

1 Title: Evaluating species distribution models with discrimination accuracy is
2 uninformative for many applications

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4 Running title: Evaluating niche models with occurrences

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19 Author Contributions: All authors contributed to study design and manuscript

20 preparation. Simulations were coded and run by DLW, literature review was

21 performed by TLI. Post hoc analyses were performed by TLI and DLW.

22 **Abstract**

23 *Aim*

24 Species distribution models are used across evolution, ecology, conservation,
25 and epidemiology to make critical decisions and study biological phenomena,
26 often in cases where experimental approaches are intractable. Choices regarding
27 optimal models, methods, and data are typically made based on discrimination
28 accuracy: a model's ability to predict subsets of species occurrence data that
29 were withheld during model construction. However, empirical applications of
30 these models often involve making biological inferences based on continuous
31 estimates of relative habitat suitability as a function of environmental predictor
32 variables. We term the reliability of these biological inferences "functional
33 accuracy." We explore the link between discrimination accuracy and functional
34 accuracy.

35

36 *Methods*

37 Using a simulation approach we investigate whether models that make good
38 predictions of species distributions correctly infer the underlying relationship
39 between environmental predictors and the suitability of habitat.

40

41 *Results*

42 We demonstrate that discrimination accuracy is only informative when models
43 are simple and similar in structure to the true niche, or when data partitioning is
44 geographically structured. However, the utility of discrimination accuracy for
45 selecting models with high functional accuracy was low in all cases.

46

47 *Main conclusions*

48 These results suggest that many empirical studies and decisions are based on
49 criteria that are unrelated to models' usefulness for their intended purpose. We
50 argue that empirical modeling studies need to place significantly more emphasis
51 on biological insight into the plausibility of models, and that the current
52 approach of maximizing discrimination accuracy at the expense of other
53 considerations is detrimental to both the empirical and methodological
54 literature in this active field. Finally, we argue that future development of the
55 field must include an increased emphasis on simulation; methodological studies
56 based on ability to predict withheld occurrence data may be largely
57 uninformative about best practices for applications where interpretation of
58 models relies on estimating ecological processes, and will unduly penalize more
59 biologically informative modeling approaches.

60

61 Species distribution models (SDM, alternatively environmental niche
62 models or ENM) use data on species occurrences in conjunction with
63 environmental data to generate statistical models of species' ecological
64 tolerances, environmental limits, and potential to occupy different geographic
65 areas. These methods have been used since the 1920s ([Cook 1925](#), [Sutherst
66 2014](#)), but recent years have seen rapid growth in the number of studies
67 employing SDM in fields including ecology, conservation biology, evolutionary
68 biology, and epidemiology ([Peterson, Soberón et al. 2011](#), [Coro, Pagano et al.
69 2013](#), [Allen and Lendemer 2016](#), [Gutierrez-Tapia and Palma 2016](#), [Lezama
70 Ochoa, Murua et al. 2016](#), [Raghavan, Goodin et al. 2016](#), [Guisan, Thuiller et al.
71 2017](#)). The primary appeal of SDMs is their tractability; estimating
72 environmental tolerances experimentally is expensive and time-consuming at
73 best, and impractical for many species. In contrast, SDMs can be constructed
74 with minimal investment of resources, using freely available data and software
75 ([Hijmans, Cameron et al. 2005](#), [Phillips, Anderson et al. 2006](#), [Thuiller,
76 Lafourcade et al. 2009](#), [Hijmans, Phillips et al. 2012](#), [Kriticos, Webber et al. 2012](#)).
77 For many species of conservation concern, they are one of the only tractable
78 means of estimating habitat suitability, often in cases where stakeholders need
79 these estimates urgently ([Keith, Mahony et al. 2014](#), [Warren, Wright et al. 2014](#)).

80 SDM construction involves many decisions which may affect model
81 predictions. These include choice of modeling algorithm, required sample size,
82 optimal model complexity, choice of study area from which data are drawn, the
83 exclusion of outliers, and selection of environmental predictors, among others
84 ([Guisan, Graham et al. 2007](#), [Wisz, Hijmans et al. 2008](#), [Acevedo, Jimenez-](#)

85 [Valverde et al. 2012](#), [Domisch, Kuemmerlen et al. 2013](#), [Boria, Olson et al. 2014](#),
86 [Varela, Anderson et al. 2014](#), [Garcia-Callejas and Araujo 2016](#), [Soley-Guardia](#),
87 [Gutierrez et al. 2016](#), [van Proosdij, Sosef et al. 2016](#)). The literature surrounding
88 these decisions is large and growing rapidly, as is the suite of associated software
89 tools. Decisions about how best to model species are typically made using
90 metrics that test discrimination accuracy on subsets of species occurrence data
91 that have been withheld during model construction ([Elith, Graham et al. 2006](#),
92 [Radosavljevic and Anderson 2014](#)). However, the binary prediction of withheld
93 occurrence data is rarely the intended application of SDMs; they are more
94 frequently used to make continuous estimates of habitat suitability, and to make
95 predictions outside of the training conditions both in space and in time. These
96 applications often implicitly assume that there is biological meaning to the
97 continuous suitability scores produced by the model, or to the functional
98 relationship between environmental gradients and habitat suitability. However,
99 it is often not clear which (if any) measurable biological phenomena should be
100 correlated with suitability estimates from SDMs. Many of the measurable
101 phenomena that are potentially related to suitability (e.g., population density
102 ([Carrascal, Aragon et al. 2015](#)), upper limit of local abundance ([VanDerWal, Shoo](#)
103 [et al. 2009](#), [Gomes, IJff et al. 2018](#))) have not been quantified in detail for many
104 real species and as such are unavailable for model validation.

105 This impracticality of studying environmental suitability experimentally
106 makes it difficult to measure the ability of SDMs to correctly make continuous
107 estimates of habitat suitability. As such, modeling decisions are typically
108 predicated on an assumed relationship between a model's ability to make
109 continuous estimates of relative habitat suitability (hereafter referred to as

110 “functional accuracy”) and its ability to predict withheld occurrence data
111 (discrimination accuracy). This assumption has been questioned before ([Lobo,](#)
112 [Jimenez-Valverde et al. 2008](#)), but its importance and validity for SDM studies is
113 largely untested.

114 Discrimination accuracy is known to be a potentially misleading measure
115 for many applications; it is known to be a poor indicator of model calibration
116 ([Reineking and Schröder 2006](#), [Jimenez-Valverde, Acevedo et al. 2013](#)), and may
117 even be negatively correlated with calibration and functional accuracy under
118 some conditions ([Murphy and Winkler 1992](#)). This general statistical problem
119 may be exacerbated by attributes of the SDM process in a number of ways. First,
120 spatial autocorrelation present in species distributions and in the environment
121 can generate spurious correlations that a model might treat as biological truth,
122 resulting in models that produce high discrimination accuracy even when
123 occurrence data is random ([Raes and ter Steege 2007](#)) or the predictors are
124 biologically meaningless ([Bahn and McGill 2007](#), [Bahn and McGill 2013](#),
125 [Fourcade, Besnard et al. 2018](#)). Second, there are phenomena other than the
126 suitability of habitat that shape species distributions (e.g., historical
127 biogeography, dispersal, biotic interactions, Figure 1) ([Soberon and Peterson](#)
128 [2005](#), [Kearney 2006](#), [Anderson 2012](#), [Warren 2012](#), [Warren 2013](#), [Warren,](#)
129 [Cardillo et al. 2014](#)). Although it is possible to include these processes as
130 predictors for SDMs, this is not often done in practice. Failure to explicitly
131 consider these processes introduces spurious correlations between species
132 occurrences and the environment into the estimate of the environmental niche.

133 Similarly, the collection of occurrence data often shows spatial biases
134 (Figure 1, panel F), which may be correlated with spatially autocorrelated

135 predictors ([Phillips, Dudik et al. 2009](#)). All of these phenomena can lead to poor
136 niche estimates (Figure 2) that still have high discrimination accuracy in
137 geographic space. Since these non-target phenomena are shared between
138 training and test data, a model that parameterizes the environmental correlates
139 of these processes may have higher discrimination accuracy than a model that
140 accurately estimates the species' environmental tolerances, and yet may produce
141 pathological behavior in applications where model transferability or continuous
142 estimates of habitat suitability are desired ([Lobo, Jimenez-Valverde et al. 2008](#),
143 [Veloz 2009](#), [Radosavljevic and Anderson 2014](#), [Torres, Sutton et al. 2015](#), [Huang](#)
144 [and Frimpong 2016](#)).

145 A further issue with discrimination accuracy is the lack of true absence
146 data. One of the primary reasons that SDM methods are so tractable is that they
147 can be used without true absence data, which is often difficult and expensive to
148 obtain. SDMs deal with the lack of true absences by sampling "pseudoabsence"
149 or "background" points which are ideally intended to represent the set of
150 environmental conditions that are potentially accessible to the species. This
151 requires users to make decisions about the size of the appropriate study area for
152 background samples ([Acevedo, Jimenez-Valverde et al. 2012](#)), as well as the
153 nature of sampling (e.g., random points or points from closely related species
154 ([Phillips, Dudik et al. 2009](#))). These decisions are often somewhat arbitrary (e.g.,
155 background areas chosen using political boundaries or poorly-justified
156 assumptions about dispersal), and can affect both the inferred model ([Acevedo,](#)
157 [Jimenez-Valverde et al. 2012](#)) and the performance of metrics used to evaluate
158 models ([Acevedo, Jimenez-Valverde et al. 2012](#), [Hijmans 2012](#), [Jimenez-Valverde,](#)
159 [Acevedo et al. 2013](#)). The lack of real absence data results in models that are

160 incapable of accurately predicting prevalence, and that incorrectly treat some
161 suitable conditions as unsuitable.

162 Finally, the usefulness of discrimination accuracy as a criterion for
163 selecting SDMs may also be negatively impacted by model complexity.
164 Discrimination accuracy only measures whether a model assigns higher
165 suitability values to presence points than it does to background or absence
166 points, and highly flexible algorithms may produce a broad range of marginal
167 suitability functions that have similar, or even identical, discrimination accuracy
168 (Figure 3). This phenomenon is likely compounded by the frequent use of large
169 numbers of predictors that are highly collinear; as the number of predictors and
170 the complexity of marginal suitability functions increase, the number of potential
171 models with similar discrimination accuracy grows very rapidly.

172 Although many of these problems with discrimination accuracy have been
173 noted before, the utility of discrimination metrics for SDM studies has not been
174 examined in a system where the true niche and habitat suitability are known. As
175 a result, we have little information on how useful these metrics are for empirical
176 studies where the goal is to estimate the relative suitability of habitat, despite
177 the ubiquity of discrimination metrics in SDM model selection.

178 Here we adopt a simulation approach to explore the relationship between
179 discrimination and functional accuracy using virtual species for which the true
180 niche is known. We build models using a number of different algorithms, study
181 area sizes, and methods of partitioning training and test data. However, these
182 simulations are not intended to represent all possible modeling approaches. The
183 goal of these simulations is not to determine which method produces the best
184 niche or distribution estimates, but rather to evaluate commonly used methods

185 for model selection across a broad range of models in a system where we know
186 the underlying true habitat suitability.

187

188 **Methods**To examine how model selection was affected by modeling
189 algorithm, sampling bias, and non-target spatial phenomena, we conducted four
190 sets of simulation experiments:

- 191 1. High complexity: Artificial niches were generated using three
192 randomly chosen variables and models were constructed using all
193 nineteen bioclimatic variables. Background data were drawn from
194 100 km circular buffers around occurrence points.
- 195 2. Geographic partitioning: Same conditions as (1) but presence and
196 background points for each species were split into four quadrants
197 using ENMEval ([Muscarella, Galante et al. 2014](#)). Presence and
198 background data from one randomly selected quadrant were withheld
199 for model evaluation.
- 200 3. Large background: Same conditions as (1), but background data were
201 drawn from 1000 km circular buffers around occurrence points.
- 202 4. Low complexity: Niches were based on two randomly chosen
203 variables and models were built using those two variables plus two
204 more chosen at random.

205

206 All analyses used CliMond data for 19 bioclimatic variables typically
207 employed in SDM studies ([Nix 1986](#)) [ENREF 1](#), including data for the present
208 and for 24 combinations of future emissions scenario (A1B and A2), year (2030,
209 2050, 2070, 2080, 2090, and 2100), and climate model (CSIRO-Mk3.0 and

210 MIROC-H) ([Kriticos, Webber et al. 2012](#)). Simulations and analyses were
211 restricted to Australia, including Tasmania.

212 Simulated niches were created using the generateRandomSp function in
213 the virtualspecies R package ([Leroy, Meynard et al. 2015](#)). Simulated species
214 with fewer than 400 suitable grid cells in the initial presence/absence raster
215 showed a strong tendency to produce models that showed no suitable habitat on
216 future climate scenarios, rendering comparisons that were uninformative for
217 model selection. As a result, these simulations were discarded.

218 To simulate the effects of non-target spatial processes (e.g., historical
219 biogeography, biotic interactions, dispersal limitation), the initial
220 presence/absence raster from virtualspecies was converted to point data, which
221 was partitioned into allopatric regions using k-means clustering. Solutions
222 ranging from 2 to 10 clusters were considered, and an algorithm was used to
223 maximize the minimum distance between clusters. One region was assigned at
224 random to be the range of the species, and converted back into a raster. We
225 recorded the total proportion of suitable cells that fell within this range, to
226 measure the extent to which species distributions departed from the distribution
227 of available suitable habitat across the entire study area.

228 Spatial sampling bias was modeled using data from 5,969,252 collection
229 records for 28,286 Australian plant species. These records were harvested from
230 GBIF ([GBIF.org 2015](#)) using the rgbif ([Chamberlain, Boettiger et al. 2013](#))
231 package, and converted to a raster representing the number of observations per
232 grid cell at the same extent and resolution as the environmental data. All values
233 were then divided by the maximum cell value, resulting in a range of sampling
234 intensity from 0 to 1.

235 Species occurrence data was sampled from a raster with values in each
236 grid cell x calculated as:

237

$$238 \quad p(x) = (1 - g_b)s(x)r(x) + g_b b(x)s(x)r(x)$$

239

240 Where probability of sampling is a function of $p(x)$, g_b is a parameter that
241 controls the magnitude of spatial sampling bias, $b(x)$ is the relative strength of
242 spatial sampling bias in cell x , $s(x)$ is the suitability of habitat in the grid cell, and
243 $r(x)$ is a binary variable taking the value 1 inside the species range and 0
244 everywhere else. For each species, we drew 100 simulated occurrence points by
245 selecting grid cells at random and sampling occurrences as a Bernoulli trial with
246 probability of success equal to $p(x)$. Presence points were drawn with
247 replacement so that we could study the effects of sampling bias. We simulated
248 data across eleven levels of spatial sampling bias, with the bias strength
249 parameter ranging from 0 to 1 in increments of 0.1. We performed 20
250 simulations for each of the 11 levels of spatial sampling bias. Each of the four
251 simulation conditions (experiments 1-4, above) therefore consisted of 220
252 simulations, for a total of 880 total simulated species across all experiments.

253 As noted in a recent review ([Meynard, Leroy et al. 2019](#)), simulation
254 studies need to choose both the simulated niches and sampling regimes that are
255 appropriate for the question involved. Since our goal here is to test which
256 metrics select models that accurately estimate the niche, it was essential for us to
257 generate data that would be capable of producing accurate niche estimates in
258 ideal conditions. Due to these concerns we chose not to apply a threshold
259 minimum suitability score below which the organism could not possibly occur;

260 the application of such a threshold would truncate the response functions we are
261 trying to estimate ([Meynard, Leroy et al. 2019](#)), resulting in lower expected
262 functional accuracy. Additionally, prior work with virtual species has
263 demonstrated that the application of thresholds results in discrimination
264 accuracy metrics that are overly optimistic ([Meynard and Kaplan 2013](#)).

265 We built models using seven algorithms; Bioclim, Domain, generalized
266 linear models (GLM), generalized additive models (GAM), Maxent, random
267 forests, and boosted regression trees. Models were built using the dismo R
268 package ([Hijmans, Phillips et al. 2012](#)) and Maxent ([Phillips, Anderson et al.
269 2006](#)). This resulted in 6160 inferred models, seven for each of the 880
270 simulated niches. Algorithm settings were left at their default values. For each
271 model, 25 occurrence points were withheld from model construction and used
272 for model evaluation. Each model's discrimination accuracy was evaluated
273 using three statistics: the area under the receiver operating characteristic curve
274 (AUC) ([Fielding and Bell 1997](#)), the true skill statistic (TSS) ([Allouche, Tsoar et al.
275 2006](#)), and Cohen's kappa ([Cohen 1960](#)). While AUC can be calculated using
276 continuous suitability scores, TSS and kappa require binary predictions of
277 presence and absence, so the values for these models that were used in model
278 assessment corresponded to their maximum value across all potential
279 thresholds, i.e., the best possible performance of a thresholded model ([Fielding
280 and Bell 1997](#)).

281 Models were projected onto the current distribution of the environmental
282 variables used for model construction. Models were also projected onto the 24
283 future climate scenarios. We used the simulated niche from the virtualspecies
284 object to project the true suitability of habitat across those same set of future

285 environments, to assess whether discrimination accuracy is a useful predictor of
286 models' ability to extrapolate to new environmental conditions. To measure
287 functional accuracy, we compared geographic projections of habitat suitability
288 from the true niche and the inferred models using Spearman rank correlation.
289 Correlations between projected and true suitability scores for the present and
290 for future climate scenarios were measured separately within the species range
291 (areas where $r(x) = 1$) and across the entire study area (Australia and Tasmania).
292 Spearman rank correlation was chosen as a measure of functional accuracy for
293 this study due to the structural differences between models produced by
294 different algorithms, and in consideration of how SDMs are often applied; any
295 two models that assign identical rankings to a set of habitat patches are
296 effectively interchangeable for applications where models are thresholded, or
297 where suitability scores are used to prioritize one habitat patch over another.
298 Rank correlation will reflect this when models produce similar rankings of
299 relative habitat suitability (e.g., $\rho = 1$ when predictions made from one model are
300 a monotonically increasing function of predictions made from another model).
301 In contrast, Pearson product moment correlation will only assign a value of 1 if
302 the relationship between suitability scores for the two models is linear, which
303 may serve to exaggerate differences that are not relevant to many empirical
304 studies. In order to test the sensitivity of our results to this choice, we also
305 conducted a separate set of analyses using Pearson product moment correlation
306 as a measure of functional accuracy (Appendix S4), but results from these
307 analyses were effectively the same as those seen in tables 1 and 2.

308 We choose to focus on functional accuracy here instead of calibration for
309 several reasons; first, the application of SDMs more often relies on the relative

310 suitability of habitat than estimating the exact probability of observing a species
311 in a particular place, and functional accuracy more directly estimates this aspect
312 of model behavior. Second, it is already known that discrimination accuracy may
313 be poorly correlated to calibration even when the model gets the relative
314 ranking of habitat right. For example, if the estimated suitability of habitat is a
315 transformation of the true suitability of habitat that preserves relative rankings
316 but not the magnitude of differences in suitability scores ([Reineking and](#)
317 [Schröder 2006](#)), both discrimination and functional accuracy would be high, but
318 calibration would be poor. Finally, the link between discrimination accuracy and
319 calibration is known to be severely affected by prevalence ([Reineking and](#)
320 [Schröder 2006](#), [Elith and Graham 2009](#)), but the link between discrimination
321 accuracy and functional accuracy as measured here would not be so affected.

322 To summarise the relationships between discrimination and functional
323 accuracy for all algorithms considered together (Table 1 and Appendix S3 and
324 S4), we used generalized linear mixed models, and evaluated correlations using
325 McFadden's pseudo- r^2 ([McFadden 1974](#)). For the remainder of the regressions,
326 we used linear models and the standard coefficient of determination, r^2 . We
327 applied Bonferroni corrections to compensate for problems arising from
328 multiple testing. For these purposes we defined four families of test that we
329 consider independently. Those examining the relationship between
330 discrimination and functional accuracy at each combination of algorithm and
331 complexity level (Tables 1 and 2, $n = 12$ comparisons per set), and the
332 remainder, which are intended primarily to examine which factors impact
333 overall model quality and as a check to establish that expected relationships
334 between metrics are seen in the simulation results (Appendix S3, $n = 11$).

335 Based on results from experiments 1-4, we performed a fifth set of
336 simulation experiments to examine more thoroughly the effects of niche
337 complexity and the number of predictor variables on the relationship between
338 discrimination and functional accuracy (Figure 4). Due to the computational
339 intensity of some SDM algorithms, we restricted analyses to a simpler set of
340 conditions for these simulations. Presence data was generated with no non-
341 target spatial biological processes and no spatial sampling bias, so occurrence
342 points were sampled across the entirety of the suitable habitat. We restricted the
343 modeling process to GLM and Maxent, and only used AUC for evaluating
344 predictions on randomly withheld test data. Simulated niches were built using a
345 number of environmental variables ranging between 1 and 19, and models were
346 inferred with between 1 and 19 variables (2 to 19 for Maxent, due to issues with
347 the software implementation), subject to the constraint that variables that were
348 included within the species' niche were selected first during model construction.
349 For each combination of number of niche axes and environmental predictors, we
350 performed 300 separate simulations, resulting in 108,300 total simulations per
351 modeling method. For each simulation we recorded the test AUC and the rank
352 correlation between the inferred and true suitability of habitat. For each
353 combination of number of niche axes and predictors, we then measured the rank
354 correlation between discrimination accuracy and functional accuracy across the
355 set of 300 models. This resulted in a metric ranging from 1, where test AUC was
356 a perfect indicator of functional accuracy, to -1, where test AUC was negatively
357 associated with functional accuracy. We fit a linear model to these results which
358 included the number of variables used for the simulated niche, the number of
359 variables used for model construction, and an interaction term.

360

361 **Results**

362 Regression outputs for experiments 1-4 are summarized in tables 1
363 (algorithms pooled) and 2 (algorithms analyzed separately), and also in
364 appendices S3, S4, and S5. TSS, kappa, and AUC were all highly correlated with
365 each other, so we will not discuss them separately. We found that discrimination
366 accuracy on training and test data were correlated, and that functional accuracy
367 in the training region was correlated with functional accuracy outside the
368 training region. This indicates that models that perform well at discrimination
369 accuracy tend to do so regardless of whether it is measured on training or test
370 data, and the same is true of models that perform well at functional accuracy.
371 Functional accuracy was generally fairly good; a majority of models produced
372 estimates of habitat suitability that were positively correlated with the true
373 suitability of habitat, whether measured in the training region (73.8%), or
374 projected to the continental scale (80.8%). However, models performed
375 somewhat worse when projected into future climate scenarios (65.7% were
376 positively correlated with true suitability within the species range, 71.0% at the
377 continental scale).

378 When all algorithms were analyzed together in a single GLM,
379 discrimination accuracy was a very poor predictor of functional accuracy in all
380 cases (Table 1). Although 31/48 regressions were statistically significant, five
381 were negative correlations, and none had an r^2 value greater than 0.2. This
382 indicates poor performance of discrimination accuracy at selecting models when
383 comparing between algorithms.

384 Results of regressions conducted for each algorithm separately are
385 presented in Table 2. For all experiments, we find that discrimination accuracy is
386 uninformative or actively misleading about models' functional accuracy in a
387 majority of cases (significant positive correlations were seen for less than half of
388 comparisons in any simulation experiment). A majority of these correlations
389 were also quite weak; the average r^2 value was 0.08 (range -.15 to .26). This
390 indicates poor performance of discrimination accuracy at selecting models with
391 high functional accuracy even when comparing models that were built using the
392 same methods. Discrimination accuracy had no negative correlations with
393 functional accuracy when test data were chosen based on a geographic partition
394 of the species' range, but was still a poor predictor of functional accuracy
395 (average $r^2 = 0.12$).

396 We note an interesting phenomenon here with respect to the size of the
397 buffer regions used to draw background data for model fitting and evaluation;
398 the models built using the largest (1000 km) buffers around occurrence points
399 performed very well, with the highest levels of functional accuracy and
400 discrimination accuracy (Appendix S5). These differences were most prominent
401 for discrimination accuracy, reinforcing previous findings showing that
402 discrimination accuracy is sensitive to study area ([Lobo, Jimenez-Valverde et al.
403 2008](#)). Some previous studies have suggested the models perform best when
404 constructed using fairly small study regions, however those studies have largely
405 assessed model quality via discrimination accuracy within the species' native
406 range ([Acevedo, Jimenez-Valverde et al. 2012](#), [Zhu, Rédei et al. 2014](#)). These
407 results indicate that the relationship between study area size and model

408 performance may be more complex than previously reported, and optimal
409 choices may depend on the applications for which models are designed.

410 Our fifth experiment examined the effects of complexity across a broader
411 range of complexity values, and found that the ability of AUC to select GLM
412 models with high functional accuracy was negatively correlated with the
413 complexity of the simulated niche and the number of predictor variables. For
414 Maxent models the relationship between discrimination accuracy and functional
415 accuracy (Figure 4) was positively but weakly correlated ($r^2 = .09$) with the
416 number of variables in the true niche, but uncorrelated with the number of
417 variables included in the modeling process.

418

419 **Discussion**

420 SDM methods are used for many applications in which niche estimates
421 are needed but experimental approaches are impractical. Results for
422 experiments 1-4 demonstrate that many of these models can provide useful
423 estimates of the relative suitability of habitat, the ability of species to invade new
424 areas, and the effects of climate change. However, one of the key steps in any
425 modeling study is the identification of which models from a candidate set
426 perform well and which perform poorly. Our results indicate that the most
427 widely used methods for selecting models are largely uninformative for studies
428 where the goal is to make continuous estimates of habitat suitability, or to
429 estimate the species' response to an environmental gradient. When algorithms
430 were analyzed separately, 15/149 statistically significant correlations between
431 discrimination and functional accuracy were negative. In these cases
432 discrimination metrics were not just uninformative, but in fact positively

433 misleading for applications where the goal of SDM is to predict the relative
434 suitability of habitat.

435 In our fifth experiment we examined the effects of niche and model
436 complexity for GLM models across a broader set of conditions, and found that
437 discrimination accuracy predicts functional accuracy only when both the niche
438 and the environmental space it is being modeled in are far simpler than those
439 seen typically in the empirical literature (Figure 4). Even at low levels of
440 complexity, the relationship between discrimination and functional accuracy for
441 GLM is fairly weak (Spearman rank correlation = 0.31 for a single niche axis and
442 predictor variable), and declines rapidly as models become more complex,
443 becoming minimally informative as models approach levels of complexity that
444 are often seen in the empirical literature.

445 For Maxent models the number of predictors used to model the niche had
446 no effect on the utility of discrimination accuracy for model selection, but there
447 was a weak positive effect of the number of variables used to simulate the true
448 niche ($\beta = .006$, $p < .05$). We hypothesize that the lack of effect of the number of
449 predictors for Maxent is due to its ability to automatically penalize
450 overparameterization; many of the predictors supplied to the algorithm may
451 ultimately have little or no weight in the model. We also note that the most
452 reliable correlations between discrimination accuracy and functional accuracy
453 seen in our simulation results were for Maxent models (Table 2), as would be
454 expected if model complexity and number of predictors were partly responsible
455 for driving the poor performance of discrimination accuracy.

456 Discrimination accuracy was generally a better predictor of functional
457 accuracy for GLM, GAM, and Maxent models than for the other methods of model

458 construction explored in this study. This is likely due to the internal structure of
459 these models. The simulation approach taken here uses a logistic function to
460 generate sampling probabilities based on a simulated niche, which is composed
461 of smooth (linear or quadratic) responses to a set of environmental variables.
462 As such, the function underlying habitat suitability lies within the set of functions
463 that may be exactly estimated by GLM, GAM, or Maxent, so that estimation of
464 simulated niches is considerably more tractable for those methods. We
465 therefore caution users to refrain from interpreting these results as an
466 endorsement of any particular method when constructing SDMs using empirical
467 data. Rather, we suggest that these results indicate that choice of modeling
468 methods should ideally include intuition or data regarding the potential
469 functional relationship between the environmental predictors and the suitability
470 of habitat. If the functional relationships that may be estimated by an algorithm
471 differ significantly from the true functional relationship, discrimination accuracy
472 is largely uninformative or misleading about models' ability to predict habitat
473 suitability. This does not necessarily imply that models built using different
474 functional shapes from the true niche are poor estimates of habitat suitability;
475 rather it indicates that discrimination accuracy is uninformative for selecting
476 models with high functional accuracy under these conditions.

477 Our results clearly indicate that most empirical studies using SDM
478 methods should ideally not rely solely on prediction of withheld occurrence data
479 to assess model quality. However, they also indicate a much more systemic
480 problem for the SDM literature: decades of methodological work in this field
481 have resulted in a set of widely-adopted "best practices", but a great majority of
482 these studies have focused on optimizing models' discrimination accuracy on

483 withheld occurrence data from real species distributions ([Guisan, Graham et al.](#)
484 [2007](#), [Wisn, Hijmans et al. 2008](#), [Domisch, Kueimmerlen et al. 2013](#), [Boria, Olson](#)
485 [et al. 2014](#), [Radosavljevic and Anderson 2014](#), [Moreno-Amat, Mateo et al. 2015](#),
486 [Garcia-Callejas and Araujo 2016](#), [Huang and Frimpong 2016](#), [Kuebler,](#)
487 [Hildebrandt et al. 2016](#), [Lopatin, Dolos et al. 2016](#), [Rovzar, Gillespie et al. 2016](#),
488 [Soley-Guardia, Gutierrez et al. 2016](#)). Given the disconnect seen here between
489 discrimination and functional accuracy, it is entirely possible that the “best
490 practices” advocated in these studies have negligible, or even detrimental, effects
491 on model quality for applications where functional accuracy is the goal.

492 In order to accurately assess the ability of different methods to achieve
493 useful levels of functional accuracy, we argue that the methodological literature
494 must reevaluate its “best practices” via simulations where true habitat suitability
495 and niche parameters are known. While some simulation studies are already
496 being conducted ([Meynard, Leroy et al. 2019](#)), these have typically been done in
497 the context of optimizing discrimination accuracy, and as such may also be
498 largely uninformative about estimating habitat suitability as a function of
499 environmental gradients. There are many common practices and assumptions in
500 the field that may need to be reevaluated based on their ability to estimate
501 habitat suitability; choice of algorithm, methods for choosing predictor variables,
502 choice of study area, rarefaction of data, and optimal model complexity are
503 obvious candidates.

504 In addition, we argue that practitioners must recognize that favoring
505 models based strictly on their spatial predictions is simply inappropriate for
506 many applications. In studies where the goal is to estimate the niche (i.e.,
507 maximize functional accuracy), users must become comfortable with the idea

508 that a biologically accurate model may produce relatively poor estimates of
509 species' current spatial distributions. This is not simply a methodological point
510 brought to light by the current simulation study; it is necessarily true given the
511 existence of non-target phenomena that themselves have spatial structure (e.g.,
512 biotic interactions, dispersal). This has been known for years ([Jackson and](#)
513 [Overpeck 2000](#), [Soberon and Peterson 2005](#), [Anderson 2012](#), [Warren 2012](#),
514 [Warren 2013](#)), yet has been largely ignored in the continued pursuit of methods
515 that produce tighter and tighter fits to training or test data in geographic space.

516 Investigators familiar with SDM methods will no doubt wish to critically
517 examine the methods used here to infer models; there are other algorithms
518 available, and there are many modeling choices that we did not explore in great
519 depth. However, these criticisms are largely irrelevant to the primary results of
520 this study; while it is certainly possible that greater effort in exploring the space
521 of model choices might improve the accuracy of models, we note that (1)
522 evaluation metrics on randomly withheld test data for the models generated
523 here are not unusual for the range seen in the empirical SDM literature (e.g.,
524 Appendix S5), (2) the overall performance of SDM methods is irrelevant to
525 whether or not discrimination accuracy is a valid indicator of functional
526 accuracy, and (3) most SDM users' methodological preferences are currently
527 chosen based on studies that seek to maximize the very performance metrics
528 that the current study demonstrates are not useful for estimating functional
529 accuracy.

530 We acknowledge the possibility that there is some subset of modeling
531 approaches not addressed here for which discrimination and functional accuracy
532 are highly correlated. It would be both gratifying and very useful to find such a

533 set of conditions, and that topic deserves to be examined in great depth.
534 However, even if such a set can be found it does not invalidate the conclusion
535 presented here; that there is a large range of modeling algorithms and
536 approaches for which the correlation between discrimination accuracy and
537 functional accuracy is not strong enough to be useful in model selection for many
538 purposes. Similarly, we acknowledge that the disconnect between functional
539 accuracy and discrimination seen here may be affected by sample size, but the
540 sample sizes used here (75 training, 25 test) are not atypical for the ENM
541 literature.

542 In summary, we demonstrate that, under a broad range of conditions, the
543 ability of a model to successfully predict withheld occurrence data within the
544 training region does not reliably measure its ability to estimate the relationship
545 between environmental gradients and habitat suitability. Discrimination
546 accuracy may be a reasonable metric when the goal is to guide further sampling
547 of occurrences within a species' current range, without regard for whether the
548 model estimates the true environmental niche or the relative suitability of
549 habitat well. However, this is not often the goal of empirical model construction
550 in the SDM literature.

551 As a result, the applied and methodological literature in this field are
552 largely based on metrics that may be irrelevant to the intended applications of
553 many models. If the field is to continue to attempt to use SDMs to infer species'
554 responses to environmental gradients, we must develop methods for model
555 construction and metrics for model evaluation that are more relevant to the
556 actual goals of the modeling process. While we find that geographically
557 structured partitioning of test data does offer some advantages over randomly

558 withheld data, it is clear from this study that even those methods have very
559 limited ability to identify models that accurately estimate the relative suitability
560 of habitat.

561 We would like to particularly highlight the implications of our results for
562 the development of new methods in this field in the coming years. Many
563 investigators are currently developing methods that incorporate more biological
564 and statistical realism into the SDM process, including the integration of
565 physiological and trait data ([Pollock, Kelly et al. 2018](#)) and explicit models of bias
566 ([Robinson, Ruiz - Gutierrez et al. 2018](#)), dispersal ([Zurell 2017](#)), plasticity ([Bush,
567 Mokany et al. 2016](#)), and evolutionary history ([Smith, Godsoe et al. 2019](#)). In any
568 system affected by non-target spatial phenomena, these methods will often
569 produce poorer estimates of species' geographic distributions precisely because
570 they provide better estimates of the environmental niche. We hope that the
571 results presented here will compel the field to evaluate these new methods
572 based on their ability to infer the biological phenomena of interest, as
573 demonstrated using simulations or physiological data, rather than simply reject
574 them due to poor discrimination accuracy on misleading occurrence data.

575 We feel it is necessary to specifically address one interpretation of these
576 results that we feel is not appropriate: the work presented here is not intended
577 to suggest that any particular method of SDM construction is inherently better or
578 worse than others. While the relative performance of different methods is a very
579 interesting question and one that deserves further exploration within a
580 simulation framework, this study was not designed to address those questions
581 and it would be inappropriate to interpret these results as such. We emphasize
582 that most of the models built from these simulated species were arguably

583 publishable distribution estimates, and were at least somewhat useful as
584 estimates of the species' niche. Rather, this study is intended to examine the
585 performance of widely-used methods of model selection, and it is those methods
586 that are performing poorly. We demonstrate that we can make both good
587 distribution estimates and good niche estimates using common methods, and in
588 fact produced many models that are good for both purposes. However, our
589 results indicate that we have a difficult time distinguishing good models from
590 bad when our goal is functional accuracy.

591 At minimum, our results suggest that any empirical study using
592 discrimination accuracy to assess model quality should start with two crucial
593 steps: (1) use a minimal set of predictor variables for which there is an a priori
594 reason to expect that they limit the suitability of habitat for the species, and (2)
595 select algorithms capable of inferring functional responses that are plausible
596 estimates of the underlying biology (e.g., not using a step function in situations
597 where suitability is expected to be a continuous function of the predictor
598 variable). In a sense, these findings are unsurprising; they recapitulate
599 longstanding best practices in the broader literature regarding statistical
600 modeling ([Anderson and Burnham 2004](#), [Burnham and Anderson 2004](#), [Gelman
601 and Hill 2006](#), [Zuur, Ieno et al. 2009](#)). However, here we show that failure to
602 make these choices appropriately does not necessarily lead to poor predictions;
603 instead it means that we are largely unable to distinguish good models from bad
604 using species occurrence data. Under these conditions any preference for a
605 given model based on discrimination accuracy may be little better than choosing
606 a model at random.

607

608

Independent variable	Dependent variable	Simple	Complex	Large BG	Geographic
Test AUC	Spearman (N)	+,.01		+,.02	+,.08
Test AUC	Spearman (C)				+,.02
Test Max TSS	Spearman (N)	+,.01		+,.02	+,.07
Test Max TSS	Spearman (C)		-,.01		+,.01
Test Max Kappa	Spearman (N)		-,.01	+,.01	+,.06
Test Max Kappa	Spearman (C)	-, .01	-,.01	-,.01	+,.01
Test AUC	Spearman (F, N)	+,.10	+,.11	+,.11	+,.12
Test AUC	Spearman (F, C)	+,.01		+,.08	+,.01
Test Max TSS	Spearman (F, N)	+,.09	+,.10	+,.11	+,.12
Test Max TSS	Spearman (F, C)				+,.01
Test Max Kappa	Spearman (F, N)	+,.20	+,.05	+,.11	+,.10
Test Max Kappa	Spearman (F, C)				+,.01

Table 1. Results of regressions functional accuracy on discrimination accuracy, all algorithms considered together. Significant positive correlations are represented by “+” and green cell color, negative correlations by “-“ and pink cell color. Numbers indicate r^2 values for each regression. Variables accompanied by (F) indicate that they were measured on models projected across 24 future climate scenarios. Variables with (N) and(C) indicated models projected within the species native range or at a continental scale, respectively. Results are presented separately for four model sets: the “simple” set of predictors (2 variables in the true niche, 4 predictors per model,

100km buffer), the “complex” set of predictors (3 variables in the true niche, 19 predictors per model, 100km buffer), the “large background” study region (same simulation settings as “complex” but with a 1000km buffer), and the “geographically structured” model set, for which models were constructed and evaluated using geographically partitioned data (same simulation settings as “complex” but with geographic partitioning of data instead of random holdouts).

Independent variable	Dependent variable	Simple						Complex							
		BC	DM	GAM	GLM	MX	RF	BRT	BC	DM	GAM	GLM	MX	RF	BRT
Test AUC	Spearman (N)				+,.15	+,.06	+,.05	+,.05	-,.05	-,.08		+,.06	+,.06	+,.06	+,.05
Test AUC	Spearman (C)			+,.08	+,.07				-,.10				+,.05		
Test Max TSS	Spearman (N)				+,.14	+,.04			-,.04	-,.1		+,.04	+,.04	+,.04	+,.05
Test Max TSS	Spearman (C)	-,.05		+,.07	+,.07				-,.11				+,.04		
Test Max Kappa	Spearman (N)				+,.11				-,.07	-,.10					
Test Max Kappa	Spearman (C)	-,.06			+,.04				-,.14						
Test AUC	Spearman (F, N)	+,.06		+,.17	+,.14	+,.18	+,.08	+,.15	+,.10	+,.05	+,.14	+,.06	+,.26	+,.11	+,.11
Test AUC	Spearman (F, C)			+,.09	+,.06	+,.04							+,.05		
Test Max TSS	Spearman (F, N)	+,.05		+,.14	+,.14	+,.15	+,.05	+,.12	+,.09	+,.05	+,.14	+,.05	+,.23	+,.08	+,.09
Test Max TSS	Spearman (F, C)			+,.07	+,.05								+,.04		
Test Max Kappa	Spearman (F, N)			+,.10	+,.10	+,.11		+,.06	+,.08	+,.04	+,.07	+,.05	+,.14		
Test Max Kappa	Spearman (F, C)			+,.04											

		Large Background						Geographic Partitioning							
		BC	DM	GAM	GLM	MX	RF	BRT	BC	DM	GAM	GLM	MX	RF	BRT
Test AUC	Spearman (N)				+,.08	+,.08	+,.05	+,.07	+,.06	+,.02	+,.05	+,.09	+,.14	+,.07	+,.17
Test AUC	Spearman (C)					+,.17								+,.04	
Test Max TSS	Spearman (N)				+,.08	+,.08	+,.05	+,.07	+,.06		+,.06	+,.09	+,.12	+,.07	+,.19
Test Max TSS	Spearman (C)	-,.04		-,.05		+,.18									
Test Max Kappa	Spearman (N)				+,.05	+,.07		+,.04	+,.05			+,.09	+,.09	+,.06	+,.13
Test Max Kappa	Spearman (C)	-,.12		-,.08		+,.10	+,.07								
Test AUC	Spearman (F, N)	+,.06			+,.10	+,.25	+,.16	+,.21			+,.10	+,.11	+,.16	+,.19	+,.21
Test AUC	Spearman (F, C)					+,.25									
Test Max TSS	Spearman (F, N)	+,.05			+,.09	+,.26	+,.18	+,.23			+,.12	+,.12	+,.17	+,.20	+,.19
Test Max TSS	Spearman (F, C)					+,.27							+,.04		
Test Max Kappa	Spearman (F, N)	+,.04			+,.06	+,.23	+,.13	+,.16			+,.10	+,.12	+,.13	+,.15	+,.15
Test Max Kappa	Spearman (F, C)					+,.17	+,.06								

Table 2. Relationship between discrimination accuracy and functional accuracy, methods considered separately. Significant positive correlations are represented by “+” and green cell color, negative correlations by “-“ and pink cell color. Numbers indicate r^2 values for each regression. Variables accompanied by (F) indicate that they were measured on models projected across 24 future climate scenarios. Variables with (N) and(C) indicated models projected within the species native range or at a continental scale, respectively. Results are presented separately for four model sets: the “simple” set of predictors (2 variables in the true niche, 4 predictors per model, 100km buffer), the “complex” set of predictors (3 variables in the true niche, 19 predictors per model, 100km buffer), the “large background” study region (same simulation settings as “complex” but with a 1000km buffer), and the “geographically structured” model set, for which models were constructed and evaluated using geographically partitioned data (same simulations settings as “complex” but with geographic partitioning of data instead of random holdouts).

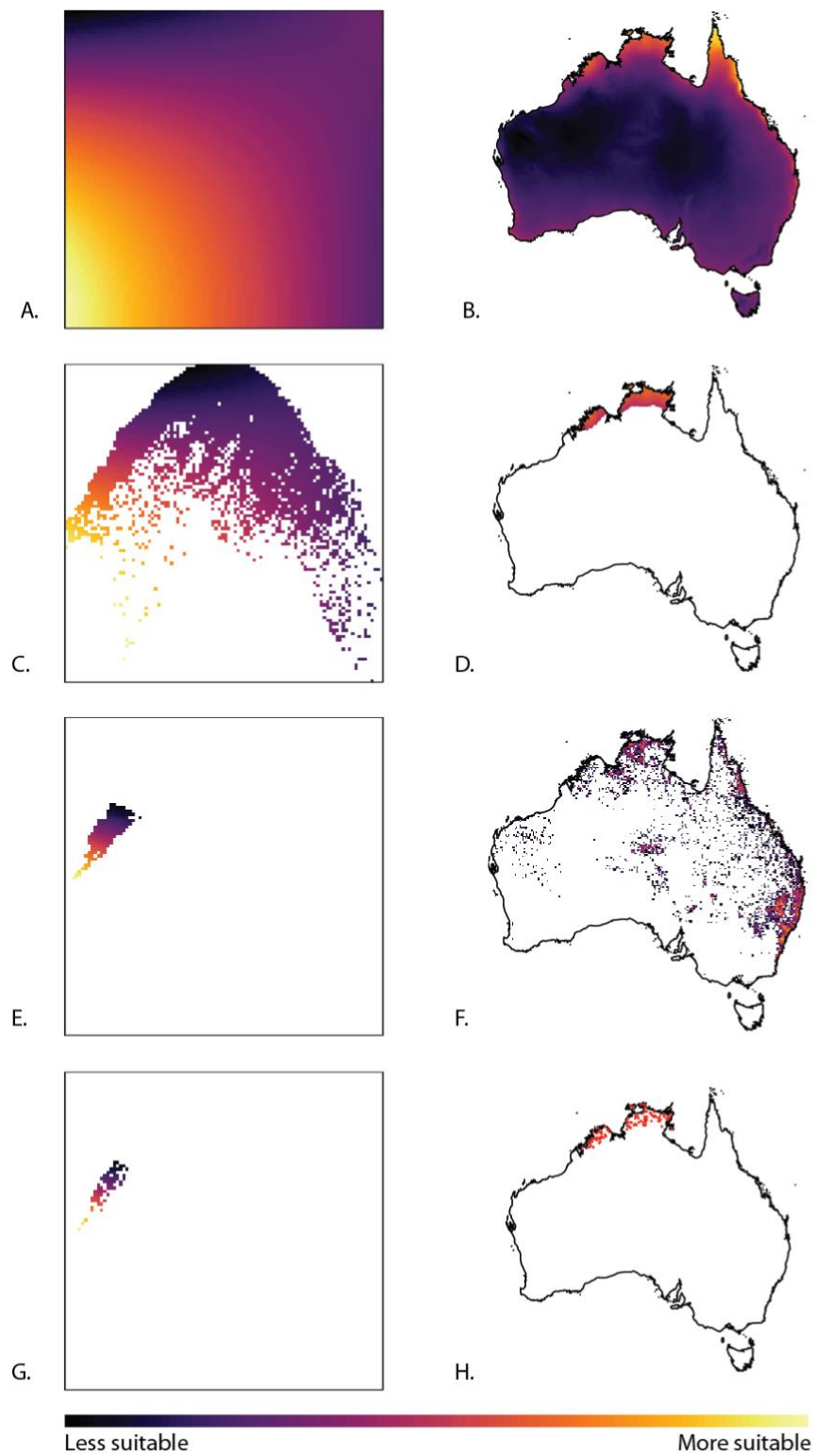


Figure 1. Phenomena affecting species distributions and inference of suitability of habitat. Panel A depicts the niche of a simulated species in the first two principal component axes of the 19 Bioclim variables for Australia. Panel B represents the distribution of suitable habitat for the simulated species. The available habitat present across the continent of Australia only represents a subset of the possible niche space (C). The species' current range only encompasses a subset of the suitable habitat (D), which further limits the potential distribution of data in environment space (E). Spatial sampling bias (F, see methods) contributes further bias to the representation of the species both in environment space (G) and geographic space (H). While the geographic distribution of the data (H, red points) may resemble the current range of the species (D), the distribution of that data in environment space (G) is a poor representation of the species' true niche (A). As a result, it may be relatively easy to achieve accurate predictions on randomly withheld occurrence data while still producing a poor estimate of the underlying biology and suitability of habitat.

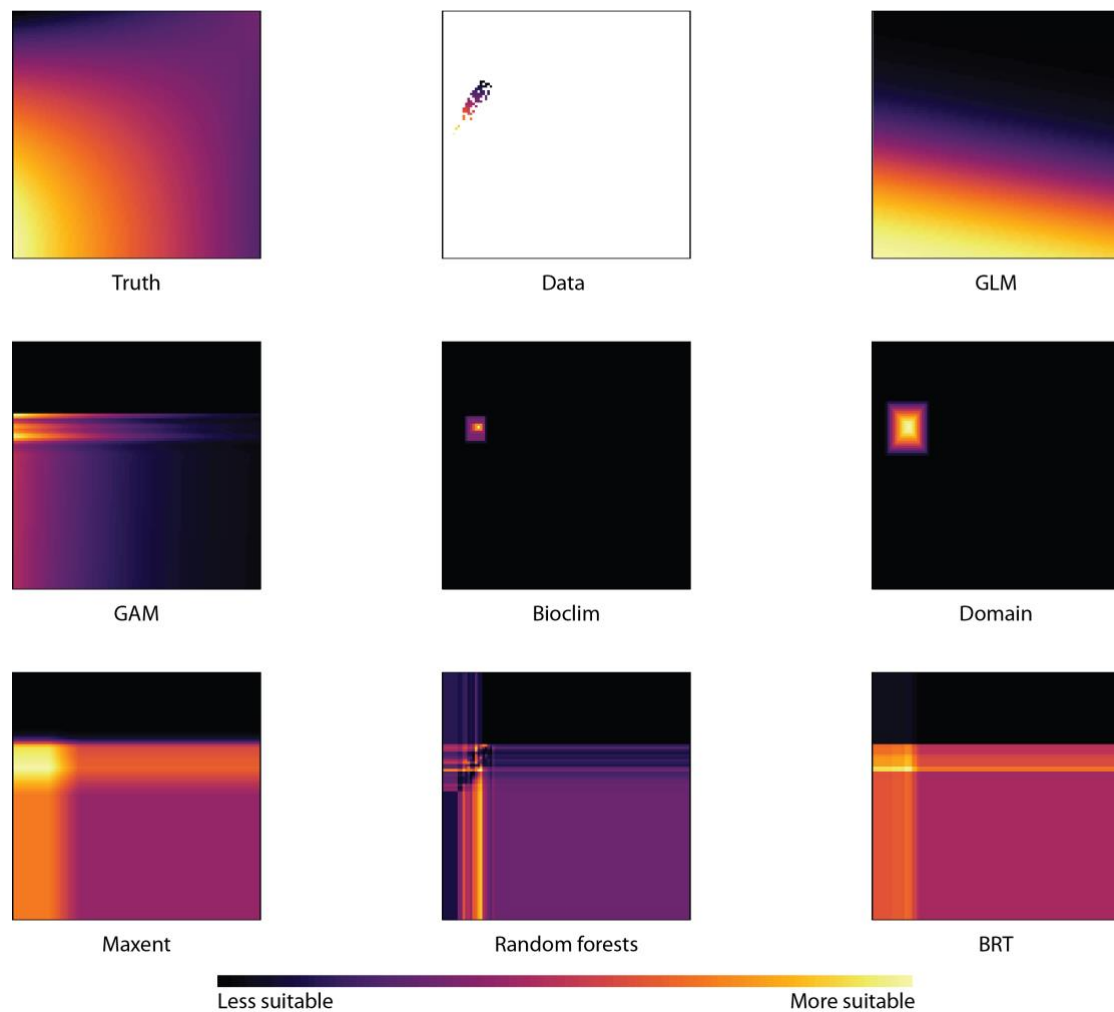


Figure 2. Projection of modeling algorithms in environment space. Using 100 occurrence points for the simulated species in figure 1, we built models using the seven algorithms employed in this study and projected them into the same two dimensional principal component space. The lowest AUC score on 20 randomly withheld data points belonged to random forests (AUC = 0.55), while the highest came from domain (AUC = 0.73). The top left and top center panels show the true niche of the simulated species and the environmental distribution of the data, respectively.

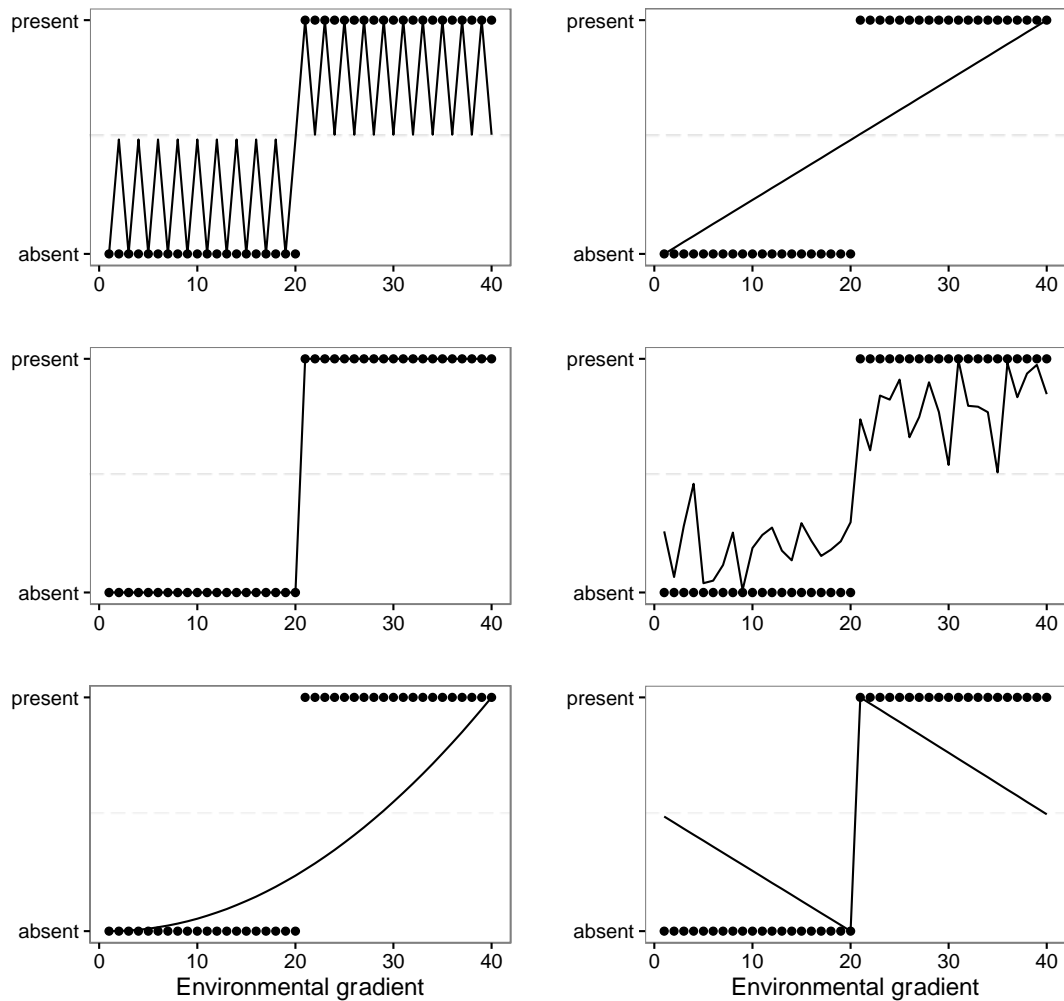


Figure 3. Low information content of discrimination accuracy for inferring functional accuracy. In the above plots, we have simulated 20 absence and 20 presence points along a hypothetical environmental gradient. The six panels represent six hypothetical functions that might be inferred using this data. Each function assigns a higher suitability score (y axis) to all of the presence points than it does to any of the background or absence points. As a result, each function has perfect discrimination accuracy. All six functions are therefore indistinguishable from each other based on discrimination metrics (AUC, TSS,

Kappa), while making very different estimates of the functional relationship of habitat suitability to the environmental predictor variable.

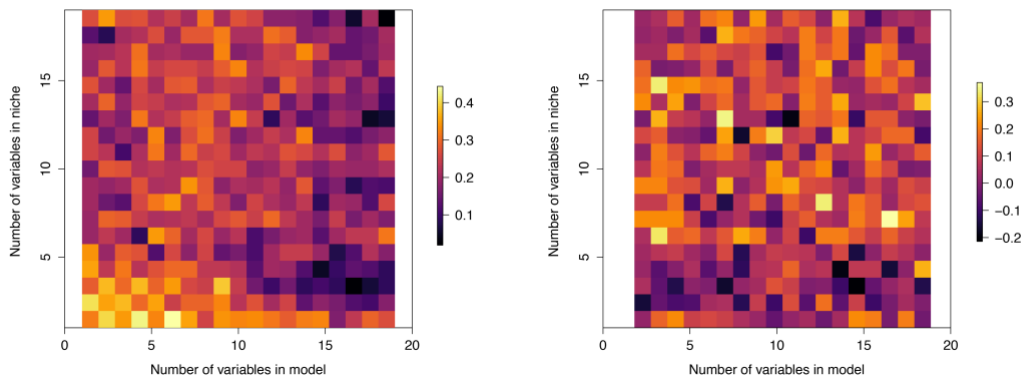


Figure 4. Relationship between number of variables in simulated niche, number of variables in model, and the ability of discrimination to infer functional accuracy for GLM (left) and Maxent (right). Each grid cell represents the output of 300 simulations. The color of each grid cell represents the Spearman rank correlation between test AUC values and functional accuracy.

Supplementary materials:

Appendix S1. Frequency of use of model fit metrics (columns) and partitioning scheme for test data (rows) from a survey of 94 recent applied SDM studies.

Appendix S2. Literature review for metrics of model fit.

Appendix S3. Relationship between evaluation metrics and simulation settings, all algorithms considered together.

Appendix S4. Relationship between discrimination accuracy and functional accuracy using Pearson product moment correlations.

Appendix S5. Discrimination and functional accuracy performance for each simulation experiment.

Data Availability:

Sample code is available on github here:

<https://github.com/danlwarren/sim-code-Warren-et-al-2019>

Acknowledgements

This work would not have been possible without the financial contributions of the Macquarie University Department of Biology and a DECRA award from the Australian Research Council.

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