Separation of hemodynamic signals from GCaMP fluorescence measured with widefield imaging

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ABSTRACT

Widefield calcium imaging is often used to measure brain dynamics in behaving mice. With a large field of view and a high sampling rate, widefield imaging can monitor activity from several distant cortical areas simultaneously, revealing cortical interactions. Interpretation of widefield images is complicated, however, by the absorption of light by hemoglobin, which can substantially affect the measured fluorescence. One approach to separating hemodynamics and calcium signals is to use multi-wavelength backscatter recordings to measure light absorption by hemoglobin. Following this approach, we develop a spatially-detailed regression-based method to estimate hemodynamics. The spatially-detailed model is based on a linear form of the Beer-Lambert relationship, but is fit at every pixel in the image and does not rely on the estimation of physical parameters. In awake mice of three transgenic lines, the Spatial Model offers improved separation of hemodynamics and changes in GCaMP fluorescence. The improvement is pronounced near blood vessels and, in contrast with other models based on regression or the Beer-Lambert law, can remove vascular artifacts along the sagittal midline. Compared to other separation approaches, the spatially-detailed model permits more accurate fluorescence-based determination of neuronal activity across the cortex.

INTRODUCTION

Over the last few years there has been a sharp increase in the number of mouse lines with GCaMP expression throughout much of neocortex (Hasan *et al.*, 2004; Chen *et al.*, 2012; Zariwala *et al.*, 2012; Madisen *et al.* 2015; Wekselblatt *et al.*, 2016; Bethge *et al.*, 2017; Daigle *et al.*, 2018), offering the opportunity to image cortical activity with high signal-to-noise and genetically-targeted expression. As a result, there has been a resurgence in the use of widefield fluorescence calcium imaging to monitor brain dynamics *in vivo*, especially in the context of mouse behavior (Wekselblatt *et al.*, 2016; Makino *et al.*, 2017; Allen et al., 2017, Mitra et al., 2018). Widefield imaging offers a large field of view (>10 mm), enabling simultaneous imaging of almost all of neocortex, can be performed through intact skull (White et al., 2011, Silasi *et al.*, 2016), eliminating invasive craniotomies, and, compared to laser scanning techniques, widefield imaging can achieve a faster sampling rate and is relatively simple and inexpensive to implement.

Widefield imaging also presents some challenges. It lacks the optical sectioning of confocal and multiphoton microscopes, with the result that fluorescence is typically an average across cells and cellular compartments. Emission can originate from intrinsic fluorophores such as flavoproteins (Zipfel *et al.*, 2003) and fluorescence excitation and emission can be affected by endogenous absorbers, like hemoglobin. The effects of intrinsic fluorophores can be negligible in mice with bright and strongly-expressed fluorophores (e.g. Zhuang *et al.*, 2017). In contrast, the absorption of fluorescence by hemoglobin cannot be overcome with strong fluorophore expression due to the multiplicative effect of absorption on fluorescence. Furthermore, hemoglobin is a strong, broad-spectrum absorber at around 500-600 nm, which includes excitation and emission wavelengths of GCaMP. Hence changes in hemoglobin absorption greatly complicate interpretation of GCaMP fluorescence measurements, even in mice with strong GCaMP expression.

Hemodynamics encompasses multiple processes, including neuro-vascular coupling, in which neural and glial activity are accompanied by dilation of blood vessels and changes in blood oxygenation, resulting in changes in the total concentration of hemoglobin and the ratio of oxygenated to deoxygenated hemoglobin (Malonek and Grinvald, 1996; Berwick *et al.*, 2005; Hillman *et al.*, 2007; Stefanovic et al., 2008; Sirontin *et al.*, 2009; Bouchard *et al.*, 2009; Hillman et al., 2014; O'Herron *et al.*, 2016). Contraction of cardiac, pulmonary and postural muscles can also drive changes in total hemoglobin concentration, via changes in intracranial blood pressure (Gisolf *et al.*, 2004; Huo *et al.*, 2015). Postural and locomotor influences on hemodynamics are common in awake, behaving animals, making the separation of hemodynamics from activity-related changes in cellular calcium concentration a common challenge in studies of sensory-motor processing in behaving mice.

There are several strategies to separate changes in calcium indicator fluorescence from hemodynamic

changes in light absorption (Bouchard *et al.*, 2009; Wekselblatt *et al.*, 2016; Allen *et al.*, 2017). One

approach relies on the measurement of hemoglobin absorption using one or more diffuse reflectance or

'backscatter' measurements, in which some portion of the photons illuminating the brain surface undergo

multiple scattering events within the tissue and return to the surface, escaping the brain to a detector.

Backscatter can be measured continuously and need not conflict with fluorescence measurements,

enabling continuous monitoring of hemodynamics during fluorescence imaging. From backscatter

measurements, hemoglobin concentrations are often calculated using a modified Beer-Lambert

relationship that relates the absorption of light by oxygenated and deoxygenated hemoglobin to the length

of the mean scattering path through tissue (Bouchard *et al.*, 2009; White *et al.*, 2011; Ma *et al.*, 2016a).

Scattering path lengths are difficult to measure empirically, forcing the use of calculated mean path

lengths that do not account for local differences in scattering and absorption. Local differences in path

length can lead to substantial errors in the estimated effects of hemodynamics on fluorescence measured

with indicators such as GCaMPs.

Here we describe and test a spatially-detailed regression model that allows for differences in optical

properties across the brain. With this model, we quantify the correction in GFP reporter mice and apply

the regression model to GCaMP mice, finding that the spatially-detailed model provides improved

separation of hemodynamics from hemodynamics from changes in GCaMP fluorescence, particularly in

brain areas where the separation is challenging with previous models.

RESULTS

Hemodynamics affect fluorescence in GCaMP- and GFP-expressing mice

We used widefield imaging to monitor fluorescence across neocortex in awake mice expressing

GCaMP in neocortical pyramidal neurons. Vasculature was prominent in fluorescence images and

changes in fluorescence near blood vessels were commonplace (figure 1). We observed three types of

putative hemodynamic effects, defined by their spatial and temporal characteristics. First, we observed

stimulus-linked changes in fluorescence that were localized within cortex (figure 1A). Fluorescence in

visual cortex increased rapidly after the onset of visual stimulation followed by a prolonged sag, often to

<50% peak amplitude. Following stimulus offset, fluorescence typically decreased below the pre-stimulus

baseline and recovered after ~2 seconds. The fluorescence increase is a GCaMP-mediated signal. The

time course of the sag and overshoot are consistent with the ~1 second delayed onset and 4-5 second

decay of local vessel dilation during neurovascular coupling following neural activity (Malonek and

Grinvald, 1996; Berwick *et al.*, 2005; Sirotin *et al.*, 2009; Ma *et al.*, 2016b). Second, we observed large

amplitude (>10%) fluctuations that were restricted mainly to the midline vasculature (figure 1B), and

typically included fast transient spikes in fluorescence, sometimes in bouts lasting 1-10 seconds. These

fluctuations may result from changes in venous blood volume along the superior sagittal sinus that relates

to movements or postural changes (Huo *et al.*, 2015, Gilad *et al.*, 2018). Finally, we observed low

amplitude (<3%), global oscillations in the 8-12 Hz frequency range of the heart rate in most recordings

(figure 1C). As expected, our results suggest that changes in fluorescence measured from GCaMP-

expressing mice are a mixture of changes in GCaMP fluorescence and hemodynamics. In many instances,

the hemodynamic effects were in the same amplitude range as changes in GCaMP fluorescence.

Consistent with the suggestion that fluorescence in GCaMP animals includes a substantial

hemodynamic component, we observed events with similar spatial and temporal characteristics in GFP

mice (figure 1D-F), in which fluorescence does not change with intracellular calcium concentration.

Optical strategy for simultaneous measurement of fluorescence and hemodynamics

Hemodynamics alter widefield fluorescence signals by absorbing light during excitation or emission.

Absorption can be measured using backscatter (figure 2A). Hemoglobin absorption extends over a broad

spectrum that includes wavelengths beyond the excitation and emission bands of GFP and GCaMP,

enabling the measurement of hemoglobin concentrations using wavelengths different from those used for

fluorescence (figure 2B). Furthermore, oxy- and deoxyhemoglobin absorption spectra differ substantially

across the visible spectrum (figure 2B), enabling one to distinguish changes in the concentrations of oxy-

(HbO) and of deoxyhemoglobin (HbR) using backscatter measurements at two wavelengths with different

HbO and HbR absorption, such as 577 nm and 630 nm (Frostig *et al.*, 1990). Using two cameras, we

simultaneously acquired fluorescence data at 100Hz and two backscatter wavelengths (577 nm and 630

nm) at ~17 Hz (figure 2C). Due to these frame rates we were unable to adequately sample heart-rate

hemodynamic signals (~8-12 Hz) and used a low-pass filter to remove fluctuations at >5Hz.

Beer-Lambert model

The Beer-Lambert law has often been employed to estimate light absorption by oxy- and

deoxyhemoglobin and thereby separate hemodynamics from changes in indicator fluorescence (Bouchard

et al., 2009; White *et al.*, 2011; Ma *et al.*, 2016a). The Beer-Lambert law relates absorption of light to the

concentration of the absorbing species and can be used to calculate hemodynamic effects across the brain

surface.

$$I = I_0 \, e^{-x(\lambda) \cdot c(t) \cdot \varepsilon(\lambda)}$$

where, I is the measured light intensity returning from source I_0, $\varepsilon(\lambda)$ is the wavelength-dependent

extinction coefficient of the absorbing species, $c(t)$ is the time-varying concentration of the absorbing

species, $x(\lambda)$ is mean path length, the wavelength-dependent distance travelled by propagating light.

We calculated and removed the changes in fluorescence resulting from absorption by oxy- and

deoxyhemoglobin, as described previously (Ma *et al.*, 2016a), and quantified the remaining variance.

Quantifying performance in a GCaMP mouse is challenging since hemodynamics and changes in

indicator fluorescence can each drive changes in measured fluorescence. Consequently, we quantified the

performance of hemodynamic correction strategies in GFP-expressing Ai140 mice (Daigle *et al.*, 2019)

crossed with 3 Cre lines, driving GFP expression enriched in different cortical layers: Cux2-Cre (layer

2/3), Rorb-Cre (layer 4), and Ntsr1-Cre (layer 6, figure 3C). In these three lines, GFP fluorescence

accounts for ~95% of the photons emitted from the preparation (Cux2-Cre 97.9 %, Rorb-Cre 93.7 %,

Ntsr1-Cre 94.4 %, figure S1) thus we expect nearly all changes in fluorescence to result from

hemodynamics with a negligible contribution from endogenous fluorophores. Complete separation of

hemodynamics from changes in indicator fluorescence would reduce the variance to ~0.05.

The initial variance of the fluorescence in GFP mice was not spatially uniform. Variance was ~3-5

times greater along the midline and over large vessels than over the center of each hemisphere (figure

3A), consistent with a strong influence of movement- or posture-related hemodynamics. After Beer-

Lambert correction, the variance was reduced in all locations across the brain. The median remaining

variance across pixels (normalized to initial variance at each pixel), averaged across mice, was $0.17 \pm$

0.01 in 3 Cux2-Ai140 mice, 0.10 ± 0.03 in 3 Rorb-Ai140 mice and 0.31 ± 0.04 in 5 Ntsr1-Ai140 mice

(figure 3D). However, remaining variance differed substantially with location. Normalized remaining

variance was generally <0.1 in the center of each hemisphere, over anterior visual cortex and across much

of somatosensory cortex (figure 3A). Performance of the correction declined towards the edges of the

image, over large vessels and along the midline, where remaining variance was commonly >0.3. In these

areas, it is likely that movement- or posture-related hemodynamic transients remained largely

uncorrected, leaving fluorescence from midline cortical regions contaminated with hemodynamic effects.

One common simplification of the Beer-Lambert model is to choose a single extinction coefficient and

path length for each wavelength band (rather than integrating over the spectrum of wavelengths; see

appendix). When applied to our data, using the extinction coefficients and path lengths of the mean of

each wavelength band, average remaining variance was $\geq$40 % greater than with the full Beer-Lambert

model (remaining variance 0.24 ± 0.03 in 3 Cux2-Ai140 mice, 0.23 ± 0.04 in 3 Rorb-Ai140 mice and

0.45 ± 0.03 in 5 Ntsr1-Ai140 mice, figure S3A,D). Our results suggest that using a single extinction

coefficient and path length foe each wavelength band substantially impairs performance of the Beer-

Lambert model and is best avoided.

Linear regression, a spatially-detailed alternative to the Beer-Lambert model

For our Beer-Lambert calculations, we used the same path length estimates at every pixel, a necessary

simplification. Naturally, performance of the model is sensitive to the choice of path lengths, particularly

of the 577 nm path length (figure S2). We hypothesized that the poor performance of the Beer-Lambert

model in some locations results from our inability to account for local variations in optical properties of

the tissue, such as mean path length.

Two-wavelength regression is a promising alternative to the Beer-Lambert model because it may

account for optical differences across the cortical surface. Unconstrained regression should always

produce results that are equivalent to or better than the Beer-Lambert model because it is fit separately at

each pixel, and thus has many additional degrees of freedom. Conversely, if we assume that pathlength is

the main free parameter in the Beer-Lambert model, and if the true path lengths are identical at all

locations in the tissue, then the Beer-Lambert and regression models should converge on the same

solution.

We begin by establishing that, in principle, linear regression with two variables can account for

hemodynamics independently for each pixel. Measured fluorescence, $I_F(x, y, t)$, can be related to two

backscatter intensities, $I_1(x, y, t)$ and $I_2(x, y, t)$, using two assumptions: that the absorbance at each

wavelength depends only on two hidden fluctuating variables, $C_{HbO}(x, y, t)$ and $C_{HbR}(x, y, t)$,

representing the molar concentrations of oxy- and deoxy-hemoglobin, respectively; and that the

absorbance on the fluorescence channel is multiplicative with the true fluorescence, $F(x, y, t)$ (the

fluorescence that would be evoked in the absence of absorption by hemoglobin). Hence,

191
$$I_F(x, y, t) = F(x, y, t) T_F\big(C_{HbO}(x, y, t), C_{HbR}(x, y, t)\big) I_F^{(ex)}(x, y), \tag{1}$$

192
$$I_1(x, y, t) = T_1\big(C_{HbO}(x, y, t), C_{HbR}(x, y, t)\big) I_1^{(ex)}(x, y), \tag{2}$$

193
$$I_2(x, y, t) = T_2\big(C_{HbO}(x, y, t), C_{HbR}(x, y, t)\big) I_2^{(ex)}(x, y), \tag{3}$$

194 where T_F, T_1, T_2 are transmittance functions that depend on HbO and HbR concentrations, and $I_F^{(ex)}$, $I_1^{(ex)}$,

195 $I_2^{(ex)}$ are incident intensities. The dynamic quantities relating to light intensity and hemoglobin

196 concentration can be expressed in terms of their mean values and deviations:

197
$$I_\star(x, y, t) = \bar{I}_\star(x, y) + \Delta I_\star(x, y, t), \tag{4}$$

198
$$F(x, y, t) = \bar{F}(x. y) + \Delta F(x, y, t), \tag{5}$$

199
$$C_{Hb\star}(x, y, t) = \bar{C}_{Hb\star}(x, y) + \Delta C_{Hb\star}(x, y, t), \tag{6}$$

200 In our results, the amplitude of the fluorescence signal is large relative to its dynamic range. Under these

201 conditions, equations 1-3 can be linearized in terms of the deviations, permitting the elimination of the

202 hemoglobin concentrations, and enabling derivation of the regression problem (see Appendix for

203 derivation):

204
$$\frac{\Delta I_F(x, y, t)}{\bar{I}_F(x, y)} \approx \frac{\Delta F(x, y, t)}{\bar{F}(x, y)} + S_1(x, y) \frac{\Delta I_1(x, y, t)}{\bar{I}_1(x, y)} + S_2(x, y) \frac{\Delta I_2(x, y, t)}{\bar{I}_2(x, y)}. \tag{7}$$

$S_1(x, y)$ and $S_2(x, y)$ are coefficient maps (figure 4C). Just as path lengths are the key unknown

parameters in the Beer-Lambert model, regression coefficients are the key to separating hemodynamics

from changes in indicator fluorescence using the regression model. As a result of the linearization,

regression coefficients can be calculated from path lengths (figure 3E, and see Appendix).

In GFP mice, where changes in measured fluorescence result only from hemodynamics, $\Delta F(t) \approx 0$

permitting simplification of equation 7:

211
$$\frac{\Delta I_F(x, y, t)}{\bar{I}_F(x, y)} \approx S_1(x, y) \frac{\Delta I_2(x, y, t)}{\bar{I}_2(x, y)} + S_2(x, y) \frac{\Delta I_2(x, y, t)}{\bar{I}_2(x, y)}. \tag{8}$$

212 From equation 8, we can solve for the coefficients (S_1 and S_2) by pixel-wise linear regression of $\Delta I_F / \bar{I}_F$

213 onto $\Delta I_1 / \bar{I}_1$ and $\Delta I_2 / \bar{I}_2$. The effectiveness of this approach is evaluated via the remaining fluorescence

214 intensity, $f(x, y, t)$

215
$$f(x,y,t) = \frac{\Delta I_F(x,y,t)}{\bar{I}_F(x,y)} - S_1(x,y)\frac{\Delta I_1(x,y,t)}{\bar{I}_1(x,y)} - S_2(x,y)\frac{\Delta I_2(x,y,t)}{\bar{I}_2(x,y)}. \tag{9}$$

$f(x,y,t)$ is expected to approximate $\Delta F(x,y,t)/\bar{F}(x,y)$, so that for GFP mice $f \ll \Delta I_F/\bar{I}_F \approx 0$. Hence,

linear regression with two variables can account for fluorescence variance due to hemodynamics

independently for each pixel, in the absence of calcium-dependent variance. Changes in the corrected

fluorescence decline towards zero as performance of the regression model approaches the limit of

complete separation.

When applied to GFP fluorescence, the regression model improved on the performance of the Beer-

Lambert model. Averaging across all pixels, the median remaining variance across pixels, averaged

across mice, was 0.08 ± 0.03 in 3 Cux2-Ai140 mice, 0.05 ± 0.02 in 3 Rorb-Ai140 mice and 0.10 ± 0.05 in

5 Ntsr1-Ai140 mice (figure 3D), ~60-70% reduction in remaining variance relative to the Beer-Lambert

model. Regression produced uniformly good correction across most of the brain, with the improved

performance being particularly noticeable over large vessels, along the midline and towards the edges of

the brain, where the Beer-Lambert correction was poor (figure 3A). The large, fast putative movement- or

posture-related hemodynamic transients along the midline were largely eliminated by spatially-detailed

regression (figure 3B). We conclude that pixelwise regression using two backscatter measurements offers

improved separation of hemodynamics from changes in indicator fluorescence, likely because regression

enables the model to account for differences in optical properties across the brain.

Interestingly, the mean regression coefficients required for optimal correction differed between mouse

lines. Regression coefficients for Cux2-Ai140 and Rorb-Ai140 were clustered (figure 3E), perhaps

because of their common GFP expression in pyramidal apical dendrites that ramify through layers 1-3.

Coefficients were noticeably different for Ntsr1-Ai140 mice, with expression in layer 6 pyramidal

neurons. These differences are consistent with the idea that optical properties such as fluorescence mean

path lengths differ between mouse lines and need to be adjusted for optimal separation.

Single-wavelength linear regression

Single-wavelength regression has often been used to separate hemodynamics from changes in

indicator fluorescence. Generally, single-wavelength regression employs backscatter at an isosbestic

wavelength such as 530 nm or 577 nm. Consequently, one might expect single-wavelength regression to

best account for changes in total hemoglobin concentration (Frostig *et al.*, 1990) but not changes in blood

oxygenation. Again, we used the same data set to compare the performance of single- and two-

wavelength regression.

We regressed the 577 nm backscatter measurement against GFP fluorescence, pixelwise:

$$\frac{\Delta I_F(x, y, t)}{\bar{I}_F(x, y)} \approx S_1(x, y) \frac{\Delta I_1(x, y, t)}{\bar{I}_1(x, y)}. \tag{10}$$

The remaining variance after 577nm single-wavelength regression was 0.13 ± 0.06 in 3 Cux2-Ai140

mice, 0.09 ± 0.03 in 3 Rorb-Ai140 mice and 0.24 ± 0.09 in 5 Ntsr1-Ai140 mice (figure S3), ~2-3 times

more remaining variance than two-wavelength regression and comparable to the Beer-Lambert model.

Unlike the Beer-Lambert model, 577 nm single-wavelength regression performed reasonably well across

most pixels (figure S3A), underlining the importance of allowing for differences in optical properties by

tuning the model at each pixel. Overall, the performance of 577 nm single-wavelength regression was

intermediate between that of the Beer-Lambert and two-wavelength regression models.

A simplified 577 nm single-wavelength regression model using a coefficient of 1 at all pixels (Xiao *et*

al., 2017) left remaining variance of 0.20 ± 0.07 in 3 Cux2-Ai140 mice, 0.21 ± 0.03 in 3 Rorb-Ai140

mice and 0.43 ± 0.03 in 5 Ntsr1-Ai140 mice ("577nm Ratiometric Demixing", figure S3). Like other

models not tuned pixelwise, correction was particularly poor over large vessels, along the midline and

towards the edges of the hemispheres. However, pixelwise regression is no guarantee of performance: 630

nm single-wavelength pixelwise regression offered poor performance with remaining variance of $0.84 \pm$

0.10 in 3 Cux2-Ai140 mice, 0.61 ± 0.04 in 3 Rorb-Ai140 mice and 0.68 ± 0.15 in 5 Ntsr1-Ai140 mice

(figure S3).

A Spatial Model to predict regression coefficients in GCaMP mice

Tuning a regression model at each pixel improves performance in many brain areas, but how can we

generate pixel-wise coefficient maps in GCaMP mice? In GFP mice, we found coefficients by regressing

changes in backscatter intensity against changes in fluorescence at each pixel, under the assumption that

changes in fluorescence were due to hemodynamics. This assumption is not valid for GCaMP mice

because hemodynamics correlate with neuronal activity, so direct regression is not an option. Instead we

developed a 'Spatial Model' that predicts regression coefficients at each pixel using features of

backscatter and fluorescence images that can be measured in GCaMP mice. We trained and validated the

performance of this Spatial Model on images from GFP mice and applied the model to GCaMP mice.

The Spatial Model uses several statistical projections (e.g. stdev, skew or kurtosis) of backscatter and

fluorescence images to predict coefficient maps (figure 4C). We regressed primary coefficient maps from

GFP animals onto 19 statistical projections (figure S4) to determine the weighting of features (table S1)

that best predicted the regression coefficients. We tested the performance of the Spatial Model in 2 stages.

First, we trained and tested spatial weights from the same GFP mouse to reveal the performance limit of

the spatial model. Remaining variance, averaged across all pixels, was 0.14 ± 0.03 in 3 Cux2-Ai140 mice,

0.08 ± 0.03 in 3 Rorb-Ai140 mice and 0.21 ± 0.08 in 5 Ntsr1-Ai140 mice (figure 4A), close to the

performance of the regression model. Second, we used leave-one-animal-out cross-validation to generate

mean spatial weights for each mouse line (table S1) and applied these mean spatial weights to generate

coefficient maps and separate hemodynamics and changes in indicator fluorescence in the left out (test)

mouse. This second test replicates the procedure that will be later employed in GCaMP mice in which

spatial weights estimated from GFP mice are applied to GCaMP mice. The median remaining variance of

all pixels in this second test, averaged across animals, was 0.14 ± 0.03 in 3 Cux2-Ai140 mice, 0.08 ± 0.03

in 3 Rorb-Ai140 mice and 0.21 ± 0.08 in 5 Ntsr1-Ai140 mice. Hence in all three mouse lines, the

remaining variance was greater than with the two-wavelength regression model (that cannot be directly

applied to GCaMP mice) but less than the remaining variance of the Beer-Lambert model (that can be

applied to GCaMP mice). Much of the improvement in performance of the Spatial Model over the Beer-

Lambert model is near vessels and along the midline. Hence, we expect the Spatial Model to offer

improved separation of hemodynamics and changes in indicator fluorescence versus the Beer-Lambert

model when applied to GCaMP mice, particularly for cortical areas along the midline and near large

vessels.

Separation of hemodynamics from changes in indicator fluorescence in GCaMP mice

We used the spatially-detailed regression model to separate hemodynamics from changes in indicator

fluorescence in Cux2-Ai148 mice, with GCaMP6f in superficial pyramidal neurons. We trained the

Spatial Model on GFP mice and then applied the resulting coefficient maps to genetically-matched

GCaMP6 mice (Cux2-Ai140 vs Cux2-Ai148 mice, etc.). During spontaneous activity, variance was

sometimes increased, and at other times reduced, especially during fast changes in fluorescence during

events along the midline (figure 5A). During presentation of a visual stimulus, the vasodilatory sag was

reduced, in GFP (figure 5B) and in GCaMP mice (figure 5C) and the baseline overshoot was eliminated.

In the GCaMP results, the difference between original and corrected traces was similar in amplitude and

time course to the change in measured fluorescence in GFP mice, consistent with successful separation of

hemodynamics and changes in indicator fluorescence in GCaMP mice.

DISCUSSION

We quantified the effects of hemodynamics on fluorescence measured from GFP mice with widefield

fluorescence imaging and the performance of several models in separating hemodynamics from changes

in indicator fluorescence. Previous methods have used physical models of light scattering and absorption

(Malonek and Grinvald, 1996; Berwick *et al.*, 2005; Hillman *et al.*, 2007, Devor *et al.*, 2012), leveraging

research on tissue absorbance spectra (Takatani and Graham, 1979; Wray *et al.*, 1988), endogenous

fluorophores (Zipfel *et al.*, 2003), and models of scattering in tissue (Kohl *et al.*, 2000). Correction

strategies based on physical parameters, such as the Beer-Lambert model, may overgeneralize and not

account for unique features in cranial windows, or tissue heterogeneities such as surface vasculature. One

might expect separation models based on physical parameterization to perform poorly in some locations.

One advantage of regression models is that they can account for pixelwise differences in optical

properties. We found that the Beer-Lambert model removed most, but not all hemodynamic effects and

poor separation was common near surface blood vessels. Regression against two backscatter wavelengths

out-performed the Beer-Lambert model, with outperformance being particularly noticeable near blood

vessels. Pixelwise tuning of the model was likely the basis for this outperformance.

Central to our approach is the linearization of the Beer-Lambert equation. The resulting linear model

cuts through the complexity of trying to estimate the spectral integrals of pathlengths and extinction

coefficients of the Beer Lambert equation by simplifying the problem to a linear estimation of two

variables.

The performance of single-wavelength regression was similar in some respects to that of the Beer-

Lambert model. Both performed adequate correction at many pixels, but poorly near blood vessels. The

Beer-Lambert model requires two backscatter measurements and, therefore, either two backscatter

cameras or multiplexed measurements on a single camera, making single-wavelength regression

considerably easier to implement.

Regression against two backscatter wavelengths out-performed other models, eliminating >90% of

variance in most GFP mice. In GCaMP mice, using the Spatial Model, residual variance was ~0.1-0.2.

Hence correction is not perfect, but is close to the expected limit of ~0.05 remaining variance after

removal of all hemodynamic effects. Residual variance ~0.1 above the expected limit corresponds to

~95% reduction in the amplitude of the mean hemodynamic transient ($0.9^{1/2}$), meaning that a large

midline hemodynamic artifact that initially caused a 10% change in apparent $\Delta F/F$ in a GCaMP mouse

would be attenuated to ~0.5% $\Delta F/F$ after application of the Spatial Model. The Spatial Model does not

completely remove hemodynamic effects from fluorescence traces in GCaMP mice, but typically reduces

the amplitudes of apparent changes in fluorescence to close to little the noise of GCaMP measurements.

One important caveat is that we considered hemodynamic variance at <5 Hz, to avoid aliasing the

heart-rate oscillations at ~8-12 Hz. One result is that fast transients often observed along the midline were

not always fully corrected by the Spatial Model. We fully expect that midline transients and heart-rate

signals would be effectively corrected by our method by pushing camera acquisition to higher frame rates.

The method to build statistical maps of backscatter data in the Spatial Model could also potentially be

improved by using alternate methods for spatial feature extraction such as using deep-learning techniques

trained on the primary coefficient maps. Similarly, it is possible that non-linearities, such as fitting time-

varying regression coefficients, could form the basis for future improvements in hemodynamic demixing,

but the margin for further improvement appears small since the Spatial Model accounts for most

hemodynamic effects on fluorescence.

An alternative to using backscatter measurements is to stimulate GCaMP with ultra-violet light (~410

nm) where GCaMP fluorescence is not calcium-dependent. This approach directly measures and corrects

for changes in GCaMP emission (but not excitation), presumably caused by hemodynamics. We found

this strategy to be effective over short time periods, but phototoxicity is a concern with ultra-violet

illumination. In addition, the very shallow penetration of 410nm light (estimated mean scattering

pathlength is ~8μm) may limit the performance of this approach for correcting for the absorption of

fluorescence from deep in tissue.

We quantified model performance in GFP mice because we lack the tools to measure the ground truth

calcium signal at all cortical locations simultaneously in GCaMP mice. We then developed the Spatial

Model to permit separation of hemodynamics and changes in indicator fluorescence. Our strategy used

genetically-matched GFP and GCaMP mice, made no assumptions regarding the source of the

fluorescence variance, and was effective when applied to several GCaMP lines. Our strategy has

drawbacks. It requires experiments in GFP and GCaMP mice with matched expression and, lacking

ground truth, it cannot provide a direct measure of separation performance.

We propose that experimenters consider different strategies for minimizing the effects of

hemodynamics on widefield fluorescence measurements. The use of longer-wavelength indicators, such

as RCaMPs, will reduce the effects of hemodynamics, but GCaMP indicators are in more widespread use.

With blue-green indicators, options include the Beer-Lambert model, single-wavelength regression and

our Spatial Model. Which offers the optimal balance of performance and experimental complexity will

depend on several factors, including the proximity of the cortical areas of interest to blood vessels, the

extent to which behavior and hemodynamic effects on fluorescence are coupled (best measured in GFP

mice), the number of cameras available and extent to which they can be synchronized, the frequency band

in which the fluorescence signals of interest occur, and the availability of transgenic or viral resources to

produce matched GFP and GCaMP expression.

METHODS

Animals and surgical preparation

We used six mouse lines, from crossing three Cre driver lines with two reporter lines.

Cre lines:

  Rorb-IRES-Cre, RRID:IMSR_JAX:023526, Harris *et al.* (2014).

  Cux2-CreERT2, RRID:MMRRC_031778-MU, Franco *et al.* (2012).

  Ntsr1-Cre_GN220, RRID:MMRRC_030648-UCD, Gong *et al.*, (2007).

Reporter lines:

  Ai140, RRID:IMSR_JAX:030220, Daigle *et al.* (2018).

  Ai148, RRID:IMSR_JAX:030328, Daigle *et al.* (2018).

Crosses were made between animals hemizygous for ai140 or ai148, and animals that were either hemi or homozygous for Cre. We refer to these crosses using abbreviations: Cux2-Ai140, Rorb-Ai140, Ntsr1-Ai140, Cux2-Ai148, Rorb-Ai148, Ntsr1-Ai148.

  For Cux2-CreERT2 animals, tamoxifen was administered via oral gavage (50 mg/ml in corn oil) at 0.2 mg/g body weight for 3-5 days. Mice were used for experiments a minimum of two weeks following induction.

  Wide-field imaging was performed on 7-30 week-old male and female mice through intact skull using a modification of the method of Silasi *et al.* (2016). Under isoflurane anesthesia, the skull was exposed and cleared of periosteum, and a #1.5 borosilicate coverslip (Electron Microscopy Sciences, #72204-01) was fixed to the skull surface with a layer of clear Metabond (Sun Medical Co.). A 3D-printed light shield was fixed around the coverslip using additional Metabond, and the outward-facing surfaces were coated with an opaque resin (Lang Dental Jetliquid, MediMark). A custom titanium headpost was fixed posterior to the lightshield/coverslip and dorsal to the cerebellum using Metabond.

  Animal experiments were performed in accordance with the recommendations in the Guide for the Care and Use of Laboratory animals of the National Institute of Health. All animals were handled according to institutional animal care and use committee protocols of the Allen Institute for Brain Science, protocol numbers 1408 and 1705.

Image acquisition and initial image processing

  Mice were head-restrained and free to run on a 16.5 cm diameter disk. With exception of experiments with visual stimulation, mice were in the dark and spontaneously active. Visual stimuli were displayed on a 27" LCD monitor placed 13.5 cm from the right eye and consisted of high-contrast gabor gratings spanning 20 degrees of the visual field, positioned at the center of the visual field. Images were presented at 0.25 Hz and averages were made from a minimum of 50 stimulus presentations.

Images were produced by a tandem-lens macroscope of custom optomechanical design (figure S5) built

around a pair of identical lenses (Leica 10450028). Epifluorescence illumination used a 470 nm LED

(Thorlabs M470L3) filtered (Semrock FF01-474/27-50) and reflected by a dichroic mirror (Semrock

FF495-Di03-50 × 70) through the objective lens. Backscatter illumination in yellow used a LED

(Thorlabs M565L3) and a bandpass filter (Semrock F01-578/21), and backscatter illumination in red used

a LED (Thorlabs 625L3). Yellow and red illumination was focused onto a 1-to-7 fan-out fiber bundle

(Thorlabs BF72HS01), and the termination of each of the seven fibers was uniformly spaced

circumferentially around a custom light shield surrounding the imaging objective with each fiber

terminating at 45 degrees incident to the brain surface. Fluorescence emission was separated from the two

backscatter wavelengths using a dichroic beamsplitter (Semrock, FF560-FDi01-50x70) and passed

through an emission filter (Semrock FF01-525/45-50) to a camera while backscatter passed through a

high-pass filter (Edmund Optics Y-50, 500nm) to a second camera.

Image acquisition used two Hamamatsu Flash4.0 v3 sCMOS cameras. One camera used for detection

of fluorescence operated with 10 ms rolling shutter exposure (100 Hz), and the second which detected

backscatter received triggered exposures at 50Hz. We used 4 illumination and detection wavelength

bands: fluorescence excitation, fluorescence emission, backscatter at ~577 nm and backscatter at ~630

nm. We measured the spectrum of each band with a spectroradiometer (SpectroCAL, Cambridge

Research Systems). The mean wavelengths of our four bands were 472, 522, 577 and 630 nm. Backscatter

measurements centered at 577 and at 630 nm were interleaved with a blank frame (for calculation of

fluorescence bleed-through) and thus the final sample rate for each channel on the backscatter camera was

50/3 ~= 17 Hz.

Analysis was performed using Matlab (v2018a, Mathworks) or Python 2.7. Images were spatially

down-sampled from 2048 x 2048 to 128 x 128 pixels by averaging. A camera offset of 100 counts was

subtracted and camera counts converted to photo-electrons (2.19 counts per photo-electron). Backscatter

signals, acquired at 17 Hz, were filtered with a 5 Hz Butterworth low pass filter to prevent aliasing of the

heart beat and were then up-sampled to 100Hz, and spatially and temporally aligned to the 100 Hz

fluorescence signal.

Calculation of remaining variance was made with pixelwise normalization to initial variance. To

account for its skewness, we took the median of the distribution of remaining variance across pixels to

represent the remaining variance in each mouse and averaged across all mice of a genetic background. In

GFP mice, the shot noise floor was substantially reduced by the spatial averaging and was 0.5 % of the

initial variance.

Beer-Lambert model

For Beer-Lambert calculations, we obtained extinction coefficients from tabulated hemoglobin spectra

(http://omlc.ogi.edu/spectra/hemoglobin/summary.html), and path lengths from Monte Carlo simulations

(Ma *et al.*, 2016a). For each wavelength band, we numerically solved the integral of the path lengths,

using the measured spectra of the fluorescence and backscatter wavelength bands (Appendix, equation

11), and tabulated GFP excitation and emission spectra (http://www.tsienlab.ucsd.edu/Documents.htm).

The approximations used in what we term the Beer-Lambert, and Simplified Beer-Lambert models are

described in detail in the appendix.

Regression model

We used either 577nm, 630nm or both channels of backscatter data and calculate the weights at each pixel

that best fit fluorescence from a GFP-expressing animal using ordinary least-squares. Alternatively, these

primary weights were estimated using the Spatial Model which consists of 19x2 secondary weights (table

S1) generated by separately fitting 19 statistical projections of backscatter and fluorescence data (see

figure S4) onto the 577nm and 630 primary weightings. A detailed examination of the relationship

between the Beer-Lambert and regression models is given in the appendix.

Matlab code to train and test Spatial Models, and perform all variants of regression and Beer-Lambert

demixing is available online: https://github.com/MichaelGMoore/MultiChanHemo

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Fig 1. Hemodynamics in GCaMP and GFP mice.

(A) Fluorescence during a five second presentation of a drifting grating. Left, fluorescence through time from a pixel in visual cortex (red marker in image). Right, image of peak fluorescence at each location. (B) Left, time-series from a Cux2- Ai140 (GFP) mouse showing mixed GCaMP and hemodynamic responses following the same stimulus. Right, fluorescence in a GFP animal 150-200 ms after stimulation. (C) Left, time-course of spontaneous activity in a GCaMP6f mouse highlighting two pixels on and off the midline vasculature. Right, image of the signal from the time indicated (red dots, left panel). (D) Same as panel C, for a GFP mouse. Image scale-bars = 2 mm.

Fig 2. Simultaneous measurement of GCaMP fluorescence and hemodynamics.

(A) Absorption spectra of oxy- and deoxyhemoglobin (HbO and HbR; left axis) in the visible spectrum, the HbO/HbR extinction coefficient ratio (right axis), and normalized spectra of wavebands used in our experiments. (B) Schematic illustration of strategy to estimate absorption of GCaMP excitation and emission (centered at ~470 and ~520 nm, respectively) and of illumination at ~577 and ~630 nm by hemoglobin. Blue illumination is susceptible to absorption when in transit from the LED to the neurons expressing GCaMP. Green fluorescence emission is susceptible to absorption while in transit from GCaMP molecules to the fluorescence camera. 577 and 630 nm illumination are susceptible to absorption during entry and during exit from the brain, before and after the scattering events that result in diffuse reflection. (C) Schematic illustration of simultaneous fluorescence and backscatter measurements, with relative locations and wavelength characteristics of LED sources, filters, lenses, dichroic mirrors and cameras (see figure S5 for a rendering of the microscope assembly). Camera frame interleaving sequence (inset, upper left) shows the continuous acquisition of fluorescence on camera 1, and strobing between detection of 577nm or 630nm backscatter and a blank frame on camera 2.

Fig 3. Comparison of models to explain variance in GFP mice.

(A) Map of variance from a Cux2-Ai140 (GFP) mouse (top) and of remaining variance after correction using two models. Numbered dots indicate locations from which traces were extracted for panel B. (B) Example traces of fluorescence (black traces) from two example pixels (dots, panel A) and corrected fluorescence from the Beer-Lambert model (grey traces) and from dual wavelength linear regression model (yellow traces). C) Laminar expression patterns in visual cortex of Cux2-Ai140, Rorb-Ai140 and Ntsr1- Ai140 mice. Dashed lines mark the dorsal surface of cortex (top), and the ventral white-matter border of cortex. (D) Summary of variance remaining after correction (averaged across cortical surface) from three Cre lines. Bars represent mean ± STD. 3 Cux2- Ai140 mice, 3 RorbAi140 mice, 5 Ntsr1-Ai140 mice. (E) Distribution of regression coefficients for Ai140 mice, fit with 577nm and 640nm backscatter data. Using estimated parameters (path length and extinction coefficients) similar but spatially-uniform coefficients can be calculated using the Beer-Lambert relationship (grey cross, see appendix for details). Points and error bars represent median ± quartiles from all pixels in the image.

Fig 4. Evaluation of the Spatial Model.

(A) Map of variance from a Cux2-Ai140 (GFP) mouse (top) and of remaining variance after correction

using the Spatial Model using averaged parameters generated during across-animal leave-one-out cross-

validation (Spatial Model CV), and the two-wavelength regression model. Numbered dots indicate

locations from which traces were extracted for panel B. (B) Example traces of fluorescence (black traces)

from two example pixels (dots, panel A) and of corrected fluorescence from Spatial Model CV and from

dual wavelength linear regression model (yellow traces). (C) Left, coefficient maps generated using

spatially-detailed regression of GFP fluorescence onto 577 nm and 630 nm backscatter. Right,

reconstructions of coefficient maps (from held-out data) using the Spatial Model. (D) Comparison of

remaining variance across models. Mean ± standard deviation across all animals, where the median

remaining variance is taken across all pixels for each animal.

Fig 5. Demixing hemodynamic responses to a visual stimulus in GFP and GCaMP mice.

(A) Spontaneous activity from a Cux2-Ai148 (GCaMP6f) mouse and correction with Beer-Lambert

Model and Spatial Model. Left, images of fluorescence at a single time point, during midline activity

(asterisk, traces). Right, ΔF/F traces for two pixels (images, left) before (black) and after correction with

Beer-Lambert Model (grey) and Spatial Model (purple). (B) Left, map of mean ΔF/F 1.5-2 seconds post

stimulus. 100 ms flashed visual stimulus to the right eye. Cux2-Ai140 (GFP) mouse. Right, raw trace

(black) and trace after Spatial Model correction (purple) extracted from a pixel in V1 (red dot, left). (C)

Left, map of mean ΔF/F 1.5-2 seconds post stimulus. 100 ms flashed visual stimulus to the right eye.

Cux2-Ai148 (GCaMP6f) mouse. Right, raw trace (black) and trace after Spatial Model correction (purple)

extracted from a pixel in V1 (red dot, left).

687   *Fig S1*. ***Relative brightness of GFP mice.***

688   Image brightness, in mean photoelectrons, calculated from 10x10 pixel regions (65.0 µm^2) over medial

689   somatosensory cortex from 3 Cux2-Ai140, 3 Rorb-Ai140 and 5 Ntsr1-Ai140 mice. Olfactory bulb

690   measurements were taken to represent the background photon count, including tissue autofluorescence,

691   skull autofluorescence, and light leak.

Fig S2. Sensitivity of Beer-Lambert model to changes in path length.

The median remaining variance of all pixels across the brain from a single Cux2-Cre;Ai140 mouse while

changing one mean path length in the Beer-Lambert model. The sensitivity of model performance to each

path length was evaluated with all other parameters (including other path lengths) constant. Path lengths

values used elsewhere in the paper are marked with dotted lines: 260μm (GFP excitation), 270μm (GFP

emission), 280 μm (577nm backscatter), 3.85mm (630nm backscatter).

Fig S3. ***Detailed comparison of all models against GFP results.***

(A) Map of variance from a Cux2-Ai140 (GFP) mouse (top), and maps of remaining variance after

correction using 5 models. (B) Example traces of spontaneous activity and corrected traces from two

example pixels (dots, left). Raw data was corrected using five methods: Simplified Beer Lambert (see

supplemental appendix), Ratiometric demixing ((1+dF/F) / (1+dR$_{577nm}$/R$_{577nm}$)), Beer-Lambert demixing

(see supplemental appendix), 577nm regression (Eq. 9 omitting the term for S$_2$), and 577nm + 640nm

regression (Eq. 9). (C) Summary of key differences between how coefficients are generated in the five

models. (D) Summary of variance remaining after correction (averaged across cortical surface) from three

Cre lines. Bars in D represent mean ± STD. 3 Cux2-Ai140 mice, 3 Rorb- Ai140 mice, 5 Ntsr1-Ai140

mice.

Fig S4**. **Maps of Spatial Model regressors.

(A) 19 different projections of backscatter data (or fluorescence data for Laplacian maps) were used as

regressors in the Spatial Model to predict coefficient maps from GFP-expressing mice. Statistical maps

are: the L1 norm of $\Delta I_1/\bar{I}_1$ and its square, the L2 norm (standard deviation) of $\Delta I_1/\bar{I}_1$ and its square, the

L1 norm of $\Delta I_2/\bar{I}_2$ and its square, the L2 norm of $\Delta I_2/\bar{I}_2$ and its square, the skewness of the 577nm and

630nm signals, the kurtosis of the 577nm and 630nm signals, the covariance of $\Delta I_1/\bar{I}_1$ and $\Delta I_2/\bar{I}_2$, the

Laplacian maps. Images from a Cux2-Ai140 mouse.

	577 L1^1	577 L1^2	577 L2^1	577 L2^2	630 L1^1	630 L1^2	630 L2^1	630 L2^2	577 skew^1	630 skew^1	577 kurt^1	630 kurt^1	577/630 cc^1	Lap 1	Lap 2	Lap 4	Lap 8	Lap 16	Lap 32	Mean
Cux2 577	-0.704	0.401	0.281	-0.095	-2.999	0.565	3.166	-0.524	-0.006	-0.049	-0.058	-0.295	0.023	-0.022	0.026	-0.001	0.024	0.238	0.098	1.443
Cux2 630	-0.416	0.204	0.340	-0.172	-0.573	-0.435	0.892	0.221	-0.056	-0.075	-0.053	-0.025	-0.013	0.046	-0.066	0.129	-0.398	0.162	0.071	-0.850
Rorb 577	-2.091	0.161	1.146	0.468	1.016	-2.041	-1.334	2.401	0.082	-0.023	-0.094	-0.121	-0.140	0.016	-0.059	-0.113	0.489	-0.075	0.109	1.600
Rorb 630	0.583	0.936	-0.435	-1.148	0.916	-0.845	-0.503	0.693	-0.140	-0.138	0.050	0.089	-0.059	0.031	-0.048	0.272	-0.760	0.222	0.201	-0.832
Ntsr1 577	6.668	-4.153	-7.559	4.855	-1.988	0.646	1.978	-0.578	-0.040	-0.052	0.170	-0.348	-0.027	0.032	-0.194	0.455	-0.633	0.642	0.010	1.981
Ntsr1 630	1.118	-0.186	0.167	-0.612	5.967	-2.082	-5.601	1.884	0.014	-0.156	0.124	0.585	-0.039	0.143	-0.236	0.574	-1.555	1.083	-0.112	-1.729

758
759
760 ***Supplementary Table 1. Tabulated coefficients for the Spatial Model.***

761 Weights for all spatial-coefficients, each representing the mean weight for the mouse line.

763
764 ***Fig S5. Custom widefield optics system.*** A modular filter-cube was designed to align cameras, objectives
765 and 2" optics (see also fig 2C for schematic of the optical system). Radial off-axis illumination of mouse
766 cortex for backscatter imaging used a custom light-shield receiving seven LED-coupled optical fibers
767 (LEDs not shown), while epiflourescence excitation enters through the open port in the bottom cube.

773 **APPENDIX**

774 *Derivation of the Beer-Lambert and Regression models*

775 A coarse-grained hemodynamic model for the fluorescence intensity recorded from a single pixel, $I_F(t)$,

776 based on the Beer-Lambert Law and general principles of incoherent optical processes, can be written in

777 compact form as

778
$$I_F(t) = F(t)T_{em}\big(\boldsymbol{c}(t)\big)T_{ex}\big(\boldsymbol{c}(t)\big)I_{ex}^S, \tag{A1}$$

where $F(T)$ is the coarse-grained intrinsic activation level of the fluorophores averaged over the PSF

of the pixel, $T_{em}\big(\boldsymbol{c}(t)\big)$ is the transmittance factor for the light emitted by the fluorophores, $T_{ex}\big(\boldsymbol{c}(t)\big)$ is

the transmittance factor for the excitation light, and I_{ex}^S is the excitation source intensity at the specific

pixel. The transmittances depend on the oxygenated and deoxygenated hemoglobin concentrations,

$C_{HbO}(t)$ and $C_{HbR}(t)$, respectively, can be combined into a 2-component vector, $\boldsymbol{c}(t) =$

$[C_{HbO}(t), C_{HbR}(t)]$. Likewise, the recorded intensity of the bth backscatter channel can be expressed

785
$$I_b(t) = T_b\big(\boldsymbol{c}(t)\big)I_b^S, \tag{A2}$$

786 where $T_b\big(\boldsymbol{c}(t)\big)$ is the round-trip transmittance, and I_b^S is the corresponding source intensity.

787 The transmittance factors, $T_\mu\big(\boldsymbol{c}(t)\big)$, where $\mu \in \{em, ex, b\}$. can be written as

788
$$T_\mu = \mathcal{G}_\mu \int d\lambda \, dx \, X_\mu(x|\lambda)P_\mu(\lambda)e^{-x\,c(t)\cdot e(\lambda)}, \tag{A3}$$

where $\mathcal{G}_\mu$ contains any geometric factors for the corresponding process, $X_\mu(x|\lambda)$ is the distribution

over optical path lengths for a given wavelength, λ, and $P_\mu(\lambda)$ is the distribution over wavelengths for the

process, including source spectra, filters, and fluorophore excitation/emission spectra, as required. While

traveling along a given path, the light is subject to absorption by hemoglobin, in accordance with the

Beer-Lambert Law. This is described by the exponential factor in equation 3, which contains the path-

length, x, the hemoglobin concentrations, $c(t)$ and $e(\lambda) = [E_{HbO}(\lambda), E_{HbR}(\lambda)]$, a two-component

vector containing the corresponding hemoglobin molar-extinction coefficients for wavelength λ.

The model has 3 dynamic variables, $F(t)$, $C_{HbO}(t)$, and $C_{HbR}(t)$, which can be expressed in terms of

mean-values and deviations as $F(t) = \bar{F} + \Delta F(t)$ and $C_v(t) = \bar{C}_v + \Delta C_v$, where $v \in \{HbO, HbR\}$. In the

limit where the deviations are small compared to the mean values, as is often the case with wide-field

calcium imaging using bright indicator dyes, we can linearize the equations relating the observed

intensities to the intrinsic variables. Linearization permits simplification by eliminating some variables.

To linearize equations (1) and (2), we first express the intensities as a mean value plus deviation, $I_F(t) =$

$\bar{I}_F + \Delta I_F(t)$, and $I_b(t) = \bar{I}_b + \Delta I_b(t)$. This leads to

803
$$\bar{I}_F + \Delta I_F = (\bar{F} + \Delta F)\, T_{em}(\bar{c} + \Delta c)\, T_{ex}(\bar{c} + \Delta c)\, I_{ex}^S, \tag{A4}$$

804
$$\bar{I}_b + \Delta I_b = T_b(\bar{c} + \Delta c)\, I_b^S. \tag{A5}$$

805 The transmittances can be expanded to first-order in terms of the hemoglobin fluctuations as

806
$$T_\mu(\bar{c} + \Delta c) \approx T_\mu(\bar{c}) + \left(\frac{\partial T_\mu(\bar{c})}{\partial \bar{C}_{HbO}}\right)\Delta C_{HbO} + \left(\frac{\partial T_\mu(\bar{c})}{\partial \bar{C}_{HbR}}\right)\Delta C_{HbR}. \tag{A6}$$

807 Inserting this expansion into equations (4) and (5), and equating the zeroth order terms with respect to
808 the fluctuations gives the mean intensities
809
$$\bar{I}_F \approx \bar{F}\, T_{em}(\bar{c})\, T_{ex}(\bar{c})\, I_{ex}^S, \tag{A7}$$

810
$$\bar{I}_b \approx T_b(\bar{c}) I_b^S. \tag{A8}$$

811 Similarly, equating first-order terms, and dividing by the mean gives

812
$$\frac{\Delta I_F(t)}{\bar{I}_F} = \frac{\Delta F(t)}{\bar{F}} + \left(M_{em,HbO} + M_{ex,HbO}\right)\Delta C_{HbO}(t) + \left(M_{em,HbR} + M_{ex,HbR}\right)\Delta C_{HbR}(t), \tag{A9}$$

813
$$\frac{\Delta I_b(t)}{\bar{I}_b} = M_{b,HbO}\,\Delta C_{HbO}(t) + M_{b,HbR}\,\Delta C_{HbR}(t), \tag{A10}$$

814 with

815
$$M_{\mu,\nu} = \frac{1}{T_\mu(\bar{c})}\left(\frac{\partial T_\mu(\bar{c})}{\partial \bar{C}_\nu}\right) = -\frac{\int d\lambda\; dx\, X_\mu(x|\lambda)P_\mu(\lambda)e^{-x\,\bar{c}\cdot e(\lambda)}x E_\nu(\lambda)}{\int d\lambda\; dx\, X_\mu(x|\lambda)P_\mu(\lambda)e^{-x\,\bar{c}\cdot e(\lambda)}}, \tag{A11}$$

where again $\mu \in \{em, ex, b\}$ and $\nu \in \{HbO, HbR\}$.
The spectral distributions for the light-sources for the fluorescence indicators and for the camera
acceptance filters are readily obtained, as are the hemoglobin molar extinction coefficients. The path
length distributions and mean hemoglobin molar concentrations, on the other hand, can vary from pixel to
pixel and would need to be measured or estimated for each pixel in the field of view.
Because there are two independent hemoglobin components, a minimum of two reflectance channels
are necessary to separate the fluorescence from hemodynamics. With a single fluorescence intensity,
$I_F(t)$, and two backscatter channels, $I_1(t)$ and $I_2(t)$, equation (5) then becomes a pair of backscatter
equations,

825
$$\frac{\Delta I_1(t)}{\bar{I}_1} = M_{1,HbO} \, \Delta C_{HbO}(t) + M_{1,HbR}\Delta C_{HbR}(t),\qquad(A13)$$

826
$$\frac{\Delta I_2(t)}{\bar{I}_2} = M_{2,HbO} \, \Delta C_{HbO}(t) + M_{2,HbR}\Delta C_{HbR}(t).\qquad(A14)$$

827   These equations can be solved for the hemodynamic variables, giving

828
$$\Delta C_{HbO}(t) = \frac{1}{M_{1,HbO}M_{2,HbR} - M_{1,HbR}M_{2,HbO}}\left(M_{2.HbR}\frac{\Delta I_1(t)}{\bar{I}_1} - M_{1,HbR}\frac{\Delta I_2(t)}{\bar{I}_2}\right),\qquad(A15)$$

829
$$\Delta C_{HbR}(t) = \frac{1}{M_{1,HbO}M_{2,HbR} - M_{1,HbR}M_{2,HbO}}\left(-M_{2.HbO}\frac{\Delta I_1(t)}{\bar{I}_1} + M_{1,HbO}\frac{\Delta I_2(t)}{\bar{I}_2}\right).\qquad(A16)$$

830   These results can be inserted into the equation for $\Delta I_F/\bar{I}_F$, giving

831
$$\frac{\Delta I_F(t)}{\bar{I}_F} = \frac{\Delta F(t)}{\bar{F}} + S_1\frac{\Delta I_1(t)}{\bar{I}_1} + S_2\frac{\Delta I_2(t)}{\bar{I}_2},\qquad(A17)$$

832   where the coefficients are given by

833
$$S_1 = \frac{\left(M_{em,HbO} + M_{ex,HbO}\right)M_{2,HbR} - \left(M_{em,HbR} + M_{ex,HbR}\right)M_{2,HbO}}{M_{1,HbO}M_{2,HbR} - M_{1,HbR}M_{2,HbO}},\qquad(A18)$$

834
$$S_2 = \frac{-\left(M_{em,HbO} + M_{ex,HbO}\right)M_{1,HbR} + \left(M_{em,HbR} + M_{ex,HbR}\right)M_{1,HbO}}{M_{1,HbO}M_{2,HbR} - M_{1,HbR}M_{2,HbO}}.\qquad(A19)$$

835   Extending this formalism to the entire image, we arrive at the final formula

836
$$\frac{\Delta F(x,y,t)}{\bar{F}(x,y)} = \frac{\Delta I_F(x,y,t)}{\bar{I}_F(x,y)} - S_1(x,y)\frac{\Delta I_1(x,y,t)}{\bar{I}_1(x,y)} - S_2(x,y)\frac{\Delta I_2(x,y,t)}{\bar{I}_2(x,y)}.\qquad(A20)$$

837   The coefficients, S_1 and S_2, generalize to maps, $S_1(x,y)$ and $S_2(x,y)$, because the mean hemoglobin
838   concentrations and optical path-length distributions can in principle vary from pixel to pixel.
839

Simplified Beer-Lambert Model: path length and wavelength approximation
There are two major approximations that can be used to simplify the calculations of the backscatter
regression coefficients, S_1 and S_2. The first is to replace the distribution over path lengths with a single

characteristic path length, $x_c(\lambda)$. This is accomplished by taking $X(x|\lambda) \to \delta(x - x_c(\lambda))$, where $\delta(x)$ is

the Dirac delta function. The second approximation is to replace the distribution over wavelengths with a

single characteristic wavelength, λ_c, accomplished by taking $P(\lambda) \to \delta(\lambda - \lambda_c)$.

Taking these two approximations together gives

847
$$S_1 = \frac{E_{HbO}(\bar{\lambda}_{em})E_{HbR}(\bar{\lambda}_2) - E_{HbR}(\bar{\lambda}_{em})E_{HbO}(\bar{\lambda}_2)}{E_{HbO}(\bar{\lambda}_1)E_{HbR}(\bar{\lambda}_2) - E_{HbR}(\bar{\lambda}_1)E_{HbO}(\bar{\lambda}_2)}\left[\frac{x_{em}}{x_1}\right]$$

848
$$+ \frac{E_{HbO}(\bar{\lambda}_{ex})E_{HbR}(\bar{\lambda}_2) - E_{HbR}(\bar{\lambda}_{ex})E_{HbO}(\bar{\lambda}_2)}{E_{HbO}(\bar{\lambda}_1)E_{HbR}(\bar{\lambda}_2) - E_{HbR}(\bar{\lambda}_1)E_{HbO}(\bar{\lambda}_2)}\left[\frac{x_{ex}}{x_1}\right], \qquad \text{(A21)}$$

849
$$S_2 = \frac{E_{HbR}(\bar{\lambda}_{em})E_{HbO}(\bar{\lambda}_1) - E_{HbO}(\bar{\lambda}_{em})E_{HbR}(\bar{\lambda}_1)}{E_{HbO}(\bar{\lambda}_1)E_{HbR}(\bar{\lambda}_2) - E_{HbR}(\bar{\lambda}_1)E_{HbO}(\bar{\lambda}_2)}\left[\frac{x_{em}}{x_2}\right]$$

850
$$+ \frac{E_{HbR}(\bar{\lambda}_{ex})E_{HbO}(\bar{\lambda}_1) - E_{HbO}(\bar{\lambda}_{ex})E_{HbR}(\bar{\lambda}_1)}{E_{HbO}(\bar{\lambda}_1)E_{HbR}(\bar{\lambda}_2) - E_{HbR}(\bar{\lambda}_1)E_{HbO}(\bar{\lambda}_2)}\left[\frac{x_{ex}}{x_2}\right], \qquad \text{(A22)}$$

which is the result from (Ma et al. 2016a).

Using our images from GFP mice, we can invalidate this simplification of the Beer-Lambert model

(equations 21, 22) for the wavelengths used in our experiment (see figure S3 for remaining variance).

Using our wavelengths ($\lambda_{ex} = 473.23$ nm, $\lambda_{em} = 519.99$ nm, $\lambda_1 = 577.20$ nm, and $\lambda_2 = 630.30$ nm),

and path lengths (577nm: 280 µm, 630nm: 3.85mm, 472nm: 260µm for one-way fluorophore excitation,

522nm: 270µm for one-way fluorescent emission, Ma *et al.*, 2016a), equation (22) predicts a positive

value for S_2 ($S_1 = 1.0314, S_2 = 0.1289$), whereas after regression our data yields a negative value over

99.53% of pixels (see figure 3E). A positive value for S_2 can only be obtained from Eqs. (21) and (22) for

our wavelengths by taking one of the backscatter path lengths to be negative. Hence this simplification of

the Beer-Lambert model requires the use of path lengths that are not physically plausible.

Spectrally-detailed Beer-Lambert Model

The alternative to the path length and wavelength approximation of the simplified Beer-Lambert model is

to replace the path length distributions with single characteristic path lengths ($X(x|\lambda) \to \delta(x - x_c(\lambda))$

equation 11, but to keep the integral over wavelengths and the exact forms of the various spectral

distributions $P_\mu(\lambda)$. When applied to our data from GFP mice, with the wavelength integrals computed

numerically, this level of approximation results in the correct signs for the backscatter coefficients, S_1 and

S_2, so that it is possible to adjust the path-lengths and obtain agreement between the experimental data

and the Beer-Lambert model. This is the form of the Beer-Lambert model used in this paper (see figure
3).
To compute the coefficients in this manner requires estimates for the background oxy- and deoxy-
hemoglobin concentrations. If the molar concentration of hemoglobin in mouse blood is 2.2 x 10^{-3} mol/L
(Raabe *et al.,* 2011), with a typical oxygenation level of 85%, and a Cortical Blood Volume in mouse
cortex of ~0.04 (Chugh *et al.,* 2008), we arrive at $\acute{C}_{HbO} 7.4 \times 10^{-5}$ mol/L and $\acute{C}_{HbR} 1.3 \times 10^{-5}$ mol/L.
We note that the results are insensitive to these numbers, e.g. the dependence vanishes altogether in the
approximations (21) and (22). Changing the values over the entire plausible range only changes the
resulting coefficients in the third significant figure, hence these reasonable estimates are sufficient.
We apply this to our experimental setup by computing the wavelength integrals in (11) numerically,
using directly measured spectra for the two back-scatter channels, combined with manufacturers spectra
for our GFP filter, and GFP fluorophore spectra from (http://www.tsienlab.ucsd.edu/Documents.htm). We
also use extinction coefficient data from (http://omlc.ogi.edu/spectra/hemoglobin/summary.html), and
estimated path-lengths from (Ma *et al.*, 2016a). This leads to the coefficients (S_1=1.176, S_2=-0.434) which
corresponds closely to the regression coefficients calculated in the absence of physical estimates (figure
3E). This shows that a negative 640nm regression coefficient can be obtained from Beer-Lambert with
positive path-lengths, and results from the details of the wavelength dependence of the extinction
coefficients and path-length data. This is the form of the Beer-Lambert model used in this paper (figure
3).
889
Spatial-Regression Model
Correction of hemodynamics in GCaMP mice presents a challenge for our regression approach because in
these animals the fluorescent signal, $\Delta I_F / \bar{I}_F$, contains an unknown calcium-dependent signal, $\Delta F / \bar{F}$ term
(Eq. (7), main text). Because of neurovascular coupling, the hemodynamic and calcium-dependent terms
are not independent so that a simple regression of $\Delta I_1 / \bar{I}_1$ and $\Delta I_2 / \bar{I}_2$ from $\Delta I_F / \bar{I}_F$ will not yield the true
calcium dynamic signal.
For a GFP mouse, the coefficient maps, $S_1(x,y)$ and $S_2(x,y)$ are obtained by pixel-wise linear
regression of the fluorescence signal onto the backscatter signals. To transfer the obtained maps between
different mice, we first correlate the features in the maps with corresponding features in the individual
brain structures. To do this we constructed a set of *M=19* maps, $M_m(x,y)$, where m $\in$ {1,2, ... M}, from
the backscatter data and fluorescence data. These maps should be chosen so that they do not reflect
calcium dynamics when they are obtained from a GCaMP mouse. Because the data is scaled by the mean-
intensities on each channel before any models are constructed, these maps should also be dimensionless
and not scale with intensity.

The statistical maps we use are: [1-2] the L1 norm of $\Delta I_1/\bar{I}_1$ and its square, [3-4] the L2 norm of
$\Delta I_1/\bar{I}_1$ and its square, [5-6] the L1 norm of $\Delta I_2/\bar{I}_2$ and its square, [7-8] the L2 norm of $\Delta I_2/\bar{I}_2$ and its
square, [9-10] the skewness of the 577nm and 630nm signals, [11-12] the kurtosis of the 577nm and
630nm signals, [13] the covariance of $\Delta I_1/\bar{I}_1$ and $\Delta I_2/\bar{I}_2$. To capture the location of the blood-vessels
independently of the excitation intensity profile, we compute the ratio of a Gaussian-blurred time-
averaged image of the fluorescence emission divided by the time-averaged image itself. Rather than
choose a blurring length-scale arbitrarily, we include maps computed at multiple blurring length-scales.
The remaining 6 maps are blood-vessel maps computed for length scales of 1, 2, 4, 8, 16, and 32 pixels,
respectively (Laplacian maps, figure S4).
We include in our training datasets only those pixels whose fractional variance explained (FVE) is
above a chosen threshold of 75%. This is because a low FVE was found to reflect pixels whose initial
variance is very low, roughly the same as that obtained on high FVE pixels after demixing, so that the
model is fitting noise rather than signal on those pixels.
We constructed three types of Spatial Models: (1) standard Spatial Models, (2) cross-validated Spatial
Models, and (3) Cre line Spatial Models.
Standard Spatial Model: the 19 maps are z-scored across pixels for a single GFP animal and merged
into a $19 \times D_{TRAIN}$ predictor array, P_{TRAIN}, where D_{TRAIN} is the number of pixels in the training set (i.e. FVE
$> .75$). The two direct-regression coefficient maps, S_1 and S_2 for the same set of pixels are merged into a
$2 \times D_{TRAIN}$ response array, R_{TRAIN}, for the same animal. From a linear regression model, $R_{TRAIN} - \langle R_{TRAIN} \rangle =$
$C_{MM} - P_{TRAIN}$, where $\langle \ldots \rangle$ indicates average over pixels, we obtain the 2×19 coefficient array, C_{MM}. We
can then reconstruct the response data as $R_{MM} = C_{MM} \cdot P_{TEST} + \langle R_{TRAIN} \rangle$, where P_{TEST} contains the 19 z-
scored predictors from all pixels in the same animal. R_{MM} is then used to demix the fluorescence from the
animal, so that the remaining variance can be compared to the optimal result obtained by direct
backscatter regression. In this way, we can learn how much error is introduced by the process of
transferring the backscatter-regression coefficient maps onto the 19-map representation.
Cross-validated Spatial-Model: This model is used to test the amount of error caused by transferring
the spatial-model coefficients from one animal to another. For each animal, we again obtain a
reconstructed response array, $R_{MMCV} = C_{MMCV} \cdot P_{TEST} + \langle R_{TRAIN} \rangle$, but here C_{MMCV} is obtained from a training
set consisting of all training pixels (FVE $> .75$) from all other animals in the same Cre line (i.e. the test
animal is excluded from the training data). The testing set then consists of all pixels in the test animal.
Here the differential between remaining variance obtained by demixing the fluorescence signal with R-
$_{MMCV}$ and that obtained via R_{MM} in a the same GFP mouse estimates the error incurred during transfer of
the spatial-model between animals.

Cre-line-wise Spatial Model: Here the training set consists of all training pixels (FVE > .75) in all

animals in a Cre line. The trained model is then expected to be used to construct the backscatter

coefficients for all pixels in a GCaMP mouse. This would represent the best attempt to demix the GCaMP

animal using all available training data from the same Cre line. Error limits would come from the cross-

validated GFP results, with the caveat that in the case of small cohorts, including the additional animal in

the training data will presumably lower the error somewhat, meaning that the cross-validation results are

likely an overestimate of the Spatial Model error.