

Neurological disorder drug discovery from gene expression with tensor decomposition

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Abstract

Background: Identifying effective candidate drug compounds in patients with neurological disorders based on gene expression data is of great importance to the neurology field. By identifying effective candidate drugs to a given neurological disorder, neurologists would (1) reduce the time searching for effective treatments; and (2) gain additional useful information that leads to a better treatment outcome. Although there are many strategies to screen drug candidate in pre-clinical stage, it is not easy to check if candidate drug compounds can be also effective to human.

Objective: We tried to propose a strategy to screen genes whose expression is altered in model animal experiments to be compared with gene expressed differentially with drug treatment to human cell lines.

Methods: Recently proposed tensor decomposition (TD) based unsupervised feature extraction (FE) is applied to single cell (sc) RNA-seq experiments of Alzheimer's disease model animal mouse brain.

Results: Four hundreds and one genes are screened as those differentially expressed during $A\beta$ accumulation as age progresses. These genes are significantly overlapped with those expressed differentially with the known drug treatments for three independent data sets: LINCS, DrugMatrix and GEO.

Conclusion: Our strategy, application of TD based unsupervised FE, is useful one to screen drug candidate compounds using scRNA-seq data set.

keywords: Amyloid, Alzheimer Disease, Gene Expression, Single-Cell Analysis, Drug Discovery, Cell Line

1 Introduction

Drug discovery for neurological disorder has never been successful in spite of massive efforts spent [1]. One possible reason is because we generally do not

28 have suitable model animals for human neurological disorder [2]. Although a
29 huge number of compounds are screened using model animals, only a few of
30 them passed the human level screening. In this sense, it is required to screen
31 candidate compounds using information retrieved from human at the earliest
32 stage. One possible strategy to do this is the usage of human cell lines; Nev-
33 ertheless, it is also not easy to perform, since generating cell line from human
34 neurological disorder patients is not easy. In contrast to the cancer cell lines,
35 which can be easily generated by immortalizing tumor cells, neuronal cells are
36 hardly converted to cell lines, since mature neurons do not undergo cell divi-
37 sion [3]. Therefore, it is difficult to test if candidate drugs work for human
38 during pre-clinical stages.

39 In order to overcome this difficulty, we proposed an alternative strategy; com-
40 paring disease gene expression with that of compound treated animals and/or
41 human cell lines. Generally, compound screening is based upon phenotype; i.e.,
42 evaluation of compounds efficiency is tested based upon if drug treatment can
43 produce symptomatic improvement. Nevertheless, since it has been recently
44 found that various neurological disorders share gene expression [4], focusing on
45 gene expression profiles might be more reasonable. Following this strategy, we
46 considered gene expression profiles (single cell RNA-seq) of mouse brain during
47 amyloid β accumulation. As being aged, some set of gene expression progresses
48 and significantly overlaps with genes that express differential expression caused
49 by various compounds treatment. Since top ranked (i.e., with the most overlaps)
50 detected compounds turn out to be tested previously toward Alzheimer disease
51 (AD) treatment, lower ranked compounds also might be promising candidate
52 compounds for AD.

53 Expression levels exhibit variations of scRNA-seq data used in this study
54 due to contributions specific to genotypes, tissues, ages, sex, plates, wells, and
55 interactions thereof. Hence, classical unsupervised decomposition methods are
56 not well-suited to explore the six-way interactions and struggle to extract in-
57 sights from data, hindering the process of finding effective drug compounds of
58 a neurological disorder.

59 **Contributions.** Our contributions over existing work are summarized as
60 follows:

- 61 – Whilst the application of tensor decomposition (TD) to the neurology
62 domain is not new, previous developments, to the best of our knowledge,
63 facilitated the neurological drug discovery process are not relevant to mod-
64 eling the several interactions of scRNA-seq data used in this work. Our
65 proposed tensor decomposition formalism is new, targeting neurological
66 drug discovery of AD and constitutes a main contribution of this work.
- 67 – We present findings on an AD with a tensor decomposition formalism
68 demonstrating the effectiveness of finding compounds for the treatment of
69 AD.
- 70 – As similar to tensor decomposition techniques, the utilized tensor decom-
71 position technique works under the unsupervised learning setting which is

72 more time effective than previous deployments that work under different
73 learning settings, including the supervised learning setting.

74 – Unlike traditional machine and deep learning approaches that provide so-
75 lutions to artificial intelligence when applied to plenty of neurological dis-
76 order problems, our approach blends techniques from linear algebra and
77 statistics to yield a tensor decomposition technique utilizing a statistical
78 linear algebra approach, requiring much less computational resources and
79 time to reach a solution [5–7].

80 **Organization.** The rest of the paper is organized as follows. Section 2 intro-
81 duces the tensor decomposition technique and the provided data to be analyzed.
82 Section 3 presents the experimental results, followed by Section 4 to discuss the
83 results. Section 5 concludes the work and points out future direction.

84 2 Materials and Methods

85 2.1 Single cell RNA-seq

86 Single cell (sc) RNA-seq used in this study was downloaded from gene expression
87 omnibus (GEO) using GEO ID GSE127892. It is composed of two genotypes
88 (APP_NL-F-G and C57Bl/6), two tissues (Cortex and Hippocampus), four ages
89 (3, 6, 12, and 21 weeks), two sex (male and female) and four 96 well plates.
90 For each of combined combinations, four 96 well plates, each of wells includes
91 one cell, were tested. Among those wells tested, wells with insufficient gene
92 expression were discarded. As a result, among 2 (genotype) \times 2 (tissues) \times
93 4 (ages) \times 2 (sex) \times 4 (plates) \times 96 (wells) = 12288 cells measured, scRNA-seq
94 for only 10801 cells were provided.

95 2.2 Tensor decomposition based unsupervised feature ex- 96 traction

97 We applied recently proposed TD based unsupervised feature extraction (FE) [8–
98 18] to scRNA-seq. A tensor $x_{j_1 j_2 j_3 j_4 j_5 j_6 i} \in \mathbb{R}^{96 \times 2 \times 2 \times 4 \times 2 \times 4 \times 29341}$ that repre-
99 sents gene expression of i th gene of j_1 th cell (well) at j_2 th genotyoe ($j_2 =$
100 1:APP_NL-F-G and $j_2 = 2$: C57Bl/6), j_3 th tissue ($j_3 = 1$:Cortex and $j_3 = 3$:
101 2:Hippocampus), j_4 th age ($j_4 = 1$: three weeks, $j_4 = 2$: six weeks, $j_4 = 3$:
102 twelve weeks, and $j_4 = 4$: twenty one weeks), j_5 th sex ($j_5 = 1$:female and
103 $j_5 = 2$:male) and j_6 th plate.

104 $x_{j_1 j_2 j_3 j_4 j_5 j_6 i}$ is standardized such that $\sum_{i=1}^{29341} x_{j_1 j_2 j_3 j_4 j_5 j_6 i} = 0$ and $\sum_{i=1}^{29341} x_{j_1 j_2 j_3 j_4 j_5 j_6 i}^2 =$
105 29341. HOSVD [9] was applied to $x_{j_1 j_2 j_3 j_4 j_5 j_6 i}$ such that

$$x_{j_1 j_2 j_3 j_4 j_5 j_6 i} = \sum_{\ell_1=1}^{96} \sum_{\ell_2=1}^2 \sum_{\ell_3=1}^2 \sum_{\ell_4=1}^4 \sum_{\ell_5=1}^2 \sum_{\ell_6=1}^4 \sum_{\ell_7=1}^{29341} G(\ell_1, \ell_2, \ell_3, \ell_4, \ell_5, \ell_6, \ell_7) u_{\ell_1 j_1} u_{\ell_2 j_2} u_{\ell_3 j_3} u_{\ell_4 j_4} u_{\ell_5 j_5} u_{\ell_6 j_6} u_{\ell_7 i} \quad (1)$$

106 where $G(\ell_1, \ell_2, \ell_3, \ell_4, \ell_5, \ell_6, \ell_7) \in \mathbb{R}^{96 \times 2 \times 2 \times 4 \times 2 \times 4 \times 29341}$ is core tensor, $u_{\ell_1 j_1} \in$
107 $\mathbb{R}^{96 \times 96}$, $u_{\ell_2 j_2} \in \mathbb{R}^{2 \times 2}$, $u_{\ell_3 j_3} \in \mathbb{R}^{2 \times 2}$, $u_{\ell_4 j_4} \in \mathbb{R}^{4 \times 4}$, $u_{\ell_5 j_5} \in \mathbb{R}^{2 \times 2}$, $u_{\ell_6 j_6} \in$
108 $\mathbb{R}^{4 \times 4}$ and $u_{\ell_6 i} \in \mathbb{R}^{29341 \times 29341}$ are singular value matrices that are orthogonal
109 matrices. In order to save time to compute, only $1 \leq \ell_1, \ell_7 \leq 10$ were computed
110 (The reason for utilizing specifically HOSVD in this research will be discussed
111 in the discussion section, because it is difficult to explain the reason before
112 demonstrating how we make use of TD for data analysis).

113 After investigation of $u_{\ell_4 j_4}$, $u_{2 j_4}$ represent monotonic dependence upon age
114 while $\ell_1, \ell_2, \ell_3, \ell_5, \ell_6 = 1$ represent independence of cells, genotype, tissue,
115 sex and plate. Since $G(1, 1, 1, 2, 1, 1, 2)$ has the largest absolute vales among
116 $G(1, 1, 1, 2, 1, 1, \ell_7)$, u_{2i} is employed to compute P -values attributed to i th gene
117 as

$$P_i = P_{\chi^2} \left[> \left(\frac{u_{2i}}{\sigma} \right)^2 \right] \quad (2)$$

118 where $P_{\chi^2}[> x]$ is the cumulative probability of χ^2 distribution when the argu-
119 ment is larger than x and σ is the standard deviation.

120 P -values are corrected by Benjamini and Hochberg criterion [19] and genes
121 associated with corrected P -values less than 0.01 are selected for downstream
122 analysis.

123 2.3 Enrichment analysis

124 Four hundreds and one genes selected by TD based unsupervised FE were up-
125 loaded to Enrichr [20] for enrichment analysis. Full list of enrichment analysis
126 as well as list of 401 genes are accessible at
127 <https://amp.pharm.mssm.edu/Enrichr3/enrich?dataset=5bbbe5602715daf9787895cd16829707>

128 List of 401 genes and three enrichment analyses used in this study, “LINCS
129 L1000 Chem Pert up”, “DrugMatrx” and “Drug Perturbations from GEO up”
130 are also available as supplementary material.

131 3 Results

132 As an unsupervised technique applied to scRNA-seq data set, we employ tensor
133 decomposition [21] that was sometimes applied to gene expression analysis [22].

134 3.1 Synthetic study of TDs

135 Before performing TD based unsupervised FE, we perform some synthetic study
136 for some TDs.

137 We prepared two synthetic data sets, $x_{ijk} \in \mathbb{R}^{N \times N \times N}$ defined as

$$x_{ijk} = v_i v_j v_k + v'_i v'_j v'_k \quad (3)$$

138 where $v'_i = v_{i+1}$ for $i \leq N - 1$ and $v'_N = v_1$.

139 For data set 1 (Fig. 1(A) and (B)),

$$v_i = \begin{cases} 0 & 1 \leq i \leq \frac{N}{2} \\ 1 & \frac{N}{2} < i \leq N \end{cases} \quad (4)$$

140 and for data set 2 (Fig. 1(C) and (D)).

$$v_i = i \quad (5)$$

141 We apply HOSVD, CP decomposition and CMTF [23] to these two synthetic
142 data set with $N = 10$. At first, we applied HOSVD to data set 1 and 2 as

$$x_{ijk} = \sum_{\ell_1=1}^N \sum_{\ell_2=1}^N \sum_{\ell_3=1}^N G(\ell_1, \ell_2, \ell_3) u_{\ell_1 i}^{(i)} u_{\ell_2 j}^{(j)} u_{\ell_3 k}^{(k)} \quad (6)$$

143 where $G(\ell_1, \ell_2, \ell_3), u_{\ell_1 i}^{(i)}, u_{\ell_2 j}^{(j)}, u_{\ell_3 k}^{(k)} \in \mathbb{R}^{N \times N \times N}$. Then, we noticed that only four
144 G s with $(\ell_1, \ell_2, \ell_3) = (1, 1, 1), (1, 2, 2), (2, 1, 2), (2, 2, 1)$ have non zero values for
145 both data set 1 and 2. Figs. 2 and 3 show $u_{\ell_1 i}^{(i)}, u_{\ell_2 j}^{(j)}, u_{\ell_3 k}^{(k)}$ and

$$\sum_{(\ell_1, \ell_2, \ell_3) \in \{(1,1,1), (1,2,2), (2,1,2), (2,2,1)\}} G(\ell_1, \ell_2, \ell_3) u_{\ell_1 i}^{(i)} u_{\ell_2 j}^{(j)} u_{\ell_3 k}^{(k)} \quad (7)$$

146 It is obvious that HOSVD successfully performs TD (Figs. 2(C) and 3(C))
147 although obtained singular value vectors (Figs. 2(A) and (B) and 3(A) and
148 (B)) are not equivalent to Fig. 1 because HOSVD assumes the orthogonality
149 between singular value vectors. The first singular value vectors, $u_{1j}^{(j)}, u_{1i}^{(i)}, u_{1k}^{(k)}$
150 (Figs. 2(A) and 3(A)), clearly represent somewhat means of \mathbf{v} (Figs. 1(A) and
151 1(C)) and \mathbf{v}' (Figs. 1(B) and 1(D)) while the second singular value vectors,
152 $u_{2j}^{(j)}, u_{2i}^{(i)}, u_{2k}^{(k)}$ (Figs. 2(B) and 3(B)), clearly represent difference of them.

153 Next, we applied CP decomposition to data set 1 and 2: eqs. (4) and (5)
154 (Fig. 1). It is obvious that CP decomposition (Fig. 4) applied to data set 1
155 successfully reproduced (Fig. 4(A) and (B)) eq. (3) with eq. (4) (Fig. 1(A) and
156 (B)). On the other hand, CP decomposition (Fig. 5) applied to data set 2 could
157 not, but required up to the third singular value vectors (Fig. 5(A), (B) and
158 (C)). Since CP decomposition depends upon initial values, although we tried
159 multiple initial values, as far as we tried, we could not find the initial values
160 by which CP decomposition can reproduce eq. (3) using eq. (5) (Fig. 1(C)
161 and (D)). In contrast to HOSVD that clearly decomposed \mathbf{v} and \mathbf{v}' into their
162 mean and difference, it is unclear what Fig. 5 represents anymore. Thus, it is
163 obvious whether CP decomposition can perform better than HOSVD is highly
164 dependent upon the data set we analyze. In this sense, HOSVD is less affected
165 by the type of data set analyzed.

166 Finally, we applied CMTF to data sets 1 and 2 (Fig. 1). In order that, we
167 need to specify loss function, f , to be minimized;

$$f(U^{(i)}, U^{(j)}, U^{(k)}, \mathbf{a}^{(i)}, \mathbf{a}^{(j)}, \mathbf{a}^{(k)}) = \sum_{ijk} \left| x_{ijk} - \sum_{\ell=1}^R u_{\ell i}^{(i)} u_{\ell j}^{(j)} u_{\ell k}^{(k)} \right|^2$$

$$\begin{aligned}
 & + \sum_i \left| v_i - \sum_{\ell=1}^R a_{\ell}^{(i)} u_{\ell i}^{(i)} \right|^2 \\
 & + \sum_j \left| v_j - \sum_{\ell=1}^R a_{\ell}^{(j)} u_{\ell j}^{(j)} \right|^2 \\
 & + \sum_k \left| v_k - \sum_{\ell=1}^R a_{\ell}^{(k)} u_{\ell k}^{(k)} \right|^2 \tag{8}
 \end{aligned}$$

168 where $U^{(i)}, U^{(j)}, U^{(k)} \in \mathbb{R}^{N \times R}$ are defined as

$$U^{(i)} = \left(\mathbf{u}_1^{(i)}, \dots, \mathbf{u}_R^{(i)} \right) \tag{9}$$

$$U^{(j)} = \left(\mathbf{u}_1^{(j)}, \dots, \mathbf{u}_R^{(j)} \right) \tag{10}$$

$$U^{(k)} = \left(\mathbf{u}_1^{(k)}, \dots, \mathbf{u}_R^{(k)} \right) \tag{11}$$

169 with $\mathbf{u}_{\ell}^{(i)}, \mathbf{u}_{\ell}^{(j)}, \mathbf{u}_{\ell}^{(k)} \in \mathbb{R}^N$ defined as

$$\mathbf{u}_{\ell}^{(i)} = \begin{pmatrix} u_{\ell 1}^{(i)} \\ \vdots \\ u_{\ell N}^{(i)} \end{pmatrix} \tag{12}$$

$$\mathbf{u}_{\ell}^{(j)} = \begin{pmatrix} u_{\ell 1}^{(j)} \\ \vdots \\ u_{\ell N}^{(j)} \end{pmatrix} \tag{13}$$

$$\mathbf{u}_{\ell}^{(k)} = \begin{pmatrix} u_{\ell 1}^{(k)} \\ \vdots \\ u_{\ell N}^{(k)} \end{pmatrix} \tag{14}$$

170 With coefficient vectors, $\mathbf{a}^{(i)}, \mathbf{a}^{(j)}, \mathbf{a}^{(k)} \in \mathbb{R}^R$, \mathbf{v} is required to be expressed by
 171 the linear transformation of $U^{(i)}, U^{(j)}, U^{(k)}$.

172 After trying to apply CMTF with $R = 2$ (because we know $R = 2$ is
 173 enough because of eq. (3)) to data sets 1 and 2, we realized that it is rare
 174 that CMTF converges to global minimum when starting from initial values,
 175 $U^{(i)}, U^{(j)}, U^{(k)}, \mathbf{a}^{(i)}, \mathbf{a}^{(j)}, \mathbf{a}^{(k)}$, drawn from $\mathcal{N}(\mu, \sigma)$ where $\mathcal{N}(\mu, \sigma)$ is normal dis-
 176 tribution having mean of μ and standard deviation of σ . After trying several
 177 tens of ninital values, we got the results shown in Figs. 6 and 7. It is obvious
 178 that CMTF performed quite well as far as it converges. $\mathbf{u}_1^{(i)}, \mathbf{u}_1^{(j)}, \mathbf{u}_1^{(k)}$, (Figs.
 179 6(A) and 7(A)) correspond to \mathbf{v} (Fig. 1(A) and (C)) while $\mathbf{u}_2^{(i)}, \mathbf{u}_2^{(j)}, \mathbf{u}_2^{(k)}$ (Figs.
 180 6(B) and 7(B)), correspond to \mathbf{v}' (Fig. 1(B) and (D)) as expected. On the other
 181 hand, it is problematic that CMTF rarely converges to global minimum. In order
 182 to improve this points, we replaced ALS employed in CMTF with BFGS.

183 Now CMTF came to converge to global minimum (Figs. 8 and 9) with starting
184 any initial values drawn from $\mathcal{N}(0, 1)$ as long as we tried. Thus, we decided to
185 apply CMTF with replacing ALS with BFGS.

186 Although CMTF looks the best method to apply, CMTF has one problem:
187 cpu time required to perform CMTF. Table 1 shows the list of cpu time required
188 when various methods are applied to data set 1 and 2. It is obvious that HOSVD
189 is the fastest since it does not require any iterations. CP decomposition is a
190 bit slower than HOSVD, since it requires ALS to converge. CMTF is much
191 more slower no matter which methods, ALS or BFGS, are employed for the
192 minimization. As far as we deal with small data set, this difference is not critical.
193 Nevertheless, when we have to deal with a massive data set, this difference is
194 critical. Although CMTF is slower than HOSVD by only several hundreds times,
195 this difference is generally enhanced when the data set becomes larger. Since
196 the cpu time required for HOSVD also increases as data set grows, it might be
197 unrealistic to perform CMTF for much larger data set.

198 Before applying TDs to real data set, we summarize the results here.

- 199 • HOSVD is the fastest and its outcome is not affected by the type of data
200 set much. Nevertheless, because of the orthogonality requirement, it has
201 less ability to derive the structure of the original data set, eq. (3), if the
202 vectors used to generate tensor are not orthogonal to each other.
- 203 • CP decomposition is the second fastest method and can reproduce the
204 structure of original data set, eq. (3) (Fig. 4). Nonetheless, CP decom-
205 position might fail dependent upon data set (Fig. 5).
- 206 • The original CMTF can successfully reproduce the data structure, eq. (3).
207 On the other hand, it is the slowest method and requires to search initial
208 values that converges to global minimum.
- 209 • With replacing ALS with BFGS, CMTF comes to converge to global min-
210 imum independent of initial values. In spite of the acceleration with this
211 replacement, CMTF is still much slower than HOSVD as well as CP de-
212 composition.

213 Based upon the observation in the above, since data set we have to analyze
214 is massive, considering primarily the cpu time required, we decided to employ
215 HOSVD first. Then, we will try other methods only when HOSVD fails to get
216 reasonable results.

217 3.2 Application of HOSVD to real data set

218 Among numerous neurodegenerative diseases, we focus on Alzheimer's disease
219 (AD) in this study, because it is the diseases for which the most number of drugs
220 were tried to develop. For example, among 322 drugs that target neurodegen-
221 erative diseases, as many as 92 drugs targeted AD [24]. The therapy targets
222 of AD are wide ranged; especially, Amyloid protein was most frequent target

223 (12 among 92 drugs target amyloid), because accumulation of amyloid has ever
224 been believed to be a primary cause of AD.

225 For this purpose, we selected one specific scRNA-seq data set, GSE127891,
226 by which we can demonstrate the effectiveness of our proposed method. When
227 selecting genes using TD based unsupervised FE, we first need to specify what
228 kind of properties of gene expression we consider. In this study, we require the
229 followings.

- 230 1. Gene expression should be independent of cells within the same 96 wells
231 plate.
- 232 2. Gene expression should be independent of genotype.
- 233 3. Gene expression should be independent of tissues.
- 234 4. Gene expression should have monotonic dependence upon age.
- 235 5. Gene expression should be independent of sex.
- 236 6. Gene expression should be independent of each of four 96 wells plates
237 under the same conditions.

238 In other words, we try to select genes with the most robust monotonic age
239 dependence as much as possible. The reason of this motivation is as follows.
240 In the paper where data set analyzed here was investigated originally, Frigerio
241 et al. [25] found that age is the primary factor of the microglia response to
242 accumulation of $A\beta$ plaques. We found that singular value vectors with $\ell_1 =$
243 $\ell_2 = \ell_3 = \ell_5 = \ell_6 = 1$ represent independence of cells, genotypes, tissues, sex
244 and plates (Figure 10 (A), (B), (C), (E), (F)). On the other hand, u_{2j_4} represents
245 monotonic dependence upon ages, $1 \leq j_4 \leq 4$ (Figure 10 (D)).

246 Next, we need to find the $G(1, 1, 1, 2, 1, 1, \ell_7)$ with the largest absolute value
247 in order to identify singular value vector, $u_{\ell_7 i}$, attributed to genes. Then we
248 found that $G(1, 1, 1, 2, 1, 1, 2)$ has the largest absolute value. Therefore, we
249 decided to use u_{2i} for attributing P -values to genes as shown in eq. (2). Finally,
250 401 genes are identified as being associated with adjusted P -values less than 0.01
251 (The list of genes is available as supplementary material).

252 These 401 genes are uploaded to Enrichr to identify the compounds, with
253 which genes expressing differential expression of cell lines treated are maximally
254 overlapped with these 401 genes. As for “LINCS L1000 Chem Pert up” cate-
255 gory (Table 2, full list is available as supplementary material), the top ranked
256 compound is alvocidib, which was previously tested for AD [26]; there are also
257 65 experiments (see supplementary material) of cell lines treated with alvocidib
258 and associated with adjusted P -value less than 0.05. The second top ranked
259 compound is AZD-8055, which was also previously tested for AD [27]; there
260 are also 6 experiments (see supplementary material) of cell lines treated with
261 AZD-8055 and associated with adjusted P -value less than 0.05.

262 One might wonder if this is an accidental agreement which is specific to
263 LINCS data set. In order to confirm that it is not an accidental agreement, we

264 also see DrugMatrix category (Table 3, full list is available as supplementary
265 material). The top, fifth and tenth ranked compound is cyclosporin-A, which
266 was also previously tested for AD [28]; there are also 57 experiments (see supple-
267 mentary material) of cell lines treated with cyclosporin-A and associated with
268 adjusted P -value less than 0.05. Finally, we tested “Drug Perturbations from
269 GEO up” category in Enrichr (Table 4, full list is available as supplementary
270 material). The top ranked compounds is imatinib, which was also previously
271 tested for AD [29]; there are also 18 experiments (see supplementary material) of
272 cell lines treated with imatinib and associated with adjusted P -value less than
273 0.05.

274 Although these findings suggest that our strategy is effective to find com-
275 pounds that can be used for AD treatment, one might think that these findings
276 are still weak. Since these 401 genes are simply genes whose expression is altered
277 because of Amyloid accumulation, they themselves are unlikely to be disease caus-
278 ing genes. Thus, we consider regulation factors that affect expression of these
279 genes. At first, we consider transcription factor (TF). With checking “ENCODE
280 and ChEA Consensus TFs from ChIP-X” category in Enrichr, we found that
281 the target genes of TFs, MYC, NELFE, TAF7, KAT2A, SPI1, RELA, TAF1
282 and PML are top ranked ten TFs associated with adjusted P -values less than
283 1×10^{-7} (They are less than ten, because some are ranked in multiple times
284 within top 10). Among them, MYC [30], KAT2A [31], SPI1 [32], RELA [33],
285 TAF1 [34], and PML [35] were reported to be related to AD. Next, we consider
286 microRNA (miRNA) as regulatory factors towards identified 401 genes. With
287 checking “miRTarBase 2017” category in Enrichr, we found that target genes
288 of miRNAs, hsa-miR-320a, hsa-miR-1260b, hsa-miR-652-3p, hsa-miR-744-5p,
289 hsa-miR-16-5p, hsa-miR-100-5p, hsa-miR-615-3p, hsa-miR-484, hsa-miR-296-
290 3p, and hsa-miR-423-5p are top ranked ten miRNAs associated with adjusted
291 P -values less than 1×10^{-3} . Among them, miR-320a [36], miR-652 [37], miR-
292 744 [38], miR-16 [39], miR-100 [40], miR-615 [41], miR-484 [42], miR-296 [43],
293 and miR-423 [36] were reported to be related to AD. These finding can add
294 more confidence that identified 401 genes are likely related to AD. Expression
295 of these 401 genes might be altered because they are simply downstream genes
296 caused by AD, it is unlikely to find more direct evidence that these genes really
297 contribute to AD directly. For our purpose, screening drugs with gene expres-
298 sion, 401 genes are enough to be downstream genes caused by AD. Thus, we do
299 not investigate biological background of these 401 genes further.

300 Thus, it might be worthwhile investigating lower ranked compounds in Ta-
301 bles 2, 3 and 4 as candidate compounds for AD, even if they were not known
302 drugs for AD.

303 4 Discussion

304 First of all, since these cell lines in Table 2 are originated in human, our strategy
305 can provide us the opportunity to check if proposed candidate drugs screened
306 with model animals are also effective in human.

307 It is also remarkable that we do not need gene expression of all genes, but
308 only a subset of genes (please remember that LINCS project measures only gene
309 expression of less than one thousand genes) in order to predict candidate drugs
310 with high accuracy. This might reduce the amount of money to screen numerous
311 number of compounds.

312 Our method is also applicable to scRNA-seq in order to screen drug com-
313 pounds candidate from scRNA-seq. To our knowledge, there are very limited
314 number of studies that relate scRNA-seq to drug design [44, 45], since scRNA-seq
315 usually lacks cell labeling which is useful to screen differentially expressed genes.
316 In this study, we simply make use of ages, which is not always directly related to
317 diseases. In spite of that, drug we listed was correct, i.e., they are known drugs
318 to some extent. Therefore, our strategy is also useful to add an alternative one
319 along this direction, i.e., making use of scRNA-seq for drug design.

320 Thus, our strategy, TD based unsupervised FE, might be promising method-
321 ology to screen drug candidate compounds.

322 One might wonder why we have specifically used HOSVD algorithm although
323 there are many other ways by which we can apply TD to data set. There are
324 multiple reasons why we did not employ other TD based approaches. First of all,
325 we would like to compare HOSVD with other simple (unsupervised) TDs, CP
326 decomposition, HOOI for Tucker decomposition and tensor train decomposition.
327 CP decomposition is the much more popular methods because it can relate
328 singular value vectors one to one. In HOSVD algorithm, we need to investigate
329 core tensor, G , for relating singular value vectors attributed to genes and those
330 attributed to individual cells. In CP decomposition, since TD is composed of
331 outer product of individual singular value vectors, it is clear which singular value
332 vectors attributed to genes are associated with selected singular value vectors
333 attributed to cells. Nevertheless, CP decomposition has two disadvantages:
334 massive computational time and the lack of guarantee that converges to unique
335 solutions. Since CP decomposition employed alternative least square (ALS), it
336 needs to initial values of singular value vectors, which often converges to distinct
337 final singular value vectors. This results in distinct set of genes selected, since
338 we make use of singular value vectors attributed to genes in order to select genes.
339 It definitely prevents us from interpreting biological meanings that should be
340 independent of numerical initial values. The employment of ALS also results
341 in the lack of estimated computational time, since it is an iterative procedure.
342 Especially when we need to deal with massive data set that requires huge cpu
343 time in each iteration, it is not a good strategy to employ the method that
344 requires iterative processes that we cannot estimate the cpu time required by
345 it in advance. On the other hand, HOSVD is essentially SVD of unfolded
346 tensor, thus it does not require any iterative computation; it is guaranteed to
347 converge within polynomial time. Since we could get reasonable results using
348 HOSVD, we have no motivation to employ the method that requires iteration
349 like CP decomposition. As for HOOI, since it also employed ALS, it is not
350 recommended to be employed for the massive data set that we analyzed in
351 this study. Especially, since it is very usual that HOOI employs the results
352 of HOSVD as initial (starting) values for the iteration, there are no reasons

353 to apply HOOI to the results of HOSVD that is good enough in this study.
354 Finally, as for tensor train decomposition, it does lack the weight factor that
355 relates between singular value vectors attributed to gene and cells. Since we
356 definitely need to relate them for our purpose, tensor train decomposition is not
357 a suitable method. All of these point about the comparisons between HOSVD
358 and other TDs from the point of views of feature selection that was discussed
359 in more details in the book [9] to be published soon.

360 After that, we would like to discuss why we do not employ more advanced su-
361 pervised methods. In the above analysis, we made use of labeling information,
362 e.g., sex, genotypes, and time points, only after TD was applied to data set.
363 On the other hand, there are multiple methods that can make use of labeling
364 information with applying TD. For example, coupled matrix and tensor factor-
365 ization (CMTF) [23] is a straight extension of unsupervised TD to supervised
366 one. CMTF requires that linear combination of singular value vectors must be
367 coincident with given labeling attributed to samples (in this study, cells). Al-
368 though it is generally expected that CMTF can derive singular value vectors
369 that are more associated with labeling than fully unsupervised TDs do, only
370 one obstacle to perform CMTF is cpu time. Since CMTF requires iterative op-
371 timization to fulfill the requirements, i.e., linear combination of singular value
372 vectors must be coincident with given labeling attributed to sample, CMTF
373 requires more computational time than unsupervised TD including HOSVD.
374 Practically, CMTF requires as many as hundreds iterations, each of which re-
375 quires cpu time as much as HOSVD requires. This means, CMTF takes as
376 many as hundreds times longer than HOSVD. In this case, since data set is
377 so massive, single HOSVD requires several hours run on computer, Although
378 we tried to implement CMTF fitted to our model and to execute it, it does
379 not converge within a day. Since our TD based unsupervised FE has already
380 achieved reasonable results we concluded that performing more advanced su-
381 pervised methods that usually require more cpu time is not effective and did
382 not employ any supervised method including CMTF.

383 5 Conclusion and Future Work

384 In this paper, we applied TD based unsupervised FE to scRNA-seq taken from
385 mouse brain with $A\beta$ accumulation. We have compared selected 401 genes
386 with differentially expressed genes in cell lines and model animals treated with
387 various compounds. As a result, as for three independent data sets, LINCS,
388 DrugMatrix and GEO, top ranked compounds are reported to be tested as AD
389 treatment. This suggests the effectiveness of our strategy and lower ranked
390 compounds should be tested as promising drug compounds candidates. To our
391 knowledge, this is the first successful one that can be applied to scRNA-seq in
392 order to identify drug compounds candidate.

393 For future work, we aim to (1) utilize the tensor decomposition technique
394 in the transfer learning setting to identify effective drugs between target and
395 related tasks in various problems in the clinical informatics domain, among other

396 uses; (2) add other data source of different diseases (e.g., Parkinson’s disease)
397 for treatment validation; and (3) apply the tensor decomposition technique in
398 more fields such as social networks to verify its effectiveness in applications such
399 as recommender systems.

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	HOSVD	CP	CMTF	
			ALS	BFGS
data set 1	22	334	5760	2002
data set 2	9	123	5787	2991

Table 1: Cpu time (msec) required to perform various methods.

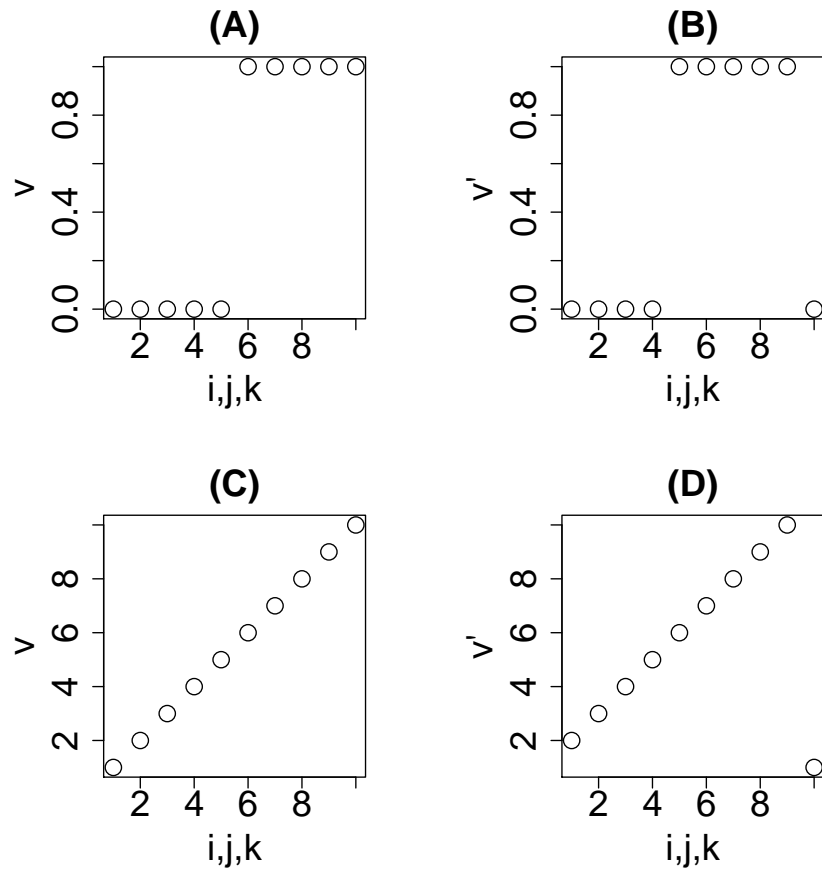


Figure 1: Data set 1, eq. (4), (A) v_i and (B) v'_i and data set 2, eq. (5), (C) v_i and (D) v'_i .

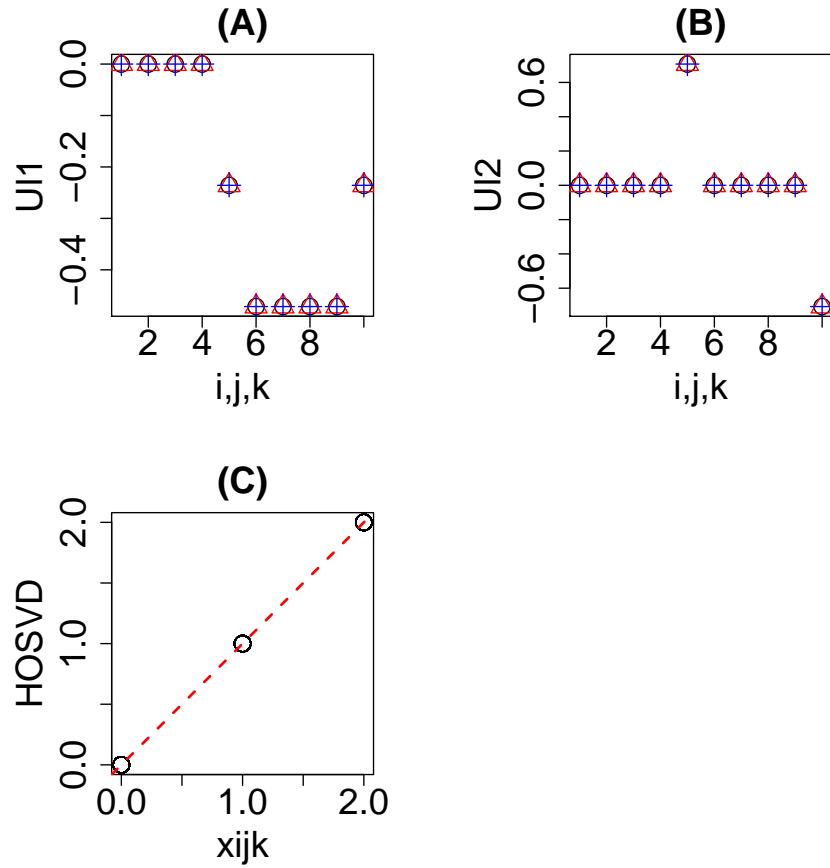


Figure 2: The results obtained by HOSVD applied to data set 1: eq. (4). (A) Open black circles: $u_{1i}^{(i)}$, open red triangles: $u_{1j}^{(j)}$, blue pluses: $u_{1k}^{(k)}$ (B) Open black circles: $u_{2i}^{(i)}$, open red triangles: $u_{2j}^{(j)}$, blue pluses: $u_{2k}^{(k)}$. (C) Scatter plot between x_{ijk} (horizontal axis) and eq. (7) (vertical axis).

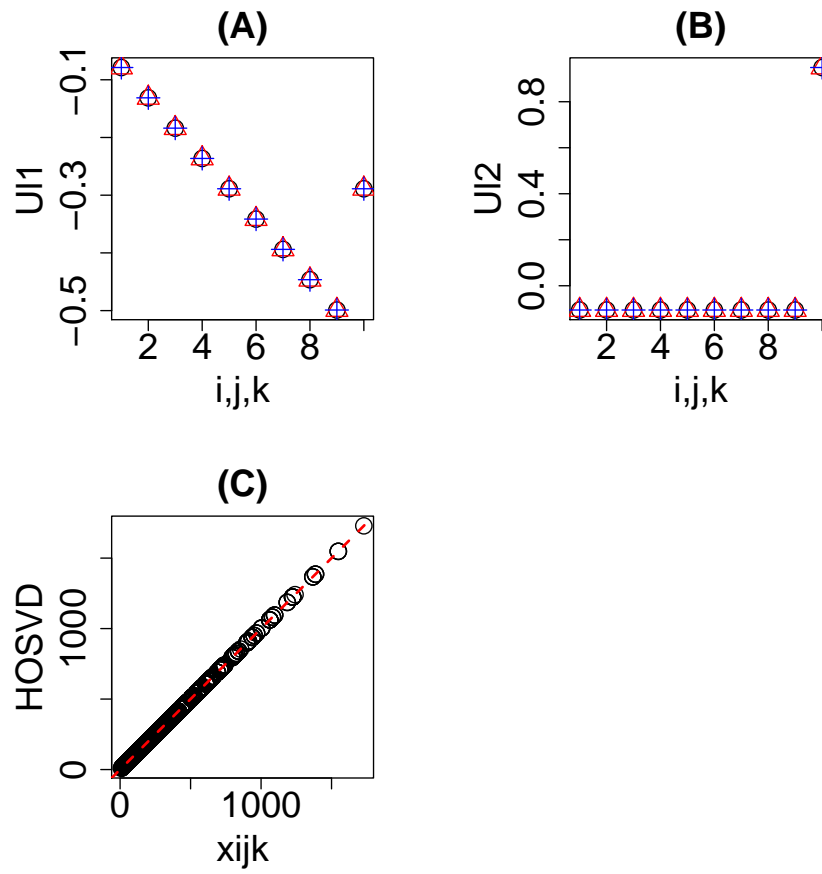


Figure 3: The results obtained by HOSVD applied to data set 2: eq. (5). Other notations are the same as Fig. 2.

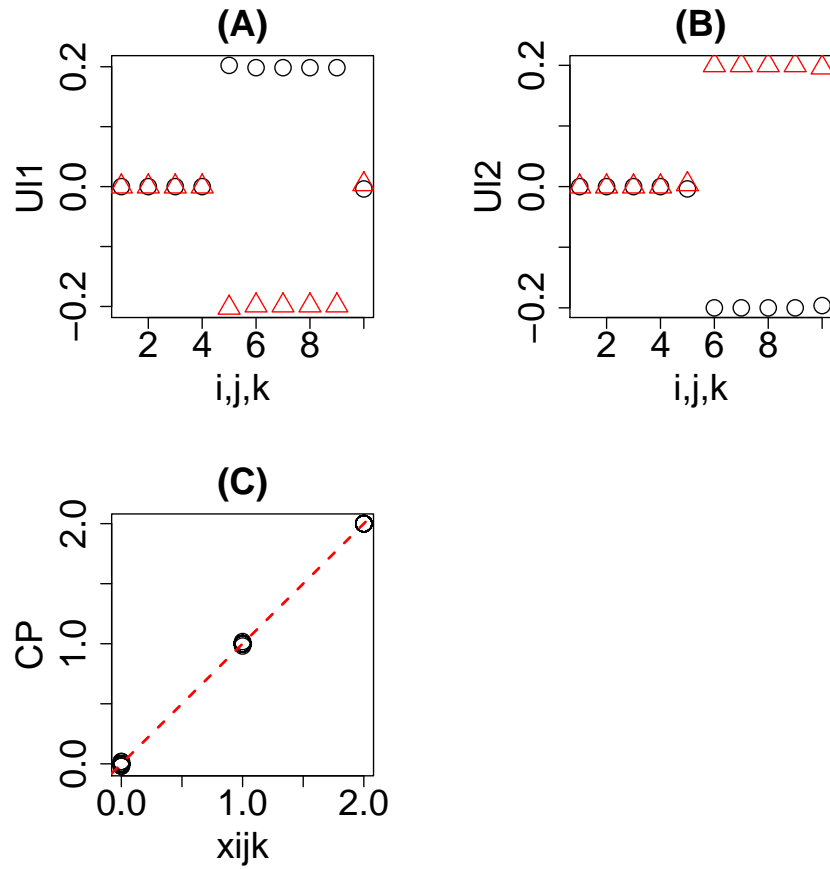


Figure 4: The results obtained by CP decomposition applied to data set 1: eq. (4). (A) Open black circles: $u_{1i}^{(i)}$, open red triangles: $u_{1j}^{(j)}$, blue pluses: $u_{1k}^{(k)}$ (B) Open black circles: $u_{2i}^{(i)}$, open red triangles: $u_{2j}^{(j)}$, blue pluses: $u_{2k}^{(k)}$. (C) Scatter plot between x_{ijk} (horizontal axis) and those reproduced by CP decomposition using singular value vectors shown in (A) and (B) (vertical axis).

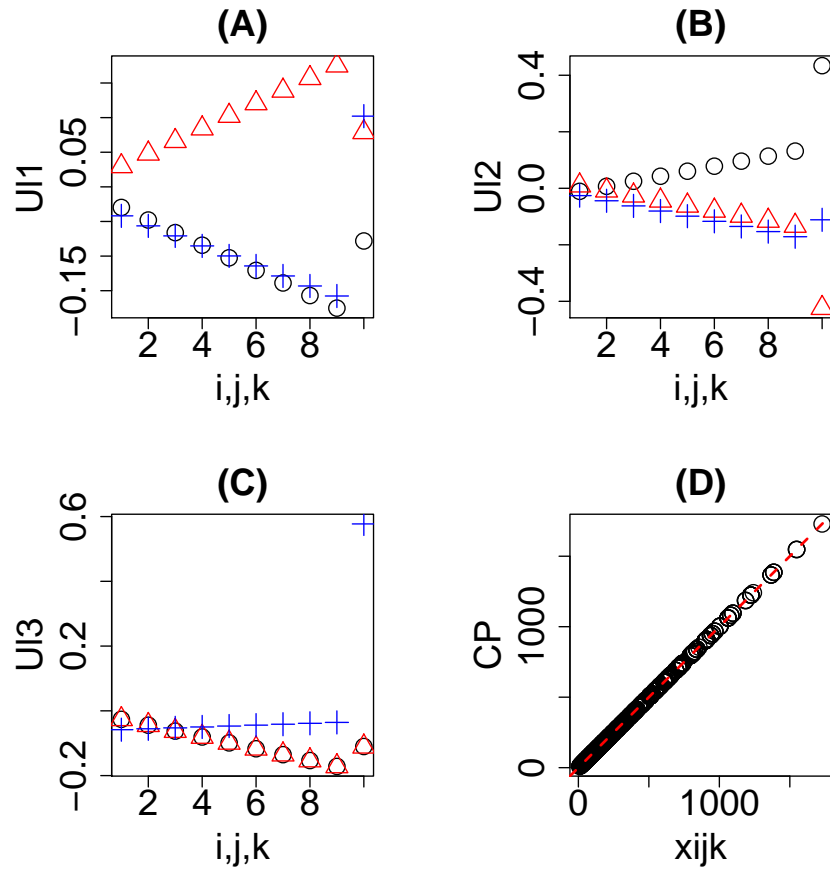


Figure 5: The results obtained by CP decomposition applied to data set 2: eq. (5). (A) Open black circles: $u_{1i}^{(i)}$, open red triangles: $u_{1j}^{(j)}$, blue pluses: $u_{1k}^{(k)}$ (B) Open black circles: $u_{2i}^{(i)}$, open red triangles: $u_{2j}^{(j)}$, blue pluses: $u_{2k}^{(k)}$. (C) Open black circles: $u_{3i}^{(i)}$, open red triangles: $u_{3j}^{(j)}$, blue pluses: $u_{3k}^{(k)}$. (D) Scatter plot between x_{ijk} (horizontal axis) and those reproduced by CP decomposition using singular value vectors shown in (A), (B) and (C) (vertical axis).

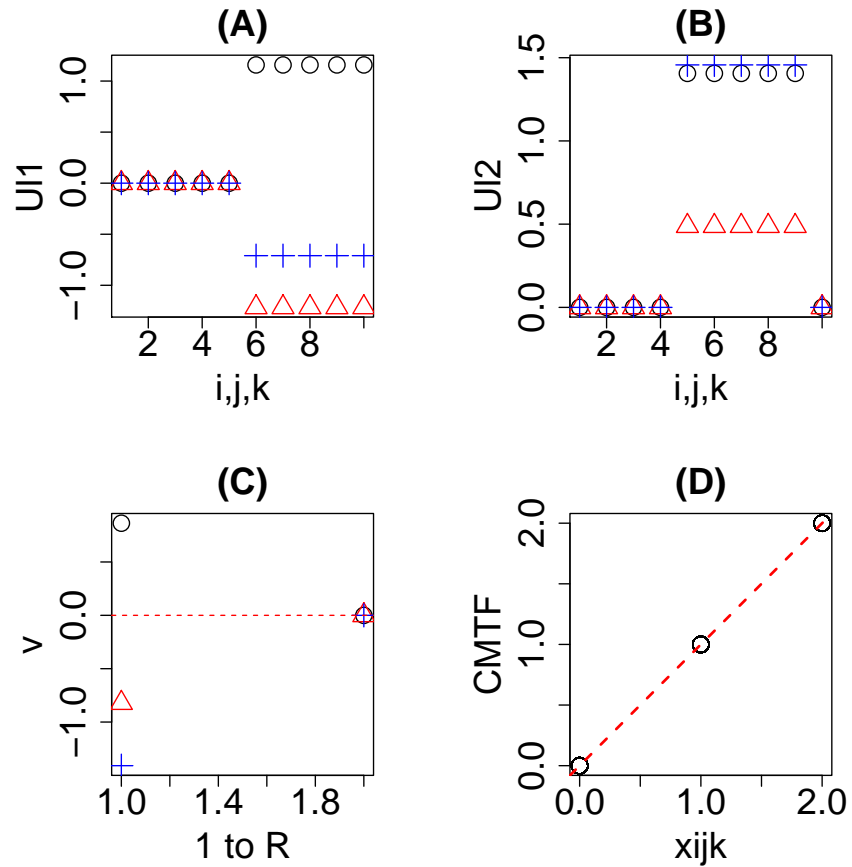


Figure 6: The results obtained by CMTF applied to data set 1: eq. (4). (A) Open black circles: $u_{1i}^{(i)}$, open red triangles: $u_{1j}^{(j)}$, blue pluses: $u_{1k}^{(k)}$ (B) Open black circles: $u_{2i}^{(i)}$, open red triangles: $u_{2j}^{(j)}$, blue pluses: $u_{2k}^{(k)}$. (C) Open black circles: $a_{\ell}^{(i)}$, open red triangles: $a_{\ell}^{(j)}$, blue pluses: $a_{\ell}^{(k)}$. (D) Scatter plot between x_{ijk} (horizontal axis) and those reproduced by CMTF decomposition using singular value vectors shown in (A) and (B) (vertical axis).

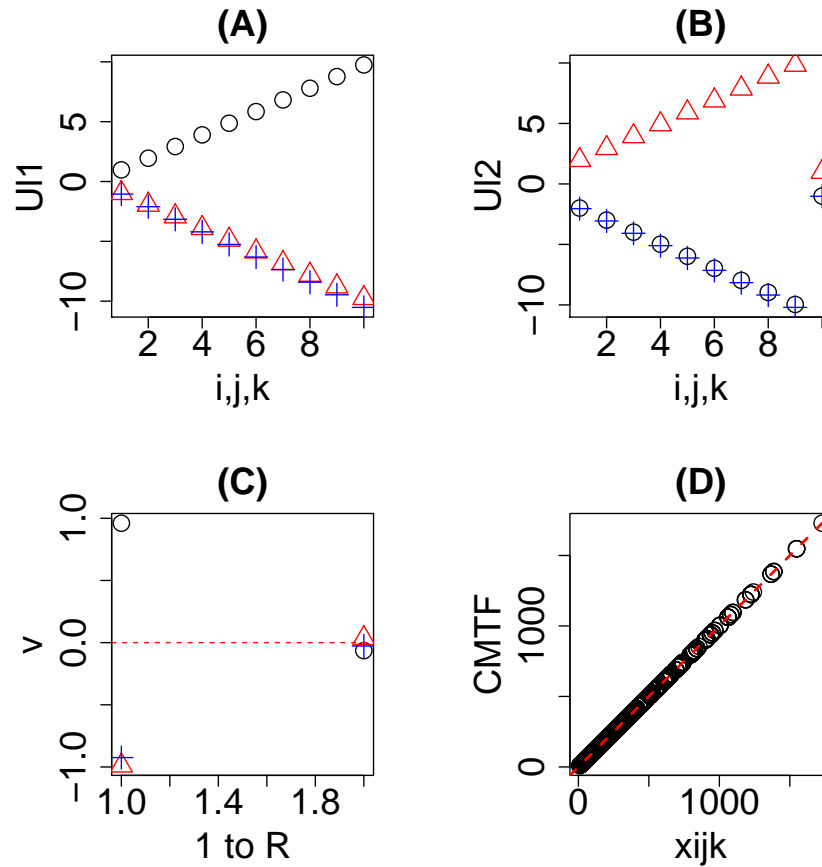


Figure 7: The results obtained by CMTF applied to data set 2: eq. (5). (A) Open black circles: $u_{1i}^{(i)}$, open red triangles: $u_{1j}^{(j)}$, blue pluses: $u_{1k}^{(k)}$ (B) Open black circles: $u_{2i}^{(i)}$, open red triangles: $u_{2j}^{(j)}$, blue pluses: $u_{2k}^{(k)}$. (C) Open black circles: $a_\ell^{(i)}$, open red triangles: $a_\ell^{(j)}$, blue pluses: $a_\ell^{(k)}$. (D) Scatter plot between x_{ijk} (horizontal axis) and those reproduced by CMTF decomposition using singular value vectors shown in (A) and (B) (vertical axis).

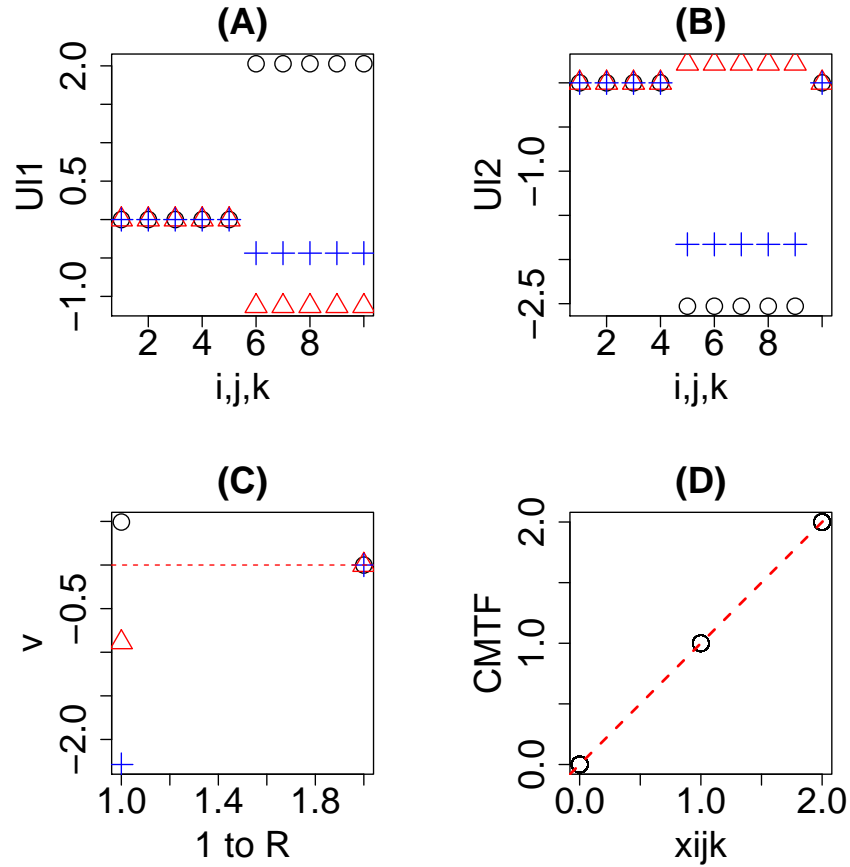


Figure 8: The results obtained by CMTF, with replacing ALS with BFGS, applied to data set 1: eq. (4). (A) Open black circles: $u_{1i}^{(i)}$, open red triangles: $u_{1j}^{(j)}$, blue pluses: $u_{1k}^{(k)}$ (B) Open black circles: $u_{2i}^{(i)}$, open red triangles: $u_{2j}^{(j)}$, blue pluses: $u_{2k}^{(k)}$. (C) Open black circles: $a_{\ell}^{(i)}$, open red triangles: $a_{\ell}^{(j)}$, blue pluses: $a_{\ell}^{(k)}$. (D) Scatter plot between x_{ijk} (horizontal axis) and those reproduced by CMTF using singular value vectors shown in (A) and (B) (vertical axis).

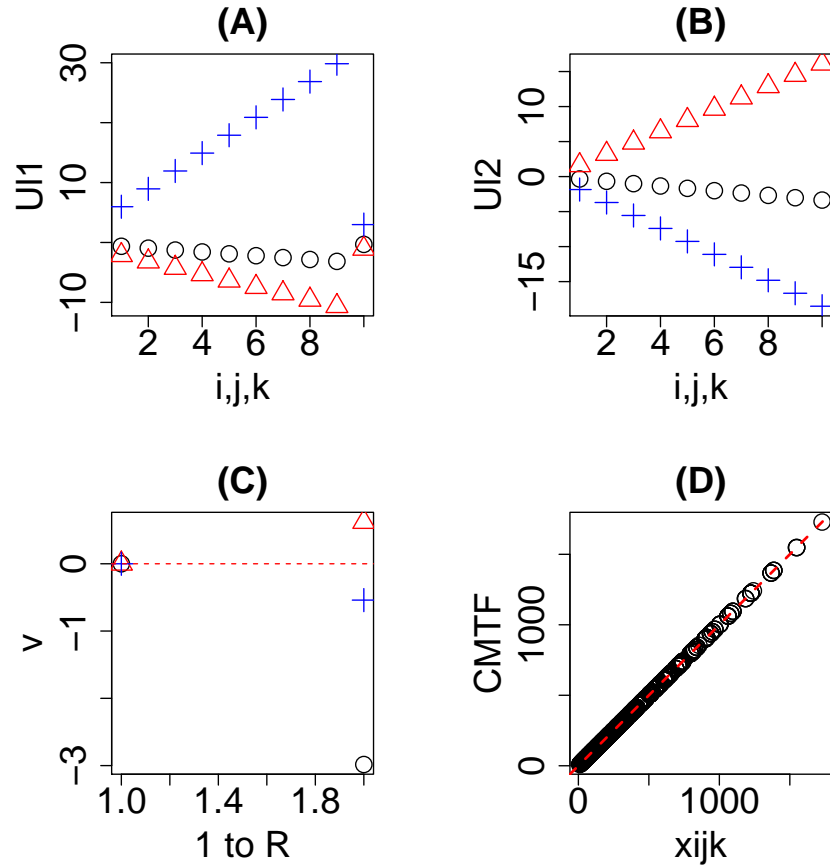


Figure 9: The results obtained by CMTF, with replacing ALS with BFGS, applied to data set 2: eq. (5). (A) Open black circles: $u_{1i}^{(i)}$, open red triangles: $u_{1j}^{(j)}$, blue pluses: $u_{1k}^{(k)}$ (B) Open black circles: $u_{2i}^{(i)}$, open red triangles: $u_{2j}^{(j)}$, blue pluses: $u_{2k}^{(k)}$. (C) Open black circles: $a_{\ell}^{(i)}$, open red triangles: $a_{\ell}^{(j)}$, blue pluses: $a_{\ell}^{(k)}$. (D) Scatter plot between x_{ijk} (horizontal axis) and those reproduced by CMTF using singular value vectors shown in (A) and (B) (vertical axis).

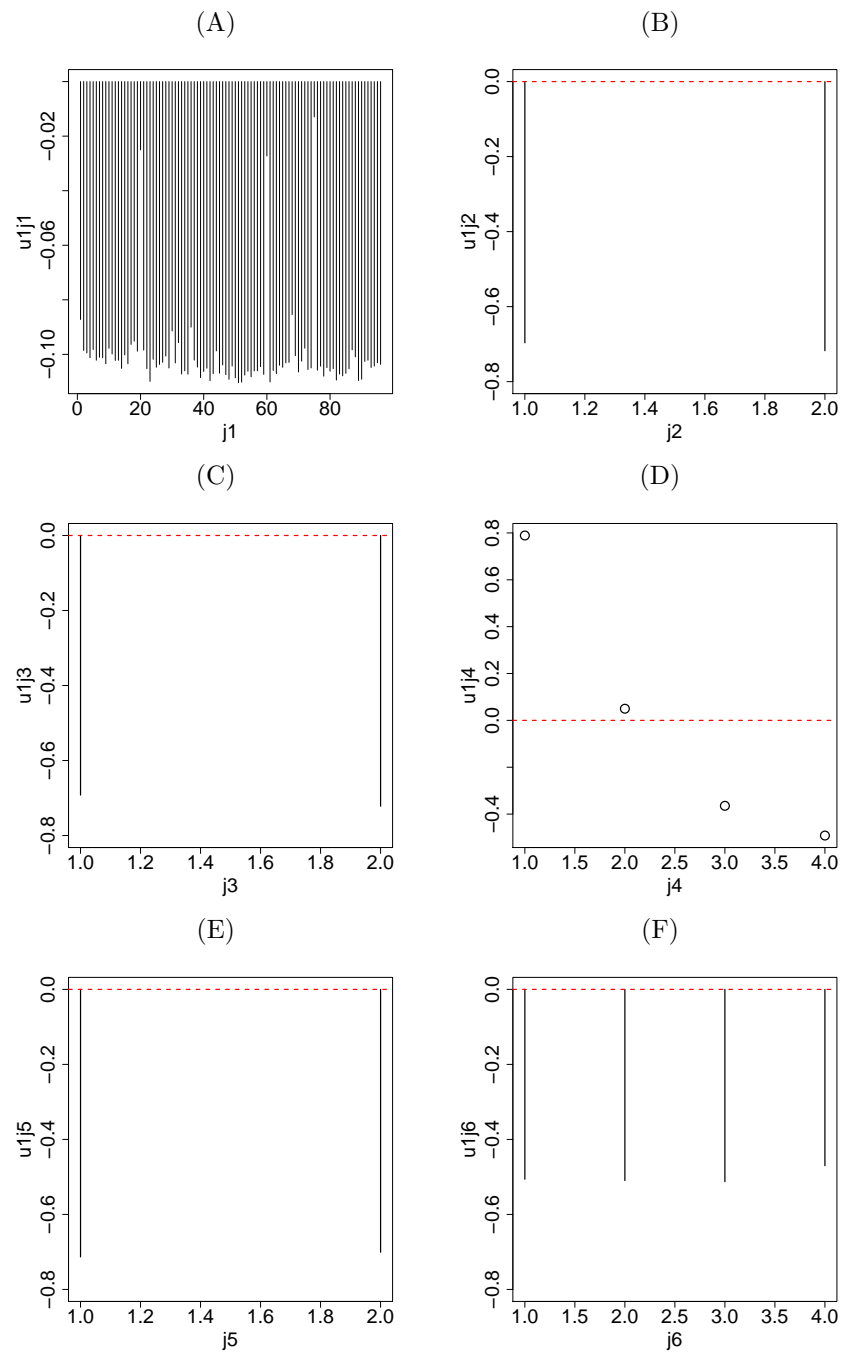


Figure 10: Singular value vectors. (A) u_{1j_1} (B) u_{1j_2} (C) u_{1j_3} (D) u_{2j_4} (E) u_{1j_5} (F) u_{1j_6} .

Table 2: Top ranked 10 compounds listed in “LINCS L1000 Chem Pert up” category in Enrichr. Overlap is that between selected 401 genes and genes selected in individual experiments.

Term	Overlap	P-value	Adjusted P-value
LJP006_HCC515_24H-alvocidib-10	28/221	7.99×10^{-15}	2.21×10^{-10}
LJP006_HCC515_24H-AZD-8055-10	24/188	5.87×10^{-13}	8.13×10^{-9}
LJP009_PC3_24H-CGP-60474-3.33	25/217	1.99×10^{-12}	1.14×10^{-8}
LJP005_MDAMB231_24H-AS-601245-10	20/132	2.05×10^{-12}	1.14×10^{-8}
LJP009_PC3_24H-saracatinib-10	24/196	1.47×10^{-12}	1.14×10^{-8}
LJP006_HCC515_24H-CGP-60474-0.37	24/225	2.89×10^{-11}	1.14×10^{-7}
LJP009_PC3_24H-PF-3758309-10	23/212	5.33×10^{-11}	1.84×10^{-7}
LJP005_HCC515_24H-WZ-3105-3.33	20/144	1.07×10^{-11}	4.95×10^{-8}
LJP006_HEPG2_24H-AZD-5438-10	21/182	1.17×10^{-10}	3.24×10^{-7}
LJP006_HCC515_24H-A443654-10	22/203	1.44×10^{-10}	3.62×10^{-7}

Table 3: Top ranked 10 compounds listed in “DrugMatrix” category in Enrichr. Overlap is that between selected 401 genes and genes selected in individual experiments.

Term	Overlap	P-value	Adjusted P-value
Cyclosporin_A-350_mg/kg_in_Corn_Oil-Rat-Bone_marrow-5d-up	51/315	2.26×10^{-31}	1.78×10^{-27}
Isoprenaline-4.2_mg/kg_in_Saline-Rat-Heart-5d-up	49/304	4.55×10^{-30}	1.79×10^{-26}
Hydroxyurea-400_mg/kg_in_Saline-Rat-Bone_marrow-5d-up	46/307	7.54×10^{-27}	1.49×10^{-23}
Netilmicin-40_mg/kg_in_Saline-Rat-Kidney-28d-up	45/314	1.90×10^{-25}	1.50×10^{-22}
Cyclosporin_A-350_mg/kg_in_Corn_Oil-Rat-Bone_marrow-3d-up	45/312	1.45×10^{-25}	1.42×10^{-22}
Chlorambucil-0.6_mg/kg_in_Corn_Oil-Rat-Spleen-0.25d-up	47/314	2.13×10^{-27}	5.60×10^{-24}
Tobramycin-40_mg/kg_in_Saline-Rat-Kidney-28d-up	45/311	1.26×10^{-25}	1.42×10^{-22}
Gemcitabine-11_mg/kg_in_Saline-Rat-Bone_marrow-3d-up	47/344	1.27×10^{-25}	1.42×10^{-22}
Terbutaline-130_mg/kg_in_Corn_Oil-Rat-Heart-3d-up	45/321	4.89×10^{-25}	2.41×10^{-22}
Cyclosporin_A-70_mg/kg_in_Corn_Oil-Rat-Bone_marrow-3d-up	45/320	4.28×10^{-25}	2.25×10^{-22}

Table 4: Top ranked 10 compounds listed in “Drug Perturbations from GEO up” category in Enrichr. Overlap is that between selected 401 genes and genes selected in individual experiments.

Term	Overlap	P-value	Adjusted P-value
imatinib DB00619 mouse GSE51698 sample 2522	81/288	2.27×10^{-70}	2.05×10^{-67}
bleomycin DB00290 mouse GSE2640 sample 2851	80/329	6.09×10^{-64}	2.75×10^{-61}
soman 7305 rat GSE13428 sample 2640	86/532	3.87×10^{-53}	3.50×10^{-51}
coenzyme Q10 5281915 mouse GSE15129 sample 3464	76/302	6.84×10^{-62}	2.06×10^{-59}
N-METHYLFORMAMIDE 31254 rat GSE5509 sample 3570	70/283	2.39×10^{-56}	3.60×10^{-54}
Calcitonin 16132288 mouse GSE60761 sample 3446	65/220	8.51×10^{-58}	1.92×10^{-55}
cyclophosphamide 2907 mouse GSE2254 sample 3626	78/413	2.47×10^{-53}	2.48×10^{-51}
Calcitonin 16132288 mouse GSE60761 sample 3447	59/177	5.88×10^{-56}	7.59×10^{-54}
PRISTANE 15979 mouse GSE17297 sample 3229	71/291	1.03×10^{-56}	1.87×10^{-54}
coenzyme Q10 5281915 mouse GSE15129 sample 3456	76/396	1.79×10^{-52}	1.35×10^{-50}