Influence of genetic interactions on polygenic prediction

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9 Abstract

Prediction of phenotypes from genotypes is an important objective to fulfill the promises of 10 genomics, precision medicine and agriculture. Although it's now possible to account for the 11 majority of genetic variation through model fitting, prediction of phenotypes remains a 12 13 challenge, especially across populations that have diverged in the past. In this study, we designed simulation experiments to specifically investigate the role of genetic interactions in 14 15 failure of polygenic prediction. We found that non-additive genetic interactions can 16 significantly reduce the accuracy of polygenic prediction. Our study demonstrated the importance of considering genetic interactions in genetic prediction. 17

18 Introduction

The problem of "missing heritability" has attracted much attention and controversy in 19 quantitative genetics (Manolio et al., 2009), yet its definition remains ambiguous in the 20 literature. A widely used definition is that genetic associations identified in large-scale 21 22 genome-wide association studies (GWAS) cannot fully account for heritability estimates (e.g. from twin studies) in the sense that the model fitting can only capture a fraction of the total 23 24 variance. As sample sizes for GWAS increase from thousands to hundreds of thousands, and 25 advanced statistical methods are developed to fit all DNA variants in the model simultaneously, including those not significantly associated with the trait, the variance that 26 can be explained by DNA variants also increase. For example, adult human height is a 27 classical quantitative trait with a narrow sense heritability (h^2) of approximately 0.8 based on 28 twin studies (Silventoinen et al., 2003). However, early GWAS studies identified common 29 variants explaining only a total of 2-4% phenotypic variance (Gudbjartsson et al., 2008; 30 Lettre et al., 2008; Weedon et al., 2008) with sample sizes in the order of 20,000. In 2010, a 31 landmark study increased this proportion to about 45% by fitting ~300,000 SNP markers in 32 the model for ~4,000 individuals with the covariance among individuals determined by 33 genome-wide SNP similarity (Yang et al., 2010). Importantly, applying the same idea, the 34 most recent study using whole genome sequences of ~20,000 individuals in the TOPMed 35 almost entirely closed the gap between the genomic heritability and the presumed 36 heritability (Wainschtein et al., 2019). The progress has been remarkable and it can be 37 cautiously expected that the combination of large sample size and full genome sequences 38 may finally capture all heritability. Perhaps more importantly, it also suggests that the failure 39 to explain all heritability in early GWAS was due largely to low statistical power and 40 incomplete variant coverage thus those with smaller effects, lower minor allele frequencies, 41 and non-SNP variants were missed from the model fitting. 42

A second, more implicit but more practical definition of missing heritability, is that the 43 prediction accuracy of quantitative phenotypes based on genotypes (polygenic scores) is far 44 less than the heritability of the trait. A perfect genetic model with precise effects and model 45 46 specification should be able to predict unobserved phenotypes with an accuracy (measured by r^2) equal to the heritability. But that's not always the case. For example, a large GWAS on 47 adult human height with almost 200,000 individuals identified over 180 loci, capturing only 48 \sim 10% of the phenotypic variation (Lango Allen et al., 2010). This proportion of variance was 49 measured based on "leave-one-out" out-of-sample prediction (International Schizophrenia 50 Consortium et al., 2009), i.e., the effects of the genetic loci were estimated in one subset of 51 the sample and polygenic scores (genetic effects summed over all significant loci) was 52 computed to predict phenotypes in another subset. The partition between the subsets 53 54 conveniently followed sample origin from different European countries (Lango Allen et al., 2010). In contrast to the mixed model genomic heritability approach, this method of 55 estimating explained heritability was more akin to genomic prediction widely used in animal 56 and plant breeding (Meuwissen et al., 2001; VanRaden, 2008), in which effects of genetic 57

58 markers across the whole genome, regardless of their statistical significance, are summed to 59 compute genetic prediction.

Both the genomic heritability and the prediction accuracy of polygenic scores (or polygenic 60 breeding values) take the form of variance proportion, but have vastly different properties. 61 One of the most contrasting differences is that prediction accuracy can be small even when 62 the genomic heritability is large (Makowsky et al., 2011). Our discussion on the two 63 definitions of missing heritability above is a clear example of this distinction. The 64 implications of this distinction are profound. Most notably, even if there was no missing 65 heritability based on genomic heritability, the utility of polygenic score would be very limited 66 if prediction accuracy is low. 67

Recently, there has been renewed interest in the application of polygenic score 68 69 (International Schizophrenia Consortium et al., 2009) with the advent of large public data sets such as the UK biobank (e.g. Khera et al., 2018). In particular, many studies have 70 observed poor prediction by polygenic scores across different ancestry groups (Martin et al., 71 2019) or even within an ancestry group but with variable characteristics (Mostafavi et al., 72 2019). In fact, earlier studies with smaller sample sizes observed similar patterns, but were 73 interpreted as missing heritability (Lango Allen et al., 2010; Makowsky et al., 2011). In animal 74 breeding, similar observations have also been made. Although genomic prediction works 75 exceedingly well within a breed, cross-breed prediction generally fails (Hayes et al., 2009). 76 The explanation is obvious, genetic effects are context dependent and heterogeneous 77 between groups. Variable linkage disequilibrium (LD) patterns, environments, and other 78 factors can all contribute to the variable genetic effects, manifesting as variable accuracy of 79 polygenic prediction. 80

Genetic interactions are pervasive, and an important type of context dependent effects 81 (Mackay, 2014; Mackay and Moore, 2014). It has been previously shown that the presence of 82 genetic interactions does not have a strong effect on genomic heritability (Hill et al., 2008; 83 Huang and Mackay, 2016), therefore the magnitude of genomic heritability offers no 84 85 indication of the genetic architecture. However, genetic interactions may influence genomic prediction accuracy and models taking into account the complexity improves prediction 86 (Morgante et al., 2018). This clearly suggests that the simplification of genetic architecture to 87 the additive infinitesimal model when the true model is not, although convenient and no 88 comparable alternatives exist, can be risky. In this study, we specifically investigate the 89 90 influence of genetic interactions on prediction of polygenic scores, with an emphasis on polygenic prediction across diverged populations. 91

92 Results

93 Experimental design

Because it's not yet possible to unambiguously know the true genetic architecture of a quantitative trait, all experiments in this study were performed using simulated data instead of real data. This allows us to specifically ask simple questions while eliminating influence from other factors. We simulated a sample of 75,000 diploid individuals from three ancestry groups, where population A and B diverged 1,000 generations ago and their ancestors diverged from population C an additional 1,000 generations ago (Figure 1a). This specification is qualitatively similar to the global human population history where the ancestral population that went out of Africa were further split into multiple populations.

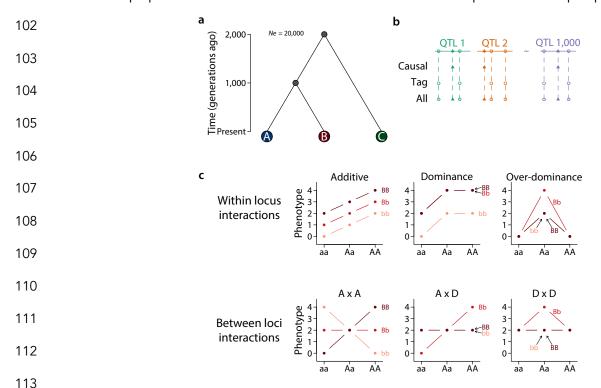


Figure 1. Simulation of genome sequences, population structure, and genetic architecture. (a) Three populations (A, B, C) were simulated with an effective population size of 20,000 each. A and B diverged 1,000 generations before present and A and C diverged 2,000 generations ago. (b) 1,000 independently inherited chromosomes were simulated, each containing one QTL. Three sets of variants were considered, including "causal", "tag", and "all" as illustrated. (c) Six different genetic architecture were simulated, each illustrated by one of the panels.

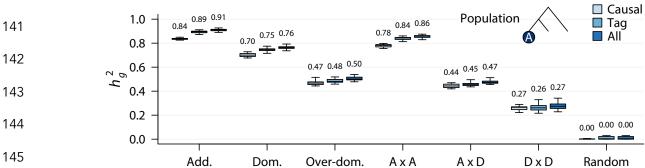
We considered three possible variant sets (Figure 1b), 1) causal: all and only causal variants; 118 2) tag: all variants except causal variants; and 3) all: all variants including causal variants. 119 These represent three simplified scenarios 1) a best case scenario where causal variants have 120 been identified, 2) a realistic scenario where causal variants are tagged by genotyped 121 variants, and 3) an achievable scenario in the near future with whole genome sequences. We 122 did not consider variants that were rare (MAF < 0.01) in all three populations as they led to 123 gross overestimation of genomic heritability approaching one, similar to findings in a 124 simulation study using real genotypes (Evans et al., 2018). The three variant sets were used 125 to compute genomic heritability and perform polygenic prediction. When performing 126 polygenic prediction, we did not select variants based on association tests. This choice was 127

based on the consideration that selection of markers introduced another variable in the experiment to complicate the design and interpretation. Instead, we draw from the distinction between causal and all variants to represent the extreme scenarios where a perfect selection or no selection was performed.

We simulated a quantitative trait controlled by 1,000 independently inherited QTLs (Figure 1b) of broad sense heritability $H^2 = 0.8$ but different types of genetic architecture. When the genetic architecture is strictly additive, the narrow sense heritability $h^2 = H^2 = 0.8$, whereas in other cases $h^2 < 0.8$. Six simple models of genetic architecture were simulated, including additive, dominance, over-dominance, and pairwise additive by additive (A x A), additive by dominance (A x D), and dominance by dominance (D x D) (Figure 1c). No higher order interaction was simulated and effects across loci or across pairs were additive.

139 Genomic heritability misses little heritability

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146Figure 2. Genomic heritability in the simulated populations. Box plot (median
indicated on top) showing the genomic heritability (h_g^2) estimated using GREML
under different genetic architecture, where Add. = additive, Dom. = dominance,
Over-dom. = over-dominance, A x A = additive by additive, A x D = additive by
dominance, D x D = dominance by dominance, and random is a non-genetic model
where the phenotypic variation was entirely due to random environmental variation.
The population in which the genomic heritability was estimated was indicated in the
top right corner. Genomic heritabilities in all populations were given in Figure S1.

151 We first recapitulated a result that has been consistently shown (Hill et al., 2008; Huang and Mackay, 2016). We fitted a linear mixed model in each of the three populations or combined 152 samples using GREML implemented in the GCTA (Yang et al., 2011) using 20,000 153 individuals. We found that h_{q^2} were uniformly high when the genetic architecture was 154 additive, dominance, or additive by additive, accounting for nearly all heritability (Figure 2, 155 Figure S1). Whether or not the variant sets included casual variants appeared to have little 156 effects on h_{q}^{2} ; variant sets excluding causal variants performed as well as causal variants only 157 and there was a slight tendency of upward bias (Figure 2). Similar results were obtained 158 159 regardless of whether the samples were from a homogeneous population or a mixture of samples from two diverged populations (Figure S1). When the genetic architecture was 160 entirely overdominance, additive by dominance, or dominance by dominance, h_q^2 was lower, 161

but still consistently explained > 50% of the heritability (Figure 2, Figure S1). Taken together, these results suggest that as long as a large number of genome-wide markers were fitted, little heritability was missed, regardless of the genetic architecture. In other words, the magnitude of genomic heritability offers no discrimination of the underlying genetic architecture (Huang and Mackay, 2016).

167 Accuracy of polygenic prediction with an additive genetic architecture

We then asked a simple question. If genome-wide variants are able to capture the majority of heritability, are they able to predict phenotypes accurately? This question directly addresses the distinction between the two definitions of missing heritability as we outlined in the introduction. If there is no missing heritability based on mixed model fitting, is there missing heritability in polygenic prediction? Many illuminating results could be obtained by comparing different scenarios of simulations (Figure S2).

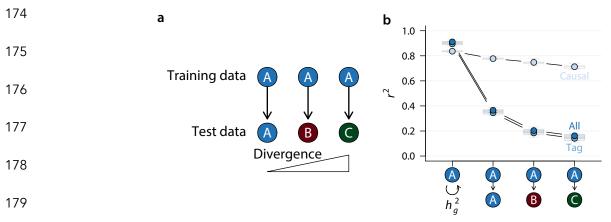


Figure 3. Polygenic prediction under additive genetic architecture. (a) Polygenic prediction was performed according to the diagram, where the model was trained in population A and tested in populations A, B, and C at increasing divergence. (b) Prediction accuracy was plotted according to the training – test population relationships. For comparison, genomic heritability was also plotted along side. Only the additive genetic architecture was considered in this plot.

We first considered the simplest and best scenario, in which the genetic architecture was 183 fully additive, and all causal and only causal variants were known. In this case, the statistical 184 model took the form of the true model and only model parameters needed to be estimated. 185 We trained the model in one population (n = 20,000, training population) and computed 186 polygenic scores of new individuals (n = 5,000, test population) either in the same 187 population or a different population. To test the performance of cross-population prediction, 188 we considered three possible relationships between the training and test populations, 189 representing a gradient of divergence between training and test data (Figure 3a). 190

As expected, the accuracy of polygenic prediction was very high in this best case scenario, approaching the true heritability ('causal' in Figure 3b). There was a small decline in accuracy when cross-population prediction was performed and the degree of population divergence

negatively affected prediction accuracy. However, when non-causal variants were included 194 to make predictions, accuracy plummeted from ~0.8 to ~0.4 (Figure 3b) even when training 195 and test samples were from the same population. This was likely due to the inclusion of 196 independent predictors whose number vastly exceeded that of the causal variants. As 197 populations become more divergent, prediction accuracy further dropped, the rate of which 198 was much more pronounced when tag or all variants were used. These results (in the cases 199 of tag or all variant sets) largely agreed with the large body of empirical work that accuracy 200 of polygenic prediction was substantially lower than genomic heritability and cross-201 population prediction was poor (Lango Allen et al., 2010; Makowsky et al., 2011; Martin et 202 al., 2019). 203

One important lesson could be learned in this simple experiment. The facts that simply adding non-causal variants to the model drastically reduced prediction accuracy, and that the rate of decay in the accuracy of cross-population prediction was much greater in the presence of non-causal variants indicated that the agreement between model and true genetic architecture mattered. This is in sharp contrast to genomic heritability estimation, where including more variants generally improves model fit (compare (Yang et al., 2010) with (Wainschtein et al., 2019)).

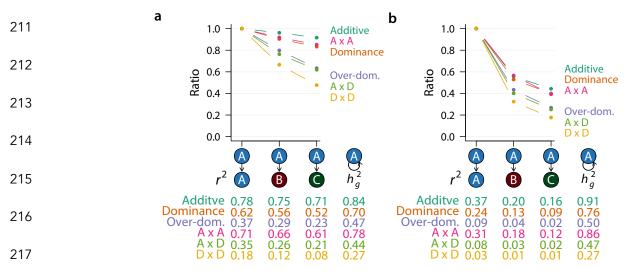


Figure 4. Polygenic prediction with different genetic architecture. (a) Polygenic prediction was performed using causal variants only for six different genetic architecture. The median prediction accuracy (r^2) across 20 replicates in each scenario was listed below the graph, as well as genomic heritability (h_g^2) . Each point on the graph represents a normalized median r^2 , dividing each prediction accuracy by its counterpart in the within population (A -> A) prediction. (b) Polygenic prediction with all variants. Data are presented the same way as in (a). Data in these graphs were summarized from Figure S2.

Accuracy of polygenic prediction in the presence of genetic interactions

We then tested the influence of genetic interactions on the accuracy of polygenic prediction, which fits an additive model. In a favorable condition when all causal variants were known

(but not their effects or interactions) and prediction was performed within the same 225 homogenous population, polygenic prediction accuracy was highly dependent on the 226 genetic architecture (A -> A in Figure 4a). In general, prediction accuracy was higher for 227 genetic architecture with higher h_a^2 , such as additive, dominance, and additive by additive. 228 In contrast, under overdominance, additive by dominance, and dominance by dominance 229 genetic architecture, polygenic prediction performed substantially worse (A -> A in Figure 230 4a). When all variants were used, including non-causal ones, the prediction accuracies 231 decreased dramatically and their dependency on genetic architecture appeared to be 232 stronger (A -> A in Figure 4b). 233

We then asked how genetic interactions influence the rate of decay in prediction accuracies 234 when the training and test populations diverge. We set the accuracy of within-population 235 prediction as the baseline and compared cross-population prediction accuracies to this 236 baseline. When all variants were used for polygenic prediction, the accuracy of cross-237 population prediction dropped to about 40-60% of the accuracy of within-population 238 239 prediction, depending on genetic architecture (Figure 4b). Additive, additive by additive, and dominance genetic architecture, those with the highest h_q^2 and r^2 retained the most 240 prediction accuracy while over-dominance, additive by dominance, and dominance by 241 dominance lost the most (Figure 4b). The more diverged the populations were, the more 242 predictive ability of polygenic scores was lost (Figure 4b). 243

There are many reasons why polygenic prediction failed when test population diverged from 244 training population. In our simple simulation setting, genetic effects were the same across 245 populations and were not sensitive to any non-genetic factors. The difference in the linkage 246 disequilibrium structure between populations may in part explain the drop. Importantly, 247 simulations allowed us to directly use causal variants for prediction, thus eliminating the 248 influence of LD (Figure 4a). Remarkably, while the accuracy of cross-population prediction 249 250 was lower for all genetic architecture, the rate of decay was much greater when the genetic architecture was over-dominance, additive by dominance, or dominance by dominance 251 252 (Figure 4a, compare slopes of the different lines). These results clearly suggest that genetic interactions can not only cause cross-population polygenic prediction to fail, but also in a 253 more severe manner compared to an additive genetic architecture. 254

255 Discussion

We demonstrate in this study through simulations that genetic interactions can influence the accuracy of polygenic prediction. In particular, cross-population polygenic prediction performed worse than intra-population prediction in all cases. For traits controlled by genetic interactions, the cross-population decay in prediction accuracy was far greater. The results make intuitive sense. For a statistical model to predict new data accurately, two conditions must be met. First, the model specification must be correct or at least sufficiently accurate to capture variation in the data. Second, parameters in the model must be precise.

When genetic interactions are present, the additive polygenic model clearly is not accurate. 263

Previous studies have mostly focused on improving parameter estimation, through 264 increasing sample size and methodological improvement. For example, increasing sample 265 size substantially increased accuracy of polygenic prediction of height within individuals of 266 European ancestry (Lello et al., 2018). Inclusion of samples of different backgrounds in the 267 training data also helped (Martin et al., 2019, Figure S2). 268

However, the complexity of the genetic architecture of a quantitative trait makes it nearly 269 impossible to specify a model prior to modeling. As a consequence, the polygenic 270 infinitesimal model or variants of it (Gianola et al., 2009) has been used as the default model. 271 The infinitesimal model has been instrumental and allowed for many theoretical insights as 272 well as applications to be developed. In particular, prediction of breeding values in animal 273 274 and plant breeding relying on the infinitesimal model has been very successful (García-Ruiz et al., 2016). However, its limitations are also apparent. Cross-population and cross-breed 275 polygenic prediction was low in accuracy (Hayes et al., 2009; Lango Allen et al., 2010; Martin 276 et al., 2019). Although many factors may contribute to this limitation, our simulation results 277 clearly indicated that genetic interactions unaccounted for was a major contributor. Indeed, 278 if the correct genetic model could be specified, cross-population prediction can achieve very 279 high accuracy (Figure 5). There have been attempts to explicitly model non-additive genetic 280 effects in the context of polygenic prediction; some moderate improvement was observed 281 (Varona et al., 2018). However, these studies modeled non-additive effects using genome-282 wide markers, which added a large number of independent predictors as noise to the model 283 and may negatively impact the performance. 284

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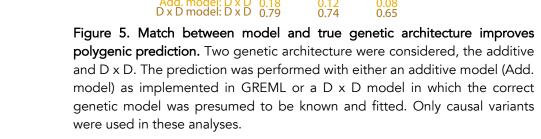
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В

1.0

0.8

0.4

0.2 0.0

r²

Ratio 0.6

Add. model: Additve 0.78

We did not analyze existing large data sets, some of which contained subjects from multiple 294 ancestries. Previous work with real data has consistently shown that cross-population 295 296 polygenic prediction generally fails (Martin et al., 2019). However, it is difficult to disentangle the different factors that may contribute to effect heterogeneity and the failure of prediction 297

in real data sets. Using simulations, we can focus on specific guestions and our results clearly 298 indicated a contribution of genetic interactions to the failure of cross-population polygenic 299 prediction. While the additive infinitesimal model is the most sensible model when no other 300 information is available, our study suggests that the development in the field should be 301 expanded to include efforts to more explicitly model genetic interactions. Although it is 302 challenging, recent advances in modeling (Boyle et al., 2017; Liu et al., 2019) and genomic 303 assays informing regulatory networks (Gerstein et al., 2012) may finally offer new ways to 304 develop biologically sensible models. 305

306 Methods

307 Population simulation

We used the coalescent simulator MaCS (Chen et al., 2008) to simulate genome sequences 308 of 75,000 individuals, with 25,000 in each of the populations, according to the demographic 309 history in Figure 1a. We simulated 1,000 independently inherited chromosomes of 100,000 310 base pairs in size and set mutation rate as 1.25×10^{-8} per bp and recombination as 1.25×10^{-8} 311 ⁸ per bp. Effective population size was set to 20,000. The MaCS command for one 312 chromosome was "macs 150000 100000 -s "\$random seed" -i 1 -h 1000 -t 313 0.001 -r 0.001 -I 3 50000 50000 50000 0 -ej 0.0125 3 2 -ej 0.025 2 314 1". This simulation was performed once but the partition between samples were repeated 315 20 time, which were summarized as box plots in figures. 316

317 Simulation of quantitative phenotypes

We simulated quantitative phenotypes according to the genetic architecture depicted in 318 319 Figure 1c. For each of the three possible genotypes for a biallelic locus with alleles A and a, we used the additive coding aa = -1, Aa = 0, and AA = 1 and the dominance coding aa = 0, 320 Aa = 1, AA = 0 to code genotypes. The simulation of phenotypes consisted of two steps. In 321 the first step, the corresponding genotype coding for an individual or multiplication of 322 genotype codings (in the case of between-loci interactions) were multiplied by a genetic 323 effect randomly drawn from the standard normal distribution and summed over all loci or all 324 pairs of loci to obtain the genetic values. In the second step, an environmental effect was 325 added by drawing from a normal distribution with a computed variance such that the broad 326 sense heritability $H^2 = 0.8$. We performed this simulation in each of the 20 random partitions 327 of populations and independently sampled causal variants and genetic effects. 328

329 Fitting GREML

We fitted the GREML model using GCTA (Yang et al., 2011) with 20,000 individuals from each of the A, B, and C populations and A + B and A + C. The GREML partitioned phenotypic variance into a genomic (σ_g^2) and an environmental component (σ_e^2). Genomic heritability was computed as $h_g^2 = \sigma_g^2/(\sigma_g^2 + \sigma_e^2)$.

334 Polygenic score prediction

The BLUP estimates of SNP effects were obtained using GCTA and provided to PLINK2 335 336 (https://www.cog-genomics.org/plink/2.0/credits) to compute a polygenic score in 5,000 new individuals either from the same population as the fitted model or from a different 337 population. Prediction accuracy of polygenic score was computed as the r^2 of correlating 338 predicted polygenic scores and the simulated true phenotypes. In the case of prediction 339 using causal variants with the correct dominance by dominance model (Figure 5), we 340 constructed pseudo-variants using the relevant genotype coding (for D x D, double 341 heterozygotes were coded as one genotype class and all others another) and ran GREML 342 and polygenic score prediction the same way as an additive model. 343

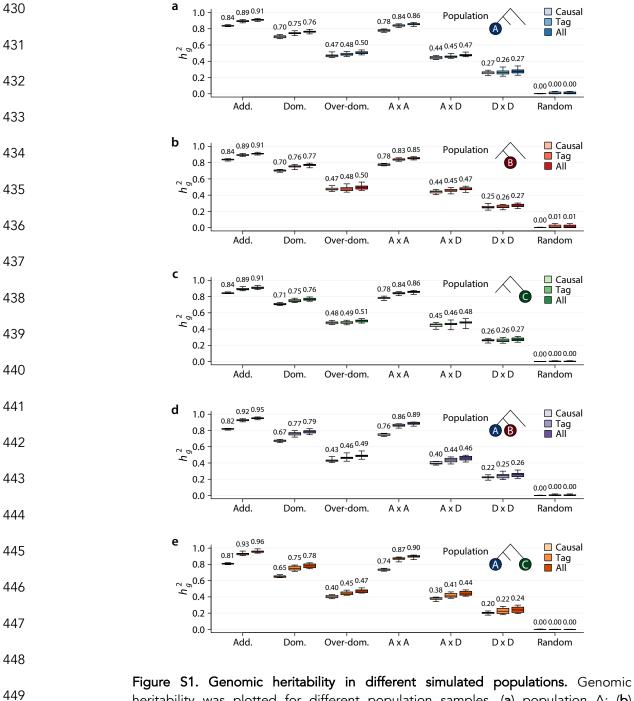
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Supplemental Figures 429



heritability was plotted for different population samples. (a) population A; (b) population B; (c) population C; (d) population A + B; and (e) population A + C.

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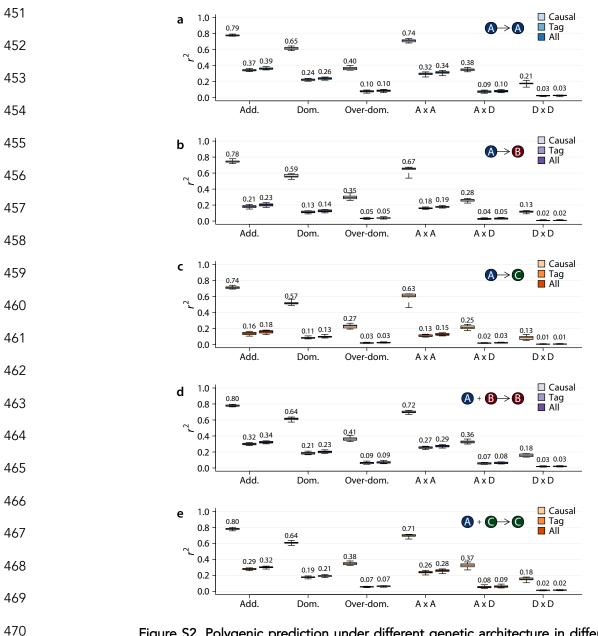


Figure S2. Polygenic prediction under different genetic architecture in different populations. Accuracies of polygenic prediction under different genetic architecture in (**a**) fit model in A, predict in A; (**b**) fit in A, predict in B; (**c**) fit in A, predict in C; (**d**) fit in A + B, predict in B; (**e**) fit in A + C, predict in C.

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