Auditory brainstem models: K_{V1} ion-channels and depleting end-bulb synapses improve spatial encoding in reverberation

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Abstract

Listeners perceive sound-energy as originating from the direction of its source, even as the direct sound is followed only milliseconds later by reflected sound from multiple different directions. Auditory neural adaptation, before spatial information is binaurally encoded in the brainstem, is suggested as a contributing mechanism, yet the form of sufficient adaptive mechanisms remains unspecified. Though a strong preference for spatial information conveyed in early-arriving sound is observed behaviourally and neurophysiologically, investigation by simultaneously recording from binaural brainstem neurons and their monaural input neurons while controlling adaptation is yet unrealised. Therefore, here we computationally model connected neurons across the auditory brainstem, exploring two biophysical mechanisms that can account for the brainstem's emphasis of early-arriving spatial information. Matching responses in the medial superior olive (MSO), of neurons encoding interaural time differences, we demonstrate that accurate localisation in reverberant environments is enhanced by realistic pre- and post-synaptic specialisations. Short-term synaptic plasticity at the inputs from auditory nerve fibres to spherical bushy cells (SBCs) in the ventral cochlear nuclei that project bilaterally to the MSO, and K_{V1} ion-channels in the SBCs and MSO neurons, promote encoding of reliable spatial information, by suppressing responses to late-arriving sound, particularly at frequencies where reverberant sound is relatively intense in outdoor environments. Suiting weak reverberation outdoors at very low sound frequencies, weak K_{V1} activity at 200 Hz promotes accurate localisation. Applied to the lateralisation of human speech near 600 Hz in a virtual reverberant room, identical synaptic depression and strong K_{V1} activity at this higher frequency enhance correct, over spurious, localisation cues at the earliest stages of spatial processing.

Author Summary

Aurally locating a talker in a reverberant room is often challenging for hearing-impaired listeners. Sound arriving directly from the talker isn't easily distinguished from reverberant sound reflecting off walls milliseconds later. Nevertheless, normal-hearing listeners easily localise sound-sources, aurally "glimpsing" the reliable spatial information of direct sound during early, rising portions of modulated sounds, while subconsciously ignoring later-arriving, confounding information corrupted by reverberation. Understanding the successful underlying mechanisms may suggest approaches to improve auditory spatial information provided to listeners with hearing aids and cochlear implants. In the auditory brainstem, binaural neurons of the medial superior olive (MSO) preferentially respond to early-arriving spatial information. As simultaneous recordings from MSO neurons and their monaural input neurons while controlling adaptation remain unrealised, to understand the contributing mechanisms, here we identify and computationally demonstrate two mechanisms that suppress responses to late-arriving sound, ultimately emphasising early-arriving sound, and enhancing the localisation of talkers despite reverberation: synaptic depletion in the bilateral cochlear nuclei that drive the MSO, and K_{V1} ion-channels which support the encoding of spatial information in MSO neurons. Our models reflect the frequency-dependent behavioural emphasis of reliable, early-arriving auditory spatial information, demonstrating brain mechanisms that suppress unreliable spatial information by spectro-temporally opposing typical outdoor reverberation.

Introduction

Sound propagating directly from its source to a listener's ears is typically followed milliseconds

later by multiple reverberant copies arriving from different directions (Fig. 1). Despite this

mixture of direct and reflected sound pressure generating non-stationary spatial information in

the binaural cues—the interaural time difference (ITD) and interaural intensity difference

(IID)—listeners typically perceive a sound as punctate, and originating from the direction of its

source. Facilitating 'cocktail party listening' – attending to a single talker against a background

of many competing voices – perception of the true source location can persist even when the

intensity of reflected sound matches or exceeds that of the early-arriving, direct sound. [1–3]

Figure 1. Reverberant copies of direct speech produce confounding binaural cues.
(A) Anechoic speech stimulus 'church' (direct sound, without reverberation), spoken at
70 dB SPL by a female talker located +30° to the right and front of a virtual listener.
Spectrogram shows speech energy <1 kHz at left ear. Gammatone filters centred at 200
Hz (light grey) and 600 Hz (dark grey) show effects of cochlear filtering on speech
waveforms in the left (blue) and right (red) ears. Instantaneous ITDs (light/dark grey)
(restricted to ±700us, human physiological range) were consistently near +363 μs. **(B)**
Reverberant speech stimulus including direct speech plus two simulated reflections from
listener's left, the first from -65° delayed by 4 ms, and the second from -130° delayed by 8
ms. Reverberant copies increased the energy at the left ear (note the generally brighter
spectrogram above 400 Hz). Reverberant energy extends into the quiet pause between
the vowel and final consonant (0.45-0.55 ms), generating rapidly varying instantaneous
ITDs (also restricted to ±700us), along with conflicting ILD cues in the 600-Hz channel.

Neural correlates of 'echo-suppression' are observed in the ascending auditory pathway, from auditory nerve and brainstem, to midbrain and primary auditory cortex. The brainstem emphasises early-arriving sound at both ears, as neurons of the medial superior olive (MSO) perform binaural coincidence detection. Driven bilaterally by the left and right auditory nerve via bushy cells of the ventral cochlear nuclei, MSO neurons encode spatial information through their sensitivity to ITDs conveyed in the temporal fine structure (TFS) of low-frequency (< 1500 Hz) sounds. The resulting responses of MSO neurons tuned to ITD are strongest during rising sound-energy. Adaptation in monaural projection pathways to binaural MSO neurons is believed to contribute, yet specific mechanisms for the emphasis of early-arriving direct sound in these neural pathways remain to be identified. [4–8]

Behavioural emphasis of early-arriving ITD information is frequency dependent [9]: for amplitude-modulated 600-Hz sounds, listeners are more sensitive to ITDs conveyed during the rising-energy portion than they are to ITDs at the energy peak; this is not the case at 200 Hz, where listeners are equally sensitive to ITDs conveyed during rising and peak energy, and where, in outdoor settings, reverberant energy can be 20 dB less intense at 200 Hz than at 600 Hz [10]. For both frequencies, listeners are least sensitive to ITD during falling sound-energy, when direct sound is most likely to be corrupted by reverberation. These data suggest that spatial auditory brain mechanisms transmit reliable information, and suppress unreliable information, accounting for natural frequency-profiles in reverberant energy which decrease below 1500 Hz.

Noting the unavailability of simultaneous recordings from the MSO and cochlear nuclei with external control of adaptation, here we apply a nonlinear, computational brainstem model to explore two cooperative biophysical mechanisms for the frequency-dependent emphasis of

ITD during rising and peak sound-energy: (i) short-term synaptic plasticity (synaptic

depression) at the Endbulbs of Held synapses between auditory nerve fibres and spherical

bushy cells (SBCs) in the ventral cochlear nuclei [11–14]; and (ii) voltage-gated, low-threshold

potassium (K_{V1}, K_{LT}) ion channels in MSO neurons [15–18] and in the SBCs [19] projecting

bilaterally to the MSO. We test whether these biophysical features suppress responses to late-

arriving sound, and support the emphasis of sensitivity to ITDs conveyed in early-arriving

sound that is observed in single MSO neurons [4]. Then, with our nonlinear model, and a linear

spiking model [20] extended to populations of MSO neurons in the left and right brain

hemispheres, we explore brainstem properties consistent with the stronger weighting of ITD

information conveyed during rising energy at 600 Hz—a frequency with higher reverberant

energy—compared to 200 Hz, where reverberant energy is less intrusive.

Our hemispheric MSO model then probes a possible link between relative weighting of spatial

information during rising energy, and correct lateralisation of natural speech in realistic

acoustic environments (the "Haas effect") [3]. We evaluate monaural synaptic depression prior

to binaural interaction, in promoting correct, unambiguous judgements in the laterality of

natural speech in a simulated reverberant space with direct sound and early reflections off

virtual walls [4]. For the 600-Hz channel investigated, achieving unambiguous, correct

lateralisation would suggest a dominance of ITD information conveyed during rising sound-

energy, which facilitates correct lateralisation by emphasising ITD cues of sound arriving

directly from its source, over the confounding ITD cues of its reflected copies.

Results

A nonlinear brainstem model with synaptic depression and K_{V1} activity reproduces the frequency-dependent emphasis of spatial information during rising and peak sound-energy

We first explored the extent to which synaptic depression at model SBCs in the cochlear nuclei accounts for the emphasis of ITDs during the rising energy of modulated sounds in a model MSO neuron (Fig. 2B). We did so, employing amplitude-modulated binaural beats (AMBBs) [2,4], in which binaurally presented tones of a slightly different frequency are modulated in amplitude at a rate equal to the difference in frequency across the two ears. This generates a stimulus in which each cycle of rising and falling sound-energy contains a full cycle of interaural phase disparities. AMBBs (Fig. 2A) centred at 600 Hz, with modulation rates 4 to 64 Hz, were presented to a standard model of peripheral auditory processing [21,22], which drove a nonlinear model of brainstem neurons. The model of peripheral auditory processing includes 24 adapting auditory nerve fibres: twelve each in the left and right ears, with characteristic frequency (CF) 600 Hz. (CF is the frequency at which a neuron has its lowest threshold in sound pressure level, SPL, for an action potential; CF is inherited from the frequency-tuning of the inner ear, and the resulting CFs of auditory nerve fibres that distally drive a neuron.) Each of three distinct model auditory nerve fibres projects an ipsilateral, uniformly depressing ($u =$ 0.5) [23], excitatory synaptic input to one of the eight (four left, and four right) model SBCs. Each model SBC projects a non-depressing, excitatory synaptic input to the multi-compartment model MSO neuron. The model SBCs and MSO neuron are Hodgkin & Huxley models [24], with circuit elements that represent membrane ion-channels, including K_{V1} [25–27].

Figure 2. Amplitude-modulated binaural beats (AMBBs) [2] **and the nonlinear**

brainstem model: (A) AMBBs in which AM rate is equal to binaural-beat frequency

(difference between frequencies at right and left ears). Presented via headphones,

interaural phase difference (IPD) cycles through 360° at the same rate as AM. *Start-IPD*

(the IPD at zero amplitude) is a free parameter. Shown with right-carrier 616 Hz, left-carrier

584 Hz, AM 32 Hz, and *start-IPD* 270° (right channel trailing by 90°), resulting in zero IPD

at the midpoint of rising-amplitude. **(B) Nonlinear brainstem model** for an MSO neuron

and its excitatory inputs with synaptic depression in the cochlear nuclei. AMBBs drive a

model for bilateral auditory nerve fibres [21,22] projecting individually depressing synapses

[23] ($u = 0.5$) onto model spherical bushy cells (SBCs) in the cochlear nuclei [26], which in

turn project bilaterally to the model MSO neuron (best-ITD = 0). The best-ITD of a neuron

is the ITD of highest spike rate, typically measured with unmodulated stimuli of equal

amplitude at the two ears. The nonlinear model MSO neurons of this study have best-ITDs

equal to zero. **(C) Sub-compartment** in the nonlinear brainstem model (see Methods).

Beginning without synaptic depression, a nonlinear model with very strong, non-depressing,

supra-threshold synapses in the cochlear nuclei, originally developed to generate strong,

sustained responses [28] consistent with strong ITD sensitivity in the MSO for unmodulated

pure-tone stimuli [29], produced only slight adaptation in the spike rates of its model SBCs

(Fig. 3A, top row). Without synaptic depression, the model MSO neuron responded strongly to

zero ITD, its best-ITD, across the amplitude modulation (AM) cycle: most strongly at peak

sound-energy, slightly less strongly during rising energy, and less strongly during falling energy

(Fig. 3A, lower three rows; in a 3-way comparison of spike counts for best-ITD during rising vs.

peak vs. falling energy, $p < 10^{-9}$ at each modulation frequency). The slightly larger suppression

in responses to best-ITD during falling energy is supported by adaptation in the auditory nerve

model, and K_{V1}-based refractory effects in the model SBCs and MSO neuron. (AMBB stimuli

had increasing IPD (positive beat direction): "best-ITD during rise" denotes start-IPD = 270°;

"best-ITD at peak" denotes start-IPD = 180°; and "best-ITD during fall" denotes start-IPD =

90°.)

Figure 3. AMBB cycle histograms for nonlinear model brainstem neurons

acoustically stimulated by sound frequencies centred at CF **600 Hz: (A) Without synaptic**

depression, auditory nerve to SBC synapses were strongly supra-threshold. Model SBCs

adapted slightly. Model MSO neuron responded to best ITD strongly at peak sound-

energy, and slightly but consistently less strongly during rising and falling energy (3-way

comparisons, $p < 10^{-9}$). The synchrony index—a measure of temporal alignment of spikes

over the AM cycle (see Methods)—ranged from 0.133 at 4 and 64 Hz to 0.161 at 16 Hz for

model SBCs, and from 0.595 (64 Hz, best-ITD at peak) to 0.794 (16 Hz, best-ITD during

fall) for the model MSO neuron (Rayleigh statistic, $p < 0.001$ in all cases). **(B) With**

synaptic depression in the cochlear nuclei, the auditory nerve to SBC synapses were

supra-threshold at full strength. Model SBCs adapted. Model MSO neuron responded to

best ITD strongly during rising energy; weakly to moderately at peak; and weakly during

falling, energy (3-way comparisons, $p \leq 0.003$). Synchrony-indices to AM for model SBCs

ranged from 0.0485 at 4 Hz to 0.174 at 32 Hz; for model MSO neuron, from 0.450 (64 Hz,

best-ITD during fall) to 0.814 (64 Hz, best-ITD during rise) (Rayleigh statistic, $p < 0.01$ for

model SBCs at 4-Hz AM, otherwise $p < 0.001$). *Definitions:* Grey silhouettes: AM envelope.

Black lines: static IPD functions. Best-ITD = 0. Best-ITD during rise: *start-IPD* = 270°. Best-

ITD at peak: *start-IPD* = 180°. Best-ITD during fall: *start-IPD* = 90°.

Next, we introduced synaptic depression in supra-threshold synapses of model SBCs,

producing adaption in their spike rates (Fig. 3B, top row). This adaptation followed a similar

time-course across modulation rates, such that at low-to-moderate rates (4 to 16 Hz) most of

the adaptation occurred by the peak in the AM cycle, and at moderate-to-high rates (16 to 64

Hz) gradual adaptation is evident across much of the AM cycle. Consistent with physiological

and behavioural data at 600 Hz [4,9], the model MSO neuron responded to its best-ITD

strongly during rising amplitude, weakly to moderately (and broadly) at peak energy, and only

weakly during falling energy (Fig. 3B, lower three rows; in this 3-way comparison of spike

counts, $p \leq 0.003$ at each modulation frequency). Adapting similarly to the model SBCs, the

model MSO neuron had higher spike counts for best-ITD during rising energy vs. peak energy

at 4- to 16-Hz modulation ($p < 0.02$), and during peak vs. falling energy at 16- to 64-Hz

modulation ($p < 0.0025$).

Thus, consistent with behavioural data at the same, 600-Hz, sound frequency, a model that

includes synaptic depression between the auditory nerve and cochlear nuclei that drove

bilateral inputs to the MSO neuron, responds preferentially to ITDs during the rising energy of

sounds. Without this synaptic depression, the preference for spatial cues during rising sound-

energy is absent, suggesting a critical role for monaural input pathways to binaural neurons in

emphasising spatial information that is likely to be reliable in reverberant listening conditions.

Sensitivity to ITDs conveyed in the temporal fine structure (TFS) of sounds is subject to highly

specialised biophysical constraints, constraints that are generally thought to hold for sound

frequencies up to 1400 Hz (higher in some non-human species), covering the range over

which ITDs in the TFS are discriminable. Therefore, given the emphasis to ITDs during the

rising energy of modulated sounds at 600 Hz—concordant with perceptual and brain-imaging

data obtained at a similar frequency [2]—we might expect a similar emphasis at the lower

sound-frequency of 200 Hz. Nevertheless, despite our model implementing identical

biophysical elements, we observed a very different pattern of results at 200 Hz compared to

600 Hz. These differences are reminiscent of behavioural data [9]: at 600 Hz, human ITD-

sensitivity is strongest during rising energy with progressively less ITD sensitivity for peak and

falling energy; but at 200 Hz, ITD sensitivity is strong for both peak and rising energy, and

again weak for falling energy.

Employing the same model with monaural depressing synapses, identical to those which

emphasised ITDs during the rising energy at 600 Hz, we assessed the relative emphasis of

ITD cues in the modulation cycle of a 200-Hz AMBB stimulus for the modulation rates of 8 and

20 Hz employed by Hu et al. [9]. At 200 Hz, the model SBCs showed slight adaptation in spike

rate across the AM cycle (Fig. 4A, top row), less adaptation than at 600 Hz. Spike counts in the

model MSO neuron (Fig. 4A, lower three rows) matched the patterns of significance in human

ITD-detection for AM stimuli at 200 Hz [9]: spike counts were slightly higher but not

significantly for best-ITD during peak vs. rising energy, and spike counts were significantly

different (higher) only for best-ITD at peak energy vs. falling energy (p = 0.0079 for modulation

at 8 Hz; p = 0.0014 for modulation at 20 Hz).

Figure 4. AMBB cycle histograms for nonlinear model brainstem neurons stimulated

by frequencies centred at CF **200 Hz**. Same synaptic depression and model SBCs as in

Fig. 3B, adapted less at 200 Hz. **(A) Same fast model MSO neuron** as in Fig. 3B: spike

counts were not significantly different for best-ITD during rising vs. peak energy, and were

higher for best-ITD at peak energy vs. falling energy (p < 0.01). Synchrony-indices to AM

for model SBCs ranged from 0.0762 at 8 Hz to 0.109 at 20 Hz; model MSO neuron from

0.433 (20 Hz, best-ITD during fall) to 0.807 (8 Hz, best-ITD during rise) (Rayleigh statistic,

p < 0.001). **(B) Moderate-speed model MSO neuron:** spike counts were not significantly

different for best-ITD during rising vs. peak energy, and were lower for best ITD during

falling energy (p < 0.005). *Definitions:* Grey silhouettes: AM envelope. Black lines: static

IPD functions. Best ITD = 0. Best-ITD during rise: *start-IPD* = 270°. Best ITD at peak: *start-*

IPD = 180°. Best ITD during fall *start-IPD* = 90°. Synchrony-indices to AM for the model

MSO neuron ranged from 0.825 (20 Hz, best-ITD during fall) to 0.888 (20 Hz, best-ITD

during rise) (Rayleigh statistic, p < 0.001)

Noting recent evidence of heterogeneity in membrane speeds in the very low-frequency region

of MSO [30], we applied AMBBs at 200 Hz to our nonlinear brainstem model, now modified

with a moderate-speed model MSO neuron having slower dendritic and somatic membranes,

derived by dividing membrane conductance values by three. The identical model SBCs again

adapted less (Fig. 4B, top row) than at 600 Hz. Synaptic strength in this moderate-speed

model MSO neuron was divided by two for low spike rates for best-ITD during falling energy,

while retaining moderate spike rates for best-ITD during rising and peak energy (Fig. 4B, lower

three rows). The moderate-speed MSO neuron then produced very few spikes at ITDs distant

from best-ITD, yielding spike counts for best-ITD at peak energy that were equal to, or slightly

less than, spike counts for best-ITD during rising energy. The moderate-speed model MSO

neuron slightly augmented patterns of significance in human ITD-detection [9]: spike counts

were not significantly different for best-ITD during rising vs. peak energy, and were significantly

lower for best-ITD at falling energy (8-Hz modulation: rise vs. fall, $p = 4.08 \times 10^{-05}$; peak vs. fall,

p = 0.0049; 20-Hz modulation: rise vs. fall, $p = 1.53 \times 10^{-09}$; peak vs. fall, $p = 1.53 \times 10^{-09}$).

Our nonlinear brainstem model accounts for the emphasis of rising energy in ITD encoding by

MSO neurons at 600 Hz, and is consistent with the shift from very strong human ITD-sensitivity

during rising energy at 600 Hz, to strong sensitivity during both peak and rising energy at 200

Hz, and with weaker sensitivity during falling energy at both frequencies. As the stimulus

frequency is reduced from 600 to 200 Hz, the reduction in suppression at the peak of the AM

cycle is likely due to decreased activation of K_{V1} channels at the lower frequency, from the

inherently longer quiet periods between intense input spiking [31,32].

A hemispheric-difference model including synaptic depression correctly

lateralises amplitude-modulated stimuli with temporally specific ITDs

To test whether synaptic depression in combination with heterogeneous neuronal properties is

consistent with the behavioural observations of Hu et al. [9], we employed a neural spiking

model of both brain hemispheres, incorporating linear model neurons in the bilateral cochlear

nuclei and MSOs [20], to generate a neuro-metric measure of lateralisation. Following the

model concept of Dietz et al. [33], two hemispheric channels ('left' and 'right') comprised

distinct MSO model neuron populations (50 neurons each) whose inputs from 'contralateral'

cochlear nucleus were delayed by 0.125 cycles of interaural phase difference (IPD, equal to

ITD x frequency) [34] such that they spiked preferentially for sounds arriving from contralateral

spatial locations (Fig. 5). The difference in spike rate between hemispheres, calculated (in 5-

ms epochs) as a signed d', was then used as a neuro-metric measure of lateralisation (see

Methods) [34,35]. A uniform synaptic depression ($u = 0.55$) [23] was implemented

independently at each synapse between an auditory nerve fibre and its target SBC of the

cochlear nucleus. Sinusoidally amplitude-modulated (SAM) tones, with non-zero, positive ITDs

positioned within the rising, peak, or falling phases of the AM cycle as per Hu et al. [9], and see

above, were presented to the linear model (Fig. 6). As in the behavioural study, the tone

frequency (200 Hz or 600 Hz) and the AM rate (8 Hz or 20 Hz) were varied, as was the

proportion (20% or 40%) of the AM cycle containing a non-zero ITD.

Figure 5. Overview of the hemispheric-difference model consisting of two MSO

populations (red—left MSO and blue—right MSO), each containing fifty linear, single-

compartment model neurons, with either fast or slow resonant properties [20]. Each MSO

neuron model receives four excitatory inputs 'bilaterally' from linear, single-compartment

SBC model neurons in the CN. Three independently-simulated, individually-depressing

and medium-spontaneous-rate auditory nerve fibres [21] provide excitatory drive to each

SBC model neuron.

Figure 6. Lateralisation by the linear, hemispheric-difference model at 200 Hz and

600 Hz, each with 8-Hz AM. (A&B) At 200 Hz, both Slow (A) and Fast (B) MSO models

correctly lateralised +300 μs ITDs (top row, black) to the right, based on d'>1 in any 5ms

bin (red vertical bands), most often at peak (middle column) of the AM cycle (grey

silhouettes) compared to rising (left column) and falling (right column) phases (Slow MSO:

Rising, 7 bins; Peak, 12 bins; Falling, 2 bins. Fast MSO: Rising, 3 bins; Peak, 4 bins;

Falling, 1 bin); d' (bottom rows, black) is a difference in mean spike rates between left (top

rows, red) and right (top rows, blue) MSO populations, normalised by variance. The same

adapting inputs are used for both MSO neuronal speeds, therefore more correct

lateralisations overall by the Slow MSO is a result of its slower integration. **At 600 Hz (C)**

introducing +150 µs ITD (top row, black) produced strong onset ITD sensitivity in the Fast

MSO during rising phase (left column) that decreased across the AM cycle (Fast MSO:

Rising, 12 bins; Peak, 5 bins; Falling, 1 bin).

At 600 Hz, MSO neurons with fast resonant properties, i.e. akin to the nonlinear model with

100% K_{LT} (K_{V1}) conductance, demonstrated a strong sensitivity to the onset ITD, as indicated

by the increased number of instances when the AM stimulus containing a (right-leading) +150

μs ITD in its rising-energy phase was correctly lateralised [d' > 1 in any bin was considered a

correct lateralisation of a signal from the 'right' (Fig. 6 *pink vertical bands*)]. This ITD sensitivity

decreased across the AM cycle reaching a minimum when non-zero ITDs were restricted to

the falling-energy phase (Fig. 6 *bottom row*). The trend for onset dominance at 600 Hz was

true for both modulation rates (8 Hz and 20 Hz) and when the proportion of the AM cycle

containing non-zero ITDs was either 20% or 40% (Fig. 7 *right column*). Notably, in all three

portions of the AM cycle, the number of correct lateralisations decreased as the proportion of

an AM cycle containing a non-zero ITD was decreased from 40% to 20% (Fig. 7 *right column*,

blue).

Figure 7. Summarising correct lateralisations of SAM stimuli by the hemispheric-

difference model. Mean (±SEM) time correctly lateralised per presentation (number of

correct lateralisations * bin duration / 25 presentations) by either Slow MSO neurons at

200 Hz (left column) or Fast MSO neurons at 200 Hz and 600 Hz (middle and right

columns respectively), for modulation rates of 8 Hz (top row) and 20 Hz (bottom row). ITDs

were inserted into either 20% (blue dotted) or 40% (black solid) of the AM cycle during

Rising, Peak, or Falling energy. At 600 Hz, the Fast MSO displays dominant ITD

weighting at onset that decreased significantly across AM cycle (2-way ANOVA, interaction

of AM cycle phase x Percentage ITD insertion: 8-Hz AM, $F_{(2,48)} = 8.310$, p = 0.001; 20-Hz

AM, $F_{(2,48)} = 50.098$, p = 0.0001). At 200 Hz, the Fast MSO showed equal or better ITD

sensitivity at Peak compared to Rising energy (2-way ANOVA, interaction of AM cycle

phase x Percentage ITD insertion: 8-Hz AM, $F_{(2,48)}$ = 7.83, p = 0.001; 20-Hz AM, $F_{(2,48)}$

= 36.01, p = 0.0001). Slow MSO generated more correct lateralisations than Fast MSO (2-

way ANOVA, interaction of AM cycle phase x Neuron Type: 8-Hz AM, $F_{(2,48)}$ = 18.82, p =

0.0001; 20-Hz AM, $F_{(2,48)}$ = 13.12, p = 0.0001) with equal or augmented ITD sensitivity at

Peak for 40% non-zero ITD (Paired two-tailed T-test, Mean Peak – Rising, N = 25: 8-Hz

AM, $t_{(24)}$ = 2.21, p = 0.037; 20-Hz AM, $t_{(24)}$ = 2.21, p = 2.37 x 10^{-4}). Correct

lateralisations also increased as the percentage of AM phase containing non-zero ITD was

raised from 20% to 40% (3-way ANOVA, main effect of Percentage ITD insertion: Fast

MSO, $F_{(1,24)}$ = 418.78, p = 0.0001; Slow MSO, $F_{(1,24)}$ = 285.622, p = 0.0001)

When an amplitude-modulated 200-Hz tone (with a right-leading, non-zero ITD of +300 µs)

was presented to the fast MSO model, the onset dominance observed at 600 Hz was replaced

by an increased weighting of ITD cues towards the peak of the AM cycle (Fig. 6). Indeed, the

frequency of correct lateralisations at the peak of AM cycles was either equal to (8-Hz AM

stimuli) or higher (20-Hz AM stimuli) than that observed at corresponding onset phases (Fig. 7

middle column). As at 600 Hz, reducing the proportion of the AM cycle containing a non-zero

ITD from 40% to 20% also generated fewer correct lateralisations across all AM phases (Fig. 7

middle column, blue). Whilst the fast-resonant MSO model could reproduce behavioural trends

observed by Hu et al. [9] at both carrier frequencies, it generated fewer correct lateralisations

overall at 200 Hz (Fig. 7 *middle* and *right columns*). We therefore presented the same 200-Hz

carrier stimulus to the linear model MSO neurons with slower, less resonant membrane

properties (Fig. 6). This generated a higher number of correct lateralisations overall, while

maintaining, or even augmenting, the maximum weighting of ITD at the peak AM energy in all

conditions tested (Fig. 7 *left column*).

Our linear model, therefore, suggests that a slower, more integrative MSO neuron may assist

lateralisation in lower-frequency channels, in particular by extending the extraction of ITD

information towards peak energy in the AM cycle, where human ITD detection is best when

comparing at 200 Hz across the AM cycle [9]. Additionally, our model qualitatively matched the

behavioural data by demonstrating a higher propensity to lateralise stimuli of either frequency

when 40% vs. 20% of the AM cycle contained a non-zero ITD.

Synaptic depression improves the hemispheric-difference model's ability to lateralise speech in artificial reverberation

Synaptic depression improves the hemispheric-difference model's ability

to lateralise speech in artificial reverberation

If neural adaptation prior to binaural integration contributes to accurate source localisation, we

would expect it to aid lateralisation of speech in a reverberant room, by emphasising ITD cues

associated with direct sound over reverberation (Fig. 1 *far left*) [4]. Speech signals were

presented to the neural model of lateralisation under simulated anechoic (non-reverberant) and

reverberant conditions. We then observed whether the model correctly lateralised the side to

which the source was located in the presence or absence of synaptic depression in SBCs of

the cochlear nuclei.

In the anechoic condition (Fig. 8A), a word token ('church') was presented to the non-adapting

linear model from a virtual location 1 metre away from the target and 30 degrees to the right of

the midline. The speech waveform—gammatone-filtered at 600 Hz (Fig. 8A *top row*)—was

more intense at the right ear (red), and led the left-ear signal (blue) by an average ITD of +363

µs (Fig. 8A *top row*, dark grey). This generated a larger response from model neurons in the

'left' MSO (Fig. 8A *middle row*) and multiple bins throughout the speech token where d' values

were > 1 (Fig. 8A *pink vertical bands*), indicating that the talker was correctly lateralised to the

right in the non-adapting, linear model.

Figure 8. Lateralisation of 'anechoic' and 'reverberant' speech stimuli by the

hemispheric-difference model (fast MSO, 600-Hz channel) with and without

synaptically adapting inputs from the auditory nerve to the cochlear nucleus: (A)

Anechoic stimulus is correctly lateralised to the right (pink vertical bands) for long periods

independently of non-adapting (left column) or adapting (right column) synaptic inputs. Dry

speech stimulus gammatone-filtered at 600 Hz with instantaneous ITDs (top row), mean

firing rates of left (middle row, red) and right (middle row, blue) MSOs and d' neuro-metric

(bottom row) are displayed. **(B) Reverberant stimulus** requires adapting synaptic inputs

(right column) for correct lateralisations alone (pink vertical bands). Non-adapting synaptic

inputs to the cochlear nuclei produced both correct (left column, pink vertical bands) and

incorrect lateralisations (left column, light blue vertical bands) due to reverberant stimulus'

highly variable ITDs and confounding ILDs (top row). The inclusion of synaptic depression

from the auditory nerve to the cochlear nuclei (using the same auditory nerve simulations)

removes all incorrect lateralisations. Remaining correct lateralisations correspond with

stimulus onsets (right column, pink vertical bands). **(C) Quantifying incorrect**

lateralisations with non-adapting and adapting synaptic inputs (same auditory nerve

simulations for both) over a hundred presentations of the reverberant speech stimulus.

Synaptic depression produces a five-fold decrease in incorrect lateralisations (N = 100,

$t(99) = 9.51$, $p = 1.31 \times 10^{-15}$, two-tailed paired T-test).

In the reverberant condition, the same word token was presented to the non-adapting linear

model from the same angle and distance, however it was also followed by two delayed copies

generated by early reflections off virtual walls added behind, and to the left of, the listener (Fig.

1B *far left*). This mixture of sound arriving direct from the source and early reflective copies led

to a more complex waveform (including a more intense signal at the 'left ear' (direct-to-

reverberant ratio: -4dB; mean ILD: -3 dB)) whose running ITDs fluctuated between extremely

large positive and negative values, culminating in an average ITD of +711 µs, a value outside

the human physiological range. Although the resulting d' output exceeded 1 in eleven epochs

coinciding with waveform onsets (Fig. 8B, *left, pink vertical bands*), it was also briefly lower

than -1 in the opposite direction during three intermediate epochs (Fig. 8B, *left*, *blue vertical*

bands), indicating a potentially ambiguous left-right localisation output.

We then increased adaptation by introducing synaptic depression to the monaurally driven

inputs from auditory nerve fibres to the cochlear nuclei of the linear model, and presented the

same reverberant stimulus (Fig. 8B) as in the previous condition. Despite the potentially

confounding ITD (and ILD) cues (Fig. 8B *top row*), adding adaptation in the monaural input

pathways enhanced the performance of the binaural model MSO neurons, and generated

correct lateralisations of the true source to the right: the d' output exceeding 1 in six time bins

without ever crossing below -1 (Fig. 8B *bottom row, right*). When the number of incorrect

lateralisations was tallied over a hundred presentations of the reverberant stimulus (Fig. 8C),

incorrect lateralisations were observed five times less frequently when synaptically depressing

auditory nerve inputs were included in the linear model (mean incorrectly lateralised time for

non-depressing synaptic inputs = 6.75 ± 0.50 ms/presentation vs. mean incorrectly lateralised

time for depressing synaptic inputs = 1.3 ± 0.24 ms/presentation). This neuro-metric profile

agrees with the psychoacoustic percept as has been previously described for similar word

tokens [4], suggesting that synaptic adaptation helps to lateralise ethological sounds in

reverberant environments.

Discussion

The brainstem suppresses responses to late-arriving reverberant sound in neural pathways that encode spatial cues

The ability to localise the source of a sound in reverberant environments, where reflections from acoustically opaque surfaces can degrade the accuracy of auditory spatial cues, is critical to prey and predator alike, and important for communication in human listeners. To explore the contribution of the brainstem to sound-source localisation, noting the unavailability of simultaneous recordings from the MSO and cochlear nuclei with external control of adaptation, we here apply physiologically realistic models of connected neurons across the auditory brainstem. We find that accurate localisation in reverberation is enhanced by both synaptic depression at spherical bushy cells (SBCs) in the ventral cochlear nucleus that project bilaterally to the medial superior olive (MSO, a site of primary binaural integration)—as well as by K_{V1} channels in the cochlear nuclei and the MSO that activate more strongly at relatively higher sound-frequencies. We show that these mechanisms account for the observed ability of MSO neurons to respond preferentially to ITDs conveyed during the early, rising-energy portion of low-frequency sounds near 600 Hz [4]. Reflecting the perception of normal-hearing listeners at 500 Hz [2], our models successfully glimpse the ITD cues conveyed in the temporal fine structure during the rising portion of the AM cycle, suppressing spatial information conveyed in all later portions of the AM cycle, including the portion with highest energy. Whilst relatively weak synaptic depression in the MSO may also contribute, preliminary modelling without synaptic depression in the cochlear nuclei showed that stronger synaptic depression in the MSO disrupted ITD sensitivity without sufficiently emphasising early-arriving spatial information.

Suppression by K_{V1} channels opposes typical frequency-profiles of reverberant energy in natural outdoor scenes

K_{V1} channels are known to enhance synchrony to sound in bushy cells of the anteroventral cochlear nuclei [28], and support ITD sensitivity in the MSO [15]. Our results suggest that K_{V1} channels also underlie the frequency dependence of ITD detection performance, observed behaviourally when ITDs are applied to different segments of the AM cycle [9]. Intrinsic K_{V1}-channel properties, that decrease K_{V1} activation more during the longer quiet periods that occur between periodic bursts of intense input spiking at lower stimulus frequencies [31,32], are likely contributing mechanisms for the shift from very strong human ITD-sensitivity during rising energy at 600 Hz, to strong sensitivity during both peak and rising energy at 200 Hz, with weaker sensitivity at both frequencies during falling energy when direct sound for accurate source localisation is most likely to be corrupted by reflected sound.

Natural outdoor acoustics appear to have influenced brain mechanisms that suppress responses to reverberation. In many outdoor environments, including rural forests and fields, and urban streets, reverberation-time ('T60'—the time for reverberant energy to fall by 60 decibels) decreases as sound frequency decreases below 1500 Hz [10]. As reverberation times decrease to a minimum near 200 Hz, K_{V1} activity independently decreases [31,32], yet remains highly effective in suppressing late-arriving sound at 500-600 Hz, yet suppression notably decreases by 200 Hz. To the extent that spike rates of auditory nerve fibres decrease with lower sound-frequency, synaptic depression at neurons in the cochlear nuclei may also decrease. At very low frequencies, including 200 Hz, where reverberant energy in natural, outdoor scenes is low, suppression of spatial information during peak energy is less important. However, in modern, indoor listening environments, characterised by enclosures with highly

reflective walls, reverberation can be high even at very low frequencies. Indoor reverberation

combined with weakly suppressing neurons, and with increasing perceptual thresholds for ITD

at sound frequencies below 500 Hz [36], may contribute to the observed low perceptual

weighting of very low frequencies when localising broadband sound [37]. This consistent

perceptual down-weighting for localisation, presumably by brain centres above the brainstem,

occurs even as these very low sound frequencies contain and apparently convey vital speech

information, including the fundamental frequency, and first formant of vowels.

Contrasting the relatively weak reverberation and weak suppression of late-arriving sound at

200 Hz, with the relatively strong suppression at 600 Hz and increasing reverberation with

higher sound frequency up to 1500 Hz, suggests that brainstem neurons effectively suppress

responses to reverberation for sound frequencies from 500 to 1200 Hz, a frequency range that

despite being relatively high in reverberation produces the lowest perceptual thresholds for ITD

discrimination in human listeners [36,38], and dominates the percept of auditory spatial cues

[37,39,40].

MSO neurons tuned to very low sound-frequencies, though remaining faster than other types

of neurons, nonetheless include a range of membrane time-constants [30]. By not expressing

more ion channels than required, the slower MSO neurons encode ITD efficiently, realising a

cellular energetic advantage. Consistent with the reported heterogeneity in temporal

properties, both moderate and fast nonlinear model MSO neurons reflected human ITD

sensitivity at 200 Hz [9]. Reduced, but still viable, K_{V1} activity provided ITD sensitivity at 200 Hz

in the nonlinear model, while combining with synaptic depression in the cochlear nuclei to

suppress responses during falling energy. Introducing slower membranes in linear model MSO

neurons boosted the hemispheric-difference model's ability to lateralise 200-Hz signals,

especially at their energetic peak, suggesting a functional benefit to a reduced density of K_{V1}

channels at lower frequencies.

Within the input pathways to the MSO, compared with the strong synaptic depression

observed *in vitro* [11–14], the contrastingly weak synaptic depression reported *in vivo* [41,42]

may indicate heterogeneity. In the excitatory pathway, weakly depressing synapses may

innervate and explain the subpopulations of spherical bushy cells with strong sustained

responses, both primary-like [43] and high-synchrony [28]. Inputs to the MSO driven by these

weakly adapting neurons would account for MSO neurons with strong sustained responses

[29], which may contribute to listeners' ability to locate slowly moving sources of sustained

sounds.

Whilst inhibition including GABAergic forms is linked to enhanced membrane excitability and

added precision in ITD encoding [17,44,45], our results suggest that synaptic depression and

intrinsic membrane properties, combined with excitatory binaural coincidence detection

mechanisms, fundamentally contribute to perceived location based on ITD. The success of our

simplified, purely excitatory, input model is consistent with the view that inhibition to MSO

neurons does not produce strongly adaptive effects, and that the glycinergic inhibition is

reasonably fast-acting, largely contralaterally driven and leads contralateral excitation in time—

with the main effect that best-ITD is shifted toward contralateral-leading ITDs by delaying the

net excitatory post-synaptic current generated by the contralateral ear [46,47].

Synaptic adaption enhances correct lateralisation of reverberant speech

Early reflections—those following the direct signal by 50 ms or less [48]—can disrupt low-

frequency sound localisation in realistic auditory environments by conveying spurious ITD cues

in the TFS of sounds [49]. Despite this, normal-hearing listeners are highly adept at locating

the true source of a sound in reverberant environments including speech in reverberant

environments. By demonstrating that the addition of synaptic adaption to a hemispheric 2-

channel model emphasises ITD cues in sound onsets, our data suggest one means by which

complex sounds, including speech, are reliably lateralised.

Whilst our adapting hemispheric-difference model correctly lateralised reverberant speech, this

was based on its d' output surpassing a threshold value in only six of the ninety 5-ms bins

where a correct ITD cue was available. Nevertheless, although this neuro-metric measure may

not appear particularly robust, it should be remembered that only the 600-Hz frequency

channel was examined for the lateralisation of speech. Studies of the precedent effect—the

suppression of auditory information, including spatial information—for late-arriving sounds—

and localisation in reverberant conditions have demonstrated strong weighting of cues in the

500-750 Hz frequency range [37,39,40], but they also highlight the inability of subjects to

localise pure tones in echoic conditions, suggesting that enhanced localisation of speech in

reverberant conditions involves localisation cues across the low-frequency spectrum. Adding a

midbrain stage where neurons in the inferior colliculus (IC), for example, receive inputs from

MSO neurons across a wide range of CFs would further test the extent to which synaptic

adaptation in the cochlear nuclei improves the localisation of speech in reverberant

environments.

We note that onset-cue dominance is demonstrated extensively in the precedence effect

[50,51], where suppression of neural responses to a brief lagging stimulus occurs over a range

of delays between leading and lagging stimuli. A future localisation model combining monaural

synaptic depression, potentially with inhibitory echo-suppressive mechanisms, such as

delayed inhibition to the midbrain [52–54], and feedforward inhibition in the brainstem from

dorsal to ventral cochlear nucleus [55] and from ventral cochlear nucleus to MSO via the

trapezoid body [56–58], would provide one means of exploring whether these mechanisms act

cooperatively in robust onset-ITD processing in reverberant conditions. The inhibition from

dorsal to ventral cochlear nucleus is associated with non-monotonic rate-level functions in

SBCs, and not with adaptation. This inhibition has onset dynamics that are too fast to account

for the slower adaptive suppression of brainstem responses to late-arriving sound [4]. The

omission of this inhibition in our models explains why the model excitatory synapses in the

cochlear nuclei are slightly weaker than expected. More broadly, brainstem and midbrain

mechanisms may combine additively or act independently for different stimuli. At least for

ongoing, amplitude-modulated sounds, the emphasis early-arriving sound in ITD-encoding by

MSO neurons, combined with the lack an increase in this emphasis at the inferior colliculus of

the midbrain [4], suggests that the brainstem contributes significantly to accurate sound

localisation in reverberation.

Early-arriving spatial cues for bilateral cochlear implant (bCI) listeners

To help bCI listeners receive spatial information, bCI processors can deliver enhanced spatial

information that emphasises early-arriving direct sound over late-arriving reverberation. Such

enhanced spatial information might be added to a recently developed bilateral stimulation

technique that provides detectable ITDs in high-rate pulse trains by including bursts of even

more rapidly successive pulses [59]. High-rate pulse trains with amplitude driven by sound are

applied for speech intelligibility. The bursts occur at a low rate, and their contained rapid

succession of current pulses within each ear overcome the excessive adaptation that can

greatly reduce responses to ITD in bCI listeners [60,61]. Although bCI listeners are most

sensitive to ITD during peaks in sound-energy [9], acoustically the most accurate ITD-

information for source location may still occur during rising sound-energy [2]. To maximise ITD

sensitivity, and provide spatial information that emphasises sound-sources, bCI processors

can during peak energy provide pulse bursts with spatial information derived milliseconds

earlier from the interaural cues soon after the preceding energy minimum. Calculation of

interaural cues might be triggered by time since a detected energy minimum, and a

proportional energy increase.

Conclusions

Suppressive biophysical mechanisms producing adaptation in the auditory brainstem

contribute to sound-source localisation, by promoting reliable spatial encoding despite

reverberation. The frequency-dependent emphasis of auditory spatial information conveyed in

early-arriving sound is consistent with brain mechanisms that transmit reliable information, and

suppress unreliable information. As the brainstem encodes interaural time differences for

determining sound-source locations, its suppression of late-arriving spatial information, by

short-term synaptic plasticity and K_{V1} channel activity, promotes accuracy and accounts for

typical frequency-profiles of reverberant energy in natural outdoor scenes.

More generally, our modelling of ion-channels yielding realistic resting potentials and

membrane time constants, within neurons spectro-temporally processing salient stimuli, is

available to any neuroscientist. Our findings may encourage further identification of brain

mechanisms that encode, enhance, and apply spatial information, including in the cortex.

Clinically, our suggested improvement for delivery of auditory spatial cues to listeners with

bilateral cochlear implants is intended to inspire application of rapidly updating binaural masks

[62] that enhance target sound-sources while preserving spatial cues.

Methods

Nonlinear brainstem model

This computational model (Fig. 2B) incorporates an MSO neuron and its excitatory input pathways including synaptic depression in the cochlear nuclei. Amplitude-modulated binaural beats (AMBBs) at 75 dB SPL rms at peak amplitude were applied as acoustic stimuli to the Zilany et al. auditory periphery model for humans [21,22] implemented in Matlab (www.mathworks.com), including 12 left and 12 right model adapting auditory nerve fibres of medium spontaneous rate, which project to depressing synaptic inputs on model SBCs in the ventral cochlear nuclei [23,26]. Three model auditory nerve fibres drive each model SBC. Four left and four right SBCs project non-depressing, excitatory synaptic inputs to a multi-compartment model MSO neuron [36] with recent updates. These model brainstem neurons are implemented as Hodgkin & Huxley models [24] in the Python 3.7 Brian2 Neural Simulator [63].

Model SBCs with synaptic depression

Spherical busy cells (SBCs) are modelled as point neurons [26], Type II compartment, adjusted for temperature 37°C) with three independent, excitatory synapses each driven by a model auditory nerve fibre. Each model synapse is an excitatory synaptic conductance in series with an excitatory reversal potential of 0 mV. Each input spike causes a variable increment in its synapse's excitatory conductance which decays exponentially with time constant 0.2 ms. The increment (i.e., the synaptic strength) is variable due to synaptic depression. Synaptic depression at the individual synapses is modelled as in Rudnicki and Hemmert [23]: immediately after an input spike and its associated increment in excitatory

conductance, the synaptic strength is multiplied by $1 - u$, where $u = 0.5$, comparable to

measurements *in vitro* [11–13]. This synaptic depression recovers with a single-exponential

function with time constant 25 ms [12].

Modelled synaptic depression contributed to realistic responses to AMBB stimuli, consistent

with low synchrony to AM in the auditory nerve at high SPL [64], and reduced synchrony in

primary-like neurons (including bushy cells) of the cochlear nuclei [65]. Compared with a single

input, three inputs per model SBC [66] increased spike rates, further reduced synchrony to

AM, and supported a realistically small number of excitatory inputs [67] to the model MSO

neuron.

Model MSO neuron

607 The model MSO neuron has separate compartments representing the bilateral dendrites,

608 soma, and axon of the neuron [68]. The soma is spherical and iso-potential. Best-ITD and

609 best-IPD are zero. Parameters for each compartment (Table 1) are explained below. Certain

610 parameters (Table 2) were adjusted for the four conditions yielding results shown in Figs. 3-4.

Table 1. Model MSO neuron parameters with membrane conductance at full value

611				
612	Parameter	Dendrites (2)	Soma (spherical)	Axon
613	Temperature (°C)	37	37	37
614	Number of sub-compartments	20	2	51
615	Diameter (μm)	3.5	30	2
616	Length (μm)	150	30	400
617	Resistivity, R_S (ohm x cm)	150	0 (iso-potential)	150
618	C_M (μF/cm^2)	1	1	1
619	V_{KLT} (mV)	-106	-106	-106
620	V_{Na} (mV)	n/a	-62.1	-62.1
621	V_H (mV)	-43	-43	-43
622	V_L (mV)	-60	-60	-65
623	$gmax_{KLT}$ (S/cm^2)	0.00132	0.0324	0.0595
624	$gmax_{Na}$ (S/cm^2)	0 (none)	0.0432	0.25
625	$gmax_H$ (S/cm^2)	0.00066	0.0216	0.0025
626	g_L (S/cm^2)	0.00005	0.00005	0.00005
627	V_E (mV)	0	n/a	n/a
628	$V_{AP\text{-}THRESHOLD}$ (mV, set)	n/a	n/a	-20
629	V_{REST} (mV)	-60.53	-60.52	-64.35

Table 2. Each column gives parameter values for one of the four cases explored.

Adjusted parameters were CF, synaptic strength and synaptic depression of inputs to SBCs, membrane conductance in MSO soma and dendrites, and MSO synaptic strength:

Results shown in	Fig. 3A	Fig. 3B	Fig. 4A	Fig. 4B
CF (Hz)	600	600	200	200
Model SBC excitatory synaptic parameters:				
Full Synaptic Strength, Δg_E (nS)	400	83	83	83
Synaptic Time Constant, τ_E (ms)	0.2	0.2	0.2	0.2
Depression, u	0 (none)	0.5	0.5	0.5
Recovery Time Constant (ms)	n/a	25	25	25
Model MSO membrane conductance factor and excitatory synaptic parameters:				
$g_{MEMBRANE}$ Factor	1	1	1	1/3
Membrane Time Constant (ms)	0.33	0.33	0.33	1.0
Synaptic Strength, Δg_E (nS)	21	36	36	18
Synaptic Time Constant, τ_E (ms)	0.4	0.4	0.4	0.4

Eight excitatory synapses are located on the model MSO bilateral dendritic membranes, one

each at 42.5, 47.5, 52.5, and 57.5% of the dendritic length. Each synapse is modelled as a

variable conductance (g_E) in series with an excitatory reversal potential (V_E) of 0 mV. The

synapses are non-depressing, and each is driven by a single model SBC from the same side.

An input spike increments its synaptic conductance by a fixed amount, and the conductance

then decays exponentially with time constant 0.4 ms. Synaptic strength (Δg_E), which is the

fixed conductance-increment, was adjusted according to CF, the overall membrane

conductance including g_{KLT}, and the presence or absence of synaptic depression in the

cochlear nuclei.

Within the model MSO neuron, its functional electric-circuit unit the sub-compartment (Fig. 2C)

connects to its neighbouring sub-compartments via series resistivity (R_S) representing the

neuron's internal cytoplasm. Within each sub-compartment, the neural membrane is modelled

as a transmembrane capacitance (C_M) in parallel with ion-channel populations: sodium ion

(Na$^+$) channels, hyperpolarisation-activated cyclic nucleotide (HCN, I_h) channels for non-

specific cations, and K_{LT} (K$_{V1}$) channels. Each ion-channel population is represented as a

reversal potential (V_{Na}, V_H, V_{KLT}) in series with a conductance (g_{Na}, g_H, g_{KLT}). With the

exception of a fixed leakage conductance (g_L) representing voltage-insensitive ion channels,

each conductance value is equal to a maximum conductance multiplied by voltage-sensitive

activation and inactivation gating variables with integer exponents [24].

Kirchhoff's current equation, applied to the model MSO neuron, states that the sum of the

membrane and series currents exiting any point in the model neuron is zero:

666
$$0 = i_{C_M} + i_{Na} + i_{K_{LT}} + i_H + i_L + i_{S1} + i_{S2}$$

Series currents, i_{S1} and i_{S2}, are calculated by the Brian2 simulator according to the voltage

differences, resistivity, and geometry of the related sub-compartments.

Capacitive membrane current (i_{C_M}) increases with membrane capacitance and the time-

derivative of membrane potential V:

$i_{C_M} = C_M \frac{dV}{dt}$.

Leakage current: $i_L = g_L(V - V_L)$.

Sodium current [27]: $i_{Na} = g_{Na}(V - V_{Na})$.

Na$^+$ conductance: $g_{Na} = gmax_{Na}m^4(0.993h + 0.007)$.

Each voltage-sensitive ionic conductance has a constant maximum conductance value ($gmax$)

(Table 1), and has voltage and time dependencies defined by a subset of the

activation/inactivation variables m, h, w, z, and r, each with a rate of change governed by a

first-order differential equation with a time constant divided by the Q_{10} temperature factor of $3^{(T}$

$^{-22)/10}$, where T is set equal to human body temperature, 37°C. For sodium:

$\frac{dm}{dt} = Q_{10}(m_\infty - m)/\tau_m$

$\frac{dh}{dt} = Q_{10}(h_\infty - h)/\tau_h$

For model Na$^+$ channels, steady-state activation (m_∞) and inactivation (h_∞), and their

respective time constants (τ_m and τ_h) in milliseconds, are functions of membrane potential in

millivolts, equal to those in Scott et al. [27]:

$m_\infty = 1./(1 + \exp((V + 46.) / (-11.)))$

$\tau_m = ((0.141 + (-0.0826 / (1 + \exp((-20.5 - V) / 10.8)))) / 3.)$

$h_\infty = 1./(1 + \exp((V + 62.5) / 7.77))$

$\tau_h = ((4. + (-3.74 / (1 + \exp((-40.6 - V) / 5.05)))) / 3.)$

K_{LT} current [15]:

$i_{KLT} = g_{KLT}(V - V_{KLT}).$

$g_{KLT} = gmax_{KLT}w^4z.$

$\dfrac{dw}{dt} = Q_{10}(w_\infty - w)/\tau_w$

$\dfrac{dz}{dt} = Q_{10}(z_\infty - z)/\tau_z$

$w_\infty = 1./(1 + \exp((V + 57.34)/(-11.7)))$

$\tau_w = ((21.5/((6.* \exp((V + 60.)/7.)) + (24.* \exp(-1 * (V + 60.)/50.6)))) + 0.35)$

$k = 0.27$

$z_\infty = ((1. - k)/(1 + \exp((V + 67.)/6.16))) + k$

$\tau_z = ((170./(5.* \exp((V + 60.)/10.) + \exp((V + 70.)/8.))) + 10.7)$

Non-inactivating HCN current [26]:

$i_H = g_H(V - V_H).$

$g_H = gmax_H r .$

$\dfrac{dr}{dt} = Q_{10}(r_\infty - r)/\tau_r$

$r_\infty = 1./(1 + \exp((V + 76.)/7.))$

$\tau_r = ((100000./(237.*\exp((V + 60.)/12.) + 17.*\exp(-(V + 60.)/14.))) + 25.)$.

Approach for setting maximum conductance values of MSO ion-channels

By selecting equilibrium membrane potentials (V_{REST}) and equilibrium ratios of i_{Na} to i_H to i_{KLT}

in each compartment (0:1:-1 in dendrites; 1:4:-5 in soma, 1:1:-2 in axon), and knowing C_M and

membrane time constants, the current equation yielded a maximum conductance value for

each ion-channel in each compartment that produced: K_{LT} activation in dendrites and soma;

Na^+ inactivation in soma; Na^+ not inactivated in axon.

Model MSO membrane time constants

In the resulting model MSO neuron of this study, with bias current to centre the somatic

membrane potential at -57.6 mV, slightly above V_{REST}, the somatic membrane impedance

magnitude as a function of frequency was lowpass with a resonance at 480 Hz. Although this

resonance frequency is slightly higher than typical for MSO neurons [20,69], this 480-Hz

resonance frequency multiplied by 2π converts to an angular frequency of 3016 radians/s, with

its reciprocal yielding a membrane time constant of 0.33 ms that is within the range of MSO

neurons [70]. For AMBB stimulation centred at 200 Hz, to reflect the range of MSO membrane

speeds at very low CF [30], slower somatic and dendritic membranes were also modelled by

dividing the fast membrane conductances by three to yield a somatic membrane time constant

of approximately 1 ms.

AMBB period histograms

For each AMBB period histogram from the nonlinear model, spikes were counted in forty non-

overlapping bins, each covering 1/40 of the AM cycle. Histograms showing results from the

725 nonlinear model were not smoothed. Spike rates were calculated by dividing the spike count

726 by the total time duration for each bin, across the multiple periods of eight different stimulus

727 presentations of 0.75-second duration.

728 *Eight starting-phases at decrements of 45° efficiently implemented IPDs*

729 At each carrier and modulation-frequency combination, 8 acoustic stimuli, each with 1 of 8

730 carrier *starting-phases* (0°, -45°, -90°, …, -315°), were applied at each model ear, driving

731 auditory nerve fibres. For computational efficiency, *start-IPD* (the IPD at zero amplitude) was

732 achieved by pairing spike times from each *starting-phase* in one ear, with the spike times from

733 the other ear having the appropriate difference in *starting-phase*. While maintaining the proper

734 *start-IPD*, each AMBB period histogram pooled spikes resulting from stimuli using the 8

735 *starting-phases* spanning each carrier period. Thus whilst the histograms show the effects of

736 *start-IPD*, they do not show phase-locking to fine structure of the carriers.

737 In this study, "best-ITD during rise" denotes *start-IPD* = 270°; "best-ITD at peak" denotes *start-*

738 *IPD* = 180°; and "best-ITD during fall" denotes *start-IPD* = 90°.

739 *Chi-squared tests for significant differences in model spike counts*

740 For each condition and modulation frequency, a chi-squared test for one and two degrees of

741 freedom (2-way and 3-way comparisons) compared spike counts from the nonlinear model

742 MSO neuron stimulated with AMBBs with best-ITD occurring during rising vs. peak vs. falling

743 amplitude. Each chi-squared test yielded a probability (*p*) of the null hypothesis that the

744 differences in spike count occurred randomly.

Synchrony index and Rayleigh statistic for significant phase-locking:

For each modulation frequency and *starting-phase* combination, the synchrony index (*SI, R*) of

spike times (t_i) [71] with respect to their phase θ_i within the AM cycle (with modulation

frequency f_m and modulation period $T_m = 1/f_m$) was calculated:

$\theta_i \triangleq 2\pi f_m mod(t_i, T_m)$

$SI = \sqrt{(\sum_{i=1}^{N} \cos \theta_i)^2 + (\sum_{i=1}^{N} \sin \theta_i)^2}$, where N is the spike count.

The Rayleigh significance statistic (*2NR²*) was then calculated and converted to a *p* value, the

probability of the null hypothesis that the AM period-histogram of spike times resulted from a

uniform distribution [72]:

p   0.10   0.05   0.025   0.01   0.001

2NR²   4.605   5.991   7.378   9.210   13.816

Lateralisation model including linear-membrane models

To study how synaptic adaptation and biophysical profiles could impact lateralisation of

acoustic stimuli in anechoic and reverberant conditions, we constructed a model of

lateralisation whose brainstem stages (SBCs and MSO neurons) are represented by point

neurons with linear biophysical properties [20]. Two stimuli were presented to the model: the

first, a SAM tone with non-zero ITDs inserted at different phases of the AM cycle, as used

behaviourally to determine how carrier frequency affects ITD sensitivity over the time course of

an AM cycle [9]; the second, a natural speech stimulus with early reflections, has been

proposed as a simple simulation of a reverberant environment where correct lateralisation is

only possible if ITD cues in the onset waveform are processed preferentially [4].

SAM tones with non-zero ITDs inserted at different phases of AM cycle

This stimulus was generated according to the Hu et al. study [9] that first used it. In summary, SAM tones were created from pulse trains that had been bandpass-filtered and then amplitude-modulated. Non-stationary ITDs were added by temporally shifting individual pulses in one of either the rising, peak or falling phases of the AM cycle. For the purposes of this study, non-stationary ITDs of +300 µs and +150 µs were inserted into SAM tones of either 200-Hz or 600-Hz carrier frequency respectively. These ITD values were chosen based on individual behavioural thresholds in the Hu et al. study [9]. At each carrier frequency, four conditions were tested: two different AM frequencies (8 Hz or 20 Hz) and two different proportions of rising, peak or falling AM phases with a non-zero ITD inserted (20% or 40%). These parameters match those tested behaviourally by [9].

A natural speech stimulus with early reflections

A single monosyllabic consonant-vowel nucleus-consonant (CNC) word token, 'church', (spoken by an Australian-English, female voice), was selected as a stimulus (Fig. 1 and Fig. 8). To simulate its arrival from a location one metre away to the right of the midline in an anechoic environment, the word's waveform (normalised at 70dB) was convolved with a large pinnae HRTF for +30° azimuthal location (CIPIC database, UC Davis). A reverberant space was simulated by adding to the direct (+30°) pathway two early reflections off virtual walls stood behind and to the right of the subject (Fig. 1). These reflected copies of the words arrived from -65° and -130° angles (again convolved with large-pinnae HRTFs from the CIPIC database) and were delayed by 4ms and 8ms respectively to reproduce their elongated paths [4].

Linear model circuitry

The linear model, like its nonlinear counterpart, consists of three stages: an initial auditory

periphery stage (the middle/inner ear and auditory nerve fibres) and two brainstem stages

(cochlear nuclei and MSO). Unlike the nonlinear model however, the linear model incorporates

two parallel circuits, representing the 'left' and 'right' MSO nuclei and their inputs. The

difference in output rate between these parallel circuits is utilised to calculate lateralisation of

the natural stimulus. The only discernible difference between 'left' and 'right' circuits is the

contralateral $\frac{1}{8}$ pi shifts in their MSO neurons' IPD tuning curve peaks which are generated by

delaying the outputs from the auditory periphery stage ipsilateral to the MSO nucleus in

question. This shift is considered physiological given experimentally observed binaural tuning

curves from the auditory brainstem whose optimal characteristics have been corroborated

theoretically [34].

Auditory periphery stage

Peripheral processing of the acoustic stimuli in the linear model is performed using an

implementation of the Zilany et al. [21] cat middle/inner ear model in Matlab. Outputs from the

auditory periphery are restricted to 200-Hz/ 600-Hz for the pulse-shifted SAM tones (matching

their SAM tone's carrier frequency) and 600-Hz for lateralisation of the speech stimulus with

early reflections. This latter value was chosen based on it laying in the middle of the 500-750

Hz frequency range in which TFS-ITD sensitivity is considered strongest [37]. When exploring

effects, of synaptic depression at the inputs from auditory nerve to cochlear nucleus, on the

lateralisation of a speech stimulus, the same auditory periphery simulations are used for both

the depressing and non-depressing inputs to the cochlear nuclei.

Linear-membrane model properties

Single-compartment, linear-membrane models are used to represent both SBC and MSO

neurons in the linear model. These linear-membrane models can incorporate two dynamic

currents as previously described in [20]: I_w, a resonant current and/or, I_n, an amplifying current.

The current balance equation for the general neural model is as follows:

815
$$c\frac{dv}{dt} = -g_M v - g_w w_w + g_n w_n + I_{app}(t)$$

816　Where c is capacitance (picofarads), g_M is total membrane conductance (nanosiemens) and

817　I_{app} is the current (picoamperes) applied to the neural model. The resonant and amplifying

818　currents, I_w and I_n, are described by their conductances, g_W and g_n (in nanosiemens); the

819　dynamics of their gating variables, w_w and w_n (in millivolts) are described generically by the

820　equation:

821
$$\tau_w \frac{dw_w}{dt} = v - w_w$$

822
$$\tau_w \frac{dw_w}{dt} = v - w_w$$

Where w_x is the gating variable whose associated time constant is τ_x (milliseconds).

Two parameter sets are chosen to represent the apparent bimodality of subthreshold

biophysical properties in the gerbil MSO *in vitro* [30]. These example models can be broadly

characterised by their impedance profiles as either band-pass with a high resonant-frequency

or band-pass with a low resonant-frequency [20]. While the band-pass model with a high-

resonant frequency is exclusively chosen to represent SBCs, both model types are used to

represent MSO neurons.

 Synaptic properties and adaptation

As in the nonlinear model, 3 independently-simulated auditory nerve fibres provide excitatory

drive to each SBC in the linear model. Excitatory unitary conductances at this synapse are

modelled as alpha functions with an exponential time course of 0.2ms. Synaptic depression

with a single exponential recovery is also implemented at this stage, matching the adaptation

observed in the nonlinear model functionally thanks to its similar parameters (u = 0.55; τ = 25

ms).

Each MSO neuron receives 4 (independently-simulated) excitatory cochlear-nucleus inputs

from "either ear" in the linear model. Alpha functions are again used to model the unitary

excitatory conductances at this synapse with time courses selected relative to the resonant

class of the MSO in question (i.e. band-pass with high resonant-frequency: 0.2ms; band-pass

with low resonant-frequency: 0.5ms). This increase in synaptic time course is performed to

reflect the slower membrane time constant associated with neurons displaying little or no

resonance at all. If, as expected, MSO neurons with slower intrinsic properties still segregate

inputs from either ear on either dendrite then the increased electrotonic propagation of

excitatory inputs somatopetally should lead to slower excitatory potentials at their somata.

Where comparisons of the two MSO resonant classes are made, the same adapting auditory

nerve inputs are presented to their respective cochlear-nucleus stages, therefore reducing any

potential confusion that might result from variability in the peripheral model's output.

Spike thresholds in the linear-membrane model

Idealised thresholds for the linear-membrane model are implemented from Remme et al. [20].

A slope threshold (dv/dt) is used for all neuronal types. Threshold values for cochlear-nucleus

cells are selected to produce good average firing rate without undermining the effects of

synaptic depression. Threshold values for the MSO neurons are selected to obtain maximum

dynamic range of ITD tuning functions for 200/600 Hz pure tone stimuli (where dynamic range

is considered the difference between the maximum and minimum ITD-modulated spike rate). A

refractory period of 1 ms is implemented as in Remme et al. [20] for cochlear-nucleus neurons

and MSO neurons with a high-resonant frequency whereas a longer refractory period of 2 ms

is used for the MSO neurons with low-resonant frequency, reflecting longer refractory periods

in neurons with lower densities of K_{LT} channels [19,26,73].

Calculating lateralisation using d' values

Lateralisation of a reverberant natural stimulus is judged in the linear model by calculating the

mean spike rate difference between a population of 50 'left' and 50 'right' MSO neurons to a

single stimulus presentation. d' values are calculated to quantify the degree of separation of

'left' and 'right' spike rates using the following equation:

865
$$d' = \frac{\mu_L - \mu_R}{\sqrt{\frac{1}{2}(\sigma_L^2 + \sigma_R^2)}}$$

Where μ_L is the mean spike rate for the 'left' population of MSO neurons in 5-ms bins; μ_R is the

mean spike rate for the 'right' population of MSO neurons in 5-ms bins; σ_L is the standard

deviation of the 'left' MSO population's spike rate and σ_R is the standard deviation of the 'right'

population's spike rate (both calculated in 5-ms bins again).

The sign and magnitude of the d' allows judgement of whether the linear model lateralises the

reverberant stimulus to the correct direction (negative d' values denote negative ITDs/left of

midline; positive d' values denote positive ITDs/right of midline) and whether this lateralisation

judgment is considered significant ($d' > 1$ or $d' < -1$ indicated a significant lateralisation in the

right and left directions respectively).

ANOVA and T-test for significant differences in lateralisation

Two-way and three-way ANOVAs are implemented to compare the duration of correct

lateralisations (time correctly lateralised = bin duration x number of bins where $d' > 1$) by the

hemispheric model of SAM tones with non-zero ITDs in either the rising, peak or falling phases

as well as the percentage of the phase including a non-zero ITD. A two-tailed T-test is also

performed for 200-Hz carrier SAM tones to compare the effect of MSO neuronal type. For the

speech stimulus, a paired two-tailed T-test is performed to compare the frequency of incorrect

lateralisations (time incorrectly lateralised = bin duration x number of bins where $d' < -1$) in the

linear model with either adapting or non-adapting auditory nerve inputs.

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1099 **Figures**

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1103 **Figure 1 [in colour, online and in print]**

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A

B Nonlinear Brainstem Model

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1111   **Figure 3 [in colour, online and in print]**

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1115   **Figure 4 [in colour, online and in print]**

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$$d' = \frac{\mu_{LeftMSO} - \mu_{RightMSO}}{\sqrt{\frac{1}{2}(\alpha^2_{LeftMSO} + \alpha^2_{RightMSO})}}$$

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1119 **Figure 5 [in colour, online and in print]**

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1123 **Figure 6 [in colour, online and in print]**

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1127 **Figure 7 [in colour, online and in print]**

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ANECHOIC

REVERBERANT

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1131   **Figure 8 [in colour, online and in print]**