Seasonal influenza: Modelling approaches to capture immunity propagation.

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Abstract

Seasonal influenza poses serious problems for global public health, being a significant contributor to morbidity and mortality. In England, there has been a long-standing national vaccination programme, with vaccination of at-risk groups and children offering partial protection against infection. Transmission models have been a fundamental component of analysis, informing the efficient use of limited resources. However, these models generally treat each season and each strain circulating within that season in isolation. Here, we amalgamate multiple data sources to calibrate a susceptible-latent-infected-recovered type transmission model for seasonal influenza, incorporating the four main strains and mechanisms linking prior season epidemiological outcomes to immunity at the beginning of the following season. Data pertaining to nine influenza seasons, starting with the 2009/10 season, informed our estimates for epidemiological processes, virological sample positivity, vaccine uptake and efficacy attributes, and general practitioner influenza-like-illness consultations as reported by the Royal College of General Practitioners (RCGP) Research and Surveillance Centre (RSC). We performed parameter inference via approximate Bayesian computation to assess strain transmissibility, dependence of present season influenza immunity on prior protection, and variability in the influenza case ascertainment across seasons. This produced excellent agreement between model and data on the annual strain composition. Parameter fits indicated that the propagation of immunity from one season to the next is weaker if vaccine derived, compared to natural immunity from infection. Projecting the dynamics forward in time suggests that while historic immunity plays an important role in determining annual strain composition, the variability in vaccine efficacy hampers our ability to make long-term predictions.

Introduction

As a significant contributor to global morbidity and mortality, seasonal influenza is an ongoing public health concern. Worldwide, these annual epidemics are estimated to result in about three

to five million cases of severe illness, and about 290,000 to 650,000 respiratory deaths [1]. In England, seasonal influenza inflicts a stark burden on the health system during winter periods, being linked with approximately 10% of all respiratory hospital admissions and deaths [2].

Influenza vaccination can offer some protection against seasonal influenza infection for the individual, while contributing to reduced risk of ongoing transmission via establishment of herd immunity [3, 4]. Influenza vaccines are designed to protect against three or four different influenza viruses; two influenza A viruses (an A(H1N1)pdm09 subtype and A(H3N2) subtype) and either one or two influenza B viruses (covering one or both of the B/Yamagata and B/Victoria lineages). In 2013, 40% of countries worldwide recommended influenza vaccination in their national immunisation programmes, although vaccine uptake varies [5–7].

For England (and elsewhere), the need to deploy updated vaccines on an annual basis means influenza vaccination programmes are costly. Yet, predictions of vaccine impact are difficult due to stochasticity in the annual strain composition, the potential misalignment between vaccine and the dominant co-circulating strains and the interaction between multiple seasons. Analysis informing the efficient use of limited resources is therefore vital, with the use of quality-assured analytical models advocated [8].

The previous ten years have seen the fruitful development of influenza transmission models tied to available real-word and experimental data sources using Bayesian techniques [9–13]. Furthermore, combining parameterised transmission models with health economic evaluations permits assessments of changes to vaccination programmes, providing evidence to inform vaccine policy decisions. An eminent study by Baguelin *et al.* [10] connected virological data from England and Wales to a deterministic epidemiological model within a Bayesian inference framework. The transmission model was subsequently interfaced with a health economic analysis model, leading to the recommendation of introducing a paediatric seasonal influenza vaccination programme in the United Kingdom [14]. Subsequent studies have analysed the effect of mass paediatric influenza vaccination on existing influenza vaccination programmes in England and Wales [15], evaluated cost-effectiveness of quadrivalent vaccines versus trivalent vaccines [16], and cost effectiveness of high-dose and adjuvanted vaccine options in the elderly [17].

Prior modelling studies have typically treated each season and each strain circulating within that season independently. In contrast, a model conceptualisation by Pitman *et al.* [11] had waning immunity for natural infection and vaccination, but considered all type A influenza strains as a sole entity rather than explicitly distinguishing between the two common influenza A subtypes. Here, we present a multi-strain, non-age structured, susceptible-latent-infected-recovered (SEIR) type transmission model for influenza incorporating a mechanism to link prior season epidemiological outcomes to immunity at the beginning of the following season. Incorporation of a mechanism for the building and propagation of immunity facilitates investigation of the impact of exposure in the previous influenza season, through natural infection or vaccination, on the disease transmission dynamics and overall disease burden in subsequent years. Accordingly, we sought insights to aid understanding of the longer-term dynamics of the influenza virus and its interaction with immunity at the population level.

In this study, we examine the contribution of the differing sources of immunity propagation between years on seasonal influenza transmission dynamics. To this end, we amalgamate multiple sources of epidemiological and vaccine data for England covering the last decade, and fit model outcomes to the available longitudinal data of seasonal rates of general practice (GP) consultations for influenza-like-illness (ILI), scaled by virological surveillance information. We demonstrate that natural infection plays a more prominent role in propagation of immunity to the next influenza season compared to residual vaccine immunity. We conclude by inspecting for-

ward projections under disparate vaccine efficacy assumptions to determine long-term patterns of seasonal influenza infection.

Methods

Historical data

Throughout, we define a complete epidemiological influenza season to run from week 36 to week 35 of the subsequent calendar year. We chose week 36 (which typically corresponds to the first full week in September) as the start week to match the start of the epidemic with the reopening of schools.

Consultations in General Practices

Since January 1967, the Royal College of General Practitioners (RCGP) Research and Surveillance Centre (RSC) has monitored the activity of acute respiratory infections in GPs. The Weekly Return reports the number of persons in the monitored RCGP RSC network practices registered population consulting for ILI (a medical diagnosis of possible influenza with a set of common symptoms, cough and measured or reported fever $\geq 38^{\circ}$C, with onset within the last 10 days [18]).

Importantly, the dataset is nationally representative both demographically and spatially; the demographics of the sample population closely resembling the country as a whole, with the RCGP RSC network of practices spread across England in order to reflect the distribution of the population. In May 2017, the RCGP RSC network included 1,835,211 patients (approximately 3.3% of the total population in England) from 174 practices [19].

For the influenza seasons 2009/2010 until 2017/2018 inclusive, RCGP RSC provided weekly, age-stratified records containing the size of the monitored RCGP RSC population, the number of individuals in the monitored population consulting for ILI, and ILI rates per 100,000. These data were aggregated across ages to produce weekly ILI rates per 100,000 for the entire sample population. We then summed the weekly ILI rates (weeks 36 through to week 35 in the following calendar year) to produce season-by-season ILI rates per 100,000. Expanded information pertaining to the data extraction is provided in Section 1.1 of the Supporting Information.

Respiratory Virus RCGP RSC Surveillance

To complement syndromic surveillance, a subset of GPs in the RCGP RSC submit respiratory samples from patients presenting in primary care with an ILI. These respiratory samples undergo virological testing to ascertain presence or absence of influenza viruses. Given not all patients reporting ILI are infected with an influenza virus, these virological sample positivity data yield the fraction of ILI reported primary care consultations that were attributable to influenza.

We collected relevant data from figures within Public Health England (PHE) annual influenza reports (for the 2009/10 to 2017/18 influenza seasons inclusive) [20, 21], and PHE Weekly National Influenza reports (for the 2013/14 influenza season onwards) [22]. (For full details, see Section 1.2 of the Supporting Information.) By scaling the longitudinal data of GP consultations

for ILI by the virological surveillance information we garnered an overall estimate of ILI GP consultations attributable to influenza. 88
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Circulating strain composition 90

We derived seasonal rates of primary care consultations attributable to each of the two influenza A subtypes (A(H1N1)pdm09 and A(H3N2)) and the two influenza B lineages (B/Victoria and B/Yamagata) per 100,000 population. We computed the circulating strain distribution in each influenza season using publicly available data from FluNet [23], a global web-based tool for influenza virological surveillance, using data for the United Kingdom (additional details are provided in Section 1.3 of the Supporting Information). 91
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ILI GP consultations attributable to influenza 97

We applied the circulating strain composition quantities to the overall estimate of ILI GP consultations attributable to influenza, disaggregating the estimate for all influenza strains of interest into strain-specific quantities:

$$\text{GP consultation rate for strain } m \text{ in season } y = C_{m,y} = \text{GP ILI consultation rate} \times \ldots$$
$$\text{Proportion of ILI samples influenza positive} \times \ldots \quad (1)$$
$$\text{Proportion of influenza viruses in circulation of strain type } m$$

These computations resulted in seasonal rates of GP consultations attributable for the two influenza A subtypes and two influenza B lineages per 100,000 population (Fig. 1(a)). Uncertainty distributions for these values were obtained via bootstrapping given the sample sizes for the three components. 98
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Fig. 1: Empirical, strain-stratified data for ILI GP consultations attributable to influenza per 100,000 population. In both panels, stacked horizontal bars in the left-half depict the cumulative total of ILI GP consultations attributable to type A influenza per 100,000 population (red shading denoting the A(H1N1)pdm09 subtype, orange shading the A(H3N2) subtype). In an equivalent manner, on the right-half of each panel stacked horizontal bars present similar data for type B influenza (cyan shading denoting the B/Victoria lineage, dark blue shading the B/Yamagata lineage). **(a)** Influenza seasons 2009/10 to 2017/18 (inclusive). In the 2009/10 and 2011/12 influenza seasons, all samples identified as influenza B were untyped (represented by black filled bars). **(b)** Influenza seasons 2012/13 to 2017/18 (inclusive), the time span for which we performed parameter inference.

Vaccine uptake and efficacy

For the 2009/10 influenza season, we acquired vaccine uptake profiles from survey results on H1N1 vaccine uptake amongst patient groups in primary care [24]. For the 2010/11 influenza season onward we collated vaccine uptake information from PHE official statistics [21, 22].

We took vaccine efficacy estimates for each historical influenza season from publications detailing end-of-season seasonal influenza vaccine effectiveness in the United Kingdom [25–31]. In seasons where equivalent publications were not available, we used mid-season or provisional end-of-season vaccine efficacy estimates from PHE reports [32, 33]. There has been substantial variation in vaccine efficacy between seasons and also within seasons across strains, with estimates spanning 23-92% (Table 1). Further, there have been two instances of a mismatch between the vaccine and circulating viruses causing the vaccine to be ineffective (i.e. 0% efficacy) against a particular strain group (B/Yamagata in the 2010/11 influenza season, A(H3N2) in the 2017/18 influenza season). As a sole exception, for the 2009/10 influenza season we used the pandemic vaccine (rather than the seasonal influenza vaccine efficacy) to inform efficacy against A(H1N1)pdm09, with the effectiveness against all other strain types set to zero [25].

The empirical data did not provide individual vaccine efficacy estimates for each influenza A subtype and influenza B lineage (Table S1). We therefore used a set of simplifying assumptions to produce the strain-specific, vaccine efficacy point estimates used within our study (Table 1). The time-varying vaccine uptake data, together with the season-specific information on vaccine efficacy, act as forcing for the within-season epidemiological model (details are described in Sections 1.4-1.5 of the Supporting Information).

Modelling overview

Following the visualisation convention used in [10], we display a directed acyclic graph repre- senting the model structure and incorporation of the data streams (Fig. 2). The model takes the form of a deterministic continuous-time set of ordinary differential equations (ODEs), which determines the within-season epidemiological dynamics, and a discrete-time map, informing the propagation of immunity from one season to the next.

Our model captures the four strains targeted by the quadrivalent seasonal influenza vaccine, namely, two influenza A subtypes, A(H1N1)pdm09 and A(H3N2), and two influenza B lineages, B/Victoria and B/Yamagata. The multi-strain model construction permits exploration of cross- reactive immunity mechanisms and their impact on the disease dynamics. Multiple infections per influenza season and/or co-infection events were not permitted. In others words, it was presumed that individuals may only be infected by one strain of influenza virus per season.

Next, we summarise, in turn, the vaccination, immunity propagation, epidemiological and ob- servation model components.

Vaccination model

Epidemiological states were compartmentalised based on present season vaccine status (indexed by N for non-vaccinated or V for vaccinated). We obtained weekly time-varying vaccine uptake rates, ν, at the population level by computing a weighted average of the individual age group uptake values, thereby accounting for the population distribution in each given influenza season. We assumed the rate of vaccination ν to be constant over each weekly period. Vaccine efficacy

Table 1: Influenza vaccine efficacy point estimates, by season and strain type. All estimates are presented as percentages. The empirical adjusted influenza vaccine efficacy estimates by season and strain type (presented in Table S1) did not provide individual vaccine efficacy estimates for each influenza A subtype and influenza B lineage. We therefore implemented a series of assumptions to produce the strain-specific, vaccine efficacy point estimates used within our study (described in Section 1.5 of the Supporting Information)).

Season	Vaccine efficacy				Source
	A(H1N1)pdm09	**A(H3N2)**	**B/Victoria**	**B/Yamagata**	
2009/10	72.0	0.0	0.0	0.0	[25]*
2010/11	56.0	56.0	78.0	0.0	[26]
2011/12	23.0	23.0	92.0	92.0	[27]
2012/13	73.0	26.0	51.0	51.0	[28]
2013/14	61.0	61.0	61.0	61.0	[32]†
2014/15	29.9	29.3	46.3	46.3	[29]
2015/16	54.5	54.5	57.3	54.2	[30]
2016/17	36.7	31.6	54.5	58.5	[31]
2017/18	66.3	0.0	24.7	24.7	[33]‡

*: The adjusted seasonal influenza vaccine efficacy in the 2009/10 season was -30% (-89%, 11%) [25]. We therefore used the pandemic vaccine to inform efficacy against A(H1N1)pdm09, with the effectiveness against all other types set to zero.

†: Mid-season estimate of seasonal influenza vaccine effectiveness from [32]. Low incidence throughout the 2013/2014 influenza season meant reliable end-of-season estimates for the vaccine efficacy could not be attained (Personal communication, PHE).

‡: Provisional end-of-season influenza vaccine effectiveness results.

Fig. 2: Schematic showing the links between the vaccination, immunity propagation, epidemiological and observation model components. We adopt the visualisation conventions of [10], with ellipses indicating variables, and rectangles indicating data. Dotted arrows indicate relationships between prior season epidemiological outcomes and immunity propagation factors. Solid arrows indicate within-season processes. Circled capitalised letters indicate the relationships connecting the variables or data involved. These relationships are: process A, propagation of immunity as a result of exposure to influenza virus in the previous influenza season (through natural infection or vaccination); process B, modulation of current influenza season virus susceptibility; process C, estimation of influenza case load via the SEIR model of transmission; process D, ascertainment of cases through ILI recording at GP.

depended upon the extent to which the strains in the vaccine matched the circulating strain in that influenza season (Table 1).

We assumed a 'leaky' vaccine, offering partial protection to every vaccinated individual, thus acting to reduce the overall susceptibility of the given group receiving vaccination. The 'leaky' vaccine action contrasts with an 'all-or-nothing' vaccine assumption, which assumes complete protection to a subset of the vaccinated individuals but no protection in the remainder of vaccinated individuals. Explicitly, under a 'leaky' vaccine action with a vaccine efficacy against strain m of α_m, the relative susceptibility of the vaccinated group towards strain m is $1 - \alpha_m$. Additionally, we assumed those administered vaccines had unmodified transmission (i.e. those receiving the 'leaky' vaccine were equally as infectious as those who did not). Vaccination is modelled irrespective of infection status (susceptible, latent, infected and recovered individuals), as vaccine history impacts the immunity levels for next season.

Immunity propagation model

A novel aspect of our model framework was the potential for exposure to influenza virus in the previous influenza season, through natural infection or vaccination, to modulate current

influenza season susceptibility. Accordingly, we tracked immunity derived from natural infection and vaccination separately (Fig. 2, process A), requiring ten distinct exposure history groupings. Three susceptibility modifying factors of interest were: (i) modified susceptibility to strain m given infection by a strain m type virus the previous season, denoted a; (ii) carry over cross-reactivity protection between influenza B lineages, denoted b (to account for infection with one influenza B virus lineage being potentially beneficial in protecting against subsequent infection with either influenza B virus lineage [34]); (iii) residual strain-specific protection carried over from the prior season influenza vaccine, denoted c_m. We mandated that $0 < a,b,c_m < 1$. The collection of exposure history groupings and associated strain-specific susceptibilities were consolidated into a single susceptibility array (Fig. 2, process B; Fig. 3).

We assumed the immunity propagation due to vaccination in the previous season (c_m) to be related to the strain-specific vaccine efficacy in the previous season (α_m^{y-1}). In particular, we introduce a linear scaling factor $\xi \in (0,1)$, which reduces the level of vaccine derived immunity between seasons: $c_m^y = 1 - \xi\alpha_m^{y-1}$.

All three propagation parameters (a, b, ξ) were inferred from epidemiological data. A mathematical description of the immunity mapping between seasons is given in Section 2.2 of the Supporting Information.

In light of there being uncertainty around the precise time scale for which immunity to seasonal influenza viruses may be retained, with individual- and population-level models having estimated infection acquired immunity to wane over a timescale of two to ten years [35–37]), we also considered an extended variant of the immunity propagation model component.

In the model extension, we fit an additional parameter (δ) representing the proportion of those who began the influenza season in an exposure history group linked to natural infection (Fig. 3: rows 2-5, 7-10), and who were also unexposed to influenza virus during the current season (who at the end of of the current influenza season remained susceptible), that retained their pre-existing natural infection acquired immunity. Those keeping immunity arising from natural infection were mapped to the relevant prior infection exposure history group dependent upon current season vaccination status. The remaining proportion $(1 - \delta)$ transitioned in the same manner as in the original model, reverting to either the naive exposure history group or vaccinated only exposure history group (Figure S19). For clarity, we did not introduce a mechanism to confer vaccine-induced immunity beyond one influenza season (i.e. vaccine-induced immunity could be retained for, at most, a single additional influenza season).

With the more complex immunity structure, we did not gain noticeable improvements in correspondence of model outputs with the data (relative to fits with a model using the simpler immunity propagation setup). Therefore, we do not discuss any further here the alternative immunity propagation structure, instead giving a complete description of the extended model and associated outcomes in Section 5 of the Supporting Information.

Epidemiological model

The within-season transmission dynamics were performed by an ODE epidemiological model based on SEIR-type dynamics. At the start of each season we passed into the epidemiological model the vaccination attributes (uptake and efficacy), immunity considerations, virus transmission rates and the initial proportion of the population infectious per strain. These collection of epidemiological inputs act as forcing parameters (Fig. 2, process C).

The epidemiological model is a deterministic, non-age, multi-strain structured compartmental

Exposure history (h)	Strain susceptibility			
	A(H1N1)pdm09	A(H3N2)	B/Victoria	B/Yamagata
Naïve	1	1	1	1
A(H1N1)pdm09	a	1	1	1
A(H3N2)	1	a	1	1
B/Yamagata	1	1	a	b
B/Victoria	1	1	b	a
Vacc. (V)	$c_{A(H1N1)}$	$c_{A(H3N2)}$	$c_{B/Victoria}$	$c_{B/Yamagata}$
A(H1N1)pdm09 & V	$\min(a, c_{A(H1N1)})$	$c_{A(H3N2)}$	$c_{B/Victoria}$	$c_{B/Yamagata}$
A(H3N2) & V	$c_{A(H1N1)}$	$\min(a, c_{A(H3N2)})$	$c_{B/Victoria}$	$c_{B/Yamagata}$
B/Victoria & V	$c_{A(H1N1)}$	$c_{A(H3N2)}$	$\min(a, c_{B/Victoria})$	$\min(b, c_{B/Yamagata})$
B/Yamagata & V	$c_{A(H1N1)}$	$c_{A(H3N2)}$	$\min(b, c_{B/Victoria})$	$\min(a, c_{B/Yamagata})$

Fig. 3: Infographic presenting the interaction between exposure history and susceptibility. The interaction between exposure history h and susceptibility to strain m in the current season, $f(h, m)$, was classified into ten distinct groups: One group for the naive (uninfected and not vaccinated, row 1); one group per strain, infected but not vaccinated (rows 2-5); one group for those vaccinated and experiencing no natural infection (row 6); one group per strain for being infected and vaccinated (rows 7-10). We let a denote modified susceptibility to strain m given infection by a strain m type virus the previous season (dark green shading), b modified susceptibility due to cross-reactivity between type B influenza lineages (dark blue shading), and c_m the change in susceptibility to strain m given vaccination in the previous season (gold shading). Unmodified susceptibilities retained a value of 1 (red shading). We enforced $0 < a, b, c_m < 1$.

based model capturing demography, influenza infection status (with susceptible-latent-infected-recovered, SEIR, dynamics) and vaccine uptake. For influenza, it is commonplace to also consider a risk-stratified population, divided into individuals at low or high risk of complications associated with influenza. However, it is health outcomes, rather than epidemiological processes, that are contingent upon risk status [10] and therefore this additional structure can be ignored for the purposes of this model. We assumed disease transmission to be frequency-dependent, such that fundamental quantities (like the basic reproductive ratio, R_0) are unaffected by changes to population size.

We assumed exponentially-distributed latent and infectious periods (arising from rates of latency loss and recovery, respectively, being constant). Loss of latency rates $\gamma_{1,m}$ were strain-dependent. From Lessler *et al.* [38], we chose rates corresponding to average latent periods of 1.4 days and 0.6 days for influenza A and influenza B associated strains respectively. Following Cauchemez *et al.* [39], we set the rate of loss of infectiousness $\gamma_2 = 1/3.8$, corresponding to an average infectious period of 3.8 days, independent of strain.

We set the mortality rate based upon a gender-averaged life expectancy for England, approximated from male and female specific statistics from Office for National Statistics data [40] (see Table 2).

The ODE equations of the SEIR epidemiological model are given in Section 2.3 of the Supporting Information. The strain specific force of infection, λ_m, satisfies

$$\lambda_m = \beta_m \sum_X I_m^X, \qquad (2)$$

where β_m is the transmission rate for strain m, implicitly comprising the contact rate and the

Table 2: Overview of parameters in the model.

Description	Notation	Value	Sources
Fixed parameters			
Mortality rate (day^{-1})	B,D	$\frac{1}{81\times365}$	[40]
Rate of latency loss, influenza A subtypes (day^{-1})	$\gamma_{1,A}$	$\frac{1}{1.4}$	[38]
Rate of latency loss, influenza B lineages (day^{-1})	$\gamma_{1,B}$	$\frac{1}{0.6}$	[38]
Recovery rate (day^{-1})	γ_2	$\frac{1}{3.8}$	[39]
Time-varying parameters			
Vaccination rate at time t	$\nu(t)$	—	[21, 22, 24]
Vaccine efficacy, season y strain m	α_m^y	—	[25–33]

Inferred parameter description	Notation	Prior	
Influenza virus transmissibility, strain m	β_m	$\mathcal{U}(0.2632,0.7896)$	
Modified susceptibility given natural infection in prior season	a	$\mathcal{U}(0,1)$	
Modified susceptibility due to type B influenza cross-reactivity	b	$\mathcal{U}(0,1)$	
Proportion of prior season vaccine efficacy carried over	ξ	$\mathcal{U}(0,1)$	
Ascertainment probability in season y	ϵ_y	$\mathcal{U}(0,0.05)$	

transmissibility of the virus (the probability that a contact between an infectious person and a susceptible person leads to transmission), and the superscript $X \in \{N, V\}$ denotes vaccination status (indexed by N for non-vaccinated, V for vaccinated).

For use in our observation model, we tracked the incidence $Z_m(y)$ of new strain m influenza infections in season y as a rate per 100,000 population:

$$Z_m(y) = \left(\int_{y-1}^{y} \gamma_{1,m}(E_m^N + E_m^V)\,\mathrm{dt} \right) \times 100,000. \tag{3}$$

Observation model

As discussed above, individuals consulting a GP for ILI do not necessarily directly correspond with individuals infected with one of the circulating influenza strains. To address this discrepancy, the final segment of the mathematical model linked the GP consultation data with the number of infections due to circulating influenza viruses in the population (Fig. 2, process D).

Our interest resided in the number of ascertainable cases, where we assumed that each individual infected by the strain of influenza under consideration had a probability ϵ of being ascertainable, i.e. going to the GP, being recorded as having ILI, and having a detectable influenza viral load. We assumed the ascertainment probability was season-specific (but strain agnostic) to account for a range of influences such as climate or co-circulating infections. We obtained model estimates of the proportion of individuals experiencing cases of ascertainable influenza (of strain type m) in season y through scaling the incidence $Z_m(y)$ by the ascertainment probability in influenza

season y, ϵ_y. Consequently, the ascertainable influenza cases in season y, $Z_m^+(y)$, obeys:

$$Z_m^+(y) = \epsilon_y Z_m(y). \tag{4}$$

The parameter ϵ_y is inferred by comparing the total predicted incidence in a given year to the calculated GP consultation rate (Eq. (1)).

Parameter inference

To realise a model capable of generating influenza-attributed ILI GP consultations estimates that resemble the empirical data (Eq. (1)), we sought to fit the following collection of model parameters (Table 2): transmissibility of each influenza virus strain (β_m), modified susceptibility to strain m given infection by a strain m type virus the previous season (a), carry over cross-reactivity protection between influenza B lineages (b), residual protection carried over from the prior season influenza vaccine (ξ), and an ascertainment probability per influenza season (ϵ_y).

For inferring posterior parameter distributions, we employed an adaptive-population Monte Carlo approximate Bayesian computation (ABC) algorithm [41] combined with a local perturbation kernel (multivariate normal kernel with optimal local covariance matrix) [42]. Prior distributions were uniform for all parameters (Table 2).

Simulations began in the 2009/2010 influenza season and ran for a specified number of seasons with one parameter set. For the 2009/2010 influenza season, only the A(H1N1)pdm09 strain was present in our simulation (in accordance with the strain composition data where proportions of samples for the remaining three strains were very low, Fig. 1(a)), with the initial proportion of the population infected being 1×10^{-5} (one per 100,000). In all subsequent influenza seasons, with all four influenza virus strains being present, the initial proportion of the population infected by each strain was 2.5×10^{-6}. We fit to the 2012/13 season onward, which omitted the influenza seasons (2009/10 and 2011/12) that had no influenza B lineage typing data (Fig. 1). This selected time frame contained a regime in which the dominant circulating influenza A subtype generally switched annually between H1N1(2009) and H3N2, while for type B influenza the Yamagata lineage incidence typically exceeded Victoria lineage incidence.

The summary statistics for our ABC procedure were comprised of two parts. The first component was a within-season temporal profile check; the peak in influenza infection (combining those in latent and infectious states) could not occur after February in any season. The second component defined the metric to measure the correspondence of the model predicted influenza-attributed ILI GP consultations versus the observed data. We worked with a metric akin to Poisson deviance. Compared to a sum of squared residuals error metric, a measure akin to Poisson deviance penalises with greater severity poor fits to data points of small magnitude. Accounting for season y and strain stratification m, we defined our deviance measure to be

$$\text{DEV} = 2 \sum_y \sum_m \left(C_{m,y} \ln \left(\frac{C_{m,y}}{M_{m,y}} \right) - (C_{m,y} - M_{m,y}) \right), \tag{5}$$

with $C_{m,y}$ the observed value for strain m in season y, and $M_{m,y}$ the model estimate for strain m in season y.

We amassed 10,000 particles representing a sample from the posterior distribution (see Section 3 of the Supporting Information for expanded details on the parameter estimation methodology).

Forward simulations

We used the parameter set returning the lowest error (in the inference procedure) to explore potential strain dynamics up to the 2029/2030 influenza season. Vaccination attributes (uptake and efficacy) for the 2009/2010 to 2017/2018 influenza seasons were taken from the observed data. For the forecasted seasons (2018/19 influenza season to the end of each simulation), we studied two scenarios arising from different hypotheses concerning future vaccine efficacy: (i) high efficacy, set at the maximum attained efficacy (single simulation); and (ii) randomly sampled from all previous vaccine efficacy values (1,000 simulation replicates). In addition, vaccine uptake in all projected influenza seasons matched that of the 2017/18 influenza season.

Simulation and software specifics

All model simulations began at week 36 of the epidemiological season. Inference and model simulations were performed in JULIA v0.6, with the system of ODEs solved numerically with the package DifferentialEquations v2.2.1. Data processing and production of figures were carried out in MATLAB R2019a.

Results

Parameter inference

We invoked the adaptive-population Monte Carlo ABC algorithm, accumulating 10,000 param- eter sets (representing a sample from the posterior distribution) to determine credible values of the model parameters (Table 3). Samples were obtained after completion of 600 generations of the adaptive-population Monte Carlo ABC scheme, at which point the generation-by-generation tolerance level updates were minor (Fig. 4(a)). Accordingly, additional simulations would only marginally change the posterior distributions. The model parameters were well defined, with Gaussian-shaped histograms (Fig. 4(b)). All parameter sets adhered to the mandatory temporal criteria of peak infection in each influenza season occurring prior to March (Figure S5).

Inspecting the attained posterior distributions for virus transmissibility, estimates for the two in- fluenza A subtypes are similar; both are larger than the corresponding estimates for the two type B lineages. However, the B/Yamagata transmissibility estimates exceeded those for B/Victoria, although the values are relatively close.

Amongst the three exposure history parameters (a, b, ξ), the parameter having a notable impact on the transmission dynamics was the modification to susceptibility due to natural infection in the previous influenza season (a). If infected by a given strain last season, the inferred median estimate of 0.7898 corresponds to an approximate 21% reduction in susceptibility to the current season variant of that strain type. Strikingly, there was little carry over of prior season vaccine efficacy (ξ), with the majority of the posterior distribution massed near 0. Similarly, being previously infected by one of the type B influenza virus conferred little immunity against the remaining type B lineage virus in the next season.

Inferred ascertainment probabilities (ϵ), across all seasons, were typically within the range of 0.001-0.006. The highest ascertainment probabilities were found for the recent 2017/18 influenza season, attaining a median of 0.005; but this still suggests that only one in two hundred infections was reported to their GP and correctly identified as influenza.

We verified model robustness by performing parameter fits using two subsets of the historical influenza season data, spanning the time periods 2012/13-2015/16 and 2012/13-2016/17 respectively. Fitting to these differing influenza season ranges, outcomes generally exhibited qualitative consistency; in particular, amongst the three mechanisms for immunity propagation, current season susceptibility was modulated greatest by natural infection in the previous influenza season. The only notable quantitative differences when fitting to the two shortened time frames (compared to the distributions inferred when fitting to the complete time period) were elevated transmissibility levels (β), counteracted by an enlarged effect of prior infection (a) and vaccination propagation (ξ); further details are given in Section 4.2 of the Supporting Information.

In addition, we assessed the parameter identifiability competency of our ABC fitting scheme via generation of synthetic data from known parameters. Employing our inference scheme to fit the model to the synthetic data, we ably recovered the parameter values from which the synthetic data had been generated, giving extra confidence to our results (see Section 4.3 of the Supporting Information).

Table 3: Values (posterior quantiles) for the transmission, exposure history and ascertainment probability parameters inferred fitting to the empirical data. Numbers inside brackets indicate 95% credible intervals. All values are given to 4 d.p.

Description	Notation	Median [95% credible interval]
Transmission parameters		
A(H1N1)pdm09	$\beta_{A(H1N1)pdm09}$	0.3955 [0.3880, 0.4039]
A(H3N2)	$\beta_{A(H3N2)}$	0.3984 [0.3904, 0.4076]
B/Victoria	$\beta_{B/Victoria}$	0.3548 [0.3498, 0.3603]
B/Yamagata	$\beta_{B/Yamagata}$	0.3694 [0.3635, 0.3759]
Exposure history parameters		
Natural infection in prior season	a	0.7898 [0.7834, 0.7966]
Type B influenza cross-reactivity	b	0.9797 [0.9511, 0.9983]
Prior season vaccine efficacy propagation	ξ	0.0061 [0.0004, 0.0163]
Ascertainment probabilities		
2012/13	$\epsilon_{2012/13}$	0.0017 [0.0015, 0.0018]
2013/14	$\epsilon_{2013/14}$	0.0010 [0.0009, 0.0012]
2014/15	$\epsilon_{2014/15}$	0.0024 [0.0022, 0.0026]
2015/16	$\epsilon_{2015/16}$	0.0036 [0.0033, 0.0040]
2016/17	$\epsilon_{2016/17}$	0.0014 [0.0012, 0.0015]
2017/18	$\epsilon_{2017/18}$	0.0051 [0.0047, 0.0055]

Fig. 4: Results of the ABC scheme, fitting to the empirical data. (a) Summary metric threshold value upon completion of each generation of the inference scheme. The inset panel displays the latter quarter of generations. (b) Inferred parameter distributions estimated from 10,000 retained samples following completion of 600 generations of the inference scheme. Vertical red lines indicate the median values for the model constants estimated from the inference procedure. Particularly noteworthy outcomes include: transmissibility of type A viruses exceeding type B viruses; prior season influenza B cross-reactivity and vaccine carry over had little impact on present season susceptibility; the highest ascertainment probability occurred in the 2017/18 influenza season.

Evaluating model fit

To assess the goodness-of-fit between our model and the available data, we performed 1,000 independent simulations using parameter sets drawn from the ABC inference procedure. There- fore, although the model is deterministic, we generated variability in epidemic composition due to the posterior distribution for the underlying parameters. The incidence of each of the four influenza types over each season was converted to attributed GP consultations (per 100,000) and compared to the data (Fig. 5). We generally obtained an excellent fit to the data, both in terms of the severity of infection each year (as controlled by the ascertainment ϵ_y) but also in terms of type and subtype composition (which is largely driven by epidemiological dynamics and propagation of immunity).

Considering type A influenza, we clearly captured the alternating pattern of dominance by A(H3N2) and A(H1N1)pdm09 subtypes for the years 2012/13 to 2016/17; but more importantly the model was able to predict the unexpected result that A(H3N2) dominated in both 2016/17 and again in 2017/18. For influenza B, we obtained excellent agreement for the overall magnitude of GP consultations as a result of type B, but this was not always in complete agreement with the subtype composition.

A more detailed comparison of predicted and observed subtypes in each season allowed us to analyse discrepancies in more detail (Fig. 6). The model predictions are shown with a violin plot to capture the variability in the distribution due to parameter uncertainty; while the observed data has confidence intervals (calculated from bootstrapping) due to the finite sample sizes. In general there was good agreement between the data and model, especially for years where par- ticular subtypes dominated (e.g. A(H1N1)pdm09 in 2013/14 and 2015/16, A(H3N2) in 2014/15 and 2016/17, and B/Yamagata in 2012/13 and 2017/18). However, there were also discrepan- cies, most notably in 2015/16 where the majority of the B-influenza cases were predicted to the wrong subtype. It was also clear that the model generally performed less well when there were very low levels of a given subtype in a particular year.

Fig. 5: Posterior predictive distributions for influenza positive GP consultations per 100,000 population. Stratified by influenza season, we present back-to-back stacked bars per simulation replicate, with 1,000 replicates performed, each using a distinct parameter set representing a sample from the posterior distribution. Each influenza season is topped out by a thicker stacked horizontal bar plot, corresponding to the strain-stratified point estimates for the empirical data. The left side depicts the cumulative total of ILI GP consultations attributable to type A influenza per 100,000 population (red shading denoting the A(H1N1)pdm09 subtype, orange shading the A(H3N2) subtype). In an equivalent manner, the right side stacked horizontal bars present similar data for type B influenza (cyan shading denoting the B/Victoria lineage, dark blue shading the B/Yamagata lineage). Simulations are arranged such that the largest epidemics are in the centre of the bar. We see a reasonable qualitative model fit to the data, especially for the two influenza A subtypes.

Fig. 6: Posterior predictive influenza positive GP consultation distributions. We generated the estimated distributions from 1,000 model simulations, each using a distinct parameter set from the retained collection of particles. Crosses represent the observed data, with solid bars the range of the bootstrapped empirical data. Shaded violin plots denote outcomes from model simulations using the empirical data on vaccination, with filled circles the median value across the simulated replicates. **(a)** A(H1N1)pdm09; **(b)** A(H3N2); **(c)** B/Victoria; **(d)** B/Yamagata.

Forward simulations

Using the parameter set from the inference scheme returning the closest correspondence with the data (lowest DEV value, Eq. (5)), we explored potential strain dynamics up to the 2029/30 influenza season under contrasting vaccine efficacy settings (Fig. 7).

When maintaining the same high vaccine efficacy (A(H1N1)pdm09: 73%; A(H3N2): 61% B/Victoria: 92%; B/Yamagata: 92%) across all future seasons (single bars), consistent levels of influenza incidence were predicted for both influenza types. Whilst combined influenza B incidence was low, ranging approximately between 600-1700 cases per 100,000 each season, seasonal influenza A incidence consistently reached 25,000-30,000 cases per 100,000. Furthermore, we again predict periodic behaviour for the portion of influenza A viruses in circulation ascribed to the subtypes A(H1N1)pdm09 and A(H3N2), mirroring the observed pattern from 2012/13 to 2016/17. Influenza seasons ending in odd numbered years (e.g. 2028/29) had a relatively even split between the two subtypes; whereas for influenza seasons ending in even numbered years (e.g. 2029/30) the A(H3N2) subtype dominated the A(H1N1)pdm09, with influenza A viruses apportioned to A(H3N2) and A(H1N1)pdm09 subtypes being 75-80% and 20-25%, respectively.

An alternative approach is to use the single (best-fit) parameter set, but to sample the vaccine efficacies from historical estimates. The most striking factor was the amount of variability that comes as a direct results of uncertainty in the vaccine efficacies. As such all between-season patterns were swamped by the within-season variability, leading to distributions that were remarkably consistent between seasons. The only notable exception was 2018/19, where the definitive knowledge of the 2017/18 season had a clear impact of the predictions for 2018/19 leading to broadly higher levels of influenza A and lower levels of influenza B. Comparing subtype distributions, we found that under randomly sampled vaccine efficacies incidence of B/Yamagata tended to exceed B/Victoria in each season (holding in more than 70% of simulations). However, we obtained greater levels of variation for the influenza A subtypes. For high vaccine efficacy conditions (single bars) less than half of total influenza A cases in any season were attributed to the A(H1N1)pdm09 subtype (rather than A(H3N2)), whereas under variable vaccine efficacies (distributed bars) A(H1N1)pdm09 incidence was greater than A(H3N2) incidence in 30-50% of all simulations. Unsurprisingly, the majority of simulations (∼85%) performed with seasonally variable vaccine efficacies returned predicted incidence rates (in all influenza seasons) that exceeded the equivalent seasonal incidence estimates generated under high vaccine efficacy conditions; this was most striking for influenza B.

Fig. 7: Projected influenza seasonal incidence (per 100,000 population) up to 2029/30. Each influenza season is topped out by a thicker stacked horizontal bar plot, corresponding to the simulated estimate under the high vaccine efficacy scenario; efficacies by strain were as follows - A(H1N1)pdm09: 73%; A(H3N2): 61%; B/Victoria: 92%; B/Yamagata: 92%. Thin bars correspond to simulation runs where vaccine efficacy against each strain were randomly sampled from the empirical distribution (totalling 1,000 replicates). The left side depicts the cumulative total of ILI GP consultations attributable to type A influenza per 100,000 population (red shading denoting the A(H1N1)pdm09 subtype, orange shading the A(H3N2) subtype).The right side stacked horizontal bars present similar data for type B influenza (cyan shading denoting the B/Victoria lineage, dark blue shading the B/Yamagata lineage). For all forward simulated seasons, vaccine uptake matched that of the 2017/18 influenza season.

Discussion

Understanding the processes that drive seasonal influenza transmission patterns is an important public-health question, given the economic cost and burden to human health afflicted by the condition [1, 2]. During recent years there has been marked progress in synthesising real-world data to inform mathematical model parameterisation. Yet, prior studies have tended to model each season and each strain circulating within that season independently [10–13]. Thus, the presence of strain and immunity interactions have been omitted. Using data subsequent to the 2009 pandemic for England, we have developed a dynamic multi-strain SEIR-type transmission model for seasonal influenza, explicitly incorporating immunity propagation mechanisms between seasons. Our model is fitted to seasonal-level data on strain competition, with a view to minimising the number of independent parameters. Predictions from this model show substantial agreement with subtype data from England, and are able to predict the main qualitative features. We attribute much of the discrepancies to the homogeneous way in which we have treated immunity propagation, in practise this is driven by complex patterns of waning and cross immunity as well as somewhat irregular genetic drift.

Inferred transmissibility of type A influenza strains exceeding those of type B, which reflects type A being the predominant class of influenza virus in circulation over the studied time period [23]. Moreover, concentrating on the parameters relevant to immunity propagation, we uncover evidence against vaccination stimulating similar long-term immunity responses as for natural infection. These conclusions corroborate findings of broad immune response (against antigenically drifted strains) fading after repeated vaccination [43], plus rapid waning of vaccine-mediated immunity [44]. There are also indications that prior natural infection boosts vaccine responses against antigenically drifted strains, whereas prior vaccination does not [45]. The clinically observed impact of prior infection for enhancing vaccine efficacy was long-lasting, which may be used to instruct further model refinements.

The extent of immunity propagation stemming from earlier influenza infection and vaccination occurrences may conceivably be quantified through serological surveys, potentially the most direct and informative technique available to infer the dynamics of a population's susceptibility and level of immunity [46]. There is scope to implement concepts monitoring changes in the immune response to infections in a rapid and cost-effective manner, by using existing primary care sentinel networks [47]. In this fashion, in England an age-stratified pilot serology study was recently initiated utilising the RCGP RSC to collect serological specimens and associated patient data to measure seropositivity and seroincidence due to seasonal influenza [48]. These progressive developments make usage of serological data to validate our study findings a realistic prospect.

Furthermore, though there have been studies carried out to quantify the strength of vaccine induced herd immunity for seasonal influenza [3, 4], the role of immunity originating from non-immunising exposure to influenza viruses in inducing herd immunity is unexplored. An upsurge in serology data would promote such assessments.

Ascertainment probabilities are key for linking population levels of influenza infection to GP-reported incidence. For greater parsimony we have assumed that ascertainment is independent of subtype, which could be an over-simplification in some years; but allowing ascertainment to depend on both season and subtype would over-fit the model. Across all considered influenza seasons, we found ascertainment probabilities were of a similar order (and concurred with the magnitudes of inferred ascertainment probabilities in [10]), with the greatest values obtained for the 2017/18 influenza season. The 2017/18 season saw moderate to high levels of influenza

activity observed in the UK [21], exacerbated by a mismatch of the A(H3N2) component of the available vaccine towards the A(H3N2) strain in circulation [33]. The effects that consequential increased media coverage of an outbreak have on transmission dynamics can be complex [49], with the perception of the disease conceivably changing among the population [50]. Chiefly in this instance, for those infected and symptomatic the propensity to consult a GP may have been abnormally raised, which would result in an increased ascertainment probability relative to prior influenza seasons.

While historic immunity is predicted to play an important role in determining annual strain composition (leading to subtype patterns between seasons), our projections of the dynamics forward in time exemplify how variability in vaccine efficacy hampers our ability to make long-term predictions. Consistently high vaccine efficacies would aid forecasting efforts, providing additional benefits beyond the reduction in disease offered by new vaccines with improved clinical efficacy and effectiveness [51]. Most importantly, with annual emergence of drift variants of influenza viruses, cross-protective vaccines are needed to heighten protective effectiveness [52].

The development of the influenza transmission model presented here was built upon a collection of simplifying assumptions. A limitation of the model is fixing the influence of prior exposure history to a single season. Studies of repeated vaccination across multiple seasons suggest that vaccine effectiveness may be influenced by more than one prior season [53]. In an United Kingdom-centric analysis, Pebody et al. [31] scrutinised the possible effect of prior season vaccination on 2016/17 influenza season vaccine effectiveness; while there was no evidence that prior season vaccination significantly reduced the effectiveness of influenza vaccine during the current season in adults, it was deemed to increase effectiveness in children. Extending exposure history and susceptibility interaction functionality to encompass immunity propagation dependencies beyond one prior influenza season would assist efforts evaluating the potential effect of repeat influenza vaccinations in the presence of vaccine interference [54].

Second, we assumed the mechanism underpinning propagation of immunity from influenza vaccination in the previous season behaved linearly. Alternative non-linear formulations warrant consideration, if there is sufficiently detailed data to underpin the models. Third, for simplicity we assumed each season was initialised with a low level of all subtypes; in practise the subtypes seeding each epidemic will be contingent on the dynamics in the rest of the world. Finally, we assumed the value of the ascertainment probability to be constant over the course of the influenza season. The underlying assumption is that the quantities contributing towards ascertainment remain stable over time. Yet, in reality there are contributory factors that are likely to vary during the course of each seasonal outbreak; for example, the propensity to consult with a GP if inflicted with symptomatic illness.

We view the dynamic influenza transmission model presented here as a foundation stage for influenza modelling constructs incorporating strain and immunity interactions. Heterogeneity in social contact patterns and the role of age in influenza transmission potential and severity of health outcomes are important considerations, with children identified as the main spreaders of influenza infection [55, 56] and most influenza associated deaths occurring among elderly adults and those with co-morbid conditions that place them at increased risk [2, 57]. As a consequence, next steps should include augmenting population mixing patterns and age-structure into the mathematical framework. In addition, coupling the transmission model together with economic evaluation frameworks will permit cost-effectiveness appraisals of prospective vaccination programmes.

In summary, through the use of mathematical modelling and statistical inference, our analysis of seasonal influenza transmission dynamics in England quantifies the contribution of distinct

immunity propagation mechanisms. We find that susceptibility in the next season to a given influenza strain type is modulated to the greatest extent through natural infection by that strain type in the current season, with residual vaccine immunity having a lesser role and inconsequential support for carry over type B cross-reactivity. As such, the approach utilised here offers a preliminary basis for long-term influenza modelling constructs incorporating strain and immunity interactions, although forecasts are strongly influenced by vaccine efficacy. We suggest that the adoption of influenza transmission modelling frameworks with immunity propagation provides a comprehensive manner to assess the impact of seasonal vaccination programmes.

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Data availability

The GP consultation data contain confidential information, with public data deposition non-permissible for socioeconomic reasons. The GP consultation data resides with the RCGP Research and Surveillance Centre and are available via the RCGP RSC website (www.rcgp.org.uk/rsc). All other raw data utilised in this study are publicly available; relevant references and data repositories are stated within the main manuscript and supporting information. Code and processed data used for the study is available at https://github.com/EdMHill/SeasonalFluImmunityPropagation.

Competing interests

The authors declare that they have no competing interests.

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Supporting Information:
Seasonal influenza: Modelling approaches to capture immunity propagation

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Table of Contents

1 Data descriptions

1.1 Consultations in General Practices

The text contained in this subsection was provided by the Royal College of General Practitioners (RCGP). Thus, throughout this subsection "we" refers to contributors from RCGP who extracted the data.

Method:
Data were extracted from four RCGP Research and Surveillance Centre (RSC) databases [1]. UK general practice is a registration based system where all citizens can register with a single GP of their choice. Practices are computerised, and data entered into computerised medical record systems either as coded data [2], or free text. We extracted the coded data, and our results are based on this element of the record [3]. We extract all coded data, pseudonymising as close to sources as possible. Where patients have a range of codes inserted suggesting they opt out of record sharing we do not analyse their data [4].

The data sources was the Real World Evidence (RWE) database, established at University of Surrey in March 2015. This database contains all continuous historical data contained in the GP systems. Bulk data are extracted four times per year taking historic coded data. Where extracts fail for major reports we attempt to extract data using Morbidity Information and Export Syntax (MIQUEST). This is a Department of Health sponsored data extract tool.

RCGP provided weekly influenza-like-illness (ILI) rates for the RSC population from week 1 2000 to week 52 2018, disaggregated as follows:

1. **ISOYear**
2. **ISOWeek**
3. **Age**
4. **Chronic Disease**
5. **Population**
6. **Number of people with ILI**
7. **Rates per 100,000**

The data compared the ILI rates of people with chronic diseases (Chronic Disease = 1) against people without chronic diseases (Chronic Disease = 0).

Contributors:

1. **Simon de Lusignan** Director, guarantor for these data, assisted with clinical knowledge
2. **Rachel Byford** Put together structures for the data extraction.
3. **Ana Correa** Carried out the quality assessment of the output.
4. **Chris McGee** Carried out data extraction of ILI rates (covering week 1 2000 to week 52 2016).
5. **Julian Sherlock** Carried out data extraction of ILI rates and data quality checks (covering week 1 2017 to week 35 2018).

6. **Sameera Pathirannehelage** Carried out data extraction of ILI rates (covering week 1 2017 to week 52 2018).

7. **Ivelina Yonova** liaison with practices, and review of the original data request.

Acknowledgements:
Practices who have agreed to be part of the RCGP RSC and allow us to extract and used health data for surveillance and research. Filipa Ferreira (programme manager), and other members of the Clinical Informatics and Health Outcomes Research Group at University of Surrey. Apollo Medical Systems for data extraction. Collaboration with EMIS, TPP, In-Practice and Micro-test CMR supplier for facilitating data extraction. Colleagues at Public Health England.

1.2 Respiratory Virus RCGP Surveillance

Data pertaining to the the weekly percentage of sentinel virology samples that were influenza positive were sourced from a subset of general practices in the RCGP Weekly Returns Service that submitted respiratory samples for virological testing from patients presenting in primary care with an ILI.

These data were displayed in figures within PHE annual influenza reports (for the 2009/10 to 2017/18 influenza seasons inclusive) [5, 6], and PHE Weekly National Influenza reports (for the 2013/14 influenza season onwards) [7].

PHE annual influenza reports were our baseline source for virological sample positivity data . Typically, curves displaying the data covered week 40 up to a variable week number dependent upon the season (week 13: 2016/2017; week 13: 2010/2011; week 15: 2011/2012,2014/2015, 2017/2018; week 20: 2013/2014). As an exception, the data curve for the entire 2009/2010 influenza season was available within the 2010/2011 PHE annual influenza report [5].

In all seasons, we assumed weeks 36-39 and weeks 21-39 had an influenza positivity of 0%.

To inform positivity values for weeks preceding week 20 for the 2013/14 influenza season onwards that were not illustrated within the PHE annual influenza report, we used PHE Weekly National Influenza reports [7], which provided UK GP sentinel swabbing scheme sample positivity on a weekly basis. Note that we gave precedence to figures explicitly stated within annual reports over positivity quantities within the weekly PHE influenza summaries.

1.3 Circulating strain composition

Here, we expand on our use of FluNet [8] to inform the circulating influenza strain distribution per influenza season.

FluNet is a global web-based tool for influenza virological surveillance first launched in 1997. The virological data entered into FluNet, e.g. number of influenza viruses detected by subtype, are critical for tracking the movement of viruses globally and interpreting the epidemiological data.

FluNet reports weekly influenza surveillance data that are provided from over 140 National Influenza Centres of the Global Influenza Surveillance and Response System, national influenza reference laboratories, and WHO regional databases [9]. Per the WHO Global Epidemiological Surveillance Standards for Influenza guidance, influenza testing is conducted on specimens collected from persons presenting for medical care at participating surveillance sites who meet a

clinical definition for influenza-like illness (defined as an acute respiratory infection with measured fever of $\geq 38°$C, and cough, with onset within the last 10 days), or severe acute respiratory infection (defined as an acute respiratory infection with history of fever or measured fever of $\geq 38°$C, and cough, with onset within the last 10 days, and requiring hospitalization) [9]. Influenza is confirmed by accepted laboratory diagnostic methods and actively reported by the reference laboratory to FluNet [10].

We computed the empirical circulating strain distribution in each influenza season (from the 2009/10 season onward) using data from FluNet for the United Kingdom. A salient feature of the influenza type data is the presence of samples whose exact subtype/lineage were not determined (Fig. S1). We assumed the fraction of undetermined samples ascribed to each subtype/lineage matched the proportions observed for the set of samples where strain-specific information were available (Fig. S2)

(a)

(b)

Fig. S1: Breakdown of subtype/lineage composition of sampled influenza viruses, per influenza type, from the United Kingdom in each influenza season (2009/10 onward). (a) Type A influenza, stratified by subtype; **(b)** Type B influenza, stratified by lineage.

Fig. S2: Breakdown of subtype/lineage composition of sampled influenza viruses, as a proportion of all influenza samples, from the United Kingdom in each influenza season (2009/10 onward). Sequenced samples confirmed as influenza positive, stratified by type and subtype/lineage. We assumed the fraction of undetermined samples ascribed to each subtype/lineage matched the observed proportions (for influenza seasons where strain-specific information were available).

1.4 Vaccine uptake

For the 2009/10 influenza season, we acquired vaccine uptake profiles from survey results on H1N1 vaccine uptake amongst patient groups in primary care [11].

For the 2010/11 influenza season onward, we sourced seasonal influenza vaccine uptake figures from Public Health England official statistics [6, 7]. These data comprised uptake profiles per target vaccination age group (e.g. at-risk under 65 years, 65 year and over, 2 year-olds, 3 year-olds) for each influenza season from PHE Weekly National Influenza Reports. Population-level measures were acquired through weighting each uptake curve by the the respective population proportion. Age-partitioned population distribution estimates for England were obtained from the Office of National Statistics (ONS) [12, 13].

All age, overall population influenza vaccine coverage has been on the rise, increasing from 21.0% to 26.0% between the 2009/10 and 2017/18 influenza seasons (Fig. S3).

We constructed daily uptake rates from either weekly or monthly uptake values via linear interpolation.

The temporal resolution of the empirical vaccine uptake data was dependent upon the age category, stratified by: (i) Non-school aged children (weekly coverage figures); (ii) monthly, school-aged children (monthly coverage figures).

(i) Non-school aged children Delivery of vaccination to those aged under 65 years in a clinical risk group or 65+ years old is through their GP. Additionally, all 2 and 3 year-olds eligible for influenza vaccination are administered the vaccine through their GPs. Uptake profiles are

Fig. S3: All age, overall population vaccination uptake for 2009/10-2017/18 influenza seasons. Vaccine uptake per influenza season were as follows (to 1 d.p.): 2009/10 - 21.0%; 2010/11 - 21.0%; 2011/12 - 21.7%; 2012/13 - 21.7%; 2013/14 - 23.0%; 2014/15 - 22.9%; 2015/16 - 22.9%; 2016/17 - 24.4%; 2017/18 - 26.0%.

constructed based upon GP practices reporting weekly to Immform (the influenza vaccine uptake monitoring programme from Public Health England).

For the groupings of at-risk under 65 years and 65 years and above, vaccine uptake profiles were available from 2012/2013 influenza season onwards. For the 2010/2011 and 2011/2012 influenza seasons we invoked the uptake profile from the 2012/2013 influenza season.

Collection of cumulative weekly vaccine uptake for 2 year-olds and 3 year-olds started in 2013/2014.

(ii) School-aged children For school-aged children, monthly vaccination uptake estimates were available. These uptake estimates specified the proportion of children in England who received the influenza vaccine via school, pharmacy or GP practice.

1.5 Vaccine efficacy

We informed vaccine efficacy estimates for each historical influenza season from publications detailing end-of-season seasonal influenza vaccine effectiveness for adults and children in preventing laboratory-confirmed influenza in primary care in the United Kingdom [14–20]. In seasons where an equivalent publication were not available, we used mid-season or provisional end-of-season seasonal vaccine efficacy estimates from Public Health England reports [21, 22].

The 2009/10 season was an exception. Due to the adjusted seasonal influenza vaccine efficacy being -30% (-89%, 11%) [14], we instead used the pandemic vaccine to inform efficacy against A(H1N1)pdm09, with the effectiveness against all other types set to zero.

The all age, strain-specific vaccine efficacy estimates gathered from the literature are displayed in Table S1. With the empirical data not providing individual estimates for each influenza A subtype and influenza B lineage, we invoked a series of assumptions to produce the strain-specific vaccine efficacy quantities used within our study (Table 1).

We outline herein the set of enacted assumptions.

Approach to address absent influenza A efficacy data

Case one: Data absent for a single subtype only

Applicable to the following seasons: 2014/2015, 2015/2016, 2016/2017.

When there were estimates present for overall influenza A efficacy, but estimates for only one of the H1N1, H3N2 subtypes, for the subtype with no efficacy data we assumed its efficacy matched the overall influenza A efficacy estimate.

Case two: Data absent for all influenza A and one subtype

Applicable to the following seasons: 2010/2011,2011/2012.

In those seasons where there is an efficacy estimate for one of the two influenza A subtypes, but efficacy estimates for the other influenza A subtype and against influenza A overall are absent, we assumed the efficacy for the subtype with no relevant empirical data available was equal to that of the other influenza A subtype (for which there is an available estimate).

Approach to address absent influenza B efficacy data

Case one: Data absent for a single lineage only

Applicable to the following seasons: 2015/2016, 2016/2017.

When there were estimates present for overall influenza B efficacy, but estimates for only one of the B/Yam and B/Vic lineages, for the subtype with no efficacy data we assumed its efficacy matched the overall influenza B efficacy estimate.

Case two: Data absent for both lineages, but present for all influenza B

Applicable to the following seasons: 2011/2012, 2012/2013, 2013,2014, 2014/2015, 2017/2018.

In those seasons where there was an overall influenza B efficacy estimate, but efficacy estimates for both influenza B lineages were absent, we assumed the vaccine efficacy for both lineages matched the overall influenza B efficacy estimate.

Table S1: Adjusted vaccine effectiveness estimates for influenza by season and strain type. 95% confidence intervals are stated within parentheses.

Season	Vaccine efficacy (95% CI)						Source
	A(H1N1)pdm09	A(H3N2)	All A	B/Yamagata	B/Victoria	All B	
2009/10	72 (21, 90)	0	—	0	0	0	[14]*
2010/11	56 (42, 66)	—	—	-34 (-448, 68))	78 (51, 91)	57 (42,68)	[15]
2011/12	—	23 (-10, 47)	—	—	—	92 (38, 99)	[16]
2012/13	73 (37, 89)	26 (-4, 48)	35 (11, 53)	—	—	51 (34, 63)	[17]
2013/14	—	—	61 (-8, 86)	—	—	61 (-8, 86)	[21]†
2014/15	—	29.3 (8.6, 45.3)	29.9 (10.5, 45.1)	—	—	46.3 (13.9, 66.5)	[18]
2015/16	54.5 (41.6, 64.5)	—	54.5 (41.6, 64.5)	—	57.3 (28.4, 74.6)	54.2 (33.1, 68.6)	[19]
2016/17	—	31.6 (10.3, 47.8)	36.7 (18.3, 51.0)	58.5 (3.1, 82.2)	—	54.5 (10.8, 76.8)	[20]
2017/18	66.3 (33.4, 82.9)	-16.4 (-59.3, 14.9)	—	—	—	24.7 (1.1, 42.7)	[22]‡

*: The adjusted seasonal influenza vaccine efficacy in the 2009/10 season was -30% (-89%, 11%) [14]. We therefore used the pandemic vaccine to inform efficacy against A(H1N1)pdm09, with the effectiveness against all other types set to zero.

†: Mid-season estimate of seasonal influenza vaccine effectiveness from [21]. Low incidence throughout the 2013/2014 influenza season meant reliable end-of-season estimates for the vaccine efficacy could not be attained (Personal communication, Public Health England).

‡: Provisional end-of-season influenza vaccine effectiveness results.

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2 Complementary details of the modelling approach

2.1 Epidemiological model specifics

Figure S4 depicts the epidemiological model, capturing within season vaccination and transmission dynamics.

Fig. S4: Epidemiological model schematic. Diagram of the compartmentalisation of the population based on an SEIR model, in conjunction with non-vaccinated (N) and vaccinated (V) statuses under a "leaky" vaccination assumption. Epidemiological processes are represented by dashed lines. Vaccination processes are represented by solid lines. Demographic process (births and deaths) have been omitted. Compartments situated within the shaded region signify vaccinated groups, with vaccination occurring at rate μ. Transmission events lead to movement from a susceptible state (S) to latent (E,infected but not yet infectiousness). Latency is lost at rate $\gamma_{1,m}$. Infected (I) transition to recovered (R) at rate γ_2. Equivalent formulation for each strain m.

The epidemiological model is a deterministic, non-age, multi-strain structured compartmental based model capturing demography, influenza infection status (with susceptible-latent-infected-recovered, SEIR, dynamics) and vaccine uptake. In addition, we assumed disease transmission to be frequency-dependent.

We let E_m^X, I_m^X and R_m^X denote the proportion of the population that have vaccination status $X \in \{N, V\}$ (indexed by N for non-vaccinated, V for vaccinated), and that are latent, infectious and recovered (as a result of natural infection) with respect to strain m.

Exposure to influenza virus in the previous influenza season, through natural infection or vaccination, modulated current influenza season susceptibility. To incorporate exposure history from the previous influenza season, we let $S^{X,h}$ denote the proportion of the population that have vaccination status $X \in \{N, V\}$ and exposure history h that are susceptible to all strains.

The epidemiological model has the following formulation, with time dependencies dropped:

$$
\begin{cases}
\frac{dS^N}{dt} & = B - \left(\sum\limits_{m} \left(\sum\limits_{h} f(h,m) S^{N,h} \right) \lambda_m \right) - \mu S^N - D S^N \\[2mm]
\frac{dE_m^N}{dt} & = \left(\sum\limits_{h} f(h,m) S^{N,h} \right) \lambda_m - \gamma_{1,m} E_m^N - \mu E_m^N - D E_m^N \\[2mm]
\frac{dI_m^N}{dt} & = \gamma_{1,m} E_m^N - \gamma_2 I_m^N - \mu I_m^N - D I_m^N \\[2mm]
\frac{dR_m^N}{dt} & = \gamma_2 I_m^N - \mu R_m^N - D R_m^N \\[2mm]
\frac{dS^V}{dt} & = - \left(\sum\limits_{m} \left(\sum\limits_{h} f(h,m) S^{N,h} \right) (1-\alpha_m) \lambda_m \right) + \mu S^N - D S^V \\[2mm]
\frac{dE_m^V}{dt} & = \left(\sum\limits_{h} f(h,m) S^{V,h} \right) (1-\alpha_m) \lambda_m - \gamma_{1,m} E_m^V + \mu E_m^N - D E_m^V \\[2mm]
\frac{dI_m^V}{dt} & = \gamma_{1,m} E_m^V - \gamma_2 I_m^V + \mu I_m^N - D I_m^V \\[2mm]
\frac{dR_m^V}{dt} & = \gamma_2 I_m^V + \mu R_m^N - D R_m^V
\end{cases}
\tag{1}
$$

where $\gamma_{1,m}$ is the strain-dependent rate of loss of latency, γ_2 the rate of loss of infectiousness, α_m the strain-specific vaccine efficacy, and $\mu = \frac{\nu}{S^N + \sum\limits_{m}(E_m^N + I_m^N + R_m^N)}$ with ν the rate of vaccination in the population.

To maintain a constant population size, birth and death rates were equal ($B = D$). We set the mortality rate based upon a gender-averaged life expectancy for newborns in England, computed from male and female specific statistics from ONS data [23]. We computed the gender-averaged life expectancy for newborns in England to be approximately 81 years, with the corresponding daily mortality rate being $D = \frac{1}{81 \times 365}$.

The strain specific force of infection, λ_m, satisfies $\lambda_m = \beta_m \sum\limits_{X} I_m^X$, where β_m is the transmission rate for strain m, implicitly comprising the contact rate and the transmissibility of the virus (the probability that a contact between an infectious person and a susceptible person leads to transmission).

2.2 Between season exposure history group mappings

At the beginning of each influenza season (1st September), we enacted the following exposure history group assignments:

- $S^N \rightarrow S^{N,h=\bar{N}}$
- $S^V \rightarrow S^{N,h=\bar{V}}$
- $\left\{ E^{N,m}, I^{N,m}, R^{N,m} \right\} \rightarrow S^{N,h=m}$
- $\left\{ E^{V,m}, I^{V,m}, R^{V,m} \right\} \rightarrow S^{N,h=m\&\bar{V}}$

where X represents vaccination status, with N corresponding to non-vaccinated and V vaccinated (bars on vaccination state symbols relate to vaccination status in the previous influenza season).

3 Parameter inference

The aim of our parameter estimation was to select parameter sets generating influenza-attributed ILI GP consultation model predictions that best resemble the empirical data.

In full, we sought to estimate: transmissibility of each influenza virus strain (q_m), modified susceptibility to strain m given infection by a strain m type virus the previous season (a), carry over cross-reactivity protection between influenza B lineages (b), proportion of prior season vaccine efficacy propagated to the current season (ξ), and an ascertainment probability per influenza season (ϵ_t).

We selected an Approximate Bayesian Computation (ABC) approach, where results are first simulated with a parameter set, after which it is rejected or accepted based on a divergence measure or statistic.

We sought parameter sets that: (i) adhered to our infection prevalence temporal profile check; the peak in influenza infection could not occur after February (i.e. during March through August inclusive) in any season; (ii) minimised our deviance statistic, measuring the correspondence of the model predicted influenza-attributed ILI GP consultations versus the observed data (Equation 1).

To update the parameter sets we employed an adaptive population Monte Carlo ABC algorithm [24], an ABC scheme combined with particle Monte Carlo methods to minimise the number of simulations.

Outlining the inference scheme in brief, we initially drew 10,000 particles (i.e. 10,000 parameter sets) from the prior distributions, simulated and calculated their statistics. From these first-generation particles, each with equal weight, we generated 10,000 additional particles. Next, we sampled new particles according to the weight of the first generation particles and perturbed according to a multivariate normal distribution with twice the weighted variance-covariance matrix (computed using analytic weights) of the first generation particles. After simulation of the new particles, we computed their statistics and new weights. Of the now 20,000 particles, we retained the 10,000 particles with the lowest statistics.

The procedure was repeated iteratively, except all subsequent perturbations were carried out with a local perturbation kernel. Local perturbation kernels assign a different covariance matrix for each particle of the previous population. The class of perturbation kernel we selected was the multivariate normal kernel with optimal local covariance matrix (OLCM) [25]. We ran the process for at least 600 generations.

The final generation of 10,000 particles represents a sample from the posterior distribution. We utilised the retained particles for counterfactual and forward projection.

4 Additional results

4.1 Fitting to the empirical data (2012/13-2017/18 influenza seasons)

Fig. S5: Example time series displaying proportion of population in infected states (latent or infectious). Grey lines represent the simulated infected prevalence time series for 10 retained parameter sets from the inference procedure. With each simulation replicate starting on 1st September, red dashed vertical lines designate the beginning of March in each year. As stipulated by our parameter selection criteria, peak infection occurs prior to the 1st March.

Fig. S6: Posterior predictive influenza positive GP visit distributions: 2012/13 influenza season. Empirical data point estimate and bootstrap samples are depicted by the red diamond and green shaded regions respectively. Blue dots denote posterior predicted replicates. **(left)** Type A versus type B; **(top right)** influenza A subtypes, A(H1N1)pdm09 versus A(H3N2); **(bottom right)** influenza B lineages, B/Yamagata versus B/Victoria.

Fig. S7: Posterior predictive influenza positive GP visit distributions: 2013/14 influenza season. Empirical data point estimate and bootstrap samples are depicted by the red diamond and green shaded regions respectively. Blue dots denote posterior predicted replicates. **(left)** Type A versus type B; **(top right)** influenza A subtypes, A(H1N1)pdm09 versus A(H3N2); **(bottom right)** influenza B lineages, B/Yamagata versus B/Victoria.

Fig. S8: Posterior predictive influenza positive GP visit distributions: 2014/15 influenza season. Empirical data point estimate and bootstrap samples are depicted by the red diamond and green shaded regions respectively. Blue dots denote posterior predicted replicates. **(left)** Type A versus type B; **(top right)** influenza A subtypes, A(H1N1)pdm09 versus A(H3N2); **(bottom right)** influenza B lineages, B/Yamagata versus B/Victoria.

Fig. S9: Posterior predictive influenza positive GP visit distributions: 2015/16 influenza season. Empirical data point estimate and bootstrap samples are depicted by the red diamond and green shaded regions respectively. Blue dots denote posterior predicted replicates. **(left)** Type A versus type B; **(top right)** influenza A subtypes, A(H1N1)pdm09 versus A(H3N2); **(bottom right)** influenza B lineages, B/Yamagata versus B/Victoria.

Fig. S10: Posterior predictive influenza positive GP visit distributions: 2016/17 influenza season. Empirical data point estimate and bootstrap samples are depicted by the red diamond and green shaded regions respectively. Blue dots denote posterior predicted replicates. **(left)** Type A versus type B; **(top right)** influenza A subtypes, A(H1N1)pdm09 versus A(H3N2); **(bottom right)** influenza B lineages, B/Yamagata versus B/Victoria.

Fig. S11: Posterior predictive influenza positive GP visit distributions: 2017/18 influenza season. Empirical data point estimate and bootstrap samples are depicted by the red diamond and green shaded regions respectively. Blue dots denote posterior predicted replicates. **(left)** Type A versus type B; **(top right)** influenza A subtypes, A(H1N1)pdm09 versus A(H3N2); **(bottom right)** influenza B lineages, B/Yamagata versus B/Victoria.

4.2 Fitting to subsets of the empirical data

To delve into model robustness, we sought parameter fits using subsets of the historical influenza season data. Categorically, we fit to two datasets. The first covered four influenza seasons spanning 2012/13-2015/16. The second also included the 2016/17 influenza season, bringing the total number of influenza seasons to five.

Invoking the adaptive population Monte Carlo ABC scheme upon each dataset, we obtained 10,000 parameter sets following the completion of 1,100 and 1,000 generations respectively (Figs. S12 and S13). To view detailed summary statistic per parameter, we refer the reader to Table S2.

We witness agreement with the statistical fit to the full dataset on the following aspects : (i) influenza A transmissibility exceeding type B virus transmissibility; (ii) amongst the three mechanisms for immunity propagation, retained natural infection in the previous influenza season having the greatest influence; (iii) little support for immunity propagation originating from influenza B cross-reactivity (b attaining values near 1); (iv) quantitatively similar ascertainment probabilities.

Whilst outcomes fitting to a range of influenza seasons generally exhibited qualitative consistency, there were notable quantitative differences. Transmissibility magnitudes were raised, with the transmissibility of the A(H3N2) subtype exceeding that of the A(H1N1)pdm09 subtype (whereas in the complete fit we inferred similar transmissibility values for the type A viruses). The elevated transmissibility levels were counteracted by the enlarged effect of prior infection and vaccination reducing susceptibility. Explicitly, while the parameter distributions inferred fitting to the period 2012/13-2017/18 indicated little residual vaccine immunity and an estimated 20% drop in strain-specific susceptibility as a result of natural infection in the previous season, when fitting to the shorter time window susceptibility at the outset of an influenza season against a given strain type saw a near 55% reduction if naturally infected in the prior season by a virus of that class, and roughly 40% of prior season vaccine efficacy was retained (Table S2).

In a similar fashion to the dataset encompassing influenza seasons ranging from 2012/13 up to and including 2017/18, we found strong, qualitative correspondence between simulations of the paramterised model and the data (Figs. S14 and S15).

(a)

(b)

Fig. S12: Results of the ABC scheme, fitting to empirical data covering 2012/13-2015/16 influenza seasons (inclusive). (a) Summary metric threshold value upon completion of each generation of the inference scheme. The inset panel displays the latter quarter of generations. **(b)** Inferred parameter distributions estimated from 10,000 retained samples following completion of 1,100 generations of the inference scheme. Vertical red lines indicate the median values for the model constants estimated from the inference procedure.

(a)

(b)

Fig. S13: Results of the ABC scheme, fitting to empirical data covering 2012/13-2016/17 influenza seasons (inclusive). (a) Summary metric threshold value upon completion of each generation of the inference scheme. The inset panel displays the latter quarter of generations. (b) Inferred parameter distributions estimated from 10,000 retained samples following completion of 1,000 generations of the inference scheme. Vertical red lines indicate the median values for the model constants estimated from the inference procedure.

(a)

(b)

Fig. S14: Posterior predictive influenza positive GP consultation distributions, post-fitting to the empirical data covering the 2012/13-2015/16 influenza seasons (inclusive). We generated the estimated distributions from 1,000 model simulations, each using a distinct parameter set from the retained collection of particles. **(a)** Back-to-back stacked bars per simulation replicate. Each influenza season is topped out by a thicker stacked horizontal bar plot, corresponding to the strain-stratified point estimates for the empirical data. **(b)** Comparison of model simulated outcomes (shaded violin plots, with filled circles corresponding to the median value across the simulated replicates) versus the observed data (crosses denote the point estimate, with solid bars the range of the bootstrapped empirical data).

(a)

(b)

Fig. S15: Posterior predictive influenza positive GP consultation distributions, post-fitting to the empirical data covering the 2012/13-2016/17 influenza seasons (inclusive). We generated the estimated distributions from 1,000 model simulations, each using a distinct parameter set from the retained collection of particles. **(a)** Back-to-back stacked bars per simulation replicate. Each influenza season is topped out by a thicker stacked horizontal bar plot, corresponding to the strain-stratified point estimates for the empirical data. **(b)** Comparison of model simulated outcomes (shaded violin plots, with filled circles corresponding to the median value across the simulated replicates) versus the observed data (crosses denote the point estimate, with solid bars the range of the bootstrapped empirical data).

Table S2: Values (posterior quantiles) for the transmission, exposure history and ascertainment probability parameters inferred fitting to 2012/13-2015/16, 2012/13-2016/17 and 2012/13-2017/18 influenza season data. Numbers inside brackets indicate 95% credible intervals. All values are given to 4 d.p.

Description	Notation	Median [95% credible interval]		
		2012/13-2015/16	2012/13-2016/17	2012/13-2017/18
Transmission parameters				
A(H1N1)pdm09	$\beta_{A(H1N1)pdm09}$	0.4036 [0.4031, 0.4042]	0.4136 [0.4129, 0.4144]	0.3955 [0.3880, 0.4039]
A(H3N2)	$\beta_{A(H3N2)}$	0.4203 [0.4197, 0.4210]	0.4298 [0.4289, 0.4308]	0.3984 [0.3904, 0.4076]
B/Victoria	$\beta_{B/Victoria}$	0.3831 [0.3827, 0.3836]	0.3912 [0.3906, 0.3918]	0.3548 [0.3498, 0.3603]
B/Yamagata	$\beta_{B/Yamagata}$	0.3945 [0.3939, 0.3950]	0.4038 [0.4031, 0.4045]	0.3694 [0.3635, 0.3759]
Exposure history parameters				
Natural infection in prior season	a	0.4665 [0.4645, 0.4686]	0.4753 [0.4729, 0.4777]	0.7898 [0.7834, 0.7966]
Type B influenza cross-reactivity	b	1.0000 [1.0000, 1.000]	1.0000 [0.9999, 1.0000]	0.9797 [0.9511, 0.9983]
Prior season vaccine efficacy carry over	ξ	0.3797 [0.3766, 0.3825]	0.3992 [0.3951, 0.4032]	0.0061 [0.0004, 0.0163]
Ascertainment probabilities				
2012/13	$\epsilon_{2012/13}$	0.0019 [0.0019, 0.0019]	0.0017 [0.0017, 0.0018]	0.0017 [0.0015, 0.0018]
2013/14	$\epsilon_{2013/14}$	0.0012 [0.0012, 0.0012]	0.0011 [0.0011, 0.0011]	0.0010 [0.0009, 0.0012]
2014/15	$\epsilon_{2014/15}$	0.0027 [0.0027, 0.0027]	0.0025 [0.0025, 0.0026]	0.0024 [0.0022, 0.0026]
2015/16	$\epsilon_{2015/16}$	0.0036 [0.0036, 0.0036]	0.0034 [0.0033, 0.0034]	0.0036 [0.0033, 0.0040]
2016/17	$\epsilon_{2016/17}$	—	0.0013 [0.0013, 0.0013]	0.0014 [0.0012, 0.0015]
2017/18	$\epsilon_{2017/18}$	—	—	0.0051 [0.0047, 0.0055]

4.3 Parameter identifiability

We generated and used a synthetic dataset to verify the parameter identifiability capabilities of our ABC inference scheme. To mimic the format of our empirical data, the synthetic data corresponded to strain-specific influenza positive ILI GP consultations rates per 100,000 population from the 2012/13 to 2017/18 influenza season (inclusive). The parameter values we used for producing the synthetic are listed in Table S3.

When fitting the model to the synthetic data, we employed our inference scheme in an equivalent manner as for fitting to the empirical data. We ably recovered the parameter values from which the synthetic data had been generated (Fig. S16 and Table S3). Furthermore, simulated outcomes from each parameter set had strong agreement with the synthetic data (Fig. S17).

Table S3: Values (posterior quantiles) for the transmission, exposure history and ascertainment probability parameters inferred fitting to synthetic data. Numbers inside brackets indicate 95% credible intervals. All values are given to 4 d.p.

Description	Notation	'True' Value	Median [95% CI]
Transmission parameters			
A(H1N1)pdm09	$\beta_{A(H1N1)pdm09}$	0.4200	0.4203 [0.4171, 0.4235]
A(H3N2)	$\beta_{A(H3N2)}$	0.4300	0.4303 [0.4270, 0.4336]
B/Victoria	$\beta_{B/Victoria}$	0.4150	0.4153 [0.4123, 0.4182]
B/Yamagata	$\beta_{B/Yamagata}$	0.4050	0.4053 [0.4025, 0.4080]
Exposure history parameters			
Modified susceptibility given natural infection in prior season	a	0.5837	0.5837 [0.5809, 0.5864]
Modified susceptibility due to type B influenza cross-reactivity	b	0.4351	0.4349 [0.4126, 0.4568]
Prior season vaccine efficacy carry over	ξ	0.7026	0.7038 [0.6935, 0.7133]
Ascertainment probabilities			
2012/13	$\epsilon_{2012/13}$	0.0015	0.0015 [0.0015, 0.0015]
2013/14	$\epsilon_{2013/14}$	0.0007	0.0007 [0.0007, 0.0007]
2014/15	$\epsilon_{2014/15}$	0.0023	0.0023 [0.0023, 0.0023]
2015/16	$\epsilon_{2015/16}$	0.0021	0.0021 [0.0020, 0.0022]
2016/17	$\epsilon_{2016/17}$	0.0004	0.0004 [0.0004, 0.0004]
2017/18	$\epsilon_{2017/18}$	0.0030	0.0030 [0.0029, 0.0030]

(a)

(b)

Fig. S16: Results of the ABC scheme, fitting to synthetic data. (a) Summary metric threshold value upon completion of each generation of the inference scheme. The inset panel displays the latter quarter of generations. **(b)** Inferred parameter distributions estimated from 10,000 retained samples following completion of 1,000 generations of the inference scheme. Vertical red lines indicate the median values for the model constants estimated from the inference procedure, and vertical black lines correspond to the true values of the parameters from which the data were generated. We ably recovered the parameter values from which the synthetic data had been generated.

Fig. S17: Posterior predictive distributions for influenza positive GP consultations per 100,000 population, using the parameter sets generated when fitting to the synthetic data. Stratified by influenza season, we present back-to-back stacked bars for 1,000 simulation replicates, each using a distinct parameter set representing a sample from the posterior distribution when fitting our mathematical model to the synthetic data. Each influenza season is topped by a thicker stacked horizontal bar plot, corresponding to the synthetic data values. The left side depicts the cumulative total of ILI GP consultations attributable to type A influenza per 100,000 population (red shading denoting the A(H1N1)pdm09 subtype, orange shading the A(H3N2) subtype). In an equivalent manner, the right side stacked horizontal bars present similar data for type B influenza (cyan shading denoting the B/Victoria lineage, dark blue shading the B/Yamagata lineage). Overall, simulated outcomes from each parameter set had strong agreement with the synthetic data.

5 Model extension: Immunity propagation across multiple influenza seasons

In our extended model, we altered the immunity propagation model component. The vaccination, epidemiological and observation model components were all unchanged.

We display a modified directed acyclic graph, which includes the revised immunity propagation component structure and incorporation of the data streams (Fig. S18).

Fig. S18: Schematic showing the links between the vaccination, immunity propagation, epidemiological and observation model components for the extended model. We adopt the visualisation conventions of [26], with ellipses indicating variables, and rectangles indicating data. Dotted arrows indicate relationships between prior season epidemiological outcomes and immunity propagation factors. Solid arrows indicate within season processes. Circled capitalised letters indicate the relationships connecting the variables or data involved. These relationships are: process A, propagation of immunity as a result of exposure to influenza virus in the previous influenza season (through natural infection or vaccination); process B, modulation of current influenza season virus susceptibility; process C, estimation of influenza case load via the SEIR model of transmission; process D, ascertainment of cases through ILI recording at GP.

5.1 Details of the expanded immunity propagation mechanism

As before, we tracked immunity derived from natural infection and vaccination separately. We kept our three, original susceptibility modifying factors: (i) modified susceptibility to strain m given infection by a strain m type virus the previous season, denoted a; (ii) carry over cross-reactivity protection between influenza B lineages, denoted b (to account for infection with one influenza B virus lineage being potentially beneficial in protecting against subsequent infection with either influenza B virus lineage [27]); (iii) residual strain-specific protection carried over from the prior season influenza vaccine, denoted c_m. We again mandated that $0 < a, b, c_m < 1$.

To enhance the flexibility of the immunity propagation component, we introduced and fit an additional parameter, δ, representing the proportion of those who both began the influenza season in an exposure history group linked to natural infection (Fig. 3: rows 2-5, 7-10) and were

unexposed to influenza virus during the current season (who at the end of of the current influenza season remained susceptible), that retained their pre-existing natural infection acquired immunity. Those keeping immunity arising from natural infection were mapped to the relevant prior infection exposure history group dependent upon current season vaccination status. The remaining proportion $(1 - \delta)$ transitioned in the same manner as in the original model, reverting to either the naive exposure history group or vaccinated only exposure history group (Fig. S19).

For clarity, there was no mechanism in the model framework to confer vaccine-induced immunity beyond one influenza season (i.e. vaccine-induced immunity could be retained for, at most, a single additional influenza season). As before, the collection of exposure history groupings and associated strain-specific susceptibilities were consolidated into a single susceptibility array (Fig. S18, process B; Fig. 3).

5.2 Between season exposure history group assignments

At the beginning of each influenza season (1st September), we enacted the following exposure history group assignments:

- $\left\{ S^{N,h=\bar{N}}, S^{N,h=\bar{V}}, (1-\delta)S^{N,h=m}, (1-\delta)S^{N,h=m\&\bar{V}} \right\} \to S^{N,h=\bar{N}}$

- $\left\{ S^{V,h=\bar{N}}, S^{V,h=\bar{V}}, (1-\delta)S^{V,h=m}, (1-\delta)S^{V,h=m\&\bar{V}} \right\} \to S^{N,h=\bar{V}}$

- $\left\{ \delta S^{N,h=m}, \delta S^{N,h=m\&\bar{V}}, E^{N,m}, I^{N,m}, R^{N,m} \right\} \to S^{N,h=m}$

- $\left\{ \delta S^{V,h=m}, \delta S^{V,h=m\&\bar{V}}, E^{V,m}, I^{V,m}, R^{V,m} \right\} \to S^{N,h=m\&\bar{V}}$

where X represents vaccination status, with N corresponding to non-vaccinated and V vaccinated in the current influenza season (bars on vaccination state symbols relate to vaccination status in the previous influenza season).

Fig. S19: Mechanism for conferring immunity to influenza across multiple influenza seasons. At the beginning of a generic influenza season y, those susceptible may be divided into two categories based on exposure history: (i) susceptibles in either the naive exposure history group , with unmodified susceptibility to infection, or in the vaccinated only exposure history group (labelled S); (ii) all those that are susceptible and in an exposure history group involving natural infection (labelled $\hat{S}$). During the influenza season, those that were initially susceptible may be infected (state I). Of those remaining in state $\hat{S}$ at the end of season y, a proportion δ are retained in state $\hat{S}$ at the beginning of season $y + 1$. The remainder $(1 - \delta)$ transition to state S. Note, $\delta = 0$ corresponds to no residual immunity being retained due to natural infection beyond one subsequent influenza season, while $\delta = 1$ coincides with residual immunity being kept in all future seasons until the occurrence of a new infection event.

Table S4: Overview of parameters in the extended model.

Description	Notation	Value	Sources
Fixed parameters			
Mortality rate (day^{-1})	B,D	$\frac{1}{81\times365}$	[23]
Rate of latency loss, influenza A subtypes (day^{-1})	$\gamma_{1,A}$	$\frac{1}{1.4}$	[28]
Rate of latency loss, influenza B lineages (day^{-1})	$\gamma_{1,B}$	$\frac{1}{0.6}$	[28]
Recovery rate (day^{-1})	γ_2	$\frac{1}{3.8}$	[29]
Time-varying parameters			
Vaccination rate at time t	$\nu(t)$	—	[6, 7, 11]
Vaccine efficacy, season y strain m	α_m^y	—	[14–22]

Inferred parameter description	Notation	Prior
Influenza virus transmissibility, strain m	β_m	$\mathcal{U}(0.2632,0.7896)$
Modified susceptibility given natural infection in prior season	a	$\mathcal{U}(0,1)$
Modified susceptibility due to type B influenza cross-reactivity	b	$\mathcal{U}(0,1)$
Proportion of prior season vaccine efficacy carried over	ξ	$\mathcal{U}(0,1)$
Fraction unexposed retaining immunity	δ	$\mathcal{U}(0,1)$
Ascertainment probability in season y	ϵ_y	$\mathcal{U}(0,0.05)$

5.3 Fitting the extended model to the data

We performed parameter inference using an equivalent ABC scheme to that used to fit the original model. For the extended model, we fit the following collection of parameters (Table S4): transmissibility of each influenza virus strain (β_m), modified susceptibility to strain m given infection by a strain m type virus the previous season (a), carry over cross-reactivity protection between influenza B lineages (b), residual protection carried over from the prior season influenza vaccine (ξ), the fraction unexposed in the prior influenza season that retain immunity (δ), and an ascertainment probability per influenza season (ϵ_y).

We amassed 10,000 parameter sets (representing a sample from the posterior distribution) to determine credible values of the model parameters (Table S5). Samples were obtained after completion of 750 generations of the adaptive-population Monte Carlo ABC scheme, at which point the generation-by-generation tolerance level updates were minor (Fig. S20(a)). Note that the error values attained for the parameter sets inferred for the extended model closely matched the error values for the parameter sets inferred for the original (less complex) model. The inferred model parameters for the extended model were well defined with Gaussian-shaped histograms (Fig. S20(b)).

Comparing the parameter fits to those for the original model, we maintained the main outcome of propagation of immunity being weaker if vaccine derived, compared to natural immunity from infection. As before, we inferred little carry over of prior season vaccine efficacy, with the majority of the posterior distribution for ξ massed near 0.

We found several other similarities amongst the transmission parameters and ascertainment probabilities when comparing the two model fits. Virus transmission rates were larger for the two influenza A subtypes than than the corresponding estimates for the two type B lineages,

and B/Yamagata transmissibility estimates exceeded those for B/Victoria. Furthermore, for each influenza season the ascertainment probability distributions closely resembled each other. An exception was, for all strains, inferred virus transmission rate distributions for the extended model being shifted towards larger values.

Discrepancies did arise amongst parameters tied to immunity processes. First, a decrease in value for parameter a, corresponding to the modified susceptibility to a given influenza type that results from natural infection by a prior influenza virus of that type (median values, extended model vs original model: 0.7163 vs 0.7898). These predictions correspond to an almost 30% reduction in susceptibility in the extended model compared to little more than 20% in the original model. Second, posterior distributions for b imply a similar amount of modulation to susceptibility via influenza B cross-reactivity. This is in stark contrast to the less complex model, where there was little support for carry over of type B influenza cross-reactivity from one influenza season to the next (median values: 0.7267 vs 0.9797).

Inspecting the posterior distribution for δ, the majority of samples attained values greater than 0.9. The inferred magnitude implies long term retention of immunity acquired from natural infection (assuming no further vaccination or infection event to alter the immunity landscape), in agreement with prior studies supporting infection acquired immunity waning over a time scale exceeding a year [30–32]).

Performing 1,000 independent simulations of the extended model with parameter sets drawn from the ABC inference procedure, we found a remarkably similar fit to the data with the extended model (Fig. S21) compared to the less complex, original model (Figs. 5-6). Thus, despite the added complexity, the extended model did not give noticeable improvements in correspondence of model outputs with the data (relative to fits with a model using the simpler immunity propagation setup).

Table S5: Values (posterior quantiles) for the transmission, exposure history and ascertainment probability parameters inferred fitting the extended model to the empirical data. Numbers inside brackets indicate 95% credible intervals. All values are given to 4 d.p.

Description	Notation	Median [95% credible interval]
Transmission parameters		
A(H1N1)pdm09	$\beta_{\text{A(H1N1)pdm09}}$	0.4115 [0.4094, 0.4136]
A(H3N2)	$\beta_{\text{A(H3N2)}}$	0.4307 [0.4283, 0.4332]
B/Victoria	$\beta_{\text{B/Victoria}}$	0.3617 [0.3602, 0.3631]
B/Yamagata	$\beta_{\text{B/Yamagata}}$	0.3735 [0.3722, 0.3748]
Exposure history parameters		
Natural infection in prior season	a	0.7163 [0.7146, 0.7181]
Type B influenza cross-reactivity	b	0.7267 [0.7020, 0.7512]
Prior season vaccine efficacy propagation	ξ	0.0004 [0.0000, 0.0012]
Fraction unexposed retaining immunity	δ	0.9589 [0.9319, 0.9863]
Ascertainment probabilities		
2012/13	$\epsilon_{2012/13}$	0.0018 [0.0018, 0.0019]
2013/14	$\epsilon_{2013/14}$	0.0011 [0.0010, 0.0011]
2014/15	$\epsilon_{2014/15}$	0.0025 [0.0024, 0.0026]
2015/16	$\epsilon_{2015/16}$	0.0038 [0.0038, 0.0039]
2016/17	$\epsilon_{2016/17}$	0.0014 [0.0014, 0.0015]
2017/18	$\epsilon_{2017/18}$	0.0052 [0.0052, 0.0053]

(a)

Fig. S20: Results of the ABC scheme, fitting the extended model to the empirical data.
(a) Summary metric threshold value upon completion of each generation of the inference scheme. The inset panel displays the latter quarter of generations. **(b)** Inferred parameter distributions estimated from 10,000 retained samples following completion of 750 generations of the inference scheme. Vertical red lines indicate the median values for the model constants estimated from the inference procedure. Particularly noteworthy outcomes include: transmissibility of type A viruses exceeding type B viruses; vaccine carry over had little impact on present season susceptibility; support for immunity stemming from natural infection being retained long term; the highest ascertainment probability occurred in the 2017/18 influenza season.

(a)

(b)

Fig. S21: Posterior predictive influenza positive GP consultation distributions, post-fitting the extended model to the empirical data covering the 2012/13-2017/18 influenza seasons (inclusive). We generated the estimated distributions from 1,000 model simulations, each using a distinct parameter set from the retained collection of particles. (a) Back-to-back stacked bars per simulation replicate. Each influenza season is topped out by a thicker stacked horizontal bar plot, corresponding to the strain-stratified point estimates for the empirical data. (b) Comparison of model simulated outcomes (shaded violin plots, with filled circles corresponding to the median value across the simulated replicates) versus the observed data (crosses denote the point estimate, with solid bars the range of the bootstrapped empirical data).

5.4 Parameter identifiability

We again generated and used a synthetic dataset to verify the parameter identifiability capabilities of our ABC inference scheme under the revised model framework. The synthetic data corresponded to strain-specific influenza positive ILI GP consultations rates per 100,000 population from the 2012/13 to 2017/18 influenza season (inclusive), to mimic the format of our empirical data. The parameter values we used for producing the synthetic are listed in Table S6.

Once more, we ably recovered the parameter values from which the synthetic data had been generated (Fig. S22 and Table S6). Furthermore, simulated outcomes from each parameter set had strong agreement with the synthetic data (Fig. S23).

Table S6: Values (posterior quantiles) for the transmission, exposure history and ascertainment probability parameters inferred fitting the extended model to synthetic data. Numbers inside brackets indicate 95% credible intervals. All values are given to 4 d.p.

Description	Notation	'True' Value	Median [95% CI]
Transmission parameters			
A(H1N1)pdm09	$\beta_{A(H1N1)pdm09}$	0.4200	0.4203 [0.4166, 0.4238]
A(H3N2)	$\beta_{A(H3N2)}$	0.4300	0.4303 [0.4265, 0.4339]
B/Victoria	$\beta_{B/Victoria}$	0.4150	0.4153 [0.4117, 0.4187]
B/Yamagata	$\beta_{B/Yamagata}$	0.4050	0.4052 [0.4019, 0.4085]
Exposure history parameters			
Modified susceptibility given natural infection in prior season	a	0.5837	0.5837 [0.5779, 0.5893]
Modified susceptibility due to type B influenza cross-reactivity	b	0.4351	0.4340 [0.4114, 0.4568]
Prior season vaccine efficacy carry over	ξ	0.7026	0.7036 [0.6886, 0.7184]
Fraction unexposed retaining immunity	δ	0.1	0.0999 [0.0859, 0.1136]
Ascertainment probabilities			
2012/13	$\epsilon_{2012/13}$	0.0015	0.0015 [0.0015, 0.0015]
2013/14	$\epsilon_{2013/14}$	0.0007	0.0007 [0.0007, 0.0007]
2014/15	$\epsilon_{2014/15}$	0.0023	0.0023 [0.0023, 0.0023]
2015/16	$\epsilon_{2015/16}$	0.0021	0.0021 [0.0020, 0.0022]
2016/17	$\epsilon_{2016/17}$	0.0004	0.0004 [0.0004, 0.0004]
2017/18	$\epsilon_{2017/18}$	0.0030	0.0030 [0.0029, 0.0031]

Fig. S22: Results of the ABC scheme, fitting the extended model to synthetic data. (a) Summary metric threshold value upon completion of each generation of the inference scheme. The inset panel displays the latter tenth of generations. **(b)** Inferred parameter distributions estimated from 10,000 retained samples following completion of 1,650 generations of the inference scheme. Vertical red lines indicate the median values for the model constants estimated from the inference procedure, and vertical black lines correspond to the true values of the parameters from which the data were generated. We ably recovered the parameter values from which the synthetic data had been generated.

Fig. S23: Posterior predictive distributions for influenza positive GP consultations per 100,000 population, using the parameter sets generated fitting the extended model to the synthetic data. Stratified by influenza season, we present back-to-back stacked bars for 1,000 simulation replicates, each using a distinct parameter set representing a sample from the posterior distribution when fitting our mathematical model to the synthetic data. Each influenza season is topped by a thicker stacked horizontal bar plot, corresponding to the synthetic data values. The left side depicts the cumulative total of ILI GP consultations attributable to type A influenza per 100,000 population (red shading denoting the A(H1N1)pdm09 subtype, orange shading the A(H3N2) subtype). In an equivalent manner, the right side stacked horizontal bars present similar data for type B influenza (cyan shading denoting the B/Victoria lineage, dark blue shading the B/Yamagata lineage). Overall, simulated outcomes from each parameter set had strong agreement with the synthetic data.

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