bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

PSX: Protein-Solvent Exchange - Software for calculation of deuterium-exchange effects in SANS measurements from protein coordinates

Martin Cramer Pedersen,[a]* Yong Wang,[b] Frederik Grønbæk Tidemand,[a] Anne Martel,[c] Kresten Lindorff-Larsen[b] and Lise Arleth[a]

[a]*Niels Bohr Institute, University of Copenhagen, Denmark,* [b]*Linderstrøm-Lang Centre for Protein Science, Department of Biology, University of Copenhagen, Denmark, and* [c]*Large Scale Structures Group, Institut Laue-Langevin, France.*

E-mail: mcpe@nbi.ku.dk

hydrogen/deuterium exchange; small-angle neutron scattering; biophysical samples; solvent exposure; bioinformatics

Abstract

Recent developments in neutron scattering instrumentation and sample handling have enabled studies of more complex biological samples and measurements at shorter exposure times. To extract most information from such experiments it is thus desirable to determine accurate estimates of deuteration levels. We introduce and document software for exploring the effect of hydrogen-deuterium exchange for proteins solubilized in D_2O as well as the underlying bioinformatical models. The software aims to be generally applicable for any atomistic structure of a protein and its surrounding environment, and thus captures effects of both heterogenous exchange rates throughout

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

the protein structure and by varying the experimental conditions such as pH and temperature. The paper concludes with examples of applications and estimates of the effect in typical scenarios emerging in small-angle neutron scattering on biological macromolecules in solution. We find that the common assumption of 90% exchange is in many cases a strong overestimate with the rapid sample handling systems currently available. Source code for the presented software is available from an online repository in which it is published under version 3 of the GNU publishing license.

1. Introduction

Small-angle neutron scattering (SANS) experiments are emerging as a powerful source of information about the structure and dynamical properties of macromolecules such as proteins. In order to extract as much information as possible from such experiments during, for example, model refinement, it is often necessary to provide external information such as scattering lengths, molecular volumes, and similar physical parameters. SANS experiments are often carried out using either D_2O or H_2O/D_2O mixtures providing opportunities for varying contrast between different parts of the sample, due to the stark difference in scattering properties between protons and deuterons. When a protonated protein is exposed to D_2O, a number of protons in the protein will exchange with the deuterons in the solvent over a timescale that may be comparable to that of the experiment. Thus, for samples and experiments such as these, this exchange of protons must be accounted for in order to refine accurate models of the samples in question .

These considerations become increasingly relevant for proteins with domains shielded from the solvent such as e.g. a membrane protein in a phospholipid bilayer nanodisc (Kynde *et al.*, 2014; Johansen *et al.*, 2018) or detergent micelle (Midtgaard *et al.*, 2018). The recent developments of so-called "invisible" carrier systems that

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

match the scattering properties of the associated solvent, have been used for solubilizing membrane proteins for solution SANS experiments; in particular the so-called match-out deuterated detergent micelles (Midtgaard *et al.*, 2018) or stealth nanodiscs (Maric *et al.*, 2014; Josts *et al.*, 2018), add further relevance to the considerations.

On a similar note, in-line size exclusion chromatography (SEC) for BioSANS has recently emerged as a promising technique for investigating particularly complicated and fragile biological samples of interest (Jordan *et al.*, 2016; Johansen *et al.*, 2018). When employing this technique, samples are exposed to the solvent, in many cases D_2O, only minutes before being irradiated by the neutron beam, meaning that the exchange process is far from equilibrium.

In this paper, we present an approach to and software for more accurately estimating the hydrogen-to-deuterium exchange (also commonly known as protium-deuterium exchange) in a protein structure as a function of the time in which the protein has been exposed to D_2O using a well established model from the world of structural bioinformatics. The software focuses on the exchange of the backbone hydrogens, as these are the most relevant exchanges in the context of neutron scattering experiments (Figure 1). Specifically, we divide hydrogens into three groups: (1) non-exchanging, carbon-bound hydrogens, (2) slowly-exchanging backbone hydrogens that exchange with the solvent at timescales relevant for neutron scattering experiments on biological samples, and (3) the remaining rapidly-exchanging side chain hydrogens.

Some existing software packages such as CRYSON (Svergun *et al.*, 1998) and ISIS' Biomolecular Scattering Length Density Calculator (ISIS, 2019) assume a homogeneous deuteration level throughout the molecule (defaulting to 90% of the backbone hydrogens and 100% of the rapidly-exchanging hydrogens in CRYSON and 90% of the rapidly exchanging hydrogens plus the backbone hydrogens in ISIS' Biomolecular

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

Scattering Length Density Calculator); thus not accounting for actual solvent exposure and the geometry of the protein. Other software packages such as e.g. SASView (The SASView Project, 2019) or WillItFit (Pedersen *et al.*, 2013) implicitly rely on accurate estimates of scattering lengths.

2. Empirical model for hydrogen-deuterium exchange

We here describe an approach to estimate the level of deuteration of each of the exchangeable backbone amide protons using the structure of the protein. We do so via estimating both the so-called intrinsic exchange rate constants from the amino acid sequence, and the perturbation away from these intrinsic rates in a give conformation of the protein. We assume that hydrogen-deuterium exchange can be described by the well-established Linderstrøm-Lang model, in which the exchange of a buried or otherwise protected proton with a solvent deuteron processes in two steps (Hvidt & Nielsen, 1966). First, the site becomes transiently exposed to the solvent in a process with an equilibrium constant termed K_{open}. Second, the transiently exposed site exchanges with the solvent with an intrinsic rate constant, k_{int}, determined by the local sequence and the experimental conditions. After a rapid transient, the exchange process can be described by a pseudo-first order reaction with a rate constant, k_{ex}, so that the probability, P_{ex}, of a backbone hydrogen having exchanged with a hydrogen atom from the solvent becomes:

$$P_{\mathrm{ex}}(t) = 1 - e^{-k_{\mathrm{ex}} t}$$

where t is the time elapsed since the exposure to D_2O.

Under relatively general assumptions and experimental conditions (leading to the so-called EX2 regime (Hvidt & Nielsen, 1966), the observed exchange rate, k_{ex}, is simply the product of the equilibrium constant for transient opening, K_{open}, and

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

the intrinsic rate, k_{int}. This relationship is typically formulated through the so-called protection factor, $P_f = K_{\text{open}}^{-1}$:

$$k_{\text{ex}} = \frac{k_{\text{int}}}{P_f}$$

The structural dependencies of the exchange rate are thus captured through differences in protection factors. Here we describe these using a model originally presented by Vendruscolo and colleagues (Vendruscolo *et al.*, 2003) in which the level of protection is predicted from examining the number of contacts and hydrogen bonds formed at an exchanging site:

$$\log(P_f) = \beta_h N_h + \beta_c N_c$$

where N_h is the number of hydrogen bonds to the backbone nitrogen/hydrogen, and N_c is the number of heavy atoms within a distance of 6.5 Å of the backbone nitrogen. For atomistic models, the coefficients $\beta_h = 2.0$ and $\beta_c = 0.35$ were refined from an variety of molecular dynamics (MD) simulations and data from hydrogen exchange (HX) experiments (Best & Vendruscolo, 2006). In the following examples and discussions, we estimate the presence of hydrogen bonds using the DSSP algorithm (Kabsch & Sander, 1983) with a default energy threshold of -0.5 kcal/mol.

We show examples of protection factors predicted as described above on their respective atomic structures (Figure 2). As expected, we observe how well folded domains are more protected than flexible, solvent exposed regions. Furthermore, we note that transmembrane regions of membrane proteins are considered to be very well protected from the solvent; again in line with intuition. We note that in case of calculations for membrane proteins we embed the protein in a lipid bilayer or other membrane mimetic, and take contacts to these into account when calculating P_f.

The intrinsic exchange rate, k_{int}, represents the exchange rate for a fully unfolded peptide chain. It is readily estimated from the amino acid residue sequence (and

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

the experimental conditions) using e.g. the Sphere server (Zhang, 1995; Fox Chase Cancer Center, 2019), which bases its estimations on values found in the literature (Bai *et al.*, 1993; Connelly *et al.*, 1993) or the data published by the Englander Lab (Englander, 2019; Nguyen *et al.*, 2018), which cites another source for the high-pH exchange rates (Mori *et al.*, 1997). The software presented in this paper uses the values from the latter two sources, which are refined from HX experiments on various reference peptides.

As an example, estimated intrinsic exchange rates for the sequence of lysozyme range from 0.03 s^{-1} to 46.60 s^{-1} across the 129 amino acid residues for a measured pH of 7 at a temperature of 293.15 K.

Apart from the backbone hydrogens, we assume that the following hydrogen atoms will exchange with the solvent at a timescale much faster than the ones observable by neutron scattering experiments due to their low pK_a values (Lide, 2005):

- The $-$NHs in the N-terminal(s)
- The $-$OHs in SER, THR, and TYR
- The $-$SHs in CYS
- The side chain $-$NHs in ASN, GLN, ARG, LYS, HIS, and TRP

In other words, these chemical groups are assumed to instantly exchange hydrogen atoms with the solvent. We refer to these atoms as rapidly-exchanging throughout this paper. The set of rapidly-exchanging hydrogens and backbone hydrogens are sometimes referred to as the "labile" hydrogens in the literature. We note that in some cases exchange of the single $-$NH group in the indole group of TRP residues may be rather slow (Wedin *et al.*, 1982), but since TRP residues are rather rare and there is no quantitative model for its exchange, we consider it as rapidly exchanging. The remaining hydrogens are considered non-exchangeable (Figure 1).

As an example of the result of these experimentally-supported assumptions, out

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

of the 959 hydrogen atoms generated by `PDB2PQR` (Dolinsky *et al.*, 2004; Dolinsky *et al.*, 2007) for the PDB ID **2LYZ** (Diamond, 1974) structure of lysozyme at a measured pH of 7.0, we find 148 rapidly-exchangeable, 126 backbone hydrogens (for a total of 274 labile hydrogens), and the remaining 685 non-exchangeable.

3. Solution small-angle neutron scattering

3.1. Estimating scattering from a protein in solution

For the calculations of the scattering profiles (i.e. the excess scattered intensity, $I(q)$, as a function of the scattering momentum transfer, q) presented here, we have used a simple fast Debye sum (Hansen, 1990) based on commonly used scattering lengths (NIST, 2019) and volumes (Fraser *et al.*, 1978) (Table 1). We stress that these values are central in our calculations. We assume a partial specific volume of solvent D_2O of 30.0 Å^3. Details of these calculations can be found in Appendix A.

We note that more advanced and involved methods for estimating scattering profiles from the atomic coordinates exist; e.g. expansion of scattering amplitudes on spherical harmonics as employed by the software CRYSON (Svergun *et al.*, 1998) or Debye sums as employed by the software FoXS (Schneidman-Duhovny *et al.*, 2010) (for x-ray scattering). However, the simple, fast Debye method we use appears to be sufficient for our purposes, ranges in scattering momentum transfer, and structures.

3.2. Comparison of time scales: Lysozyme

As a first example, let us consider the application of the presented scheme in a Gedanken experiment: a generic solution SANS experiment on lysozyme at room temperature, 293.15 K, in a D_2O-based buffer with a measured pH of 7.0. In Figure 3, a calculation of the scattering profile at selected times is shown, along with the amount of backbone hydrogens expected to have exchanged with the solvent.

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

We observe that in order for the imagined lysozyme to obtain fully or even 90% deuterated backbone hydrogens, the relevant time scales are orders of magnitude beyond those relevant in an experimental experiment. Indeed, the model predicts that the 90% backbone hydrogen deuteration commonly assumed, would not be reached until between 10^9 s and 10^{10} s or a timespan of more than 30 years under the defined conditions. As expected, the excess scattering cross-section for vanishing values of q, usually dubbed "the forward scattering", decreases as the protein deuterates; as the exchange process brings the scattering length density of the protein closer to that of D_2O. In total, the forward scattering drops to 62% of the initial value; see Figure 3 (top). It is particularly noteworthy that within typical experiment times of 1 hour and 1 day, the forward scattering intensity drops to, respectively, 98% and 94% of the initial value.

In particular, we note that of the 274 labile sites, only 54% are rapidly-exchanged, and after more than a day (10^5 s) of exposure to D_2O the model by Vendruscolo *et al.* predicts that only a total of 61% of the 274 labile hydrogen atoms will have exchanged. This value should be considered in relation to the usually applied 90% discussed earlier. We note also many residues in lysozyme have experimentally-determined values of $k_{\mathrm{ex}} < 10^{-7}\mathrm{s}^{-1}$ at pH 7.0 (Pedersen *et al.*, 1993). This is fully consistent with the very long exchange times obtained from the model calculations.

3.3. Comparison to experimental data: BSA

The data presented in Figure 4 were collected at the SANS instrument D22 (D22, 2019), Institut Laue-Langevin, in Grenoble, France. Four samples of bovine serum albumin (BSA) were prepared from the same H_2O-based stock solution at either pH 7.3 or pH 8.8 measured by pH-meter and changed into two analogous D_2O-based buffers using a NAP-5 desalting column (GE healthcare) either 9 or 36 hours before

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

irradiation. The experiment, including sample storage, was conducted at approximately 6 °C. For further details on the sample preparation and the experimental set up, consult the appendix.

We used PROPKA (Olsson *et al.*, 2011) and chain A of PDB ID **4F5S** (Bujacz, 2012) to estimate 4564 hydrogens in the BSA monomer, at pH 7.3 (pD of 7.7) and 4560 at pH 8.8 (pD of 9.2). According to the discussed model for H/D-exchange, the structure contains 499 hydrogen sites which will exchange rapidly (at pH 7.3 and an additional 4 at pH 8.8) with the D_2O-based solvent and 554 slowly exchanging backbone hydrogens, the exchange rates of which we estimate using the presented software.

From Figure 4, we conclude that quantitively we observe the expected behaviour. We see the forward scattering, $I(q \to 0)$, decreasing as a function of how long time the proteins have been exposed to D_2O (Figure 4, insert). Similarly, we note that the high-pH samples appear to have considerably lower forward scattering than the low-pH samples, in line with the expectation of more rapid exchange in these samples (Table 2). We note also that the effect of varying the time is greater at pH 8.8 where exchange is faster than at pH 7.3.

The presented fits are calculated as described. However, to fit the data we had to fit a scaling parameter which refined to $1.05 - 1.14$ along with a small constant background for the four presented samples. While it is obviously unsatisfactory to have to fit these adjustment parameters, we consider the refined values to be well within the margin-of-error of the absolute calibration of our data.

3.4. Comparison of homogenouos and site-specific deuteration: SERCA

Let us consider the membrane protein sarco-/endoplasmatic reticulum Ca^{2+} ATPase (SERCA) in an equilibrium between the E1 state, from PDB ID **5XA7** (Norimatsu *et al.*, 2017), and the E2 state, from PDB ID **5XAB** (Norimatsu *et al.*, 2017), described

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

by an ensemble of structures in a carrier system, which is assumed to be 'invisible' in D_2O as previously discussed (Midtgaard *et al.*, 2018; Maric *et al.*, 2014; Josts *et al.*, 2018).

We generated the ensemble of E1 and E2 states of SERCA using two independent one-microsecond MD simulations with CHARMM36m force field (Huang *et al.*, 2016) initiating from the aforementioned crystal structures inserted into a 1-palmitoyl-2-oleoylphosphatidylcholine (POPC) membrane bilayer. The simulations used the TIP3P water model and a periodic box of 13 nm by 13 nm by 16 nm and were performed using Gromacs2016.3 (Abraham *et al.*, 2015). In total, we generate an ensemble of 40 structures describing the intermediate states between the aforementioned crystal structures. As previously described we average the calculated protection factors over these structures (Best & Vendruscolo, 2006):

$$\log(P_f) = \langle \beta_h N_h + \beta_c N_c \rangle \tag{1}$$

and show calculated scattering profiles for the described structure under various conditions (Figure 5) at a measured pH of 7.0 and a temperature of 293.15 K.

We observe how the model predicts that the extra-cellular domains of the protein exchange faster than the transmembrane parts buried in the bilayer and how the effect of specifically exchanging specific sites mostly impacts the shape of the scattering profile for $q > 0.1$ Å^{-1}. In line with intuition, we observe that the difference between homogeneous deuteration and specific exchange matters most when the solvent-exposed domains of the proteins are mostly exchanged, while the transmembrane domains are still mostly protonated; i.e. the situation, wherein the protein appears mostly like a two-contrast molecule.

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

4. Software

4.1. Input and output

As input, the software takes the atomic coordinates in PDB-format (Bernstein *et al.*, 1977) of a protein alongside the coordinates of any other atoms relevant to the calculation e.g. a lipid bilayer for a membrane protein or bound ligands. We emphasize that unique model and chain identifiers specifying the individual models and molecules must be specified in the file as the calculation of k_{int} depends on the chain structure of the protein. Several additional, optional arguments can be supplied for the calculation. A list of the most important optional arguments are listed in Table 3.

The intrinsic exchange rates, k_{int}, are calculated from the reference data published by the Englander Lab (Englander, 2019; Nguyen *et al.*, 2018). As default, the software uses the reference values for poly-DL-Alanine; however, using their reference data from oligopeptides in the calculations is available as an alternative via a command line argument.

Whether hydrogens are present in the provided structure or not is irrelevant to the output. The software will remove any hydrogens from the structure and add them using the PDB2PQR software as well as the PROPKA algorithm.

The software outputs two files containing the provided structure. In one, values of k_{int} are exported as the B-factor column and values of $\log(P_f)$ are exported as the occupancy column. The other file contains $\log(k_{\text{ex}})$ as the B-factors and P_{ex} as the occupancies. In the second structure, hydrogen atoms will have been exchanged to deuterium atoms if P_{ex} exceeds a preset threshold for the individual residues.

If several models are present in the given file (separated using the MODEL keyword), the protection factor calculation is done for each individual model and outputted. The protection factors are subsequently averaged as outlined in equation 1, and each model is deuterated according to this average in an effort to simplify using the software on

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

e.g. ensembles from nuclear magnetic resonance or MD trajectories.

4.2. Code, dependencies, and availability

Source code for the presented software is available for download or cloning from this Gitlab repository:

`https://gitlab.com/mcpe/PSX`

The software is published under version 3 of the GNU Publishing License, GPLv3, and is available 'as is'.

The software is written in Python and relies on the `DSSP` software (Kabsch & Sander, 1983) for identifying hydrogen bonds and the `PDB2PQR` software for adding hydrogens to the structure based on the `PROPKA` algorithm. The reading and writing of the protein structures are handled using the PDB-tools (Hamelryck & Manderick, 2003) in the BioPython package (Cock *et al.*, 2009). As such, these modules must be available for the software to run correctly.

In passing, we mention that for the examples shown in this paper the running time of the software is a couple of seconds on an ordinary laptop. The software has been tested on Ubuntu and OSX.

5. Perspectives and conclusions

We have presented software to estimate the effects of solvent exposure using well established models and assessed this effect in the context of small-angle neutron scattering. Future investigations will attempt to estimate these effects in the context of other scattering techniques; most notably neutron reflectometry, as this technique would be susceptible to and affected by inaccurate estimates of scattering length (densities). For neutron reflectometry in particular, H_2O/D_2O-contrast variations are done *in*

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

situ and is usually an integrated part of the experiment. Thus, the outlined effects are especially relevant in this context.

Given recent developments and experiences in biological small-angle neutron scattering methods, we believe more precises approaches to the problem of solvent exchange are needed in the neutron scattering community in order to utilize the experimental set ups and the acquired data fully.

The model that we use to estimate protection factors could be optimized, including improved values of β_c and β_h. Refining optimal values for these parameters is an ongoing endeavour (Mohammadiarani *et al.*, 2018) and future versions of the software might utilize different values, or indeed functional forms, than the one used here.

Finally, we observe that the default assumption of 90% deuteration of proteins in SANS experiments appears to be a very high estimate for generic, modern BioSANS samples according to the considered model and typical temperatures and values of pH in experiments. Values between 50% and 70% seem more appropriate given our examples; however, ideally, these calculations should be repeated for each sample in an experiment. We hope the presented software will aid users in estimating this parameter.

Appendix A
Calculating scattering profiles

We use the Fast Debye sum approach to calculating scattering profiles begins by establishing a scattering-weighted pair distance distribution over N scatterers (Hansen,

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

1990):

$$p(r) = 4\pi \sum_{j}^{N} \sum_{k}^{N} \delta(r - r_{jk}) b_j b_k \tag{2}$$

where b_j and b_k are the (excess) scattering lengths of the j'th and k'th scatterer, and r_{jk} is the distance between them. In practice, this expression is usually binned into the data structure of a histogram. From this construction, we can calculate the scattering profile from the scatterers with a Fourier transformation:

$$I(q) = 4\pi n \int_0^\infty dr\, p(r) \frac{\sin(qr)}{qr} \tag{3}$$

where n is the number density of the sample.

This method is readily extended for the structures emerging from the presented software.

If we (using e.g. the presented software) associate an exchange probability, P_{ex}, to each backbone hydrogen (and set $P_{\mathrm{ex}} = 0$ for all other scatterers), we get a concise expression by assigning two scattering lengths, b^{H} and b^{D}, to each scatterer, where b^{H} is the scattering length in the case where the backbone hydrogen has not exchanged, and b^{D} is the scattering length elsewise. Note that $b^{\mathrm{H}} = b^{\mathrm{D}}$ for the scatterers that are not backbone hydrogens.

If we assume that the P_{ex}s are statistically independent, we can construct a substitute for equation 2:

$$\begin{aligned} p(r) =& 4\pi \sum_{j}^{N} \sum_{k}^{N} \delta(r - r_{jk}) \cdot \\ & (b_j^{\mathrm{H}} b_k^{\mathrm{H}} (1 - P_{\mathrm{ex},j})(1 - P_{\mathrm{ex},k}) + b_j^{\mathrm{H}} b_k^{\mathrm{D}} (1 - P_{\mathrm{ex},j}) P_{\mathrm{ex},k} + \\ & b_j^{\mathrm{D}} b_k^{\mathrm{H}} P_{\mathrm{ex},j} (1 - P_{\mathrm{ex},k}) \qquad + b_j^{\mathrm{D}} b_k^{\mathrm{D}} P_{\mathrm{ex},j} P_{\mathrm{ex},k}) \end{aligned}$$

The Fourier transformation can now be carried out using equation 3.

Appendix B

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

Preparation and handling of BSA samples

B.1. Sample preparation

BSA (Sigma Aldrich) was dissolved in gel filtration buffer (20 mM Tris-HCl, *pH* 7.5, 100 mM NaCl) and applied to a Superdex 200 Increase (GE Healthcare) equilibrated in gel filtration buffer. Fractions spanning the peak corresponding to monomeric BSA were pooled and kept on ice until exchange into D_2O. The sample was split in four and changed into D_2O using a NAP-5 desalting column (GE healthcare) equilibrated in 20 mM Tris-DCl, 100 mM NaCl at either *pH* 7.3 or 8.8 (both 100% D2O) and either 9 or 36 hours before irradiation.

B.2. Experimental conditions

The samples were irradiated by neutrons with a nominal wavelength of 6.0 Å from a distribution with a width of 0.6 Å in two experimental settings: one with a collimation length of 2.8 m and a sample-to-detector distance of 1.5 m, and one with a collimation length of 8.0 m with a sample-to-detector distance of 8.0 m covering a range in scattering momentum transfer from 0.0084 $Å^{-1}$ to 0.57 $Å^{-1}$. 1 mm rectangular Hellma Suprasil quartz cuvettes (Hellma Analytics) were usied as sample containers during the experiment.

Furthermore, absorption at 280 nm was measured on the irradiated samples using a Nanodrop 1000 spectrophotometer (Thermo Fisher Scientific), from which we estimate the protein concentration of the irradiated fraction. The extinction coefficient at 280 nm for a BSA monomer was calculated to be 42925 $M^{-1}cm^{-1}$.

Instrumental effect were accounted for as described in the literature (Pedersen

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

et al., 1990) using the values produced by GRASP (Dewhurst, 2019), which was also used to reduce the data and bring them to absolute units using the direct beam chopped by an ultra-fast chopper as reference. The presented models were calculated and instrumental effects were taken into account using WillItFit (Pedersen *et al.*, 2013).

We thank the staff at Institut Laue-Langevin, Grenoble, France for the beam time and support resulting in the presented data, and thank Nicolai Tidemand Johansen for aiding in the preparation and irradiation of the BSA sample. We thank Raul Araya-Secchi for discussions on general implementations of the selected algorithms. This research was supported by the Lundbeck Foundation BRAINSTRUC initiative in structural biology, and the Synergy project funded by the Novo Nordisk foundation. NVidia's Academic Grant Program is acknowledged for granting the Titan Xp GPU on which many of the presented calculations were performed.

References

Abraham, M. J., Murtola, T., Schulz, R., Páll, S., Smith, J. C., Hess, B. & Lindah, E. (2015). *SoftwareX*, **1-2**, 19–25.

Bai, Y., Milne, J., Mayne, L. & Englander, W. (1993). *Proteins*, **17**(1), 75–86.

Bernstein, F. C., Koetzle, T. F., Williams, G. J., Meyer, E. F., Brice, M. D., Rodgers, J. R., Kennard, O., Shimanouchi, T. & Tasumi, M. (1977). *Eur. J. Biochem.* **80**(2), 319–324.

Best, R. B. & Vendruscolo, M. (2006). *Structure*, **14**(1), 97–106.

Bugge, K., Papaleo, E., Haxholm, G. W., Hopper, J. T. S., Robinson, C. V., Olsen, J. G., Lindorff-Larsen, K. & Kragelund, B. B. (2016). *Nat. Commun.* **7**(May), 11578.

Bujacz, A. (2012). *Acta Crystallogr. Sect. D Biol. Crystallogr.* **68**(10), 1278–1289.

Cock, P. J., Antao, T., Chang, J. T., Chapman, B. A., Cox, C. J., Dalke, A., Friedberg, I., Hamelryck, T., Kauff, F., Wilczynski, B. & De Hoon, M. J. (2009). *Bioinformatics*, **25**(11), 1422–1423.

Connelly, G. P., Bai, Y., Jeng, M. F. & Englander, S. W. (1993). *Proteins*, **17**(1), 87–92.

D22, (2019). D22 - Large dynamic range small-angle diffractometer. https://www.ill.eu/users/instruments/instruments-list/d22/description/instrument-layout/.

Dewhurst, C., (2019). GRASP - Graphical Reduction and Analysis SANS Program. http://www.ill.fr/lss/grasp/.

Diamond, R. (1974). *J. Mol. Biol.* **82**(3), 371–391.

Dolinsky, T. J., Czodrowski, P., Li, H., Nielsen, J. E., Jensen, J. H., Klebe, G. & Baker, N. A. (2007). *Nucleic Acids Res.* **35**, 522–525.

Dolinsky, T. J., Nielsen, J. E., McCammon, J. A. & Baker, N. A. (2004). *Nucleic Acids Res.* **32**, 665–667.

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

Dutzler, R., Campbell, E. B. & MacKinnon, R. (2003). *Science*, **108**(2003), 108–112.

Englander, W., (2019). The Englander Lab Website, University of Pennsylvania. http://hx2.med.upenn.edu/.

Fox Chase Cancer Center, (2019). Sphere - A Server Program for Hydrogen Exchange Rate Estimation. http://landing.foxchase.org/research/labs/roder/sphere/sphere.html.

Fraser, R., MacRae, T. & Suzuki, E. (1978). *J. Appl. Crystallogr.* **11**, 693–694.

Granier, T., Gallois, B., Dautant, A., D'Estaintot, B. L. & Précigoux, G. (1997). *Acta Crystallogr. Sect. D Biol. Crystallogr.* **53**(5), 580–587.

Guinier, A. & Fournet, G. (1955). *Small-angle scattering of X-rays*. John Wiley and Sons, New York.

Hamelryck, T. & Manderick, B. (2003). *Bioinformatics*, **19**(17), 2308–2310.

Hansen, S. (1990). *J. Appl. Crystallogr.* **23**(4), 344–346.

Huang, J., Rauscher, S., Nawrocki, G., Ran, T., Feig, M., De Groot, B. L., Grubmüller, H. & MacKerell, A. D. (2016). *Nat. Methods*, **14**(1), 71–73.

Hvidt, A. & Nielsen, S. O. (1966). In *Advances in protein chemistry*, vol. 21, pp. 287–386. Elsevier.

ISIS, (2019). Biomolecular Scattering Length Density Calculator. http://psldc.isis.rl.ac.uk/Psldc/.

Johansen, N. T., Pedersen, M. C., Porcar, L., Martel, A. & Arleth, L. (2018). *Acta Crystallogr. Sect. D Biol. Crystallogr.* p. Accepted.

Jordan, A., Jacques, M., Merrick, C., Devos, J., Forsyth, V. T., Porcar, L. & Martel, A. (2016). *J. Appl. Crystallogr.* **49**(6), 2015–2020.

Josts, I., Nitsche, J., Maric, S., Mertens, H. D., Moulin, M., Haertlein, M., Prevost, S., Svergun, D. I., Busch, S., Forsyth, V. T. & Tidow, H. (2018). *Structure*, **26**, 1–8.

Kabsch, W. & Sander, C. (1983). *Biopolymers*, **22**(12), 2577–2637.

Kynde, S., Skar-Gislinge, N., Pedersen, M. C., Midtgaard, S. R., Simonsen, J. B., Schweins, R., Mortensen, K. & Arleth, L. (2014). *Acta Crystallogr. Sect. D Biol. Crystallogr.* **70**(2), 371–383.

Lide, D. R. (ed.) (2005). *CRC Handbook of Chemistry and Physics*. CRC Press, Boca Raton, Florida.

Maric, S., Skar-Gislinge, N., Midtgaard, S., Thygesen, M. B., Schiller, J., Frielinghaus, H., Moulin, M., Haertlein, M., Forsyth, V. T., Pomorski, T. G. & Arleth, L. (2014). *Acta Crystallogr. Sect. D Biol. Crystallogr.* **70**(2), 317–328.

Midtgaard, S. R., Darwish, T. A., Pedersen, M. C., Huda, P., Larsen, A. H., Jensen, G. V., Kynde, S. A. R., Skar-Gislinge, N., Nielsen, A. J. Z., Olesen, C., Blaise, M., Dorosz, J. J., Thorsen, T. S., Venskutonyté, R., Krintel, C., Møller, J. V., Frielinghaus, H., Gilbert, E. P., Martel, A., Kastrup, J. S., Jensen, P. E., Nissen, P. & Arleth, L. (2018). *FEBS J.* **285**(2), 357–371.

Mohammadiarani, H., Shaw, V. S., Neubig, R. R. & Vashisth, H. (2018). *J. Phys. Chem. B*, **122**(1), 9314–9323.

Mori, S., van Zijl, P. C. & Shortle, D. (1997). *Proteins*, **28**(3), 325–32.

Nguyen, D., Mayne, L., Phillips, M. C. & Walter Englander, S. (2018). *J. Am. Soc. Mass Spectrom.* **29**(9), 1936–1939.

NIST, (2019). Neutron scattering lengths and cross sections. https://www.ncnr.nist.gov/resources/n-lengths/.

Norimatsu, Y., Hasegawa, K., Shimizu, N. & Toyoshima, C. (2017). *Nature*, **545**(7653), 193–198.

Olsson, M. H. M., Sondergaard, C. R., Rostkowski, M. & Jensen, J. H. (2011). *J. Chem. Theory Comput.* **7**, 525–537.

Pedersen, J., Posselt, D. & Mortensen, K. (1990). *J. Appl. Crystallogr.* **23**(4), 321–333.

Pedersen, M. C., Arleth, L. & Mortensen, K. (2013). *J. Appl. Crystallogr.* **46**(6), 1894–1898.

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

Pedersen, T. G., Thomsen, N. K., Andersen, K. V., Madsen, J. C. & Poulsen, F. M. (1993). *J. Mol. Biol.* **230**(2), 651–660.

Schneidman-Duhovny, D., Hammel, M. & Sali, A. (2010). *Nucleic Acids Res.* **38**(Web Server issue), 540–544.

Svergun, D. I., Richard, S., Koch, M. H., Sayers, Z., Kuprin, S. & Zaccai, G. (1998). *Proc. Natl. Acad. Sci. U. S. A.* **95**(5), 2267–2272.

The SASView Project, (2019). SASView for Small Angle Scattering Analysis. https://www.sasview.org.

Vendruscolo, M., Paci, E., Dobson, C. M. & Karplus, M. (2003). *J. Am. Chem. Soc.* **125**(51), 15686–15687.

Wedin, R. E., Delepierre, M., Dobson, C. M. & Poulsen, F. M. (1982). *Biochemistry*, **21**(5), 1098–1103.

Williams, T., Kelley, C. *et al.*, (2019). Gnuplot 5.2: an interactive plotting program. http://www.gnuplot.info/.

Zhang, Y.-Z. (1995). *Protein and peptide structure and interactions studied by hydrogen exchange and NMR*. Ph.D. thesis, University of Pennsylvania.

Table 1. *The (coherent) scattering lengths and volumes used in the calculation of scattering profiles for proteins presented in this paper. The values are from NIST (NIST, 2019) and the literature (Fraser* et al.*, 1978), respectively.*

Atom	Scattering length, fm	Assigned volume, Å^3
H	−3.7406	5.15
D	6.671	5.15
C	6.646	16.44
N	9.36	2.49
O	5.803	9.13
S	2.847	19.86

Table 2. *Concentration, c, radius of gyration, R_g, and normalized forward scattering, $I(q \to 0)/c$ for the data presented in Figure 4. The Guinier fits (Guinier & Fournet, 1955) were done using Gnuplot (Williams* et al.*, 2019).*

Sample	c, mg/ml	R_g, $\AA$	$I(q \to 0)/c$, cm^2/mg
■	1.18	25.8 ± 0.31	0.1280 ± 0.00072
■	1.24	26.0 ± 0.26	0.1336 ± 0.00063
■	1.30	25.7 ± 0.25	0.1460 ± 0.00067
■	1.32	26.2 ± 0.26	0.1476 ± 0.00071

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

Table 3. *Selected optional command line arguments.*

Argument	Description	Default value
`-bc`	The coefficient β_c used to calculate protection factors	0.35
`-bh`	The coefficient β_h used to calculate protection factors	2.0
`-dc`	Distance threshold used in the calculation of the contact number, N_c. in Å	6.5
`-eh`	Energy threshold for hydrogen bond energy in `DSSP` algorithm in kcal/mol	-0.5
`-ph`	pH used to estimate exchange rates as measured by pH-meter	7.0
`-pc`	Probability threshold above which hydrogens will be exchanged in the output structure	0.5
`-ti`	Time elapsed since the protein was exposed to D_2O in seconds	0.0
`-te`	Temperature used to intrinsic estimate exchange rates in K	293.15

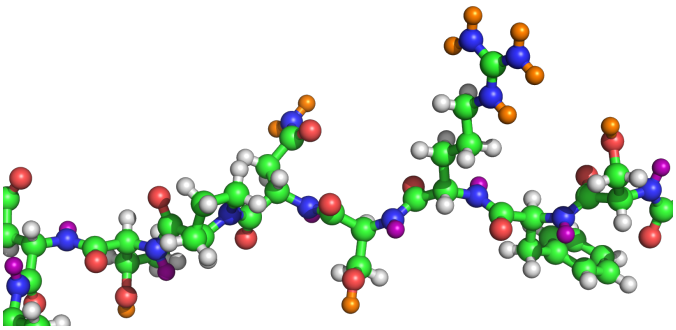

Fig. 1. A generic protein structure with backbone amide hydrogens highlighted in purple, un-exchangeable hydrogens in white, and the rapidly-exchanging hydrogens in orange. Carbon-, nitrogen-, and oxygen-atoms are shown in green, blue, and red, respectively.

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

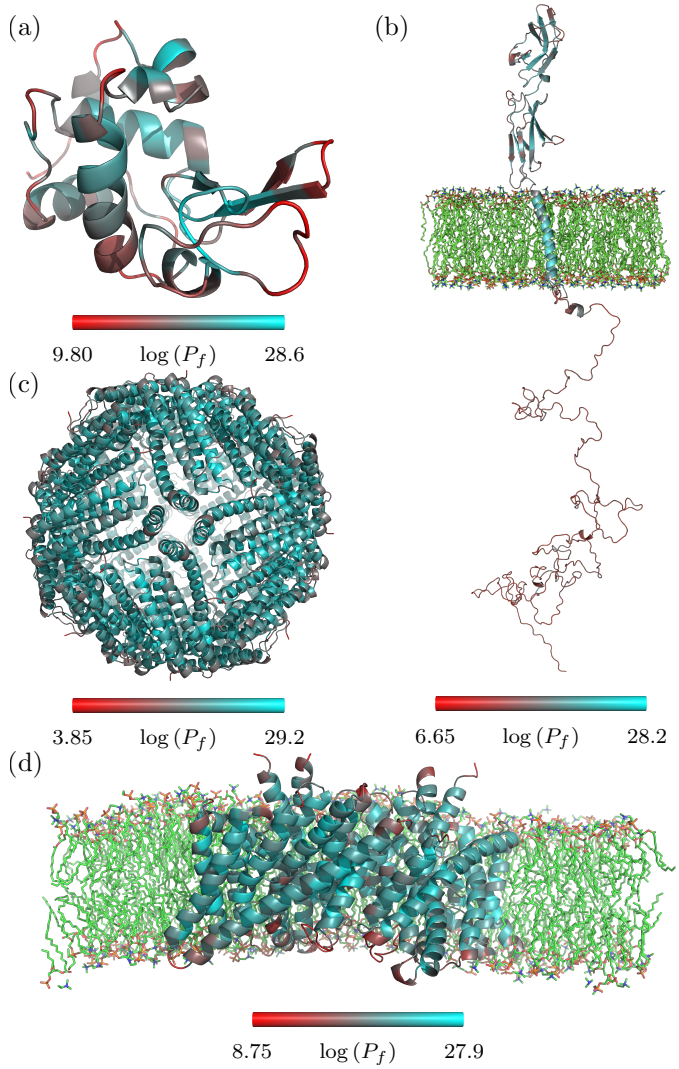

Fig. 2. Examples of protection factors calculated from protein structures. (a): Lysozyme, from PDB ID **2LYZ**. (b): Prolactin receptor in a bilayer of POPC phospholipids (half of which are not shown), from Bugge *et al.* (Bugge *et al.*, 2016). (c): Apoferritin (24-mer), from PDB ID **1IES** (Granier *et al.*, 1997). (d): H^+/Cl^- Exchange Transporter in a bilayer of DPPC phospholipids (half of which are not shown), from PDB ID **1OTU** (Dutzler *et al.*, 2003).

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

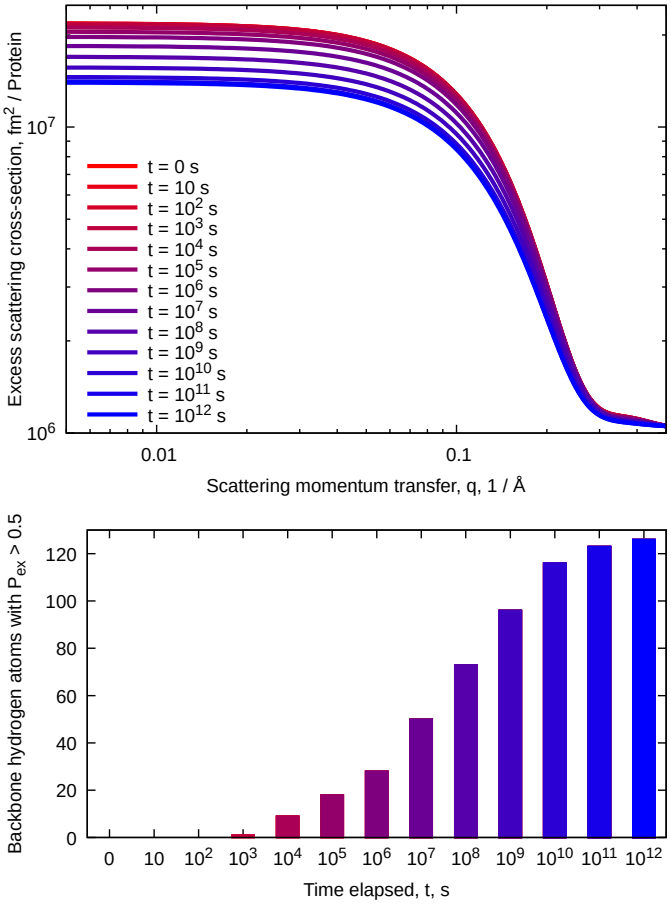

Fig. 3. Time evolution of the structure PDB ID **2LYZ**, lysozyme, shown in Figure 2(a), according to the solvent exposure model discussed in this paper. Top: Scattering profiles calculated as explained in the text; a small background has been added the the profiles for a more realistic presentation. Bottom: The number of the 126 backbone hydrogens atoms with $P_{\mathrm{ex}} > 0.5$ for selected time points. We remind the reader that 10^5 s is approximately 1.15 days and that 10^8 s is approximately 3.16 years.

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

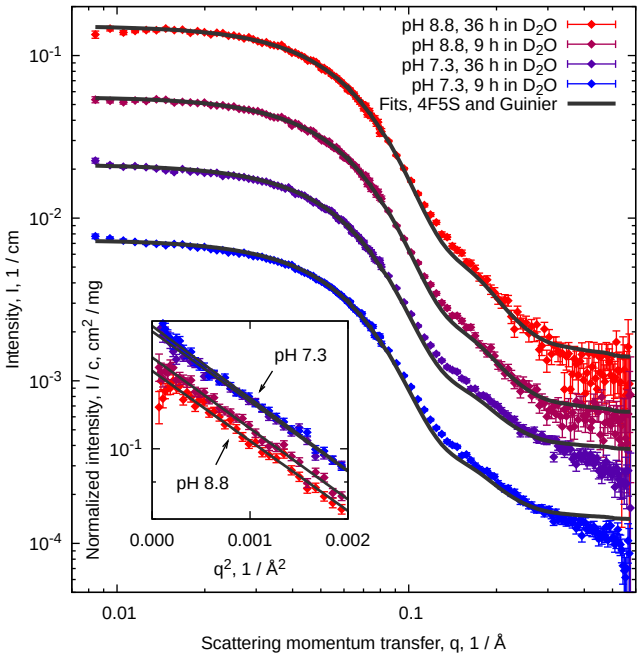

Fig. 4. SANS data from BSA. The top-most data and fit are correctly scaled, whereas the lower data and fits are scaled by factors of 3 relative to the one above. The insert shows Guinier fits. Selected parameters are listed in Table 2.

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

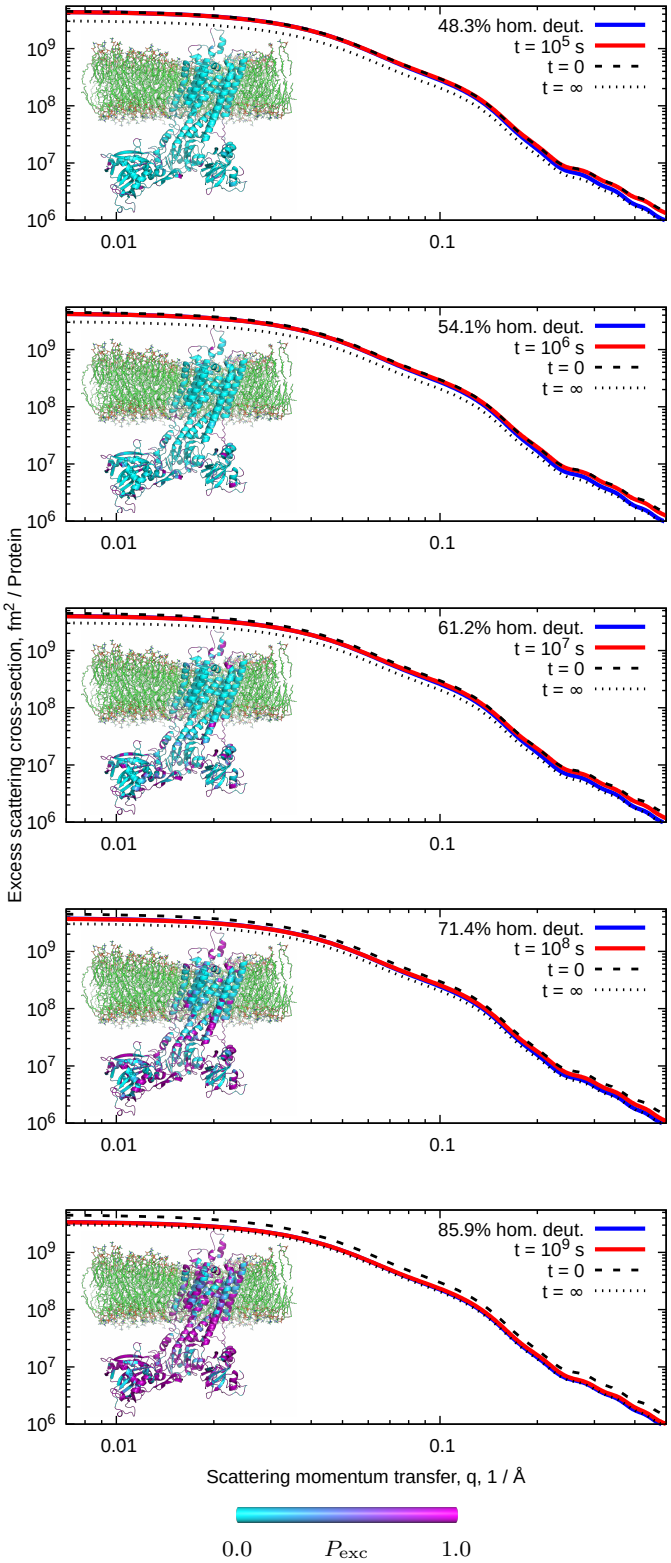

Fig. 5. Scattering profiles of SERCA. As inserts, we visualize P_{ex} on the E1 state of SERCA in a bilayer of POPC phospholipids (half of which are not shown). The phospholipids do not contribute to the scattering pattern in an effort to mimick the scattering from match-out deuterated carrier systems. For reference, we also plot the scattering profiles of the fully deuterated structure and the structure with only the rapidly-exchanging sites exchanged to deuterium.

bioRxiv preprint doi: https://doi.org/10.1101/609859; this version posted April 23, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder. All rights reserved. No reuse allowed without permission.

Synopsis

Using established models, we calculate the effect of exposing protonated protein samples to D_2O and assess the impact in small-angle neutron scattering experiments. We introduce software to evaluate the effect of this from a given structure and give examples of applications.