1 Sleep prevents catastrophic forgetting in spiking neural networks by

2 forming joint synaptic weight representations

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- 10 Abstract: 150 words; Main Text: 5295 words; Methods: 2554 words
- 11 **Pages:** 31; **Figures:** 7
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- 19 Keywords: Spiking neural network model, catastrophic forgetting, sleep, rewarded spike-timing-
- 20 dependent plasticity
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22 **Abstract (150 max)**

Artificial neural networks overwrite previously learned tasks when trained sequentially, a 23 phenomenon known as catastrophic forgetting. In contrast, the brain learns continuously, and 24 25 typically learns best when new learning is interleaved with periods of sleep for memory consolidation. In this study, we used spiking network to study mechanisms behind catastrophic 26 27 forgetting and the role of sleep in preventing it. The network could be trained to learn a complex foraging task but exhibited catastrophic forgetting when trained sequentially on multiple tasks. 28 New task training moved the synaptic weight configuration away from the manifold representing 29 old tasks leading to forgetting. Interleaving new task training with periods of off-line 30 reactivation, mimicking biological sleep, mitigated catastrophic forgetting by pushing the 31 synaptic weight configuration towards the intersection of the solution manifolds representing 32 33 multiple tasks. The study reveals a possible strategy of synaptic weights dynamics the brain applies during sleep to prevent forgetting and optimize learning. 34

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36 Introduction

Humans are capable of continuously learning to perform novel tasks throughout life without
interfering with their ability to perform previous tasks. Conversely, while modern artificial
neural networks (ANNs) are capable of learning to perform complicated tasks, ANNs have
difficulty learning multiple tasks sequentially¹⁻³. Sequential training commonly results in
catastrophic forgetting, a phenomenon which occurs when training on the new task completely
overwrites the synaptic weights learned during the previous task, leaving the ANN incapable of
performing a previous task¹⁻⁴. Attempts to solve catastrophic forgetting have drawn on insights

44	from the study of neurobiological learning, leading to the growth of neuroscience-inspired
45	artificial intelligence (AI) ⁵⁻⁷ . While these approaches are capable of mitigating catastrophic
46	forgetting in certain circumstances ⁶ , a general solution which can achieve human level
47	performance for continual learning is still an open question.
48	Historically, an interleaved training paradigm, where multiple tasks are presented within
49	a common training dataset, has been employed to circumvent the issue of catastrophic
50	forgetting ^{4,8,9} . In fact, interleaved training was originally construed to be an approximation to
51	what the brain may be doing during sleep to consolidate memories; spontaneously reactivating
52	memories from multiple interfering tasks in an interleaved manner ⁹ . Unfortunately, explicit use
53	of interleaved training, in contrast to memory consolidation during biological sleep, imposes the
54	stringent constraint that the original training data be perpetually stored for later use and
55	combined with new data to retrain the network ^{1,2,4,9} . Thus, the challenge is to understand how the
56	biological brain enables memory reactivation during sleep without access to past training data.
57	Parallel to the growth of neuroscience-inspired ANNs, there has been increasing
58	investigation of spiking neural networks (SNNs) which attempt to provide a more realistic model
59	of brain functioning by taking into account the underlying neural dynamics and by using
60	biologically plausible local learning rules ¹⁰⁻¹³ . A potential advantage of the SNNs, that was
61	explored in our new study, is that local learning rules combined with spike-based communication
62	allow previously learned memory traces to reactivate spontaneously and without interference
63	during off-line processing – sleep. A common hypothesis, supported by a vast range of
64	neuroscience data, is that the consolidation of memories during sleep occurs through local
65	unsupervised synaptic changes enabled by reactivation of the neuron ensembles engaged during

66	learning ¹⁴ . Indeed, spike sequence replay was observed in the neocortex ¹⁵⁻¹⁷ following both
67	hippocampal-dependent tasks ¹⁵ and hippocampal-independent tasks ¹⁸ .

68 Here we used a multi-layer SNN with reinforcement learning to investigate whether interleaving periods of new task training with periods of noise-induced spontaneous reactivation, 69 resembling sleep in the brain¹⁹⁻²¹, can circumvent catastrophic forgetting. The network could be 70 trained to learn one of two complementary complex foraging tasks involving pattern 71 72 discrimination but exhibits catastrophic forgetting when trained on the tasks sequentially. Significantly, we show that catastrophic forgetting can be prevented by periodically interrupting 73 74 reinforcement learning on a new task with unsupervised sleep phases. While new task training 75 alone moved synaptic weight configuration away from the solution manifold representing old tasks and towards the manifold specific for new task, interleaving new task training with 76 unsupervised sleep replay allowed the synaptic weights to stay near the manifold specific for the 77 old task and still to move towards its intersection with the manifold representing the new task. 78 79 Our study predicts that sleep prevents catastrophic forgetting in the brain by forming joint 80 synaptic weight representations suitable for storing multiple memories.

81

82 **Results**

83 Complementary complex foraging tasks can be robustly learned

We modeled a simple 3-layer feedforward spiking neural network (see Figure 1A and *Methods: Network Structure* for details) simulating basic steps from sensory input to motor output in the
brain. Excitatory synapses between the input (I) and hidden (H) layers were subjected to
unsupervised learning (implemented as non-rewarded STDP)^{22,23} while those between the H and

output (O) layers were subjected to reinforcement learning (implemented using rewarded 88 STDP)²⁴⁻²⁷ (see *Methods: Synaptic plasticity* for details). Unsupervised plasticity allowed 89 90 neurons in layer H to learn different particle patterns at various spatial locations of the input layer I, while rewarded STDP allowed the neurons in layer O to learn motor decisions based on 91 the type of the particle patterns detected in the visual field¹². We trained the network on one of 92 93 two complementary complex foraging tasks. In either task, the network learned to discriminate between a rewarded and a punished particle pattern in order to acquire as much of the rewarded 94 95 patterns as possible. In the following we consider pattern discriminability (rewarded vs punished) as a measure of performance, with chance performance being 0.5. 96 97 The paradigm for Task 1 is shown in Figure 1B. First, during an unsupervised learning 98 period, all 4 types of 2-particle patterns (horizontal, vertical, positive diagonal, and negative diagonal) were present in the environment with equal densities. This was a period, equivalent to 99 100 a developmental critical period in the brain, when the network learned the environmental 101 statistics and formed, in layer H, high level representation of all possible patterns found at the different visual field locations (see Figure 2 for details). Unsupervised training was followed by 102 103 a reinforcement learning period, equivalent to task specific training in the brain, during which the 104 synapses between layers I and H were frozen but synapses from H to O were updated using a 105 rewarded STDP rule. The reinforcement learning period was when the network learned to make 106 decisions about which direction to move based on the visual input. Whether patterns were 107 rewarded during reinforcement learning depended on the task – for Task 1 horizontal patterns 108 were rewarded and negative diagonal patterns were punished (Figure 1D). During both the 109 rewarded training and the testing periods only 2 types of patterns were present in the 110 environment (e.g. horizontal and negative diagonal for Task 1).

111	After training Task 1, mean performance on Task 1 was 0.70 ± 0.2 while on Task 2
112	(which has not been trained yet) was 0.53 ± 0.2 (chance level). Figure 1D shows examples of
113	trajectories of the simulated agent at the beginning of (left) and after (right) reinforcement
114	learning period. The naive agent moved randomly through the environment, but after training it
115	moved to seek out horizontal patterns and largely avoid negative diagonal ones. The
116	complementary paradigm for Task 2 (vertical patterns are rewarded and positive diagonal are
117	punished) is shown in Figure 1C,E. These results demonstrate that the network is capable of
118	learning and performing either one of the two complementary complex foraging tasks.
119	To get an understanding of the policy developed by the network for each task, we
120	computed the receptive field of each neuron in layer O with respect to the input from layer I (see
121	schematic in Figures 2A/C). This was done by first computing the receptive fields of all of the
122	neurons in layer H with respect to I, then performing a weighted average where the weights were
123	given by the synaptic strength from each neuron in layer H to the particular neuron in layer O.
124	Figure 2A shows a representative example of the receptive field which developed after training
125	on Task 1 for one specific neuron in layer O which controls movements to the upper-left
126	direction. This neuron responded most robustly to bars of horizontal orientation (rewarded) in the
127	upper-left quadrant of the visual field and, importantly, did not respond to bars of negative
128	diagonal orientation (punished).

Figure 2B shows examples of receptive fields of six neurons in layer H which synapse strongly onto the upper-left neuron in layer O (the neuron shown in Figure 2A). These neurons form high level representations of the input patterns, similar to the neurons in the higher levels of the visual system or later layers of a convolutional neural network²⁸⁻³⁰. The majority of these receptive fields revealed strong selection for the horizontal (i.e. rewarded) food particles in the

upper-left quadrant of the visual field. As a particularly notable example, one of these layer H 134 neurons (Figure 2B; middle-right) preferentially responded to negative diagonal (i.e. punished) 135 food particles in the bottom-right quadrant of the visual field. Thus, spiking in this neuron caused 136 the agent to move away from these punished food particles. Similar findings after training on 137 Task 2 are shown in Figures 2C and 2D. 138 139 Catastrophic forgetting occurs following sequential but not interleaved training 140 141 We next tested whether the network model could exhibit catastrophic forgetting by training 142 sequentially on Task 1 (old task here) followed by Task 2 (new task) (Figure 3A). Following 143 Task 2 training, performance on Task 1 was down to no better than chance (0.52 ± 0.02) , while 144 performance on Task 2 improved to 0.69 ± 0.03 (Figure 3 A,B). Thus, sequential training on a complementary task caused the network to undergo catastrophic forgetting of the task trained 145 earlier, remembering only the most recent task. 146 Interleaved training was proposed as a solution for catastrophic forgetting^{4,8,9}, so we 147

added an Interleaved Task 1 and Task 2 (Interleaved_{T1,T2}) training phase to our simulation 148 149 (Figure 3A) to test whether it was a capable of learning Task 1 (now new task) without overwriting Task 2 (old task). For interleaved training we alternated short presentations of Task 150 151 1 and Task 2 every 100 movement cycles. Figure 3B shows that, following Interleaved_{T1,T2} 152 training, the network achieved a performance of 0.65 ± 0.03 on Task 1 and a performance of 0.67 ± 0.04 on Task 2. Therefore, Interleaved_{T1,T2} training allowed the network to relearn Task 1 153 154 without forgetting what the network had just learned during training on Task 2. Note, we also tested Interleaved_{T1,T2} training right after the unsupervised phase and found the same high 155 156 performance for both Task 1 and Task 2 (not shown).

157	We identified task-relevant synapses after training on a given task (top 10% of synapses),
158	and we traced the same set of synapses after training on the opposing task or after
159	Interleaved $_{T1,T2}$ training. The structure in the distribution of Task 1-relevant synapses following
160	Task 1 training (Figure 3C, top-left) was destroyed following Task 2 training (top-middle; i.e.,
161	majority of Task 1-relevant synapses were reduced to zero after Task 2 training) but partially
162	recovered following Interleaved $_{T1,T2}$ training (top-right). Similarly, the structure in the
163	distribution of Task 2-relevant synapses following Task 2 training (bottom-middle) was not
164	present following Task 1 training (bottom-left) and was partially retained following
165	Interleaved _{T1,T2} training (bottom-right).
166	To better understand the effect of Interleaved $_{T1,T2}$ training on the synaptic weights, we
167	trained a support vector machine (SVM; see Method: Support Vector Machine Training for
168	details) with a radial basis function kernel to classify the synaptic weight configurations between
169	layers H and O (i.e. those responsible for decision making) according to whether they serve to
170	perform Task 1 or Task 2. Figure 3D shows the average distance from the decision boundary
171	across trials for synaptic weights associated with Task 1, Task 2, and Interleaved _{T1,T2} training.
172	While the SVM robustly classified the synaptic weight matrices from Task 1 and Task 2, the
173	weight states after Interleaved $_{T1,T2}$ training were significantly closer to the decision boundary
174	(typically on the task 2 side). This indicates that the synaptic weight matrices from
175	Interleaved _{T1,T2} training are a mixture of Task 1 and Task 2 states.
176	Figure 3E shows the trajectory of the synaptic weight distribution for the experiment in
177	Figure 3A projected to 3-dimensions using principal components analysis (PCA). It can be seen
178	that while synaptic weight matrices associated with Task 1 and Task 2 training cluster in distinct

regions of PC space, Interleaved_{T1,T2} training pushes the synaptic weights to an intermediate
location between Task 1 and Task 2.

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182 Periods of sleep allow for sequential training without catastrophic forgetting

Sleep is believed to be an off-line processing period when recent memories are replayed to avoid damage by new learning. Particularly for procedural (hippocampal-independent) memories, rapid-eye-movement (REM) sleep may organize neuronal activity to replay memory traces³¹.
Can we implement a sleep like phase to our model to protect an old task and still accomplish new task learning without explicit re-training of the old task (e.g., without doing explicit interleaved training of Task 1 and Task 2)?

189 Again, we first trained the network on Task 1 and Task 2 sequentially to illustrate occurrence of catastrophic forgetting (Figure 4A). At this point the network remembered the 190 191 most recent task (i.e. Task 2) but Task 1 was forgotten. Next, we implemented a training phase consisted of alternating periods of training on Task 1 (considered to be a new task here) lasting 192 100 movement cycles and periods of "sleep" of the same duration (we will refer to this training 193 phase as Interleaved_{S,T1}). To simulate sleep, the rewarded STDP rule was replaced by 194 unsupervised STDP, ensuring a truly offline learning period, and hidden layer neurons were 195 artificially stimulated by Poisson distributed spike trains in order to maintain spiking rates 196 197 similar to that during task training (indeed, in vivo, activity of the neocortical neurons during REM sleep is similar to awake³²; see *Methods: Simulated Sleep* for details). Importantly, no 198 training on Task 2 (old task here) was performed at any time during Interleaved_{S.T1}. Figure 4B 199 200 shows that following Interleaved_{S.T1} the network achieved a performance of 0.69 ± 0.02 on Task 1 and a performance of 0.67 ± 0.03 on Task 2, comparable to both single task performances 201

202following sequential training on Task 1 (0.70 ± 002) and Task 2 (0.69 ± 0.03) (Figure 1B/C) and203exceeding those achieved through Interleaved_{T1,T2} training (Figure 3B). When durations of Task2041 individual training episodes was increased significantly beyond 100 cycles during205Interleaved_{S,T1}, the network was only able to perform well on the new Task 1 while performance206on the old Task 2 dropped to the chance level (not shown).207We interpret these results as follows (see sections below for detailed synaptic208connectivity analysis). Each episode of new Task 1 training improves Task 1 performance but

209 damages synaptic connectivity responsible for old Task 2. If continuous Task 1 training is long

enough, the damage to Task 2 becomes irreversible. Having a sleep phase after a short period of

211 Task 1 training enables spontaneous forward (H->O) replay that preferentially benefits the

strongest synapses. Thus, if Task 2 synapses are still strong enough, they are replayed and

213 increase. To keep the protocol consistent with our previous experiments on Interleaved_{T1,T2}

training, we used a combination of sleep and Task 1 training – the same task that was initially

trained to naïve network but overwritten during Task 2 training (i.e., entire sequence of events

was T1 -> T2 -> Interleaved_{S,T1}). However, we obtained the same results in an experiment when,

217 after initial Task 1 training, Task 2 training was interleaved with sleep (i.e., T1 ->

Interleaved_{S,T2}), which prevented forgetting Task 1 while Task 2 was learned (see Extended Data
Figure 1).

We next traced "task-relevant" synapses, i.e. synapses identified in the top 10% distribution following training on that specific task (Figure 4C; compare to Figure 3C for Interleaved_{T1,T2} training). The structure in the distribution of Task 1-relevant synapses following Task 1 training (Figure 4C; top-left) was destroyed following Task 2 training (top-middle) but partially recovered following Interleaved_{S,T1} training (top-right). The structure in the distribution of Task 2-relevant synapses following Task 2 training (bottom-middle) was not present
following Task 1 training (bottom-left) and was partially retained following Interleaved_{S,T1}
training (bottom-right). Thus, sleep can preserve important synapses while incorporating new
ones.

Figure 4D shows that the SVM robustly classified the synaptic weight states from Task 1 229 230 and Task 2 while those from Interleaved_{S,T1} weight states fell significantly closer to the decision 231 boundary. This indicates that, similar to Interleaved T_{1,T_2} , the synaptic weight matrices which result from Interleaved_{S.T1} training are a mixture of Task 1 and Task 2 states. The trajectory of 232 the synaptic weights in PC space shown in Figure 4E provides a visualization of these dynamics. 233 234 Importantly, the smoothness of this trajectory to its steady state suggests that Task 2 information is never completely erased during this evolution. We take this as evidence that Interleaved_{S,T1} 235 236 training is capable of integrating synaptic information relevant to Task 1 while preserving Task 2 237 information.

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239 Receptive fields of decision-making neurons after sleep represent multiple tasks

To observe that the network has learned both tasks after Interleaved_{S,T1} training, we mapped the 240 receptive fields of decision-making neurons in layer O (Figure 5; see Figure 2 for comparison). 241 Figure 5A shows the receptive field for the neuron in layer O which controls movement in the 242 243 upper-left direction. This neuron responds to both horizontal (rewarded for Task 1) and vertical (rewarded for Task 2) orientations in the upper-left quadrant of the visual field. Although it 244 245 initially appears that this layer O neuron may also be responsive to diagonal patterns in this region, analysis of the receptive fields of neurons in layer H (Figure 5B) revealed that these 246 247 receptive fields are selective to either horizontal food particles (left; rewarded for Task 1) or

vertical food particles (right; rewarded for Task 2) in the upper-left quadrant of the visual field. 248 Other receptive fields were responsible for avoidance of punished particles for both tasks (see 249 250 examples in Figure 5B, bottom-middle-right and bottom-middle-left). Thus, the network will utilize one of two distinct sets of layer H neurons, selective for either Task 1 or Task 2, 251 depending on which food particles are present in the environment. 252 253 254 Periods of sleep allow reintegration of new task without interference through 255 renormalization of task-relevant synapses 256 To visualize synaptic weight dynamics during Interleaved_{S,T1} training, traces of all synapses 257 projecting to a single representative output layer neuron were plotted (figure 6A). At the onset of 258 Interleaved_{S,T1} training (i.e. 240,000 aeons), the network was only able to perform on Task 2, 259 meaning the strong synapses in the network were specific to this task. These synapses were 260 represented by a cluster ranging from ~ 0.08 to ~ 0.4 ; the rest of synapses grouped near 0. As Interleaved_{S,T1} training progressed, Task 1 specific synapses moved to the strong cluster and 261 262 some, presumably less important, Task 2 synapses moved to the weak cluster. After a period of 263 time the rate of transfer decreased and the total number of synapses in each group stabilized, 264 showing that the network is approaching equilibrium (Figure 6B). To visualize how sleep renormalizes task relevant synapses, we plotted two-dimensional 265

weight distributions for Task 1->Task2 (Figure 6C) and Task 2 -> Interleaved_{S,T1} (Figure 6D)
experiments (see *Methods: 2-D Synaptic Weight Distributions* for details). To establish a

baseline, in Figure 6C (left) the weight state at the end of Task 1 training (X-axis) (see overall

- timeline of this experiment in Figure 4A) was compared to itself (Y-axis). This formed a
- 270 perfectly diagonal plot. Most synapses were weak (red dots) with stronger synapses forming a

tail in the distribution. The next comparison (Figure 6C, middle) was between the weight state 271 after Task 1 training (X-axis) and a time early on Task 2 training (Y-axis). At that time, synapses 272 were only able to modify their strength slightly, causing most points to lie close to the diagonal. 273 As training on Task 2 continued until maximum performance was reached, synapses moved far 274 away from the diagonal (Figure 6C, right). Two trends were observed. A set of synapses that had 275 276 a strength near zero following Task 1 training increased strength following Task 2 training 277 (Figure 6D, right, red dots along Y-axis). At the same time, many strongly trained by Task 1 278 synapses were depressed down to zero (Figure 6C, right, red dots along X-axis). The latter 279 illustrates the effect of catastrophic forgetting - complete overwriting of the synaptic weight matrix caused performance of Task 1 to return to baseline after training on Task 2. 280

Does sleep prevent overwriting of the synaptic weight matrix? The Figure 6D plots use 281 the weight state at the end of training Task 2 as a reference that is compared to different times 282 283 during Interleaved_{S,T1} training. The first two plots (Figure 6D, left/middle) are similar to those in 284 Figure 6C. However, after Interleaved_{S,T1} training (Figure 6D, right) many synapses that were strong following Task 2 training were not depressed to zero but rather were pushed to an 285 intermediate strength where they are still functional (note cluster of points parallel to X-axis; see 286 287 also projection to 1D on the right side of the graph). Thus, Interleaved_{S,T1} training, combining 288 new training on Task 1 with periods of unsupervised sleep, moved synapses in a way that 289 preserved strong synapses from a previously learned task while also introducing new strong 290 synapses to perform a new task. Since a significant fraction of the strong synapses from training 291 on Task 2 were preserved (due to the sleep periods), performance on Task 2 remained high 292 following Interleaved_{S,T1} training despite the fact that the networks received no new training examples of Task 2. 293

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Periods of sleep push the network towards the intersection of the solution manifolds representing Task 1 and Task 2 specific weight configurations

To visualize the approximate task-specific solution manifolds (M_{T1} and M_{T2}) and their 297 intersection $(M_{T1\cap T2})$ in synaptic weight space, we used multiple trials (with different 298 initialization) of Task 1 and Task 2 training to sample the manifolds. Figure 7A shows (in kPCA 299 300 space) that multiple different configurations of synaptic weights can provide high performance for a given task. For example, all red dots in Figure 7A represent the states with the same high 301 302 level of performance for Task 1 (but not Task 2). In addition, cyan and green dots represent states with high level of performance for both Task 1 and Task2. We interpret these results as 303 304 evidence that synaptic weight space includes a manifold, M_{TI} , where different configurations of 305 weights (red, green, cyan dots) all allow for Task 1 to perform well. This manifold intersects 306 with another one, M_{T2} , where different weights configurations (blue, green, cyan dots) are all 307 suitable for Task 2. Figures 7B and 7C show 2D projections of this space onto PCs 1 and 2 and 308 PCs 1 and 3, respectively. From these projections, we can see that PC 1 seems to capture the 309 extent to which a synaptic weight configuration is associated with Task 1 (positive values) or 310 Task 2 (negative values), while PC 2 and PC 3 capture the variance in synaptic weight 311 configurations associated with Task 1 and Task 2, respectively. Note, the trajectories through this space (red/blue lines) during Interleaved_{T1,T2} and Interleaved_{S,T1/T2} training would also belong to 312 313 the respective task manifolds as performance on the old tasks was never lost in these training 314 scenarios.

315 We calculated the distance from the current synaptic weight configurations to M_{TI} 316 (Figure 7D), M_{T2} (Figure 7E), and $M_{TI\cap T2}$ (Figure 7F; see *Methods: Distance from Solution*

317 Man	<i>folds</i> for details). Figures 7D and 7E show that while Sequential (T1->T2 or T2->T1)

- training causes synaptic weight configurations to diverge quickly from its initial solution
- manifold (i.e. M_{T1} or M_{T2}), both Interleaved_{T1,T2} and Interleaved_{S,T1/T2} training cause synaptic
- weight configurations to stay close to the initial solution manifold as the new task was learned.
- 321 (Note, that we under sampled M_{T1} and M_{T2} , which explains initial distance increase.)
- 322 Importantly, Figure 7F shows that while both Interleaved_{T1,T2} and Interleaved_{S,T1/T2} training cause
- 323 synaptic weight configurations to smoothly converge towards $M_{TI \cap T2}$, Sequential training avoids
- this intersection entirely.

In Figure 7G we show a schematic depiction of these results. The task-specific manifolds, 325 326 M_{T1} and M_{T2} , are roughly defined in 3D projection by two orthogonal elliptic paraboloids with opposite orientation, with an approximately ellipsoidal intersection, $M_{TI \cap T2}$. Figures 7H and 7I 327 328 depict the trajectories the network takes in this space following Task 2 and Task 1 training, 329 respectively. Sequential training causes the network to jump directly from one task-specific 330 solution manifold to the other, resulting in catastrophic forgetting. In contrast, interleaving new task training with sleep (Interleaved_{S,T1/T2}) prevents catastrophic forgetting by keeping the 331 network close to the old task solution manifold as it converges towards $M_{TI\cap T2}$ – a region capable 332 a supporting both tasks simultaneously. 333

334

335 **Discussion**

In this study we report that a multi-layer SNN utilizing reinforcement learning may exhibit
catastrophic forgetting upon sequential training of two complementary complex foraging tasks,
but the problem is mitigated if the network is allowed, during new task training, to undergo

intervening periods of spontaneous reactivation which we consider to be equivalent to the replay 339 observed during periods of sleep in biological systems. This scenario was effectively equivalent 340 341 to explicit interleaved training of both tasks, however, no training data for the old task were required during "sleep". At the synaptic level, training a new task alone led to complete 342 overwriting of synaptic weights responsible for the previous task. In contrast, interleaving 343 344 periods of reinforcement learning on a new task with periods of unsupervised learning during sleep preserved old task synapses damaged by new task training to avoid forgetting and 345 346 enhanced new task synapses to allow new task learning. Thus, the network was pushed towards 347 the intersection of the solution manifolds representing synaptic weight configurations associated with each task - an optimal compromise for performing both tasks. 348

349 The critical role that sleep plays in learning and memory is supported by a vast, interdisciplinary literature spanning both psychology and neuroscience^{21,33-36}. Specifically, it has 350 351 been suggested that REM sleep supports the consolidation of non-declarative or procedural memories while non-REM sleep supports the consolidation of declarative memories^{21,35,37}. In 352 353 particular, REM sleep has been shown to be important for the consolidation of memories of tasks involving perceptual pattern separation, such as the texture discrimination task 21,38 . Despite the 354 difference in the cellular and network dynamics during these two stages of sleep^{21,35}, both are 355 356 thought to contribute to memory consolidation through repeated reactivation, or replay, of specific memory traces acquired during learning^{19-21,33,34,37,39}. These studies suggest that through 357 358 replay, sleep can support the process of off-line memory consolidation to circumvent the 359 problem of catastrophic forgetting.

From mechanistic perspective, the sleep phase in our model protects old memories byenabling unsupervised learning - spontaneous replay of synapses responsible for previously

learned tasks. We previously reported that in the thalamocortical models, a sleep phase may 362 enable replay of spike sequences learned in awake to improve post-sleep performance^{39,40} and to 363 protect old memories from catastrophic forgetting⁴¹. Although in this work we model sleep and 364 noise with spiking statistics similar to awake training, theoretical work from another group has 365 also shown that noise causes implicit rehearsal of older memories which protects against 366 interference⁴². Here we found, however, that a single episode of new task training using 367 368 reinforcement learning could quickly erase an old memory to the point that it cannot be 369 recovered by subsequent sleep. The solution was similar to how brain slowly learns procedural (hippocampal-independent) memories^{21,35,37,38,43}. Each episode of new task training improves this 370 task performance only slightly but also damages slightly synaptic connectivity responsible for 371 the older task. Subsequent sleep phases enable replay that preferentially benefits the strongest 372 synapses, such as those from old memory traces, to allow them to recover. 373

374 We found that multiple distinct configurations of synaptic weights can support each task 375 in our model, suggesting the existence of task specific solution manifolds in synaptic weight space. Sequential training of new tasks makes the network to jump from one solution manifold to 376 another, enabling memory for the most recent task but erasing memories of the previous tasks. 377 378 Interleaving new task training with sleep phases enables the system to evolve towards 379 intersection of these manifolds where synaptic weight configurations can support multiple tasks 380 (a similar idea was recently proposed in the machine learning literature to minimize catastrophic interference by learning representations that accelerate future learning⁴⁴). From this point of view 381 382 having multiple episodes of new task training interleaved with multiple sleep episodes allows 383 gradual convergence to the intersection of the manifolds representing old and new tasks, while a

single long episode of new task learning would push the network far away from the old taskmanifold making it impossible to recover by subsequent sleep.

Although classical interleaved training showed similar performance results in our model 386 as interleaving training with sleep, we believe the latter to be superior on the following 387 theoretical grounds. Classical interleaved training will necessarily cause the system to oscillate 388 about the optimal location in synaptic weight space which can support both tasks because each 389 390 training cycle uses a cost function specific to only a single task. While this can be ameliorated 391 with a learning rate decay schedule, the system is never actually optimizing for the desired dual-392 task state. Sleep, on the other hand, can support not only replays of the old task, but also support replays which are a mixture of both tasks^{42,45,46}. Thus, through unsupervised learning during 393 sleep replay, the system is able to perform approximate optimization for the desired dual-task 394 395 state.

396 While our model represents a dramatic simplification of any biological system, we 397 believe that it captures some important processing steps of how animal and human brains interact 398 with the external world. The primary visual system is believed to employ a sequence of 399 processing steps when visual information is increasingly represented by neurons encoding higher level features²⁸⁻³⁰. This processing step was reduced to very simple convolution from input to 400 hidden layer in our model. Subsequently, in the brain, associative areas and motor cortex are 401 trained to make decisions based on reward signals released by neuromodulatory centers^{8,47-49}. 402 403 This was reduced in our model to synaptic projections from the hidden to output (decision making) layer implementing rewarded STDP to learn a task²⁴⁻²⁶. 404

Our results are in line with a large body of literature suggesting that interleaved training
is capable of mitigating catastrophic forgetting in ANNs^{4,8,9} and SNNs^{10,11}. The novel

contribution from this study is that the data intensive process of interleaved training can be 407 avoided in SNNs by inserting periods of noise-induced spontaneous reactivation - unsupervised 408 learning – during new task training; similar to how brains undergo offline consolidation periods 409 during sleep resulting in reduced retroactive interference to previously learned tasks^{21,43}. In fact, 410 our results are in line with previous work done in humans showing that perceptual learning tasks 411 412 are subject to retroactive interference by competing memories without an intervening period of REM sleep^{37,38}. Moreover, performance on visual discrimination tasks in particular have been 413 shown to steadily improve over successive nights of sleep³⁸, consistent with our findings that 414 415 interleaving multiple periods of sleep with novel task learning leads to optimal performance on each task. 416

Our study predicts synaptic level mechanisms of how sleep-based memory reactivation can protect old memory traces during training of a new interfering memory task. It suggests the apparent loss of recall performance for older tasks in ANNs and SNNs after new training does not necessarily imply a complete erasure of the old task, but instead indicates that the old tasks decision states became unreachable by the associated inputs. Sleep can reverse the damage to synaptic connectivity by replaying the old memory traces without explicit usage of the old training data.

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425 Methods

Environment. Foraging behavior took place in a virtual environment consisting of a 50x50 grid
with randomly distributed "food" particles. Each particle was two pixels in length and could be
classified into one of four types depending on its orientation: vertical, horizontal, positively

sloped diagonal, or negatively sloped diagonal. During the initial unsupervised training period, 429 the particles are distributed at random with the constraints that each of the four types are equally 430 431 represented and no two particles can be directly adjacent. During training and testing periods only the task-relevant particles were present. When a particle was acquired as a result of the 432 virtual agent moving, it was removed from its current location (simulating consumption) and 433 434 randomly assigned to a new location on the grid, again with the constraint that it not be directly adjacent to another particle. This ensures a continuously changing environment with a constant 435 436 particle density. The density of particles in the environment was set to 10%. The virtual agent 437 can see a 7x7 grid of squares (the "visual field") centered on its current location and it could move to any adjacent square, including diagonally, for a total of eight directions. 438

439

440 Network structure. The network was composed of 842 spiking map-based neurons (see *Methods: Map-based neuron model* below) ^{50,51}, arranged into three feed-forward layers to 441 442 mimic a basic biological circuit: a 7x7 input layer (I), a 28x28 hidden layer (H), and a 3x3 output layer (O) with a nonfunctional center neuron (Fig 1). Input to the network was simulated as a set 443 444 of suprathreshold inputs to the neurons in layer I, equivalent to the lower levels of the visual 445 system, which represent the position of particles in an egocentric reference frame relative to the virtual agent (positioned in the center of the 7x7 visual field). The most active neuron in layer O, 446 playing the role of biological motor cortex, determined the direction of the subsequent 447 448 movement. Each neuron in layer H, which can be loosely defined as higher levels of the visual system or associative cortex, received excitatory synapses from 9 randomly selected neurons in 449 450 layer I. These connections initially had random strengths drawn from a normal distribution. Each neuron in layer H connected to every neuron in layer O with both an excitatory (W_{ij}) and an 451

452 inhibitory (WI_{ij}) synapse. This provided an all-to-all connectivity pattern between these two 453 layers and accomplished a balanced feed-forward inhibition ⁵² found in many biological 454 structures ⁵²⁻⁵⁷. Initially, all these connections had uniform strengths and the responses in layer O 455 were due to the random synaptic variability. Random variability was a property of all synaptic 456 interactions between neurons and was implemented as variability in the magnitude of the 457 individual synaptic events.

458

Policy. Simulation time was divided up into epochs of 600 timesteps, each roughly equivalent to 300 ms. At the start of each epoch the virtual agent received input corresponding to locations of nearby particles within the 7x7 "visual field". Thus 48 of the 49 neurons in layer I received input from a unique location relative to the virtual agent. At the end of the epoch the virtual agent made a single move based on the activity in layer O. If the virtual agent moved to a grid location with a "food" particle present, the particle was removed and assigned to a randomly selected new location.

Each epoch was of sufficient duration for the network to receive inputs, propagate activity forward, produce outputs, and return to a resting state. Neurons in layer I which represent locations in the visual field containing particles received a brief pulse of excitatory stimulation sufficient to trigger a spike; this stimulation was applied at the start of each movement cycle (epoch). At the end of each epoch the virtual agent moved according to the activity which has occurred in layer O.

The activity in layer O controlled the direction of the virtual agent's movement. Each of the neurons in layer O mapped onto a specific direction (i.e. one of the eight adjacent locations or the current location). The neuron in layer O which spiked the greatest number of times during

the first half of the epoch defined the direction of movement for that epoch. If there was a tie, the 475 direction was chosen at random from the set of tied directions. If no neurons in layer O spiked, 476 the virtual agent continued in the direction it had moved during the previous epoch. 477 There was a 1% chance on every move that the virtual agent would ignore the activity in 478 layer O and instead move in a random direction. Moreover, for every movement cycle that 479 passed without the virtual agent acquiring a particle, this probability was increased by 1%. The 480 random variability promoted exploration vs exploitation dynamics and essentially prevented the 481 virtual agent from getting stuck in movement patterns corresponding to infinite loops. While 482 biological systems could utilize various different mechanisms to achieve the same goal, the 483 484 method we implemented was efficient and effective for the scope of our study.

485

486 Neuron models. For all neurons we used spiking model identical to the model used in ^{12,13} that
487 can be described by the following set of difference equations ^{51,58,59}:

488
$$V_{n+1} = f_{\alpha}(V_n, I_n + \beta_n),$$

489
$$I_{n+1} = I_n - \mu(V_n + 1) + \mu \sigma + \mu \sigma_n,$$

490 where V_n is the membrane potential, I_n is a slow dynamical variable describing the effects of 491 slow conductances, and *n* is a discrete time-step (0.5 ms). Slow temporal evolution of I_n was 492 achieved by using small values of the parameter $\mu \ll 1$. Input variables β_n and σ_n were used to 493 incorporate external current I_n^{ext} (e.g. background synaptic input): $\beta_n = \beta^e I_n^{ext}$, $\sigma_n = \sigma^e I_n^{ext}$. 494 Parameter values were set to $\sigma = 0.06$, $\beta^e = 0.133$, $\sigma^e = 1$, and $\mu = 0.0005$. The nonlinearity $f_a(V_n, \sigma_n)$

495 I_n) was defined in the form of the piece-wise continuous function:

496
$$f_{\alpha}(V_n, I_n) = \begin{cases} \alpha (1 - V_n)^{-1} + I_n, & V_n \le 0\\ \alpha + I_n, & 0 < V_n < \alpha + I_n \& V_{n-1} \le 0\\ -1 & \alpha + I_n \le V_n \text{ or } V_{n-1} > 0, \end{cases}$$

497 where $\alpha = 3.65$.

This model is very computationally efficient, and, despite its intrinsic low dimensionality, produces a rich repertoire of dynamics capable of mimicking the dynamics of Hodgkin-Huxley type neurons both at the single neuron level and in the context of network dynamics ^{51,58,60}.

501 To model the synaptic interactions, we used the following piece-wise difference equation:

502
$$I_{n+1}^{syn} = \gamma I_n^{syn} + \begin{cases} (1-R+2XR)g_{syn}/W_j, & spike_{pre} \\ 0, & \text{otherwise} \end{cases}$$

503 Here g_{syn} is the strength of the synaptic coupling, modulated by the target rate W_i of receiving 504 neuron *j*. Indices *pre* and *post* stand for the pre- and post-synaptic variables, respectively. The first condition, *spike*_{pre}, is satisfied when the pre-synaptic spikes are generated. Parameter γ 505 506 controls the relaxation rate of synaptic current after a presynaptic spike is received ($0 \le \gamma < 1$). 507 The parameter R is the coefficient of variability in synaptic release. The standard value of R is 508 0.12. X is a random variable sampled from a uniform distribution with range [-1, 1]. Parameter 509 V_{rp} defines the reversal potential and, therefore, the type of synapse (i.e. excitatory or inhibitory). 510 The term (1-R+2XR) introduces a variability in synaptic release such that the effect of any 511 synaptic interaction has an amplitude that is pulled from a uniform distribution with range [1-R, 1+R] multiplied by the average value of the synapse. 512

513

Synaptic plasticity. Synaptic plasticity closely followed the rules introduced in ^{12,13}. A rewarded
 STDP rule ²⁴⁻²⁷ was operated on synapses between layers H and O while a standard STDP rule

operated on synapses between layers I and H. A spike in a post-synaptic neuron that directly

517 followed a spike in a pre-synaptic neuron created a *pre before post* event while the converse

518 created a *post before pre* event. Each new post-synaptic (pre-synaptic) spike was compared to all

519 pre-synaptic (post-synaptic) spikes with a time window of 120 iterations.

520 The value of an STDP event (trace) was calculated using the following equation 22,23:

$$p = \frac{-|t_r - t_p|}{T_c},$$

522
$$tr_k = Ke^p$$

523 where t_r and t_p are the times at which the pre- and post-synaptic spike events occurred

respectively, T_c is the time constant and is set to 40 ms, and K is maximum value of the trace tr_k

and is set to -0.04 for a *post before pre* event and 0.04 for a *pre before post* event.

A trace was immediately applied to synapse between neurons in layers I and H. However, for synapses between neurons in layers H and O the traces were stored for 6 epochs after its creation before being erased. During storage, a trace had an effect whenever there was a rewarding or punishing event. In such a case, the synaptic weights are updated as follows:

530
$$W_{ij} \leftarrow W_{ij} \prod_{k=1}^{traces} \left(1 + \frac{W_{i0}}{W_i} * \Delta_k\right),$$

531
$$\Delta_k = S_{rp} \left(\frac{tr_k}{t - t_k + c} \right) \frac{Sum_{tr}}{Avg_{tr}}$$

532
$$Sum_{tr} = \sum_{k}^{traces} \frac{tr_k}{t - t_k + c}$$

533
$$Avg_{tr} \leftarrow (1 - \delta)Avg_{tr} + \delta Sum_{tr}$$

where *t* is the current timestep, S_{rp} is a scaling factor for reward/punishment, tr_k is the magnitude of the trace, t_k is the time of the trace event, *c* is a constant (=1 epoch) used for decreasing sensitivity to very recent spikes, $W_i = \sum_j W_{ij}$ is the total synaptic strength of all connections from the neuron *i* in layer H to all neurons in layer O, W_{i0} is a constant that is set to the initial value (*target value*) of W_i at the beginning of the simulation. The term W_{i0}/W_i helped to keep the output weight sum close to the initial target value. The effect of these rules was that neurons with lower total output strength could increase their output strength more easily.

The network was rewarded when the virtual agent moved to a location which contained a particle from a "food" pattern (horizontal in Task 1, vertical in Task 2) and $S_{rp} = 1$, and received a punishment of $S_{rp} = -0.001$ when it moved to a location with a particle from a neutral pattern (negative/positive diagonal in Task 1/2). A small punishment of $S_{rp} = -0.0001$ was applied if the agent moved to a location without a particle present to help the virtual agent learn to acquire "food" as rapidly as possible. During periods of sleep the network received a constant reward of $S_{rp} = 0.5$ on each movement cycle.

To ensure that neurons in layer O maintained a relatively constant long-term firing rate, the model incorporated homeostatic synaptic scaling which was applied every epoch. Each timestep, the total strength of synaptic inputs $W_j = \sum_i W_{ij}$ to a given neuron in layer O was set equal to the target synaptic input W_{j0} – a slow variable which varied over many epochs depending on the activity of the given neuron in layer O – which was updated according to:

553
$$W_{j0} \leftarrow \begin{cases} W_{j0}(1+D_{tar}) & \text{spike rate < target rate} \\ W_{j0}(1-D_{tar}) & \text{spike rate > target rate} \end{cases}$$

To ensure that the net synaptic input W_j to any neuron was unaffected by plasticity events at the individual synapses at distinct timesteps and equal to W_{j0} , we implemented a scaling

556 process akin to heterosynaptic plasticity which occurs after each STDP event. When any

557 excitatory synapse of neuron in layer O changed in strength, all other excitatory synapses

received by that neuron were updated according to:

559
$$W_{ij} \leftarrow W_{ij} \frac{W_{j0}}{\sum_i W_{ij}}$$

560

Simulated Sleep. To simulate the sleep phase, we inactive the sensory receptors (i.e. the input layer of network), cut off all sensory signals (i.e. remove all particles from the environment), and decouple output layer activity from motor control (i.e. the output layer can spike but no longer causes the agent to move). We also change the learning rule between the hidden and output layer from rewarded to unsupervised STDP (see *Methods: Synaptic Plasticity* for details) as there is no way to evaluate decision-making without sensory input or motor output.

To simulate the spontaneous activity observed during REM sleep, we provided noise to 567 each neuron in the hidden layer in a way which ensured that the spiking statistics of each neuron 568 569 was conserved across awake and sleep phases. To determine these spiking rates, we recorded 570 average spiking rates of neurons in the hidden layer H during preceding training of both Task 1 and Task 2; these task specific spiking rates were then averaged to generate target spiking rates 571 572 for hidden layer neurons. Interleaved_{S,T1} training consisted of alternating intervals of this sleep 573 phase and training on Task 1, with each interval lasting 100 movement cycles (although no 574 movement occurred).

575

576 Support Vector Machine Training. A support vector machine with a radial basis function
577 kernel was trained to classify synaptic weight configurations as being related to Task 1 or Task

2. Labeled training data were obtained by taking the excitatory synaptic weight matrices between 578 the hidden and output layers from the last fifth of the Task 1 and Task 2 training phases (i.e. after 579 performance had appeared to asymptote). These synaptic weight matrices were then flattened 580 into column vectors, and the column vectors were concatenated to form a training data matrix of 581 size number of features x number of samples. The number of features was equal to the total 582 583 number of excitatory synapses between the hidden and output layer -6272 dimensions. We then used this support vector machine to classify held out synaptic weight configurations from Task 1 584 585 and Task 2 training, as well as ones which resulted from Interleaved_{T1,T2} and Interleaved_{S,T1} training. 586

587

588 **2-D Synaptic Weight distributions (Figure 6).** First for each synapse we found how its 589 synaptic strength changes between two slices in time, where the given synapse's strength at time 590 slice 1 is the point's X-value and strength at time slice 2 is its Y-value. Then we binned this 591 space and counted synapses in each bin to make two dimensional histograms where blue color 592 corresponds to a single synapse found in a bin and brown corresponds to the max of 50 synapses. 593 These two-dimensional histograms assist in visualizing the movement of all synapses between 594 the two slices in time that are specified by the timelines at the top of each plot. Conceptually, it is important to note that if a synapse does not change in strength between time slice 1 and time 595 slice 2, then point the synapse corresponds to in this space will lie on the diagonal of the plot 596 597 since the X-value will match the Y-value. If a great change in the synapse's strength has occurred between time slice 1 and time slice 2, then the synapse's corresponding point will lie 598 599 far from the diagonal since the X-value will be distant from the Y-value. The points on the X-

600 (Y-) axis represent synapses that lost (gained) all synaptic strength between time slice 1 and time601 slice 2.

602

Distance from Solution Manifolds (Figure 7). Each of the two solution manifolds (i.e. Task 1 603 and Task 2 specific manifolds) were defined by the point-sets in synaptic weight space which 604 were capable of supporting robust performance on that particular task, namely the sets M_{TI} and 605 606 M_{T2} . This included the synaptic weight states from the last fifth of training on a particular task 607 (i.e. after performance on that task appeared to asymptote) and all of the synaptic weight states 608 from the last fifth of both Interleaved_{T1,T2} and Interleaved_{S,T1/T2} training. The intersection of the two solution manifolds (i.e. the point-set $M_{TI \cap T2}$) was defined solely by the synaptic weight states 609 610 from the last fifth of both Interleaved_{T1,T2} and Interleaved_{S,T1} training. As the network evolved 611 along its trajectory in synaptic weight space, the distance from the current point in synaptic 612 weight space, p_t , to the two solution manifolds and their intersection were computed as follows:

613
$$d^n(p_t, M_\tau) = \min_{x \in M} \left(d^n(p_t, x) \right)$$

Here, d^n is the n-dimensional Euclidean-distance function, where *n* is the dimensionality of synaptic weight space (i.e. n = 6272 here), M_τ is the point-set specific to the manifold or intersection in question (i.e. either M_{T1} , M_{T2} , or $M_{T1\cap T2}$), and *x* is a particular element of the point-set *M*.

618

Acknowledgements: This study was supported by Lifelong Learning Machines program from
DARPA/MTO (HR0011-18-2-0021) and ONR MURI (N000141612829)

621	Author Contribu	tions: J.E.D. carried	out experiments;	J.E.D conducted	l computational
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- analyses; R.G. designed experiments; R.G. and J.E.D. designed analysis approaches; R.G.,
- J.E.D., P.S., and M.B. interpreted data; R.G., P.S., and M.B. conceived the project; R.G. and
- 624 M.B. wrote the majority of the paper. All authors commented on and contributed to the paper.
- 625 **Conflicts of Interest:** None.

626

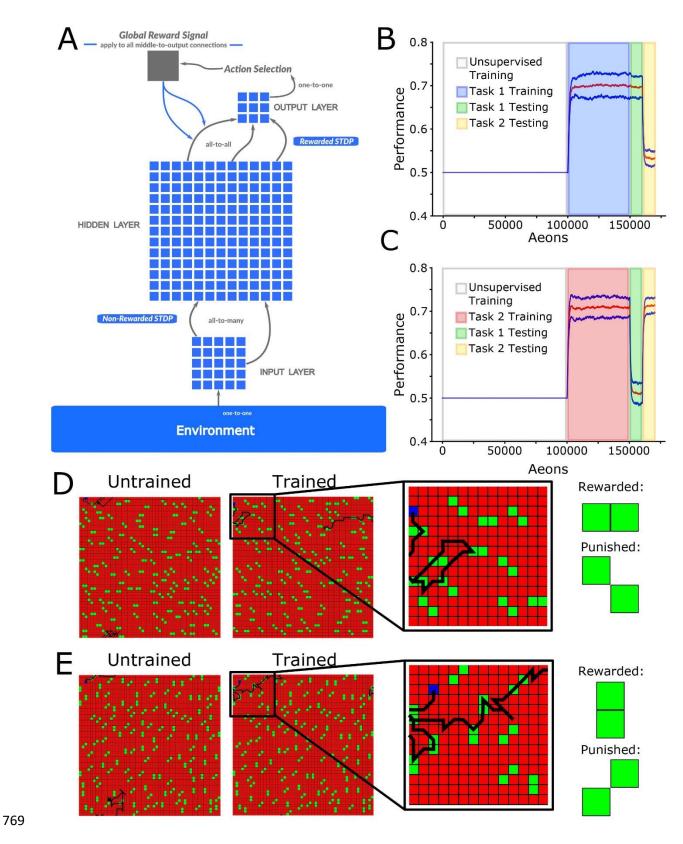
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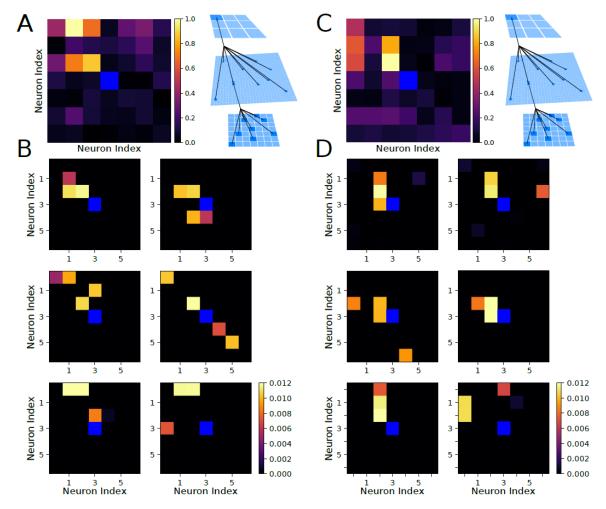
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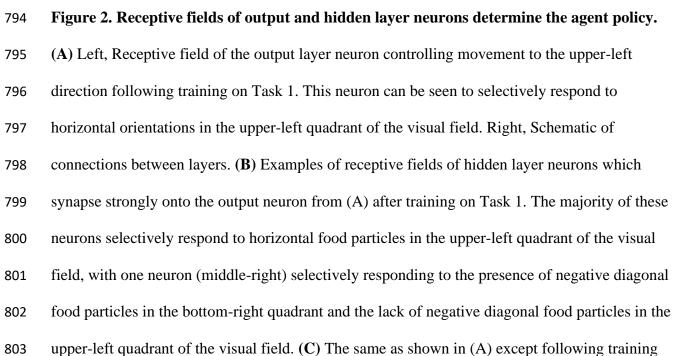
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770 Figure 1. Network architecture and complementary foraging task structure. (A) The

771 network had three layers of neurons with a feed-forward connectivity scheme. Input from the "visual field" (7x7 subspace of 50x50 virtual environment) was simulated as a set of excitatory 772 773 inputs to the input layer neurons representing the position of food particles in an egocentric reference frame relative to the virtual agent. Each hidden layer neuron received an excitatory 774 synapse from 9 randomly selected input layer neurons. Excitatory synapses between input and 775 776 hidden layer neurons were subject to unsupervised STDP, while those between hidden and 777 output layer neurons were subject to rewarded STDP. Each output layer neuron received one 778 excitatory and one inhibitory synapse from each hidden layer neuron. The most active neuron in 779 the output layer (size 3x3) determined the direction of movement. (B) Mean performance (red line) and standard deviation (blue lines) over time: 100,000 aeons (1 aeon = 100 movement 780 781 cycles) of unsupervised training (white), 50,000 aeons of Task 1 training (blue), and 10,000 782 aeons of Task 1 (green) and Task 2 (yellow) testing. The y-axis represents the agent's 783 performance, or the probability of acquiring rewarded as opposed to punished particle patterns. 784 The x-axis is time in aeons. Mean performance during testing on Task 1 was 0.70 ± 0.02 while Task 2 was 0.53 ± 0.02 . (C) The same as shown in (B) except now for: 10,000 aeons of 785 unsupervised training (white), 5000 aeons of Task 2 training (red), and 1,000 aeons of Task 1 786 787 (green) and Task 2 (yellow) testing. Mean performance during testing on Task 1 was 0.51 ± 0.02 while Task 2 was 0.71 ± 0.02 . (D) Examples of trajectories through the environment at the 788 789 beginning (left) and at the end (middle-left) of training on Task 1, with a zoom in on the 790 trajectory at the end of training (middle-right), and the values of the task-relevant food particles 791 (right). (E). The same as shown in (D) except now for Task 2.





804	on Task 2. The upper-left decision neuron can be seen to selectively respond to vertical
805	orientations in the upper-left quadrant of the visual field. (D) The same as shown in (B) except
806	following training on Task 2. All of these neurons selectively respond to vertical food particles in
807	the upper-left quadrant of the visual field.
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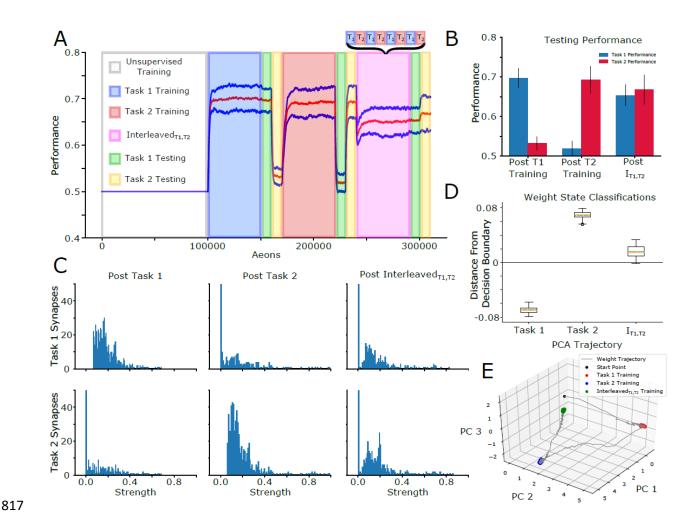
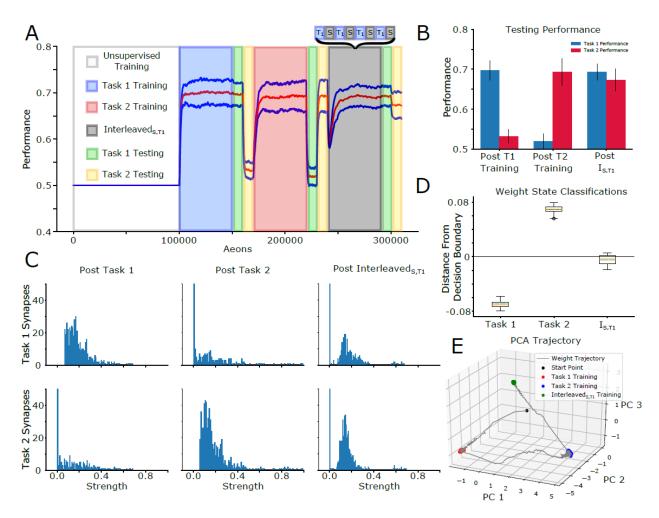


Figure 3. Sequential training on complementary tasks induces catastrophic forgetting 818 which can be rescued by interleaved training. (A) Mean performance (red line) and standard 819 820 deviation (blue lines) over time: 100,000 aeons of unsupervised training (white), 50,000 aeons of 821 Task 1 training (blue), 10,000 aeons of Task 1 (green) and Task 2 (yellow) testing, 50,000 aeons of Task 2 training (red), 10,000 aeons of Task 1 (green) and Task 2 (yellow) testing, 50,000 822 823 aeons of Interleaved_{T1,T2} training (purple), 10,000 aeons of Task 1 (green) and Task 2 (yellow) testing. (B) Mean and standard deviation of performance during testing on Task 1 (blue) and 824 Task 2 (red) after each training period. Following Task 1 training, mean performance on Task 1 825 826 was 0.69 ± 0.02 while Task 2 was 0.53 ± 0.02 . Conversely, following Task 2 training, mean 827 performance on Task 1 was 0.52 ± 0.02 while Task 2 was 0.69 ± 0.04 . Following Interleaved_{T1,T2}

828	training, mean performance on Task 1 was 0.65 ± 0.03 while Task 2 was 0.67 ± 0.04 . (C)
829	Distributions of task-relevant synaptic weights. The distributional structure of Task 1-relevant
830	synapses following Task 1 training (top-left) is destroyed following Task 2 training (top-middle),
831	but partially recovered following Interleaved $_{T1,T2}$ training (top-right). Similarly, the distributional
832	structure of Task 2-relevant synapses following Task 2 training (bottom-middle), which was not
833	present following Task 1 training (bottom-left), was partially preserved following
834	Interleaved _{T1,T2} training (bottom-right). (D) Box plots with mean (dashed green line) and median
835	(dashed orange line) of the distance to the decision boundary found by an SVM trained to
836	classify Task 1 and Task 2 synaptic weight matrices for Task 1, Task 2, and Interleaved $_{T1,T2}$
837	training across trials. Task 1 and Task 2 synaptic weight matrices had mean classification values
838	of -0.069 and 0.069 respectively, while that of Interleaved _{T1,T2} training was 0.016. (E) Trajectory
839	of H to O layer synaptic weights through PC space. Synaptic weights which evolved during
840	Interleaved _{T1,T2} training (green dots) clustered in a location of PC space intermediary between
841	the clusters of synaptic weights which evolved during training on Task 1 (red dots) and Task 2
842	(blue dots).

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845 Figure 4. Periods of sleep interleaved with training on a new task can prevent catastrophic forgetting. (A) Task paradigm similar to that shown in (3A) but with 50,000 aeons of 846 Interleaved_{S,T1} training (gray) instead of Interleaved_{T1,T2} training. Note that performance for Task 847 848 2 remains high despite no Task 2 training during this period. (B) Mean and standard deviation of performance during testing on Task 1 (blue) and Task 2 (red) after each training period. 849 Following Task 1 training, mean performance on Task 1 was 0.70 ± 0.02 while Task 2 was 0.53 850 \pm 0.02. Conversely, following Task 2 training, mean performance on Task 1 was 0.52 \pm 0.02 851 while Task 2 was 0.69 ± 0.04 . Following Interleaved_{S,T1} training, mean performance on Task 1 852 was 0.69 ± 0.02 while Task 2 was 0.67 ± 0.03 . (C) Distributions of task-relevant synaptic 853 weights. The distributional structure of Task 1-relevant synapses following Task 1 training (top-854

855 left) is destroyed following Task 2 training (top-middle), but partially recovered following Interleaved_{S.T1} training (top-right). Similarly, the distributional structure of Task 2-relevant 856 synapses following Task 2 training (bottom-middle), which was not present following Task 1 857 training (bottom-left), was partially preserved following Interleaved_{S,T1} training (bottom-right). 858 Task-relevant synapses were considered to be those which had a synaptic weight of at least 0.1 859 860 following training on that task. (B) Box plots with mean (dashed green line) and median (dashed orange line) of the distance to the decision boundary found by an SVM trained to classify Task 1 861 862 and Task 2 synaptic weight matrices for Task 1, Task 2, and Interleaved_{S,T1} training across trials. 863 Task 1 and Task 2 synaptic weight matrices had mean classification values of -0.069 and 0.069 respectively, while that of Interleaved_{S.T1} training was -0.0047. (C) Trajectory of H to O layer 864 synaptic weights through PC space. Synaptic weights which evolved during Interleaved_{S,T1} 865 866 training (green dots) clustered in a location of PC space intermediary between the clusters of synaptic weights which evolved during training on Task 1 (red dots) and Task 2 (blue dots). 867

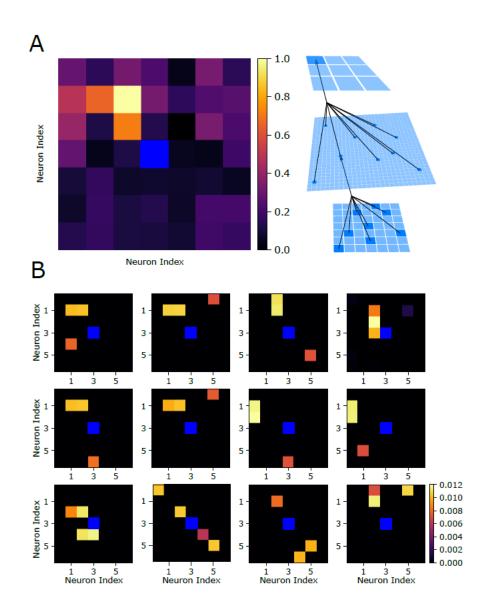


Figure 5. Receptive fields following interleaved Sleep and Task 1 training reveal how the network can multiplex the complementary tasks. (A) Left, Receptive field of the output layer neuron controlling movement to the upper-left direction following interleaved sleep and Task 1 training. This neuron has a complex receptive field capable of responding to horizontal and vertical orientations in the upper-left quadrant of the visual field. Right, Schematic of the connectivity between layers. (B) Examples of receptive fields of hidden layer neurons which synapse strongly onto the output neuron from (A) after interleaved Sleep and Task 1 training.

877	The majority of these neurons selectively respond to horizontal food particles (left half) or
878	vertical food particles (right half) in the upper-left quadrant of the visual field, promoting
879	movement in that direction and acquisition of the rewarded patters. A few neurons (bottom-
880	middle-left/right) can be seen to selectively respond to the presence of positive/negative diagonal
881	food particles in the bottom-right quadrant of the visual field. Activation of these neurons will
882	promote avoidance movement to the upper-left direction away from the punished patterns.
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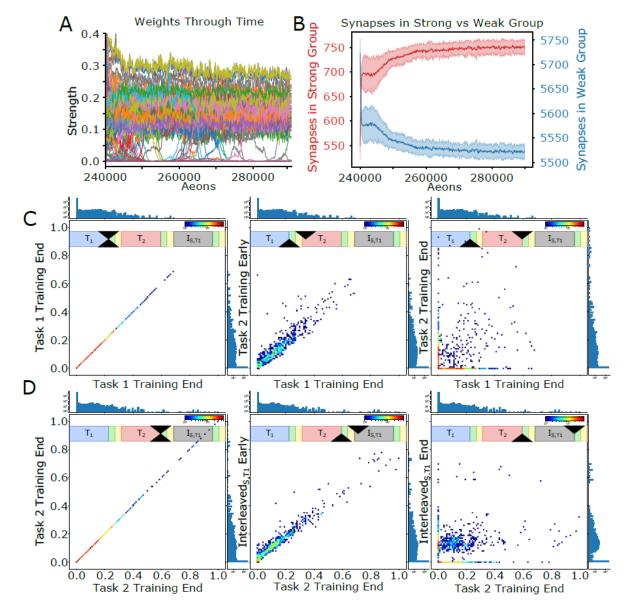


Figure 6. Periods of sleep allow learning Task 1 without interference with old Task 2
through renormalization of task-relevant synapses. (A) Dynamics of all incoming synapses to
a single output layer neuron during Interleaved_{S,T1} training shows the synapses separate into two
clusters.(B) Number of synapses in the strong (red) and weak (blue) clusters during
Interleaved_{S,T1}. (C) Two-dimensional histograms illustrating synaptic weights dynamics. For
each plot, the x-axis represents synaptic weight after Task 1 training and the y-axis represents the
synaptic weight at a different point in time(Scale bar: brown - 50 synapses/bin, blue - 1

895	synapse/bin. One-dimensional projections along top and right sides show the global distribution
896	of synapses at the time slices for a given plot. If no training occurred between the time slices, a
897	diagonal plot depicts that synaptic weights have not changed (left). After a small amount of Task
898	2 training, all points lie near the diagonal (middle) indicating minimal changes to synaptic
899	weights. Once Task 2 is fully trained (right), many synapses move far away from their original
900	values. In particular, a red cluster along the x-axis indicates synapses which were strong after
901	Task 1 training but were erased after Task 2 training. (D) Same as (C) except the x-axis refers to
902	the end of Task 2 training. Again, a diagonal plot is attained when no training takes place
903	between the time slices (left), and points lie near the diagonal when only a small amount of
904	Interleaved _{S,T1} training occurs (middle). After a full period of Interleaved _{S,T1} training (right),
905	weak synapses were recruited to support Task 1 (red cluster along the y-axis) and many Task 2
906	specific synapses remained moderately strong (blue cluster along x-axis).
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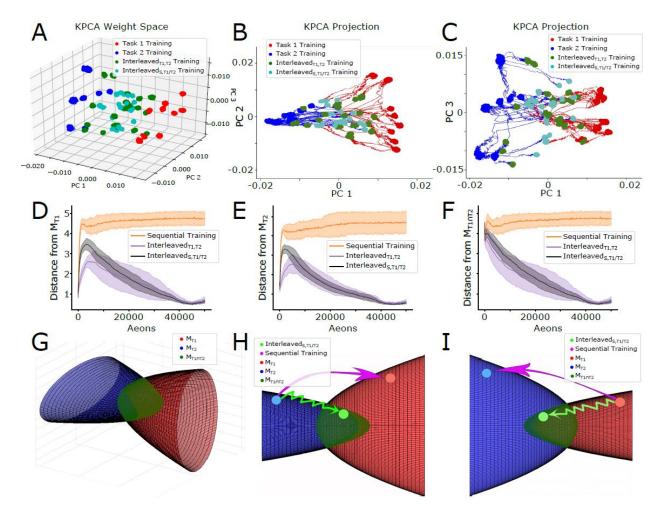
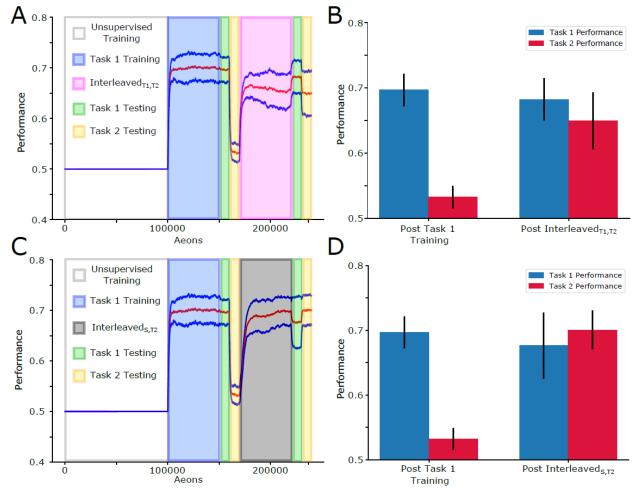
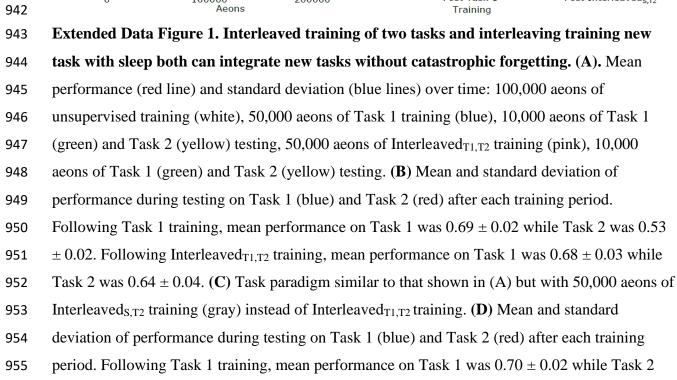


Figure 7. Periods of sleep push the network towards the intersection of Task 1 and Task 2 911 specific solution manifolds. (A-C) Low-dimensional visualizations of the synaptic weight 912 configurations of 10 networks obtained through kPCA for 3-dimensions (A), 2-dimensions using 913 PC 1 and PC 3 (B), and 2-dimensions using PC 1 and PC 3 (C). Synaptic weight configurations 914 taken from the last fifth of Task 1 (red dots), Task 2 (blue dots), Interleaved_{T1,T2} (green dots), and 915 Interleaved_{S,T1/T2} (cyan dots) training are shown. PC 1 characterizes good performance on Task 1 916 917 (positively valued) or Task 2 (negatively valued) training. PC 2 (PC 3) characterizes the variability in Task 1 (Task 2) training. Trajectories resulting from Interleaved_{T1,T2} and 918 Interleaved_{S.T1/T2} training following Task 1 (Task 2) training are shown in red (blue). (**D-F**) 919 920 Average (solid lines) and standard deviation (shaded regions) of the n-dimensional Euclidean

921	distances between the current synaptic weight configuration and M_{TI} (D), M_{T2} (E), and $M_{TI\cap T2}$
922	(F) during Sequential (orange), Interleaved _{T1,T2} (purple), and Interleaved _{S,T1/T2} (black) training.
923	Following Task 2 (D) or Task 1 (E) training, Sequential training on the opposite task causes the
924	synaptic weight configuration to diverge from the initial solution manifold, while Interleaved $T_{1,T2}$
925	and Interleaved _{S,T1/T2} training do not. (F) Interleaved _{T1,T2} and Interleaved _{S,T1/T2} training cause the
926	synaptic weight configuration to converge to $M_{T1 \cap T2}$ while Sequential training avoids this
927	intersection. (G) Authors' interpretation of the task-specific point-sets shown in (A-C) as
928	solution manifolds M_{T1} (red) and M_{T2} (blue). M_{T1} and M_{T2} can be thought of as two oppositely
929	oriented elliptic paraboloids which intersect orthogonally near the origin ($M_{TI \cap T2}$; dark green).
930	(H,I) Sequential training (pink arrow) causes the network to jump from one solution manifold to
931	the other while avoiding $M_{TI \cap T2}$, while Interleaved _{S,T1/T2} training (light green arrow) keep the
932	network close to the initial solution manifold as it converges towards $M_{TI \cap T2}$.
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- 956 was 0.53 ± 0.02 . Following Interleaved_{S,T2} training, mean performance on Task 1 was $0.68 \pm$
- 957 0.05 while Task 2 was 0.70 ± 0.03 .