Most cancers carry a substantial deleterious load due to Hill-Robertson interference

Susanne Tilk[1], Christina Curtis[2,3,4], Dmitri A Petrov[1], Christopher D McFarland[1]

[1]Department of Biology, Stanford University, Stanford CA 94305
[2]Department of Medicine, Division of Oncology, Stanford University School of Medicine, Stanford, CA, USA
[3]Department of Genetics, Stanford University School of Medicine, Stanford, CA, USA.
[4]Stanford Cancer Institute, Stanford University School of Medicine, Stanford, CA, USA.

Abstract

Introduction

Cancer genomes exhibit surprisingly weak signatures of negative selection[1,2]. This may be because tumors evolve either under very weak selective pressures ('weak selection') or under conditions that prevent the elimination of many deleterious passenger mutations ('poor efficacy of selection').

Rationale

The weak selection model argues that the majority of genes are only important for multicellular function. The poor efficacy of selection model argues, in contrast, that genome-wide linkage in cancer prevents many deleterious mutations from being removed via Hill-Robertson interference[3]. Since these linkage effects weaken as mutation rates decrease, we predict that cancers with lower mutational burdens should exhibit stronger signals of negative selection. Furthermore, because linkage affects driver mutations as well, low mutational burden cancers should also show stronger evidence of positive selection in driver genes. Neither pattern — in drivers or passengers — is expected under the weak selection model. We leverage the 10,000-fold variation in mutational burden across cancer subtypes to stratify tumors by their genome-wide mutational burden and used a normalized ratio of nonsynonymous to synonymous substitutions (dN/dS) to quantify the extent that selection varies with mutation rate.

Results

We find that appreciable negative selection (dN/dS ~ 0.4) is present in tumors with a low mutational burden, while the remaining cancers (96%) exhibit dN/dS ratios approaching 1, suggesting that the majority of tumors do not remove deleterious passengers. A parallel pattern is seen in drivers, where positive selection attenuates as the mutational burden of cancers increases. Both trends persist across tumor-types, are not exclusive to essential or housekeeping genes, and are present in clonal and subclonal mutations. Two additional orthogonal lines of evidence support the weak efficacy model: passengers are less damaging in low mutational burden cancers, and patterns of attenuated selection also emerge in Copy Number Alterations. Finally, we find that an evolutionary model incorporating Hill-Robertson interference can reproduce both patterns of attenuated selection in drivers and passengers if the average fitness cost of passengers is 1.0% and the average fitness benefit of drivers is 19%.

Conclusion

Collectively, our findings suggest that the lack of signals of negative selection in most tumors is not due to relaxed selective pressures, but rather the inability of selection to remove individual deleterious mutations in the presence of genome-wide linkage. As a result, despite the weak individual fitness effects of passengers, most cancers harbor a large mutational load (median ~40% total fitness cost) and succeed due to acquisition of additional strong drivers (~5 with an overall benefit of ~130%). Understanding how this deleterious load is overcome may help identify cancer vulnerabilities that may be targeted by new and existing therapies.

Introduction

Tumor progression is an evolutionary process acting on somatic cells within the body. These cells acquire mutations over time that can alter cellular fitness by either increasing or decreasing the rates of cell division and/or cell death. Mutations which increase cellular fitness (drivers) are observed in cancer genomes more frequently because natural selection enriches their prevalence within the tumor population. Conversely, mutations that decrease cellular fitness (deleterious passengers) are expected to be observed less frequently. This enrichment or depletion is often measured by comparing the expected number of nonsynonymous mutations (dN) within a region of the genome to the expected number of synonymous mutations (dS), which are presumed to be neutral. This ratio, dN/dS, is expected to be below 1 when the majority of nonsynonymous mutations are deleterious and removed by natural selection, be approximately 1 when all nonsynonymous mutations are neutral, and can be greater than 1 when a substantial proportion of nonsynonymous mutations are advantageous.

Two recent analyses of dN/dS patterns in cancer genomes found that for most non-driver genes dN/dS is ~1 and that only 0.1-0.4% of genes exhibit detectable negative selection (dN/dS < 1)[1,2].This differs substantially from patterns in germ-line evolution (dN/dS ~ 0.4) where most genes show signatures of negative selection[1]. Two explanations for this difference have been posited. First, the vast majority of nonsynonymous mutations may not be deleterious in somatic cellular evolution despite their deleterious effects on the organism. While most genes may be critical for proper organismal development and multicellular functioning, they may not be essential for clonal tumor growth. In this hypothesis, negative selection (dN/dS < 1) should be observed only within essential genes and absent elsewhere (dN/dS ~ 1).

A second hypothesis is that fundamental differences in asexual somatic tumor evolution reduce signatures of selection relative to sexually-recombining germ-line evolution. Specifically, interference between mutations due to genome-wide linkage, known as-Hill-Robertson interference, reduces the efficacy of natural selection[3]. Indeed, without recombination to link and unlink combinations of mutations, natural selection must act on entire genomes — not individual mutations — and select for clones with combinations of mutations of better aggregate fitness. Thus, advantageous drivers may not fix in the population, if they arise on an unfit background, and conversely, deleterious passengers can fix, if they arise on particularly fit backgrounds.

The inability of asexuals to eliminate deleterious passengers is driven by two Hill-Robertson interference processes: *hitchhiking* and *Muller's ratchet* (Fig. 1A). Hitchhiking occurs when a strong driver arises within a clone already harboring several passengers. Because these passengers cannot be unlinked from the driver under selection, they are carried with the driver to a greater frequency in the population. Muller's ratchet is a process where deleterious mutations continually accrue within different clones in the population until natural selection is overwhelmed. Whenever the fittest clone in an asexual population is lost through genetic drift, the maximum fitness of the population declines to the next most fit clone (Fig. 1A). The rate of hitchhiking and Muller's ratchet both increase with the genome-wide mutation rate[4,5]. Therefore, the second hypothesis

predicts selection against deleterious passengers should be more efficient and more evident (dN/dS < 1) in tumors with lower mutational burdens.

Here, we leverage the 10,000-fold variation in tumor mutational burden across 50 cancer types to quantify the extent that selection attenuates, and thus becomes more inefficient, as the mutational burden increases. Using dN/dS, we find that selection against deleterious passengers and in favor of advantageous drivers is more efficient in low mutational burden cancers. Furthermore, low mutational burden cancers exhibit efficient selection across cancer subtypes, as well as within subclonal mutations, homozygous mutations, somatic copy-number alterations, and essential genes. Finally, we demonstrate that a simple evolutionary model incorporating Hill-Robertson interference can explain these observed patterns of selection. This model predicts that most cancers carry a substantial deleterious burden (~40%) that necessitates the acquisition of multiple strong drivers (~5) in successful tumors that together provide a benefit of ~130%. Collectively, these results explain why signatures of selection are largely absent in cancers with elevated mutational burdens and indicate that the vast majority of tumors harbor a large mutational load.

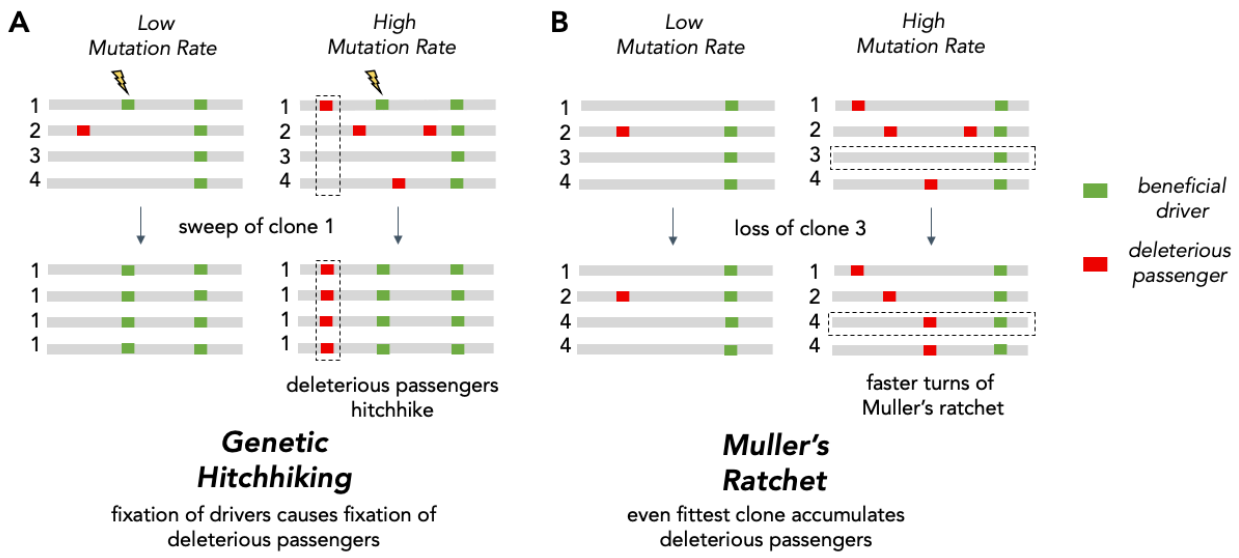


Figure 1. Two Hill-Robertson interference processes can lead to an accumulation of deleterious mutations at high mutation rates. (A) Genetic hitchhiking. Each number identifies a different segment of a clone genome within a tumor. *De novo* beneficial driver mutations that arise in a clone can drive other mutations (passengers) in the clone to high frequencies (black dotted column). If the passenger is deleterious, both beneficial drivers and deleterious passengers can accumulate. **(B) Muller's ratchet.** As the mutation rate within a tumor increases, deleterious passengers accumulate on more clones. If the fittest clone within the tumor is lost through genetic drift (black dotted row), the overall fitness of the population will decline.

Results

A nonparametric null model of mutagenesis in cancer. Mutational processes in cancers are heterogeneous, which can bias dN/dS estimates of selective pressures. To overcome this issue, it is essential to design a bias-corrected version of *dN/dS* in which observed counts are compared to what is expected under neutral evolution. It is also important to consider that mutational biases are often specific to cancer type and genomic region. Such corrections are generally accomplished using parametric mutation models, which can become very complex in cancer and may posit many free parameters (>5,000)[1,6].

To circumvent these issues, we use a permutation-based, nonparametric (parameter-free) estimation of *dN/dS*. In this approach, every observed mutation is permuted while preserving the gene, patient samples, specific base change (e.g. A>T) and tri-nucleotide context. The permutations are then tallied for both nonsynonymous $d_N^{(\text{permuted})}$ and synonymous $d_S^{(\text{permuted})}$ substitutions (Fig. S1) and used as proportional estimates of the observed number of nonsynonymous $d_N^{(\text{observed})}$ (or simply d_N) and synonymous $d_S^{(\text{observed})}$ (d_S) mutations in the absence of selection. The unbiased effects of selection on a gene, *dN/dS*, is then:

$$\frac{dN}{dS} = \frac{dN^{(\text{observed})}/dN^{(\text{permuted})}}{dS^{(\text{observed})}/dS^{(\text{permuted})}}$$

For all cancer types and patient samples, *P*-values and confidence intervals are determined by bootstrapping patient samples. Note that this permutation procedure will account for all gene and tumor-level mutational biases (e.g. neighboring bases[7], transcription-coupled repair, S phase timing[8], mutator phenotypes) and their covariation. We confirmed that this approach accurately measures selection even in the presence of simulated mutational biases (Methods, Fig. S2) and demonstrate that this approach identifies similar patterns of selection as parametric models (Fig. S3).

Attenuation of selection in drivers and passengers for elevated mutational burden tumors. We estimated *dN/dS* patterns in both driver and passenger gene sets across 11,855 tumors from TCGA (whole-exome) and ICGC (whole-genome) aggregated over 50 cancer types (Methods). We used the following four mutational tallies as a proxy for the genome-wide mutation rate: (1) the total number of mutations or tumor mutational burden (TMB) (2) the total number of observed substitutions in both synonymous and nonsynonymous sites ($d_N + d_S$) (Fig. 1), and (3) the total number of mutations in intergenic, and (4) intronic regions. All estimates are strongly correlated ($R^2 > 0.97$, Fig. S4).

In principle, only the last two tallies — the number of substitutions in intergenic or intronic regions — are orthogonal to dN/dS, and least likely to be biased by selection. However, these measures can only be used on whole-genome data, which represents 15% of samples in our datasets. Therefore, for most of the analyses, we used the second measure ($d_N + d_S$) to define mutational burden, while being cognizant that the analysis could be complicated by the fact that the same mutation tallies are used for both the x-axis ($d_N + d_S$) and y-axis (*dN/dS*). We note that this interdependence leads to

a slight underestimation of the degree of purifying selection, rendering our analysis conservative (Fig. S5, Methods).

Consistent with the 'poor efficacy of selection' model, whereby selection fails to eliminate deleterious mutations in high mutational burden tumors, we observe pervasive selection against passengers exclusively in cancers with low mutational burdens (dN/dS ~ 0.4 in tumors with mutational burden ≤ 3, while dN/dS ~ 0.9 in tumors with mutational burden > 10, Fig. 2A). We observed little negative selection in passengers when aggregating tumors across all mutational burdens (*dN/dS* = 0.88), which is broadly similar to previous estimates[1,2,6,9]. Also consistent with the 'poor efficacy of selection' model, drivers exhibit a similar but opposing trend of attenuated selection at elevated mutational burdens (dN/dS ~ 3.5 when mutational burden ≤ 3 and gradually declines to ~1.38 when mutational burden > 100). This pattern is not specific to oncogenes or tumor suppressors (Fig. S6). While the attenuation of selection against passengers in higher mutational burden tumors is a novel discovery, this pattern among drivers has been reported previously[1]. We confirmed that these patterns were robust to the choices that we made in our analysis pipeline, including: (1) the somatic mutation calling algorithm (Mutect2 and MC3 SNP calls[10], Fig. S7), (2) the dataset (TCGA[11], ICGC[12], and COSMIC[13], Fig. S3), (3) the choice of driver gene set (Bailey et al,[14], IntOGen[15], and COSMIC[13], Fig.S8), (4) mutational burden metric, and (5) the null model of mutagenesis (dNdScv)[1], (Fig. S3).

If negative selection is more pronounced in low mutational burden tumors, then the nonsynonymous mutations observed should also be less functionally consequential. By annotating the functional effect of all missense mutations using PolyPhen2[16] (Fig 2B), we indeed found that observed nonsynonymous passengers are less damaging in low mutational burden cancers. Similarly, driver mutations are less functionally consequential as mutational burden increases, as expected for mutations experiencing weaker positive selection (Fig 2B). Together these two trends provide additional and orthogonal evidence that selective forces on nonsynonymous mutations are more efficacious in low mutational burden cancers.

Finally, since all mutational types experience Hill-Robertson interference, attenuated selection should also persist in Copy Number Alterations (CNAs). Since CNAs cannot be partitioned into synonymous and nonsynonymous events, but can still disrupt protein function and dosage, we quantified selection in CNAs using two alternative measures: Breakpoint Frequency[17] and Fractional Overlap[18]. For both measures, we compare the number of CNAs that either terminate (Breakpoint Frequency) within or partially overlap (Fractional Overlap) **E**xonic regions of the genome relative to non-coding (**I**ntergenic and **I**ntronic) regions (dE/dI, See Methods). Like dN/dS, dE/dI is expected to be <1 in genomic regions experiencing negative selection, >1 in regions experiencing positive selection (e.g. driver genes), and approximately 1 when selection is absent or inefficient. Using dE/dI, we observed attenuation of selection in both driver and passenger CNAs as the total number of CNAs increases using both Fractional Overlap (Fig. 2C) and Breakpoint Frequency (Fig. S9). While CNAs of all lengths experience attenuated selection, CNAs longer than the average gene length (>100 KB) experience greater selective pressures in drivers ($p < 10^{-4}$).

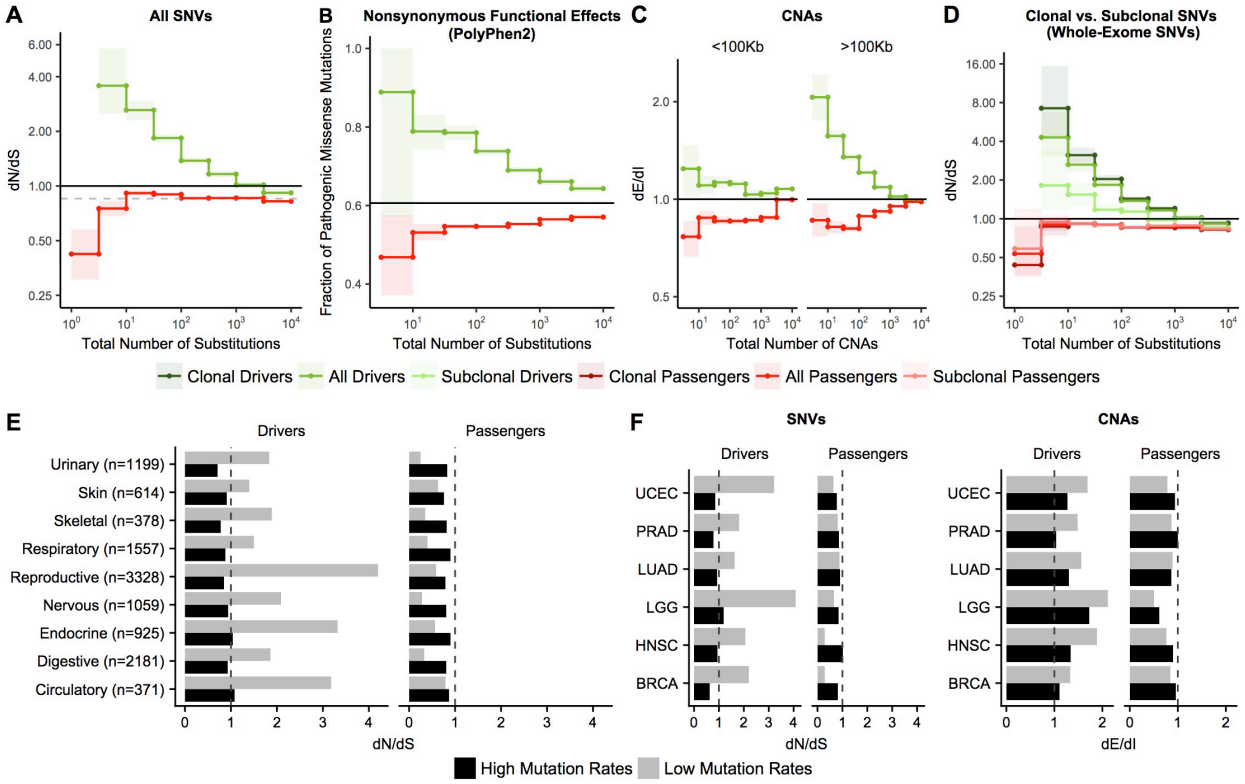


Figure 2. Signatures of positive and negative selection attenuate at high mutation rates. (A) dN/dS of passenger (red) and driver (green) gene sets within 11,855 tumors (ICGC and TCGA) stratified by total number of substitutions present in the tumor ($d_N^{(observed)} + d_S^{(observed)}$). dN/dS of 1 (solid black line) is expected under neutrality. Dashed gray line denotes pan-cancer genome-wide dN/dS. **(B)** Fraction of pathogenic missense mutations, annotated by PolyPhen2, in the same driver and passenger gene sets also stratified by total number of substitutions. Black line denotes the fraction of pathogenic missense mutations in the entire human proteome. **(C)** Fractional overlap of CNAs that reside within exonic (dE) to intergenic (dI) regions within putative driver and passenger gene sets (identified by GISTIC 2.0, Methods) in tumors stratified by the total number of CNAs present in each tumor and separated by CNA length. Solid black line of 1 denotes values expected under neutrality. **(D)** dN/dS of clonal (VAF > 0.2) and subclonal (VAF < 0.2) passenger and driver gene sets in tumors stratified by the total number of substitutions. Darker colors denote clonal passengers and drivers, while lighter colors denote subclonal passengers and drivers. dN/dS of 1 (solid black line) is expected under neutrality. **(E)** Driver and passenger dN/dS of the highest and lowest defined mutational burden bin in broad anatomical sub-categories. **(F)** Same as **(E)**, except for specific cancer subtypes with ≥500 samples. All shaded error bars are 95% confidence intervals determined by bootstrap sampling.

Strong selection in low mutational burden tumors cannot be explained by mutational timing, gene function, or tumor type. We next tested alternative hypotheses to the 'poor efficacy of selection' model for the observed pattern of attenuated selection in higher mutational burden tumors. We considered the possibility that selection is strong only during normal tissue development but absent after cells have transformed to malignancy. This would disproportionately affect low mutational burden tumors, as a greater proportion of mutations in them will be generated prior to tumor transformation. If true, then attenuated selection should be absent in sub-clonal mutations, which must arise during tumor growth. However, we do detect clear attenuation of selection for the subset of likely subclonal mutations with Variant Allele Frequency (VAF) below 20% (Fig. 2D & S10). Attenuated selection in drivers and passengers is detected in both sub-clonal and clonal mutations, but is weaker in both drivers and passengers with lower VAFs. Weaker efficiency of selection among less frequent polymorphisms is expected under a range of population genetic models[19] and especially so in rapidly-expanding, spatially-constrained cancers[20]. Here, it can also be partially due to the fact that heterozygous mutations are only partially-dominant[21] and will necessarily exhibit lower VAFs.

Next, we considered and rejected the possibility that attenuated selection is limited to particular types of genes. We first annotated our observed mutations by different functional categories and Gene Ontology (GO) terms[22] and found that negative selection is not specific to any particular gene functional category, and specifically not limited to essential or housekeeping genes — a key prediction of the 'weak selection' model[1] (Fig. S11, $p < 0.05$, Wilcoxon signed-rank test).

Finally, we found that these patterns of attenuated selection persist across cancer subtypes for both SNVs and CNAs. We calculated dN/dS in tumors grouped by nine broad anatomical sub-categories (e.g. neuronal) and 50 subtype classifications [23](Fig 2E-F). We find that patterns of attenuated selection in SNVs persists in the broad and specific (drivers $p = 1.3 \times 10^{-5}$, passengers $p = 1.2 \times 10^{-2}$; Fig. S12) classification schemes. Furthermore, dE/dI measurements of CNAs exhibit these same patterns of selection in broad (Fig S13) and specific subtypes (Fig. 2F; drivers $p < 10^{-6}$ and passengers $p = 7.3 \times 10^{-4}$). Collectively, these results strongly support the 'poor efficacy of selection' model and argue that the observed patterns must be due to forces that are universal for tumor evolution.

Estimate of the fitness effects of drivers and passengers, and Hill-Robertson interference processes using an evolutionary model. Our findings indicate that selection consistently attenuates in both drivers and passengers across all cancers as mutational burden increases. To determine whether Hill-Robertson interference alone can explain these findings, we modeled tumor progression as a simple evolutionary process with advantageous drivers and deleterious passengers. We then used Approximate Bayesian Computation (ABC) to compare these simulations to observed data and infer the mean fitness effects of drivers and passengers.

Our evolutionary simulations model a well-mixed population of tumor cells that can stochastically acquire advantageous drivers and deleterious passengers during cell division[24]. The multiplicative sum of the individual fitness effects of these mutations

determines the relative birth and death rate of each cell, which in turn dictates the population size N of the tumor. If the population size of a tumor progresses to malignancy (N > 1,000,000) within a human lifetime (≤100 years), the accrued mutations, as well as the patient age are recorded. Each simulated tumor is assigned a randomly-sampled mutation rate from a broad range (10^{-12} to 10^{-7} mutations • nucleotide^{-1} • generation^{-1}, Methods).

Figure 3A illustrates the ABC procedure. To compare our model to observed data, we simulated an exponential distribution of fitness effects with mean fitness values that spanned a broad range (10^{-2} - 10^{0} for driver and 10^{-4} - 10^{-2} for passengers, Methods). We summarized observed and simulated data using statistics that capture three relationships: (i) the dependence of driver and passenger dN/dS rates with mutational burden, (ii) the rate of cancer age-incidence (SEERs database[25]), and (iii) the distribution of mutational burdens (summary statistics of (ii) and (iii) were based on theoretical parametric models[26], Methods, Fig. S14 & S15). We then inferred the posterior probability distribution of mean driver fitness benefit and mean passenger fitness cost using a rejection algorithm that we validated using leave-one-out Cross Validation (Methods, Fig. S16). Using this approach, the Maximum Likelihood Estimate (MLE) of mean driver fitness benefit is 18.8% (Fig. 3B), while the MLE of passenger mean fitness cost is 0.96% (Fig. 3C). Simulations with these MLE values agree well with all observed data (Fig. 3D-F, Pearson's R = 0.95, 0.80, 0.99, 0.97 for driver dN/dS, passenger dN/dS, Age-Incidence, and Mutational Burden respectively).

While Hill-Robertson interference alone explains dN/dS rates in the passengers well, the simulations most consistent with observed data exhibited consistently higher elevated dN/dS rates in drivers (Fig. 3D). We tested whether positive selection on synonymous mutations within driver genes could explain this discrepancy. Indeed, we find that a model incorporating synonymous drivers agrees modestly better with observed statistics (p = 0.043, ABC posterior probability). The best-fitting model predicts that ~10% of synonymous mutations within driver genes experience positive selection, which is consistent with previous estimates for human oncogenes[27] (Methods, Fig. 3D, S17). Furthermore, we observe additional evidence of selection and codon bias in synonymous drivers exclusive to low mutational burdens (TCGA samples, Methods, Fig. S17). Lastly, we considered and rejected the possibility that the attenuation of selection in drivers could be due to a diminishing benefit of additional drivers (akin to a 5-hit multistage model[26], Methods, p > 0.5, ABC posterior probability).

Our results indicate that rapid adaptation through natural selection – acting on entire genomes, rather than individual mutations – is pervasive in all tumors, including those with elevated mutational burdens. Given the quantity of drivers and passengers observed in a typical cancer (TCGA), we estimate that cancer cells are in total ~90% fitter than normal tissues (130% benefit of drivers, 40% cost of passengers). This is roughly consistent with the difference in division times between normal (primary) cells and cancer cell lines[28]. A median of five drivers accumulate per tumor in these simulations – also consistent with estimates from age-incidence curves and known hallmarks of cancer[29]. Lastly, the mutation rates of tumors that progress to cancer in our

model also recapitulate observed mutation rates in human cancer[30] (median 3.7 x 10^{-9}, 95% Interval 1.1 x 10^{-10} - 8.2 x 10^{-8}, Fig. S18).

Most notably, aggregate passenger load confers a fitness cost of ~40%. While this collective burden is large, the individual fitness effects of accumulated passengers in these simulations (mean 0.8%) are similar to observed fitness changes in cancer cell lines (1 - 3%)[31]. These passengers accumulated primarily via Muller's Ratchet, while only ~14% accumulated via hitchhiking (inferred using population genetics theory[24] and MLE fitness effects, Methods, Fig. S19).

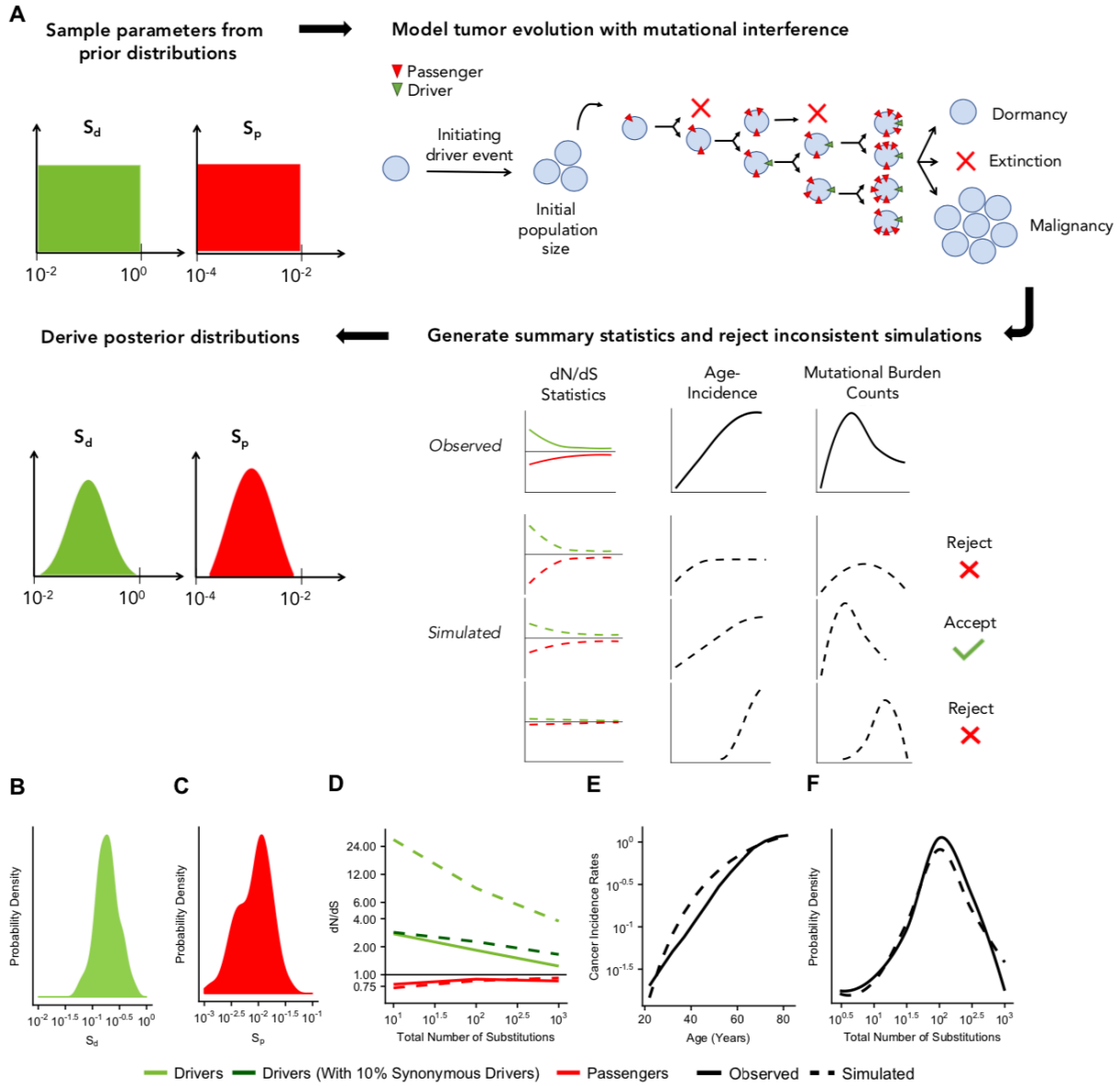


Figure 3. ABC procedure estimates the strength of selection in passengers and drivers. (A) Schematic overview of the ABC procedure used. A model of tumor evolution with Hill-Robertson interference contains two parameters — s_d (mean fitness benefit of drivers) and s_p (mean fitness cost of passengers) — sampled over broad prior distributions of values. Simulations begin with an initiating driver event that establishes

the initial population size of the tumor. The birth rate of each individual cell within the tumor is determined by the total accumulated fitness effects of drivers and passengers. If the final population size of the tumor exceeds one million cells within a human lifetime (100 years), patient age and accrued mutations are recorded. Summary statistics of four relationships are used to compare simulations to observed data: (i) dN/dS rates of drivers and (ii) passengers across mutational burden, (iii) rates of cancer incidence versus age, and (iv) the distribution of mutational burdens. A rejection algorithm is used to either reject or accept simulations. **(B-C)** Inferred posterior probability distributions of s_d and s_p. The Maximum Likelihood Estimate (MLE) of s_d is 18.8% (green, 95% CI [13.3, 32.7]), and the MLE of s_p is 0.96% (green, 95% CI [0.28, 3.6%]). **(D-F)** Comparison of best-fitting simulations (MLE parameters, dashed lines) to observed data (solid lines). **(D)** dN/dS rates of passengers (red) and drivers (light green) for simulated and observed data versus mutational burden. A model where 10% of synonymous mutations within drivers experience positive selection (dark green) was also considered. **(E)** Cancer incidence rates for patients above 20 years of age. **(F)** Comparison of the distribution of the mutational burdens of tumors.

Discussion

Here we argue that signals of selection are largely absent in cancer because of the poor efficacy of selection and not because of weakened selective pressures. In low mutational burden tumors (≤ 3 total substitutions per tumor), increased selection for drivers and against passengers is observed and ubiquitous: in SNVs and CNAs; in heterozygous, homozygous, clonal, and subclonal mutations; and in mutations predicted to be functionally consequential. These trends are not specific to essential or housekeeping genes. Importantly, these patterns persist across broad and specific tumor subtypes. Collectively, these results suggest that inefficient selection is generic to tumor evolution.

Importantly, these patterns of selection are missed when dN/dS rates are not stratified by mutational burden. Since a small minority of tumors (4% in TCGA and ICGC) have a low mutational burden, accounting for 0.1% of mutations in these databases, the dN/dS of passengers at low mutational burdens (~0.4) do not appreciably alter the pan-cancer dN/dS of passengers (0.88 in our study, 0.82 — 0.98 in [1,2,6,9]). Thus, these patterns can only be detected now given the vast amounts of available cancer sequencing data. Furthermore, we believe that low mutational burden tumors should be particularly valuable for identifying genes and pathways under positive and negative selection.

We show that a simple evolutionary model that incorporates Hill-Robertson Interference can explain this ubiquitous trend of attenuated selection in both drivers and passengers. dN/dS rates attenuate in drivers because the background fitness of a clone becomes more important than the fitness effects of an additional driver at elevated mutation rates. Furthermore, these simulations indicate that, despite dN/dS patterns approaching 1 in tumors with elevated mutational burdens, passengers are not effectively neutral ($Ns > 1$). Instead, passengers confer an individually-weak, but

collectively-substantial fitness cost of ~40% that impacts tumor progression. While this simple model does not explicitly incorporate many known aspects of tumor biology (Table S2), we note that previous studies demonstrate that spatial constraints further reduce the efficacy of selection in cancer[20].

The functional explanation for why passengers in cancer are deleterious is unknown. In germ-line evolution, mutations are primarily deleterious because of protein misfolding[32]. Deleterious passengers in somatic cells should confer similar effects[33], but may carry additional costs (e.g. immunoediting[34]). Furthermore, we do not yet understand how tumors overcome the functional effects of deleterious passengers. Potential mechanisms may include (1) silencing of non-essential proteins that carry deleterious passengers[35], (2) upregulation of heat shock and proteolytic pathways[36], (3) abdication of cellular functions (e.g. oxidative phosphorylation), (4) polyploidization[21], and (4) immune escape[34]. Understanding and identifying how tumors manage this deleterious burden ought to identify new cancer vulnerabilities that may allow researchers to develop new therapies and better target existing ones.

Acknowledgements

We thank Grant Kinsler, Gabor Boross, Chuan Li, Alison Feder and other members of the Petrov and Curtis labs for helpful comments and discussions. This work was supported by XXX. S.T. is supported by NIH/NHGRI training grant T32HG000044-21. C.D.M. is supported by NIH grant K99CA226506-02.

References

1. Martincorena, I. *et al.* Universal Patterns of Selection in Cancer and Somatic Tissues. *Cell* **171**, 1029-1041.e21 (2017).
2. Weghorn, D. & Sunyaev, S. Bayesian inference of negative and positive selection in human cancers. *Nat. Genet.* **49**, 1785–1788 (2017).
3. HILL, W. G. & ROBERTSON, A. The effect of linkage on limits to artificial selection. *Genet. Res. (Camb).* **89**, 311–336 (2007).
4. Johnson, T. Beneficial mutations, hitchhiking and the evolution of mutation rates in sexual populations. *Genetics* (1999).
5. Neher, R. a & Shraiman, B. I. Fluctuations of fitness distributions and the rate of Muller's ratchet. *Genetics* **191**, 1283–1293 (2012).
6. Zapata, L. *et al.* Negative selection in tumor genome evolution acts on essential cellular functions and the immunopeptidome. *Genome Biol.* **19**, 67 (2018).
7. Alexandrov, L. B. & Stratton, M. R. Mutational signatures: the patterns of somatic mutations hidden in cancer genomes. *Curr. Opin. Genet. Dev.* **24**, 52–60 (2014).
8. Haradhvala, N. J. *et al.* Mutational Strand Asymmetries in Cancer Genomes Reveal Mechanisms of DNA Damage and Repair. *Cell* **164**, 538–49 (2016).
9. Ostrow, S. L., Barshir, R., DeGregori, J., Yeger-Lotem, E. & Hershberg, R. Cancer Evolution Is Associated with Pervasive Positive Selection on Globally Expressed Genes. *PLoS Genet.* **10**, 16–20 (2014).
10. Ellrott, K. *et al.* Scalable Open Science Approach for Mutation Calling of Tumor Exomes Using Multiple Genomic Pipelines. *Cell Syst.* **6**, 271-281.e7 (2018).
11. Cancer Genome Atlas Research Network *et al.* The Cancer Genome Atlas Pan-Cancer analysis project. *Nat. Genet.* **45**, 1113–20 (2013).
12. Hudson, T. J. *et al.* International network of cancer genome projects. *Nature* **464**, 993–998 (2010).
13. Forbes, S. a *et al.* The Catalogue of Somatic Mutations in Cancer (COSMIC). *Curr Protoc Hum Genet* **Chapter 10**, Unit 10.11 (2008).
14. Bailey, M. H. *et al.* Comprehensive Characterization of Cancer Driver Genes and Mutations. *Cell* **173**, 371-385.e18 (2018).
15. Gonzalez-Perez, A. *et al.* IntOGen-mutations identifies cancer drivers across tumor types. *Nat. Methods* **10**, 1081–1082 (2013).
16. Adzhubei, I. a *et al.* A method and server for predicting damaging missense mutations. *Nat. Methods* **7**, 248–9 (2010).
17. Korbel, J. O. *et al.* Systematic prediction and validation of breakpoints associated with copy-number variants in the human genome. *Proc. Natl. Acad. Sci.* **104**, 10110–10115 (2007).
18. Zack, T. I. *et al.* Pan-cancer patterns of somatic copy number alteration. *Nat Genet* **45**, 1134–1140 (2013).
19. Messer, P. W. Measuring the Rates of Spontaneous Mutation From Deep and Large-Scale Polymorphism Data. *Genetics* **182**, 1219–1232 (2009).
20. Sottoriva, A. *et al.* A Big Bang model of human colorectal tumor growth. *Nat. Genet.* **47**, 209–216 (2015).
21. Lopez, S. *et al.* Whole Genome Doubling mitigates Muller's Ratchet in Cancer Evolution. *bioRxiv* 513457 (2019).
22. Gene Ontology Consortium. The Gene Ontology (GO) database and informatics resource. *Nucleic Acids Res.* **32**, 258D – 261 (2004).
23. Grossman, R. L. *et al.* Toward a Shared Vision for Cancer Genomic Data. *N. Engl. J. Med.* **375**, 1109–1112 (2016).
24. McFarland, C. D., Korolev, K. S., Kryukov, G. V, Sunyaev, S. R. & Mirny, L. a. Impact of deleterious passenger mutations on cancer progression. *Proc. Natl. Acad. Sci.* **110**, 2910–2915 (2013).
25. National Cancer Institute, S. S. B. Cancer Incidence – Surveillance, Epidemiology, and End Results (SEER) Registries Research Data. *Surveillance, Epidemiology, and End Results (SEER) Program (http://www.seer.cancer.gov).* (2007).
26. Frank, S. A. *Dynamics of cancer: Incidence, Inheritance, and Evolution*. (2007).
27. Supek, F., Miñana, B., Valcárcel, J., Gabaldón, T. & Lehner, B. Synonymous Mutations Frequently Act as

Driver Mutations in Human Cancers. *Cell* **156**, 1324–1335 (2014).
28. Cooperman, J., Neely, R., Teachey, D. T., Grupp, S. & Choi, J. K. Cell division rates of primary human precursor B cells in culture reflect in vivo rates. *Stem Cells* **22**, 1111–20 (2004).
29. Hanahan, D. & Weinberg, R. A. The Hallmarks of Cancer. *Cell* **100**, 57–70 (2000).
30. Camps, M., Herman, A., Loh, E. & Loeb, L. a. Genetic constraints on protein evolution. *Crit Rev Biochem Mol Biol* **42**, 313–326 (2007).
31. Williams, B. R. *et al.* Aneuploidy Affects Proliferation and Spontaneous Immortalization in Mammalian Cells. *Science (80-.).* **322**, 703–709 (2008).
32. Powers, E. T. & Balch, W. E. Costly Mistakes: Translational Infidelity and Protein Homeostasis. *Cell* **134**, 204–206 (2008).
33. Wang, M. & Kaufman, R. J. Protein misfolding in the endoplasmic reticulum as a conduit to human disease. *Nature* **529**, 326 (2016).
34. Glaire, M. A. & Church, D. N. Hypermutated Colorectal Cancer and Neoantigen Load. *Immunother. Gastrointest. Cancer* 187–215 (2017).
35. Gorgoulis, V. G., Pefani, D. E., Pateras, I. S. & Trougakos, I. P. Integrating the DNA damage and protein stress responses during cancer development and treatment. *J. Pathol.* **246**, 12–40 (2018).
36. Dai, C., Whitesell, L., Rogers, A. B. & Lindquist, S. Heat shock factor 1 is a powerful multifaceted modifier of carcinogenesis. *Cell* **130**, 1005–1018 (2007).

Methods & Supplementary Materials

Mutation calling and quality controls. Mutations were downloaded from online repositories that have already invested heavily in quality control. Multiple data repositories were used to ensure reproducibility. Post-processing was minimal to avoid engendering a particular result, and only excluded sequencing samples obtained from cell lines, or studies that did not report synonymous variants, or (on occasion) mutations within pseudogenes. These exclusions are described in greater detail below.

Somatic Nucleotide Variants (SNVs). Exomic, open-access SNV calls (WES) of 10,486 cancer patients in (The Cancer Genome Atlas) TCGA were downloaded from the Multi-Center Mutation Calling in Multiple Cancers (MC3) project[1]. This repository uses a consensus of seven mutation-calling algorithms. Whole-Genome Sequencing SNV calls (WGS) of 1,830 patients were downloaded from the ICGC data portal in November 2018[2]. Only consensus mutation calls from the PCAWG Consensus SNV-MNV caller were considered. Both missense and nonsense mutations are defined as nonsynonymous mutations. Frameshift, indels, and splice-site variants were not included in analyses. Samples without any synonymous or nonsynonymous mutations and unexpressed genes in either dataset were excluded. Note that there is no evidence of germline contamination by common SNPs (MAF >5%) from 1,000 Genomes Project[3] (v 2015 Aug) using ANNOVAR[4] to annotate mutations in either datasets (Supplementary Figure 7). A final of 1,703 whole-genome and 10,152 whole-exome sequencing samples were used for the analyses in this paper.

For supplemental analyses on the effect of variant callers, SNVs from exome and whole genome wide screens were downloaded on October 2016 from the Catalog of Somatic Mutations in Cancer's (COSMIC) Mutant Export Census[5]. Studies before 2010 that didn't report silent mutations, and cell lines were removed from the analysis. Whole-exome SNVs in TCGA were also called using Mutect2[6] (Supplementary Figure 3).

Defining tumor burden. We tested four different mutation burden metrics as a proxy for the genome-wide mutation rate: (1) the total number of observed mutations, (2) total number of substitutions in both synonymous and nonsynonymous sites ($d_N^{(observed)} + d_S^{(observed)}$), (3) the total number of mutations in intergenic, and (4) intronic regions. Although only the last two definitions of mutational burden are completely independent to dN/dS, the vast majority of samples (10,152 vs 1,703) are derived from whole-exome data. We note that all mutation rates are strongly correlated to each other ($R^2 > 0.97$). Because only $d_N + d_S$ could be applied to WES data — the majority of samples — and all metrics worked equally-well, we primarily used $d_N + d_S$ to measure mutational burden. Lastly, because dN/dS is undefined for tumors with no synonymous mutations, we necessarily excluded these samples. We also excluded samples with no nonsynonymous mutations so as to apply a symmetric filter on the data and because data quality may be compromised in these samples.

A Nonparametric Null Model of Mutagenesis to calculate dN/dS. We assume that for any particular tumor, mutation rates are constant across a gene for a particular tri-nucleotide context and base change (e.g. C > G). Our procedure is inspired by Constrained Marginal Models (or 'edge switching' in network analysis), whereby the marginal distributions of observations aggregated over known confounding variables are preserved under permutation to create a null distribution. In our application of this strategy, the marginal distributions of mutations (across tri-nucleotide context, base change, gene, and tumor) remain preserved – as they would be in a Constrained Marginal Model; however, we exhaustively consider every acceptable permutation of the data. Because our approach is highly-constrained, these permutations are exhaustively computable (median 61 alternatives per mutation). Thus, resampling is unnecessary.

Our null model presumes that all mutations of type i, defined by a tri-nucleotide context and base change, arise with probability M_{igt} within each gene g and tumor t. For each gene, we tally the total quantity of nonsynonymous mutations N_{ig} and synonymous mutations S_{ig}. Suppose selection enriches or depletes nonsynonymous mutations within a gene and tumor by a rate ω_{gt}. The expected number of nonsynonymous and synonymous mutations within a particular tumor and gene are simply $\mathrm{E}[d_N] = \omega_{gt} \sum_i M_{igt} N_{ig}$ and $\mathrm{E}[d_S] = \sum_i M_{igt} S_{ig}$ in the absence of selective pressures on synonymous mutations. As with the main text, d_N and $d_N^{(observed)}$

are used interchangeably. Although M_{igt} is unknown, dN/dS statistics attempt to infer selection nonetheless by noting that:

$$\frac{E[d_N]}{E[d_S]} = \frac{\omega_{gt}\sum_i M_{igt}N_{ig}}{\sum_i M_{igt}S_{ig}} = \omega_{gt}\frac{< M_{igt},\ N_{igt} >}{< M_{igt},\ S_{igt} >} = \omega_{gt}\frac{\rho_{MN}\|M_{gt}\|\|N_{gt}\|}{\rho_{MS}\|M_{gt}\|\|S_{gt}\|} = \omega_{gt}\frac{\rho_{MN}\|N_{gt}\|}{\rho_{MS}\|S_{gt}\|}$$

Note that $\rho_{AB} =< A, B >/(\|A\|\|B\|)$ where $\|A\| = \sqrt{< A, A >}$ is the Pearson product-moment correlation coefficient. When $\rho_{MN} \approx \rho_{MS}$,

$$\frac{E[d_N]/\|N\|_i}{E[d_S]/\|S\|_i} \approx \omega_{gt}$$

I.e. dN/dS is approximately equal to the selective pressures on nonsynonymous mutations when the accessible nonsynonymous and synonymous loci are properly accounted and when the correlation between mutational processes and nonsynonymous loci are roughly equivalent to the correlation between mutational processes and synonymous loci. Traditionally, this assumption was used to calculated dN/dS. To improve resolution of dN/dS, researchers have attempted to account for these correlations using sophisticated parametric models of M_{igt}. An alternative statistical approach, however, is to treat these correlations as nuisance parameters.

Constrained Marginal Models permute observed data in all possible manners that preserve the underlying covariance structure of the data (e.g. ρ_{MN}, ρ_{MS}). In our particular case of this method, we note that by definition, $d_N^{permuted} = \sum_i(d_N^{observed}{}_i N_i + d_S^{observed}{}_i N_i)$. Thus:

$$\frac{E[d_N^{permuted}]}{E[d_S^{permuted}]} = \frac{\sum_i(\omega_{gt}M_{igt}N_{igt}^2 + M_{igt}N_{igt}S_{igt})}{\sum_i(\omega_{gt}M_{igt}N_{igt}S_{igt} + M_{igt}S_{igt}^2)} = \frac{\omega_{gt}\rho_{MN}\|M_{gt}\|\|N_{gt}\|^2 + \rho_{MN}\|M_{gt}\|\|N_{gt}\|\|S_{gt}\|}{\omega_{gt}\rho_{MS}\|M_{gt}\|\|S_{gt}\|\|N_{gt}\| + \rho_{MS}\|M_{gt}\|\|S_{gt}\|^2} = \frac{\rho_{MN}\|N_{gt}\|}{\rho_{MS}\|S_{gt}\|}$$

Hence, by dividing the observed mutations by all permutations, we eliminate the covariance of mutational processes with available loci and, thus, measure ω_{gt} directly for any particular gene-tumor combination without mutational bias.

Unfortunately, because of the log-sum Inequality, mutational bias can arise once cohorts of genes and cohorts of tumor samples are binned. This problem is common to all dN/dS measures and is a consequence of the correlation of mutational biases with *selection* (i.e. $< M_{igt}, \omega_{gt} >$) – not the correlation of mutational biases with one another, as these covariances are already accounted-for in a Constrained Marginal Model. For example, if tri-nucleotide biases covary linearly with gene-level biases, and are independent of tumor-level biases, then a parametric estimate of M_{igt} may deconstruct M_{igt} into $M_{igt} = f(i, g, t, \rho_{ig})$, where ρ_{ig} is the covariation of tri-nucleotide mutational biases with gene-level biases. Nonetheless, $< M_{igt}, \omega_{gt} > \propto < \rho_{ig}, \omega_{gt} >$ will still be ignored. Indeed, this covariation of mutational processes with selective forces is the raison d'etre of the current study: because of Hill-Robertson Interference, selection is correlated with genome-wide mutation rate (i.e. $\sum_t M_{igt}\omega_{gt} \neq 0$). Hence, the level at which observed d_N values d_S are binned necessarily ignores covariation between mutational processes and selection (in addition to any variation of ω_{gt} within the cohort (e.g. balanced positive and negative selection that might also be misinterpreted as neutral evolution).

To confirm that our null model can accurately estimate dN/dS even in the presence of extreme mutational biases, we simulated artificial data where different COSMIC signatures[5] (SBS Signatures 1-9, v3) contribute to all of the mutations. Permuted d_N and d_S tallies for each mutational context were simulated by randomly sampling 1,000 genes with the same mutational context. The fraction of permuted d_N and d_S tallies for each mutational context was used as weighted probabilities to derive observed d_N and d_S tallies. To simulate negative selection, d_N counts were randomly removed from each context at a rate 1 - ω_{gt} (e.g. a Simulated or 'true' dN/dS of 0.8 in a cohort of samples indicates a 20% chance of non-synonymous mutations being removed in the samples). These simulated (true) rates were then compared to observed and permuted d_N and d_S tallies according to the dN/dS metric that we used throughout this study:

$$\frac{dN}{dS} = \frac{d_N^{(\text{observed})} / d_N^{(\text{permuted})}}{d_S^{(\text{observed})} / d_S^{(\text{permuted})}}$$

Lastly, we note that binning nonsynonymous and synonymous mutations at the genome-wide level (e.g. drivers and passengers) provided the most robust estimates of dN/dS when bootstrapping observed tumor samples. Without binning at this level, statistical power is insufficient. Bootstrapping also demonstrated that log-transformed dN/dS values were more robust than untransformed values and thus were generally used in this study.

A Parametric Null Model of Mutagenesis. For comparison, we also calculated dN/dS using dNdScv[7] – a previously-published parametric null model of mutagenesis in cancer[8]. To compare both methods, dNdScv was ran globally and separately on samples stratified by the total number of substitutions using the following parameters:

```
max_coding_muts_per_sample = Inf
max_muts_per_gene_per_sample = Inf
```

Global dN/dS values of all non-synonymous mutations (w_{all}) reported by dNdScv were used. This model reproduced observed dN/dS trends (Supplemental Figure 3) and was used to infer patterns of selection in synonymous mutations (Supplemental Figure 17).

Orthogonality of dN/dS with Mutational Burden and effects of excluding samples with no synonymous mutations. Mutational burden is generally calculated as the total number of substitutions within a sample (i.e. $d_N + d_S$), however these tallies are also used in our measurement of dN/dS. Hence, any interdependence of mutational burden with dN/dS could bias our understanding of the relationship between selection and genome-wide mutation rate. We consider the interdependence of these two measures by assuming that both d_N and d_S are Poisson-distributed with rate parameters λ_N and λ_S. The joint probability mass density of any combination of these two quantities is then:

$$f(d_N, d_S) = \frac{\lambda_S^{d_N + d_S} r^{d_N} e^{-\lambda_S (r+1)}}{d_N!\, d_S!\, (1 - e^{-\lambda_S})}$$

Here, $r = \lambda_N / \lambda_S$. The expectation value of dN/dS, for any degree of selection versus any combination of nonsynonymous and synonymous mutation tallies can then be calculated simply by exhaustively summing over all combinations that arise with probability above machine precision. In Supplementary Figure 5, we compare the variation in dN/dS for a typical genome under neutral selection or equally-balanced positive and negative selection (r = 2.8) using the $d_N + d_S$ and d_S mutational burden metrics. We observe less deviation from expectation using $d_N + d_S$ primarily because d_S alone is a poor proxy for the mutation rate — i.e. there are far fewer synonymous mutations to use to estimate the mutation rate. $d_N + d_S$ did exhibit slightly greater bias in observed dN/dS relative to expectation, however this bias was small compared to the variation in estimates (<5% for mutational burdens greater than 2) and biased observed estimates towards increased values of dN/dS, which will only understate the degree of negative selection. Lastly, we note that because the genome-wide dN/dS is approximately 1, deviations from these theoretical calculations should be minimal.

We also tested the effects of this non-orthogonality of our approach in three additional ways. First, we investigating the correlation of mutational burden metrics mutation rate in our simulated tumors (see below) and found that $d_N + d_S$ correlated most strongly with mutation rate (Supplemental Figure 5C). Next, we randomly-partitioned all protein-coding mutations into two necessarily-orthogonal halves: a half that defined the mutational burden and a half that was used for calculating dN/dS and found that selection patterns persisted (Supplemental Figure 5B). Finally using the WGS data, we compared dN/dS to measures of mutational burden that excluded data from protein-coding regions (all intergenic and all intronic mutations), which once again represents a completely-orthogonal measure (Supplemental Figure 3).

Identification of driver genes in cancer. For all analysis using SNVs unless explicitly stated, a comprehensive list of 299 pan-cancer driver genes were derived from 26 computational tools used to catalog driver genes[9]. Other pan-

cancer driver gene sets tested were derived from COSMIC's Driver Gene Census[5] (downloaded on October 2016) and IntOGen's Cancer Drivers Database[10] (v2014.12) which contained 602 and 459 number of driver genes, respectively.

Many driver genes are associated with only particular tumor subtypes. To compare patterns of selection across cancer subtypes without increasing or decreasing the size of the list for each subtype, we chose to use a single set of driver genes for most analyses. This may understate the degree of positive selection in driver genes as mutations in these genes may be passengers in some tumor subtypes. In Supplementary Figure 8, we investigate patterns of selection using the top 100 driver genes identified for each tumor type and observe decreased signatures of positive selection overall in driver genes. Nevertheless, the patterns of attenuated selection in drivers and passengers remains. While tissue-type specific driver genes certainly exist, our results suggest that our statistical power to detect drivers still remains too limited to justify subdividing analyses by tumor type in many cases.

For all CNA analysis, GISTIC 2.0[11] was used to identify a set of genomic regions enriched for copy number gains and copy number losses using recommended settings with a confidence threshold of 0.9. CNAs used to identify these peaks were downloaded from the NIH Genomic Data Commons (GDC)[12] in the TCGA cohort. For each amplification peak, the closest gene was annotated as a putative Oncogene, and similarly the closest gene to each deletion peak was annotated as a putative Tumor Suppressor. The top 100 amplification peaks (oncogenes) and deletion peaks (Tumor Suppressors) were classified as drivers for each of the 32 tumor types. 34% of identified driver genes appear in more than one tumor type, while 2.6% of identified driver genes appear in more than five tumor types.

Annotation of clonal and subclonal mutations. Since TCGA contains SNVs with high coverage and available purity estimates, only MC3 SNVs (exclusive to TCGA) were used in this analysis (WGS read-depth is generally lower than WES read-depth). Variant allele frequencies (VAFs) were calculated per site as the number of mutant read counts divided by the total number of read counts. VAFs were adjusted for purity using calls made by ABSOLUTE[12,13], collected from GDC. A VAF threshold of 0.2 was used to define 'subclonal' (< 0.2) vs 'clonal' (> 0.2) SNVs. Different VAF thresholds were considered (Supplemental Figure 10) and the choice of 'clonal' thresholding did not impact the conclusions of this study.

Polyphen2 analysis. PolyPhen2 annotations in the MC3 SNP calls were used[14]. Only missense mutations that were categorized as either 'benign', 'probably damaging' or 'possibly damaging' were used. Fraction of pathogenic missense mutations was calculated as the number of pathogenic mutations of all confidence levels divided by the total number of categorized mutations.

Classification of genes by functional category. To test for patterns of selection in functionally related genes, we annotated all mutations by different functional categories and Gene Ontology (GO) terms[15]. Oncogenes and tumor suppressors were annotated from a curated set of 99 high confidence cancer genes[16]. Essential genes were collected from a genome-wide CRISPR screen that identified genes required for proliferation and survival in a human cancer cell line[17]. Housekeeping genes were defined as genes with an exon that is expressed in all tissues at any nonzero level, and exhibits a uniform expression level across tissues[18]. Interacting proteins were downloaded from the mentha database in April 2019[19].

To identify highly expressed genes, median transcripts per million (TPM) in 54 tissue types (v7 release) were downloaded from the Genotype-Tissue Expression (GTEx) project[20]. Tissues that contained high expression in most genes, specifically testes, were removed. Only genes that had TPM counts above zero in any of the 53 remaining tissues were used. TPM counts were averaged across all tissues. Highly expressed genes were defined as the top 1000 genes expressed across all tissues.

To test for signals of negative selection in other functional groups, we annotated mutations by candidate GO terms according to Biological Processes: Transcription Regulation (GO Term ID: 0140110), Translation Regulation (GO Term ID: 0045182), and Chromosome Segregation (GO Term ID: 0007059).

Somatic Copy Number Alteration (CNAs). All CNAs were downloaded from the COSMIC database on June 2015[5]. Mitochondrial CNAs were discarded from analysis, as copy number changes are difficult to infer. Gene annotations and the locations of telomeres and centromeres were downloaded from the UCSC Genome Browser (hg19). Telomeric and centromeric regions (also defined by the UCSC Genome Browser) were masked from all measurements of dE/dI. Because the selection patterns of non-focal CNAs — alterations with at least one terminus in a telomere or centromeric region — were not noticeably different from long (>100kb) focal CNAs, these two alteration classes were aggregated for analysis. Because we observed positive selection for deletions (copy number losses) within oncogenes and amplifications (copy number gains) within Tumor Suppressors, we did not delineate between gains and losses, nor oncogenes and Tumor Suppressors, in reported analyses. CNAs that overlapped an oncogene or tumor suppressor in any region (for any fraction of the CNA) were classified as drivers. Mutational burden was defined simply as the total number of CNAs within a sample. Pan-cancer CNAs from cBioPortal (August 2018) were also analyzed, however consistent purity and ploidy estimates could not be obtained by using either ABSOLUTE[13] or TITAN[21], so this data was not used for published analyses.

Measurements of selection on CNAs. dE/dI was calculated using a 'Breakpoint Frequency' metric and a 'Fractional Overlap' metric. For both metrics, the dE/dI of a particular gene set *i* (e.g. driver or passenger genes) is defined by a genomic track $T_{i,g}$, which is one for every annotated region g of the track and zero elsewhere. Only non-centromeric and non-telomeric regions are considered in the mappable human genome G. Each CNA $C_{\mathrm{g,m}}$ is defined by its position on the genome *g* and the mutational burden *m* of the tumor harboring the mutation. For 'Breakpoint Frequency' $C_{\mathrm{m,i}}$ is one at the position of both termini of the CNA and zero elsewhere. For 'Fractional Overlap' $C_{\mathrm{m,i}}$ is $1/L$, where L is the length of the CNA, for every region of the genome spanned by the CNA and zero elsewhere. For a particular range of mutational burdens M, dE/dI was defined as:

$$\frac{dE}{dI}_{i,M} = \frac{\sum_m^M \sum_g^G T_{i,g}\, C_{m,g}}{\sum_g^G T_{i,g}}$$

We note that calculation is accelerated by >100x by commuting $T_{\mathrm{G,i}}$ with the outer summation ($\Sigma_m{}^M$). Lastly, we note that the pan-cancer genome-wide Breakpoint Frequency dE/dI slightly exceeds 1, which may be driven by a mutational bias for CNAs to arise in open chromatin (Supplemental Figure 20).

Cancer subtype analysis. All tumor subtypes in TCGA and ICGC were grouped into 9 sub-categories, based on broad, predominantly-anatomical features. Anatomical features (i.e. organ and systems of organs), rather than histological features or inferred cell-of-origin, were used as groupings because we believe that the fitness effects of mutations should be predominantly defined by the environment of the tumor. Nevertheless, we observed attenuated selection in both drivers and passengers in many broad histologically-defined classifications (e.g. adenocarcinomas & sarcomas). For all cancer grouping analysis (broad and subtype), tumors were stratified into bins by the total number of substitutions ($d_N + d_S$) on a log-scale. Since tumor subtypes vary in their range of mutational burdens, (e.g. KIRC cancer subtypes only have tumors with <100 substitutions), dN/dS values in the lowest and highest mutational burden bin for each cancer-subtype are shown.

Specific cancer subtype categories were taken directly from the NCI Genomic Data Commons (GDC)[12]. Because CNAs were downloaded from COSMIC, CNA datasets were not classified with this same ontology. Table S1 details how CNA classifications were mapped on GDC categories (and sometimes more broadly-defined groups). All subtypes with >200 samples were used in our CNA subtype analyses (Supplemental Figure 13).

An evolutionary model with Hill-Robertson Interference. Somatic cells in our populations are modeled as individual cells that can stochastically divide and die in a first-order (memoryless) Gillespie Algorithm. This model was developed and described previously[22]. During division, cells can acquire advantageous drivers with rate μT_{d} and deleterious passengers with rate μT_{p} – these values specify the mean of Poisson-distributed pseudo-random number (PRN) generators that prescribe the number of drivers and passengers conferred during division (e.g. the number of drivers per division $n_{\mathrm{d}} = \mathrm{Poisson}[n_{\mathrm{d}} = k; \lambda = \mu T_{\mathrm{d}}] = \lambda^k e^{-k} / k!$). The Distribution of Fitness Effects (DFE)

conferred by each driver and each passenger are Exponentially-distributed PRNs with probability densities $P(s_i = x; s_d) = \mathrm{Exp}[-x/s_d]/s_d$ and $P(s_i = x; s_p) = -\mathrm{Exp}[-x/s_p]/s_p$ respectively. Simulations with other exponential-family DFEs do not qualitatively differ from these exponential distributions[23]. The aggregate absolute cellular fitness is $f = \prod_i^{all\ mutations}(1 + s_i)$ in our Multiplicative Epistasis model and $\Delta f = s_i/(1 + \nu f)$ with ν = 1 in our Diminishing-Returns Epistasis Model where Δf is the change in cellular fitness with each mutation (borrowed from [PMID: 9888858]). The rate of cell birth is inversely proportional to cellular fitness, while the rate of cell death $D(N; N^0) = \mathrm{Log}[1 + \frac{N}{(e-1)N^0}]$ increases with the population size of the tumor *N*. With these birth and death processes, mean population size abides by a Gompertzian growth law in the absence of additional mutations, which is scaled by the mean cellular fitness $\mathrm{E}[N(<f>)] = \mathrm{Log}[1 + <f> / N^0]$ (derived from Master Equation[23]). While, programmatically, mutations exclusively affect the birth rate and the constraints on growth exclusively affect the death rate, we previously demonstrated that birth and death rates are generally nearly-balanced such that dynamics are not affected by this design choice. Simulations progressed until tumor extinction (*N* = 0 cells), malignant transformation ($N = 10^6$ cells), or until approximately 100 years had passed (18,500 generations). Only fixed mutations (present in the Most Recent Common Ancestor) within clinically-detectable growths were analyzed in our ABC pipeline. The behavior of this model has been described previously[22,23] and the most relevant assumptions of this model and their effects on the conclusions of this study are described in Table S2.

Cells in our populations are fully described by their accrued mutations, and birth and death times. Birth and death events were modeled using an implementation of the Next Reaction[24], a Gillespie Algorithm that orders events using a Heap Queue. Generation time in our model was defined as the inverse of the mean birth rate of the population: 1/ <B(d, p)>. While all mutation events occurred during cell division, if mutations were to occur per unit of time (rather than per generation), rapidly growing tumors would acquire drivers at a slightly slower rate as generation times decline over time. This effect, however, is negligible compared to the variation in waiting times conferred by the variation in mutation rates (division times merely double, while mutation rates vary by 100,000x).

This simply evolutionary model is defined by five parameters μT_d, μT_p, s_d, s_p, and N^0. The target size of drivers is defined as the approximate number of nonsynonymous mutations in the Bailey Driver Screen T_d = (# of driver genes)•(mean driver length)•(fraction of SNVs that are nonsynonymous) = 300 genes • 1298 loci/gene • 0.737 nonsynonymous loci / loci = 286,886 nonsynonymous loci. The target size of passengers was simply the remaining loci in the protein coding genome, T_p = 20,451,136 nonsynonymous loci. The mutation rate was constant throughout each tumor simulation and randomly-sampled from a uniform distribution in log-space that ranged from 10^{-12} to 10^{-7} mutations•loci^{-1}•generation^{-1}. While tumors were initiated from this broad range, successful tumors ($N > 10^6$ cells) were almost always restricted to mutation rates between 10^{-10} and 10^{-8} (Supplementary Figure 18), as tumors with mutation rates drawn below this range almost never progressed to cancer within 100 years and tumors with mutation rates drawn above this range went extinct through natural selection.

The likelihood that tumors progress to cancer in the presence of deleterious passengers depends heavily on the initial population size N^0 of the tumor. This dependence was studied previously[22], where it was demonstrated that reasonable evolutionary simulations (those that progress to cancer >10% of the time, but less than 90% of the time) are restricted to a four-dimensional manifold N^* within the five-dimensional phase space of parameters. For this reason, $N^0 = N^*(s_d, s_p, \mu T_d, \mu T_p)$ was determined by the other four parameters. To first-order, this manifold is $T_p\, s_p / T_d\, s_d^2$, however a more precise estimate (Eq. S8 of [22]) incorporating more precise estimates of Muller's Ratchet and the effects of hitchhiking on both driver and passenger accumulation rates, which does not exist in closed form was used. Additionally, at very low values of s_d, progression to cancer is limited by time, not by the accumulation of deleterious passengers. Hence, we assigned N0 such that:

$$N^0 = Max_{N^0}[P_{cancer}(N^0/N^*) = 0.5, \overline{t_{cancer}}(N^0/N^*) = 18{,}500 \text{ generations}]$$

Here, P_{cancer} and t_{cancer} – the likelihood and waiting-time to cancer – are defined by equations S8 and S10 respectively in [22]. N^0 was determined from these equations using Brent's Method. Supplementary Figure 15 depicts the values of N^0, which ranged from 1 to 100 for all simulations. All code for the simulations, associated theoretical analysis, and generation of summary statistics will be available at https://github.com/petrov-lab/pdSim.

In tumors that progress to malignancy ($N = 10^6$), only fixed nonsynonymous mutations (present in all simulated cells) were recorded. We also recorded (i) the fitness effect of these mutations, (ii) the mean population fitness, (iii) the number of generations until malignancy, and (iv) the mutation rate. These two values were used to generate the number of synonymous drivers and passengers, where $\mathrm{P}(d_s = k) = \mathrm{Poisson}[k; \lambda = \mu T_{d/p} / r\, t_{\mathrm{MRCA}}]$ defines the number of synonymous drivers/passengers conferred, t_{MRCA} represents the number of division until the Most Recent Common Ancestor arose in the simulation, r = 2.795 represents the ratio of nonsynonymous to synonymous loci within the genome, weighted by the genome-wide trinucleotide somatic mutation rate, and the Poisson PRN generator was defined above. In simulations where synonymous drivers could arise, a fraction of the recorded nonsynonymous mutations (ranging from 0 – 20%) were simply re-labeled as synonymous drivers (as opposed to nonsynonymous drivers). This was done, again, by Poisson-sampling in proportion to the desired fraction for each cancer simulation.

20 x 20 combinations of s_d and s_p parameters were simulated (Supplemental Figure 14 & 15). Simulations were repeated until 10,000 cancers at each parameter combination were obtained or until 10 million tumor populations were simulated. While we attempted to initiate tumors at a population size where the probability of progression to cancer was 50%, some parameter combinations still did not yield 10,000 cancers after 10 million attempts (i.e. $P_{\mathrm{cancer}} < 0.1\%$). These combinations were predominately at low values of s_d, which were far from the MLE estimate of s_d and represent unrealistic evolutionary scenarios, as drivers cannot be weakly beneficial, relegated to only 300 genes, and yet still overcome the deleterious load that passengers impart within 100 years. These simulations are annotated as "Progression Impossible." Simulation parameter sweeps were performed for both the Multiplicative and Diminishing Returns Epistasis models. Twenty fractions of synonymous drivers were also generated (ranging from 0% to 20%). These fractions were generated by simply re-labeling the driver mutations which conferred fitness (generated during the simulation) as synonymous, instead of nonsynonymous.

Summary statistics of simulated and observed tumors. For both simulated and observed data, we summarized dN/dS rates versus mutational burden for drivers and for passengers by decade-sized bins: (0, 10], (10, 100], (100, 1,000]. Mutational burden for simulations was defined as the total number of substitutions ($d_N + d_S$) – exactly as it was defined for observed data. For simulated data, $\mathrm{dN/dS} = d_N/(d_S \bullet \mathrm{r})$. Like observed data, dN/dS rates attenuated towards 1 for both drivers and passengers for all values of s_d and s_p.

Mutational Burdens (MB) for simulated and observed data were summarized with the parameters of a Negative Binomial distribution, where $P(\mathrm{MB} = k;\ n, p) = \binom{k+n-1}{n-1} p^n (1-p)^k$. This distribution has been used previously to summarize the mutational burdens of human tumors [25] and exactly defines the expected number of mutations at transformation in a Multi-Stage Model of Tumorigenesis[26] when n drivers are needed for transformation and the probability that any mutation be a driver is $1 - p$ [27]. Both n and p were used to summarize MB. These quantities were determined by Maximum Likelihood optimization of the probability mass function above over the support of mutational burdens of [1, 1,000] substitutions. The Han-Powell quasi-Newton Least-squares method was used for optimization.

Age-dependent Cancer Incidence rates (CI) were summarized with the parameters of a Gamma distribution, where $P(CI \leq t;\ k, \theta) = \frac{1}{\Gamma(k)} \gamma\left(k, \frac{t}{\theta}\right)$. Here, $\gamma(s, x) = \int_0^x t^{s-1} e^{-t} dt$ is the lower incomplete gamma function and $\Gamma(k) = \gamma(k, \infty)$ is the regular gamma function. Similar to our summarization of mutational burdens, this distribution is a generalization of the exact waiting time to transformation expected from a Multi-Stage Model of Tumorigenesis when tumors arise at a uniform rate over time, require k drivers for transformation, and wait an average time of θ between drivers [27]. This Cumulative Distribution Function was fit to observed incidence rates for all patients above 20 years of age using the least squares numerical optimization defined above (All cancer sites combined, both sexes, all races, 2012 – 2016 [28]). Patients under 20 years of age were excluded because cancers in these patients generally arise from germ-line predispositions to cancer, which are not directly modeled by our simulations, not detected as somatic mutations, and result in age-incidence curves that do not agree with a Gamma distribution[26]. Because all cancer simulations are initiated at $t = 0$ (instead of uniformly in time, as is presumed in the Multi-Stage Model), the simulated data was fit using the probability *density* function of this distribution (instantaneous derivative) using Maximum Likelihood and the optimization algorithm described above.

The cumulative distribution, then, represents the expected age-incidence cancer incidence rate when simulations begin at uniformly-distributed moments in time and, thus, was used to generate Figure 3D. Only the shape parameter k was used in ABC (and θ was ignored), as this parameter only specifies the dimensionality of time (simulation time was measured in cellular generations, not years) and all values of θ in our simulations are equivalent under a Gauge transformation. Additionally, we do not expect the exact times of incidence to be particularly informative as the time of transformation is somewhat earlier than the time of detection.

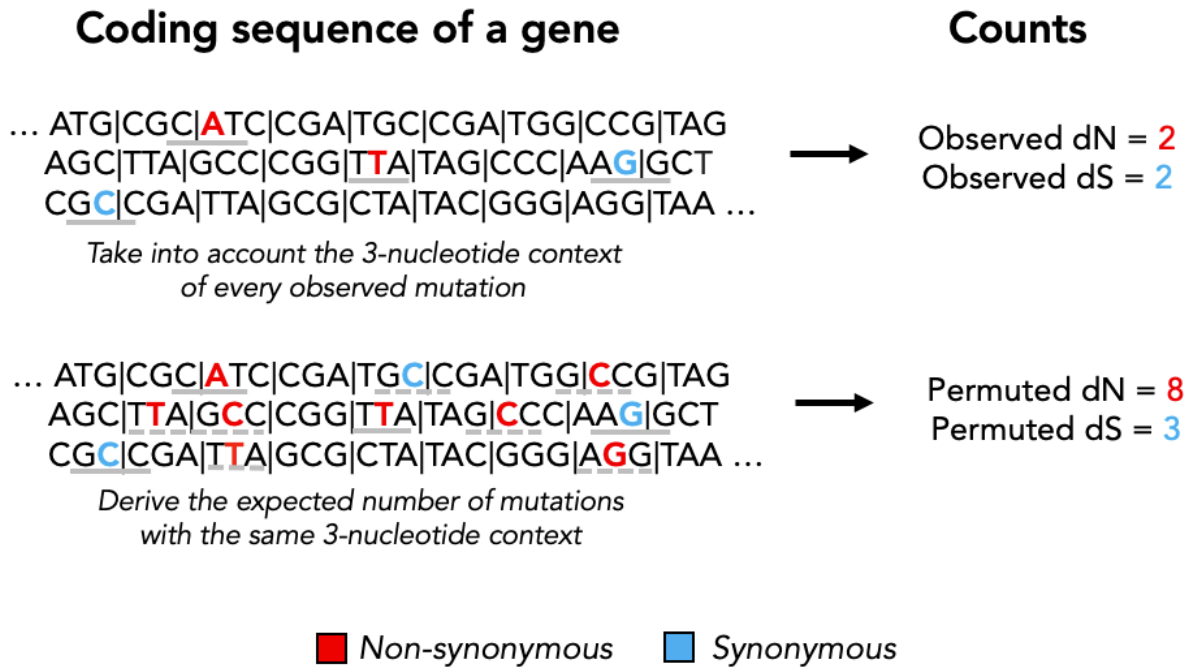
Use of Approximate Bayesian Criterion (ABC) for model selection and parameter inference. The main steps of an ABC analysis follow the general scheme of any Bayesian analysis: (1) formulating a model, (2) fitting the model to data (parameter estimation), and (3) improving the model by checking its fit (posterior-predictive checks) and (4) comparing it to other models [29,30].

The nine summary statistics described above were used to compare simulations to observed data. Agreement was summarized with a Log-Euclidian distance, as all summary statistics resided on the domain $[0, \infty)$ and log-transformation of the summary statistics minimized heteroscedasticity of the simulated data relative to a square-root or no transformation. Variance of the summary statistics was not normalized. ABC was performed using the `abc` R package[29].

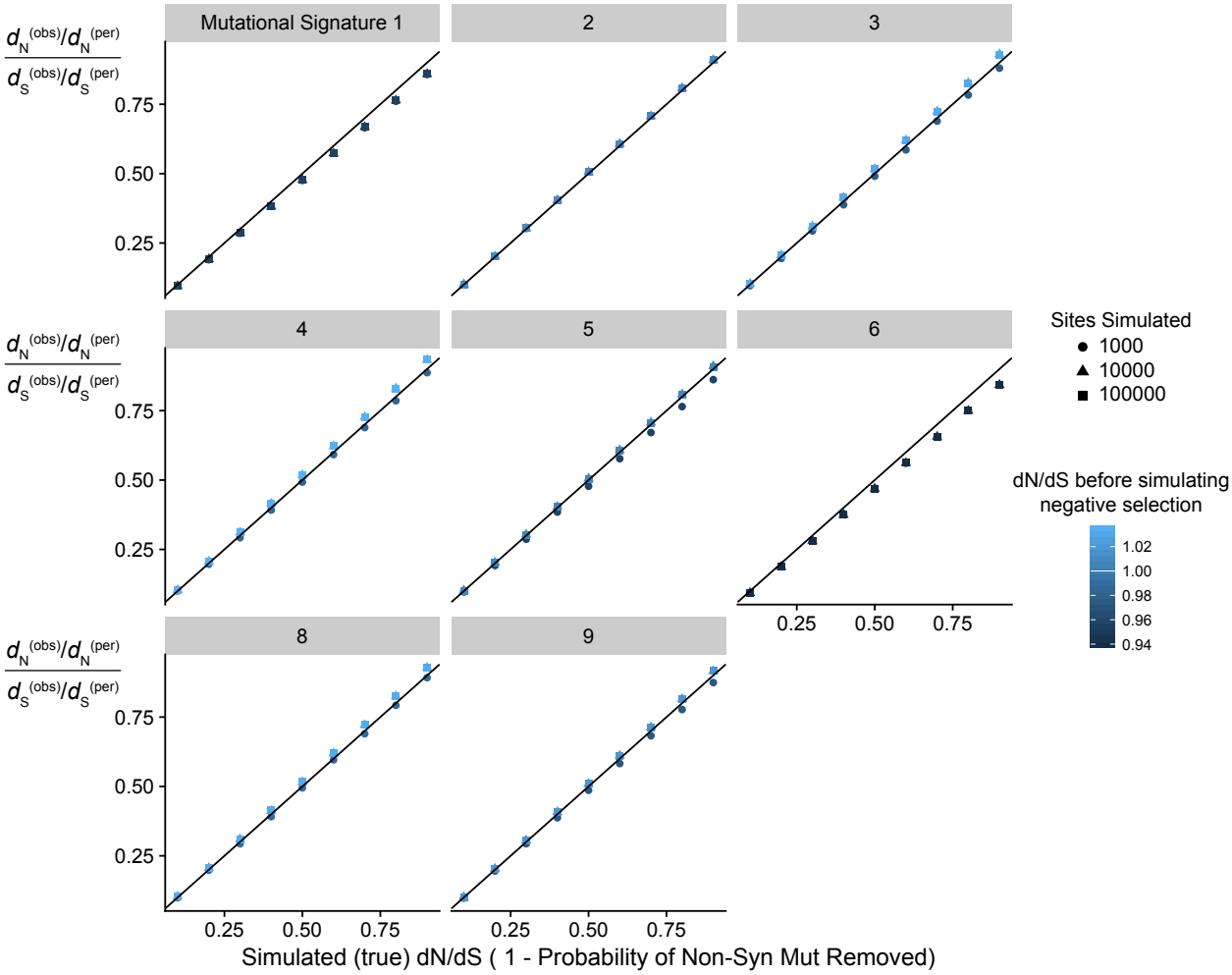
The rejection method (Feedforward Neural Net) and tolerance (0.5) were chosen based on their capacity to minimize prediction error of the simulated data using Leave-one-out Cross Validation (CV, Supplemental Figure 16A). 10,000 instances of the neural network, which was restricted to a single layer, were initiated and the median prediction of these networks were used. These parameters were used for both model comparison and parameter inference. The posterior model probability (postpr) was used to compare the two epistatic models (Diminishing Returns versus Multiplicative). The likelihood of the data under the Diminishing Returns model (14%) was less than the likelihood under the Multiplicative Epistasis Model (86%).For parameter inferencing, the s_d and s_p prior values were log-transformed.

For the synonymous driver model, the base model (without synonymous drivers) was simply the lowest quantity of synonymous drivers (0%) in the parameter sweep of synonymous driver quantities (Supplemental Figure 16B). The posterior probability mass of this value 0.043 was used as the one-sided *p*-value for the null hypothesis that these two models are equally predictive. Although the synonymous driver model agreed with the observed data slightly-better, s_d and s_p parameters could not be inferred from the data because the potential for synonymous drivers destroys the utility of dN/dS statistics – dN/dS is predicated on the notion that synonymous mutations are neutral. Virtually any value of dN/dS is attainable when the right combinations of selective pressures on nonsynonymous and synonymous are paired (Supplemental Figure 16C).

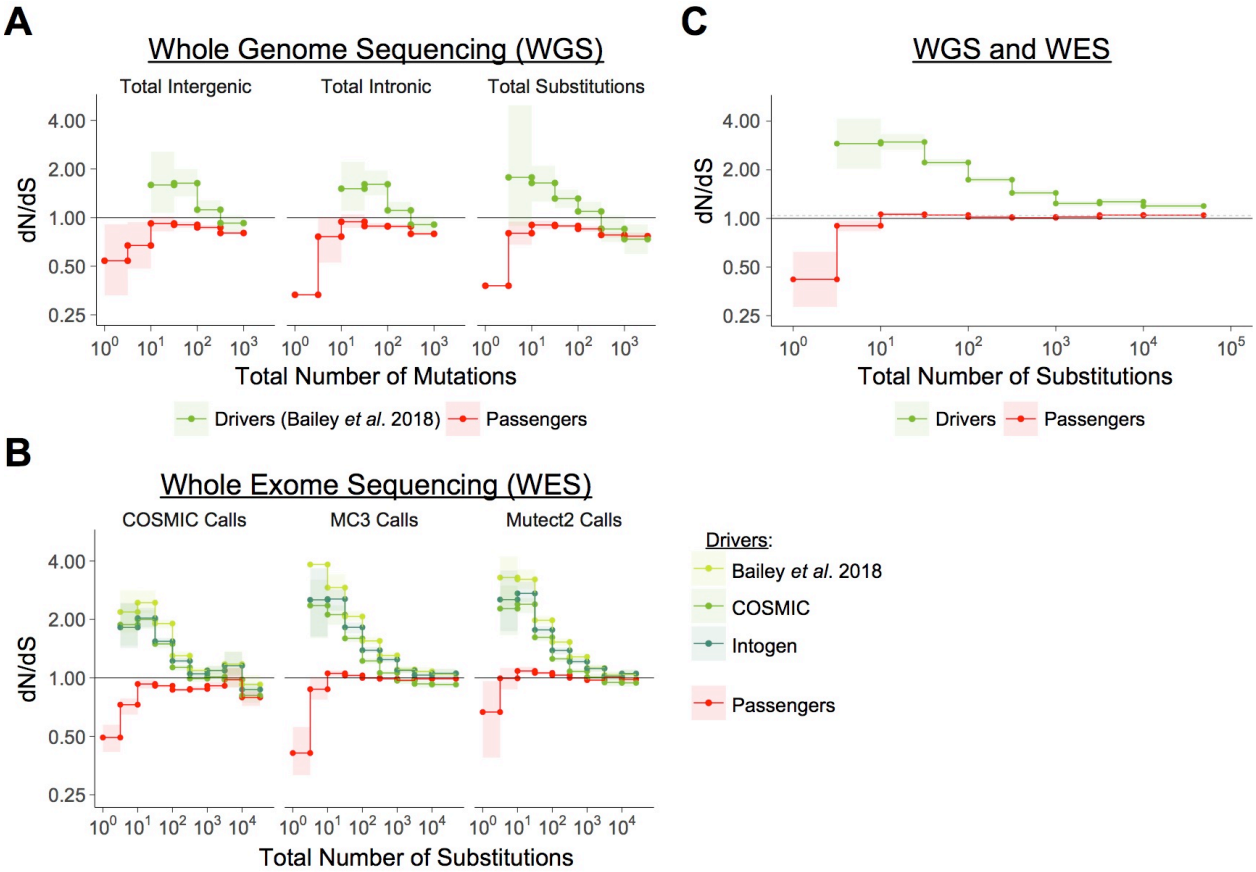
Supplementary Figures



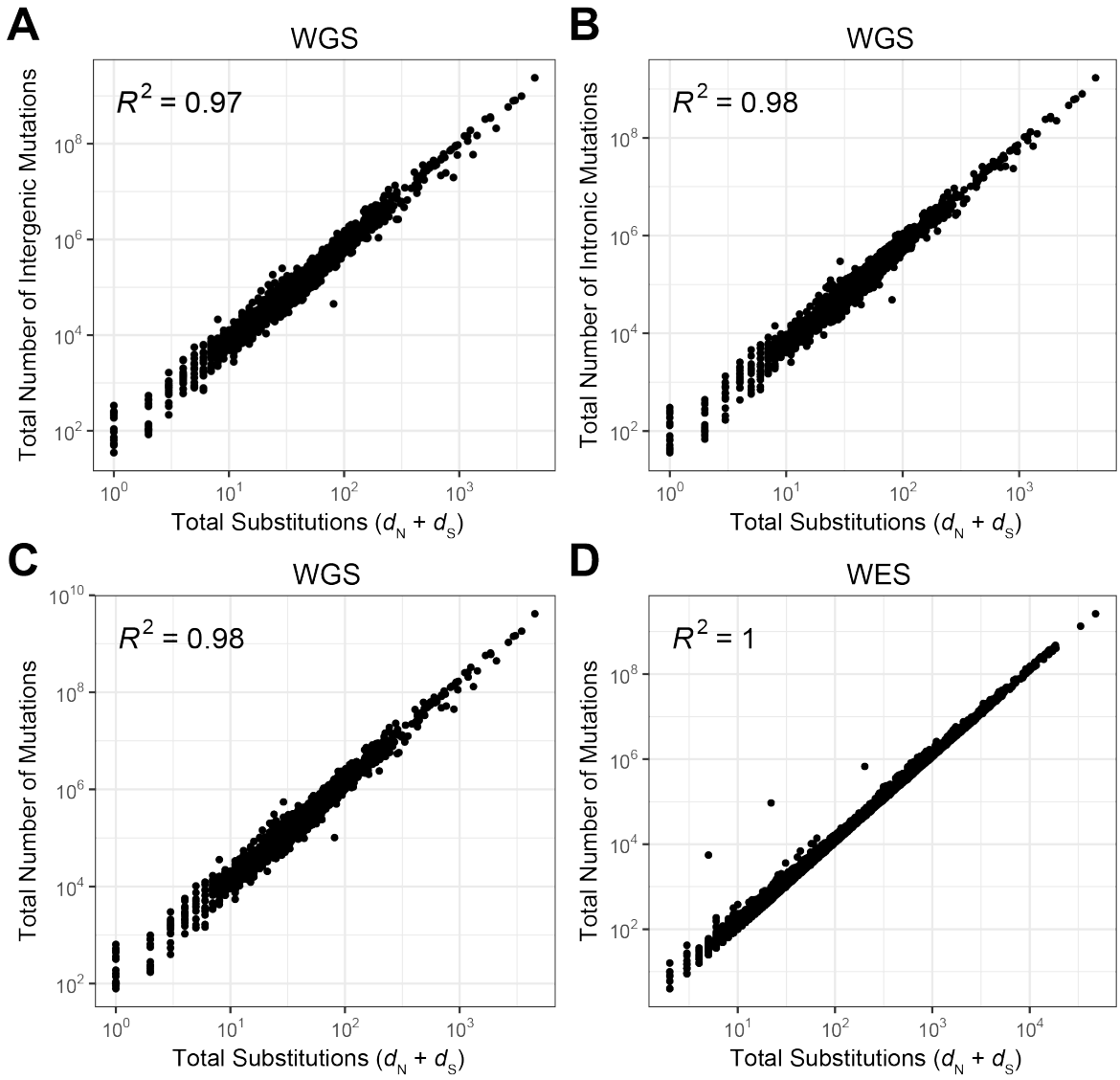
Supplemental Figure 1. Schematic of our permuted dN and dS calculation. Permuted synonymous and nonsynonymous counts are used to account for mutational biases in dN/dS calculations. Observed mutations and their 3-nucleotide context is shown in a solid gray bar. Permuted mutations with the same 3-nucleotide context are shown in dashed gray lines.



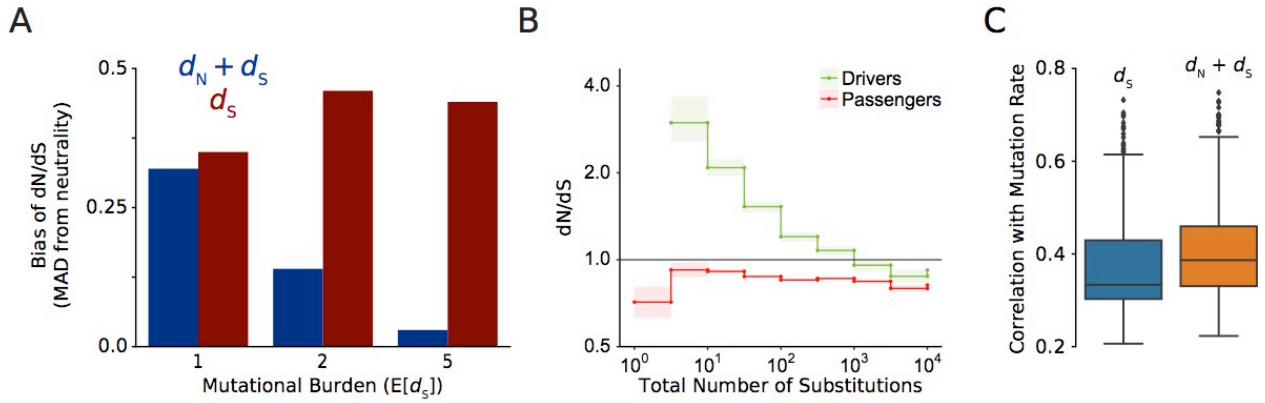
Supplemental Figure 2. Permutation-based null model of mutagenesis corrects for mutational biases in dN/dS calculations. Simulations (*N* = 100) of negative selection under extreme mutational bias scenarios where all mutations are generated from a single Mutational Signature (e.g. APOBEC or smoking, COSMIC Signatures 1-9, grey titles). Bias-corrected dN/dS values calculated from these simulations are compared to simulated levels of negative selection. Colors denote bias-corrected dN/dS before negative selection was simulated, which is expected to be neutral (~1). Negative selection is simulated as the probability of randomly removing nonsynonymous mutations, (e.g. a Simulated dN/dS of 0.1 defines simulations where each nonsynonymous mutation had a 90% probability of removal). Shapes correspond to different numbers of sites simulated. Black line identifies perfect correspondence between bias-correct dN/dS and Simulated (true) dN/dS.



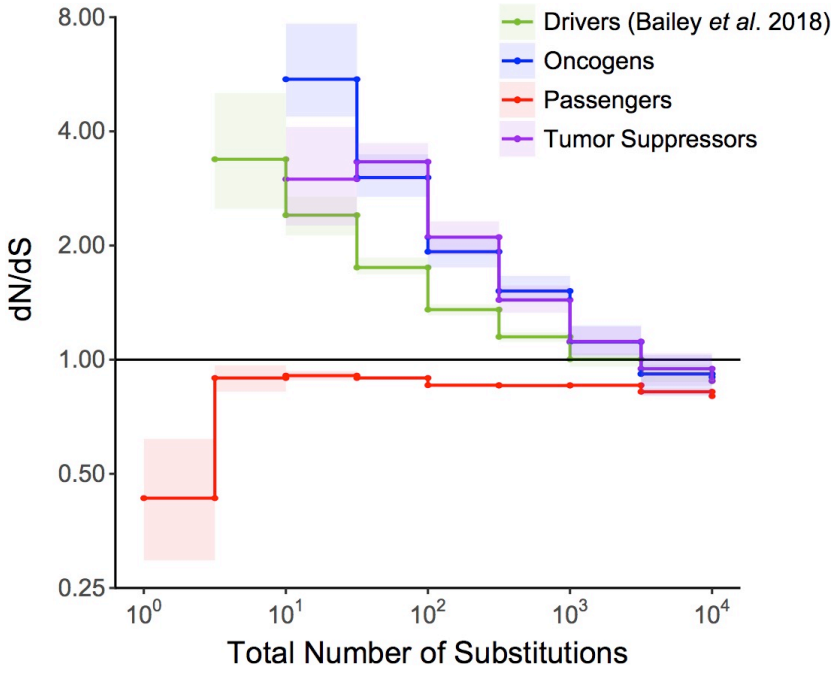
Supplemental Figure 3. Patterns of attenuated selection persist across mutation burden metrics, sequencing platforms, mutation calling algorithms, data repositories, choice of driver gene set, and null model of mutagenesis. (A) dN/dS calculations within passenger and driver gene sets within tumors in ICGC stratified by either the total number of intergenic mutations, intronic mutations or substitutions. **(B)** dN/dS calculations within passenger and various pan-cancer driver gene sets within tumors stratified by the total number of substitutions. Shown are tumors within TCGA called by different mutation callers (Mutect2 vs consensus SNP calls), and SNP calls from COSMIC. **(C)** dN/dS calculations within passenger and driver gene sets within tumors in ICGC and TCGA stratified by the total number of substitutions. Instead of using our nonparametric null model (e.g. AB and elsewhere), we calculate dN/dS using dNdScv[8] as a null model of mutagenesis (with default parameters and unrestricted quantities of coding mutations per gene). The solid black line (dN/dS = 1) annotates expected dN/dS under neutrality in all panels. Error bars are 95% confidence intervals determined by bootstrap sampling.



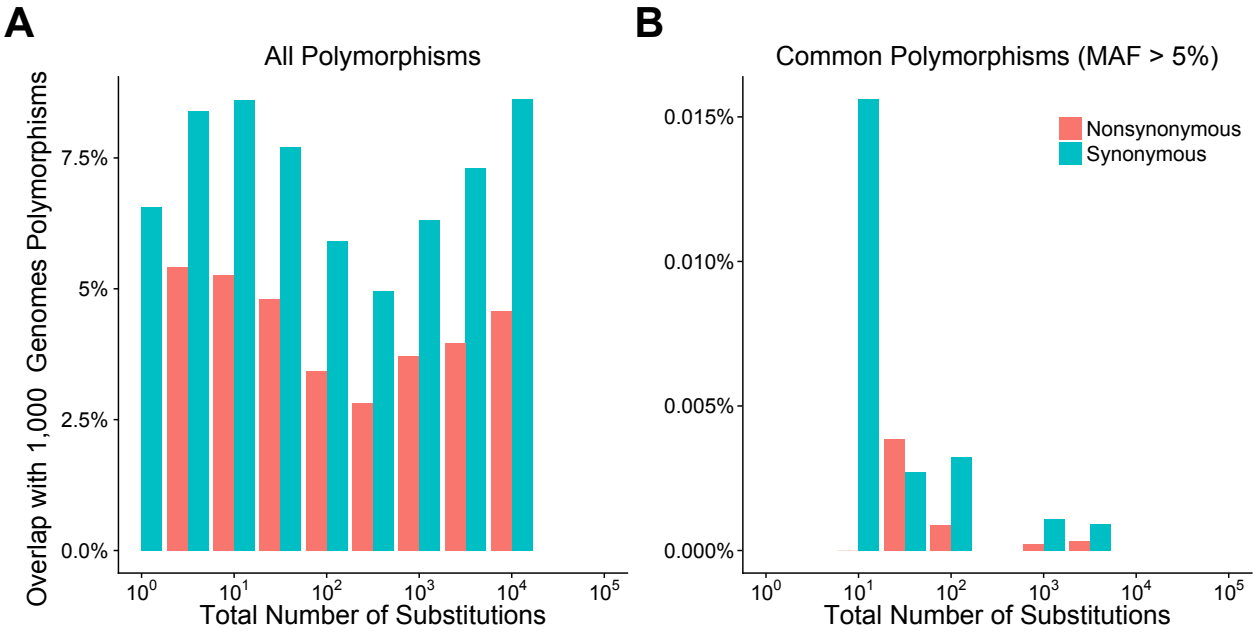
Supplemental Figure 4. Mutation burden metrics, used as a proxy for the tumor mutation rate, are correlated across datasets. (A) Comparison of the total number of substitutions within a tumor and the total number of intergenic or **(B)** intronic mutations within the tumor. **(C)** Comparison between datasets the correlation of Tumor Mutational Burden (TMB) and total number of substitutions for Whole Genome Sequening (WGS) of tumors and **(D)** Whole Exome Sequencing (WES) of tumors. Because all mutational burden metric are highly correlated, general patterns of selection are unaffected by choice of metric.



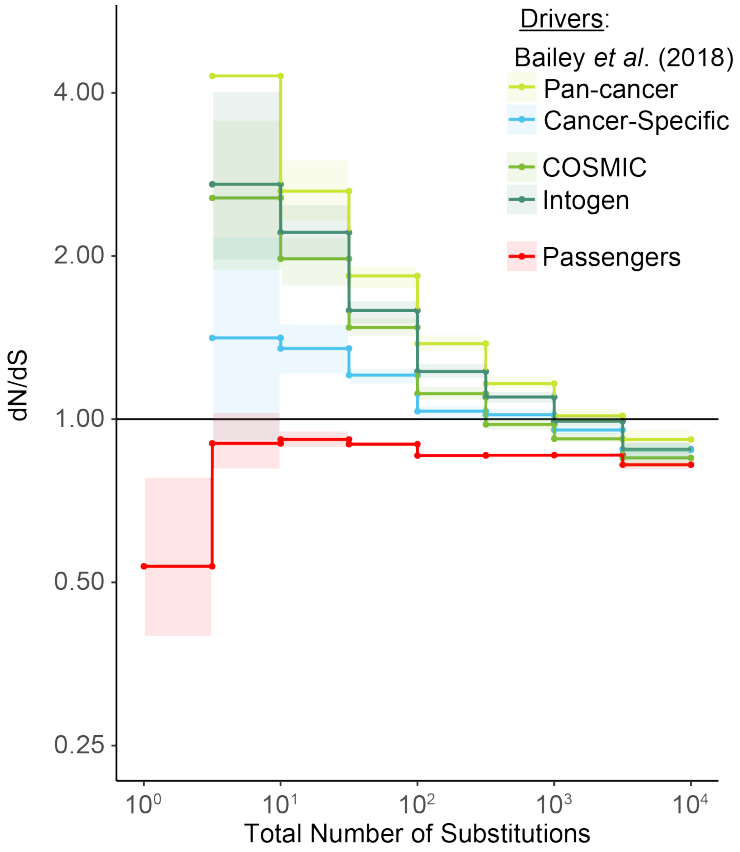
Supplemental Figure 5. Mutational Burden (defined as $d_N + d_S$) is nearly orthogonal to dN/dS, reproduces observed patterns of selection when completely orthogonalized, and is well-correlated with the genome-wide mutation rate in tumor simulations. (A) Theoretical bias of dN/dS (Mean Absolute Deviation from neutrality) of mutational burden metrics that contribute to dN/dS calculations. $d_N + d_S$ (i.e. Total Substitutions) imparts less bias than d_S (i.e. Total Synonymous Substitutions). Bias determined by analytical model of dN/dS with ratios of Poisson-sampled mutation tallies (Methods). Bias rapidly decreases with mutational burden for $d_N + d_S$. Total Substitutions ($d_N + d_S$) exhibit less bias than Total Synonymous Substitutions (d_S). **(B)** Patterns of selection persist when independent mutation counts (completely orthogonal) were used for estimating selection (dN/dS) and mutational burden ($d_N + d_S$). Independent accounts were achieved by randomly-partitioned mutations into two halves and using one half to calculate dN/dS and the half to calculate Total Number of Substitutions separately. Tumors were from TCGA. dN/dS and Error Bars (95% Confidence Interval) are same as in Figure 2. Solid black line of 1 denotes dN/dS expected under neutrality. **(C)** Pearson correlation of both mutational burden measures with mutation rate in computational model of tumor evolution (Methods). The mutational burdens of ~4 million simulated cancers were compared to their programmed mutation rate. $d_N + d_S$ correlated well with mutation rates across a range of evolutionary parameters and was more highly-correlated with mutation rate than d_S alone.



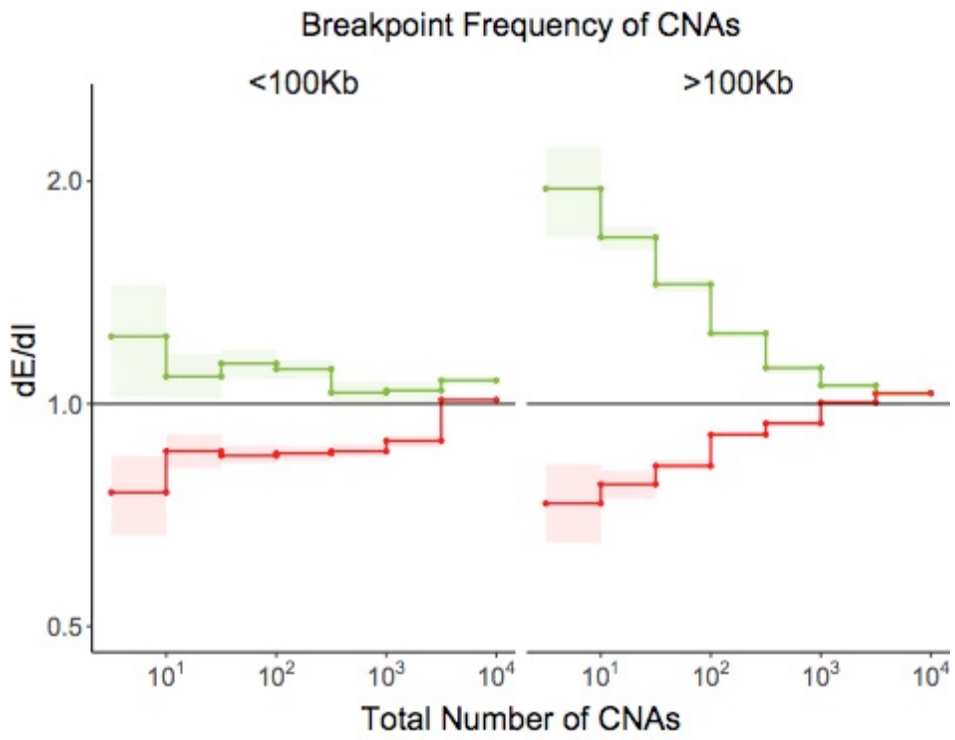
Supplementary Figure 6. Attenuation of selection with increasing mutational burden in both Oncogenes and Tumor Suppressors. dN/dS of passenger and driver gene cohorts[9] within tumors in TCGA stratified by the total number of substitutions present in the tumor (d_N + d_S). Tumor suppressors (purple), oncogenes (blue) and pan-cancer driver (green) gene sets are shown. Solid black shows dN/dS values of 1, expected under neutrality. Error bars are 95% confidence intervals determined by bootstrap sampling.



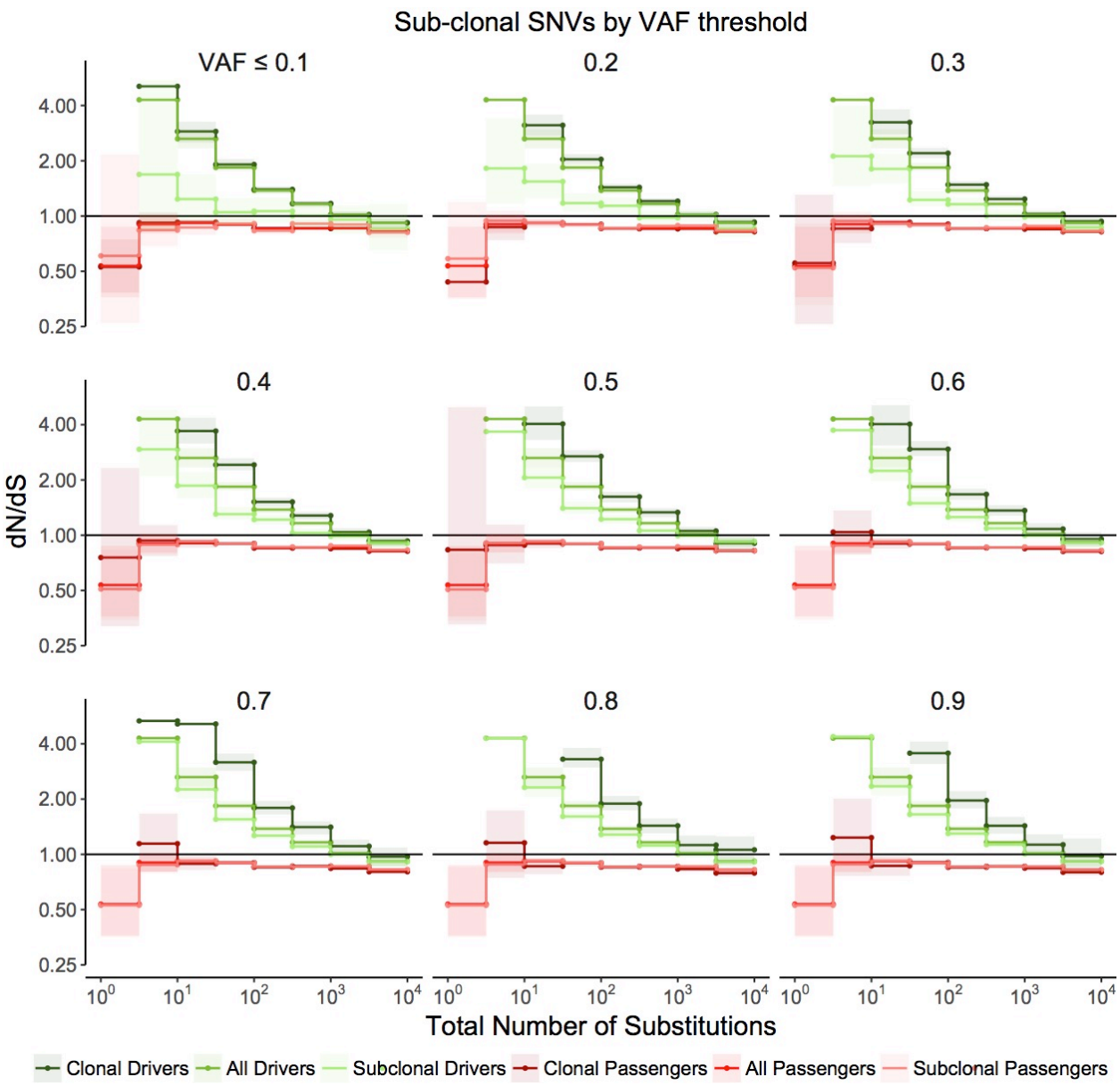
Supplemental Figure 7. No common germline polymorphisms observed in low mutation rate cancers. (A) Fraction of mutations that overlap all germline polymorphisms in the 1000 Genomes Project within tumors stratified by the total number of substitutions. **(B)** Fraction of mutations that overlap only common (MAF > 0.05) polymorphisms in the 1000 Genomes Project within tumors stratified by the total number of substitutions. WGS and WES datasets are shown. Colors denote mutations that are synonymous (blue) or nonsynonymous (red). Strong negative germline selection is expected only within common polymorphisms. Because no mutations within low mutational burden cancers (≤10 substitutions) overlap common polymorphic sites, germline contamination of somatic genome sequencing simply cannot explain the observed negative selection in passengers at low mutational burdens.



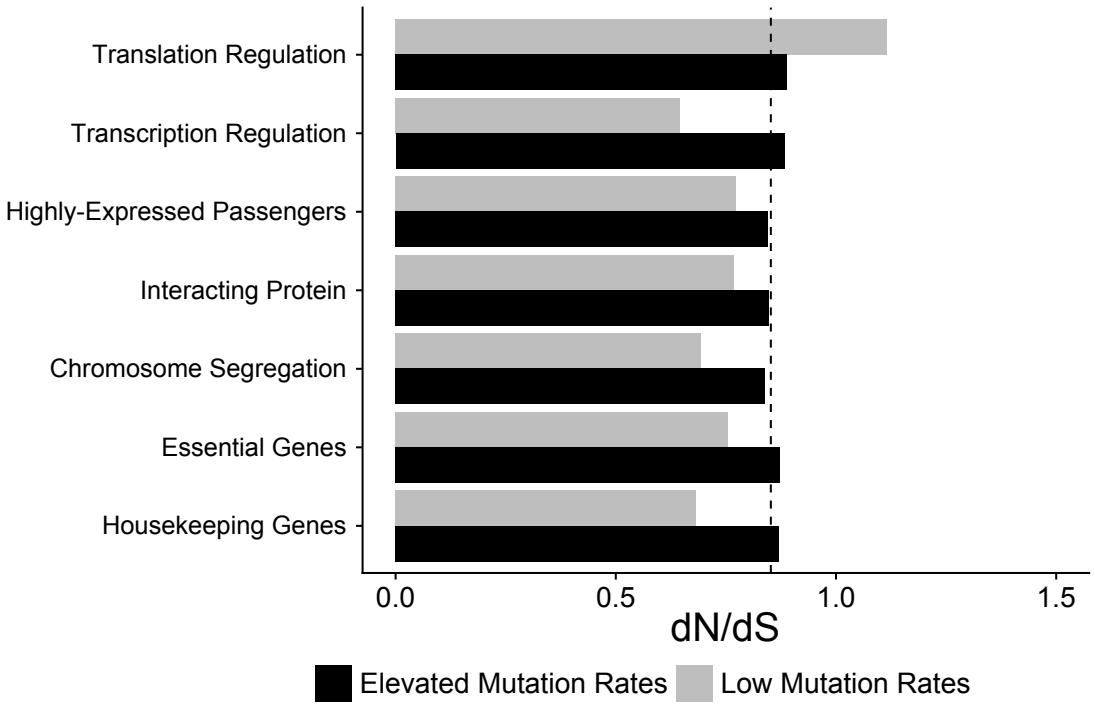
Supplemental Figure 8. Weaker signals of positive selection within cancer-specific drivers. dN/dS values of passenger and different driver gene sets within tumors in TCGA stratified by the total number of substitutions present in the tumor (d_N + d_S). Pan-cancer driver (lime) and cancer-specific (blue) driver gene sets identified by Bailey *et al*. 2018[9] are shown. Pan-cancer driver genes identified in this study also exhibited stronger signatures of positive selection than driver genes identified by COSMIC[31] (light green) and Intogen[10] (forest green). Hence, pan-cancer drivers from Bailey *et al.* 2018 were used throughout this study. Cancer-specific gene sets are defined as the top 100 recurrently mutated genes within the particular cancer type, and used separately for each of the 33 cancer types in TCGA. Solid black shows dN/dS values of 1, expected under neutrality. Error bars are 95% confidence intervals determined by bootstrap sampling.



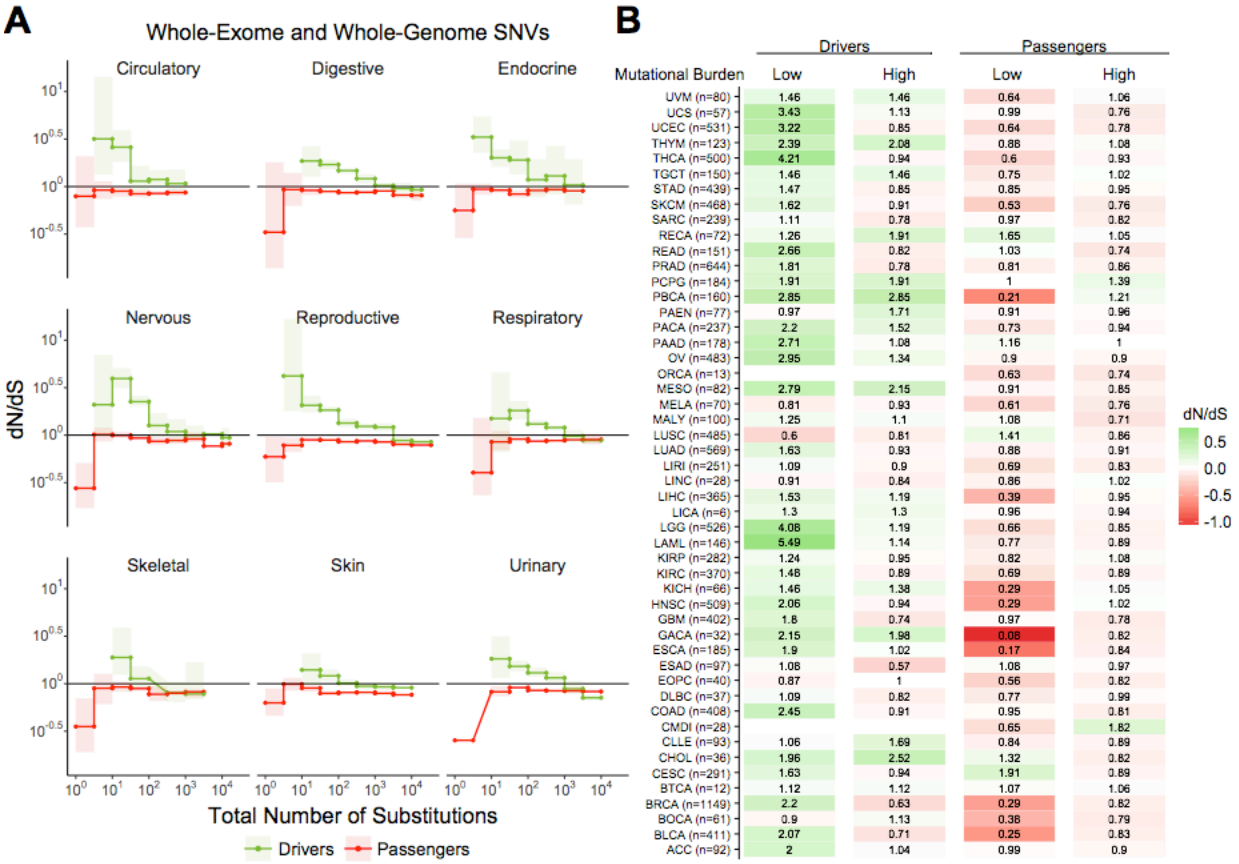
Supplemental Figure 9. Breakpoint frequency of CNAs within exomic regions (dE) relative to intergenic regions (dI) exhibits similar patterns of selection as Fractional Overlap. Calculations of breakpoint frequency[32] of exomic regions (dE) to intergenic (dI) regions within passenger and GISTIC[11] driver gene sets in tumors stratified by the total number of CNAs present. dE/dI is shown separately for CNAs greater than 100Kb in length (right) and smaller than 100Kb in length (left). Solid black line of 1 denotes values expected under neutrality. Error bars are 95% confidence intervals determined by bootstrap sampling.



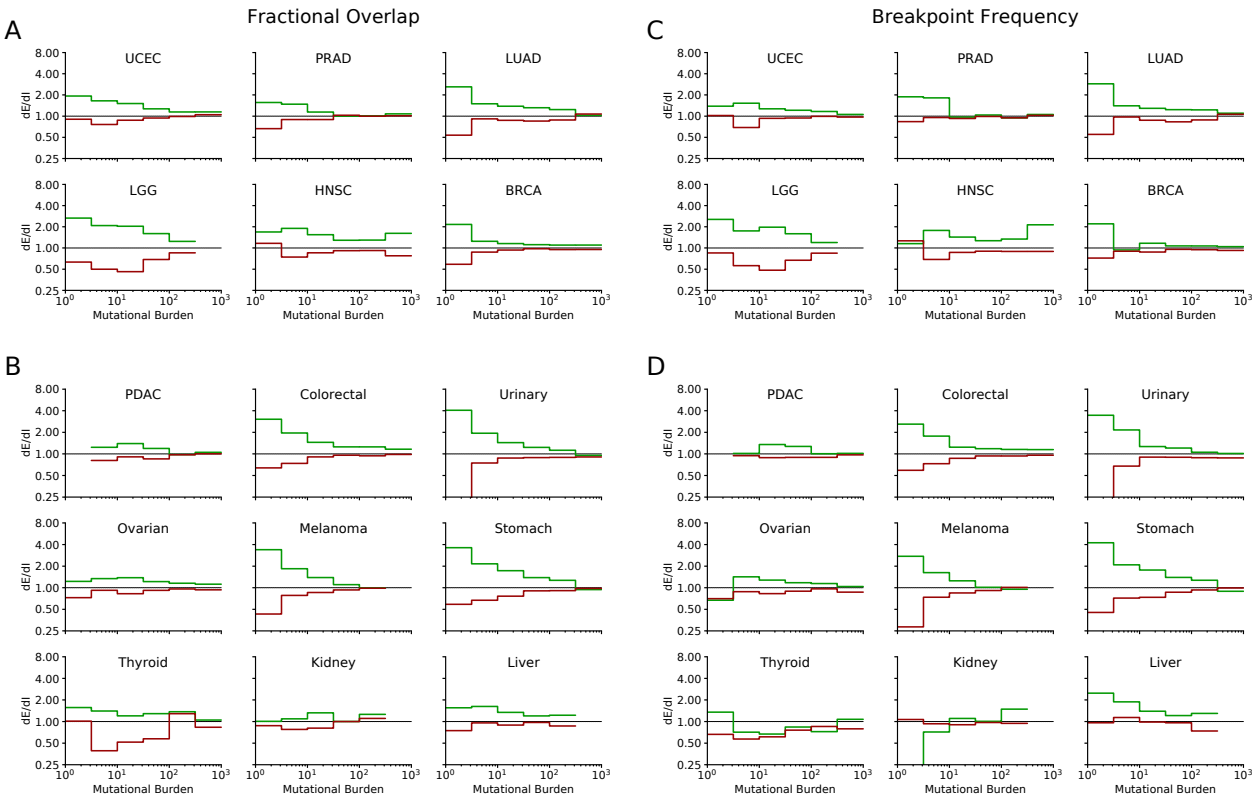
Supplemental Figure 10. Signal of negative selection in subclonal mutations are robust to VAF threshold. dN/dS calculations within clonal and subclonal passenger and driver gene sets within tumors in TCGA stratified by the total number of substitutions. Title of each graph corresponds to increasing VAF threshold value used to define 'subclonal' (e.g. mutations with a VAF > 0.2 are clonal; mutations with a VAF < 0.2 are subclonal). Darker colors denote clonal passengers and drivers, while lighter colors denote subclonal passengers and drivers. Solid line of 1 is shown of dN/dS values expected under neutrality. Error bars are 95% confidence intervals determined by bootstrap sampling.



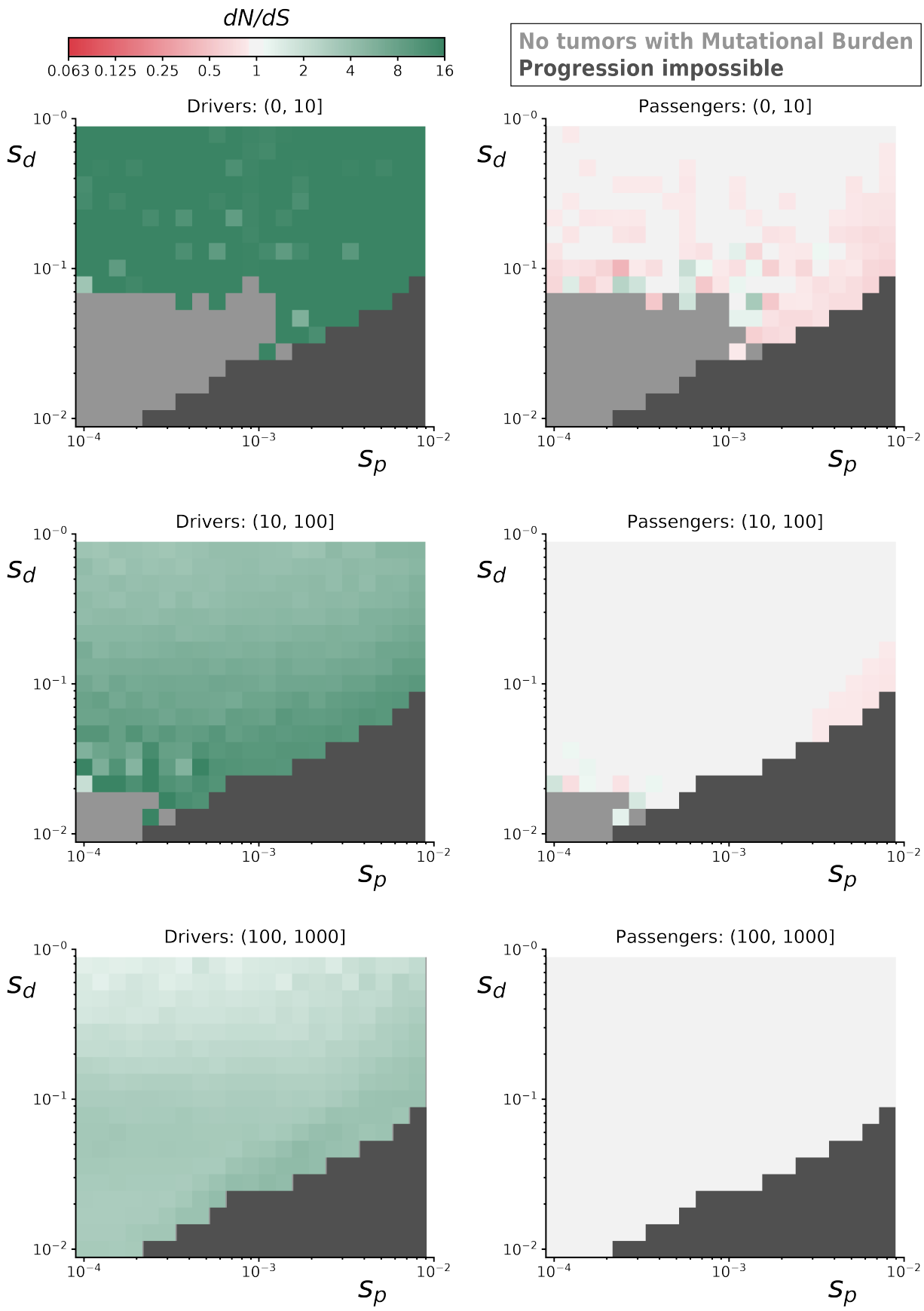
Supplemental Figure 11. Attenuation of negative selection within different functional gene sets. dN/dS of passengers within different functional gene sets in low and high mutational burden tumors ($d_N + d_S < 10$ for low, grey; dn + ds > 10 for high, black). Both TCGA and ICGC genomic data were used. Dotted line denotes genome-wide dN/dS of passengers for all mutation rates. Error bars are 95% confidence intervals determined by bootstrap sampling. Patterns of negative selection are not specific to any particular functional category (e.g. Essential or Housekeeping genes).



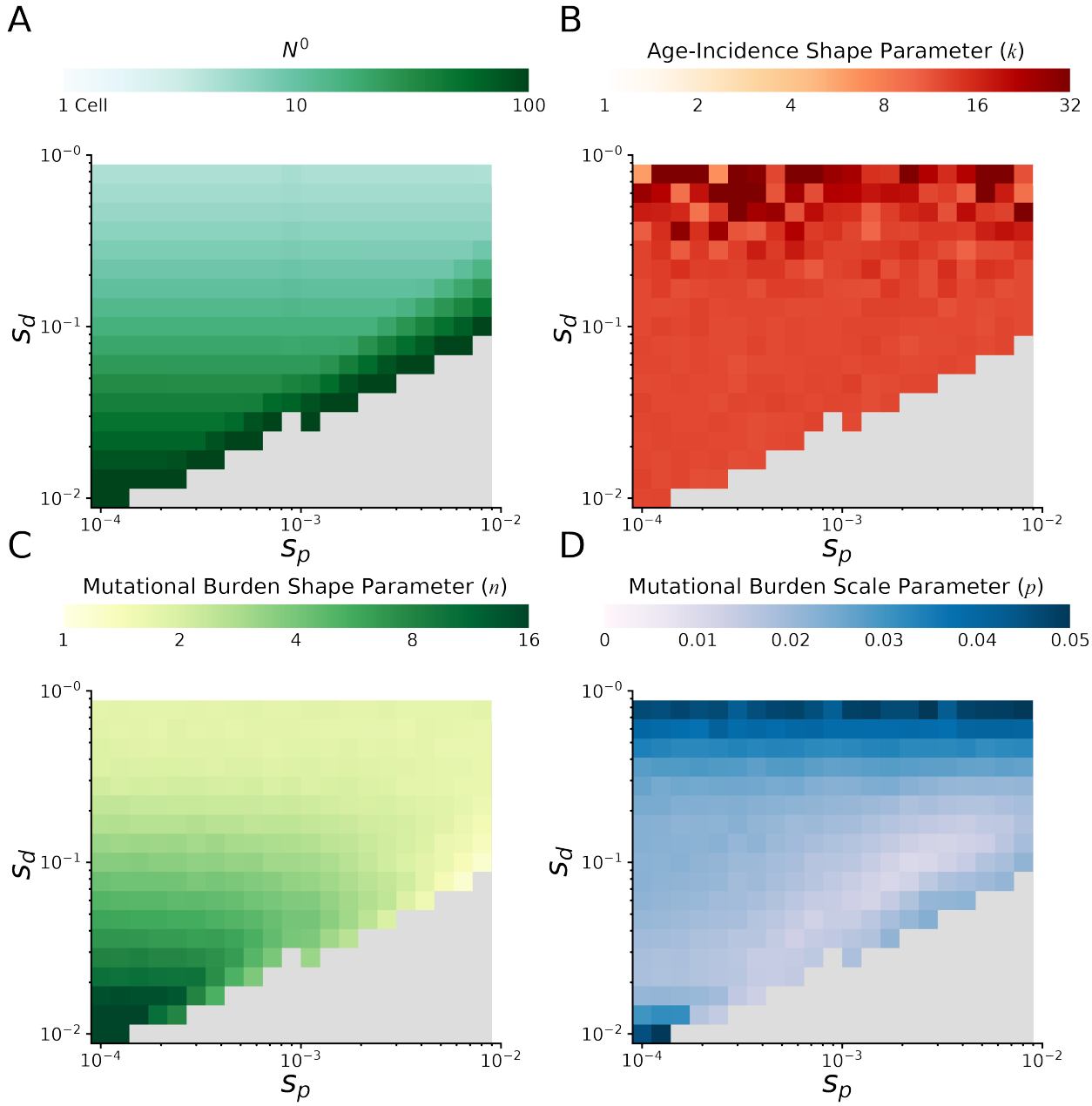
Supplemental Figure 12. Attenuation of selection in SNVs persists across cancer subtypes and broad cancer group categories. (A) dN/dS in passenger and driver gene sets within tumors stratified by the total number of substitutions in broad tumor subcategories. Error bars are 95% confidence intervals determined by bootstrap sampling. **(B)** Log-scale heatmap of dN/dS values in passenger and driver gene sets of tumors stratified by the total number of substitutions within all 50 cancer subtypes in ICGC and TCGA. dN/dS of the lowest and highest mutational burden bin for each cancer subtype are shown.



Supplemental Figure 13. Attenuation of selection in CNAs is robust to cancer subtypes and broad cancer group categories. (A) Normalized fractional overlap (dE/dI) of driver (green) and passenger (red) Copy Number Alterations (CNAs) with the human exome for the six most commonly-sequenced cancer subtypes (presented in Fig. 2). dE/dI > 1 suggests positive selection, while dE/dI < 1 suggests negative selection. Tumors are stratified by Mutational Burden (Total CNAs). **(B)** Same as in **(A)** for cancer subtypes with >200 genotyped samples that were not presented above (nine subtypes). **(C-D)** dE/dI of normalized breakpoint frequency stratified by Mutational Burden and segregated by cancer subtype. Subtype groupings are same as **(A-B)**. In general, both dE/dI measures exhibit positive selection on drivers that attenuates with mutational burden as well as negative selection on passengers that also attenuates with mutational burden across tumor subtypes. However, several exceptions are evident – especially for less-sequenced subtypes (bottom row of B & D).

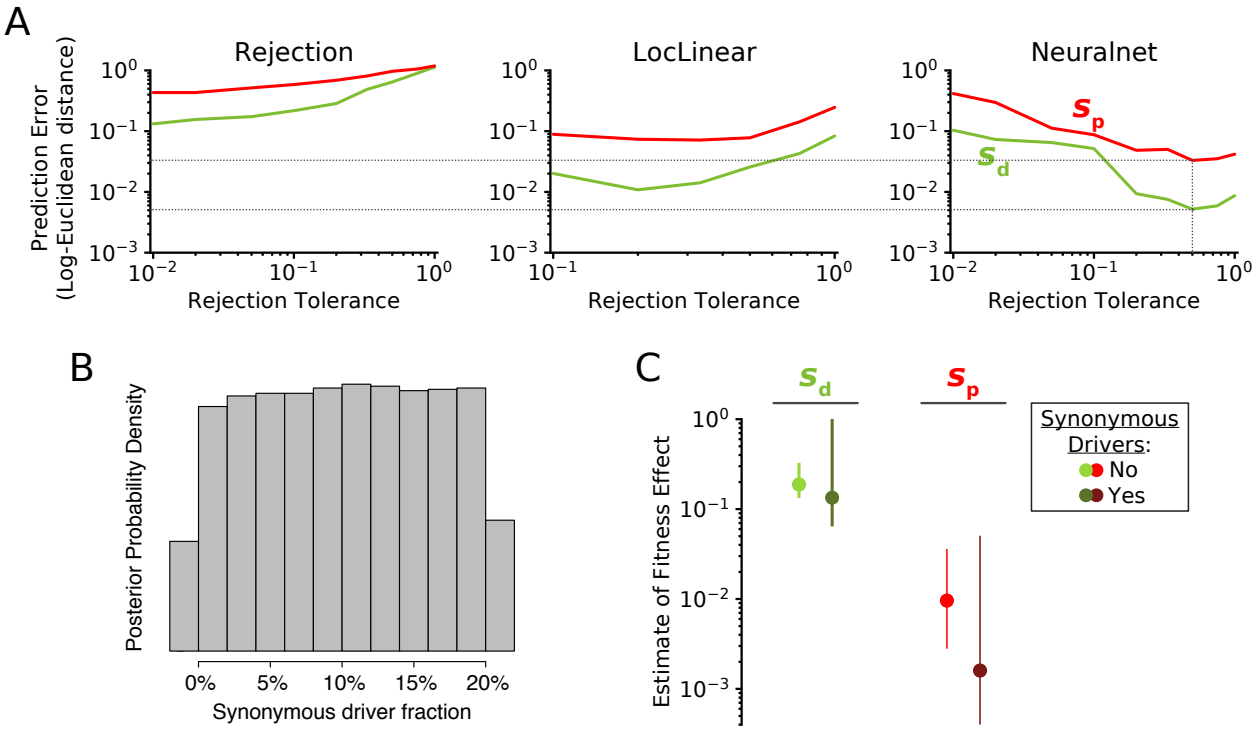

dN/dS
0.063 0.125 0.25 0.5 1 2 4 8 16
No tumors with Mutational Burden
Progression impossible
Drivers: (0, 10]
Passengers: (0, 10]
Drivers: (10, 100]
Passengers: (10, 100]
Drivers: (100, 1000]
Passengers: (100, 1000]
s_d
s_p
10^{-0}
10^{-1}
10^{-2}
10^{-4}
10^{-3}
10^{-2}

Supplemental Figure 14. dN/dS rates of drivers and passengers in simulated cancers with various fitness coefficients. 10,000 simulated tumors were generated for various combinations of mean driver fitness benefits (s_d) and mean passenger fitness costs (s_p, Methods). For some parameter combinations, the combined fitness cost of passengers overwhelmed the fitness benefit of drivers and prevented cancer progression within 100 years (dark grey). dN/dS values of simulated mutations were calculated for drivers (left) and passengers (right) at various mutational burden (Total number of nonysnonymous and synonymous mutations). Top row is a mutational burden of 1 – 10 ; middle row is 11 – 100, and bottom row is 100 – 1,000. Some parameter combinations did not produce any tumors with low mutational burdens (light grey). Across all parameters, positive selction on drivers and negative selection against passengers attenuates with mutational burden. Passengers exhibit minimial negative selection in general, despite a collective burden that often prevented tumor progression, because of strong Hill-Roberston interference in asexual populations.

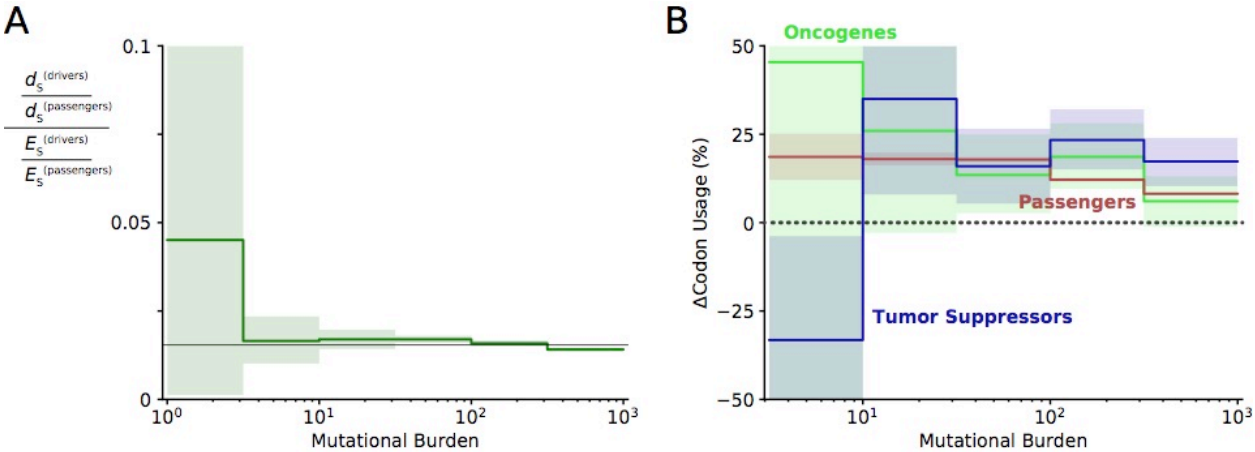


Supplementary Figure 15. Probability of cancer by age and mutational burdens in simulated cancers at various fitness coefficients. Clinical summary statistical of simulated tumors at various combinations of mean driver fitness benefits (s_d) and mean passenger fitness costs (s_p, Methods). **(A)** Initial population size N^0 of simulated tumors. Initial population size approximates the equilibrium population size of a tumor following an initiating driver. Large population sizes are necessary for tumor progression when passenger deleteriousness is large compared to driver advantageousness – otherwise natural selection cannot drive carcinogenesis. Eventually, tumor progression is not possible for any reasonable initial population size (grey area). **(B)** MLE of Gamma distribution shape parameters describing the cancer age-inicidence rates of simulated

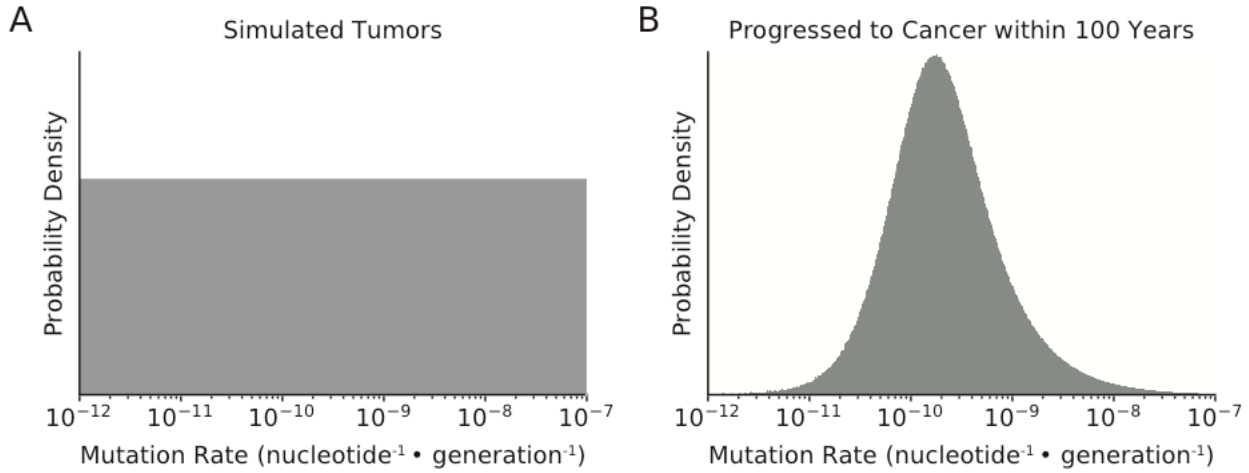
tumors. A Gamma distribution of age-incidence is expected from the Armitage-Doll multistage model of tumorigenesis and describes human age-incidence rates well (Methods)[26]. Larger values correspond to a steeper increase in rate with age; human patient rates are ~5 pan-cancer. Scale parameter of the parametric fit is not informative because of a Gauge freedom in the model. **(C)** MLE of shape and **(D)** scale parameters of Negative Binomial distributions describing the mutational burdens of simulated tumors. Smaller values of shape parameter correspond to broader distributions of mutational burden; human tumors exhibit a value of ~2 pan-cancer. Smaller values of scale parameter correspond to a larger mean mutational burden; human tumors exhibit a value of ~1/50 (i.e. 50 passengers per rate-limiting driver).



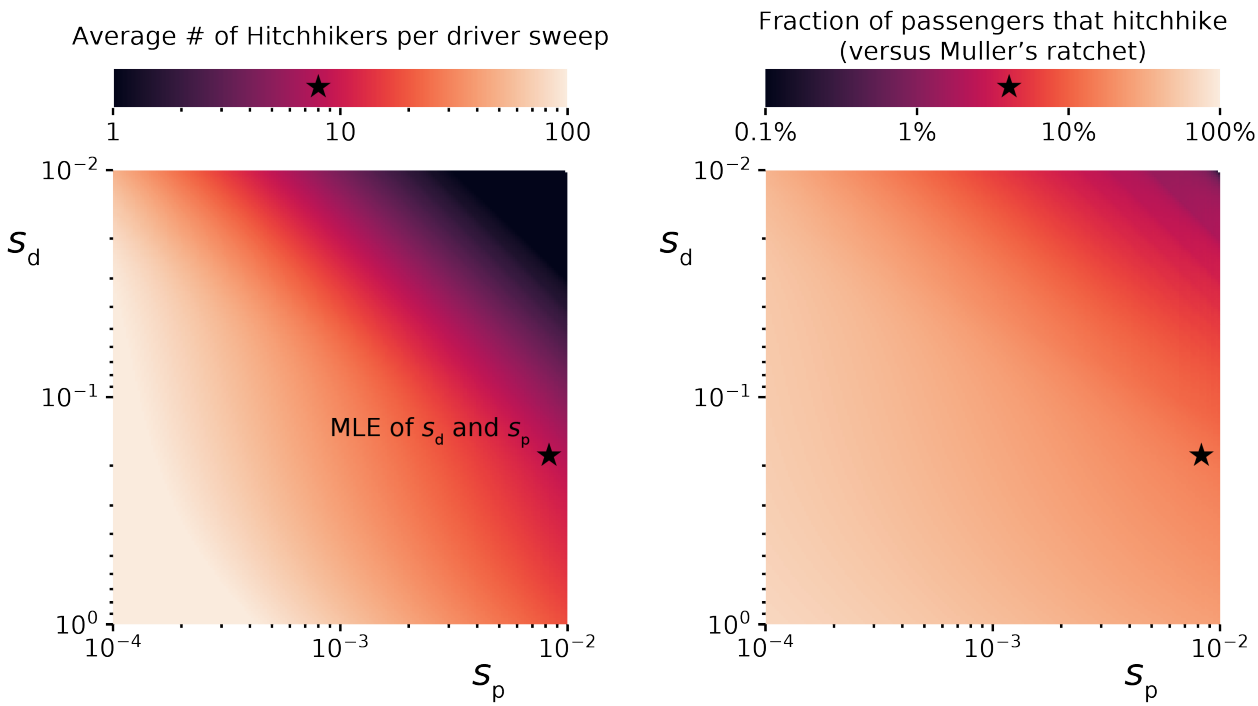
Supplementary Figure 16. Implementation and use of ABC for model selection and parameter estimation. (A) Leave-one-out Cross Validation (CV) on the simulated data was used to select an optimal Rejection Tolerance and optimal rejection method. Observed data can be compared to simulated data using model rejection alone (left), or by comparing observed data to a (middle) local-linear regression or (right) Feed-Forward Neural Network (1-layer) model trained on the simulated data. Training a machine learning model on simulated data (before comparison to observed data) often improves the performance of ABC by smoothing-out stochasticity in the summary statistics of simulations. A neural network with a rejection tolerance of 0.5 was used because it minimized prediction error of both driver and passenger fitness effects in the simulated data (illustrated by dotted lines). This Cross Validation approach to implement ABC is advised[29]. **(B)** Posterior probability of models of tumor evolution incorporating synonymous drivers. The prior distribution of synonymous driver fractions (uniform from 0% to 20%) is nearly-identical to this posterior distribution. This suggests that nearly all models incorporation synonymous drivers can explained observed dN/dS patterns in humans, if the right combination of driver fitness benefits (s_d) and passenger fitness costs (s_p) are chosen. **(C)** Posterior distribution of fitness effect of driver fitness benefits (s_d) and passenger fitness costs (s_p) after synonymous drivers are incorporated. MLE (circles) and 95% Confidence Intervals (lines) are reported. Similar to (B), incorporation of synonymous drivers undermines the ability of ABC to accurately infer the fitness effects of drivers and passengers.



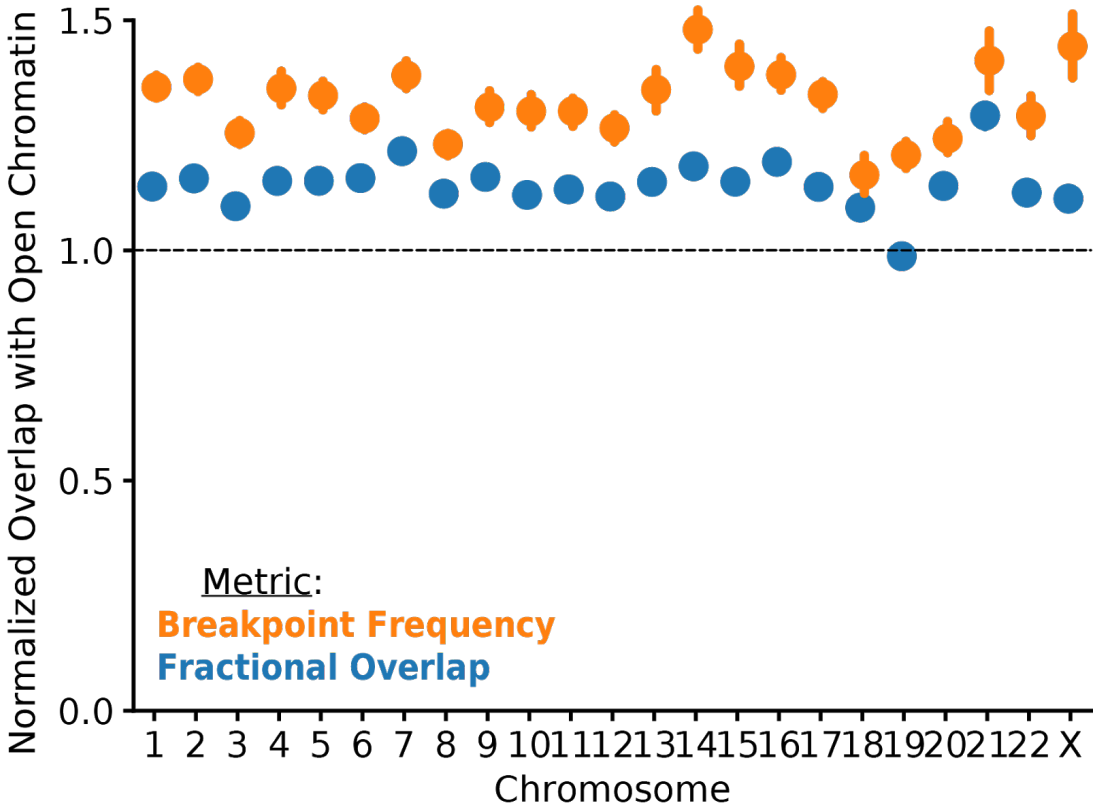
Supplementary Figure 17. Evidence of positive selection on synonymous mutations within driver genes at low mutational burdens. (A) The quantity of synonymous mutations within driver genes was compared to the quantity of synonymous mutations within passenger genes and both were normalized by their expected frequencies using dNdScv. Black line denotes the genome-wide ratio of synonymous drivers to synonymous passengers (~2%, i.e. driver genes are ~2% of the human coding genome). At low mutational burdens, a non-significant increase in the quantity of synonymous drivers is observed, suggestive of positive selection for these mutations. **(B)** The change in codon usage imparted by all synonymous mutations was calculated for oncogenes, tumor suppressors, and passenger genes. Bias in codon usage suggests a functional effect of synonymous mutations. Increase in codon usage is expected to increase translational efficiency and increase protein abundance. Oncogenes are expected to exhibit positive selection for increased codon usage and exhibit a non-significant increase as mutational burden declines – consistent with positive selection for synonymous mutations within oncogeneic drivers that is attenuated by Hill-Robertson interference. Similarly, tumor suppressors are expected to exhibit a decrease in codon usage at low mutational burdens, which is indeed significant (p = 0.03) presumably because there are more annotated tumor suppressor genes.



Supplementary Figure 18. Distribution of Mutation Rates of simulated tumors. (A) Mutation rates of all simulated tumors were randomly-sampled from a uniform distribution (in log-space) from 10^{-12} to 10^{-7} nucleotide^{-1} • generation^{-1}. **(B)** In simulations that best agreed with observed data (MLE of s_d = 18.8%, s_p = 0.96%), only tumors with intermediate mutation rates progressed to cancer within 100 years. Tumors with lower mutation rates do not progress to cancer within the 100-year time constraint of simulations, while tumors with exceptionally high mutation rates collapse via mutational meltdown.



Supplemental Figure 19. Relative contribution of Genetic Hitchhiking and Muller's Ratchet to fix deleterious passengers. Using analytical theory developed in [22,33,34], we can estimate the relative rates of genetic hitchhiking and Muller's Ratchet in our pan-cancer model of tumor evolution. As the relative strength of driver alterations increase (s_d) relative to the selective cost of passengers (s_p), more passengers hitchhike with each driver sweep (left). This increases the relative contribution of observed passengers that accumulate via hitchhiking (right). Using the Maximum Likelihood Estimates (MLE) of selection for drivers and against passengers, we estimate that an average of 8 passengers hitchhike with each driver, which account for 5.0% of accumulated passengers (the majority, and remainder, accumulate via Muller's Ratchet).



Supplemental Figure 20. Overlap of CNAs with open chromatin region of the genome. We determined the overlap of all CNAs with open chromatin regions (ATAC-seq peaks) of the genome (Methods). Overlap was normalized as described for other genomic tracks (e.g. drivers, passengers). CNA breakpoints appear to be enriched in open chromatin regions of the genome suggesting that these regions of chromosomes are fragile. This elevated overlap may slightly bias dE/dI estimates towards positive selection.

Supplementary Tables

Table S1. Broad (meta-categories) of cancer subtypes.

BROAD CATEGORY	GDC TUMOR SUBTYPES IN GROUP
Circulatory (n=371)	LAML, DLBC, CLLE, CMDI, MALY
Endocrine (n=925)	ACC, THYM, THCA, PAEN, PCPG
Urinary (n=1199)	BLCA, KICH, KIRC, RECA
Nervous (n=1059)	LGG, GBM, PBCA
Reproductive (n=3328)	BRCA, CESC, EOPC, OV, PRAD, UCEC, TGCT, UCS
Respiratory (n= 1557)	LUSC, LUAD, HNSC
Skeletal (n=378)	SARC, BOCA, MESO
Digestive (n=2181)	ORCA, LIRI, PAAD, STAD, READ, CHOL, COAD, ESCA, GACA, LINC, ESAD, BTCA, LIHC
Skin (n=614)	UVM, SKCM, MELA

Table S2. Assumptions of model of tumor evolution and anticipated effects

ASSUMPTION	ANTICIPATED EFFECT ON CONCLUSIONS	REFERENCES
Exponential DFE for drivers & passengers	ABC estimates e*ffective* selection coefficients	[35]
Cells are well-mixed (no spatial structure)	Reduced Hill-Robertson interference	[36–38]
Gompertzian growth dynamics in-between drivers	Decreased inferred strength of drivers relative to no growth constraints	[22]
Only 50% of tumors progress to cancer	Mutational burdens widen as progression probability declines	[22]
No (reciprocal) sign epistasis	Stronger fitness benefits of drivers in adaptive contexts	[39,40]
Constant mutation rate for each tumor	Hill-Robertson interference would increase	[41]
Simulated tumor is genotyped at transformation	Late (subclonal) mutations are ignored; incidence age reduced	[38]

References

1. Ellrott, K. *et al.* Scalable Open Science Approach for Mutation Calling of Tumor Exomes Using Multiple Genomic Pipelines. *Cell Syst.* **6**, 271-281.e7 (2018).
2. Zhang, J. *et al.* International Cancer Genome Consortium Data Portal--a one-stop shop for cancer genomics data. *Database* **2011**, bar026–bar026 (2011).
3. Auton, A. *et al.* A global reference for human genetic variation. *Nature* **526**, 68–74 (2015).
4. Wang, K., Li, M. & Hakonarson, H. ANNOVAR: functional annotation of genetic variants from high-throughput sequencing data. *Nucleic Acids Res.* **38**, e164–e164 (2010).
5. Forbes, S. a *et al.* The Catalogue of Somatic Mutations in Cancer (COSMIC). *Curr Protoc Hum Genet* **Chapter 10**, Unit 10.11 (2008).
6. Cibulskis, K. *et al.* Sensitive detection of somatic point mutations in impure and heterogeneous cancer samples. *Nat. Biotechnol.* **31**, 213–219 (2013).
7. Campbell, P. & Martincorena, I. dNdScv. *Welcome Sanger Institute* (2017). Available at: https://www.sanger.ac.uk/science/tools/dndscv.
8. Martincorena, I. *et al.* Universal Patterns of Selection in Cancer and Somatic Tissues. *Cell* **171**, 1029-1041.e21 (2017).
9. Bailey, M. H. *et al.* Comprehensive Characterization of Cancer Driver Genes and Mutations. *Cell* **173**, 371-385.e18 (2018).
10. Gonzalez-Perez, A. *et al.* IntOGen-mutations identifies cancer drivers across tumor types. *Nat. Methods* **10**, 1081–1082 (2013).
11. Mermel, C. H. *et al.* GISTIC2.0 facilitates sensitive and confident localization of the targets of focal somatic copy-number alteration in human cancers. *Genome Biol* **12**, R41 (2011).
12. Grossman, R. L. *et al.* Toward a Shared Vision for Cancer Genomic Data. *N. Engl. J. Med.* **375**, 1109–1112 (2016).
13. Carter, S. L. *et al.* Absolute quantification of somatic DNA alterations in human cancer. *Nat. Biotechnol.* **30**, 413–421 (2012).
14. Adzhubei, I. a *et al.* A method and server for predicting damaging missense mutations. *Nat. Methods* **7**, 248–9 (2010).
15. Gene Ontology Consortium. The Gene Ontology (GO) database and informatics resource. *Nucleic Acids Res.* **32**, 258D – 261 (2004).
16. Kumar, R. D., Searleman, A. C., Swamidass, S. J., Griffith, O. L. & Bose, R. Statistically identifying tumor suppressors and oncogenes from pan-cancer genome-sequencing data. *Bioinformatics* btv430 (2015). doi:10.1093/bioinformatics/btv430
17. Wang, T. *et al.* Identification and characterization of essential genes in the human genome. *Science (80-.).* **350**, 1096–1101 (2015).
18. Eisenberg, E. & Levanon, E. Y. Human housekeeping genes, revisited. *Trends Genet.* **29**, 569–74 (2013).
19. Calderone, A. & Cesareni, G. mentha: the interactome browser. *EMBnet.journal* **18**, 128 (2012).
20. Carithers, L. J. & Moore, H. M. The Genotype-Tissue Expression (GTEx) Project. *Biopreserv. Biobank.* **13**, 307–308 (2015).
21. Ha, G. *et al.* TITAN: inference of copy number architectures in clonal cell populations from tumor whole-genome sequence data. *Genome Res.* **24**, 1881–1893 (2014).
22. McFarland, C. D., Mirny, L. a & Korolev, K. S. Tug-of-war between driver and passenger mutations in cancer and other adaptive processes. *Proc. Natl. Acad. Sci.* **111**, 15138–15143 (2014).
23. McFarland, C. D., Korolev, K. S., Kryukov, G. V, Sunyaev, S. R. & Mirny, L. a. Impact of deleterious passenger mutations on cancer progression. *Proc. Natl. Acad. Sci.* **110**, 2910–2915 (2013).
24. Gibson, M. a. & Bruck, J. Efficient Exact Stochastic Simulation of Chemical Systems with Many Species and Many Channels. *J Phys Chem A* **104**, 1876–1889 (2000).
25. Turajlic, S. *et al.* Whole genome sequencing of matched primary and metastatic acral melanomas. *Genome Res.* **22**, 196–207 (2012).
26. Frank, S. A. *Dynamics of cancer: Incidence, Inheritance, and Evolution*. (2007).
27. Michor, F., Iwasa, Y., Lengauer, C. & Nowak, M. a. Dynamics of colorectal cancer. *Semin. Cancer Biol.* **15**,

484–493 (2005).
28. Howlader, N. *et al.* SEER Cancer Stastistics Review 1975-2010. *SEER Cancer Statistics Review, 1975-2010, National Cancer Institute.* (2013).
29. Csilléry, K., François, O. & Blum, M. G. B. abc: an R package for approximate Bayesian computation (ABC). *Methods Ecol. Evol.* **3**, 475–479 (2012).
30. Gelman, A. Parameterization and Bayesian Modeling. *J. Am. Stat. Assoc.* **99**, 537–545 (2004).
31. Futreal, P. A. *et al.* A census of human cancer genes. *Nat Rev Cancer* **4**, 177–183 (2004).
32. Korbel, J. O. *et al.* Systematic prediction and validation of breakpoints associated with copy-number variants in the human genome. *Proc. Natl. Acad. Sci.* **104**, 10110–10115 (2007).
33. Bachtrog, D. & Gordo, I. Adaptive evolution of asexual populations under Muller's ratchet. *Evolution (N. Y).* **58**, 1403–1413 (2004).
34. Neher, R. a & Shraiman, B. I. Fluctuations of fitness distributions and the rate of Muller's ratchet. *Genetics* **191**, 1283–1293 (2012).
35. Good, B. H., Rouzine, I. M., Balick, D. J., Hallatschek, O. & Desai, M. M. Distribution of fixed beneficial mutations and the rate of adaptation in asexual populations. *Proc Natl Acad Sci USA* **109**, 4950–4955 (2012).
36. Korolev, K. S. *et al.* Selective sweeps in growing microbial colonies. *Phys Biol* **9**, 26008 (2012).
37. Erik A. Martens, Rumen Kostadinov, Carlo C. Maley, and O. H. *et al.* Spatial structure increases the waiting time for cancer. *New J Phys* **13**, 1–25 (2012).
38. Sottoriva, A. *et al.* A Big Bang model of human colorectal tumor growth. *Nat. Genet.* **47**, 209–216 (2015).
39. Krug, J. Adaptation in tunably rugged fitness landscapes: The Rough Mount Fuji Model. 1–33 (2014).
40. Rogers, Z. N. *et al.* Mapping the in vivo fitness landscape of lung adenocarcinoma tumor suppression in mice. *Nat. Genet.* **50**, 483–486 (2018).
41. Goyal, S. *et al.* Dynamic mutation-selection balance as an evolutionary attractor. *Genetics* **191**, 1309–1319 (2012).