Making the most of Clumping and Thresholding for polygenic scores

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Abstract

Polygenic prediction has the potential to contribute to precision medicine. Clumping and Thresholding (C+T) is a widely used method to derive polygenic scores. When using C+T, people usually test several p-value thresholds to maximize predictive ability of derived polygenic scores. Along with this p-value threshold, we propose to tune 3 other hyper-parameters for C+T. We implement an efficient way to derive C+T scores corresponding to many different sets of hyper-parameters. For example, you can now derive thousands of different C+T scores for 300K individuals and 1M variants in less than one day. We show that tuning 4 hyper-parameters of C+T consistently improves its predictive performance in both simulations and real data applications as compared to tuning only the p-value threshold.

Using this grid of computed C+T scores, we further extend C+T with stacking. More precisely, instead of choosing one set of hyper-parameters that maximizes prediction in some training set, we propose to learn an optimal linear combination of all these C+T scores using an efficient penalized regression. We call this method Stacked Clumping and Thresholding (SCT) and show that this makes C+T more flexible. When the training set is large enough, SCT can provide much larger predictive performance as compared to any of the C+T scores individually.

1 Introduction

The ability to predict disease risk accurately is a principal aim of modern precision medicine. As more population-scale genetic datasets become available, polygenic risk scores (PRS) are expected to become more accurate and clinically relevant. The most commonly used method for computing polygenic scores is Clumping and Thresholding (C+T), also known as pruning and thresholding (P+T). The C+T polygenic score is defined as the sum of allele counts (genotypes), weighted by estimated effect sizes obtained from genome-wide association studies, where two filtering steps have been applied (Wray *et al.* 2007; Purcell *et al.* 2009; Dudbridge 2013; Wray *et al.* 2014; Euesden *et al.* 2014; Chatterjee *et al.* 2016). More precisely, the variants are first clumped (C) so that only variants that are weakly correlated with one another are retained. Clumping looks at the most significant variant iteratively, computes correlation between this index variant and nearby variants within some genetic distance w_c, and removes all the nearby variants that are correlated with this index variant beyond a particular value r_c^2. Thresholding (T) consists in removing variants with a p-value larger than a chosen level of significance ($p > p_T$). Both steps, clumping and thresholding, represent a statistical compromise between signal and noise. The clumping step prunes redundant correlated effects caused by linkage disequilibrium (LD) between variants. However, this procedure may also remove independently predictive variants in nearby LD regions. Similarly, thresholding must balance between including predictive variants and reducing noise in the score by excluding null effects. This is why hyper-parameters of clumping and thresholding must be chosen with care when using C+T in order to maximize its predictive ability.

When applying C+T, one has 3 hyper-parameters to select, namely the squared correlation threshold r_c^2 and the window size w_c of clumping, along with the p-value threshold p_T. Usually, C+T users assign default values for clumping, such as r_c^2 of 0.1 (default of PRSice), 0.2 or 0.5 (default of PLINK), and w_c of 250kb (default of PRSice and PLINK) or 500kb, and test several values for p_T ranging from 1 to 10^{-8} (Purcell *et al.* 2009; Wray *et al.* 2014; Euesden *et al.* 2014; Chang *et al.* 2015). Moreover, to match the variants of summary statistics and to compute the PRS, the target sample genotypes are usually imputed to some degree of precision. Liberal inclusion of imputed variants is common, assuming that using more variants in the model yields better prediction, whatever the imputation accuracy of these variants. Here, we explore the validity of this approach and suggest an additional $INFO_T$ threshold on the quality of imputation (often called the INFO score) as a fourth parameter of the C+T method.

We implement an efficient way to compute C+T scores for many different parameters (LD, window size, p-value and INFO score) in R package bigsnpr (Privé *et al.* 2018). Using a training set, one could therefore choose the best predictive C+T model among a large set of C+T models with many different parameters, and then evaluate this model in a test set. Moreover, instead of choosing one set of parameters that corresponds to the best prediction, we propose to use stacking, i.e. we learn an optimal linear combination of all computed C+T scores using an efficient penalized regression to improve prediction beyond the best prediction provided by any of these scores (Breiman 1996). We call this method SCT, which stands for Stacked Clumping and Thresholding. Using the UK Biobank

data (Bycroft *et al.* 2018) and external summary statistics for simulated and real data analyses, we show that testing a larger grid of parameters consistently improves predictions as compared to using some default parameters for C+T. We also show that SCT consistently improves prediction compared to any single C+T model when sample size of the training set is large enough.

2 Material and Methods

2.1 Clumping and Thresholding (C+T) and Stacked C+T (SCT)

We compute C+T scores *for each chromosome separately* and for several parameters:

- Threshold on imputation INFO score INFO_T within $\{0.3, 0.6, 0.9, 0.95\}$.

- Squared correlation threshold of clumping r_c^2 within $\{0.01, 0.05, 0.1, 0.2, 0.5, 0.8, 0.95\}$.

- Base size of clumping window within $\{50, 100, 200, 500\}$. The window size w_c is then computed as the base size divided by r_c^2. For example, for $r_c^2 = 0.2$, we test values of w_c within $\{250, 500, 1000, 2500\}$ (in kb). This is motivated by the fact that linkage disequilibrium is inversely proportional to genetic distance between variants (Pritchard and Przeworski 2001).

- A sequence of 50 thresholds on p-values between the least and the most significant p-values, equally spaced on a log-log scale.

Thus, for individual i, chromosome k and the four hyper-parameters INFO_T, r_c^2, w_c and p_T, we compute C+T predictions

$$V_i^{(k)}\left(\text{INFO}_T,\ r_c^2,\ w_c,\ p_T\right) = \sum_{j \in S_{\text{clumping}}(k,\ \text{INFO}_T,\ r_c^2,\ w_c)} \hat{\beta}_j \cdot G_{i,j} \cdot \mathbb{1}\{p_j < p_T\},$$

where $\hat{\beta}_j$ (p_j) are the effect sizes (p-values) estimated from the GWAS, $G_{i,j}$ is the dosage for individual i and variant j, and the set $S_{\text{clumping}}(k,\ \text{INFO}_T,\ r_c^2,\ w_c)$ corresponds to first restricting to variants of chromosome k with an INFO score $\geq \text{INFO}_T$ and that further result from clumping with parameters r_c^2 and w_c.

Overall, we compute $22 \times 4 \times 7 \times 4 \times 50 = 123200$ vectors of polygenic scores. Then, we stack all these polygenic scores (for individuals in the training set) by using these scores as explanatory variables and the phenotype as the outcome in a regression setting (Breiman 1996). In other words, we fit weights for each C+T scores using an efficient penalized logistic regression available in R package bigstatsr (Privé *et al.* 2019). This results in a linear combination of C+T scores, where C+T scores are merely linear combinations of variants, so that we can derive a single vector of effect sizes corresponding to each variant. The single vector of new variant effects resulting from stacking C+T scores is used for evaluation in the test set. We refer to this method as "SCT" in the rest of the paper.

From this grid of 123,200 vectors of polygenic scores, we also derive two C+T scores for comparison. First, "stdCT" is the standard C+T score using some default parameters, i.e. with $r_c^2 = 0.2$, $w_c = 500$, a liberal threshold of 0.3 on imputation INFO score, and choosing the p-value threshold ($\geq 10^{-8}$)

maximizing the AUC on the training set (Wray *et al.* 2014). Second, "maxCT" is the C+T score maximizing the AUC on the training set among the 5600 (123200 / 22) C+T scores corresponding to all different sets of parameters tested. Note that stdCT and maxCT use the same set of parameters for all chromosomes, i.e. for one set of the four hyper-parameters, they are defined as $V^{(1)} + \cdots + V^{(22)}$. In contrast, SCT uses the whole matrix of 123,200 vectors.

2.2 Simulations

We use variants from the UK Biobank (UKBB) imputed dataset that have a minor allele frequency larger than 1% and an imputation INFO score larger than 0.3. There are almost 10M such variants, of which we randomly choose 1M. To limit population structure and family structure, we restrict individuals to the ones identified by the UK Biobank as British with only subtle structure and exclude all second individuals in each pair reported by the UK Biobank as being related (Bycroft *et al.* 2018). This results in a total of 335,609 individuals that we split into three sets: a set of 315,609 individuals for computing summary statistics (GWAS), a set of 10,000 individuals for training hyper-parameters and lastly a test set of 10,000 individuals for evaluating models.

We read the UKBB BGEN files using function `snp_readBGEN` from package bigsnpr (Privé *et al.* 2018). For simulating phenotypes and computing summary statistics, we read UKBB data as hard calls by randomly sampling hard calls according to reported imputation probabilities. For the training and test sets, we read these probabilities as dosages (expected values). This procedure enables us to simulate phenotypes using hard calls and then to use the INFO score (imputation accuracies) reported by the UK Biobank to assess the quality of the imputed data used for the training and test sets.

We simulate binary phenotypes with a heritability $h^2 = 0.5$ using a Liability Threshold Model (LTM) with a prevalence of 10% (Falconer 1965). We vary the number of causal variants (100, 10K, or 1M) in order to match a range of genetic architectures from low to high polygenicity. Liability scores are computed from a model with additive effects only: we compute the liability score of the i-th individual as $y_i = \sum_{j \in S_{\text{causal}}} w_j \widetilde{G_{i,j}} + \epsilon_i$, where S_{causal} is the set of causal variants, w_j are weights generated from a Gaussian distribution $N(0, h^2/|S_{\text{causal}}|)$, $G_{i,j}$ is the allele count of individual i for variant j, $\widetilde{G_{i,j}}$ corresponds to its standardized version (zero mean and unit variance), and ϵ follows a Gaussian distribution $N(0, 1 - h^2)$.

We explore three additional scenarios with more complex architectures. In scenario "2chr", 100 variants of chromosome 1 and all variants of chromosome 2 are causal with half of the heritability for both chromosomes; it aims at assessing predictive performance when disease architectures are different for different chromosomes. In scenario "err", we sample 10,000 random causal variants but 10% of the GWAS effects are reported with an opposite effect in the summary statistics; it aims at assessing if methods are able to partially correct for errors or mere differences in effect sizes between GWAS and the target data. In scenario "HLA", 7105 causal variants are chosen in one long-range LD region of chromosome 6; it aims at assessing if methods can handle strong correlation between causal variants.

To compute summary statistics, we use Cochran-Armitage additive test (Zheng *et al.* 2012). Given that we restricted the data to have minimal population structure, this test based on contingency tables is much faster than using a logistic regression with 10 principal components as covariates (a few minutes vs several hours) while providing similar effect sizes and Z-scores (Figure S1).

In simulations, we compare four methods: stdCT, maxCT, SCT (defined in section 2.1) and lassosum (Mak *et al.* 2017). Each simulation scenario is repeated 10 times and the average AUC is reported. We prefer to use AUC over Nagelkerke's R^2 because AUC has a desirable property of being independent of the proportion of cases in the validation sample; one definition of AUC is the probability that the score of a randomly selected case is larger than the score of a randomly selected control (Wray *et al.* 2013). An alternative to AUC would be to use a better R^2 on the liability scale (Lee *et al.* 2012; Allegrini *et al.* 2019).

2.3 Real summary statistics

We also investigate predictive performance of C+T and SCT in the UK Biobank using external summary statistics from published GWAS of real diseases, for which we summarize the number of individuals and variants in table 1 (Buniello *et al.* 2018). As in simulations, we restrict individuals to the ones identified by the UK Biobank as British with only subtle structure and exclude all second individuals in each pair reported by the UK Biobank as being related (Bycroft *et al.* 2018). Table 1 also summarizes the number of cases and controls in the UKBB, after this filtering and for each phenotype analyzed. For details on how we define phenotypes in the UKBB, please refer to our R code (Section 2.4). Briefly, we use self-reported illness codes (field #20001 for cancers and #20002 otherwise) and ICD10 codes (fields #40001, #40002, #41202 and #41204 for all diseases, and field #40006 specifically for cancers).

Table 1: Number of cases and controls in UK Biobank (UKBB) for several disease phenotypes, along with corresponding published GWAS summary statistics. Summary statistics are chosen from GWAS that did not include individuals from UKBB. For depression, we remove UKBB individuals from the pilot release since they were included in the GWAS from which we use summary statistics.

Trait	UKBB size	GWAS size	GWAS #variants	GWAS citation
Breast cancer (BRCA)	11,578 / 158,391	137,045 / 119,078	11,792,542	Michailidou *et al.* (2017)
Rheumatoid arthritis (RA)	5615 / 226,327	29,880 / 73,758	9,739,303	Okada *et al.* (2014)
Type 1 diabetes (T1D)	771 / 314,547	5913 / 8828	8,996,866	Censin *et al.* (2017)
Type 2 diabetes (T2D)	14,176 / 314,547	26,676 / 132,532	12,056,346	Scott *et al.* (2017)
Prostate cancer (PRCA)	6643 / 141,321	79,148 / 61,106	20,370,946	Schumacher *et al.* (2018)
Depression (MDD)	22,287 / 255,317	59,851 / 113,154	13,554,550	Wray *et al.* (2018)
Coronary artery disease (CAD)	12,263 / 225,927	60,801 / 123,504	9,455,778	Nikpay *et al.* (2015)
Asthma	43,787 / 261,985	19,954 / 107,715	2,001,280	Demenais *et al.* (2018)

We keep all variants with a GWAS p-value lower than 0.1 except for prostate cancer (0.05) and asthma (0.5). This way, we keep around 1M variants for each phenotype, deriving all C+T scores and stacking them in SCT in less than one day for each phenotype, even when using 300K individuals in the training set. To match remaining summary statistics with data from the UK Biobank, we first remove ambiguous alleles [A/T] and [C/G]. We then augment the summary statistics twice: first by

duplicating each variant with the complementary alleles, then by duplicating variants with reverse alleles and effects. Finally, we include only variants that we match with UKBB based on the combination of chromosome, position and the two alleles. Note that, when no or very few alleles are flipped, we disable the strand flipping option and therefore do not remove ambiguous alleles; this is the case for all phenotypes analyzed here. For example, for type 2 diabetes, there are 1,408,672 variants in summary statistics ($p < 0.1$), of which 215,821 are ambiguous SNPs. If we remove these ambiguous SNPs, 1,145,260 variants are matched with UKBB, of which only 38 are actually flipped. So, instead, we do not allow for flipping and do not remove ambiguous alleles, then 1,350,844 variants are matched with UKBB.

Training SCT and choosing optimal hyper-parameters for C+T (stdCT and maxCT) use 63%-90% of the UK Biobank data reported in table 1. The training set can therefore contain as many as 300K individuals. To assess how sample size affects predictive performance of methods, we also compare these methods using a much smaller training set of 500 cases and 2000 controls.

2.4   Reproducibility

The code to reproduce the analyses and figures of this paper is available as R scripts at `https://github.com/privefl/simus-PRS/tree/master/paper3-SCT` (R Core Team 2018). To execute these scripts, you need to have access to the UK Biobank data that we are not allowed to share (`http://www.ukbiobank.ac.uk/`). A quick introduction to SCT is also available at `https://privefl.github.io/bigsnpr/articles/SCT.html`.

3   Results

3.1   Simulations

We test 6 different simulations scenarios. In all these scenarios, maxCT –that tests a much larger grid of hyper-parameters values for C+T on the training set– consistently provides higher AUC values on the test set as compared to stdCT that tests only several p-value thresholds while using default values for the other parameters (Figure 1). The absolute improvement in AUC of maxCT over stdCT is particularly large in the cases of 100 and 10,000 causal variants, where causal effects are mostly independent of one another. In these cases, using a very stringent $r_c^2 = 0.01$ threshold of clumping provides higher predictive performance than using a standard default of $r_c^2 = 0.2$ (Figures S4a and S4b). However, $r_c^2 = 0.2$ provides best predictive performance when simulating 1M causal variants. Still, using a large window size w_c of 2500 kb increases AUC as compared to using default values of either 250 or 500 kb (Figure S4c).

As for SCT, it provides equal or higher predictive performance than maxCT in the different simulation scenarios (Figure 1). In the first three simple scenarios simulating 100, 10K or 1M causal variants anywhere on the genome, predictive performance of SCT are similar to maxCT. In the "2chr" scenario where there are large effects on chromosome 1, small effects on chromosome 2 and no effect

Figure 1: Results of the 6 simulation scenarios: (100) 100 random causal variants; (10K) 10,000 random causal variants; (1M) all 1M variants are causal variants; (2chr) 100 variants of chromosome 1 are causal and all variants of chromosome 2, with half of the heritability for both chromosomes; (err) 10,000 random causal variants, but 10% of the GWAS effects are reported with an opposite effect; (HLA) 7105 causal variants in a long-range LD region of chromosome 6. Mean and 95% CI of 10^4 non-parametric bootstrap replicates of the mean AUC of 10 simulations for each scenario. The blue dotted line represents the maximum achievable AUC for these simulations (87.5% for a prevalence of 10% and an heritability of 50% – see equation (3) of Wray *et al.* (2010)). See corresponding values in table S1.

on other chromosomes, mean AUC is 78.7% for maxCT and 82.2% for SCT. In the "err" scenario where we report GWAS summary statistics with 10% reversed effects (errors), mean AUC is 70.2% for maxCT and 73.2% for SCT. SCT also provides higher AUC than lassosum, expect when simulating all variants as causal (1M).

Effects resulting from SCT (Figure S3) are mostly comprised between the GWAS effects and 0. For the simulation with only 100 causal variants, resulting effects are either nearly the same as in the GWAS, or near 0 (or exactly 0). When there are some correlation between causal predictors (Scenarios "1M" and "HLA") or when reporting GWAS effects with some opposite effect ("err"), some effects resulting from SCT are in the opposite direction as compared to the GWAS effects.

3.2   Real summary statistics

In terms of AUC, maxCT outperfoms stdCT for all 8 diseases consireded with a mean absolute increase of 1.3% (Figures 2 and S2). A particularly large increase can be noted when predicting depression status (MDD), from an AUC of 55.7% (95% CI: [54.4-56.9]) with stdCT to an AUC of

59.2% (95% CI: [58.0-60.4]) with maxCT. For MDD, a liberal inclusion in clumping ($r_c^2 = 0.8$) and a stringent threshold on imputation accuracy ($\text{INFO}_T = 0.95$) provides the best predictive performance (Figure S6f). For all 8 diseases, predictions were optimized when choosing a threshold on imputation accuracy of at least 0.9, whereas optimal values for r_c^2 where very different depending on the architecture of diseases, with optimal selected values over the whole range of tested values for r_c^2 (Table S3).

Figure 2: AUC values on the test set of UKBB (mean and 95% CI from 10^4 bootstrap samples). Training SCT and choosing optimal hyper-parameters for C+T use 63%-90% of the data reported in table 1. See corresponding values in table S2.

Furthermore, when training size uses a large proportion of the UK Biobank data, SCT outperforms maxCT for all 8 diseases considered with an additional mean absolute increase of AUC of 2.2%, making it 3.5% as compared to stdCT (Figure 2 and table S2). Predictive performance improvement of SCT versus maxCT is particularly notable for coronary artery disease (2.8%), type 2 diabetes (3.1%) and asthma (3.4%).

Effects resulting from SCT have mostly the same sign as initial effects from GWAS, with few effects being largely unchanged, and others having an effect that is shrunk to 0 or equals to 0, i.e. variants not included in the final model (Figure S5).

When training size is smaller (500 cases and 2000 controls only instead of 200K-300K individuals), SCT is not as good as when training size is large, yet SCT remains a competitive method expect for depression for which maxCT performs much better than SCT (Figure S2).

4 Discussion

4.1 Predictive performance improvement of C+T

C+T has the advantage that it is intuitive and an easily applicable method for obtaining polygenic scores trained on GWAS summary statistics. Two popular pieces of software that implement C+T, PLINK and PRSice, have further contributed to the prevalence of C+T (Purcell *et al.* 2007; Euesden *et al.* 2014; Chang *et al.* 2015). Usually, C+T scores for different p-value thresholds are derived, using some default values for the other 3 hyper-parameters. In R package bigsnpr, we extend C+T to efficiently consider more hyper-parameters (4 by default) and enable the user to define their own qualitative variant annotations to filter on (e.g. minor allele frequency could be used as a fifth parameter). Using simulated and real data, we show that choosing different values rather than default ones for these hyper-parameters can substantially improve the performance of C+T, making C+T a very competitive method. Indeed, in our simulations (Figure 1), we found that optimizing C+T (maxCT) performed on par with more sophisticated methods such as lassosum. Moreover, it is possible to rerun the method using a finer grid in a particular range of these hyper-parameters. For example, it might be useful to include variants with p-values larger than 0.1 for predicting rheumatoid arthritis and depression (Figures S6b and S6f). Another example would be to focus on a finer grid of large values of r_c^2 for coronary artery disease (Figure S6g), or to focus on a finer grid of stringent imputation thresholds only (Table S3).

Using a large grid of C+T scores for different hyper-parameters, we show that stacking these scores instead of choosing the best one improves prediction further (Breiman 1996). Combining multiple PRS is not a new idea (Krapohl *et al.* 2018; Inouye *et al.* 2018), but we push this idea to the limit by combining 123,200 polygenic scores. This makes SCT more flexible than any C+T model, but it of course also requires a larger training dataset with individual-level genotypes and phenotypes to learn the weights in stacking.

Normally, cross-validation should be used to prevent overfitting when using stacking and it is also suggested to use positivity constraints in stacking (Breiman 1996). However, cross-validation is not necessary here since building C+T scores does not make use of the phenotype of the training set that is later used in the stacking; the training set is only used to choose the best set of hyper-parameters for C+T. Moreover, we allow C+T scores to have negative weights in the final model for three reasons. First, because C+T scores are overlapping in the variants they use, using some negative weights allows to weight groups of variants that correspond to the difference of two sets of variants. Second, because of LD, variants may have different effects when learned jointly with others (Figures S3c and S3f). Third, if reported GWAS effects are heterogenous between the GWAS dataset and the validation or target dataset, then having variants with opposite effects can help adjust the effects learned during GWAS.

4.2 Limitations of the study

In this study, we limited the analysis to 8 common diseases and disorders, as these all had substantial number of cases and publicly available GWAS summary statistics based on substantial sample sizes. For example, for psychiatric disease, we include only depression (MDD) because diseases such as schizophrenia and bipolar disorder have very few cases in the UK Biobank; dedicated datasets should be used to assess effectiveness of maxCT and SCT for such diseases. We also do not analyze many autommimune diseases because summary statistics are often outdated (2010-2011[1]) and, because there are usually large effects in regions of chromosome 6 with high LD, methods that use individual-level data instead of summary statistics are likely to provide better predictive models (Privé *et al.* 2019). We also chose not to analyze any continuous trait such as height or BMI because there are many individual-level data available in UKBB for such phenotypes and methods directly using individual-level data are likely to provide better predictive models for predicting in UKBB than the ones using summary statistics (Privé *et al.* 2019; Chung *et al.* 2019). Phenotypes with tiny effects such as educational attainment for which huge GWAS summary statistics are available might be an exception (Lee *et al.* 2018).

The principal aim of this work is to study and improve the widely used C+T method. The idea behind C+T is simple as it directly uses weights learned from GWAS; it further removes variants as one often does when reporting hits from GWAS, i.e. only variants that pass the genome-wide threshold (p-value thresholding) and that are independent association findings (clumping) are reported. Yet, there are two other established methods based on summary statistics, LDpred and lassosum (Vilhjálmsson *et al.* 2015; Mak *et al.* 2017; Allegrini *et al.* 2019). Several other promising and more complex methods such as NPS, PRS-CS and SBayesR are currently being developed (Chun *et al.* 2019; Ge *et al.* 2019; Lloyd-Jones *et al.* 2019). Here, we include lassosum in the simulations since no other method yet shown that they provide some improvement over lassosum. In addition, we found lassosum to be easy to set up and use. However, lassosum requires substantial computation time when there are too many samples or too many variants. Therefore, we did not apply lassosum to the full UK Biobank data. A full comparison of methods (including individual-level data methods), including binary and continuous traits with different architectures, using different sizes of summary statistics and individual-level data for training, and in possibly different populations would be of great interest, but is out of scope for this paper. Indeed, we believe that different methods may perform very differently in different settings and that understanding what method is appropriate for each case is of paramount interest if the aim is to maximize prediction accuracy to make PRS clinically useful.

4.3 Extending SCT

The stacking step of SCT can be used for either binary or continuous phenotypes. Yet, for some diseases, it makes sense to include age in the models, using for example Cox proportional-hazards model to predict age of disease onset, with possibly censored data (Cox 1972). Cox regression has already proven useful for increasing power in GWAS (Hughey *et al.* 2019). Currently, we support linear and

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[1]https://www.immunobase.org/downloads/protected_data/GWAS_Data/

logistic regressions in our efficient implementation of package bigstatsr, but not Cox regression. This is an area of future development; for now, if sample size is not too large, one could use R package glmnet to implement stacking based on Cox model (Tibshirani *et al.* 2012).

One might also want to use other information such as sex or ancestry (using principal components). Indeed, it is easy to add covariates in the stacking step as (possibly unpenalized) variables in the penalized regression. Yet, adding covariates should be done with caution (see the end of supplementary materials).

Finally, note that we added an extra parameter in the SCT pipeline that makes possible for an user to define their own groups of variants. This allows to refine the grid of computed C+T scores and opens many possibilities for SCT. For example, we could derive and stack C+T scores for two (or more) different GWAS summary statistics, e.g. for different ancestries or for different phenotypes. This would effectively extend SCT as a multivariate method. We could also learn to differentiate between two genetically different phenotypes with similar symptoms such as type 1 and type 2 diabetes, which is in our research interests.

4.4 Conclusion

In this paper, we focused on understanding and improving the widely-used C+T method by testing a wide range of hyper-parameters values. More broadly, we believe that any implementation of statistical methods should come with an easy and effective way to choose hyper-parameters of these methods well. We believe that C+T will continue to be used for many years as it is both simple to use and intuitive. Moreover, as we show, when C+T is optimized using a larger grid of hyper-parameters, it remains a competitive method since it can adapt to many different disease architectures by tuning all hyper-parameters.

Moreover, instead of choosing one set of hyper-parameters, we show that stacking C+T predictions improves predictive performance further. SCT has many advantages over any single C+T prediction: first, it can learn different architecture models for different chromosomes, it can learn a mixture of large and small effects and it can more generally adapt initial weights of the GWAS in order to maximize prediction. Moreover, SCT remains a linear model with one vector of coefficients as it is a linear combination (stacking) of linear combinations (C+T scores).

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Supplementary Materials

Figure S1: Comparison of estimated effect sizes (**A**) and Z-scores (**B**) if computed using a logistic regression with 10 principal components as covariates, or with a simple Cochran-Armitage additive test. Phenotypes were simulated using 100 causal variants only, allowing for large effects.

Table S1: AUC values on the test set for simulations (mean [95% CI] from 10^4 bootstrap samples).

Scenario	stdCT	maxCT	SCT	lassosum
100	79.8 [77.0-82.0]	86.9 [86.6-87.3]	86.3 [85.8-86.8]	83.2 [81.8-84.2]
10K	72.5 [71.8-73.3]	75.1 [74.7-75.5]	76.0 [75.5-76.6]	74.9 [74.3-75.6]
1M	68.9 [68.3-69.4]	69.5 [68.8-70.0]	69.0 [68.5-69.6]	70.4 [70.0-70.9]
2chr	77.2 [76.7-77.7]	78.6 [78.0-79.2]	82.2 [81.8-82.7]	78.9 [78.4-79.4]
err	69.8 [68.9-70.7]	70.7 [70.1-71.2]	73.2 [72.5-73.9]	72.1 [71.5-72.8]
HLA	78.7 [78.0-79.5]	79.8 [79.1-80.4]	80.7 [80.2-81.3]	79.4 [78.7-80.2]

Table S2: AUC values on the test set of UKBB (mean [95% CI] from 10^4 bootstrap samples) and the number of variants used in the final model. Training SCT and choosing optimal hyper-parameters for C+T use 63%-90% of the data reported in table 1.

Trait	stdCT	maxCT	SCT
Breast cancer (BRCA)	62.1 [60.5-63.6]	63.3 [61.7-64.8]	65.9 [64.4-67.4]
	6256	2572	670,050
Rheumatoid arthritis (RA)	59.8 [57.7-61.8]	60.3 [58.3-62.4]	61.3 [59.1-63.4]
	12,220	88,556	317,456
Type 1 diabetes (T1D)	75.4 [72.4-78.4]	76.9 [73.9-79.7]	78.7 [75.7-81.7]
	1112	267	135,991
Type 2 diabetes (T2D)	59.1 [58.1-60.1]	60.7 [59.8-61.7]	63.8 [62.9-64.7]
	177	33,235	548,343
Prostate cancer (PRCA)	68.0 [66.5-69.5]	69.3 [67.8-70.8]	71.7 [70.2-73.1]
	1035	356	696,575
Depression (MDD)	55.7 [54.4-56.9]	59.2 [58.0-60.4]	59.5 [58.2-60.7]
	165,584	222,912	524,099
Coronary artery disease (CAD)	59.9 [58.6-61.2]	61.1 [59.9-62.4]	63.9 [62.7-65.1]
	1182	87,577	315,165
Asthma	56.8 [56.2-57.5]	57.3 [56.7-58.0]	60.7 [60.0-61.3]
	3034	360	446,120

Table S3: Choice of C+T parameters based on the maximum AUC in the training set. Choosing optimal hyper-parameters for C+T use 63%-90% of the data reported in table 1.

Trait	w_c	r_c^2	$INFO_T$	p_T
Breast cancer (BRCA)	2500	0.2	0.95	2.2e-04
Rheumatoid arthritis (RA)	200	0.5	0.95	7.5e-02
Type 1 diabetes (T1D)	10K-50K	0.01	0.90	2.6e-05
Type 2 diabetes (T2D)	625	0.8	0.95	1.1e-02
Prostate cancer (PRCA)	10K-50K	0.01	0.90	4.2e-06
Depression (MDD)	625	0.8	0.95	1.0e-01
Coronary artery disease (CAD)	526	0.95	0.95	3.5e-02
Asthma	2500	0.2	0.90	2.2e-04

Figure S2: AUC values on the test set of UKBB (mean and 95% CI from 10^4 bootstrap samples). Training SCT and choosing optimal hyper-parameters for C+T use 500 cases and 2000 controls only. See corresponding values in table S4.

Table S4: AUC values on the test set of UKBB (mean [95% CI] from 10^4 bootstrap samples) and the number of variants used in the final model. Training SCT and choosing optimal hyper-parameters for C+T use 500 cases and 2000 controls only.

Trait	stdCT	maxCT	SCT
Breast cancer (BRCA)	62.2 [61.6-62.7]	63.4 [62.8-63.9]	62.9 [62.4-63.5]
Rheumatoid arthritis (RA)	59.2 [58.4-60.0]	59.5 [58.7-60.3]	59.5 [58.7-60.3]
Type 1 diabetes (T1D)	75.6 [72.4-78.7]	76.7 [73.6-79.8]	78.7 [75.5-81.8]
Type 2 diabetes (T2D)	59.8 [59.3-60.3]	60.2 [59.7-60.7]	61.0 [60.6-61.5]
Prostate cancer (PRCA)	67.1 [66.4-67.8]	68.7 [68.0-69.3]	69.3 [68.7-70.0]
Depression (MDD)	54.5 [54.1-54.9]	58.4 [58.0-58.8]	54.7 [54.3-55.1]
Coronary artery disease (CAD)	59.7 [59.2-60.3]	60.0 [59.5-60.5]	61.4 [60.8-61.9]
Asthma	56.2 [55.9-56.4]	56.9 [56.7-57.2]	57.2 [56.9-57.4]

(a) "100": 100 random causal variants

(b) "10K": 10,000 random causal variants

(c) "1M": all 1M variants are causal variants

(d) "2chr": Causal variants on chromosomes 1 & 2

(e) "err": 10,000 random causal variants, but 10% of the GWAS effects are reported with an opposite effect

(f) "HLA": 7105 causal variants in a long-range LD region of chromosome 6

Figure S3: New effect sizes resulting from SCT versus initial effect sizes of GWAS in the first simulation of each simulation scenario. Only non-zero effects are represented. Red line corresponds to the 1:1 line.

(a) "100": 100 random causal variants

(b) "10K": 10,000 random causal variants

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(f) "HLA": 7105 causal variants in a long-range LD region of chromosome 6

Figure S4: AUC values (for the training set) when predicting disease status for many parameters of C+T in the first simulation of each simulation scenario. Facets are presenting different clumping thresholds r_c^2 from 0.01 to 0.95, window sizes w_c from 52 to 50,000 kb, and imputation thresholds from 0.3 to 0.95. The x-axis corresponds to the remaining hyper-parameter, the p-value threshold p_T; here, -log10(p-values) are represented using a logarithmic scale.

(a) Breast cancer

(b) Rheumatoid arthritis

(c) Type 1 diabetes

(d) Type 2 diabetes

(e) Prostate cancer

(f) Depression

(g) Coronary artery disease

(h) Asthma

Figure S5: New effect sizes resulting from SCT versus initial effect sizes of GWAS in real data applications. Only non-zero effects are represented. Red line corresponds to the 1:1 line.

(a) Breast cancer

(b) Rheumatoid arthritis

(c) Type 1 diabetes

(d) Type 2 diabetes

(e) Prostate cancer

(f) Depression

(g) Coronary artery disease

(h) Asthma

Figure S6: AUC values (for the training set) when predicting disease status for many parameters of C+T in real data applications. Facets are presenting different clumping thresholds r_c^2 from 0.01 to 0.95, window sizes w_c from 52 to 50,000 kb, and imputation thresholds from 0.3 to 0.95. The x-axis corresponds to the remaining hyper-parameter, the p-value threshold p_T; here, -log10(p-values) are represented using a logarithmic scale.

Caution on using covariates

For example, because prevalence of CAD is much higher in men than in women in the UKBB (8-9% vs 2%), adding sex in the model amount to fitting two different intercepts, centering distributions of fitted probabilities around disease prevalence (Figure S7). This increases the AUC from 63.9% to 74.4% but results in a model that would classify all women as healthy. A possible solution would be to report AUC figures for each gender separately, or even to fit a model for each gender separately (in the stacking step). Fitting models separately would enable the use of sex chromosomes without introducing bias. As for ancestry concerns, fitting different models for different ancestries might be a way to get more calibrated results and to account for differences in effect sizes and LD. However, here for CAD, fitting two separate models for each gender results in a slight loss of predictive performance, while using variable 'sex' does not change results when they are reported for each gender separately, with an AUC of 64.9% [63.5-66.3] for men and 62.5% [59.8-65.2] for women. Thus, adding 'sex' as a covariate in the model may provide a model with similar discrimination and with better calibration of probabilities (if prevalence in the data is representative of prevalence in the population). Yet, we would like to emphasize again that reporting one AUC figure for all individuals would be misleading in the case of using variable 'sex' in the model.

Figure S7: Distribution of predicted probabilities of Coronary Artery Disease (CAD) in the UK Biobank using SCT. Upper / lower panels corresponds to women / men. Left panels correspond to a model using C+T scores and variable 'sex' when fitting penalized logistic regression in the stacking step. Right panels correspond to performing stacking of C+T scores without using variable 'sex'.