (gradual environmental change). Under

scenario (2), adaptation proceeds towards $\mathbf{O}_A$ in patch A and towards $\mathbf{O}_B$ in patch B,

again where the optima move either rapidly once or gradually over τ fixation events.

295   We measure the level of reproductive isolation between the two populations

through crosses, generating F_1, F_2, and backcross (BC) hybrids. To generate F_1 individuals

in the haploid case, for example, when there are x fixed mutants in patch A and y fixed

mutations in patch B, we randomly transmit each mutation to offspring with a 50%

probability, so that there are, on average, $(x+y)/2$ mutations in each hybrid. In the diploid

case, all F_1 hybrids are identical and are heterozygous for all x and y mutations. The

phenotype of a hybrid individual is then calculated as the sum of the mutational vectors,

and its fitness is assessed in both parental environments. This is repeated 1000 times for

each hybrid type. FGM simulations for adaptation and for producing hybrids were written

in C++ and *Mathematica*, respectively (to be deposited in Dryad).

305   We were also interested in the time course over which reproductive

incompatibilities developed. Whereas some models have assumed that all divergent pairs

of loci are equally likely to give rise to speciation barriers (Orr and Turelli 2001), we

speculated that large-effect mutations that accumulate during periods of rapid adaptation

to a changing environment may contribute disproportionately. For each population, we

thus accumulate an equal number of fixation events in two phases: the phase during which

adaptation occurs ("adaptation phase") and the phase during which the population moves

randomly around the optimum ("stationary phase"), with drift as well as selection

affecting the fate of a mutation. For simplicity, we define the initial adaptation phase as

the time until the first mutation fixes with a negative selection coefficient in each

population. With a moving optimum, the adaptation phase is defined as the time until the

first mutation fixed with a negative selection coefficient after the optimum stops moving,

as sometimes deleterious alleles fixed when the phenotype happens to be near the current

optimum. In addition, for modular pleiotropy, we assume that the adaptation phase

continues until the first allele with a negative selection coefficient fixes within the focal

sphere in which the optimum has moved.

321   To translate the number of fixation events into a more biologically meaningful

time scale, we calculated the expected number of generations until appearance and

fixation of the next mutation and summed this quantity across the series of mutations

fixed. Given the mutation rate u, we first calculated the waiting time until the appearance

of the next "successful" mutation that would survive stochastic loss while rare. This

waiting time was assumed to be exponentially distributed with a rate of events equal to

the mutation rate, u (set as 10^{-5} throughout this paper) multiplied by the number of

haplotypes in the population ($c\,N$, where $c = 1$ for haploids and 2 for diploids) times the

average fixation probability, P. The latter varies depending on the current distance of the

population from the optimum and was determined by integrating P over the distribution

of possible mutations for each state of the population. The mean waiting time of this

exponential distribution is $1/(cNuP)$ generations. Then, we calculated the fixation time of

the successful allele that was drawn, using the expected waiting time until fixation for a

new mutation (Ewens 2004; Otto and Day 2007). Given the selection coefficient and the

dominance coefficient of a mutation, the expected waiting time, conditional upon fixation,

is approximately (Kimura 1980):

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$$T = \int_0^1 \int_0^y \frac{2}{V(x)} e^{-2\int_x^y \frac{M(z)}{V(z)}dz} \, dx\,dy, \qquad \text{(Eq. 2)}$$

where M and V are the mean and variance of the change of mutation allele frequency p

per generation. Specifically, $M(p) = sp(1-p)$ and $V(p) = \dfrac{p(1-p)}{N}$ in haploids and

$M(p) = p(1-p)\big[sp + h(1-2p)\big]$ and $V(p) = \dfrac{p(1-p)}{2N}$ in diploids. The expected

waiting time until the next mutation appears and fixes then becomes $1/(cNuP)$ plus T.

Results

Evolutionary trajectory of adaptation

Under Fisher's geometric model (FGM), mutations have nearly a 50% chance of being

beneficial when a population starts far from the optimum relative to the effect size of the

mutation, but they are more likely to overshoot the optimum and less likely to fix once

the population approaches the optimum (Fisher 1930; Kimura 1983). As a consequence,

during the process of adaptation, the average phenotypic effect size of fixed mutations is

typically larger at first and declines as populations become increasingly adapted (Figure

2a; Orr 1998). When the distribution of mutations has a larger average magnitude, we

find that the optimum is reached faster, as expected (Figure 2c). After nearing the

optimum, populations accumulate a combination of slightly deleterious and beneficial

mutations (inset to Figure 2b), resulting in a phase of mutation-selection-drift where the

populations stochastically move around the optimum through successive fixation events.

We then accumulated the same total number of fixation events in the initial

adaptation phase and in the second stationary phase in each parental population

(allowing each parental population to accumulate a different number of fixed

mutations). This procedure ensured that we allowed enough time to pass in the

stationary phase that the level of divergence contributed by the two phases is the same

(in terms of substitutions). Table S2 gives the number of fixation events in each parental

population, the corresponding expected number of generations, and the proportion of

time in the adaptation phase. The adaptation phase was typically much faster than the

stationary phase. After the adaptation and stationary phase had finished, we performed

crosses between populations to determine how hybrid fitness depended on the nature of

environmental change, the mutation effect size, ploidy, and the modularity of pleiotropy.

In these simulations, we allowed

Adaptation to a common optimum – Figure 3 shows hybrid fitness after a period of

adaptation towards a common optimum in haploids and diploids (for an exploration of

introgression effects, see Fraïsse *et al.*, 2016), assuming that the optimum shifted in one

step (rapid environmental change). For the parameters considered, substantial intrinsic

reproductive isolation is observed in all hybrids, with the exception of diploid F_1s.

Diploid F_1s are not yet recombinant but heterozygous at all sites that differ between the

parents. When parents near the same optimum are crossed in the FGM, averaging their

phenotype in the F_1 reduces the distance to the peak and increases fitness relative to the

parents, as discussed by Barton (2001), Fraïsse *et al.* (2016), and Simon *et al.* (2018).

By contrast, all recombinant hybrids have reduced average fitness, relative to

the parents, reflecting the segregation load studied by Chevin *et al.* (2014). Importantly,

the incompatibility results primarily from the large-effect mutations that accumulate

during adaptation, which combined can generate hybrids that move far off the peak

fitness and that exhibit substantial pleiotropic side effects (Figure 1). Such

incompatibilities are not observed to any substantial degree when the optimum remains

at the origin, even with the same number of fixation events (Figure S1). That is,

reproductive isolation is not simply a function of the number of divergent alleles.

Rather, the vast majority of reproductive isolation that accumulated arose during the

first adaptation phase when large-effect mutations were likely to fix. Considering only

these mutations, F_2 hybrid fitness, for example, was reduced below the optimum by, on

average, 0.72 in haploids and 0.74 in diploids. By contrast, F_2 hybrid fitness remained

much higher, 0.99 in haploids and 0.98 in diploids, when we add the same number of

mutations that occurred only during the stationary phase to the optimum (see Table S2

for the number of fixation events in each population).

The Brownian bridge theory of Simon et al. (2018) allows us to connect the

fitness of any hybrid genotype, given the parental fitness, the hybrid index (H), the

heterozygosity of the hybrid (p_{12}), and one free parameter, which measures the extent of

hybrid breakdown. As illustrated in Figure S2 (a,b), the method of Simon et al. (2018)

works well to predict the fitness of each class of hybrids, once we fit the free parameter

by minimizing the sum of squared deviations between the observed and expected

fitnesses for the different hybrids.

During the period of adaptation, large mutations can fix, even if they shift the

phenotype substantially away from the origin in some directions, as long as the average

phenotypic distance to the optimum is shorter. In subsequent generations, these negative

pleiotropic side effects favor the fixation of compensatory mutations that move the

phenotype back toward the optimum (Figure 1). In recombinant hybrids, however, these

compensatory mutations are separated from the mutant backgrounds in which they are

favored, reducing fitness. Consequently, the fitness reduction in hybrids is more severe

when mutational effect sizes (and hence pleiotropic side effects) are larger, on average

(see Figure 4a,b with a 0° angle for populations experiencing a common optimum, with

dots from left to right representing smaller to larger average effects). It is also worth

highlighting the substantial amount of variation in reproductive isolation observed

across replicates, depending on the exact adaptive path taken, with more variability

occurring when the average mutational effect is larger (for Figure 4a, for example, the

standard deviation in the average F_1 haploid fitness among replicates rose from 7.41×10^{-3}

when $\lambda = 0.04$ to 1.26×10^{-2} when $\lambda = 0.12$).

The above simulations were repeated but allowing the optimum to move

gradually towards its final position, $\mathbf{O}_E$. With a history of slower environmental change,

large-effect mutations have a lower probability of fixation, reducing the accumulation of

negative pleiotropic side-effects. Consequently, we find that much weaker reproductive

isolation develops, with higher hybrid fitness, after a period of slow environmental

change, even when ultimately reaching the same optimum (see Figure 4c,d with a 0°

angle for populations experiencing a common optimum, with dots from left to right

representing slower to faster environmental change). We thus conclude that rapid

environmental change, resulting in the accumulation of large-effect mutations, is

particularly conducive to mutation-order speciation.

Adaptation to different optima – In the next scenario, we simulated isolated populations

adapting to different fixed optima, assessing hybrid fitness in both parental

environments. The results are qualitatively different in diploids, and now all hybrids,

including F_1 hybrids, have lower fitness within each environment, as their phenotype

falls between the optima of the two environments (extrinsic reproductive

incompatibility). The larger the angle between the two optima, the lower the the fitness

of hybrids (Figure 4). In addition, hybrid breakdown is more severe when mutational

effect sizes are larger (see sets of three adjacent points in Figure 4a,b), but the effect is

smaller than the effect of the angle between the two environments.

We next explored the sensitivity of ecological speciation to the speed of

environmental change. As observed with mutation-order speciation, greater

reproductive isolation arises when the environment changes rapidly (see sets of four

adjacent points in Figure 4c,d), but again the effect is smaller than the effect of the angle

between the two environments. Essentially, the strong extrinsic reproductive

incompatibility caused when parents are adapted to different environmental optima

masks the intrinsic incompatibilities that arise from accumulating incompatible

mutations (Figure 1). The more similar the current parental environments (the lower the

angle between them), the greater the difference in hybrid breakdown observed between

a history of slow versus rapid environmental change.

Again, the Brownian bridge theory of Simon et al. (2018) allows us to

correctly predict the fitness of any hybrid genotype, by fitting one parameter along with

the parental fitnesses, H, and p_{12} (Figure S2). The fitted parameter, a measure of the

extent of hybrid breakdown, depends on the current parental environments and is

greater when populations have been selected to more divergent optima (compare Figure

S2 panels c,d to e,f). Consistent with the conclusions drawn above, the breakdown

parameter is also greater when fit to simulation data that have allowed larger-effect

mutations to accumulate, either because the average effect of mutations is larger (as in

Figure 4a,b) or because the environmental change occurred faster (as in Figure 4c,d).

When parental population have experienced divergent selection toward

different optima, backcross hybrids to the local parent, BC_L, show much higher fitness

than backcross hybrids to the foreign parent, BC_F (Figure S3a,b), a hallmark of

ecological speciation (Rundle and Whitlock 2001). The relative performance of the

various hybrids depends, however, on the angle between the two optima (compare

Figure S3c,d with an angle of 90º to Figure S3a,b with 30º). As a measure of the

importance of ecological speciation, Rundle and Whitlock (2001) suggest calculating

the fitness of BC_L minus the fitness of BC_F, averaged over the two local environments,

as this estimates the strength of additive-by-environment interactions (AE). Indeed, AE

rises from zero when parental environments are identical to ~0.4-0.6 for environments

separated by an angle of 90º (Figure 5a,b). Across the full range of angles, however, AE

behaves non-monotonically (Figure 5a,b). For very dissimilar environments, the fitness

of the local BC_L falls to zero, severely limiting the maximum value of AE.

The degree to which ecological speciation contributes to reproductive

isolation may be better captured by measuring AE relative to the maximum value it

could take (i.e., AE divided by the fitness of BC_L). This rescaled value measures the

degree to which additive-by-environment interactions reduce the fitness of hybrids

backcrossed to the foreign parent compared to the fitness expected based on

backcrosses with the local parent. When AE/BC_L is zero, fitness is the same regardless

of which parental population is used in the backcrosses (as expected when the parental

environments are the same), whereas an AE/BC_L of one indicates that the genetic

differences between the parents reduces the fitness of backcross hybrids to zero when

raised in the foreign environment (as expected following strong divergent selection).

The rescaled measure AE/BC_L does rise monotonically with the angle between the

optima and hence the degree of divergent selection (Figure 5c,d), although sample sizes

would need to be sufficient to avoid bias caused by measurement error in the

denominator.

Impact of modularity

We next investigated the degree to which modularity of the phenotype would affect the

development of reproductive incompatibilities between adapting populations. To

investigate different degrees of modular pleiotropy, we held the total number of

phenotypic dimensions constant (the number of spheres times the number of traits per

sphere = $m \, n$) but varied the number of spheres. To simplify the presentation, we consider

only F_1 hybrids in haploid simulations. Our prediction was that we would observe less

negative pleiotropy when the phenotype was more modular, leading to less hybrid

breakdown, but this was not the case (Figure 6a). Instead, reproductive isolation showed

a non-monotonic pattern, with more hybrid breakdown in the fully pleiotropic model (m

$= 1$) and in the model with no pleiotropy ($n = 1$) than with intermediate levels of pleiotropy.

To understand this counter-intuitive result, we investigated how the genes

contributing to hybrid breakdown accumulated over time. Relatively little contribution

came from mutations accumulating during the stationary phase, so we sub-divided the

mutations accumulated during the adaptation phase into two groups: the first 50% of

mutations that fixed and the second 50% of mutations that fixed. With more modular

genetic networks (m larger; Figure 6b), mutations that fixed during the first half of

adaptation were more likely to work well together, increasing mean hybrid fitness as we

had expected. When the environmental change occurs in a module with few traits (low

n), mutations that fix in one population are more likely to point towards the optimum and

be beneficial in another population. By contrast, as the population approached the

optimum during the second half of the adaptation phase, small-effect mutations in

different modules made up an increasingly large fraction of the mutations that fixed in

different populations (recall that the stationary phase was defined to start only after a

deleterious mutation arose in the module experiencing environmental change).

Consequently, the more modules, the less likely mutations in different populations would

compensate for one another, so that decreased hybrid fitness was observed with more

modularity (Figure 6c). Thus, the role of modularity in speciation had opposite effects

during rapid early periods of adaptation, where reproductive isolation developed faster in

less modular systems, compared to later periods of relatively slow adaptation, where

reproductive isolation developed faster in more modular systems.

Homoploid hybrid speciation

As discussed above, the history of environmental change can have a strong impact on the

degree of reproductive isolation exhibited among populations. Here, we briefly explore

how this history can also impact the potential to produce hybrids that are able to colonize

new environments, leading to hybrid speciation. Specifically, we investigated the

possibility of homoploid hybrid speciation by crossing the two parental populations

generated in our simulations and measuring the fitnesses of hybrids across a range of

possible new environments. For each environment, representing a potential site for

colonization, the fitness of F_1 hybrid haploids was assessed given the optimal phenotype

in that environment, $\mathbf{O}_P$. The probability of establishment in a site, P_e, was determined

for any genotype by the branching process approximation $1 - P_e = e^{-wbP_e}$, assuming a

Poisson number of offspring with mean equal to the genotypic fitness w times the average

reproductive capacity, b, of an individual with full fitness of $w=1$ (b was set to 5 in the

simulations). We repeated this calculation for 1000 hybrids and averaged P_e to get the

expected establishment probability. We then measured the establishment probability of

hybrids relative to the average establishment probability of the two parental genotypes.

Figure 7 illustrates the colonization success of hybrid haploids versus their

parents, as a function of the phenotypic optimum in the colonized environment. Whether

hybrids are more likely to colonize a given environment depends strongly on the history

of adaptation in the parental populations. When the parental populations diverged in a

constant environment, hybrids are almost never better colonists than the parental

populations (top panels; optimum constant at zero as in Figure S1). By contrast, hybrids

are more variable following a period of adaptation to a common environment (mutation-

order speciation), and so at least some individual hybrids are able to colonize substantially

different environments than the parental populations (using parents from simulations

reported in Figure 4 with a 0º angle between environments). With ecological speciation

between parental populations adapted to different environments (> 0º angle in Figure 4),

hybrids are much better at colonizing new environments that fall between the optima of

the parental populations (bottom panels). Homozygous diploid F_2s behave similarly, but

the establishment probability of diploids in general would have to account for segregation

variance after colonization, which was not explored.

Thus, the history of the parental populations has a large influence on the fate of

hybrids and their ability to survive in and colonize new environments. Even when the

parental populations are phenotypically similar, distinct hybrids that can survive quite

different environmental conditions are more likely to be produced if the parents had

recently undergone a period of adaptation and accumulated different large effect

mutations (compare middle panels to top panels of Figure 7).

Discussion

We used a simple model of optimizing selection on multiple traits ("Fisher's geometric
model") to explore speciation in the face of environmental change. Because the path of
adaptation in Fisher's geometric model varies among populations evolving in allopatry,
genetic crosses between populations can yield mis-matched combinations of adaptive
mutations, producing hybrid offspring of lower fitness (Chevin *et al.* 2014; Fraïsse *et al.*
2016; Simon *et al.* 2018). Our main conclusion from this model is that periods of
environmental change are likely engines of speciation for allopatric populations, allowing
populations to develop strong intrinsic reproductive incompatibilities even when they are
adapting to similar environmental changes ("mutation-order speciation"; Figure 4), as
well as contributing additional intrinsic incompatibilities to the extrinsic hybrid
breakdown that occurs when parents are adapted to different environments ("ecological
speciation"; Figure 4). Reproductive incompatibilities were strongest when large-effect
mutations could accumulate, i.e., during times of rapid environmental change, which
challenges the notion that all genetic substitutions are equally likely to generate
reproductive incompatibilities.

We also explored the relative importance of mutation-order speciation versus
ecological speciation by comparing the fitness of different hybrid crosses. Rundle and
Whitlock (2001) showed that the contribution of ecological speciation could be captured
by the additive-by-environment interaction (AE), estimated from the fitness of
individuals backcrossed to the local population (BC_L) minus the fitness of individuals
backcrossed to a foreign population (BC_F). Only under ecological speciation are these
backcross fitnesses expected to differ. We find that this AE measure does indeed rise with
the angle of environmental optima between two evolving populations (measured here
relative to their ancestral origin), but only when that angle was small. With larger
environmental differences, the fitness of even the local backcrossed individuals (BC_L)
could be very low, leading AE to drop (Figure 5a,b). As a correction for this non-
monotonic behavior, we instead investigated a new measure of the importance of
ecological speciation, dividing AE by its maximum expected value (BC_L), which we
found does rise with the angle of environmental differences in our study and hence is a
better indicator of the extent of divergent selection (Figure 5c,d).

We also considered how the modularity of the genotype-phenotype relationship
impacted the development of reproductive isolation under mutation-order speciation.
With a more modular genetic architecture, allopatric populations experiencing the same

environmental change are more likely to accumulate mutations that are compatible,
because the negative pleiotropic effects of adaptive mutations are constrained within the
module affected by the environmental change. Thus, we expected a higher degree of
parallel evolution, leading to less reproductive isolation, in cases where the environment
changed in the same direction in different populations. Unexpectedly, we found a non-
monotonic relationship between the extent of reproductive isolation and the degree of
modularity (Figure 6). By separating out the first half of mutations fixed during the rapid
early phase of adaptation from the latter half of mutations fixed during the adaptation
phase, we were able to verify that reproductive isolation is less likely to develop in more
modular systems early on during adaptation when selection is strong, but this is
counteracted by a greater chance that mutations generate reproductive isolation during
later phases of adaptation as populations more slowly approach the optimum. The key
difference between these phases was whether fixed mutations tended to fix primarily in
the same module – the sphere with the shifting environment – or in different modules.
Once the populations were near the optimum, different populations tended to fix
mutations and compensatory mutations in different modules, substantially increasing the
chance of hybrid breakdown when crossed.

In addition, we explored how the history of adaptation of the parental
populations influenced the potential to produce hybrid offspring that could colonize a new
environment and lead to homoploid hybrid speciation. Because hybrids can vary in
phenotype beyond the range of parental populations, hybrids can successfully colonize
environments inaccessible to parental populations, potentially contributing to homoploid
hybrid speciation (Gross and Rieseberg 2005). Importantly, we found that hybrid
speciation was especially likely when the parental populations had undergone a period of
rapid adaptation in allopatry (Figure 7). The parents were then more likely to differ by
large-effect mutations, allowing hybrid genotypes to vary more broadly in phenotype and
producing at least some individuals that could succeed in more extreme environments.
We thus predict that periods of adaptation by the parental forms may be particularly
conducive to subsequent homoploid hybrid speciation.

In this study, we have made several simplifying assumptions that warrant more
exploration in future work. For one, we assumed that populations are largely
monomorphic, punctuated in time by the fixation of new mutations. This assumption
breaks down in larger populations (N) or in environments with a larger number of

potential mutations (higher u), either of which increases the flux of mutations into a

population. A higher flux of mutations can increase the rate at which large-effect

mutations appear, increasing the probability that intrinsic incompatibilities arise, but more

mutations also increase the standing genetic variation of the parental populations, which

can mean that the same alleles are present and fix in the parental populations when the

environment changes (Thompson *et al*. 2019). Which effect is more important depends

on the exact details, e.g., when the parental populations became isolated relative to the

change in environment. Future work is needed to explore the development of reproductive

isolation allowing for polymorphic alleles at multiple loci throughout the genome.

Relaxing the assumption of monomorphism is particularly important for diploid

populations, because large effect mutations often arise that overshoot the optimum,

leading to overdominance that maintains polymorphism (Sellis *et al*. 2011).

Our understanding of the role of rapid adaptation and the fixation of large-effect

mutations to speciation would also benefit from exploring other forms of selection

beyond the simple Fisherian geometric model considered here. With multiple optima or

other complex fitness landscapes (e.g., the "holey adaptive landscape" of Gavrilets 1997),

mutation-order speciation is thought to be even more likely, as populations may move to

different points on the fitness landscape, depending on the order in which mutations arise

(Gavrilets 2004). Nevertheless, we conjecture that the degree of reproductive isolation

may still be stronger when initially further away from the peaks of the fitness surface

because large-effect mutations may then be more likely to fix in allopatric populations,

relative to the small-effect mutations providing slight improvements in fitness near a local

optimum.

As an example of speciation across a more complex fitness landscape,

Benkman (2003) showed that the fitness surface of red crossbills feeding on cones from

different coniferous tree species displayed different peaks, associated with distinct call

types, with both ridges of relatively high fitness and deep fitness valleys. Although not

explored in this paper, the combination of fitness ridges with deep valleys might facilitate

reproductive isolation by allowing large-effect mutations that reach different points along

the ridge and that, when combined, cause hybrid phenotypes to exhibit low fitness.

Fluctuating selection could also contribute to the accumulation of large-effect

mutations and be a potent driver of speciation (see, e.g, Barton 2001; Chevin *et al*. 2014;

Fraïsse *et al*. 2016). For example, beak phenotypes of the medium ground finch *Geospiza*

fortis on Galapagos have experienced selection that fluctuates between life stages, years

and generations (Price and Grant 1984; Grant and Grant 2008). Stabilizing selection with

a fluctuating optimum allows the population to accumulate relatively large mutations,

which contribute disproportionately to the accumulation of reproductive isolation.

In conclusion, our work shows that the tempo of speciation does not tick at a

steady rate. Rather, reproductive isolation between allopatric populations should rise

faster after bouts of rapid environmental change. A rapidly changing environment is

particularly important when selection acts in parallel among populations (mutation-order

speciation), as extrinsic reproductive incompatibilities are lacking. In our simulations,

crossing the few large-effect mutations that arose during bouts of rapid adaptation caused

more hybrid breakdown than combining many small-effect mutations, whose effects

tended to cancel (Figure 1; see also eq. 3 in Chevin *et al*. 2014). These results help explain

the surprisingly rapid appearance of genetic incompatibilities during short-term

experimental evolution studies in the lab (e.g., Dettman *et al*. 2007, 2008; Kvitek and

Sherlock 2011; Chou *et al*. 2014; Ono *et al*. 2017). Periods of strong selection are

unusually powerful drivers of speciation, helping to account for why reproductive

isolation arises so rapidly in experimental evolution studies and yet the biological world

has not diversified into an infinite variety of species.

Author contributions

RY and SPO designed the study; RY developed the computer simulation code and conducted analyses in consultation with SPO; RY and SPO wrote the manuscript.

Data accessibility

All code necessary to repeat the analysis described in this study have been made available. C++ source codes of our simulation models for adaptation process, *Mathematica* (version 11.2.0.0) codes for calculating hybrids genotypes and fitnesses, R (version 3.5.1) scripts that we used to produce figures, and simulation results in this paper will be available from the Dryad Digital Repository. For now, these are hosted on Github (https://github.com/ryamaguchi0731/FGM-master).

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Table 1. Notation used. Default values are given in square brackets, except where noted

in the text.

Notation	Description
m	Number of spheres [1]
n	Number of traits in each sphere [10]
$\mathbf{z}_i = \left\{ z_{i,1}, z_{i,2}, ..., z_{i,n} \right\}$	Phenotype in the ith sphere
$\mathbf{o}_i = \left\{ o_{i,1}, o_{i,2}, ..., o_{i,n} \right\}$	Optimum phenotype in the ith sphere
$w\left(\mathbf{z}_1, \mathbf{z}_2, ..., \mathbf{z}_m \right)$	Individual's relative fitness
q	Parameter translating the phenotypic distance from the optimum into the strength of selection [1]
k	Degree of epistasis [2]
$\mathbf{Z} = \left\{ \mathbf{z}_1, \mathbf{z}_2, ..., \mathbf{z}_m \right\}$	Vector of phenotype sets of all spheres. $\mathbf{Z}_I$ is an initial condition
r	Mutation size, drawn from an exponential distribution with mean λ
ξ_j	Random number drawn from a standard normal distribution
$\Delta\mathbf{z}_i = \left\{ \Delta z_{i,1}, \Delta z_{i,2}, ..., \Delta z_{i,n} \right\}$	Phenotypic change due to mutation in the ith sphere
$\Delta\mathbf{Z} = \left\{ \Delta\mathbf{z}_1, \Delta\mathbf{z}_2, ..., \Delta\mathbf{z}_m \right\}$	Vector of mutational effects across all spheres
s	Selection coefficient
h	Measure of dominance
N	Number of individuals in a population [2000]
c	Ploidy level [1 for haploids, 2 for diploids]
u	Mutation rate [10^{-5}]
b	Number of offspring per individual of maximum fitness when calculating establishment probability [5]
$\mathbf{O} = \left\{ \mathbf{o}_1, \mathbf{o}_2, ..., \mathbf{o}_m \right\}$	Vector describing the optimal phenotype across all sets of spheres

816   Table S1. The location of the environmental optima.

Angle between two optima	Population 1	Population 2	Distance from Z_0 to O
0º	{2,0,0,0,0,0,0,0,0,0}	{2,0,0,0,0,0,0,0,0,0}	2
30º	$\{-\sqrt{2-\sqrt{3}}, -\sqrt{2+\sqrt{3}},$ 0,0,0,0,0,0,0,0\}	$\{\sqrt{2-\sqrt{3}}, -\sqrt{2+\sqrt{3}},$ 0,0,0,0,0,0,0,0\}	2
45º	$\{-\sqrt{2-\sqrt{2}}, -\sqrt{2+\sqrt{2}},$ 0,0,0,0,0,0,0,0\}	$\{\sqrt{2-\sqrt{2}}, -\sqrt{2+\sqrt{2}},$ 0,0,0,0,0,0,0,0\}	2
90º	$\{-\sqrt{2}, -\sqrt{2},$ 0,0,0,0,0,0,0,0\}	$\{\sqrt{2}, -\sqrt{2},$ 0,0,0,0,0,0,0,0\}	2
180º	{-2,0,0,0,0,0,0,0,0,0}	{2,0,0,0,0,0,0,0,0,0}	2

Vector angle is defined as $\mathrm{Arccos}\left[\dfrac{a \cdot b}{\|a\|\,\|b\|}\right]$ where a and b are different vectors.

Table S2. Number of fixation events tracked within the parental populations P_1 and P_2
and the corresponding number of generations, based on the expected waiting time until
fixation. In each population, we tracked the same total number of fixations events during
the adaptation phase and the stationary phase (e.g., 92 for P_1 and 88 for P_2 in each phase
for the first set of simulations).

Figure number & Population		Total fixations	Number of generations	% of time in adaptation phase
Figure 3a, 7a-f, S1a, S2a (Haploid)	P_1	184	2.31×10^7	8.32
	P_2	176	1.86×10^7	3.89
Figure 3b, S1b, S2b (Diploid)	P_1	204	6.73×10^7	4.99
	P_2	184	5.72×10^7	2.75
Figure 3c (Haploid)	P_1	68	2.62×10^7	6.59
	P_2	76	2.81×10^7	8.44
Figure 3d (Diploid)	P_1	124	1.19×10^8	3.29
	P_2	122	1.65×10^8	4.52
Figure 4a,c, 5 a,c, S2a (Haploid, $\lambda = 0.04$)	P_1	159.52 ± 2.95	$1.85\times10^7 \pm 6.14\times10^5$	5.94 ± 0.38
	P_2	153.12 ± 4.45	$1.74\times10^7 \pm 7.54\times10^5$	7.15 ± 1.12
Figure 4a (Haploid, $\lambda = 0.08$)	P_1	99.20 ± 1.98	$1.94\times10^7 \pm 6.17\times10^5$	5.99 ± 0.41
	P_2	98.44 ± 2.38	$1.86\times10^7 \pm 8.81\times10^5$	6.21 ± 0.46
Figure 4a (Haploid, $\lambda = 0.12$)	P_1	83.44 ± 1.87	$2.25\times10^7 \pm 8.37\times10^5$	5.79 ± 0.43
	P_2	83.40 ± 1.44	$2.36\times10^7 \pm 6.63\times10^5$	7.03 ± 0.48
Figure 4b,d, 5b,d, S2b (Diploid, $\lambda = 0.04$)	P_1	183.04 ± 2.93	$5.69\times10^7 \pm 1.73\times10^6$	3.86 ± 0.25
	P_2	181.48 ± 4.79	$5.36\times10^7 \pm 2.73\times10^6$	5.55 ± 1.01
Figure 4b (Diploid, $\lambda = 0.08$)	P_1	133.08 ± 2.99	$1.11\times10^8 \pm 8.62\times10^6$	6.07 ± 1.97
	P_2	128.60 ± 4.91	$1.06\times10^8 \pm 5.79\times10^6$	6.40 ± 2.12
Figure 4b (Diploid, $\lambda = 0.12$)	P_1	111.88 ± 2.31	$1.26\times10^8 \pm 1.28\times10^6$	5.68 ± 1.99
	P_2	112.56 ± 1.61	$1.30\times10^8 \pm 3.71\times10^6$	5.97 ± 1.98
Figure 4c (Haploid, slow)	P_1	222.36 ± 1.88	$3.05\times10^7 \pm 4.08\times10^5$	17.8 ± 0.51
	P_2	216.20 ± 1.68	$2.97\times10^7 \pm 4.41\times10^5$	17.4 ± 0.48

Figure 4c	P_1	166.32 ± 2.67	$2.02 \times 10^7 \pm 4.94 \times 10^5$	9.46 ± 0.27
(Haploid, medium)	P_2	166.12 ± 2.05	$2.02 \times 10^7 \pm 4.40 \times 10^5$	9.87 ± 0.33
Figure 4c	P_1	155.24 ± 3.52	$1.79 \times 10^7 \pm 6.42 \times 10^5$	7.64 ± 1.31
(Haploid, fast)	P_2	158.22 ± 3.23	$1.78 \times 10^7 \pm 6.32 \times 10^5$	6.34 ± 0.31
Figure 4d	P_1	215.12 ± 1.82	$8.02 \times 10^7 \pm 1.05 \times 10^6$	18.1 ± 0.70
(Diploid, slow)	P_2	216.64 ± 1.78	$8.11 \times 10^7 \pm 1.16 \times 10^6$	17.0 ± 0.67
Figure 4d	P_1	180.04 ± 3.08	$5.83 \times 10^7 \pm 1.87 \times 10^6$	8.06 ± 0.29
(Diploid, medium)	P_2	170.12 ± 2.88	$5.41 \times 10^7 \pm 1.61 \times 10^6$	7.91 ± 0.34
Figure 4d	P_1	177.68 ± 4.70	$5.47 \times 10^7 \pm 2.38 \times 10^6$	7.52 ± 1.74
(Diploid, fast)	P_2	177.88 ± 4.11	$5.66 \times 10^7 \pm 2.34 \times 10^6$	6.69 ± 1.12
Figure 4a,c, 5a,c, S2c	P_1	154.24 ± 3.84	$1.71 \times 10^7 \pm 7.37 \times 10^5$	5.83 ± 0.64
(Haploid, 30°,	P_2	158.28 ± 3.48	$1.78 \times 10^7 \pm 6.54 \times 10^5$	5.90 ± 0.40
$\lambda = 0.04$)				
Figure 4a	P_1	101.36 ± 1.70	$1.92 \times 10^7 \pm 5.28 \times 10^5$	5.46 ± 0.41
(Haploid, 30°,	P_2	100.36 ± 2.75	$1.91 \times 10^7 \pm 7.88 \times 10^5$	6.30 ± 0.85
$\lambda = 0.08$)				
Figure 4a	P_1	80.28 ± 1.52	$2.24 \times 10^7 \pm 6.07 \times 10^5$	7.36 ± 0.51
(Haploid, 30°,	P_2	82.48 ± 1.70	$2.19 \times 10^7 \pm 7.84 \times 10^5$	6.29 ± 0.63
$\lambda = 0.12$)				
Figure 4a,c, 5a,c	P_1	155.20 ± 2.81	$1.78 \times 10^7 \pm 5.35 \times 10^5$	5.48 ± 0.33
(Haploid, 45°,	P_2	153.26 ± 3.85	$1.77 \times 10^7 \pm 6.03 \times 10^5$	6.70 ± 0.88
$\lambda = 0.04$)				
Figure 4a	P_1	103.24 ± 2.21	$2.06 \times 10^7 \pm 7.01 \times 10^5$	6.15 ± 0.42
(Haploid, 45°,	P_2	106.96 ± 2.31	$2.14 \times 10^7 \pm 6.42 \times 10^5$	6.61 ± 0.47
$\lambda = 0.08$)				
Figure 4a	P_1	81.72 ± 1.84	$2.26 \times 10^7 \pm 8.27 \times 10^5$	6.77 ± 0.48
(Haploid, 45°,	P_2	85.20 ± 1.78	$2.46 \times 10^7 \pm 7.65 \times 10^5$	7.93 ± 0.58
$\lambda = 0.12$)				
Figure 4a,c, 5a,c, S2e,	P_1	156.88 ± 2.45	$1.80 \times 10^7 \pm 4.57 \times 10^5$	6.05 ± 0.36
7g-i	P_2	149.96 ± 3.17	$1.66 \times 10^7 \pm 6.31 \times 10^5$	5.10 ± 0.26
(Haploid, 90°,				
$\lambda = 0.04$)				

Figure 4a (Haploid, 90°, $\lambda = 0.08$)	P_1	101.60 ± 2.10	$1.99\times10^7 \pm 6.31\times10^5$	6.75 ± 0.39
	P_2	101.44 ± 2.68	$1.99\times10^7 \pm 8.18\times10^5$	7.24 ± 0.63
Figure 4a (Haploid, 90°, $\lambda = 0.12$)	P_1	83.52 ± 1.76	$2.38\times10^7 \pm 8.53\times10^5$	7.97 ± 0.59
	P_2	81.64 ± 1.76	$2.29\times10^7 \pm 7.79\times10^5$	7.05 ± 0.50
Figure 4b,d, 5b,d, S2d (Diploid, 30°, $\lambda = 0.04$)	P_1	189.32 ± 2.88	$6.02\times10^7 \pm 1.57\times10^6$	4.70 ± 0.30
	P_2	175.08 ± 5.62	$5.40\times10^7 \pm 2.53\times10^6$	6.67 ± 1.58
Figure 4b (Diploid, 30°, $\lambda = 0.08$)	P_1	134.12 ± 2.56	$1.14\times10^8 \pm 3.81\times10^6$	4.09 ± 0.73
	P_2	133.56 ± 2.30	$1.24\times10^8 \pm 3.42\times10^6$	3.45 ± 0.44
Figure 4b (Diploid, 30°, $\lambda = 0.12$)	P_1	111.92 ± 2.19	$1.29\times10^8 \pm 4.47\times10^6$	3.65 ± 0.93
	P_2	109.80 ± 2.25	$1.23\times10^8 \pm 4.31\times10^6$	4.79 ± 0.79
Figure 4b,d, 5b,d (Diploid, 45°, $\lambda = 0.04$)	P_1	188.16 ± 4.86	$5.90\times10^7 \pm 2.23\times10^6$	5.34 ± 0.82
	P_2	185.28 ± 3.94	$5.78\times10^7 \pm 1.79\times10^6$	5.05 ± 1.01
Figure 4b (Diploid, 45°, $\lambda = 0.08$)	P_1	138.08 ± 2.61	$1.19\times10^8 \pm 3.99\times10^6$	3.84 ± 0.40
	P_2	138.28 ± 2.31	$1.20\times10^8 \pm 3.45\times10^6$	4.31 ± 0.45
Figure 4b (Diploid, 45°, $\lambda = 0.12$)	P_1	110.88 ± 2.75	$1.22\times10^8 \pm 5.33\times10^6$	3.49 ± 0.71
	P_2	115.72 ± 1.60	$1.31\times10^8 \pm 4.04\times10^6$	3.13 ± 0.49
Figure 4b,d, 5b,d, S2f (Diploid, 90°, $\lambda = 0.04$)	P_1	186.06 ± 3.25	$5.82\times10^7 \pm 1.75\times10^6$	3.92 ± 0.26
	P_2	190.88 ± 3.69	$5.80\times10^7 \pm 1.99\times10^6$	4.08 ± 0.25
Figure 4b (Diploid, 90°, $\lambda = 0.08$)	P_1	133.56 ± 2.68	$1.15\times10^8 \pm 4.08\times10^6$	3.79 ± 0.47
	P_2	138.88 ± 3.16	$1.15\times10^8 \pm 4.30\times10^6$	4.73 ± 0.88
Figure 4b (Diploid, 90°,	P_1	116.92 ± 1.83	$1.38\times10^8 \pm 4.19\times10^6$	3.84 ± 0.45
	P_2	112.16 ± 1.87	$1.27\times10^8 \pm 4.25\times10^6$	3.55 ± 0.55

$\lambda = 0.12$)

Figure 4c (Haploid, 30º, slow)	P_1	218.76 ± 1.22	$3.28\times10^7 \pm 3.47\times10^5$	19.88 ± 4.58
	P_2	213.56 ± 1.12	$2.92\times10^7 \pm 2.47\times10^5$	11.52 ± 1.55
Figure 4c (Haploid, 30º, medium)	P_1	165.96 ± 2.20	$2.21\times10^7 \pm 4.62\times10^5$	10.70 ± 2.17
	P_2	166.48 ± 2.01	$2.18\times10^7 \pm 4.33\times10^5$	9.94 ± 2.43
Figure 4c (Haploid, 30º, fast)	P_1	162.68 ± 1.90	$2.08\times10^7 \pm 4.23\times10^5$	7.86 ± 2.67
	P_2	154.52 ± 2.41	$1.96\times10^7 \pm 5.02\times10^5$	8.29 ± 3.52
Figure 4c (Haploid, 45º, slow)	P_1	219.16 ± 1.30	$3.37\times10^7 \pm 3.69\times10^5$	20.86 ± 4.49
	P_2	215.68 ± 1.31	$2.89\times10^7 \pm 2.36\times10^5$	10.43 ± 1.82
Figure 4c (Haploid, 45º, medium)	P_1	166.24 ± 2.06	$2.18\times10^7 \pm 4.85\times10^5$	11.63 ± 2.84
	P_2	164.88 ± 2.18	$2.17\times10^7 \pm 5.18\times10^5$	10.56 ± 5.83
Figure 4c (Haploid, 45º, fast)	P_1	160.44 ± 2.06	$2.05\times10^7 \pm 3.97\times10^5$	7.96 ± 2.29
	P_2	155.24 ± 2.19	$1.93\times10^7 \pm 4.86\times10^5$	7.19 ± 2.77
Figure 4c (Haploid, 90º, slow)	P_1	217.48 ± 1.25	$3.27\times10^7 \pm 2.78\times10^5$	20.33 ± 4.91
	P_2	215.72 ± 1.13	$2.87\times10^7 \pm 2.71\times10^5$	8.57 ± 2.03
Figure 4c (Haploid, 90º, medium)	P_1	164.92 ± 1.55	$2.17\times10^7 \pm 3.59\times10^5$	10.60 ± 1.82
	P_2	168.68 ± 2.08	$2.15\times10^7 \pm 4.43\times10^5$	8.25 ± 2.00
Figure 4c (Haploid, 90º, fast)	P_1	156.08 ± 2.25	$1.93\times10^7 \pm 5.06\times10^5$	8.95 ± 8.51
	P_2	160.44 ± 2.69	$2.00\times10^7 \pm 5.46\times10^5$	7.51 ± 2.76
Figure 4d (Diploid, 30º, slow)	P_1	214.32 ± 1.14	$8.01\times10^7 \pm 7.08\times10^5$	18.43 ± 4.68
	P_2	217.00 ± 1.21	$8.05\times10^7 \pm 7.60\times10^5$	17.45 ± 4.15
Figure 4d (Diploid, 30º, medium)	P_1	173.20 ± 1.80	$5.61\times10^7 \pm 1.08\times10^6$	8.00 ± 2.11
	P_2	174.92 ± 1.88	$5.61\times10^7 \pm 1.10\times10^6$	7.89 ± 1.81
Figure 4d (Diploid, 30º, fast)	P_1	175.84 ± 2.65	$5.39\times10^7 \pm 1.42\times10^6$	6.64 ± 8.76
	P_2	184.92 ± 2.05	$5.75\times10^7 \pm 1.00\times10^6$	5.46 ± 2.01
Figure 4d (Diploid, 45º, slow)	P_1	213.16 ± 1.27	$7.98\times10^7 \pm 9.08\times10^5$	18.76 ± 4.32
	P_2	215.08 ± 1.24	$8.00\times10^7 \pm 8.54\times10^5$	17.63 ± 4.79

Figure 4d	P_1	169.32 ± 1.79	$5.42 \times 10^7 \pm 1.08 \times 10^6$	8.12 ± 2.11
(Diploid, 45°, medium)	P_2	168.36 ± 2.40	$5.26 \times 10^7 \pm 1.33 \times 10^6$	8.90 ± 2.37
Figure 4d	P_1	167.56 ± 3.52	$5.02 \times 10^7 \pm 1.93 \times 10^6$	7.25 ± 10.39
(Diploid, 45°, fast)	P_2	178.92 ± 2.40	$5.54 \times 10^7 \pm 1.41 \times 10^6$	5.26 ± 1.84
Figure 4d	P_1	215.20 ± 1.19	$8.08 \times 10^7 \pm 6.94 \times 10^5$	18.93 ± 4.75
(Diploid, 90°, slow)	P_2	216.56 ± 1.29	$8.02 \times 10^7 \pm 8.52 \times 10^5$	17.45 ± 4.31
Figure 4d	P_1	169.60 ± 2.03	$5.68 \times 10^7 \pm 1.02 \times 10^6$	8.84 ± 2.29
(Diploid, 90°, medium)	P_2	171.76 ± 2.39	$5.34 \times 10^7 \pm 1.48 \times 10^6$	9.06 ± 4.76
Figure 4d	P_1	173.12 ± 2.66	$5.28 \times 10^7 \pm 1.59 \times 10^6$	6.55 ± 2.92
(Diploid, 90°, fast)	P_2	182.48 ± 2.40	$5.77 \times 10^7 \pm 1.42 \times 10^6$	5.71 ± 2.75
Figure 5a,c	P_1	147.32 ± 3.41	$1.75 \times 10^7 \pm 5.24 \times 10^5$	6.00 ± 0.83
(Haploid, 180°)	P_2	151.13 ± 4.42	$1.78 \times 10^7 \pm 6.19 \times 10^5$	7.02 ± 1.06
Figure 5b,d	P_1	187.72 ± 3.91	$5.81 \times 10^7 \pm 2.76 \times 10^6$	4.68 ± 0.98
(Diploid, 180°)	P_2	182.84 ± 3.80	$5.33 \times 10^7 \pm 1.62 \times 10^6$	4.19 ± 0.37
Figure 6	P_1	168.17 ± 4.56	$1.67 \times 10^7 \pm 2.99 \times 10^5$	9.81 ± 3.48
(1, 10)	P_2	166.64 ± 3.07	$1.77 \times 10^7 \pm 5.15 \times 10^5$	4.40 ± 1.74
Figure 6	P_1	133.56 ± 3.47	$2.97 \times 10^7 \pm 1.59 \times 10^6$	26.44 ± 1.42
(2, 5)	P_2	128.76 ± 3.06	$2.73 \times 10^7 \pm 1.15 \times 10^6$	25.09 ± 1.05
Figure 6	P_1	119.88 ± 5.84	$3.33 \times 10^7 \pm 2.54 \times 10^6$	43.17 ± 0.99
(5, 2)	P_2	114.92 ± 5.11	$3.04 \times 10^7 \pm 1.81 \times 10^6$	43.47 ± 1.05
Figure 6	P_1	138.36 ± 8.12	$4.09 \times 10^7 \pm 2.81 \times 10^6$	47.76 ± 0.90
(10, 1)	P_2	133.84 ± 8.35	$4.64 \times 10^7 \pm 5.36 \times 10^6$	46.31 ± 1.44
Figure S2c, S3a	P_1	122	1.24×10^7	2.84
(Haploid)	P_2	138	1.52×10^7	3.44
Figure S2d, S3b	P_1	166	4.26×10^7	1.80
(Diploid)	P_2	196	5.64×10^7	4.77
Figure S2e, S3c	P_1	144	1.19×10^7	2.59
(Haploid)	P_2	168	2.02×10^7	4.07
Figure S2f, S3d	P_1	188	5.23×10^7	2.98
(Diploid)	P_2	202	6.14×10^7	4.45

(a)　(b)

Figure 1: Conceptual figure illustrating why rapid environmental change is more likely
to lead to reproductive isolation. Both panels show a two-dimensional phenotype with a
new optimum at the center of the sphere, illustrating the adaptive paths taken by two
populations (red and white). In (a), the environment shifted rapidly and favored large-
effect mutations; in (b), the environment shifted slowly and favored small-effect
mutations. Rapid environmental change (a) is more likely to generate genetic
incompatibilities that reduce hybrid fitness because combining large-effect mutations can
shift the offspring off of the fitness peak and because such mutations can have substantial
negative pleiotropic effects, here measured as displacements along the y-axis (see dashed
black arrow for one example hybrid combination). By contrast, slow environmental
change (b) is more likely to lead to many small-effect mutations, which when combined
create hybrids whose phenotypes remain near the peak.

Figure 2. Trajectories within haploid simulations of (a) phenotypic effect size among fixed mutations, (b) selection coefficient, (c) distance to the optimum, and (d) time in units of generations versus the number of fixation events. Blue, red, and black represent maximum, minimum, and mean, respectively. Selection coefficients are positive in the first "adaptation phase" (taking, on average, 86.9 fixation events) but are more often negative in the second "stationary phase" (inset to b). In (c), mutations are drawn from an exponential distribution with $\lambda = 0.04$ (right solid line), 0.08 (center dashed line), and 0.12 (left dashed-dotted line). All other panels set $\lambda = 0.04$. 100 simulations were run for each parameter set. The other parameters are $m=1$, $n=10$, $N=2000$, $q=1$ and $k=2$.

Figure 3. Mutation-order speciation and fitness of hybrids in (a, c) haploids and (b, d) diploids. We arbitrarily consider population 1 to be the "local" population used as the backcross parent, BC_L (backcross results using the "foreign" population 2, BC_F, are similar). The phenotypic optimum was displaced from the origin along the x-axis by 2 units, after which the appearance and fixation of mutations was tracked for a total of (a) 360, (b) 388, (c) 144, (d) 246 substitutions (see Table S2). The majority of fitness loss accumulates during the first adaptation phase (open circles). Top panels show $\lambda = 0.04$ and bottom $\lambda = 0.12$. Parameters: $m=1$, $n=10$, $N=2000$, $q=1.0$, $k = 2.0$, with distributions and solid points representing the mean $\pm$SD calculated from one simulation. 1000 individuals were generated for each hybrid type.

Figure 4. Stronger reproductive isolation arises via ecological speciation when populations are selected in more divergent directions, with more isolation arising when mutations have a larger average effect size (top panels) and the environment changes rapidly (bottom panels) in haploids (a, c) and diploids (b, d). For top panels, mutations are drawn from an exponential distribution with $\lambda = 0.04$, 0.08, and 0.12 (three adjacent points from left to right). Grey points show the fitness of the parental genotypes. For bottom panels, the optimum is gradually moved from the origin in one trait dimension over $\tau = 100$ (slow), 50 (medium), 20 (fast) or 0 (immediate) fixation events until the new optimum is reached (four adjacent points from left to right), assuming $\lambda = 0.04$. The x-axis gives the angle between the optima $\mathbf{O}_A$ in patch A and $\mathbf{O}_B$ in patch B relative to the ancestral optimum $\mathbf{O}_0$ (as illustrated on the right bottom). All other parameters are as in Figure 3 except that this figure is calculated from 50 simulations.

Figure 5. Estimating the degree of ecologically-dependent reproductive isolation. Top

panels give $BC_L - BC_F$ for (a) haploids and (b) diploids, as a function of the angle between

the optima toward which the parental populations were evolving. Bottom panels give

$(BC_L - BC_F)/BC_L$ for (c) haploids and (d) diploids. While $BC_L - BC_F$ shows a non-

monotonic relationship, $(BC_L - BC_F)/BC_L$ rises monotonically with the degree of

ecological difference between the two environments. Mutations are drawn from an

exponential distribution with $\lambda = 0.04$. All other parameters are as in Figure 3, with

distributions and solid points representing the mean $\pm$ SE calculated from 50 simulations.

Figure 6. Effect of modularity on the accumulation of reproductive isolation in haploid

F_1 hybrids. Panel (a) includes all mutations fixed, while (b) includes only the first 50%

of mutations fixed during the adaptation phase and (c) includes only the second 50% of

mutations fixed during the adaptation phase; panel (d) includes only mutations fixed

during the stationary phase. In each case, the phenotypic effects were added to parents

whose phenotypes were at the origin. All other parameters are as in Figure 3 with

$\lambda = 0.04$, except that this figure changes the number of spheres along the x-axis (from

1 on left to 10 on right) and is calculated from 50 simulations.

Figure 7. Establishment probability of haploid hybrids relative to parents when

colonizing a new environment. The optimal phenotype in the new environment is varied

along two dimensions (x and y axes), holding the optimum at zero for all other

phenotypic dimensions (n=10). Left panels show the establishment probability in each

environment for the best of the two parental genotypes (red dots). Middle panels show

the establishment probability of F_1 recombinant hybrids (black dots). Shading indicates

establishment probability, from low (blue) to high (orange), as indicated at top. Right

panels show the colonization success of hybrids relative to the parents, where the degree

of orange indicates the amount by which hybrids have a mean establishment probability

greater than the mean of the two parents (fixation probabilities $<10^{-6}$ were set to 10^{-6} to

avoid division by small numbers). The potential for hybrid speciation depends strongly

on the history of the parental populations: (a-c) diverged in a constant environment

(parents from Figure S1a), (d-f) diverged through parallel adaptation to a new optimum

at 2 along the x-axis (mutation-order speciation, parents from Figure 3a), (g-i) diverged

through adaptation to different environments (ecological speciation with an angle

901 between the two optima of 90º, parents from Figure S3c). All other parameters are as in

902 Figure 3, with $b = 5$ and $\lambda = 0.04$.

903   Figure S1. Little reproductive isolation arises during mutation-order speciation during

904   the stationary phase in (a) haploids or (b) diploids. Note that the y-axis range does not

905   start at 0. Data based on the mutations accumulated in Figure 3 (see Table S2 for the

906   number of events). All other parameters are as in Figure 3 with $\lambda = 0.04$.

Figure S2. The fitness of hybrids can be predicted using the Brownian bridge approximation of Simon *et al.* (2018). Left and right panel represent haploid and diploid simulations respectively. Top panels show hybrid fitnesses following mutation-order speciation in the same parental environments (as in Figure 3a,b). Remaining panels show hybrid fitnesses following ecological speciation in populations adapting to optima that differ by 30° (middle panels as in Figure S3a,b) or 90° (bottom panels; as in Figure S3c,d). The dots represent data generated data in the current paper. The dashed line is predicted by fitting the free parameter $E(S_\dagger)$ of Simon *et al.* (2018) by minimizing the sum of squared deviations between the observed and predicted fitnesses. Three different colors represent three different simulation runs. Choosing $E(S_\dagger)$ based on the class of hybrid with the lowest fitness, as suggested by Simon et al. (2018), does not always provide a good fit, especially when the parents differ in fitness, but fitting the $E(S_\dagger)$ parameter provides a robust predictor to the full set of hybrid fitnesses.

Figure S3. Ecological speciation and the fitness of hybrids in (a, c) haploids and (b, d)

diploids. We illustrate the case where the "local" environment is that of population 1

(P_1), using $\lambda = 0.04$. The angle between the optima of the two environments is set to

30° in top panels and 90° in bottom panels, relative to the origin (see Table S1 for

details). All other parameters are as in Figure 3, with distributions and solid points

representing the mean $\pm$ SD calculated from one simulation. 1000 individuals were

generated for each hybrid type.