1   **An emergent flow of the nuclear array in syncytial embryos**
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Summary

Many aspects in tissue morphogenesis relay on the collective behavior of
participating cells. Despite a good understand of the underlying individual
processes, the mechanism for emergence of dynamic tissue behavior is
unclear in most cases. Here we reveal how isotropic elongation of mitotic
spindles drives an anisotropic collective flow of the nuclear array in syncytial
Drosophila embryos. We found that the asynchrony of nuclear divisions, which
is visible as a mitotic wave front sweeping over the embryo, allows elongation
of mitotic spindles beyond the average of inter-nuclear distances. As a
consequence of this overshooting, adjacent nuclei are pushed apart in early
interphase. Strikingly, the nuclei anisotropically move several nuclear diameter
away from the mitotic wave front, albeit the orientation of spindles was
isotropic. Shortly afterwards the nuclei return to their original position in a type
of elastic movement. We found that spindle overshooting drove directional
nuclear flow and that the elastic back and forth movement was controlled by
cortical actin. The nuclear array did not return to its original position in mutants
of the formin Dia and moved three times further away without returning in
mutants of the Rac activator ELMO. The actin cortex effectively acts as a
viscoelastic material with an *ELMO*-depending apparent viscosity and *dia-* and
ELMO-dependent apparent elasticity. Our analysis provides insight into the

molecular mechanism leading to the emergence of a collective flow
movement.
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Introduction
Early *Drosophila* embryo develop as a syncytium. Based on direct neighbor
interactions, the nuclei and their associated centrosomes and microtubule
asters form an extended two-dimensional array. The interactions between
individual nuclei lead to collective behavior at tissue level. At least three
features of emergent collective behavior can be observed. Firstly, the nuclei
divide synchronously to their immediate neighbors but asynchronously to more
distant nuclei. This leads to a wave front of mitoses sweeping over the
embryo[1,2]. Secondly, the nuclei arrange in an ordered array in interphase
following disturbance during nuclear division. Ordering involves interactions by
the microtubule asters but also with F-actin at the cortex[3,4]. Thirdly, the nuclei
and the cytoplasm undergo stereotypic flow movements following the mitotic
wave front. The mechanism for the emergence of this collective flow and its
underlying forces have not been studied yet.
60
Nuclear movements are likely driven by active elements of the cytoskeleton.
Candidates are the motor proteins of microtubules. During mitosis, the
daughter chromosomes are pushed apart by the mitotic spindle, which pushes
them close to adjacent nuclei. During interphase, nuclei potentially interact by
their astral microtubules, which originate from the centrosomes and link nuclei
to each other and to the cortex[5]. Force is potentially generated by sliding of
antiparallel aligned microtubules of adjacent asters.
68
In addition to microtubules, the actomyosin cytoskeleton may generate force.
No prominent actin structure is directly associated with the nuclei. Actomyosin
is largely found at the cortex and undergoes a stereotypic reorganization linked
to the nuclear cycle[6]. During mitosis, actin is associated with the metaphase
furrow which separates the spindles. Actin caps are prominent structures
during interphase. Myosin II is detected at the metaphase furrow and is
enriched at the cortical region between the caps in interphase[7].
76
77   Beside the force generating mechanism, the material properties of the
78   embryos[8-10] may influence the movement of the nuclei. The actin cytoskeleton
79   inhibits short time-scale movements[11] and promotes ordering of the nuclear
80   array[3]. The actin cortex may act as a viscoelastic medium, to which the
81   centrosomes and their associated nuclei are connected.
82
Here we found that the nuclear movement was isotropic for individual spindles
but anisotropic for the collective flow over several nuclear diameters away from

the mitotic wave front and back to the original position slightly later. We
comprehensively quantified nuclear trajectories in wild type and mutant
embryos and modelled the process by computational simulation. In this way,
we uncovered that spindle overshooting was a major driving force for the
collective movement of the nuclear array. In addition, we defined a function of
cortical F-actin for the apparent viscoelastic material properties.
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92 **Results**
93
Long mitotic spindles and distance between daughter nuclei require
pseudo-synchronous nuclear cycles
The nuclear density at the cortex doubles with every division during the
syncytial blastoderm (nuclear cycles NC 10–13) (Supp. Data Fig. S1). The
nuclei divide slightly asynchronous especially during the last syncytial division
in NC13 with a time lag of up to minutes, which is easily visible as a mitotic
wave front sweeping over the embryo (Fig. 1A, B, Supp. Data Movie 1). The
function and the consequences of this pseudo-synchrony are unknown. Given
the increase of asynchrony with nuclear density, we speculated that nuclear
crowding may pose a problem for synchronous divisions.
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To test this hypothesis, we simulated nuclear divisions within a limited area.
We assigned each nucleus and mitotic spindles a protected area representing
the entity in real embryos (Fig. 1C). After chromosome division, the daughter
nuclei were pushed apart until reaching the protected area of a neighboring
spindles/pair of daughter nuclei, thus assessing the maximal possible distance
between daughter nuclei (maximal spindle length). We assumed synchronous
divisions and symmetric spindles with isotropic orientations (Fig. 1D). Our
simulations showed that the maximal spindle length decreased with an
increase in nuclear number and thus marked the transition line between
structurally allowed and forbidden regime of combinations of nuclear density
and spindle length (Fig. 1E). Next, we measured the maximal distance
between daughter nuclei and their corresponding nuclear densities in wild type
embryos (Supp. Data Fig. S1). We also included data from haploid embryos,
which undergo an extra nuclear division. Only the parameters of NC11 fell into
the allowed area, whereas the parameters of NC12, NC13, and NC14 in
haploids fell into the forbidden regime. This analysis indicated that a
synchronous division with the observed spindle lengths was possible only in
the early cycles but impossible in later cycles. Thus, pseudo-synchrony allows
for the observed spindle length in NC12, NC13 and NC14 in haploid embryos.
124
Collective flow and density changes follow the mitotic wave front

The mitotic pseudo-synchrony and its corresponding wave front are associated
with a stereotypic nuclear movement, which can be readily observed in time
lapse movies (Fig. 2a, Supp. Data Movie 2). To obtain a precise description of
the nuclear movements, we determined the trajectories of all nuclei within the
field of view from time lapse recordings of fluorescently labeled nuclei. From
the trajectories, we extracted time courses for displacements, velocities, and
nuclear density (Fig. 2b, c, f). Every nucleus is assigned an individual time axis
with the splitting of daughter chromosomes (metaphase-anaphase transition)
as reference time t=0.

135
Concerning displacement (Fig. 2b), the nuclei moved in average about 20 µm
which corresponds to about 4–5 nuclear diameters away from the position of
their mother nucleus at t=0. The maximal displacement was reached after
about 2 min (Fig. 2b). Following maximal displacement, the nuclei then
returned to almost their initial position. We calculated the speed of nuclear
movement from the individual trajectories as the derivative of the trajectories.
The averaged flow speed revealed three peaks (Fig. 2c). The first peak
corresponds to the chromosome segregation in anaphase with about 0.4 µm/s.
The second peak after about 1 to 2 min corresponds to the flow away from the
mitotic wave front. The least pronounced, third peak corresponds to the return
movement after about 4 min (Fig. 2d).

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As flow is linked to density changes, we next established spatial and temporal
maps of nuclear density. Each nucleus was assigned an area and
corresponding density according to Voronoi segmentation (Fig. 2e, Supp. Data
Movie 3). In the case of synchronous divisions, the density would be expected
to double at t=0 (metaphase anaphase transition) and remain constant
throughout interphase. In contrast, but consistent with the observed nuclear
flow, our measurements revealed a peculiar time of the density. Although
initially doubling, the density dropped in telophase before finally reaching the
doubled density again a few minutes later (Fig. 2e, f). Corresponding profiles
for displacement and flows were detected in preceding nuclear cycles 11 and
12, although in a less pronounced manner (Supp. Data Fig. S3).

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The forth and back movement of the nuclei is reminiscent of a spring (Fig. 2g).
To obtain a phenomenological description of this behavior, we applied a simple
mechanical model to the nuclear trajectories during the period of maximal
displacement (Fig. 2h). By fitting a square function to the displacement curve,
we obtained an apparent spring constant for each nucleus. The actual value of
the apparent spring constant is not informative, since our model and
assumptions are too simple. Friction is not included, for example. Yet, the

apparent constant helps to compare experimental conditions and mutant
phenotypes.
169

Isotropic individual behavior is associated with an anisotropic collective flow

Our analysis revealed a collective directional flow of the nuclear array. Yet the individual spindles are isotropically oriented. The axes between daughter nuclei are uniformly distributed over the angles against the anterior-posterior axis of the embryo (Fig. 3a–c). In contrast, the same nuclei almost unidirectionally moved along the embryonic axis a minute later, indicating an anisotropic behavior (Fig. 3a–c). The transition of isotropic individual to anisotropic collective behavior is strikingly obvious in the extreme cases of spindle orientation. In the case of a spindle oriented in parallel to the embryonic axis, one set of chromosomes segregated towards, whereas the daughter chromosomes moved away the wave front during anaphase. One minute later both nuclei moved away from the wave front (Fig. 3d). Similarly, in case of a perpendicular orientation of chromosome segregation, the movement during anaphase was perpendicular to the embryonic axis but along the axis a minute later during collective flow. (Fig. 3d).

During collective flow the nuclei may move as individuals characterized by neighbor exchanges. Alternatively nuclei may behave as an array, which would be indicated by fixed neighbor relationships. To distinguish these options, we labeled groups of cells before mitosis and followed them during the course of chromosome segregation and collective flow. We found that the nuclei moved as an array. The groups of nuclei did neither intersperse with unlabeled nuclei nor nuclei of the other groups indicating that neighbor relationships were maintained during mitosis and collective flow despite the movement over several nuclear diameters (Fig. 3e). In summary, our observations indicate that the nuclear layer phenomenologically behaves like an elastic sheet with fixed neighbor relationships.

Computational modeling of nuclear movement points to spindle length as a major driver of collective behavior

To gain an understanding for how the isotropic individual movements give rise to an anisotropic collective flow, we conducted numerical simulations. Starting from a theoretical model based on static nuclear interactions in interphase[4], we added a time axis for the interactions to account for the changes during mitosis. The model is based on active and passive forces (Fig. 4a, Supp. Data Fig. S4). Stochastic active forces repulse adjacent nuclei, thus resembling the sliding activity of motor proteins, e. g. Kinesin-5, on antiparallel aligned microtubules. In addition, a passive elastic force leads to repulsion accounting for the

embedding of the nuclei into the cytoplasm and cytoskeleton. This may include
the link of the nuclei to the cortex. Chromosome segregation is triggered at t=0
by a separation force acting between the daughter nuclei. The interaction
forces are dynamic according to the mitotic stage and interphase (Fig. 4b). For
example, the active force is low in anaphase, since astral microtubules
prominently appear only in telo- and interphase. Similarly, the passive force
increases in telo- and interphase as cortical actin increases during these
stages. The segregation force decays in telo and interphase. Balancing the
magnitude of passive and active forces over time, model simulation
reproduced the experimentally observed stereotypic flow behavior (Fig. 4c, d,
Supp. Data Movie 4).
220
The simulations lead to multiple predictions. Firstly, the maximal displacement
was reach only about 1.5 min after the maximal distance between daughter
nuclei (maximal spindle length) was reached (Fig. 5a, b). The model predicted
a time lag between daughter separation and nuclear displacement. This is
interesting because it predicted that spindle separation may lead to
displacement but importantly in an indirect manner. Secondly, we tested the
role of pseudo-synchrony (speed of the mitotic wave front) of mitosis. The
model predicted a negative correlation (Fig. 5e), i.e. a slow wave leads to a
large displacement. Thirdly, the simulations predicted that the force for
separation of the daughter nuclei positively correlated with maximal distance
between daughter nuclei and importantly with maximal displacement (Fig. 6e,
Supp. Data Fig. S4b). Thus, our simulations predicted that spindle length is a
major driving force for nuclear movement. Mechanistically, this is not a simple
relationship because spindles are isotropically oriented, whereas the direction
of displacement is anisotropic.
236
We tested the predictions with experimental data. Consistent with the first
prediction (maximal spindle length precedes maximal displacement), we found
a time lag of 1–2 min in all embryos (Fig. 5c, d). The time lag demonstrated
that these two processes were mechanistically not directly linked, since
spindles were isotropically oriented and preceded the flow behavior. The
second prediction also matched the experimental data. We collected data from
50 embryos (Fig. 1b) for quantification of the speed of wave front and maximal
displacement. Plotting corresponding parameter sets revealed a negative
correlation (R^2=45%, Fig. 5f).
246
Ensemble spindle elongation is the driving force for nuclear
displacement
Providing an experimental test of the third prediction (Fig. 6e) required an
experimental condition, in which spindle extension but not spindle function

would be impaired. We experimentally tested the prediction in mutants with
shorter spindles. Spindle elongation in anaphase B requires the four-headed
microtubule motor Kinesin 5, which can slide microtubules against each
other[12]. We employed embryos, in which endogenous Kinesin 5 was
substituted by a version susceptible to TEV protease[5]. We titrated the amount
of TEV protease to achieve a partial depletion which still allowed completion of
mitosis. Spindles in these embryos were short (Fig. 6a). The average maximal
spindle length was 8 µm instead of 10 µm in wild type embryos.
Complementary, we employed embryos from females homozygous for *Map60*,
which also displayed short spindles[3] with an average length of 9 µm (Fig. 6a).
261
Consistent with the third prediction from the computer model, quantification of
nuclear movement revealed a strongly reduced maximal displacement in both
experimental conditions and thus a positive correlation of spindle length and
maximal displacement (Fig. 6b, c, d, f) Interestingly, the distances are different.
While division distance and maximal displacement are comparable (about 8
µm), maximal displacement is almost twice as the division distance. In
summary, as predicted by our computational model, analysis of mutant
embryos with shorter division distance support the model that an overshooting
of the mitotic spindle (pushing apart the daughter nuclei more than the average
inter-nuclear distance) constitutes a major driving force for the nuclear
movement thereafter.
273
F-actin cortex is required for the return movement.
We speculated that cortical F-actin is involved in nuclear movement. It has
been previously reported that the nuclei are strongly attached to F-actin
cortex[13]. The actin cortex suppresses the fluctuation movements of
centrosomes[11] and contributes to an ordered nuclear array in interphase[3].
Cortical F-actin undergoes stereotypic remodeling during the course of nuclear
cycles[6] (Fig. 7a). We quantified total F-actin with a Utrophin-GFP as a
marker[14]. We found that the signal dropped in mitosis, with lowest level during
anaphase and steadily increased afterwards (Fig. 7b, c). Given the timing of
this dynamics, it is conceivable that cortical actin plays an important part in
controlling nuclear movement.
285
To test this conceivable function of the cortical F-actin, we employed two
mutants to genetically interfere with the organization of the actin cortex. Firstly,
we prevented the formation of actin caps with the mutant *ELMO*[11,15]. ELMO
forms part of an unconventional guanyl nucleotide exchange factor, which
activates Rac signaling in a complex with Sponge/DOCK[16]. *ELMO* mutants
lack any actin caps and are characterized by a uniformly structured cortical
F-actin (cite here Winkler 2015) (Fig. 7d). Secondly, we employed *dia*

mutants[17-19]. Dia is a founding member of the formin family, which nucleate
and polymerize linear actin filaments. *dia* mutants lack metaphase furrows but
contain actin caps[17] (Fig. 7d).
296
We applied our quantitative assay to *ELMO* embryos. A strongly increased
nuclear mobility was obvious in time lapse movies (Fig. 7e). Quantification of
nuclear trajectories revealed a maximal nuclear displacement of 60 μm as
compared to 20 μm in wild type embryos (Fig. 7f, g). In addition to the threefold
increased displacement, we observed as a second phenotype that the nuclei
did not return to their initial position in *ELMO* mutants (Fig. 7f, h). The impaired
back movement indicates a loss of the spring-like behavior. Consistently, we
calculated an almost 10-fold reduced spring constant at the turning point of the
nuclear trajectories (Fig. 7i). A similar behavior and profiles were detected in
NC12 of ELMO embryos (Supp. Data Fig. S5).
307
We also detected changes in nuclear movement in *dia* mutants. Similar to
ELMO mutants, we observed a loss of the spring-like back movement. The
nuclei did not return to their initial position and the spring constant was almost
10-fold reduced (Fig. 7e, f, g, h, i). In contrast to *ELMO*, the maximal
displacement was similar to wild type indicating that the stabilizing function of
the cortex does not depend on *dia*. The neighborhood relationships were
largely maintained *dia* and *ELMO* embryos (Fig. 7j). In summary, by employing
two mutants affecting F-actin organization, we identified distinct functions of
the actin cortex. F-actin is required for the back movement as revealed by the
reduced apparent spring constant and the permanent displacement. The
ELMO-dependent organization into caps appears to be important for limiting
nuclear movement.
320
Discussion
The direct interactions between the nuclei and their associated cytoskeleton
are a special feature of syncytial embryos. Due to the lack of separating cell
membranes, microtubule asters originating from the centrosomes associated
with each nucleus form an extended network of hundreds to thousands of
elements. Emergent features arise in this network by summing up the behavior
of individual elements, such as fluctuations or duplication, and their
interactions, such as repulsion. The analysis of the mechanism underlying the
emergent features is essential for understanding how the individual cells
function collectively to form a tissue.
331
We identified an anisotropic flow of the nuclear array as an emergent feature.
Based on a morphodynamical analysis of the nuclear array in wild type and
mutant embryos together with computational simulations, we analyzed the

mechanism of the flow behavior. In this way we identified spindle elongation as
a major driving force for nuclear movement. The emergent nature of the
nuclear flow becomes obvious, since individual behavior is strikingly different
than the collective behavior of the nuclear array. Nuclei divide with an isotropic
orientation, whereas the flow direction is anisotropic. Furthermore the maximal
division distance is about 10 μm, whereas the maximal displacement is about
20 μm.
342
The physical basis for the directionality of the flow is not clear, albeit the
pseudo-synchrony is an essential part of it. With strongly synchronous
divisions, the pushing forces of mitotic spindles would generate a spatially
isotropic force distribution. Consequently, the nuclei would not move due to a
balance in forces. In the case of pseudo-synchronous divisions, the force
balance is broken leading to an imbalance and thus a flow away from the wave
front. The forces are higher at and before the wave front than in the region
after the wave front. The physical nature for what causes the imbalance is
unclear. It is conceivable that the nuclear array is apparently stiffer in
metaphase than in telophase due to stronger interactions. We implemented
this mechanism in our model. Alternatively, friction between blastoderm and
vitelline envelope in metaphase might cause the imbalance. It has been
reported that the mechanical interactions between embryonic tissue and the
vitelline envelope are involved in generating directional flow and tissue
movement[10,20,21]. In the syncytial embryo, although the nuclei moving closer to
the vitelline envelope just after metaphase-anaphase transition, the distance
between the blastoderm and vitelline envelope was not detected. (Supp. Data
Fig. S6).
361
A specific and likely essential feature of syncytial embryos is the dynamical
cytoskeleton. Microtubules change from a strongly asymmetric network with
strong repulsion between separating daughter nuclei and weak neighbor
repulsion to a symmetric network with uniform repulsive interactions. The actin
cytoskeleton transforms from mitotic organization with metaphase furrows to
the cap structure typical for interphase. We have experimentally and by
simulation dissected the contribution by these factors. We identified a
contribution of the actin cortex to the elastic feature of the nuclear movement,
i.e. that nuclei return to their starting position. This is consistent with previous
findings that the elasticity of *Drosophila* embryonic cortex in cellularization
stage depends on the actin cytoskeleton[9,10](Doubrovinski et al., 2017;
D'Angelo et al., 2019). In addition, ELMO and its functionally dependent actin
caps clearly suppress displacement.
375

In order to investigate these molecular features of the nuclear movement,
novel assays for the driving forces and the material properties of the cytoplasm
and especially the cortex are needed[8,22]. In hydrodynamics, any movement in
a viscous medium will be counteracted by friction. Although we have
calculated a phenomenological spring constant describing the elastic
movement, it is clear that a pure spring model is too simple, since it lacks a
loss term accounting for the viscosity of the medium. Future work including
novel assays for the apparent material properties of the embryo will address
these issues and thus allow for a full physical model for the emergence of this
morphologically visible movement.
386

Methods and Materials
***Drosophila* Genetics**
Fly stocks were obtained from the Bloomington Drosophila Stock Center[23,24],
unless otherwise noted. Fly strains used in this study are the followings: w;
Histone2Av-GFP. *w*; sqh-Utr-GFP/CyO; ubi-His2Av-RFP[14]. *Map60^{KG00506}. w*;
ubi-GFP-D-Cad *dia^5* Frt^{2L} ubi-His2Av-RFP/CyO[17]. *w* ; *ELMO^{367}* Frt^{2L}/CyO[11]. *w*
Hira^{ssm}/FM7c, w^a B [25]. His2Av-RFP; Kinesin5-[TEV]-GFP [5]. Fly stocks were
kept at 25°C on a standard cornmeal food. Germline clones of *dia* and *ELMO*
were induced by crossing with corresponding Frt chromosomes and the
following heat shock at 37˚C for one hour on two consecutive days after
hatching. Short spindle induced by TEV injection was described previously[5]. In
addition, we titrated the amount of TEV protease to achieve a partial depletion
allowing mitosis but with shorter spindles during the cleavage cycle.
400

Phalloidin staining and imaging
Wild type embryos and embryos from *dia* and *ELMO* germline clones were
fixed with 8% formaldehyde according to standard procedures. The vitelline
membrane was manually removed. Fixed embryos were incubated with
phalloidin-Alexa 488 (1:500, Thermo Fisher) for 1.5 h. After rinsing three times
and washing three times for 15 min each with PBT (PBS(Phosphate-Buffered
Saline) with 0.1% Tween 20), embryos were stained with DAPI
(4′,6-Diamidine-2′-phenylindole dihydrochloride) (0.2 µg/ml) for 10 min, rinsed
three times in PBT, washed in PBT for 10 min and mounted in
Aqua-Poly/Mount (Polysciences). The images of fixed embryos were acquired
using a Zeiss LSM780 confocal microscope.
412

Microinjection
1–2 h old embryos were collected, dechorionated with 50% bleach solution for
90 s, rinsed thoroughly with deionized water. After aligning on a coverslip, the
embryos were desiccated for 10 min, and covered with halocarbon oil (Voltalef
10S, Lehmann & Voss). TEV protease (a gift from Dirk Görlich) and

Histone1-Alexa-488 protein (2 mg/ml, Thermo Fisher) were injected to the
desired embryos using Microinjector FemtoJet® (Eppendorf) on an inverted
microscope.
421

Live imaging for nuclear dynamics

Nuclear dynamics was recorded by movies of embryos with the fluorescently
labeled nuclei, by expression of Histone2Av-GFP or injection of
Histone1-Alexa-488 protein. Embryos were attached on a coverslip coated
with embryo glue and covered with halocarbon oil. Time-lapse images were
recorded on a spinning disc microscope (Zeiss, 25x/NA0.7 multi immersion)
with an emCCD camera (Photometrics, Evolve 512). To ensure reliable
tracking of the nuclei, the frame rate was 0.5–0.2 Hz with 4 axial sections,
covering 8 µm. Images were merged maximal intensity projections
(Fiji/ImageJ[26]).
432

Images process and quantification

434 Imaging segmentation and analysis were performed with custom-written
435 Python algorithms. The software code is available on request. Briefly, the
436 nuclear positions were detected as blob-like features of size σ_i at position
437 (x_i, y_i) by finding the maxima (x_i, y_i, σ_i) of a rescaled Laplacian of Gaussian
438 (LoG) function

$$L(x, y, \sigma) = \sigma^2 \big(\Delta(g_\sigma * f) \big)(x, y, \sigma),$$

440 where $f_t(x, y)$ is the nuclei gray-scale value at time t, $g_\sigma(x, y)$ is Gaussian
441 kernel of width σ, and "$g * f$" stands for the convolution of function g and f.
442 When multiple blobs were detected in a single nucleus, we deleted a
443 neighboring blob b_2 of b_1 with a heuristic test function T

$$T(b_1, b_2) = \frac{1}{2\big(f_t(b_1) + f_t(b_2)\big)} - \int_r f_t(x) e^{-\left(x - \frac{1}{2}\right)^2} dx,$$

445 where $\gamma : [0, 1] \to \mathbb{R}^2$ is the straight line from b_1 of b_2.
446

447 We tracked the nuclei across frames based on a proximity criterion. The
448 distance between nucleus k in frame i and l in frame $i + 1$ was defined as

$$d_{k,l} = \| x_{k,i} - x_{l,i+1} \|_2.$$

We determined the interval of mitosis time using the k-means-clustering
algorithm on the observed nucleus positions at time t. If a new blob was
detected, we considered this nucleus and its nearest neighbor were daughter
nuclei from a recent mitosis, and set their internal nucleus clock to 0.
Calculations of nuclear displacement, speed, nuclear density, spindle length
and orientation were done for each nucleus in its own eigentime after mitosis.
456

Quantification of F-actin over cell cycle

458 Embryos expressing Histone2Av-RFP; Utrophin-GFP were imaged with a
459 Zeiss LSM780 confocal microscope (25x/NA0.7 multi immersion). The frame
460 rate was 0.1 Hz, and 10 µm was covered in z direction. Utrophin-GFP stacks
461 were merged by average intensity projection (Fiji/ImageJ). F-actin was
462 quantified manually with Fiji/ImageJ.
463
2D simulation of synchronous mitosis
In the simulation, the nuclei are randomly placed in a 50um*50um square via
Poisson-disc sampling, which produces random tightly-packed locations with
pair-wise distances not smaller than a specified value d_{disc}>4um. We assume
the nuclei divide simultaneously and form mitotic spindles with isotropic
orientations. As the spindles extend with a constant speed, we check at each
time step if any two of the spindles touch each other by scanning a restricted
area of 4um*4um in the vicinity of each spindle (see supplementary video). If a
spindle touches at least one other, we assume it stops extending and reaches
its maximal length due to limited space. When all spindles reach their
respective maximal lengths, the simulation is ended and we compute the
average maximal length l_{max} over all spindles in the simulation. For each fixed
d_{disc}, we run the simulation 50 times, producing 50 l_{max} values for various
nuclear density around $1/(4d_{disc}^2)$. The mean of the 50 l_{max} values and the
mean of the 50 nuclear densities provide the coordinates of one point in Fig.1C.
The x- and y- error bars indicate the respective standard deviations. Varying
the minimum distance d_{disc} between nuclei, we obtain the mean l_{max} values for
a range of nuclear densities. The data from simulation are fitted to a power-law
function (solid curve in Fig.1C) with the method of least squares.
483
Computational modeling of the nuclear movement
We base our model on a previously successful model for static nuclei packing

during interphase[4]: Nuclei, positioned at $\vec{r}_i$, move due to active forces,

$\vec{F}_{act,ij}$, exerted by motor-activated pushing apart of neighbouring overlapping

microtubule asters and due to passive repulsive forces between neighbouring

nuclei, $\vec{F}_{pass,ij}$, arising from the visco-elastic matrix embedding nuclei, mainly

build by actin cytoskeletal elements. The overdamped equation of motion is

given by $r_i = \frac{1}{\eta} \sum_{j \neq i} \left(\vec{F}_{act,ij} + \vec{F}_{pass,ij} \right)$, where η denotes the viscosity of the

matrix. Aiming to describe the motion of nuclei during mitosis we adjust force
amplitudes to change as microtubuli and actin cortex of nuclei considered

remodels over time, $\vec{F}_{pass,ij} = -A_{pass}(t_i)A_{pass}(t_j)\frac{\vec{e}_{r_{i,j}}}{r_{i,j}^4}$, $\vec{F}_{act,ij} =$

$-A_{act}(t_i)A_{act}(t_j)\dfrac{\vec{e}_{r_{i,j}}}{r_{i,j}^4}$, where $\vec{e}_{r_{i,j}}$ and $r_{i,j}$ denote the unit vector and the

distance between nuclei i,j considered. Individual nuclei times t_i are shifted
with respect to nuclei division at $t_{\mathrm{div}} = 0$. To capture the dynamics of
cytoskeletal elements during mitosis we subdivided the time course of events
into the series: $t_{\mathrm{spindle\ ass}} < t_{\mathrm{spindle\ const}} < t_{\mathrm{div}} < t_{\mathrm{div\ max}} < t_{\mathrm{sp\ diss}} < t_{\mathrm{MT\ ass}} <$
$t_{\mathrm{actin\ ass}} < t_{\mathrm{MT\ inter}} < t_{\mathrm{actin\ inter}}$. Passive forces change only between $t_{\mathrm{spindle\ ass}} <$
$t_{\mathrm{spindle\ const}}$ when actin caps shrink while spindles assemble to generate
balancing forces and during regrowth of actin caps between $t_{\mathrm{actin\ ass}} <$
$t_{\mathrm{actin\ inter}}$ before entering interphase. Active forces due to spindle formation as
well as microtubule asters are in contrast much more dynamic. Between
$t_{\mathrm{spindle\ ass}} < t_{\mathrm{spindle\ const}}$ spindles assemble. Upon division $t_{\mathrm{div}} < t_{\mathrm{spindle\ diss}}$
spindles move daughter nuclei apart, active force between only the division
partners is now increased by an additional time-dependent factor A_{div} that
reaches a value of up to 3. Afterwards, forces between paired daughter nuclei
reduce linearly to regular levels. Meanwhile, for all other nuclei, after division
the active force is halved due to distribution of centrosomes on two nuclei. This
is balanced by the effective increase of passive forces as nuclei are closer
packed due to division while the passive force amplitude stays constant.
Between $t_{\mathrm{spindle\ diss}} < t_{\mathrm{MT\ ass}}$ spindles disassemble before the microtubule
asters regrow during $t_{\mathrm{MT\ ass}} < t_{\mathrm{MT\ inter}}$. All dynamics are interpolated linearly.
In detail:

$A_{\mathrm{pass}}(t) =$

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$$A_{\mathrm{pass}}(t) = \begin{cases} h_{\mathrm{inter}} & t \le t_{\mathrm{spindle\ ass}} \\[2mm] h_{\mathrm{inter}} + (h_{\mathrm{mitosis}} - h_{\mathrm{inter}})\dfrac{t - t_{\mathrm{spindle\ ass}}}{t_{\mathrm{spindle\ const}} - t_{\mathrm{spindle\ ass}}} & t_{\mathrm{spindle\ ass}} \le t \le t_{\mathrm{spindle\ const}} \\[2mm] h_{\mathrm{mitosis}} & t_{\mathrm{spindle\ const}} \le t \le t_{\mathrm{actin\ ass}} \\[2mm] h_{\mathrm{mitosis}} + (h_{\mathrm{inter}} - h_{\mathrm{mitosis}})\dfrac{t - t_{\mathrm{actin\ ass}}}{t_{\mathrm{actin\ inter}} - t_{\mathrm{actin\ ass}}} & t_{\mathrm{actin\ ass}} \le t \le t_{\mathrm{actin\ inter}} \\[2mm] h_{\mathrm{inter}} & t_{\mathrm{actin\ inter}} \le t \end{cases} ,$$

520    $A_{\mathrm{act}}(t) =$

521
$$A_{\mathrm{act}}(t) = \begin{cases} h_{\mathrm{MT}} & t \le t_{\mathrm{spindle\ ass}} \\[2mm] h_{\mathrm{MT}} + (h_{\mathrm{sp}} - h_{\mathrm{MT}})\dfrac{t - t_{\mathrm{spindle\ ass}}}{t_{\mathrm{spindle\ const}} - t_{\mathrm{spindle\ ass}}} & t_{\mathrm{spindle\ ass}} \le t \le t_{\mathrm{spindle\ const}} \\[2mm] h_{\mathrm{spindle}} & t_{\mathrm{spindle\ const}} \le t \le t_{\mathrm{div}} \\[2mm] \frac{1}{2}h_{\mathrm{spindle}} & t_{\mathrm{div}} \le t \le t_{\mathrm{spindle\ diss}} \\[2mm] \frac{1}{2}h_{\mathrm{spindle}} + \frac{1}{2}(h_{\mathrm{spindle\ diss}} - h_{\mathrm{spindle}})\dfrac{t - t_{\mathrm{spindle\ diss}}}{t_{\mathrm{MT\ ass}} - t_{\mathrm{spindle\ diss}}} & t_{\mathrm{spindle\ diss}} \le t \le t_{\mathrm{MT\ ass}} \\[2mm] \frac{1}{2}h_{\mathrm{spindle\ diss}} + \frac{1}{2}(h_{\mathrm{MT}} - h_{\mathrm{spindle\ diss}})\dfrac{t - t_{\mathrm{MT\ ass}}}{t_{\mathrm{MT\ inter}} - t_{\mathrm{MT\ ass}}} & t_{\mathrm{MT\ ass}} \le t \le t_{\mathrm{MT\ inter}} \\[2mm] \frac{1}{2}h_{\mathrm{MT}} & t_{\mathrm{MT\ inter}} \le t \end{cases} ,$$

$$A_{\text{div}}(t) = \begin{cases} h_{\text{div}}\dfrac{t - t_{\text{div}}}{t_{\text{spindle diss}}/2 - t_{\text{div}}} & t_{\text{div}} \leq t \leq t_{\text{spindle diss}}/2 \\ h_{\text{div}} & t_{\text{spindle diss}}/2 \leq t \leq t_{\text{spindle diss}} \\ h_{\text{div}} - (h_{\text{div}} - 1)\dfrac{t - t_{\text{spindle diss}}}{t_{\text{MT ass}} - t_{\text{spindle diss}}} & t_{\text{spindle diss}} \leq t \leq t_{\text{MT ass}} \\ 1 & t_{\text{MT ass}} \leq t \end{cases}$$

Note that changes in both passive and active forces only get out of balance
during spindle disassembly initiating nuclei motion with significant time delay
relative to the time point of nuclei division. At that point in time nuclei that have
not divided yet have a stronger repulsive force than the already divided nuclei
due both actin caps and microtubule asters not yet being fully formed.
Therefore, nuclei move toward the region of higher nuclei density, only
returning back when actin caps and microtubule asters are forming again.

Nuclei dynamics are evolved on a sphere to capture the topology of the
embryo. Division wave is initiated on one pole and propagates with velocity v
toward the opposing pole. For numerical stability we place two daughter nuclei
upon division a short distance r at a random angle apart, their center of
mass coincides with the position of their mothers.

Spring constant fitting
The data sets consisted of 1–5 nuclear displacement curves for 2–4 embryos
of each type (*dia*, *ELMO*, *Kinesin5* and *Map60* mutants, wild type).
The nuclear displacement curves (in the first phase) are similar to the
oscillation of a not-actively driven and non-damped harmonic oscillator.
Therefore, the individual nuclear displacement curves were fitted to a sine
curve of the form $y(t) = A\sin(\omega t + \varphi)$,
where *A* is the amplitude, ω the angular frequency and φ the phase shift, using
a self-written script in Python. The biological rational behind this approach is
that the nuclei behave like they were linked to an elastic spring, which could be
e.g. linkages to the cytoskeleton. At t=0 the spring is stretched and the nuclei
start to move until the spring is compressed and the nuclei move back.

The fit region was determined as follows. For all curves, the lower bound on
the fitting range was set equal to the point in time where the nuclear
displacement first exceeds 5 µm, as some curves show a small, reversible
displacement in the beginning. The upper bound was chosen independently
for each of the data sets since the elastic part of the curve depends on the
stiffness and dampening of the spring and hence differs across data sets. For
the *dia* and *Map60* mutants as well as the wild type, the upper bound was set

equal to 100 s after the turning point, while it was set to 180 s after for the *ELMO* mutant and 240 s for the Kinesin5 mutants. The results of the fit parameter ω were averaged for each embryo to give a set of angular frequencies ω_i for each type, where i runs over the number of embryos. The spring constant was derived from the average ω_i *via* the relation $k = m\,(\omega_i)^2$, in which m denotes the mass of the nucleus. It was assumed that the nuclei are spherical with a diameter of 4.9 µm and a density equal to that of water at room temperature. Error bars, which correspond to one standard deviation, were calculated in the frequency domain and then converted to the force domain by the analogue of the relation above.

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Author contributions

ZL conducted the experiments. ZL, JR, HP, SK analyzed the data. SM, XZ, KA conducted the simulations. JG and ZL conceived and JG, TA, SG, KA supervised the study. JG, ZL wrote the manuscript.

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Figure 1. Asynchronous nuclear division is required for long mitotic spindles.
a, Live image of an embryo during mitosis. The left half is in metaphase, the right half in anaphase. The dotted line in red indicates metaphase-anaphase transition sweeping over the embryo from right to left as a wave front. **b,** Embryo to embryo variation of the speed of the wave front (n=50 embryos). **c**, The protected area between daughter nuclei containing the spindle is indicated by an overlaid colored area. **d**, Illustration of the simulation. Daughter nuclei (arrow heads) are symmetrically pushed apart until they reach a neighboring arrow (red dot). Mother nucleus (green). **e**, Observed spindle lengths/distances between daughter nuclei are plotted against the corresponding nuclear density. Data from simulation (blue) and measurements in embryos in NC11, NC12, NC13 and NC14 in haploids (orange) (n=15 spindles in each embryo and 3 embryos for each type). Data are mean±s.e.m. Scale bar: 10 μm.

Figure 2. Quantitative assay for nuclear movement

a, Live images with nuclear labelling. Dotted line indicates the wave front of the metaphase-anaphase transition. Arrows in yellow indicate nuclear movement. **b**, Time course of nuclear displacement with the position if the mother nucleus during metaphase-anaphase transition as a reference (t=0). (n=260 nuclei in one embryo). **c**, Time course of nuclear speeds. Labels 1, 2 and 3 which represent the 3 different movements as shown in **d**. (n=260 nuclei in one embryo). **d**, Live image with backward trajectories of two daughter nuclei. Schematic drawing of (1) chromosome segregation, (2) forth movement away and (3) back movement toward the mitotic wave front. **e**, Image series with Voronoi maps with the mitotic wave front in images at 35 s and 55 s. Color code indicates nuclear density. **f**, Time course of nuclear density with metaphase-anaphase transition at t=0. Numbers indicate the three stages of nuclear movement. (n=260 nuclei in one embryo). **g**, Embryo to embryo variation of the low point in density relative to the double density. (n=12 embryos). **h**, Illustration of the collective nuclear movements leading to a stretching and relaxation of the nuclear array, which thus resembles an elastic sheet. **i**, A simple square function (red) was fitted to the forth and back movement around the maximal displacement. According to Hook's law an apparent spring constant was calculated (n=15 nuclei from 3 embryos). The statement data are representative of more embryos. Data are mean±s.e.m. Scale bar: 10 μm.

Figure 3. Emergence of collective nuclear movement

a, Schematic drawing of an embryo with definition of angles. **b**, Image from live imaging after mitosis. Orientations of the corresponding spindle at t=0 s and the directions of nuclear movement at t = 60 s are indicated by a magenta bar and green arrow, respectively. **c**, Distribution of observed angles for spindle orientation at t=0 s and nuclear movement at t=60 s. (n=20 embryos including 6230 nuclei). **d**, Image series with previous trajectories showing cases of perpendicular and parallel mitosis. **e**, Images from live imaging. Groups of nuclei were labelled at metaphase. Corresponding nuclei were labeled in same color in later images of the movie. Data are mean±s.e.m. Scale bar: 10 µm.

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Figure 4. Numerical simulation of nuclear movement
a, Scheme of division, active and passive forces in syncytial embryo. **b**, Time course of the division, active force and passive force used in the simulation. **c**, Snap shots from the simulation. Nuclei were projections. Color code indicates speed of nuclear movement. **d**, Time course of nuclear displacement (n=300 nuclei). Data are mean±s.e.m.

Figure 5. Comparison of data from simulation and experiment.
a, **c**, Time course of nuclear displacement (blue) and distance between corresponding daughter nuclei (orange). The time lag (t) between maxima is indicated. **b**, **d**, Distribution of the time lag (t). Data from simulation (**a**, **b**) and experiment (**c**, **d**). (n=300 nuclei in one embryo in a; n=21 embryos in b. n=286 nuclei in one embryo in c; n=21 embryos in **d**.) **e**, **f**, Maximal displacement plotted against the corresponding speed of the mitotic wave. Data from simulation (**e**) and experiment (**f**). (n=50 embryos in **f**.) Data are mean±s.e.m.

Figure 6. The ensemble of spindle elongation indirectly drives the nuclear movement. a, Spindle length/distance between respective daughter nuclei in embryos partially depleted of Kinesin-5 and *Map60* mutants. (n=30 spindle in 3 embryos for each genotype). **b**, images from live image. The trajectories of two nuclei over 300 s were plotted into the last images. **c**, **d**, Quantification of nuclear trajectories for indicated genotypes. **c**, Time course of nuclear displacement. **d**, Maximal displacement. **e**, **f**, Maximal displacement was plotted against corresponding division distance. Data from simulation (**e**) and experiment (**f**). The Data are mean±s.e.m. Scale bar: 10 μm.

Figure 7. Role of the actin cortex

a, Scheme of cortical actin dynamics during nuclear division cycles. **b**, Live-images showing F-actin organization during nuclear cycle. **c**, Quantification of F-actin. (n=10 regions in 3 independent recordings). **d**, Fixed *dia* and *ELMO* mutants stained for F-actin (red) and DNA (blue). **e**, Images from movies of *dia* and *ELMO* mutants. Nuclear trajectories over 10 min are plotted into the last images. **f**–**g,** Quantification of nuclear trajectories in *dia* and *ELMO* mutants. **f**, Time course of displacement, **g**, Maximal displacement, **h**, Final displacement (at t=600 s in wild type and *dia* mutant, 1200 s in *ELMO* mutant). **i**, Apparent spring constant. **j**, Neighborhood relationship. Images from movies at indicated time. Groups of cells have been marked in color at metaphase. Their daughter nuclei were labelled with the same color in the following images. n=15 nuclei in 3 embryos for dia and *ELMO* mutants, respectively (**f**, **g**, **h**, **i**). Data are plotted as mean±s.e.m. Scale bar: 10 μm.

Figure S1. Nuclear densities in different cycles. a, images of Drosophila syncytial embryo expressing Histone2Av-GFP in different cycles. **b**, quantification of nuclear density in the indicated cycles. n=10 embryos. Data are mean±s.e.m.

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Figure S2. Image analysis pipeline and the quantification of nuclear dynamics. a, The live images of the embryos with labelled nuclei were taken with a frame rate of 0.2 Hz. Nuclei were detected and tracked using custom-written Python algorithms. **b**, Time course of nuclear displacement, with colour-coding for individual nuclei (n=10 nuclei). **c**, Time course of nuclear flow speed, with colour-coding for individual embryos (n=10 embryos). **d**, The distribution of angles of spindle and nuclear flow, with colour-coding for individual embryos (n=20 embryos). n>50 nuclei in each embryo in figure **c** and **d**.

Figure S3. Nuclear displacement and flow speeds are less pronounced in earlier cycles. a, The time course of nuclear displacement in NC11, 12 and 13 in one embryo (n=58, 107 and 206 nuclei in NC11, 12 and 13, respectively). **b**, Maximal displacement distribution in NC11, 12 and 13 from **a. c**, Time course of nuclear flow speed from the same embryo as shown in a, with colour-coding for indicated nuclear cycles. **d**, The percentage of embryos showing the nuclear flow in different cycles (n=6, 18, 26 embryos in NC11, 12 and 13, respectively). Data are mean±s.e.m.

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Figure S4. Numerical simulation. a, The time dependence of amplitude of active force, passive force and division force. **b**, Increasing in spindle strength ($h_{spindle}$) leads to increasing of maximal displacement and division distance. Data are mean±s.e.m.

Figure S5. Nuclear displacement is more prominent in *ELMO* mutant embryos in NC12. a, Images from movies of wild type and *ELMO* mutants in NC12. Nuclear trajectories are plotted into the first images. **b**, The time course of nuclear displacement in NC12. (n=130 nuclei in *ELMO* and 290 nuclei in wild type. The statement data are from one embryo, but representative of more embryos). Data are mean±s.e.m. Scale bar: 10 μm.

Figure S6.   The nuclei move closer to the vitelline envelope (VE) just after metaphase-anaphase transition, but the distance between blastoderm and VE is constant over cleavage cycle. Sagittal image series of syncytial embryo expressing Histone2Av-RFP and Utrophin-GFP. The vitelline envelope was visible due to autofluorescence, shown in the first image, and indicated using arrowhead. The vitelline envolope is marked by white dashline in the following image series. Scale bar: 10 µm.

Movie list:

Movie 1. Mitotic wave sweeps over the embryo.

Movie 2. Nuclei undergo stereotypical movement after metaphase-anaphase transition. Scale bar: 10 µm.

Movie 3. The time course of the nuclear Voronoi map over nuclear division. Scale bar: 10 µm.

Movie 4. Computational simulation.

Movie 5. The nuclear displacement in wild type, dia and ELMO mutant embryos. Scale bar: 20 µm.