| 1 | A Computational Framework to Study the Primary Lifecycle |
|----|---|
| 2 | Metabolism of Arabidopsis thaliana |
| 3 | |
| 4 | Running title: A Lifecycle Metabolic Modeling Framework |
| 5 | |
| 6 | Authors: Wheaton L. Schroeder ¹ and Rajib Saha ^{\Box^*} |
| 7 | ¹ Department of Chemical and Biomolecular Engineering, University of Nebraska – Lincoln, |
| 8 | USA |
| 9 | |
| 10 | Correspondence: |
| 11 | Dr. Rajib Saha |
| 12 | rsaha2@unl.edu |
| 13 | |
| 14 | Keywords: stoichiometric model, Arabidopsis thaliana, metabolism, core metabolism, carbon |
| 15 | metabolism, lifecycle, multi-tissue |
| 16 | Language Style: American English |
| 17 | Article Type: Research Article |
| 18 | Article Length: 9539 words (excluding abstract, summary, references, captions) |
| 19 | Number of Figures: 5 |
| 20 | Number of Tables: 1 |
| 21 | |

22 Abstract

Stoichiometric Models of metabolism have proven valuable tools for increased understanding of 23 metabolism and accuracy of synthetic biology interventions to achieve desirable phenotypes. 24 25 Such models have been used in conjunction with optimization-based and have provided "snapshot" views of organism metabolism at specific stages of growth, generally at exponential 26 growth. This approach has limitations in that metabolic history of the modeled system cannot be 27 studied. The inability to study the complete metabolic history has limited stoichiometric 28 metabolic modeling only to the static investigations of an inherently dynamic process. In this 29 30 work, we have sought to address this limitation by introducing an optimization-based computational framework and applying to a stoichiometric model of the model plant Arabidopsis 31 thaliana of four linked sub-models of leaf, root, seed, and stem tissues which models the core 32 carbon metabolism through the lifecycle of arabidopsis (named as p-ath780). Uniquely, this 33 framework and model considers diurnal metabolism, changes in tissue mass, carbohydrate 34 35 storage, and loss of plant mass to senescence and seed dispersal. p-ath780 provide "snapshots" of 36 core-carbon metabolism at one hour intervals of growth, in order to show the evolution of metabolism and whole-plant growth across the lifecycle of a single representative plant. Further, 37 it can simulate important growth stages including seed germination, leaf development, flower 38 production, and silique ripening. The computational framework has shown broad agreement with 39 published experimental data in tissue mass yield, maintenance cost, senescence cost, and whole-40 plant growth checkpoints. Having focused on core-carbon metabolism, it serves as a scaffold for 41 lifecycle models of other plant systems, to further increase the sophistication of in silico 42 metabolic modeling, and to increase the range of hypotheses which can be investigated in silico. 43

As an example, we have investigated the effect of alternate growth objectives on this plant overthe lifecycle.

46

47 Author Summary

In an attempt to study the evolution of metabolism across the lifecycle of plants, in this work we 48 have created an optimization-based framework for the in silico modeling of plant metabolism 49 50 across the lifecycle of a model plant. We then applied this framework to four core-carbon tissue-51 level (namely, leaf, root, seed, and stem) stoichiometric models of the model plant species Arabidopsis thaliana, and further informed this framework with a wide array of published in vivo 52 data to increase model and framework accuracy. Unique to the p-ath780 model, comparted to 53 other models of plant metabolism, is the simultaneous considerations of diurnal metabolism, 54 55 carbohydrate storage, changes in tissue mass (including losses), and changes in metabolism with respect to plant growth stage. This provides a more complete picture of plant metabolism and 56 allows for a wider array of future studies of plant metabolism, particularly since we have only 57 58 modeled the core carbon metabolism of A. thaliana, allowing this work to serve as a framework for studies of other plant systems. 59

Introduction 60

The use of synthetic biology for the engineering of uni- and multi-cellular organisms to enhance 61 desirable phenotypes in microbe, plant, and animal systems, has been well established and has 62 been capable of affecting the lives of millions of individuals, such as in the case of artemisinin 63 production in yeast or enhancing nutritional value of agricultural products [1-2]. Synthetic 64 biology techniques have been applied to many plant systems such as tomatoes [3], rice [4], and 65 maize [5] to produce enhanced phenotypes often with application to human nutrition [2], pest 66 resistance [5], and resilience to abiotic stresses [6]. Many of these efforts have focused on a 67 68 genetic understanding and manipulation of the plant system (or plant tissue) in question, having relied on intuitive interventions such as changes in regulation, insertion of new gene(s), and 69 deletion of gene(s) from competing pathway(s) [2,5,6]. Alternatively, computation-based 70 71 systems biology approaches, such as the use of stoichiometric genome-scale models (GSMs) of metabolism, have predicted non-intuitive genetic interventions [7] by accounting for Gene-72 73 Protein-Reaction (GPR) links and understanding how a gene knockout, or a change in gene 74 regulation, affects the entire system through tools such as Flux Balance Analysis (FBA) [8], OptKnock [9], and OptForce [10]. Other tools are built upon previously existing tools, such as 75 dynamic FBA (dFBA), which performs FBA over windows of time by solving a non-dynamic 76 77 linear or a static linear problem, both of which integrate system variables over discrete time windows to solve to metabolite concentration, in addition to reaction flux [11]. Such tools have 78 led to enhanced mechanistic understanding for exploring the system-wide effects of synthetic 79 biology interventions especially in a microbial or a fungal system, such as E. coli [10], 80 cyanobacteria [12], and yeast [13]. 81

82

83 Stoichiometric global plant models, which treat the metabolism of the plant as a single unit, have 84 been developed for Arabidopsis thaliana (hereafter arabidopsis) [14-17], Zea mayz (maize) [18], Sorghum bicolor (sorghum) [19], Saccharum officinarum (sugarcane) [19], Brassica napus 85 (rapeseed) [19], and Oryza sativa (rice) [20]. These models have sought to analyze metabolic 86 maintenance, response to abiotic stimuli, enzyme regulation changes, and metabolism as a whole 87 88 at steady state (or pseudo-steady state). In addition, tissue-specific single-unit models have been reconstructed for various arabidopsis tissues [21], a maize leaf [22], and a barley seed [23] to 89 better understand how present metabolites, metabolic pathways, and nutrient availability differ 90 91 between tissues. Multi-tissue models have been created to characterize whole-plant metabolism 92 for arabidopsis [16] and barley [17] and subsequently to study whole-plant metabolic response to the diurnal cycle and the source-to-sink relationship of leaves and seeds [16,17]. These studies 93 either have considered metabolism at a single point [14,15,18-20], having taken a metabolic 94 95 "snapshot" of a single point in growth time (often in the exponential growth phase) or have 96 considered a single diurnal cycle [16]. This approach has been inherently limited in that 97 metabolism is a dynamic and cumulative process. To clarify, metabolic state is dependent on both on external factors, such as availability of light, carbon sources, and availability of 98 micronutrients, which these "snapshots" have captured, but also are dependent on metabolic 99 100 history. These limitations have been inconsequential for single-cell systems in that laboratory apparatuses have held single-cell cultures at an exponential growth state; therefore, the 101 "snapshot" approach has given good approximation of metabolism in these steady-state systems. 102 In contrast, multi-cellular organisms, such as plants, will have passed through multiple and 103 distinct stages of growth throughout its lifecycle [24], and the organism cannot be held at a 104 105 steady state growth point. For this study, we have chosen Arabidopsis thaliana as the multi-

106 cellular organism for several reasons. Firstly, since the advent of modern genetics, arabidopsis 107 has served as a model plant species in that it has a small genome; therefore, arabidopsis has been well studied. Secondly, arabidopsis has a limited number of basic tissues which will have 108 109 required the construction of a tissue-level model. Thirdly, arabidopsis has at least two distinct metabolic modes dependent on the availability of light. When studying the effects of a synthetic 110 biology intervention on a plant system, such as arabidopsis, understanding the evolution of 111 112 metabolism throughout the plant lifecycle can increase understanding of the cumulative effect of a synthetic biology intervention. The multi-tissue Edinburgh forest model, which has made use 113 114 of Ordinary Differential Equations (ODEs) rather than stoichiometric matrices, has modeled the lifecycle of a tree for the purposes of studying lumber yield [16,17]; however, the intent of the 115 aforementioned model has not been to consider individual reactions or genetic interventions, and 116 therefore the GPR links which are central to the sought understanding and testing hypotheses 117 118 when using SMs have not been included.

119

120 In this work, a core carbon stoichiometric metabolic model of arabidopsis has been reconstructed which consists of major primary carbon metabolism pathways, including, but not limited to, 121 photosynthesis; the citrate cycle; starch and sucrose synthesis; fatty acid synthesis and 122 123 degradation; and amino acid synthesis. The multi-tissue arabidopsis stoichiometric model, referred to as p- ath780 has 1033 total (and 633 unique) reactions (R), 1157 total (and 325 124 unique) metabolites (M), and accounts for 780 genes (G) including 42 chloroplastic and 11 125 mitochondrial genes. The model p-ath780 (plant-scale primary arabidopsis thaliana model 126 127 including 780 genes) consists of four tissue-level models of metabolism: leaf (R: 537, M: 479, 128 and G: 703), root (R: 130, M: 126, and G: 250), seed (R: 428, M: 411, and G: 529), and stem (R:

129 160, M: 140, and G: 250). The models are linked to one another and their respective environment 130 by a comprehensive Flux Balance Analysis (FBA)-based [8] optimization framework [25] which considers both inter-tissue and environmental interactions. These four tissues have been chosen 131 132 for model reconstruction to represent core plant functions. The root has been chosen and reconstructed for nutrient uptake and growth; the leaf for photosynthesis, carbon fixation, and as 133 a source tissue for plant nutrition; the seed for metabolite storage and a sink tissue for metabolic 134 investment; and the stem for metabolic transport and acting as a conduit for all metabolic 135 interactions between other tissues. The dFBA method determines metabolite concentrations at 136 the start and end points of the time frame [11], whereas the method developed does not focus on 137 concentrations and considers multiple points within the time interval to make more accurate 138 time-derivative estimates of steps in plant and tissue masses, as well as plant maintenance and 139 140 senescence costs. The optimization framework of the p-ath780 model has taken a series of 141 metabolic "snapshots" of arabidopsis metabolism throughout the lifecycle of a single 142 representative plant subject to diurnal status, carbohydrate storage/uptake, changes in tissue mass 143 (including losses), changes in relative tissues masses (due to growth stages), and changes in metabolism with respect to plant growth stage. p-ath780 has taken "snapshots" at hour intervals, 144 and information from these snapshots have advanced plant and tissue masses forward one hour, 145 146 when the next "snapshot" is taken. The series of "snapshots" produced by p-ath780 has given a framework for the investigation of the central metabolism of arabidopsis across its lifecycle. 147 Several different objectives for this optimization-based framework have been investigated, with 148 the default framework being the maximization of plant growth. Other alternative objectives 149 150 investigated have included linear photonic efficiency and seed fatty acid production. This

151 framework with the default objective has shown general agreement with experimental data and is 152 potentially useful as an initial framework for other plant systems.

153 **Results**

154 Reconstruction of arabidopsis primary carbon metabolism in tissue-specific models. Figure 1 shows an overview of the workflow designed for determining the optimal reaction rates and mass 155 step for each "snapshot" (top), how these "snapshots" have been advanced from one time point 156 157 to the next; and how tissues have interacted at various stages of growth along with listing some 158 important characteristics of a given growth stage that differs from other stages (bottom). In order 159 to track the important metabolic interactions and transactions within and between major tissues of arabidopsis plant, namely seed, leaf, root, and stem, corresponding tissue-level metabolic 160 models have been reconstructed. Model files for each tissue can be found in Supplemental Files 161 162 1 (seed), 2 (leaf), 3 (root), and 4 (stem). Figure 2 shows a summary of the distribution of model reactions across KEGG-defined pathways of each tissue model and an overview of reasons for 163 164 reaction inclusion through confidence scoring (see Method section) [26]. Figure 2(A)165 summarizes the pathways common to all tissues, Figure 2(B) summarizes the pathways common to seed and leaf tissues, and Figure 2(C-G) graphically summarize the sources of reactions in 166 each tissue model and p-ath780 as a whole through confidence scores (see methods section) [26]. 167 First, the seed model has been reconstructed based on gene annotations and available MFA data 168 [27] and then tissue model reactions have been distributed across five compartments based on 169 170 literature evidence (see list of works cited in Supplemental File 5): extracellular space, cytosol, 171 non-green plastid, inner mitochondria, and outer mitochondria. Next, transport and exchange reactions have been added to the model based on literature evidence (see list of works cited in 172 173 Supplemental File 5) or modeling necessity to increase model connectivity [26]. The leaf model

174 has been reconstructed using common reactions and pathways from the seed model and having 175 added new pathways and functions essential to the major functions of the leaf tissue, such as photosynthesis [18]. In addition to the five compartments in the seed model, the leaf model 176 177 contains chloroplast and thylakoid compartments. Similarly, by having extracted common 178 reactions/pathways from the seed model, the root and stem models have been reconstructed. The root and stem models have been focused primarily on nutrient uptake (root) and transport (root 179 180 and stem). Both these models contain necessary transport/exchange reactions to ensure model connectivity and to facilitate their roles in transport processes. The stem and root models have all 181 182 the subcellular compartments present in the seed model. Once initial reconstructions have been accomplished, thermodynamically infeasible cycles in addition to atom and charge imbalances 183 have been resolved [26] and tissue-specific biomass equations based on literature information 184 185 have been defined [18,27,28].

186

187 Figure 1. The design-build-test used cycle in constructing the p-ath780 model, where each box 188 represents a step used in this cycle. The numbers in the lower left corner of each box indicates the approximate order in which these steps are undertaken for this cycle. This cycle is repeated 189 until the *in silico* representation of *Arabidopsis thaliana* that is p-ath780 converges satisfactorily 190 191 with *in vivo* experimental data as described in the results section.

192

193 Figure 2. A heuristic look at the four tissue models in terms of number of reactions in various 194 KEGG-defined pathways which provides some clarity as to the metabolic functions of each model (A and B) and in terms of the sources of included model reactions, indicated by 195 confidence scores (C through F). A) A bar graph showing tissue model reaction counts in 196 KEGG-defined pathways (with the exceptions being the user defined pathways of exchange and 197

transport) common to most or all tissue (threshold: at least one model has at least three reactions
in that pathway). B) Additional KEGG-defined pathways common to the seed and/or leaf model
as these models contain more complete metabolism. C) - F) The source of each reaction included
in the models through confidence scores for each tissue. G) The source of all reactions included
in the p-ath780 model. See the methods section discussion related to confidence scores in this
model.

204

205 Development and tuning of the p-ath780 model. Once these core tissue models have been reconstructed and curated, these have been linked within a comprehensive FBA-based 206 optimization framework (provided in Supplemental File 6) for in silico representation of 207 metabolic behavior across the arabidopsis lifecycle. This framework has next been applied to the 208 209 p-ath780 model that includes all four tissue-specific models and has 1033 total reactions, 1157 210 total metabolites, and 780 unique genes. Further details of the model development steps can be 211 found in the methods section. The seed and leaf tissue have been selected to model an important 212 source-to-sink relationship, whereas the stem and root tissues have been included to model nutrient transport and nutrient uptake in arabidopsis, respectively. The FBA-based framework 213 has defined constraints related to tissue interactions and whole-plant growth heuristics based on 214 215 experimental data, and also helped align *in silico* growth with experimentally determined *in vivo* growth through the modified design-build-test cycle shown in Figure 3, which will be discussed 216 217 in greater detail later in this subsection.

218

Figure 3. A simplified workflow of the calculations made to estimate the plant mass step size taken from one "snapshot" to the next (large top box) and visual representation of how these

221 "snapshots" are strung together and grouped into stages and transitions (large bottom box). Each 222 "snapshot" has been represented visually as small boxes containing initial time point, a figure 223 highlighting major metabolic interactions, initial plant mass, step estimate, and cumulative 224 relative growth rate. The contained figures show some major metabolic interactions across the plant system boundaries (full-headed arrows crossing the dashed system boundary) and indicates 225 226 which tissues interact (single-headed arrows with circles to indicate a shared metabolic pool 227 between the two tissues) for the given stage of growth which is indicated by the beveled box 228 below the group of "snapshots". The beveled boxes below a group of snapshots indicate the stage 229 name (or transition name), the time points in growth which this stage encompasses, and some distinguishing characteristics of that stage. 230

231

232 The output of this framework has given metabolic "snapshots", consisting of plant mass, growth rate, and flux rate of each reaction, at one-hour intervals across 61 days of growth, as the plant 233 234 disperses all new seeds (through silique shattering) by 61 days after germination (DAG) [24]. 235 After 61 DAG the plant begins to desiccate, eventually resulting in plant death [24]. The p-236 ath780 model is not used to model plant metabolism after 61 DAG because no in vivo data has 237 been found in literature concerning the metabolomics of plant death and desiccation. This optimization-based framework has allowed for the sampling of changes in central carbon 238 metabolism at different stages in the arabidopsis lifecycle (see Figure 3). For all the following 239 240 analyses, the objective of this framework at each point has been the maximization of the sum of 241 all tissue biomass production rates, unless otherwise indicated.

242

243 In having determined the mass steps taken for each hour intervals, three FBA-like calculations at 0, $\frac{1}{3}$, and $\frac{2}{3}$ hours past the hour have been made to increase the accuracy of the derivative 244 estimate by an explicit numerical integration method calculating the mass step at each hour 245 246 interval using Heunn's rule for the third order Runge-Kutta method (see methods for greater detail). Figure 4 shows a more detailed workflow for each individual step in the form of a 247 workflow diagram. Optimal flux points at every whole hour have been saved as the optimal flux 248 249 rates at that growth point. To evaluate these balanced flux estimates, Flux Variability Analysis 250 (FVA) [29] has been performed, at nine points, selected to represent each non-transition growth 251 stage and diurnal status in those stages, subject to all growth constraints and a growth rate equivalent to the optimal growth rate (see methods for enumeration of these points). 252

253

254 Figure 4. The workflow diagram of the p-ath780 model, including inputs (orange), outputs 255 (green), and internal workflow (blue). The inputs for the p-ath780 model include each individual tissue model, a file of growth specifications, and a list of point at which to take metabolic 256 257 "snapshots". The internal workflow has read these inputs and then used them to construct model objects (bold, Times New Roman text) which are used to perform FBA, to solve for what the 258 259 plant mass step is from the current to the next "snapshot", and to perform FVA. For each 260 iteration, the time of the snapshot is stepped forward 1/3 step (hour), the FBA model object is solved, the mass step is calculated, and process is repeated. Every third iteration (e.g. where step 261 = 3), Heun's method for a third order Runge-Kutta is used to estimate the plant mass step from 262 263 the previous whole hour to the next whole hour and FVA is performed on the model at the previous whole hour using saved values. Once all iterations are complete (e.g. model is at final 264 265 time point), then the output files are written.

266

The simulations of the p-ath780 model has been advanced through several growth stages using 267 time point for changes in growth stage taken from experimental data [24]. In the seed 268 269 germination stage, uptake of fatty and amino acids from seed storage has been modeled as a constant rate of fatty acid usage which results in all stored fatty and amino acids being depleted 270 by the end of the seed germination stage [30]. The 12 hours of light and 12 hours of dark diurnal 271 272 rhythm has been chosen to match experimental conditions for studies on starch and sucrose 273 storage/uptake dependence on the diurnal cycle [31]. These patterns have been fit to a sine wave 274 model constraint with +1% tolerance. In growth stages when plant tissue ratios have been constant, the tissue mass ratio values had been taken from values typical for herbaceous plants 275 276 [32].

277

Returning to the design-build-test cycle used to improve the p-ath780 model, experimental data 278 related to plant growth and plant growth stages have been collected from a variety of literature 279 sources to serve as checks for the accuracy of the modeled system [24,33]. The first set of 280 experimental data has included mass data, including whole plant and individual tissue. At 281 282 approximately 17, 24, and 31 DAG the total dry plant mass should be between 0.5 and 2.0 mg; 2 and 5 mg; and 10 and 30 mg, respectively [33]. Once the design-build-test cycle has been 283 284 completed, the p-ath780 model has shown a total dry plant mass of 0.554 mg at 17 days (408 285 hours), 3.74 mg at 24 days (576 hours), and 25.2 mg at 31 days (744 hours) after germination, demonstrating growth consistent with in vivo data. Furthermore, the relative growth rate for the 286 first 31 days of plant growth has been reported as between 0.21 and 0.25 day⁻¹ [33], and the final 287 288 p-ath780 has shown a relative growth rate of 0.246 over this time period. To adjust model

289 behavior in latter stages of growth, tissue-specific mass data has been obtained from literature. Specifically, the dry weight of the stem, the leaves, and the seeds has been reported as 290 approximately 188 mg (standard deviation 39.3 mg), 163.7 mg (standard deviation 52.0 mg), and 291 292 127.9 mg (standard deviation 52.7 mg), respectively [24]. As p-ath780 models both plant growth and loss of seed (and other) mass in the silique ripening stage, the peak mass of each of these 293 tissues has been comparted to this data. In the final p-ath780 model, the peak mass of the stem, 294 295 leaves, and seeds has been determined as 189 mg, 177 mg, and 130, respectively, all of which are 296 within one standard deviation of the experimental value (see the methods section for how tissue masses are determined). In summary, through the results of the design-build-test cycle 297 implemented, in silico tissue and plant mass values are similar to in vivo data, thus showing 298 strong agreement with respect to growth trends. 299

300

In early rounds of model reconstruction, it has been noticed that the plant model's photosynthesis 301 is too efficient at fixing carbon. This is due to the fact that plants do not make full use of 302 303 available light source(s), but the reconstructed metabolic model had been. Published in vivo data which has been used in the modeling and verification of p-ath780 made use of fluorescent lights, 304 which have tight transmission spectra peaks at 544 and 609 nm [34]. In contrast, peak 305 306 absorbance for plant leaves is at approximately 440 and 680 nm [35]. The problem of the availability of light has been addressed by scaling the transmission of the fluorescent lights by 307 the absorbance of plant leaves. This has left approximately 21.06% of light transmitted by the 308 fluorescent bulbs usable by the plant (see Supplemental File 5 and methods). An additional 309 310 restriction, namely biomass yield, has also been placed on metabolic efficiency in plant systems. 311 Biomass yield has been defined as the carbon fraction of biomass produced appearing in new

312 growth for each unit of carbon used for growth [36]. This yield value accounts for repair of 313 existing biomass and replacement of lost biomass. Experimentally, this value has been identified as generally between 0.7 and 0.85 [37]. Here, for p-ath780 mass values to align with 314 315 experimental data, two separate mass yield vales have been set at 0.32 and 0.23 for when the plant system lacks and has seed tissue respectively. This represents an incongruity with 316 experimental evidence, although this value is still in the same order of magnitude as 317 experimental evidence. All files necessary for p-ath780 have been included with this work in 318 Supplemental Files 7 through 16. The *in silico* results of the final p-ath780 model can be found 319 320 in Supplemental File 17.

321

In silico Plant Growth under Alternative Objective Functions. A total of six different objective 322 323 functions for p-ath780 have been investigated and a summary of that investigation has been shown in Table 1. In all cases, root and stem tissue objectives have been defined as biomass 324 325 production, where the leaf and seed objective functions are varied. When any tissue has a non-326 biomass objective, that objective is weighted by some scaling factor (either α for light-based objectives or β for fatty acid-based objectives) to ensure the new terms do not dominate or be 327 insignificant compared to biomass (e.g. be an order or magnitude or more different) and to 328 investigate the different effects of weight factors. The first row (green) of Table 1 contains the *in* 329 vivo arabidopsis data which has been used as targets and verification of the p-ath780 model. The 330 second row (blue) contains the *in silico* data from p-ath780 where the objective for all tissues is 331 biomass production (default objective), and has summarized the findings of the preceding 332 subsection. For the mathematical definition of this and other objective functions discussed here 333 334 see the methods section. The next two objective functions presented (grey) we have considered

335 set the seed tissue-level objective as the maximization of fatty acid stored in the seed tissue at two different weight factor values (β). At low β values, this causes a scavenging of carbon 336 wasted in the plant metabolism which is then diverted to the seed fatty acid production without a 337 338 change in plant growth. At high β values, this alternate seed objective results in stunted plant growth as carbon used elsewhere is diverted to the seed tissue. This alternate objective function 339 has no effect when the plant does not have seed tissue present. Photonic efficiency for the leaf 340 341 tissue has been attempted as an alternative objective function and results are reported in the next 342 two grey rows; however, depending on the weight of the photonic efficiency parameter, the 343 model is generally photophobic (no light has been uptaken) or grows as normal. In all photophobic growth cases, the plant mass of the model eventually becomes negative, leading to 344 nonsense in later time points, thus the results of these α values are not reported. No α value has 345 346 been identified which produced a result between these extremes (photophobic and normal 347 growth), and these attempts are not included in this work. The full output of each reported result 348 can be found in Supplemental File 17. The final objective function investigated (and reported in 349 Table 1) is one which combined the leaf linear photonic efficiency objective and the seed fatty acid storage objective at a moderate weight value (values enumerated in Table 1). As with other 350 351 linear photonic efficiency objectives, the amount of light uptaken by the plant is unaffected, and 352 as with other investigations of the seed fatty acid objective, the plant growth is stunted when the 353 seed tissue is present. In summary, the p-ath780 model is robust to small and moderate perturbations in the objective related to photonic efficiency, fails with large perturbations to 354 355 photonic efficiency objectives, and results in continuously changeable growth levels to 356 metabolite production objectives.

357

Discussion 358

In the current work, a multi-tissue core metabolism stoichiometric model, including leaf, root, 359 360 seed, and stem tissues, of Arabidopsis thaliana has been reconstructed (Figure 3), and linked in 361 an FBA-based optimization framework (Figure 1). This framework has been embedded in a workflow (Figure 1) which has simulated how plant metabolism evolves over time with respect 362 to the presence or absence of light, the transition to different growth stages, and the gain or loss 363 of tissues (such as seed). This model has incorporated a wide variety of data which has not been 364 incorporated in other stoichiometric modeling efforts such as the effect of plant mass, the effect 365 of tissue mass difference on tissue interactions, whole-plant growth heuristics such as yield, the 366 availability of usable light, and biomass-based plant maintenance (as opposed to ATP-based). 367 The tissue models taken together with these literature-based constraints has been named the p-368 ath780 model. The whole-plant growth characteristics of p-ath780 have shown general 369 agreement with experimental data, particularly with respect to whole plant mass at certain 370 371 growth milestones and lifecycle tissue yields.

372

The design-build-test cycle used to develop and tune p-ath780, shown in Figure 3, has been 373 implemented. As a result, in the final p-ath780 model, in silico predictions compared well to in 374 375 vivo data, particularly plant, leaf, seed, and stem masses, with the exception of biomass yield. 376 The incongruity between *in* vivo and *in silico* biomass yield has likely resulted from the p-ath780 model only having included primary carbon metabolism, which in turn means that plant biomass 377 has been built entirely from generally less metabolically expensive primary metabolites. This had 378 379 resulted in too efficient biomass production, hence the lower yield for the model. This 380 discrepancy in biomass yield has served to highlight the large effect of secondary metabolism on

plant growth and has served as a correction factor on the model due to the lack of modeled secondary metabolism. In addition, likely the plant mass yield is lower when seed tissue is present because flower tissue is metabolically expensive yet is not modeled in this work. In additional, biomass drains for plant senescence and maintenance have been included [36,37].

385

Once the model has been developed, six different objective functions have been applied to it, 386 387 including the default objective of maximizing plant growth, linear photonic efficiency, and seed fatty acid production. In summary, the p-ath780 model is robust to small and moderate 388 389 perturbations in the objective related to photonic efficiency, breaks when large perturbations are made to the photonic efficiency objective, and is capable of some fine tuning with respect to 390 metabolite production objectives. The behavior of p-ath780 with respect to the linear photonic 391 392 efficiency objective function is due to multiple factors. First, as the partially photophobic case exists, this suggests that seed tissue is the most metabolically expensive tissue to create. This is 393 394 as expected because the seed tissue requires storage of high-energy molecules such as fatty acids, 395 proteins, and sugars to feed its embryo when dispersed. Further, the rate of biomass production for all tissues are linked in the optimization-based framework. Secondly, seed tissue has a target 396 fraction of overall plant mass which it must grow to for each hour interval of the flower 397 development stage. If seed tissue is too metabolically expensive to produce, relative to the cost to 398 uptake more light, it appears that the solution strategy then becomes to decrease the mass of 399 other tissues while leaving the growth of the seed tissue to be minimal. This can result in sharp 400 changes in mass which falls outside the realm of stability for Heunn's third order Runge-Kutta 401 rule, resulting in predictions with no biological relevance. Thirdly, biomass composition and 402 403 metabolic cost is not dependent on the amount of light uptaken, so the biomass cost is constant

404 with respect to light uptaken so there is no steady equilibrium between the two terms except at 405 the extremes. Fourthly, minimizing light uptake and maximizing biomass growth as objectives are competitive, increase light uptake results in increased growth in stoichiometric models. In 406 407 contrast, this is not an issue for maximizing fatty acid production as biomass partially consists of fatty acids, therefore these two objectives can be complimentary to some degree and a variety of 408 β values can be used without the model failing to find a solution. Theoretically, there exists some 409 410 highly-specific value of α at which the cost to the light needed to drive growth is balanced with the rate of production of new biomass, but this is an unsteady equilibrium which when the value 411 of α is slightly perturbed finds the new equilibrium at either extreme. Therefore, the value of α 412 might be imagined as a fulcrum between the two terms as illustrated in Figure 5. Figure 5(A)413 restates the linear photonic efficiency objective equation, and Figure 5(A-D) represents the 414 415 action of α as a fulcrum. Figure 5(D) in particular illustrates why the p-ath780 model is robust to 416 changes in the value of α below this theoretical balance point.

417

418 **Figure 5.** This figure highlights how the weight factor, α , fails to reach some kind of equilibrium between light uptake and biomass production in the linear photonic efficiency objective. A) 419 Restates the linear photonic efficiency objective function. B) Shows the theoretical balance 420 421 which might exist between light uptake and biomass production at some highly specific value of α . C) Shows how as slight increase in α from that point causes light to outweigh biomass in 422 terms of influence on the objective function value. This results in photophobic growth as light 423 "outweighs" growth. D) Shows how as slight decrease in α from that point causes light to 424 425 outweigh biomass in terms of influence on the objective function value. This results in normal 426 growth as growth "outweighs" light.

427

428 This work does not account for diurnal rhythms in the transcriptome of Arabidopsis thaliana for several reasons. Firstly, the majority of transcriptomic studies have focused on the regulatory 429 430 network of proteins which regulate metabolism based on the availability of light and rhythm [43,44], rather than considering metabolic proteins which are represented in the p-ath780 model. 431 Secondly, tissue-specific diurnal transcriptomic information is only available for the leaf tissue 432 [43,44]. Further, these experiments generally consider a single point in the growth cycle of 433 arabidopsis under specific growth conditions. The framework of p-ath780 is already highly 434 435 constrained, and that the inclusion of too much data will invariably cause model failure. This is because in vivo experiments, in general and those used in this work, often occur under different 436 conditions, at different points in the plant lifecycle, have different methods to some degree, or 437 438 even seem quantitatively difference due to the noise inherent to biological systems, making 439 alignment of quantitative *in vivo* data from too many sources impossible. In this work, we have decided to use data which described a wide range of time point in arabidopsis growth, such as 440 441 biomass yield, relative growth rate, growth up to a certain time point, and overall tissue yield, rather than data which may be specific to a single point in growth, such as transcriptomics. 442

443

This work provides the basis for much future development and sophistication. For instance, the 444 current p-ath780 model could be further sophisticated by adding the secondary metabolism of the 445 plant system, which is a considerable resource drain in many plant systems. Further, at present 446 several simplifications are made regarding tissues, particularly related to seed tissue. For 447 instance, the model currently assumes that when the plant is flowering, that flower biomass and 448 449 metabolism is roughly equivalent to that of the seed. While this resulted in a simpler model, this

450 model cannot be then used to investigate certain metabolic hypothesis such as the cost to the 451 plant resulting from flower pigmentation, pollen, and nectar production. Future work will include producing models for other plant tissues, such as flowers. In addition, as this is a core carbon 452 453 metabolism model, it is likely quite similar to the core metabolism of other plant systems; therefore, the p-ath780 model can serve as a basis for the development of lifecycle models for 454 other plant systems, particularly annual eudicots which are of agricultural interest, such as rice 455 456 (Oryza sativa), potatoes (Solanum tuberosum), tomatoes (Solanum lycopersicum), and soybeans (Glvcine max). 457

458

Methods 459

Overview of the reconstruction of core metabolic models of leaf, root, seed, and stem tissues. 460 The seed tissue model. The general workflow which has been used for the development of the 461 four core tissue models has been illustrated in Figure 3. We have developed the seed model first, 462 463 with the central metabolic pathways based on a Metabolic Flux Analysis (MFA) of four seed genotypes published previously [27]. We have then manually filled gaps in this model with 464 reactions based on literature and genomic evidence [26] or with reactions being necessary for 465 466 ensuring model connectivity. The stoichiometric coefficients of biomass precursors have been determined using sink reactions, dry biomass weight composition, and amino acid mass ratios 467 provided in a previous work [27] (see Supplemental File 22). The resultant seed tissue model has 468 focused on storage, respiration, and growth, and consists of 428 reactions, 529 genes, and 411 469 metabolites (included as Supplemental File 1). 470

471

The leaf tissue model. Next, we have reconstructed the leaf model by taking common 472 473 reactions/pathways from the seed model and adding synthesis pathways for amino acids that are

474 not synthesized in the seed, in addition to photosynthesis, carbon fixation, gluconeogenesis, and 475 transport reactions. We have then developed the biomass equation for the leaf tissue using that of 476 a previously published Arabidopsis model [18] (see Supplemental File 22). The resultant leaf 477 tissue model has focused on photosynthesis, respiration, gas exchange, fatty acid synthesis, and 478 growth, and contains of 537 reactions, 703 genes, and 479 metabolites. We have included the 479 leaf model with this work as Supplemental File 2.

480

The root and stem tissue models. We have constructed the root and stem models, similarly, by 481 482 extracting common reactions/pathways from the seed model and adding necessary transport and 483 exchange reactions. Then exchange reactions have been added to allow the root to be linked to micronutrient uptake processes from the soil, and the stem to be involved in inter-tissue transport 484 485 processes. In the absence of Arabidopsis-specific estimates, the dry weight composition of switchgrass (*Panicum virgatum*) root and stem [28] have been assumed to be equivalent to the 486 487 biomass composition of these tissues in Arabidopsis. Due to the low detail level of the dry weight composition analysis, the biomass of root and stem tissues have been composed entirely 488 of carbohydrates. The resultant root tissue model has focused on nutrient uptake, transport, and 489 growth, consisting of 130 reactions, 250 genes, and 126 metabolites, while the stem tissue model 490 focuses on transport and growth, consisting of 160 reactions, 250 genes, and 140 metabolites. 491 492 We have included the root and stem models with this work as Supplemental Files 3 and 4 493 respectively.

494

495 Confidence scoring. Reaction confidence scores have been defined in a manner consistent with a 496 previously published protocol [26]. Additional information on confidence scoring of the p-497 ath780 model can be found in Supplemental File 22.

498

Curation of all these tissue models. For all four models, we have balanced (both in terms of 499 elements and charge) all model reactions and have resolved thermodynamically infeasible cycles 500 by removing reactions, breaking composite reactions, and adding metabolic costs to transport 501 502 reactions. For all these tissue models, GPR links have been established through a largely 503 automated workflow utilizing the KEGG API for the majority of reactions using the code 504 included in Supplemental File 18. This is followed by having manually curated the GPR links and/or inclusion rational of reactions with non-KEGG identifiers. The count of tissue model 505 506 reactions present in KEGG-defined pathways is shown in Figure 2(A), showing pathways 507 common to most all tissue models, and Figure 2(B), showing pathways common to seed and leaf 508 tissues, these figures have been created using code included in Supplemental Files 19, 20, and 509 21. The results of this automated workflow can be found in Supplemental File 5. Sources for reactions included in leaf, root, seed, and stem models are shown in Figure 2(C-F), respectively 510 through confidence scoring (see confidence score section). Similarly, the confidence scores for 511 512 all reactions in the p-ath780 model have been reported in Figure 2(G).

513

514 *Overview of the developed of the optimization-based framework of p-ath780.* The models have 515 next been linked using well-known computational framework known for modeling microbial 516 communities [25]. An objective function for each of these models has then been defined, 517 specifying the maximization of the tissue-level biomass production rate followed by adding

518 constraints for simulating growth in light and dark conditions. Next, literature information 519 including embryo mass [30], initial tissue masses [38], growth stages [24], time points at which 520 growth stages occur [24], constraints to link tissue growth rates to appropriate tissue ratios, 521 transpiration [33,39], leaf surface area [28], usability of provided light [31,34,35], and defining changes in tissue mass ratios [24,40] has been integrated into these models, which are typically 522 overlooked in most other SMs. In this work, we have decided to simulate arabidopsis biomass 523 524 across 61 days (1464 hours) of growth, as all plant seeds are dispersed by day 61, and after 525 which *in vivo* data on plant growth and mass is sparse. More specific details can be found in the following sub-sections. The full optimization-based framework used in this work has been 526 provided in Supplemental File 6, and further requires Supplemental Files 7 through 16. 527

528

529 Generalized statement of the FBA-like optimization-based framework used. The optimization-530 based framework used can be stated in general terms as follows. The FBA-based framework which determines the optimal rates of flux through each reactions can be stated as follows (using 531 532 the default objective).

533

$$maximize \ Z = v_{leaf, biomass} + v_{root, biomass} + v_{stem, biomass} \tag{1}$$

Subject to

$$10 \ge \sum_{j \in J} S_{ij} v_j \ge 0 \qquad \qquad \forall i \in I \qquad (2)$$

 $M_{leaf}v_{CO_2,in,leaf}$

$$\geq M_{root} v_{CO_2,out,root} + M_{seed} v_{CO_2,out,seed}$$
(3)

$$+ M_{stem} v_{CO_2,out,stem}$$
 (when light available)

$$M_{leaf}v_{O_2,out,leaf}$$

 $v_{m,in,root} \leq$

$$\geq M_{root} v_{O_{2},in,root} + M_{seed} v_{O_{2},in,seed}$$
(4)
+ $M_{stem} v_{O_{2},in,stem}$ (when light available)
 $v_{m,in,root} \leq M$ $\forall m \in Micro$ (5)
 $M_{root} v_{m,out,root} \leq M_{root} v_{m,in,root}$ $\forall m \in Micro$ (6)

$$M_{root}v_{m,out,root} = M_{stem}v_{m,in,stem} \qquad \forall m \in Micro$$
(7)

$$M_{stem}v_{m,out,stem} \le M_{stem}v_{m,in,stem}$$
 $\forall m \in Micro$ (8)

$$M_{stem}v_{m,out,stem} = M_{leaf}v_{m,in,leaf} + M_{seed}v_{m,in,seed} \qquad \forall m \in Micro \qquad (9)$$

$$M_{stem}v_{x,in,stem} = M_{leaf}v_{x,out,leaf} \qquad \forall x \in X$$
(10)

$$M_{stem}v_{x,out,stem} = M_{stem}v_{x,in,stem} \qquad \forall x \in X$$
(11)

$$M_{stem}v_{x,out,stem} = M_{seed}v_{x,in,seed} \qquad \forall x \in X$$
(12)

$$M_{stem}v_{sucrose,in,stem} = M_{leaf}v_{sucrose,out,leaf}$$
(13)

$$M_{stem}v_{sucrose,out,stem} \le M_{stem}v_{sucrose,in,stem} \tag{14}$$

$$M_{stem}v_{sucrose,out,stem} = M_{root}v_{sucrose,in,root} + M_{seed}v_{sucrose,in,seed}$$
(15)

$$v_{starch,store,leaf} = s_{la} \sin\left(s_{lf}(n+s_{lx})\right) \tag{16}$$

$$v_{starch,store,stem} = s_{sa1} \sin\left(s_{sf1}(n+s_{sx1})\right) \tag{17}$$

$$v_{sucrose,store,stem} = s_{sa2} \sin\left(s_{sf2}(n+s_{sx2})\right) \tag{18}$$

$$v_{water,in,root} \le M \tag{19}$$

$M_{root}v_{water,out,root} = M_{stem}v_{water,in,stem}$ (20)

$$M_{stem}v_{water,out,stem} = M_{leaf}v_{water,in,leaf} + M_{seed}v_{water,in,seed}$$
(21)

$$v_{water,in,leaf} = t_{leaf} (when light available)$$
(22)

$$v_{root,biomass} = \ln(\mu) + v_{leaf,biomass}$$
(23)

$$\mu = \frac{x_{root} M_{leaf}}{x_{leaf} M_{root}} \tag{24}$$

$$v_{seed,biomass} = \begin{cases} 0 & M_{seed} = 0, s = 0\\ \ln(\theta) + v_{leaf,biomass} & M_{seed} \neq 0, s \neq 0\\ -v_{leaf,biomass} & M_{seed} \neq 0, s = 0\\ v_{leaf,biomass} & M_{seed} = 0, s \neq 0 \end{cases}$$
(25)

$$\mu\theta = \frac{x_{seed}M_{leaf}}{x_{leaf}M_{seed}} \tag{26}$$

 $v_{stem,biomass} = \ln(\lambda) + v_{leaf,biomass}$ (27)

$$\lambda = \frac{x_{stem} M_{leaf}}{x_{leaf} M_{stem}} \tag{28}$$

$$v_{seed,biomass\ loss} = \begin{cases} -v_{seed,biomass} & n \ge n_{flowering}\ n \ge n_{seed\ loss} \\ 0 & n \le n_{seed\ loss} \end{cases}$$
(29)

$$v_{scen} = \left(\frac{k_m + k_s}{24}\right) M_{tissue} \tag{30}$$

534

535 Where I is the set of metabolites; J is the set of reactions; *Micro* is the set of micronutrients (phosphate, ammonium, and sulfate) and is a subset of I; X is the set of amino acids which are 536 synthesized in the leaf tissue and exported to other tissues; and Y is the set of sugars stored by 537 538 various plant tissues. In addition, M is defined as a very large number, t_{leaf} is the massnormalized transpiration rate from the leaf; s_{la} , s_{sa1} , and s_{sa2} are the amplitudes of the sine wave 539 modeling of starch storage in the leaf and stem and sucrose storage in the stem, respectively; s_{lf} , 540 s_{sf1} , s_{sf2} are the frequencies of the sine wave modeling of starch storage in the leaf and stem and 541 542 sucrose storage in the stem, respectively; s_{lx} , s_{sxl} , and s_{sx2} are the x-intercept shifts of the sine 543 wave modeling of starch storage in the leaf and stem and sucrose storage in the stem, respectively; s is the level of seeding of the model; x_{tissue} is the fraction of total plant mass 544

accounted for by that tissue; and M_{tissue} is the mass of the given tissue. The following subsections will explain the constraints used in the FBA framework.

547

548 *Defining model objective functions.* For most analyses and results, the objective function of p-549 ath780 has been to maximize the sum of the biomass production rates for all four tissues 550 according to the following equation (referred to as the default objective).

551

$$maximize \ z = v_{growth \ leaf} + v_{growth \ root} + v_{growth \ seed} + v_{growth \ stem}$$
(31)

552

Where z has been defined the objective function and $v_{growth\ tissue}$ is defined as the rate of biomass production, in units of h⁻¹, of the tissue referenced. This objective function is approximately equivalent to having maximized the growth rate (change in mass per unit time) of the plant as a whole. This objective function has led to one major issue, namely how to avoid the model producing only the metabolically "cheapest" tissue which could result in the maximum objective value but is biologically unrealistic. This is addressed by equations (23) through (28) and will be further discussed later.

560

It has been noted that the maximization of plant biomass has not been the only feasible objective function for plant SM system, for instance one alternate objective function is the maximization of plant photonic efficiency [15,16]. This objective has generally been framed as minimizing the amount of light used by the plant system, given a required growth rate [15,16]. As it has been assumed that the only (significant) photosynthetic tissue in the p-ath780 model is the leaf tissue,

bioRxiv preprint doi: https://doi.org/10.1101/761189; this version posted September 9, 2019. The copyright holder for this preprint (which was not certified by peer review) is the author/funder, who has granted bioRxiv a license to display the preprint in perpetuity. It is made available under aCC-BY-NC 4.0 International license. A Lifecycle Metabolic Modeling Framework Schroeder & Saha, 2019

only the objective with relation to the leaf tissue has been altered. As a result, the leaf tissue termin equation (1) has been replaced with a photonic efficiency term in the following equation.

568

$$maximize \ z = -\alpha \left(v_{photon \ uptake} \right) + v_{growth \ root} + v_{growth \ seed} + v_{growth \ stem}$$
(32)

569

570 Where α has been defined a correction factor to scale $v_{photon\,uptake}$ to be on the same order of 571 magnitude as the growth rates for each other tissue.

572

An alternative objective function has also been defined for the seed tissue. Specifically, as fatty acids have been shown to one of the most prominent forms of carbon storage in the seed tissue [38], the alternate objective function is the maximization of seed fatty acid stores. This has resulted in seed objective function as follows:

577

maximize
$$z = v_{growth \ root} + v_{growth \ root} + \beta \sum v_{FA \ sinks} + v_{growth \ stem}$$
 (33)

578

579 Where the new seed flux term is defined as the sum of fatty acid storing (sink) reactions and β 580 serves to reduce this term to be equal in order of magnitude to the other objectives. Similar to α , 581 β has been determined through trial and error. One additional objective function has been studied 582 which combines linear photonic efficiency and fatty acid storage:

583

$$maximize \ z = -\alpha (v_{photon \ uptake}) + v_{growth \ root} + \beta \sum v_{FA \ sinks} + v_{growth \ stem}$$
(34)

584

Equation (33) has combined three separate objective types: linear photonic efficiency (leaf), biomass production (root and stem), and fatty acid storage (seed). It should be noted that the objective for the root and stem tissues are always to maximize biomass production. For more details see Supplemental File 22.

589

590 *Mass balance*. In this model, the mass balance, equation (2), is allowed some flexibility for the 591 storage of metabolites in the plant tissue up to 10 mmol per gDW hour. This has been found to 592 be necessary in the design-build-test cycle so that all points would be feasible.

593

*Enforcing net CO*₂ *consumption O*₂ *production.* In equations (3) and (4), it is required that the net effect plant metabolism is carbon fixation and oxygen production, since this is a well-known role of plant systems (see Supplemental File 22).

597

Enforcing logical flow of micronutrients. In equations (5) through (9) the logical flow of 598 599 micronutrients is dictated. Equation (5) ensures that the uptake rate is bounded, equation (6) ensures that the rate of each micronutrient exported by the root to the other tissues is less than or 600 equal to that uptaken by the root from the soil, allowing for the root to use a portion of the uptake 601 nutrients. Equation (7) ensures that all micronutrient exported by the root is uptaken by the stem, 602 and equation (8) is essentially the same as equation (6), but for the stem tissue. Finally, equation 603 604 (9) ensures that the micronutrients exported by the stem are all given to other tissues, specifically 605 leaf or seed. Both sides of the equation in equations (6) through (9) are multiplied by each tissues mass to convert the units of the constraint from mmol per gDW hour to mmol per hour as each 606 607 tissue has a different mass value in gDW. For more details see Supplemental File 22.

608

609 Enforcing logical flow of amino acids. Similar to micronutrients, the logical flow of amino acids has been defined explicitly via equations (10) to (12), as having been synthesized in the leaf 610 611 tissue and exported to seed tissue. This is because seed tissue has not been shown to produce all needed amino acids in the MFA study consulted [27], and the root and stem models do not 612 require amino acids for biomass production in the defined biomass composition. Essentially, 613 these constraints ensure that all amino acids exported by the leaf are uptaken by the stem 614 [equation (6)]; that these amino acids are not stored in the stem [equation (7)]; and that all amino 615 616 acids are exported by the stem to the seed tissue. For more details see Supplemental File 22.

617

Enforcing logical flow of sucrose. As with amino acids, sucrose is modeled as being produced in 618 619 the leaf tissue and exported to other tissues. In contrast to amino acids, sucrose is necessary for all tissue models. Therefore, equation (13) is analogous to equation (10), equation (14) allows 620 the stem to use the sucrose it receives from the leaf, unlike equation (11), and equation (15)621 exports sucrose both to the seed and root, unlike equation (12). For more details see 622 Supplemental File 22. 623

624

Enforcing diurnal patterns of carbohydrate storage. Plants store carbohydrates in leaf and stem 625 tissues in the form of starch (leaf and stem) and sucrose (stem) in a pattern where the rates of 626 storage may be modeled by a sine wave with a period of 24 hours [31,41]. The calculations for 627 defining the necessary parameters, parameters s_{la} , s_{sa1} , s_{sa2} , s_{lf} , s_{sf2} , s_{lx} , s_{sx1} , and s_{sx2} in 628 equations (16) through (18), of the fit sine waves (see Supplemental Files 5 and 22). 629

630

Enforcing logical flow of water. The flow of water in the p-ath780 model is constrained as similar to that of micronutrients and are defined in equations (19) through (22), but without the equivalents of equations (6) and (8), and with the addition of a transpiration constraint. This difference is because oxidative phosphorylation in tissues creates water. Hence, in tissues without significant photosynthetic activity, water might be produced in this model, and the largest usage to which plants put water, to maintain turgor pressure, is not modeled as SMs use gDW as a basis of calculation, rather than fresh weight (see Supplemental File 22).

638

Defining the relationship between tissue growth rates. To avoid the aforementioned problem of having p-ath780 produce only the "cheapest" biomass, the growth rates of all four tissues have been linked by a series of constraints which ensure that they grow at rates which maintain the desired tissue mass ratios. The rate of biomass production determined by a SM is the exponential growth rate of the biological system being modeled [8]; therefore, plant mass can be defined as: 644

$$M_{tiss,n+1} = M_{tis,n} e^{v_{tis\,growth,n}t} \quad \forall tis \in [leaf, root, seed, stem]$$
(35)

645

646 Where *M* has been defined as the plant mass at time n + 1, $v_{plant growth,n}$ is defined as the rate 647 of plant growth at time *n*, and M_{n-1} is defined as the plant mass at time *n*. Further, the ratio of 648 the masses to two tissues can be defined with reference to a single tissue, such as leaf, in the 649 following manner:

650

$$M_{tiss,n} = \frac{x_{tis}}{x_{leaf}} M_{leaf,n} \quad \forall tis \in [leaf, root, seed, stem]$$
(36)

651

By having substituted the former equation into the latter and simplifying the result (see Supplemental File 22), linear equations have been written to constrain biomass production rates of root, seed, and stem tissues with respect to leaf tissue as follows:

655

$$v_{tiss,n} = \ln\left(\frac{x_{tis,n+1}M_{leaf,n}}{x_{leaf,n+1}M_{tis,n}}\right) + v_{leaf,n} \quad \forall tis \in [root, seed, stem]$$
(37)

656

This constraint we have added to the SM model, as equations (23) through (28) in order to ensure that all tissues do have biomass production (or loss) and that it is in an amount which will result in tissue masses in the correct proportions.

660

Ensuring non-productive loss of seed mass in silique shattering. A constraint has been found necessary to enforce that metabolites associated with the loss of seed biomass, modeled by the biomass production constraint having reversed flow, when seeds are being lost during silique shattering (in the Silique Ripening Stage) and are not recycled into other parts of plant metabolism. This constraint just does that by forcing recovered metabolites into the biomass loss reaction of the seed tissue.

667

Defining model maintenance and senescence costs. An important consideration in any SM is the definition of a maintenance cost, which is typically defined as ATP hydrolysis [26]. Biomassbased maintenance and senescence costs have been defined as they have been suggested as more accurate or applicable for plant systems [36,42], but have not yet been used in an SM. We have defined maintenance and senescence costs as a biomass drain on each tissue scaled by tissue mass in equation (30). A maintenance cost value of $k_m=0.03$ day⁻¹ has been defined which is in

674 an order of magnitude typical for plant systems [42], and the same value has been defined for 675 plant senescence, k_s, as this parameter appears to generally be of the same order of magnitude [36,42]. These rates are then converted into their per hour equivalent and scaled by tissue mass to 676 677 enforce these constraints. Only a single constraint has been defined for both phenomena as both are biomass drains whose effect is additive. Literature evidence, including pictorial evidence of 678 plant phenotype at various growth stages, appears to suggest that the rate of plant senescence 679 680 increases drastically as the flowering production stage finishes and the Silique Ripening phases begin (in literature, growth stage 0.65 to 9.70) [24]. Further, it appears that the plant no longer 681 maintains current mass, but allows tissues to die and desiccate [24]. This has been included in the 682 p-ath780 model in that plant senescence is increased by two orders of magnitude and plant 683 maintenance is set to zero following the end of the Flower Production stage. This results in a 684 685 growth curve in-line with in vivo evidence (see Table 1).

686

Other constraints enforced on the FBA-like optimization framework. There are other constraints 687 688 enforced on the optimization framework discussed above that are more difficult or cumbersome to state mathematically and are therefore discussed here. 689

690

Defining the usage of seed stores by the seedling. A seedling's source of carbon is primarily its 691 reserves of stored carbohydrates, proteins, and lipids. Namely, it has been shown that seeds have 692 693 stores of approximately 0.425 μ g of sucrose, 6 μ g of fatty acids, and 6 μ g of proteins (modeled here as component amino acids) available [30]. As no information concerning the pattern of 694 695 usage of the seed storage has been found, it has been assumed that the stores are utilized at a 696 constant rate during the duration of the seed germination period and that all the storage is fully

697 consumed by 88.5 hours after germination, which has been defined the point at which the 698 cotyledons are fully open and leaf development intensifies [24]. The rate at which the seedling 699 should have uptaken the seed storage has been determined by identifying the moles (mmol) of 700 each major component of the seed storage and dividing by the time over which the seedling consumes those. This has resulted in a mmol/h quantity. See Supplemental File 5 for this 701 calculation. This quantity has then been scaled by plant mass to result in a mmol/gDW \Box h 702 703 quantity, which is used to bound the uptake rates of seed store metabolites. As the leaf has 704 proven the most metabolically active tissue, it is assumed that the leaf tissue of an arabidopsis 705 seedling uptakes the stored fatty acids, amino acids, and carbohydrates which is provided for 706 seedling growth during the Seed Germination stage when the leaves have no access to light (see 707 Figure 1, Seed Germination).

708

709 Defining initial plant and tissue ratios. As the model advances plant and tissue masses with 710 respect to time, the establishment of initial mass for plant and tissues has become important in 711 this framework. Experimental evidence has shown that arabidopsis seeds have a fresh weight (FW) of 25.3 μ g and have only about 7% water content [30]. The embryo itself is assumed equal 712 713 to the seed mass less the mass of seed stores of sucrose (0.425 μ g), Fatty Acids (6 μ g), and 714 proteins (6 μ g) [30]. Having assumed that the dry matter content ratio holds for the embryo as 715 well, this has left approximately 11.0 μ g dry weight (DW) for the embryo. As information on the 716 ratio of tissue masses in arabidopsis has not been documented in literature, the general ratio for 717 herbaceous plants has been used as a starting point, namely 0.46:0.24:0.3 leaf:root:stem FW [32]. 718 This ratio has been converted to DW ratio for stoichiometric modeling. Experimental data has 719 shown that the dry matter content of leaf tissue is 0.212 DW/FW, of root tissue is 0.170 DW/FW,

and of the stem tissue is 0.176 DW/FW [44]. Having converted the FW ratios to DW ratios has given the ratio of 0.511:0.267:0.211 leaf:root:stem DW. While the dry matter content of an embryonic arabidopsis is much higher than that of a mature plant (the source of the utilized dry matter content ratios), this DW tissue ratio has non-the-less been assumed to be accurate for the embryo due to lack of evidence to the contrary.

725

726 Defining stage times. Time points which define the transition between different stages of growth 727 have been taken from a single source of experimental evidence [24]. Stage transitions selected 728 include the transition to stage 0.70 (Seed Germination to Leaf Development transition in Figure 729 3), stage 6.00 (Leaf Development to Flower Production transition in Figure 3), and stage 8.00 (Flower Production to Silique Ripening transition in Figure 3). Not all lifecycle stage transitions 730 731 for which there is experimental evidence have been incorporated into this model. In some cases, this has been due to a lack of metabolic relevance, such as the transition from stage 1.04 to stage 732 733 1.05 where the plant transitions from 4 rosette leaves to 5 rosette leaves that are greater than 734 1mm in length. This has not been important to the p-ath780 model as a ratio of plant mass to leaf surface area ratio is used instead [33] (see Supplemental File 5). Others cannot be modeled by 735 the current framework tissues such as stage 5.10 which is when the first flower bud is visible 736 [24], as the current p-ath780 model has no flower bud tissue. The length of the seed ripening 737 stage is also determined by experimental evidence [24]. 738

739

Defining the change in tissue mass ratios with growth stage. Using available literature evidence, two endpoints for the plant tissue mass ratios have been defined when no seeds are present and all seeds are produced [24,38]. The transition between these states are assumed to be linear with

respect to a parameter called seeding, defined above as *s*. These relationships are then modeled

744 as:

745

$$x_{leaf} = c_{leaf} * seeding + x_{leaf,0}$$
(38)

$$x_{root} = c_{root} * seeding + x_{root,0}$$
⁽³⁹⁾

$$x_{seed} = c_{seed} * seeding + x_{seed,0} \tag{40}$$

$$x_{stem} = c_{stem} * seeding + x_{stem,0}$$
(41)

$$c_{leaf} = -0.2514; c_{root} = -0.02862; c_{seed} = 0.2030; c_{stem} = 0.07698$$

$$x_{leaf,0} = 0.511; x_{root,0} = 0.267; x_{seed,0} = 0; x_{stem,0} = 0.211$$

746

Where x_{tissue} has been defined as the tissue mass fraction with respect to the total mass of the plant, c_{tissue} is defined as the change in tissue mass fraction with respect to seeding, and x_{tissue} is defined as the initial mass fraction of each tissue. The gain in the seeding parameter has been assumed to be linear with time and is fit to experimental time point describing the fraction of flowers produced [24] (see Supplemental Files 5 and 22).

752

Defining the availability of light. The amount of light available to the model to use for photosynthesis has been defined initially by literature sources used for other constraints [31], and scaled by the transmittance of that light source (fluorescent lights) [34] and the absorbance of arabidopsis leaves [34] and surface area to plant mass of arabidopsis leaves [33] to define the amount of light usable by the plant system, which has been approximately estimated to be 4.00 mmol/gDW plant-h. This value has been shown to be 21.50% of the total photons output by the fluorescent light (see Supplemental Files 5 and 22).

760

761

Defining the FVA for the p-ath780 model. A Flux Variability Analysis (FVA) model has been
defined for growth both in light and dark growth. All flux bounds and constraints are the same
and the FBA models, but the objective function is defined as:

765

$$maximize/minimize \ z = \gamma_j v_j \tag{42}$$

766

Where the FVA model solution has been iterated for each reaction j, and γ_i has been valued at 1 767 for the current reaction whose maximum and minimum are to be investigated and 0 for all others 768 769 and is stepped through first maximizing and then minimizing each reaction. Due to restrictions of 770 the time allowed for model solutions, nine points has been selected at which to perform FVA. 771 These points are 70 hours after germination (HAG, seed germination stage, dark), 408 HAG (leaf development stage, light), 576 HAG (leaf development stage, light), 590 HAG (leaf development 772 stage, dark), 800 HAG (flower production stage, light), 810 HAG (flower production stage, 773 774 dark), 1156 HAG (flower production to silique ripening transition), 1200 HAG (silique ripening 775 stage, light), and 1220 HAG (silique ripening stage, dark).

776

777 *Defining the mass step between time points.* Using the biomass production rates calculated by 778 the FBA-like optimization framework, a Constrained Non-linear System (CNS) of equations can 779 be defined to advance the plant mass by treating the growth rates as constants. This system of 780 equations has been derived from the basic principles of FBA (e.g. that growth rates are 781 exponential rates of growth) through a sequence of simplifications and assumptions which can be

found in Supplemental File 22, and therefore will not be elaborated on here. The end result is 782

shown below for a given time point *t*. 783

784

$$\frac{dM_{plant}}{dt}\Big|_{n \to n+1/3} = \frac{e^{v_{leaf,bio}}M_{leaf,n}}{x_{leaf,n}} \Big[x_{leaf,n}v_{leaf,bio,n} + \frac{d}{dt} \big(v_{leaf,bio,n}\big) + \xi(t)\Big]$$
(43)

$$\xi(t) = x_{root}\psi(t) + x_{seed}\pi(t) + x_{stem}\kappa(t) + x_{leaf}(\psi(t)\zeta(t) + \pi(t)\rho(t) + \kappa(t)\iota(t))\frac{d}{dt}(s)$$

$$d \qquad d \qquad (44)$$

$$+ x_{root} \frac{d}{dt} (\ln(\mu(t))) + x_{seed} \frac{d}{dt} (\ln(\theta(t))) + x_{stem} \frac{d}{dt} (\ln(\lambda(t)))$$

$$\psi(t) = \ln(\mu(t)) + v_{leaf,bio,n} \tag{45}$$

$$\pi(t) = \ln(\theta(t)) + v_{leaf,bio,n} \tag{46}$$

$$\kappa(t) = \ln(\lambda(t)) + v_{leaf,bio,n}$$
(47)

$$\zeta = \frac{c_{root}(c_{leaf}s + x_{leaf,n}) - c_{leaf}(c_{root}s + x_{root,n})}{c_{leaf}^2 s^2 + 2c_{leaf}s x_{leaf,n} + x_{leaf,n}^2}$$
(48)

$$\rho = \frac{c_{seed}(c_{leaf}s + x_{leaf,n}) - c_{leaf}(c_{seed}s)}{c_{leaf}^2 s^2 + 2c_{leaf}sx_{leaf,n} + x_{leaf,n}^2}$$
(49)

$$u = \frac{c_{stem}(c_{leaf}s + x_{leaf,n}) - c_{leaf}(c_{stem}s + x_{stem,n})}{c_{leaf}^2 s^2 + 2c_{leaf}sx_{leaf,n} + x_{leaf,n}^2}$$
(50)

$$\frac{d}{dt}\left(v_{leaf growth,n}\right) = \frac{3v_{leaf growth,n} - 4v_{leaf growth,n-1/3} + v_{leaf growth,n-2/3}}{2\left[\frac{1}{3}h\right]}$$
(51)

785

786 Where, μ , θ , λ are parameters defined in equations (24), (26), and (28), The above system of nine equations has nine corresponding variables: the mass step [LHS of equation (43)], $\xi, \psi, \pi, \zeta, \rho, \iota$, 787 788 and the time derivative of the leaf growth rate [LHS of equation (53)].

Equation (51), as shown above, comes from a backwards finite difference formula of error order 789

 h^2 . For the purposes of increased model accuracy and stability, the FBA-like framework is solved 790

relaxed using a tolerance parameter (*tol*) to a pair of inequalities:

795

$$\left|\frac{d}{dt}(v_{leaf\ growth,n})\right|$$

$$\geq (1-tol)\left|\frac{3v_{leaf\ growth,n}-4v_{leaf\ growth,n-1/3}+v_{leaf\ growth,n-2/3}}{2\left[\frac{1}{3}h\right]}\right| \quad (52)$$

$$+ O\left(\left[\frac{1}{3}h\right]^{2}\right)$$

$$\left|\frac{d}{dt}(v_{leaf\ growth,n})\right|$$

$$\leq (1+tol)\left|\frac{3v_{leaf\ growth,n}-4v_{leaf\ growth,n-\frac{1}{3}}+v_{leaf\ growth,n-\frac{2}{3}}}{2\left[\frac{1}{3}h\right]}\right| \quad (53)$$

$$+ O\left(\left[\frac{1}{3}h\right]^{2}\right)$$

796

Where, *tol* begins at 0.00 and increases by 0.10 for each iteration if a solution is not found. This results in an mixed-integer non-linear programming (MINLP) problem (8 equality constraints and 9 variables), and the BARON solver has been used to attempt to solve the model. In all cases where a solution has not been found via a CNS solver, a solution has been found using the MINLP solver at *tol* = 0.10. The above set of equations [either equations (43) through (51) as a CNS problem or (43) through (50), (52), and (53)] is solved three times to make estimates of the

803 LHS of equation (42) usable in Heunn's rule for explicit third-order Runge-Kutta method. For

804 why this method has been used (see Supplemental File 22).

805

$$\frac{dM_{plant}}{dt}\Big|_{n \to n+1/3} = k_1 \tag{54}$$

$$\frac{dM_{plant}}{dt}\Big|_{n^{1}/_{3} \to n^{+2}/_{3}} = k_{2}$$
(55)

$$\left. \frac{dM_{plant}}{dt} \right|_{n+2/3 \to n+1} = k_3 \tag{56}$$

806

After each partial step, the plant and tissues masses are updated for the next solution. These mass step estimates are then combined using Heunn's rule for explicit third-order Runge-Kutta method, where the new mass is calculated as follows.

810

$$M_{plant,n+1} = M_{plant,n} + h\left(\frac{1}{4}k_1 + \frac{3}{4}k_3\right)$$
(57)

811

812 And the mass of each individual tissue is then updated as follows:

813

 $M_{leaf,n+1} = x_{leaf,n+1} M_{plant,n+1}$ (58)

$$M_{root,n+1} = x_{root,n+1} M_{plant,n+1}$$
⁽⁵⁹⁾

$$M_{seed,n+1} = x_{seed,n+1} M_{plant,n+1} \tag{60}$$

 $M_{stem,n+1} = x_{stem,n+1} M_{plant,n+1} \tag{61}$

814

815 Why p-ath780 updates overall plant mass rather than solving the above problem for each 816 individual tissue is discussed in Supplemental File 22.

817

818 **Software platforms used.** See Supplemental file 23 for which programming language various 819 supplemental files utilize. For Python code, version 3.3 is used; for Perl, version 5.26 for Supplemental Files 18 through 21 and Strawberry Perl version 5.24.0.1 is used for Supplemental 820 File 8; GAMS code utilizes version 24.7.4. All GAMS and Python code, in addition code 821 included in Supplemental File 8 is run using the Holland Computing Center at the University of 822 Nebraska, Lincoln. Supplemental Files 18 through 21 utilize the additional module the LWP (the 823 world-wide web library for Perl) module 6.39, and have been run on a windows desktop 824 825 computer. 826

827 Code availability. The authors declare that the code supporting the findings of this study is
828 available within the article's Supplementary Information files.

829

Abbreviations used. For the convenience of our readers, a list of abbreviations used is givenbelow:

832 GPR: Gene-Protein-Reaction

833 SM: Stoichiometric Model

834 FBA: Flux Balance Analysis

835 FVA: Flux Variability Analysis

836 LP: Linear Problem

837 CNS: Constrained Non-linear System

- 838 MINLP: Mixed Integer Non-Linear Problem
- 839 arabidopsis: Arabidopsis thaliana
- 840 LHS: Left-Hand Side
- 841 wrt: with respect to
- gDW: grams Dry Weight 842
- 843 DW: Dry Weight
- 844 gFW: grams Fresh Weight
- FW: Fresh Weight 845
- 846 MFA: Metabolic Flux Analysis
- KEGG: Kyoto Encyclopedia of Genes and Genomes 847
- DAG: Days After Germination 848
- 849 HAG: Hours After Germination
- 850
- Acknowledgement. This work has been completed utilizing the Holland Computing Center of 851

852 the University of Nebraska, which receives support from the Nebraska Research Initiative. The

853 authors gratefully acknowledge funding from UNL Faculty Startup Grant 21-1106-4038.

854

855 Author contributions. Experiments have been conceived by R.S. and W.L.S. W.L.S. performed 856 the experiments and analyzed the data. R.S. and W.L.S. contributed analysis tools. R.S. and 857 W.L.S. wrote the manuscript.

858

| 859 | Supplementary information is provided. To help readers navigate the extensive set of included |
|-----|---|
| 860 | data and replicate this study, Supplemental File 23 provides an overview of the included |
| 861 | supplemental files and lays out the file structure to use in conjunction with the p-ath780 model. |
| 862 | |
| 863 | Conflict of interest: The authors declare no conflicts of interest. |

864 **References**

- 1. Beyer P, Al-Babili S, Ye X, Lucca P, Schaub P, Welsch R, et al. Golden rice: introducing the
- 866 β carotene biosynthesis pathway into rice endosperm by genetic engineering to defeat
- vitamin A deficiency. J Nutr. 2002;132:506S-510S.
- 868 2. Hall RD, Brouwer ID, Fitzgerald MA. Plant metabolomics and its potential application for
 869 human nutrition. Physiol Plant. 2008;132(2):162-175.
- 3. Gonzali S, Mazzucato A, Perata P. Purple as a tomato: towards high anthocyanin tomatoes.
 Trends Plant Sci. 2009;14(5):237-241.
- 4. Paddon CJ, Keasling Semi-synthetic artemisinin: a model for the use of synthetic biology in
 pharmaceutical development. Nat Rev Microbiol. 2014;12(5):355–367.
- 5. Hilder VA, Boulter D. Genetic engineering of crop plants for insect resistance a critical
 review. Crop Prot. 1999;18(3):177–191.
- 6. Chen THH, Murata N. Enhancement of tolerance of abiotic stress by metabolic engineering
 of betaines and other compatible solutes. Curr Opin Plant Biol. 2002;5(3):250–257.
- 878 7. Srinivasan S, Cluett WR, Mahadevan R. Constructing kinetic models of metabolism at
 879 genome-scales: A review. Biotechnol J. 2015;1359:1345–1359.
- 880 8. Orth JD, Thiele I, Palsson BØ. What is flux balance analysis? Nat Biotechnol.
 881 2010;28(3):245–248.
- 882 9. Burgard AP, Pharkya P, Maranas CD. OptKnock: a bilevel programming framework for
 883 identifying gene knockout strategies for microbial strain optimization. Biotechnol Bioeng.
 884 2003;84(6):647–657.
- 10. Ranganathan S, Suthers PF, Maranas CD. OptForce: An optimization procedure for
 identifying all genetic manipulations leading to targeted overproductions. *PLoS Comput Biol*

- 887 2010;6(4):1-11.
- 88811. Mahadevan R, Edwards JS, Francis DJ. Dynamic flux balance analysis of diaxic growth in
 889 Escherichia coli. Biophys J. 2002;83(3):1331–1340.
- 89012. Saha R, Liu D, Hoynes-O'Connor A, Liberton M, Yu J, Bhattacharyya-Pakrasi M, et al.
- Diurnal regulation of cellular processes in the Cyanobacterium synechocystis sp. strain PCC
- 6803: insights from transcriptomic, fluxomic and physiological analyses. MBio. 2016;7(3):1–

893 14.

- 89413. Ng CY, Jung M, Lee J, Oh M-K. Production of 2,3-butanediol in Saccharomyces cerevisiae
- by in silico aided metabolic engineering. Microb Cell Fact. 2012;11(68):1-14.
- 89614. Poolman MG, Miguet L, Sweetlove LJ, Fell DA. A genome-scale metabolic model of
 Arabidopsis and some of its properties. Plant Physiol. 2009;151(3):1570–81.
- 89815. Gomes de Oliveira Dal'Molin C, Quek LE, Palfreyman RW, Brumbley SM, Nielsen LK.
- AraGEM, a genome-scale reconstruction of the primary metabolic network in Arabidopsis.
 Plant Physiol. 2010;152:579–589.
- 90116. Gomes de Oliveira Dal'Molin C, Quek LE, Saa PA, Nielsen LK. A multi-tissue genomescale metabolic modeling framework for the analysis of whole plant systems. Front Plant Sci.
 2015;6(4):1–12.
- 90417. Grafahrend-Belau E, Junker A, Eschenröder A, Müller J, Schreiber F, Junker B. Multiscale
 905 metabolic modeling: dynamic flux balance analysis on a whole-plant scale. Plant Physiol.
 906 2013;163(2):637–647.
- 90718. Saha R, Suthers PF, Maranas CD. Zea mays iRS1563: a comprehensive genome-scale
 908 metabolic reconstruction of maize metabolism. PLoS One. 2011;6(7):1-12.
- 90919. Gomes de Oliveira Dal'Molin C, Quek LE, Palfreyman RW, Brumbley SM, Nielsen LK.

- 910 C4GEM, a genome-scale metabolic model to study C4 plant metabolism. Plant Physiol.
 911 2010;154(4):1871–1885.
- 20. Poolman MG, Kundu S, Shaw R, Fell DA. Responses to light intensity in a genome-scale
 model of rice metabolism. Plant Physiol. 2013;162(2):1060–1072.
- 914 21. Mintz-Oron S, Meir S, Malitsky S, Ruppin E, Ahoroni A, Shlomi T. Reconstruction of
- Arabidopsis metabolic network models accounting for subcellular compartmentalization and
 tissue-specificity. Proc Natl Acad Sci. 2012;109(1):339–344.
- 917 22. Simons M, Saha R, Guillard L, Clément G, Armengaud P, Cañas R, et al. Nitrogen-use
- 918 efficiency in maize (Zea mays L.): from "omics" studies to metabolic modelling. J Exp Bot.
- 919 2014;65(19):5657–5671.
- 920 23. Grafahrend-Belau E, Schreiber F, Koschutzki D, Junker BH. Flux balance analysis of barley
 921 seeds: a computational approach to study systemic properties of central metabolism. Plant
 922 Physiol. 2009;149(1):585–598.
- 24. Boyes DC, Zayed AM, Ascenzi R, McCaskill AJ, Hoffman NE, Davis KR, et al. Growth
 stage-based phenotypic analysis of Arabidopsis: a model for high throughput functional
 genomics in plants. Plant Cell. 2001;13:1499–1510.
- 926 25. Zomorrodi AR, Maranas CD. OptCom: A multi-level optimization framework for the
 927 metabolic modeling and analysis of microbial communities. *PLoS Comput Biol* 2012;8(2):1–
 928 13.
- 929 26. Thiele I, Palsson BØ. A protocol for generating a high-quality genome-scale metabolic
 930 reconstruction. Nat Protoc. 2010;5(1):93–121.

| 931 | 27. Lonien J, Schwender J. Analysis of metabolic flux phenotypes for two Arabidopsis mutants |
|-----|--|
| 932 | with severe impairment in seed storage lipid synthesis. Plant Physiol. 2009;151(3):1617- |
| 933 | 1634. |

28. Johnson JMF, Barbour NW, Weyers SL. Chemical composition of crop biomass impacts its

935 decomposition. Soil Sci Soc Am J. 2007;71(1):155-162.

- 936 29. Thiele I, Gudmundsson S. Computationally efficient flux variability analysis. BMC
 937 Bioninformatics. 2010;11(489):1-3.
- 938 30. Tomaz T, Bagard M, Pracharoenwattana I, Lindén P, Lee CP, Carroll AJ, et al.
- 939 Mitochondrial malate dehydrogenase lowers leaf respiration and alters photorespiration and
- plant growth in Arabidopsis. Plant Physiol. 2010;154(3):1143–1157.
- 31. Hendrik Poorte A, Nagel O. The role of biomass allocation in the growth response of plants
 to different levels of light, CO2, nutrients and water: a quantitative review. Aust J Plant
 Physiol. 2000;27(189):595–607.
- 32. Poorter H, Nagel O. The role of biomass allocations in the growth respose of plants to
 different levels of light, CO2, nutrients and water: a quantitative review. Aust J Plant Physiol.
 2000;27:595-607.
- 33. Clauss MJ, Aarssen LW. Phenotypic placity of size-fecundity relationships in Arabidopsis
 thaliana. J Ecol. 1994;82(3):447–455.
- 34. Bläsing OE, Gibon Y, Günther M, Höhne M, Morcuende R, Osuna D, et al. Sugars and
 Circadian Regulation Make Major Contributions to the Global Regulation of Diurnal Gene
- 951 Expression in Arabidopsis. Plant Cell. 2007;17:3257–3281.
- 952 35. Baleja R, Šumpich J, Bos P, Helštýnová B, Sokanský K, Novák T. Comparison of LED
- properties, compact fluorescent bulbs and bulbs in residential areas. Proceedings of the 16th

- International Scientific Conference on Electrical Power Engengineering; 2015 May 20-22;
 Kouty nad Desnou, Czech Republic: IEEE, 2015.
- 36. Cannell MGR, Thornley JHM. Modelling the components of plant respiration: representation
- 957 and realism. Ann Bot. 1999;85:55–67
- 37. Cannell MGR, Thornley JHM. Modelling the components of plant respiration: some guiding
 principles. Ann Bot. 1999:85:45–54.
- 38. Baud S, Boutin J, Miquel M, Lepiniec L, Rochat C. An integrated overview of seed
 development in Arabidopsis thaliana ecotype WS. *Plant Physiol Biochem* 2002;40:151–160.
- 962 39. Li B, Suzuki JI, Hara T. Latitudinal variation in plant size and relative growth rate in
- 963 Arabidopsis thaliana. Oecologia. 1998;115:293–301.
- 40. Solovchenko AE, Merzlyak MN. Screening of visible and UV radiation as a photoprotective
 mechanism in plants. Russ J Plant Physiol. 2008;55(6):719–737.
- 41. Yazdanbakhsh N, Sulpice R, Graf A, Stitt M, Fisahn J. Circadian control of root elongation
 and C partitioning in Arabidopsis thaliana. Plant, Cell Environ. 2011;34(6):877–894.
- 42. Amthor JS. The role of maintenance respiration in plant growth. Plant, Cell Environ.
 1984;7(8):561–569.
- 43. McClung CR. Plant circadian rhythms. The Plant Cell. 2006;18:792-803.
- 44. Oakenfull RJ, Davis SJ. Shining a light on the Arabidopsis circandian clock. Plant Cell
 Envirn. 2017;40:2571-2585.

973

974

975 Supporting Information Captions

976 Supplemental_File_1.txt: This file is a text file (extension ".txt") which contains the seed tissue
977 model of p-ath780. This file is referenced as "p-ath780Seed.txt" by other supplemental files,
978 particularly code, and this correct name should replace the default name for attached code to run
979 properly.

980

981 Supplemental_File_2.txt: This file is a text file which contains the leaf tissue model of p-982 ath780. This file is referenced as "p-ath780Leaf.txt" by other supplemental files, particularly 983 code, and this correct name should replace the default name for attached code to run properly.

984

985 Supplemental_File_3.txt: This file is a text file which contains the root tissue model of p-986 ath780. This file is referenced as "p-ath780Root.txt" by other supplemental files, particularly 987 code, and this correct name should replace the default name for attached code to run properly. 988

Supplemental_File_4.txt: This file is a text file which contains the stem tissue model of path780. This file is referenced as "p-ath780Stem.txt" by other supplemental files, particularly code, and this correct name should replace the default name for attached code to run properly.

992

Supplemental_File_5.xlsx: This file is a Microsoft Excel file which store a wide variety of information concerning the p-ath780 model. This include the manually-curated GPR results for each tissue model, the calculations pertaining to the determination of the biomass equation for each tissue model, calculations for various parameters used in the p-ath780 model to incorporate literature data, and calculations pertaining to the diurnal storage and uptake of carbohydrates.

998

999 Supplemental_File_6.txt: This file is the GAMS code for the p-ath780 model itself. It is 1000 generally named "p-ath780.gms".

1001

- 1002 Supplemental_File_7.txt: This is an executable Python code which takes the input of a model
- 1003 (such as Supplemental Files 1 through 4) and outputs a number of files which can be read by
- 1004 GAMs code. Generally, this code is named "convert.py". This code requires slight modifications
- 1005 depending on which model file is to be converted (see in-code comments).

1006

Supplemental_File_8.txt: This is an executable Perl code which takes the results of converting
each tissue model file using Supplemental File 11 and creates some of the necessary inputs for
the p-ath780 GAMS code. This is generally referenced as "makeGrowthInputs.pl".

1010

1011 **Supplemental_File_9.txt:** This is a text file which contains a list of the names of parameters 1012 used to defined p-ath780 model growth. This is referred to by other files as 1013 "growthSpecsNames.txt".

1014

Supplemental_File_10.txt: This is a text file which contains the actual specifications used for growing by the p-ath780 model. This is referred to by other files as "growthSpecs.txt", importantly it is referred to as this by Supplemental File 6.

1018

Supplemental_File_11.txt: This is a text file containing the list of time points to iterate over for
each day, e.g. this contains each hour of the day, beginning at 0 and ending at 23. This file is

referenced by others as "timepointsH.txt", importantly it is referred to as this by SupplementalFile 6.

1023

1024 Supplemental_File_12.txt: This is a text file containing a list of days to solve the model over, in

this case from day 0 to day 61. This file is referred to by others as "timepoints.txt", importantly it

1026 is referred to as this by Supplemental File 6.

1027

Supplemental_File_13.txt: This is a text file containing a list of data labels for much of the data saved at each time point (combination of day and hour) and reported on in the troubleshooting file. This file is referred to by others as "timeData.txt", importantly it is referred to as this by Supplemental File 6.

1032

Supplemental_File_14.txt: This is a text file which lists the time at which the sun rises (or light is made available) each day. At present, light is made available at a default time of 0. This file is referred to by others as "sunrise.txt", importantly it is referred to as this by Supplemental File 6.

1036

Supplemental_File_15.txt: This is a text file which lists the time at which the sun sets (or light
is no longer made available) each day. At present, light is made available at a default time of 0.
This file is referred to by others as "sunset.txt", importantly it is referred to as this by
Supplemental File 6.

1041

Supplemental_File_16.txt: This file basically converts the set time of day to a parameter of equal value. Necessary because mathematical operations cannot be performed on sets. This file is

referred to by other files as "timeofday.txt", importantly it is referred to as this by SupplementalFile 6.

1046

1047 Supplemental_File_17.xlsx: This is a Microsoft Excel file which contains the results of the p-

1048 ath780 model for various alternative objective functions. The sheet tabs indicate which

alternative objective function the data corresponds to. The key is as follows:

1050 lpe_g_g_X: linear photonic efficiency objective for the leaf, growth objective for other tissues.

1051 The number which replaces "X" indicates the run number.

- 1052 <u>g_g_g</u>: Growth objective for all tissues.
- 1053 nlpe_X: Non-linear photonic efficiency objective, the number which replaces the "X" denotes1054 the run number.
- 1055 $g_g_fa_g_X$: Fatty acid storage objective for the seed tissue, growth objective for all other, the 1056 number which replaces the "X" denotes the run number.

1057

Supplemental_File_18.txt: This is an executable Perl code file which is used to automatically curate the Gene-Protein-Reaction (GPR) links for all tissue models using the KEGG API (advanced programming interface, rest.kegg.jp). Inside the documentation of the code is the instructions for adapting it to investigate the GPR links for each tissue. Generally, this file is named "RxnstoGenes.pl". This file requires the LWP Perl package.

1063

Supplemental_File_19.tex: This file is a comma separated values file. This file contains a list of
73 KEGG pathways for which to get the list of associated reactions. This file is referred to by

code as ".csv", and must have the proper name for the code to function properly. Generally
referred to as "PathRxns.csv".

1068

Supplemental_File_20.txt: This file is an executable Perl code file (extension of ".pl") which automatically generates the lists of reactions associated with various KEGG pathways. The KEGG pathways used are listed in Supplemental File 19. This file is generally named "PathGetRxnsComps.pl".

1073

Supplemental_File_21.txt: This file is an executable Perl code file which is used to automatically read the files created from Supplemental Files 7 to give counts of how many reactions a model has which belong to each of the pathways indicated by Supplemental File 7. Generally, this file is named "ModelPathComp.pl".

1078

1079 **Supplemental_File_22.docx:** This file is a Microsoft Word file which contains all the 1080 calculations simplifications, and rational used for the determination of the function for whole-1081 plant mass step with respect to time.

1082

Supplemental_File_23.docx: A Microsoft Word file designed to help navigate other files provided as well as to outline the general file structure and barebones workflow used with the path780 model to make model implementation easier.

1086

1087 **Table Legends**

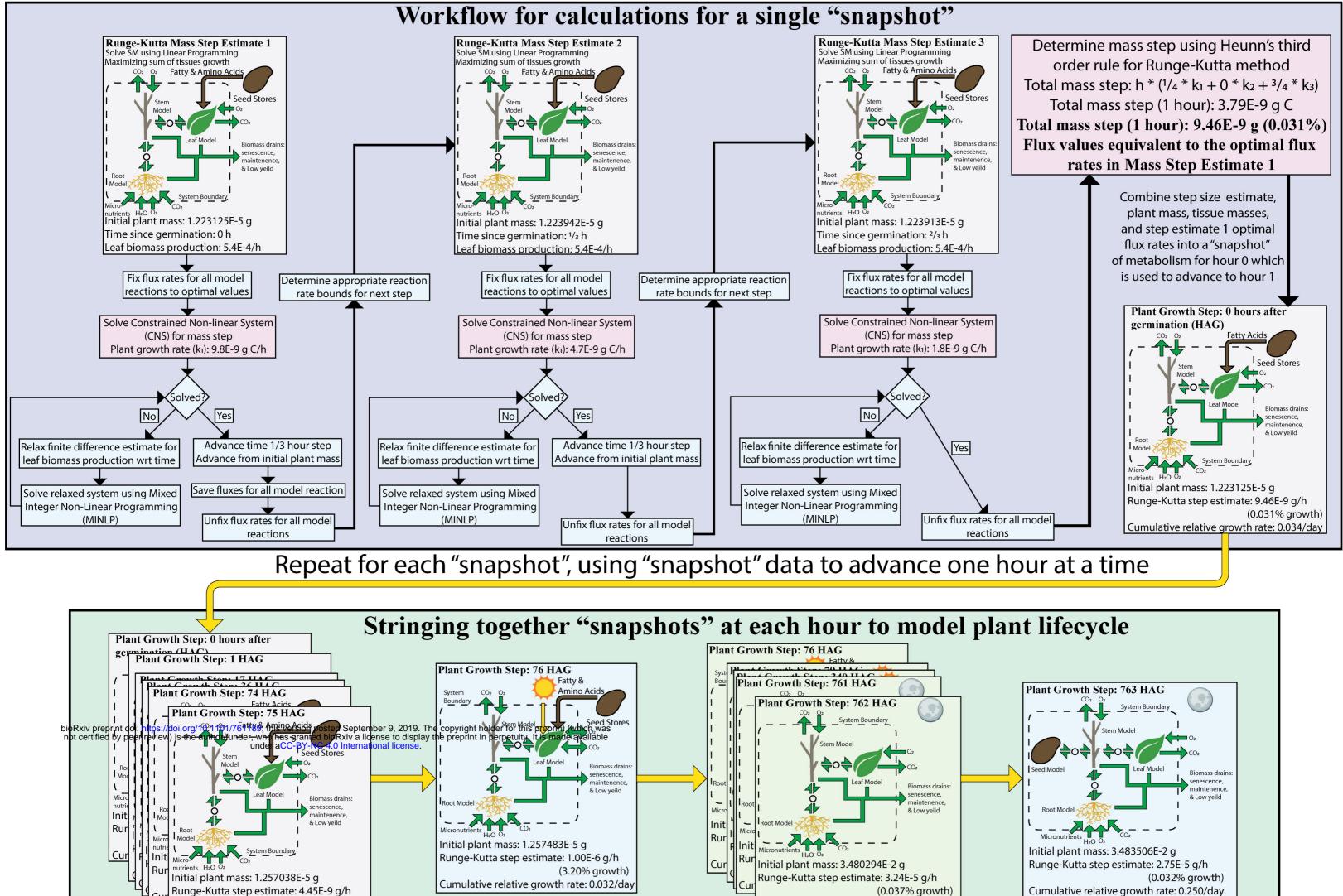
1088 **Table 1:** This table compares the critical mass-based metrics which have been used for *in silico* to in vivo data comparison across different objective functions for the p-ath780 model. The final 1089 1090 two columns are for metrics which have been targets of change when applying different 1091 objective functions. The green row is the *in vivo* data ranges which have served as targets for *in* silico model behavior. The blue row is the behavior of the p-ath780 model with the usual 1092 1093 objective function used in all other analyses (maximizing biomass production of all tissues). The 1094 grey rows are alternate objective functions we have explored. The photonic efficiency objective functions for the leaf tissue have caused lower fractions of available light used, while the fatty 1095 1096 acid production objective for the seed tissue has caused greater diversion of carbon resources toward fatty acid production and storage. All alternative objective functions have resulted in 1097 1098 lower production silico. mass in

| Total Plant Mass (mg) Tissue-Level Objectives | | | | | Relative GrowthRate (RGR)Peak Tissue Mass (mg) | | | | Resource utilization or production (median %) | | |
|--|---|-----------------------|-----------|-----------|--|---|----------------|--------------|--|-------------------------------------|--|
| Leaf | Seed | Root & Stem | 17 DAG | 24 DAG | 31 DAG | Whole-plant RGR (day ⁻¹) | Leaf | Stem | Seed | Of usable light used in light | Of carbon uptaken by seed to fatty acid storage |
| In vivo data | <i>In vivo</i> data | In vivo data | 0.5-2 | 2-8 | 10-30 | 0.21 – 0.25 | 163.7 ±52.0 | 188 ±39.3 | 127.9 ±52.7 | ? | ? |
| Biomass production | Biomass production | Biomass production | 0.554 | 3.74 | 25.2 | 0.246 | 177 | 189 | 130. | 100% | 0% |
| Biomass production | Fatty acid Storage $(\beta = 1E - 6)$ | Biomass production | 0.554 | 3.74 | 25.2 | 0.246 | 177 | 189 | 130. | 100% | 61.6% |
| Biomass production | Fatty acid Storage $(\beta = 2E - 2)$ | Biomass production | 0.554 | 3.74 | 25.2 | 0.246 | 94.1 | 100. | 68.9 | 100% | 61.7% |
| Linear | Biomass | Biomass | 0.554 | 3.74 | 25.2 | 0.246 | 177 | 189 | 130. | 100% | 0% |

| photonic | production | production | | | | | | | | | |
|-----------------|--------------------|------------|-------|------|------|-------|-----|------|------|-------|-------------|
| efficiency | | | | | | | | | | | |
| $(\alpha = 25)$ | | | | | | | | | | | |
| Linear | | | | | | | | | | | |
| photonic | Biomass | Biomass | 0.554 | 3.74 | 25.2 | 0.246 | 177 | 189 | 130. | 100% | 0% |
| efficiency | production | production | 0.001 | 5.71 | 23.2 | 0.210 | 177 | 107 | 100. | 10070 | 070 |
| $(\alpha = 50)$ | | | | | | | | | | | 0% 61.7% |
| Linear | E-44 | | | | | | | | | | |
| photonic | Fatty acid | Biomass | 0.554 | 0.74 | 25.2 | 0.046 | 100 | 1.40 | 077 | 1000/ | |
| officiency | Storage | production | 0.554 | 3.74 | 25.2 | 0.246 | 133 | 142 | 97.7 | 100% | 61.7% |
| efficiency | $(\beta = 1E - 2)$ | 1 | | | | | | | | | nterna |
| $(\alpha = 50)$ | | | | | | | | | | | ationa |

1099

- -



Cumulative relative growth rate: 0.250/day Seed Germination to Leaf Leaf Development Stage Time points 0 to 75 hours after germination (HAG) Time points 77 to 762 HAG **Development Transition** Constant tissue mass ratio **Time point 76 HAG** (0.51:0.27:0:0.21 leaf:root:seed:stem) Constant tissue mass ratio (0.51:0.27:0:0.21 leaf:root:seed:stem) Cotyledon removed at 76.5 hours after germination



(0.51:0.27:0:0.21 leaf:root:seed:stem) Cotyledon obscure leaves preventing photosynthesis • Plant uptakes fatty acids from seed stores

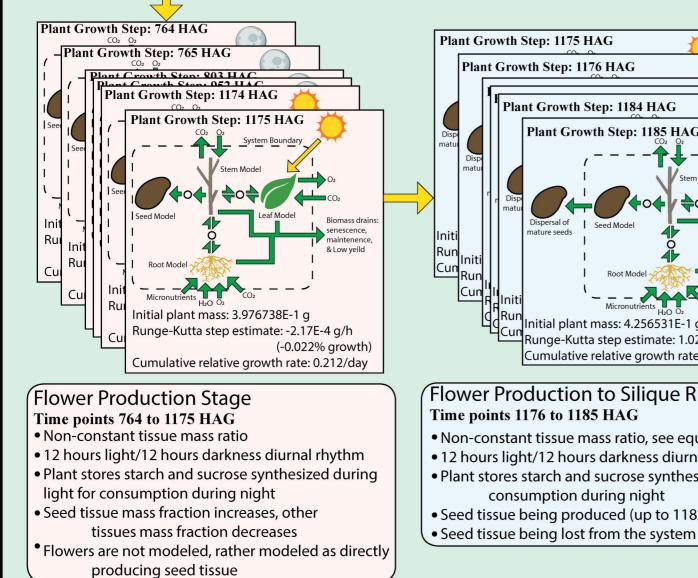
Seed Germination Stage

Constant tissue mass ratio

Start with embryonic mass (1.22E-5)

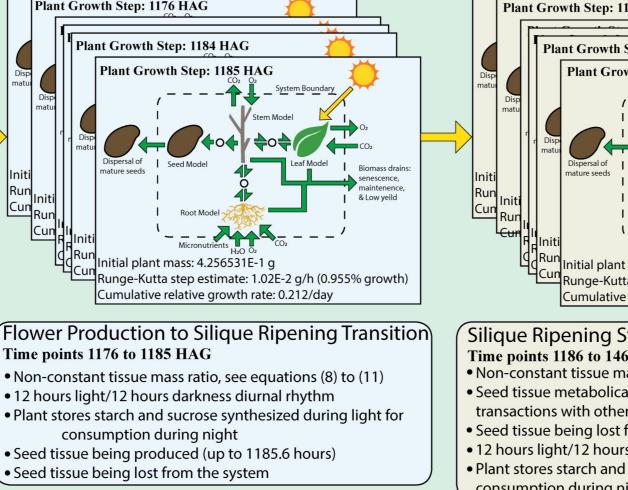
- 12 hours light/12 hours darkness diurnal rhythm Plant stores starch and sucrose synthesized during light for consumption during night
- Seed stores exhausted at 88.5 HAG

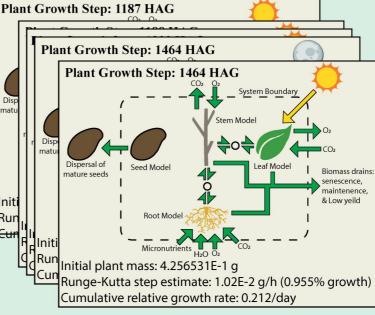
 Seed tissue mass fraction increases, other tissues mass fraction decreases • Seed mass first develops at 763.2 hours after germination



(0.014% growth)

Cumulative relative growth rate: 0.009/day





Silique Ripening Stage

Plant Growth Step: 1186 HAG

- Time points 1186 to 1464 HAG
- Non-constant tissue mass ratio
- Seed tissue metabolically inactive and has no metabolic
- transactions with other tissues
- Seed tissue being lost from the system
- 12 hours light/12 hours darkness diurnal rhythm
- Plant stores starch and sucrose synthesized during light for
- consumption during night

