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1 **A cross-scale assessment of productivity-diversity** 2 **relationships**

3 **Running title:** Cross-scale diversity-productivity

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 41 improve analyses.

42 **Biosketch**

43 The authors are a group of (mostly) early career researchers united by their interest in ecological
 44 synthesis, in areas ranging from macroecology to experimental ecology, ecological theory, and ecological
 45 modeling.

46 **Data accessibility statement**

47 All data on species richness, biomass, NPP, covariates, and R code used for the data processing and
 48 analyses are available on Figshare (DOI: 10.6084/m9.figshare.5948155) under a CC-BY license.

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Abstract

Aim: Biodiversity and ecosystem productivity vary across the globe and considerable effort has been made to describe their relationships. Biodiversity-ecosystem functioning research has traditionally focused on how experimentally controlled species richness affects net primary productivity ($S \rightarrow NPP$) at small spatial grains. In contrast, the influence of productivity on richness ($NPP \rightarrow S$) has been explored at many grains in naturally assembled communities. Mismatches in spatial scale between approaches have fostered debate about the strength and direction of biodiversity-productivity relationships. Here we examine the direction and strength of productivity's influence on diversity ($NPP \rightarrow S$) and of diversity's influence on productivity ($S \rightarrow NPP$), and how this varies across spatial grains.

Location: contiguous USA

Time period: 1999 - 2015

Major taxa studied: woody species (angiosperms and gymnosperms)

Methods: Using data from North American forests at grains from local (672 m^2) to coarse spatial units (median area = $35,677 \text{ km}^2$), we assess relationships between diversity and productivity using structural equation and random forest models, while accounting for variation in climate, environmental heterogeneity, management, and forest age.

Results: We show that relationships between S and NPP strengthen with spatial grain. Within each grain, $S \rightarrow NPP$ and $NPP \rightarrow S$ have similar magnitudes, meaning that processes underlying $S \rightarrow NPP$ and $NPP \rightarrow S$ either operate simultaneously, or that one of them is real and the other is an artifact. At all spatial grains, S was one of the weakest predictors of forest productivity, which was largely driven by biomass, temperature, and forest management and age.

Main conclusions: We conclude that spatial grain mediates relationships between biodiversity and productivity in real-world ecosystems and that results supporting predictions from each approach

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76 (NPP → S and S → NPP) serve as an impetus for future studies testing underlying mechanisms.

77 Productivity-diversity relationships emerge at multiple spatial grains, which should widen the focus of

78 national and global policy and research to larger spatial grains.

79 **Keywords:** spatial grain, biomass, biodiversity-ecosystem function, climate, machine learning, species-
80 energy

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96 **Introduction**

97 One of the most prominent questions in ecology is how to describe relationships between biodiversity and
 98 ecosystem-level productivity (Currie, 1991; Rosenzweig, 1995; Mittelbach *et al.*, 2001; Balvanera *et al.*,
 99 2006; Adler *et al.*, 2011; Cardinale *et al.*, 2011, 2012; Hooper *et al.*, 2012; Naeem *et al.*, 2012; Tilman *et*
 100 *al.*, 2014). Two fields of research with different motives have tried to understand causality between these
 101 variables (Loreau *et al.*, 2001). The first examines how biodiversity varies across space as a result of
 102 different levels of productivity created by environmental variation (e.g., temperature, precipitation), and
 103 has resulted in a voluminous literature on the shapes of the patterns and their potential underlying
 104 causality (Connell & Orias, 1964; Currie, 1991; Rosenzweig, 1995; Waide *et al.*, 1999; Mittelbach *et al.*,
 105 2001; Adler *et al.*, 2011; Fraser *et al.*, 2015). The second aims to quantify changes in vital ecosystem
 106 functions such as productivity following anthropogenically-induced changes in diversity (Schulze &
 107 Mooney, 1993; Tilman, 1999; Cardinale *et al.*, 2012; Isbell *et al.*, 2017). As a result of the different
 108 perspectives on the direction of causality, there remains considerable debate and confusion surrounding
 109 the relationship between diversity and productivity (Grace *et al.*, 2016), which is exacerbated by differing
 110 spatial grains at which studies are conducted (Whittaker, 2010; Cardinale *et al.*, 2011).

111 Recently, there has been growing interest in assessing biodiversity ecosystem functioning (BEF)
 112 relationships in real-world, non-experimental ecosystems over large geographic extents, but likely due to
 113 logistical constraints, relationships are typically measured at local spatial grains (Liang *et al.*, 2016; Duffy
 114 *et al.*, 2017; van der Plas, 2019). Results suggest that the positive effect of species richness on
 115 productivity and other ecosystem functions can be as, or more, important than abiotic environmental
 116 drivers' effects on productivity, suggesting that diversity-productivity relationships can be even stronger
 117 in real-world communities than in controlled experiments (Duffy *et al.*, 2017). However, to fully
 118 understand the influence of diversity on productivity, and vice versa, it is critical to recognize that
 119 traditional bivariate analyses may underestimate the strength of these relationships by not accounting for
 120 the effects of spatial grain, as well as those of biomass, shading, macro-climate, and management (Loreau

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121 *et al.*, 2001; Cardinale *et al.*, 2009; Oberle *et al.*, 2009; Grace *et al.*, 2016).

122 The striking mismatch between the spatial grains of BEF experiments (cm² to m²; Cardinale *et al.*, 2011),
 123 observational studies of BEF (0.04 to 1.0 ha; Chisholm *et al.*, 2013; Liang *et al.*, 2016), and
 124 macroecological diversity-productivity correlations (m² to thousands of km²; Mittelbach *et al.*, 2001;
 125 Hawkins *et al.*, 2003; Field *et al.*, 2009; Adler *et al.*, 2011) further obscures comparisons between
 126 perspectives. However, there is a diverse array of theoretical expectations for grain dependency of the
 127 effects of productivity on diversity (NPP → S) and of diversity on productivity (S → NPP), which predict
 128 effects to either strengthen or weaken as the spatial grain increases (Table 1; Gonzalez *et al.*, 2020). For
 129 example, spatial turnover of species that are functionally equivalent within the regional grain can offset
 130 low species richness at local grains, resulting in a strengthening of S → NPP with increasing spatial grain.
 131 The effects of NPP → S are also hypothesized to increase with spatial grain, because higher NPP is
 132 associated with greater heterogeneity at larger spatial grains, which enhances coexistence of more species
 133 at the regional grain. Moreover, other components of a community, such as biomass, can mediate
 134 relationships between productivity and diversity via their effects on competitive dominance (Grace *et al.*,
 135 2016). These theoretical expectations have been supported by observational data for the effects of
 136 productivity on diversity (Mittelbach *et al.*, 2001; Chase & Leibold, 2002; Belmaker & Jetz, 2011). In the
 137 case of BEF relationships (i.e. S → NPP), there is also empirical and theoretical support for grain
 138 dependence, which comes from a restricted range of small spatial grains (Luo *et al.*; Chalcraft, 2013; Hao
 139 *et al.*, 2018).

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145 **Table. 1** Overview of hypotheses predicting grain dependence of relationships between net primary
146 productivity (NPP) and species richness (S).

No.	Direction	Mechanism of grain dependence	Weakens or strengthens towards coarse grain?	Reference
I	NPP → S and S → NPP	Spatially asynchronous demographic stochasticity impacts small populations (or small grains) and averages out over large grains.	Both NPP → S and S → NPP strengthen towards coarse grains	(Lande <i>et al.</i> , 2003)
II	NPP → S	At larger grains, higher NPP is associated with increased heterogeneity and/or dissimilarity of local patches, allowing for greater regional coexistence.	NPP → S strengthens towards coarse grains	(Abrams, 1988; Wright <i>et al.</i> , 1993; Chase & Leibold, 2002)
III	NPP → S	A statistical interaction between NPP and grain in their effect on S emerges as a consequence of increasing occupancy with NPP.	NPP → S weakens towards coarse grains	(Storch <i>et al.</i> , 2005)
IV	NPP → S	At very large grains (thousands of km ² and larger), high productivity increases occupancy and population size, thus increasing the probability of reproductive isolation and speciation	NPP → S strengthens towards coarse grains	(Jetz & Fine, 2012)
V	S → NPP	Stochastic sampling effects dominate at small grains, resource partitioning at larger grains ('spatial insurance'), and their relative magnitude determines the grain dependency.	Both strengthening or weakening possible	(Loreau <i>et al.</i> , 2003; Cardinale <i>et al.</i> , 2004)
VI	S → NPP	Functionally redundant species at intermediate or coarse grains can compensate for low richness at local grains.	S → NPP strengthens towards coarse grains	(Srivastava & Vellend, 2005)
VII	S → NPP	With incomplete compositional turn-over, proportional changes in larger-grain richness are always less than proportional changes in smaller-grain richness such that the explanatory power of richness on changes in functioning decreases with spatial scale.	S → NPP strengthens towards coarse grains until species richness saturates	(Thompson <i>et al.</i> , 2018)

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148 Here, we aim to address the dual nature by which productivity influences diversity (NPP → S) and
149 diversity influences productivity (S → NPP) across spatial grains by combining structural equation models
150 (SEM) and random forest models (RFs) to explicitly account for the bidirectionality of NPP → S and
151 S → NPP. Using SEM, we propose and test hypothesis-based models (Fig. S1) that estimate the direction
152 and strength of NPP → S and S → NPP. Next, we use RFs, an assumption-free machine learning approach
153 (Breiman, 2001; Hastie *et al.*, 2009), to quantify the relative importance of predictors of species richness
154 and productivity. We examine both hypothesized directions of the relationship, along with a number of
155 important covariates that influence both diversity and productivity, such as biomass, precipitation,
156 temperature, and forest age, using a comprehensive observational dataset of North American forests at

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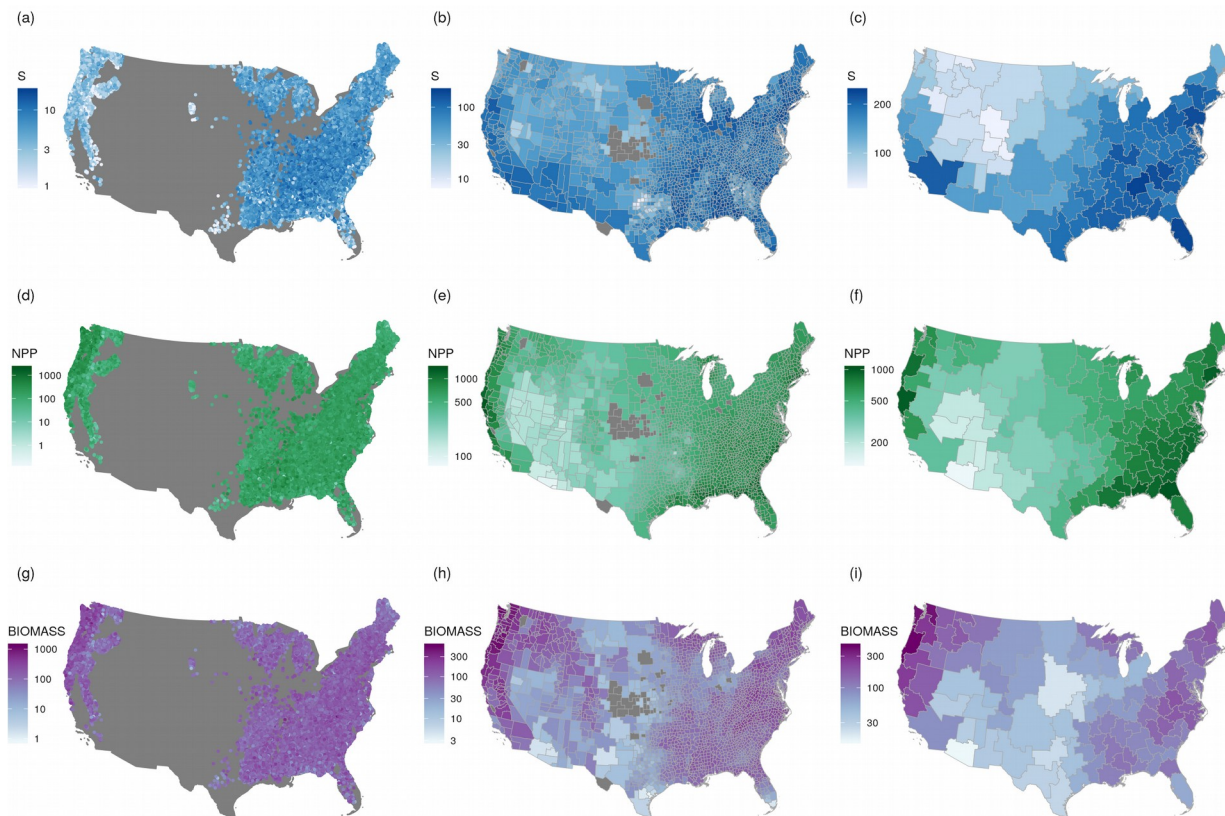
157 fine (area = 672 m²; n = 46,211 plots), medium (median area = 1,386 km²; n = 1,956 spatial units), and
 158 coarse spatial grains (median area = 35,677 km²; 98 spatial units). We specifically ask whether the
 159 influence of productivity on diversity (NPP → S) was stronger or weaker than the influence of diversity on
 160 productivity (S → NPP), and how these relationships manifest across grains in real-world ecosystems.

161 **Methods**

162 **Data**

163 **Geographic extent and grain.** We conducted analyses across the contiguous USA at three spatial grains
 164 (Fig. 1): (1) fine grain (46,211 plots, 672 m² or 0.000672 km² each), (2) intermediate grain (1,956 units,
 165 median 1,386 km²) created by aggregating US counties to larger units based on the forested area within
 166 them (see ‘spatial aggregation algorithm’ below), and (3) coarse grain (95 units, median 35,677 km²)
 167 created by further aggregating the intermediate grain units. We restricted our analyses to forested areas to
 168 make comparisons within and among spatial grains in similar ecosystems. For the intermediate and coarse
 169 grains, we defined an area as forested if it fell into a 1 km² pixel with non-zero forest biomass following
 170 Blackard *et al.* (2008).

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172 **Fig.1.** Maps of species richness (S), MODIS-derived net primary productivity (NPP) [gC/m²/year], and
173 biomass [Mg/ha] of forests at three spatial grains across the contiguous USA. The values in all plots are
174 on log₁₀ scale.

175 **Species richness (S).** For all spatial grains, we estimated diversity as species richness (S) because it is the
176 most commonly used and best understood metric of biodiversity, although other measures of diversity
177 may be better predictors of net primary productivity (Paquette & Messier, 2011; Cadotte, 2015; Venail *et*
178 *al.*, 2015). We extracted S at the fine spatial grain from the Forest Inventory and Analysis National
179 Program (FIA) database v. 1.7.0 (USDA Forest Service, 2017). We restricted our analysis to plots on
180 forested land that were sampled using the national FIA design (plot design code 1)(Burrill *et al.*, 2018).
181 All plots were surveyed between 1998 and 2016, each consisting of four circular 168 m² sub-plots with a
182 total area of 672 m² ha in which all individuals larger than 12.7 cm diameter at 1.3 m were recorded and
183 identified to species level. For each plot we pooled data from all subplots to estimate S. In total, our final
184 dataset included 344 woody species and 93,771 plots. We estimated S at the intermediate and coarse
185 spatial grains by counting the number of unique woody species in each spatial unit using data for the

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186 contiguous USA provided in The Biota of North America Program's (BONAP) North American Plant
187 Atlas (Kartesz, 2015).

188 **Taxonomic harmonization of species names.** We cleaned scientific names from the FIA and BONAP
189 datasets and harmonized them to accepted species based on The Plant List (2013) and the Taxonomic
190 Name Resolution Service (2018), following the protocol described in Meyer et al. (2016). We included
191 hybrid forms, but excluded any names that could not be resolved to the species level.

192 **Filtering of species occurrences.** We restricted our analyses to tree species that likely occur in forests.
193 At the fine spatial grain, we included native and alien species. At the intermediate and coarse spatial
194 grains, however, we excluded alien species because we could not be certain if they occurred in forests as
195 many are cultivated, particularly in urban ecosystems (Kowarik, 2008; Pearse *et al.*, 2018). We therefore
196 filtered the BONAP data to native species classified as 'trees' in BONAP's taxonomic query database
197 (Kartesz, 2015). We further filtered out 70 county-level occurrences of 5 non-woody species from the
198 BONAP dataset. Species woodiness was inferred from woodiness data (Zanne *et al.*, 2013) and species
199 lists of trees, shrubs and subshrubs (USDA NRCS, 2018), except for 37 species without such data for
200 which we instead inferred woodiness from online searches or assumed resemblance among congeneric
201 species. We also filtered out 8 FIA plot-level species occurrences and 1,595 BONAP county-level species
202 occurrences that we deemed unlikely to be forest occurrences, as inferred from independent species
203 occurrences within forested pixels recorded in FIA plots and Global Biodiversity Information Facility
204 (GBIF) point-occurrence records (Downloaded via <https://www.gbif.org/> on 26th September 2016;
205 doi:10.15468/dl.mka2y5; Supplementary Note 1). To make species richness data internally consistent
206 across the different spatial grains, we added a further 6,593 quality-vetted county-level forest occurrences
207 of woody species from FIA plot records to the 282,991 occurrences in the taxonomically harmonized
208 BONAP dataset.

209 **Net primary productivity (NPP).** At all spatial grains, we calculated NPP using MODIS-derived

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210 estimates, which we further supplemented with plot-derived estimates at the fine spatial grain. Briefly, we
 211 calculated NPP using the MODIS-derived MOD17 A3 product (Zhao *et al.*, 2005; Zhao & Running,
 212 2010), which gives annual values of NPP as $\text{gC m}^{-2} \text{yr}^{-1}$ in 30 arc-sec pixels (roughly 1 km^2 around the
 213 equator). Here, NPP is defined as the annual sum of daily net photosynthesis minus the cost of growth
 214 and maintenance of living cells in permanent woody tissue. We averaged the annual values from 2000 to
 215 2015 for each pixel, and then averaged these across the intermediate and coarse grains. We use MODIS-
 216 derived NPP in the analyses presented in the main text to ensure comparability across spatial grains.

217 At the fine spatial grain, we also estimated NPP using plot-derived data. For a large subset of plots in the
 218 FIA database that have been measured at least twice between 1999 and 2015 ($n = 46,211$, on average
 219 plots re-measured every 5.8 years), we calculated net annual net aboveground C change ($\text{gC m}^{-2} \text{y}^{-1}$). This
 220 was measured as the net change in aboveground tree C between two measurements as the sum of
 221 aboveground C growth of living trees, ingrowth by recruitment, and loss from tree mortality (NPPmort;
 222 Chen & Luo, 2015). Tree-level carbon was estimated by multiplying tree-level biomass (see below) by
 223 0.48, but we recognize that gymnosperms may have higher carbon content than that of angiosperms
 224 (Thomas & Martin, 2012). For plots with more than two inventories, tree productivity was calculated for
 225 each period and then averaged. NPPmort was weakly correlated with MODIS-derived NPP at the fine
 226 spatial grain ($r = 0.19$), suggesting that it may capture different processes. Therefore, we provide the
 227 analyses using the plot-derived NPP at the fine spatial grain in the Supplementary Information.
 228 Importantly, results concerning the strength of the S-NPP relationship were qualitatively similar for both
 229 NPP measures.

230 **Biomass (BIOMASS).** At all spatial grains, we derived biomass values using a map of aboveground
 231 forest biomass of the USA, which is derived by modeling FIA plot biomass as a function of geospatial
 232 predictor variables (Blackard *et al.*, 2008). This data layer had a grain of $250 \times 250 \text{ m}^2$, therefore, the
 233 average within each of the intermediate- and coarse-grain spatial units was taken.

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234 For analyses using plot-derived NPP, we estimated tree-level biomass at the fine spatial grain using
 235 generalized biomass equations developed for North American tree species (Chojnacky *et al.*, 2013). For
 236 each FIA plot we calculated aboveground biomass (Mg ha^{-1}) as the sum of individual biomass of living
 237 trees per hectare.

238 **Number of trees (N).** At the fine scale, we estimated the number of trees directly from each FIA plot. For
 239 the intermediate and coarse spatial grains, we estimated the number of trees using a global map of tree
 240 density (Crowther *et al.*, 2015). As the grain of the data layer was $1 \times 1 \text{ km}^2$, average tree density was
 241 calculated within each spatial unit at the intermediate and coarse spatial grains.

242 **Forest age (AGE) and management (MANAGED).** For each plot in the fine-scale dataset, we
 243 extracted forest age and management history from the FIA data set. Forest age is estimated using
 244 dendrochronological records (Burrill *et al.*, 2018). Management regime was a binary variable that
 245 indicated whether any forest management activity, e.g. harvest, thinning, tree planting, had been observed
 246 in any inventory or not.

247 At the intermediate and coarse grain, forest age was calculated as the average forest age from NASA
 248 NACP 1 km^2 resolution layer (Pan *et al.*, 2012). Management regime at the intermediate and coarse grains
 249 was calculated as the proportion of managed FIA plots within all FIA plots that were within each spatial
 250 unit.

251 **Climatic variables.** For all grains, we used WorldClim (Hijmans *et al.*, 2005) bioclimatic variables at 30
 252 sec resolution. Many of the WorldClim variables are strongly collinear with one another, or with other
 253 variables in the analysis (Table S1, Fig. S1). Thus, only three variables that captured different aspects of
 254 the climate were selected; mean annual temperature (BIO1; ANN.TEMP), mean precipitation (BIO12;
 255 ANN.PREC), and temperature seasonality (BIO4; TEMP.SEAS). At the fine scale, for each FIA plot we
 256 extracted the values of the 30 sec pixel in which the plot was found. For the intermediate and coarse
 257 grains, we averaged the values across all pixels within each spatial unit.

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258 **Elevation range (ELEV.RANGE).** We used elevation range as a proxy for topographic and habitat
 259 heterogeneity, a variable that has been shown to be a good predictor of species richness (Stein *et al.*,
 260 2014). The USGS SRTM1 dataset (USGS, 2009) with 1 sec (approx. 30 x 30 m²) resolution was used for
 261 all spatial grains. At the fine-scale, we calculated a 250 m diameter buffer around each FIA plot and
 262 calculated the elevation range using all 1 sec SRTM pixels within the buffer. At the intermediate and
 263 coarse scale, elevation range was calculated as the difference between the minimum and maximum
 264 elevation points within each spatial unit.

265 **Species pools (S.POOL).** We calculated regional species pools for each spatial grain as probabilistic
 266 dispersal pools (Karger *et al.*, 2016). For each intermediate-grain spatial unit and each species in our data
 267 set, we first estimated the species' probability of being part of the unit's species pool as the joint
 268 probabilities that dispersal might happen between that unit and any of the species' intermediate-grain
 269 occurrences within the contiguous US. Due to insufficient data on species' dispersal abilities, we assumed
 270 that dispersal probability between focal units and species' occurrences would decay with great-circle
 271 distance between the respective regions' centroids. We explored five alternative exponential distance-
 272 decay functions, with scaling coefficients P that determined the probability of a species occurring in
 273 neighboring units would disperse to the focal unit of 0.975, 0.95, 0.90, 0.80, and 0.60. We chose the
 274 function with $P = 0.8$, which exhibited the strongest correlation between species pool and species richness
 275 at all spatial grains (Fig. S2). Finally, we calculated species pools for each spatial unit as the sum of all
 276 species' individual probabilities of dispersal from any of their respective occurrences. For each coarse-
 277 grain unit, we summed the species' joint probabilities of dispersal between any of their intermediate-grain
 278 occurrences and any of the intermediate-grain units nested within the coarse unit. For fine-grain units, we
 279 assumed that their species pools would equal those of the intermediate-grain spatial units in which they
 280 were nested.

281 All of the variables used in our analyses are listed and summarized in Table S1 and visualized in Fig. S1.

Spatial aggregation algorithm. Because US counties vary dramatically in their area (Fig. S3), from Falls Church (VA) being as small as 5.1 km², to San Bernardino (CA) with 52,109 km², it is difficult to assign one categorical grain size to county-level data. Thus, we aggregated county data for species richness to create new spatial units, with the goal to minimize variation in forested area (A) between spatial units. We achieved this using a greedy algorithm which worked as follows: (1) Calculate variance (V_1) of forested area (A) across all counties. (2) Randomly select a focal county with a probability proportional to $1/\sqrt{A}$, which will most likely select counties with small A . (3) Randomly choose a county adjacent to the focal county and merge it with the focal county. (4) Update the variance (V_2) of forested area across all spatial units in the USA and compare it to the original variance V_1 . If the $V_2 < V_1$, the algorithm accepts the merged unit and returns to step one. If the variance does not decrease, the algorithm repeats step 3 until $V_2 < V_1$, with the maximum number of attempts of 1,000. If the variance still does not decrease even after 1,000 attempts, the algorithm rejects the merge, and returns to step one. The algorithm started with 3,107 counties, and we first terminated it when 1,956 merged spatial units were created. We classified these spatial units as the intermediate spatial grain (Fig. 1). We then allowed the algorithm to continue until it reached 98 merged spatial units, which we classified as the coarse spatial grain (Fig. 1). Although the algorithm substantially reduced variation in area within both spatial grains (Fig. S3), it did not eliminate the variation entirely. For this reason, we used area as a covariate in the statistical analyses at the intermediate and coarse spatial grains.

Stratified random sampling. Large areas of the contiguous US are environmentally homogeneous, while other parts are environmentally unique and small. We employed stratified random sampling (Cochran, 1977) for the fine and intermediate spatial grains in order to (1) enhance environmental representativeness of the data, (2) prevent excessive statistical leverage of the large number of data points from homogeneous areas and (3) reduce spatial pseudoreplication (autocorrelation) by increasing the geographic distance between data points. We first identified 11 strata at the fine and intermediate grains respectively, using multivariate regression trees with S, NPP and biomass as response variables and all

covariates as predictors (Fig. 1). We then took a random and proportionally sized sample of spatial units from each strata (fine grain, N = 1,000; intermediate grain, N = 500). We did not use stratified random sampling at the coarse spatial grain because of the small number of spatial units (N = 98). The spatial locations of the stratified samples are in Fig. S4. All of the analyses presented here, as well as our main conclusions, are based on these stratified sub-samples of the data.

Data transformation and standardization. Prior to analysis, species richness, biomass, N, NPP, and area were natural-log transformed to meet normality assumptions of the standardised major-axis regressions and SEMs.

Data Analyses

We quantified simple bivariate relationships between diversity and productivity for each spatial grain using standardised major-axis regression with the 'sma' function in the R package 'smatr' (Warton *et al.*, 2012). We then used two complementary statistical approaches to assess the impacts of diversity and productivity and vice versa while simultaneously accounting for covariates that influence both.

First, we fitted structural equation models (SEMs), which allow the assessment of indirect effects including feedback loops, address causality, and take into account potential collinearity among covariates (Grace *et al.*, 2010; Shipley, 2016). The paths in our candidate SEMs were based on previous evidence of causal links between S, biomass, and NPP (Fig. 2; Grace *et al.*, 2016). Second, to better understand the relative importance of each variable in explaining variation in the response variables within models, we fitted random forest models (RFs) (Hastie *et al.*, 2009). The results from SEMs provide insight into differences among models (i.e. between the two causal pathways per spatial grain, and among spatial grains), while results from RFs provide additional insights into the relative importance of different predictors variables within models.

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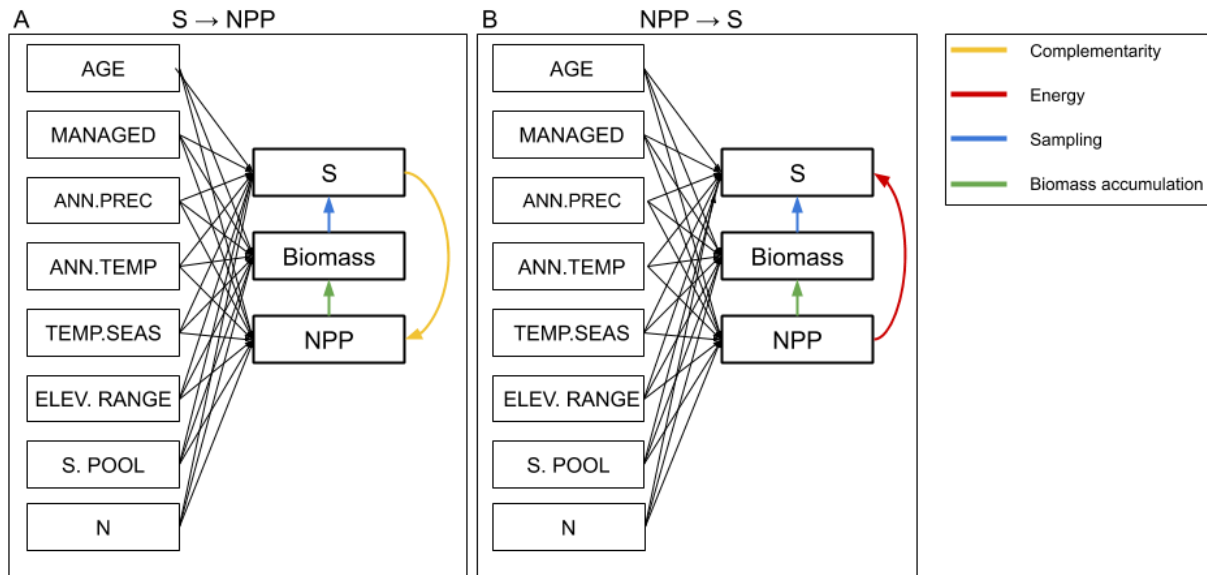


Fig. 2. Hypothetical causal models for structural equation models (SEM) testing the relative importance of species richness (S) on net primary productivity (NPP) ('S → NPP'; A) and NPP on S ('NPP → S'; B) in forests across the contiguous USA at three spatial grains. Paths in color represent possible ecological mechanisms influencing the direction of the relationship; yellow paths represent complementarity effects, red paths represent 'species-energy' relationships, blue paths represent sampling (or niche) effects and green paths represent biomass accumulation. Black paths are relationships of additional covariates with S, NPP, and BIOMASS and are not hypothesized to occur in a particular direction. AGE is forest age, MANAGED is forest management, ANN.PREC is mean annual precipitation, ANN.TEMP is mean annual temperature, TEMP.SEAS is temperature seasonality, ELEV.RANGE is elevation range, S.POOL is the regional species pool, and N is the number of individuals. At the intermediate and coarse spatial grains, we added AREA to the SEMs to account for differences in the area of spatial units. S, BIOMASS, NPP, and AREA were natural log transformed prior to analysis.

Structural Equation Modelling (SEM). To test the relative importance of S on NPP ('S → NPP') and NPP on S ('NPP → S') we fitted two SEMs per spatial grain. For each SEM, we started with a 'saturated' model, which included the relationships between S, NPP, and biomass, and relationships of all additional covariates on S, NPP, and biomass (except for area at the fine spatial grain) (Fig. 2). The S → NPP model evaluated how S directly affects NPP and how NPP indirectly affects S via biomass and, therefore, included a feedback loop. The NPP → S model tested the direct effect of NPP on richness and, unlike the S → NPP model, did not include a feedback loop. This way, we tested the direct effect of S on NPP (S → NPP model), the direct effect of NPP on S (NPP → S), and the indirect effect of NPP on S (included in both models).

Model fit can only be tested on unsaturated models, i.e. those that have at least one missing path.

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354 Therefore, we removed the path with the lowest standardized path coefficient from the model. As SEMs
 355 had an equal number of paths, we could compare model fit across all models within each spatial grain
 356 using their unadjusted R^2 values. After excluding the additional paths, path coefficients of S, NPP, and
 357 biomass remained qualitatively the same, and model fit to the data were still accepted (Chi-square test;
 358 $P > 0.05$). This indicates that the models are identifiable and their results are robust. Therefore, we did not
 359 further reduce the model, and models maintained the same number of paths within each scale. Because
 360 models at the fine spatial grain including the number of individuals (N) did not fit the data well ($P <$
 361 0.05), we excluded this variable. Models at the intermediate and coarse spatial grains including N fit the
 362 data well ($P > 0.05$), but we present models without N for consistency with the fine spatial grain and
 363 because the sampling effects captured by N are also captured by area.

364 To assess the differences among scales in the relationships between S, NPP and biomass for each model,
 365 we compared the standardized regression coefficients using their 95% confidence intervals. All SEMs
 366 were fitted using the ‘sem’ function of the ‘lavaan’ package in R (Rosseel, 2012).

367 **Random forest models (RFs).** To assess the relative importance of each variable in predicting the
 368 response variables within models, we used random forest models (RFs) (Breiman, 2001; Liaw & Wiener,
 369 2002; Hastie *et al.*, 2009). We used the ‘randomForest’ function in the R package ‘randomForest’, with
 370 all RF models produced using the default settings: 500 trees, one third of predictors sampled in each tree,
 371 sampling with replacement of the entire dataset, and terminal node size of 5.

372 At each of the three spatial grains we fitted two RFs, one with S as a response variable and the other with
 373 NPP as a response variable. All predictors that were used in the SEMs were used in the RF models
 374 (including biomass). To quantify the relative importance of each predictor, we calculated the mean
 375 decrease of squared error across all 500 trees using the ‘importance’ function. The importance values
 376 were then scaled between 0 and 1, with 1 being the most important predictor. Using the function
 377 ‘partialPlot’, we extracted the partial responses of S and NPP to visualize the relationship between the

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378 two variables after accounting for all other covariates.

379 **Non-linear responses and spatial autocorrelation.** SEMs offer the advantage of modelling complex,
 380 causal relationships (Grace *et al.*, 2010; Shipley, 2016), but they can be difficult to fit to data with non-
 381 linear responses or spatial pseudoreplication. While it is possible to model non-linearity in SEMs, e.g.
 382 using polynomials (Grace *et al.*, 2010; Shipley, 2016), this often comes at the cost of interpretability. A
 383 similar problem applies when it comes to another prevalent problem of observational geographic data:
 384 spatial autocorrelation, which statistical models have so far addressed by modelling it either in residuals,
 385 or in the response (Dormann *et al.*, 2007). However, because of the causal loop in the SEMs (Fig. 2), the
 386 key response variables are also predictors, which prevented us from estimating spatial autocorrelation. In
 387 our analyses, we account for these issues in the following manner: (1) In the SEM analyses, we keep the
 388 relationships linear, given the approximately linear pairwise relationships between the raw NPP, S and
 389 biomass data (Figs. S5-7). (2) In the SEM analyses we do not directly model spatial autocorrelation. (3)
 390 We address spatial autocorrelation in the random forest analysis by allowing the algorithm to model
 391 smooth geographic trends in the response (by including the X and Y spatial coordinates as predictors),
 392 and we measure spatial autocorrelation in the response and in residuals. (4) We allow the random forest
 393 analysis to detect non-linear responses.

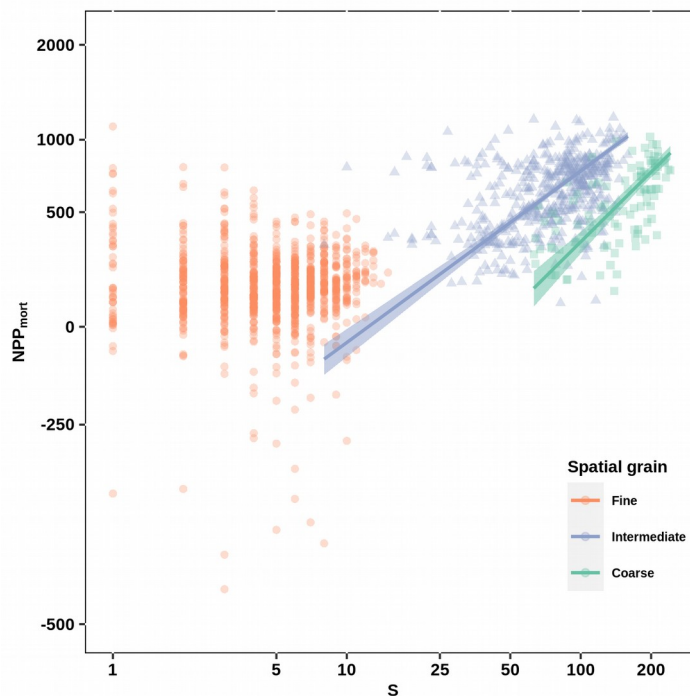
394 **Reproducibility.** All data on species richness, biomass, NPP, covariates, and R code used for the data
 395 processing and analyses are available on Figshare (DOI: 10.6084/m9.figshare.5948155) under a CC-BY
 396 license.

397 **Results**

398 Spatial patterns in productivity (NPP) and richness (S) emerged at coarser spatial grains, with higher S
 399 and NPP usually observed in the eastern USA than in the western USA (Fig. 1). Biomass, a time-
 400 integrated measure of NPP that also influences diversity, also exhibited similar patterns (Fig. 1). Bivariate
 401 relationships between S and NPP exhibited scale dependence (Fig. 3). While not significantly correlated

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402 at the fine spatial grain (standardised major axis regression: $R^2 = 0.00$, $P = 0.73$), S and NPP were
 403 significantly correlated at the intermediate (standardised major axis regression: $R^2 = 0.15$, $P < 0.001$) and
 404 coarse spatial grains (standardised major axis regression: $R^2 = 0.35$, $P < 0.001$). The slope of S-NPP
 405 increased from 0.86 (95% confidence intervals: 0.80, 0.94) at the intermediate spatial grain to 1.23 (95%
 406 confidence intervals: 1.05, 1.45) at the coarse spatial grain. Similar patterns were observed when using
 407 plot-derived estimates of NPP at the fine spatial grain (Fig. S8).



408

409 **Fig. 3.** Bivariate relationships between observed species richness (S) and productivity (NPP) of forests at
 410 three spatial grains across the contiguous USA. Solid lines are standardised major-axis regressions fitted
 411 at each spatial grain and shaded areas are 95% confidence intervals; only regressions with statistically
 412 significant slopes ($P < 0.05$) were visualised. NPP is MODIS-derived at all spatial grains. Note that axes
 413 are on the natural log scale. Analyses were performed using stratified random samples of 1000, 500 and
 414 98 spatial units at the fine, intermediate and coarse spatial grains, respectively.

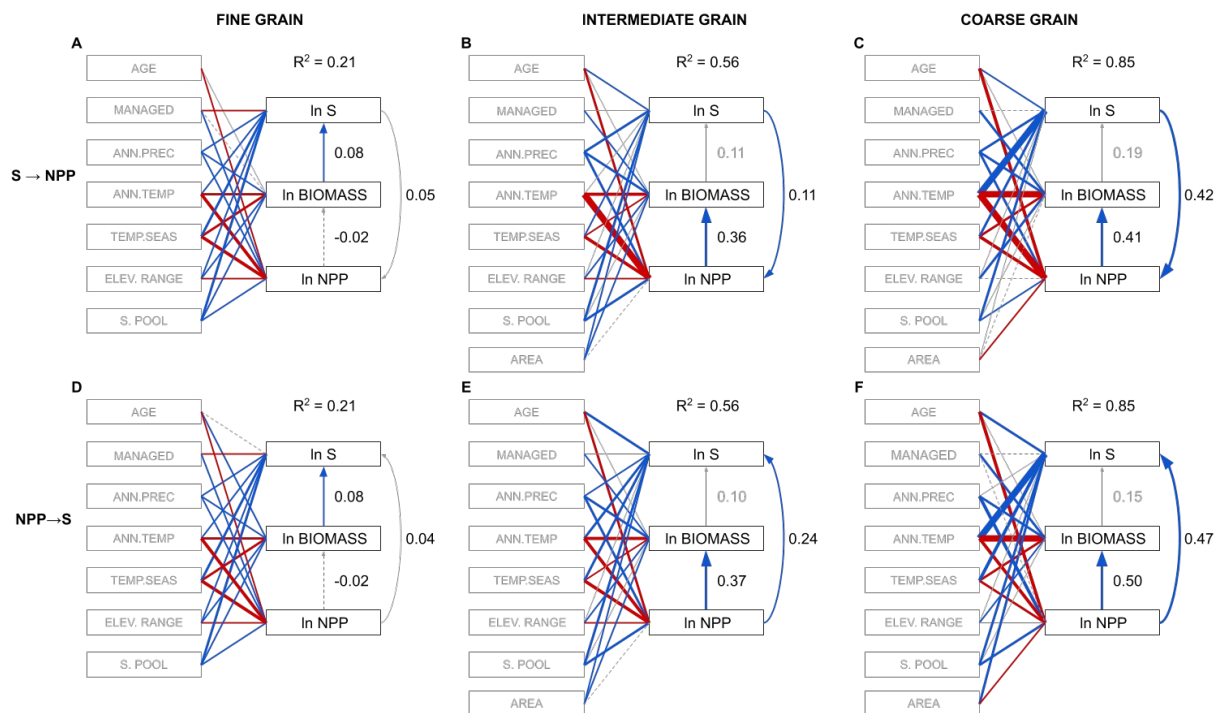
415

416 **Structural Equation Models (SEM).** We examined relationships between species richness and net
 417 primary productivity (NPP) across spatial grains using two SEMs for each spatial grain: the first
 418 ($S \rightarrow NPP$) testing the direct effect of S on NPP and the indirect effect of NPP on S (via biomass), and the

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second (NPP → S) testing both the direct and indirect effects of NPP on S (Fig. 4). In both SEMs, environmental variables (e.g., mean annual precipitation, mean annual temperature, temperature seasonality, and elevation range), size of the species pool, forest age, and management were used to explain variation in S, biomass, and NPP. At the intermediate and coarse grains, we also included area (of each spatial unit) to account for variation in species richness due to sampling effects.

424



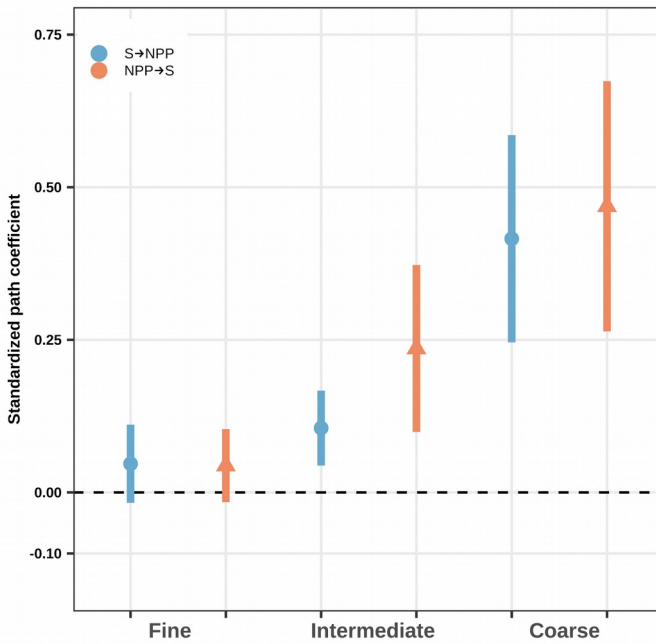
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Fig. 4. Structural equation models (SEM) testing the influence of diversity (S) on productivity (NPP) ('S → NPP'; A, B, C) and that of NPP on S ('NPP → S'; D, E, F), once controlling for environmental variables (e.g., mean annual precipitation, mean annual temperature, temperature seasonality, and elevation range), size of the species pool, forest age, and management, in forests across the contiguous USA at three spatial grains. All models fit the data well at all spatial grains (P-value of the Chi-square test > 0.1; Table S1). Boxes represent measured variables and arrows represent relationships among variables. Solid blue and red arrows represent significant (P < 0.05) positive and negative standardized path coefficients, respectively, and their width is scaled by the corresponding standardized path coefficient. Solid and dashed gray arrows represent non-significant (P > 0.05) positive and negative standardized path coefficients, respectively. R² is the average of R² values for S, BIOMASS, and NPP. NPP is MODIS-derived at all spatial grains. AGE is forest age, MANAGED is forest management, ANN.PREC is mean annual precipitation, ANN.TEMP is mean annual temperature, TEMP.SEAS is temperature seasonality, ELEV.RANGE is elevation range, S.POOL is the regional species pool, and AREA is area. S,

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439 BIOMASS, NPP, and AREA were natural log transformed prior to analysis.

440



441

442 **Fig. 5.** Direct effects of diversity on productivity ($S \rightarrow NPP$) and productivity on diversity ($NPP \rightarrow S$)
443 estimated with structural equation models (SEM) in forests across the contiguous USA at three spatial
444 grains. Points are standardized path coefficients and solid lines are 95% confidence intervals.

445

446 Both models fit the data well for all spatial grains (P-value of the Chi-square test > 0.1; Table S2). At
447 each spatial grain, both SEMs had similar R^2 values averaged over S, biomass and NPP, indicating a
448 similar fit of the model to the data. R^2 values for both SEMs increased with spatial grain, from 0.21 at the
449 fine grain, to 0.56 at the intermediate grain and 0.85 at the coarse grain. Generally, the strength of effects
450 of $S \rightarrow NPP$ and $NPP \rightarrow S$ were similar within each spatial grain, but both increased in strength with
451 increasing spatial grain (Figs. 4 & 5). At the fine spatial grain, we found a weak direct effect of $S \rightarrow NPP$
452 (Fig. 4A) and $NPP \rightarrow S$ (Fig. 4D), and effectively a null indirect effect of NPP on S via biomass
453 (standardized path coefficient of indirect effect = -0.002; Fig. 4A). At the intermediate spatial grain, we
454 found a similarly strong direct effect of S on NPP (standardized path coefficient of direct effect = 0.11,
455 Figs. 4B and 5) as NPP on S (standardized path coefficient of direct effect = 0.24; Figs. 4E and 5) and

43

456 weak indirect effects of NPP on S via biomass (standardized path coefficient of indirect effect = 0.04; Fig.
457 4B). Similarly at the coarse spatial grain, we found strong direct effects of S on NPP (0.42, Fig. 4C and 5)
458 and of NPP on S (0.47, Fig. 4F and 5) and weak indirect effects of NPP on S via biomass (standardized
459 path coefficient of indirect effect = 0.08; Fig. 4C).

460 Overall, the SEMs suggest that the productivity-diversity relationship increases in strength with spatial
461 grain, and both relationships ($S \rightarrow NPP$ and $NPP \rightarrow S$) explain similar amounts of variation. At all spatial
462 grains, our SEMs do not conclusively show stronger support for one direction of causality over the other.
463 Similar patterns were observed when using plot-derived estimates of NPP (Fig. S9; Table S2), except for
464 the direction of direct effects of S on NPP and NPP on S, which was negative.

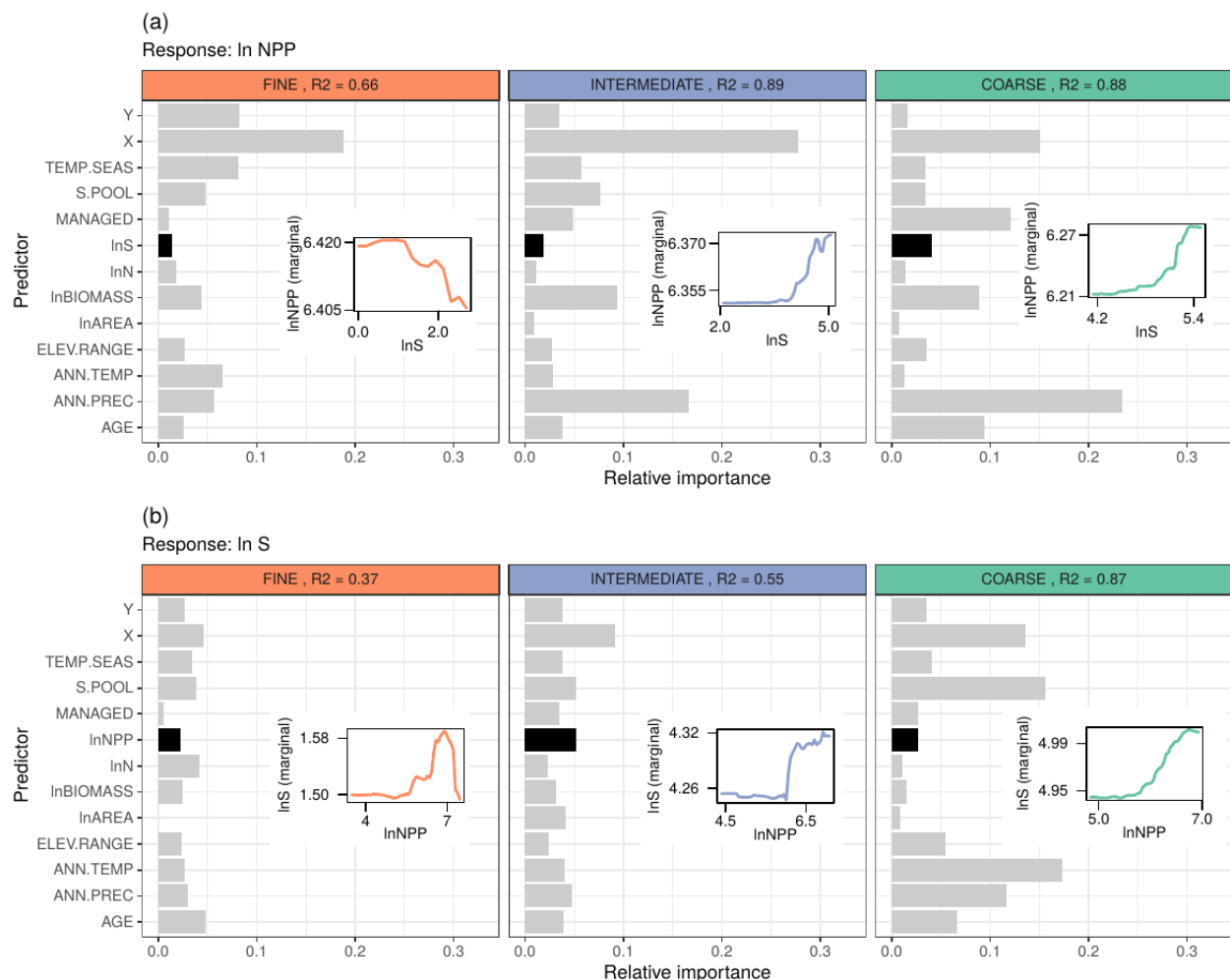
465 **Random forest models (RFs).** To assess the relative importance of each predictor of species richness and
466 NPP, and to provide an assumption-free alternative to the SEMs that also accounts for spatial
467 autocorrelation, we fitted two random forest models for each of the three spatial grains: one with NPP and
468 the other with S as response variables. We found that species richness was one of the weakest predictors
469 of NPP relative to other predictors at all spatial grains (Fig. 6A), with management, forest age, MAP, and
470 biomass being the most important predictors (Fig. 6A). The overall explained variation of NPP also
471 increased from the fine to the two coarser spatial grains, from 0.64 at the fine spatial, to 0.89 at the
472 intermediate spatial grain and 0.88 at the coarse spatial grain.

473 We found that NPP was an important predictor of S (with a positive effect) only at the intermediate
474 spatial grain (Fig. 6B), but was less important relative to other predictors at fine and coarse spatial grains.
475 For S, we found that species pool, mean annual temperature and precipitation, and forest age were the
476 best predictors, and their importance increased towards coarse spatial grains (Fig. 6). In line with the
477 SEM analyses, the overall explained variation of S increased towards coarse spatial grains, from 0.39 at
478 the fine grain to 0.55 at the intermediate and 0.87 at coarse grains (see Fig. S10 for predicted vs. observed
479 values).

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480 In all RF analyses, there is a clear East-West spatial component in both S and NPP (represented by the X
481 coordinate in Fig. 6), which was not explained by any of the other predictors. This spatial component was
482 stronger for NPP than for S. Residual autocorrelation in all of the RF models was negligible (Fig S11).
483 Finally, we also fitted all of the RFs with local plot-derived measures of productivity (as an alternative to
484 the MODIS-derived productivity used in the main analyses), showing that the strength of the S-NPP
485 relationships were similar across all NPP measures (Fig. S12).

486



487 **Fig. 6.** Relative variable importance from random forest models explaining (a) MODIS-derived NPP and
488 (b) species richness (S) at three spatial grains. Relative variable importance is the mean decrease in
489 squared error caused by each of the variables, rescaled such that it sums up to the total pseudo R² of the
490 whole random forest model. The curves in the insets show shapes of the marginal responses of ln NPP or
491 ln S after accounting for all of the covariates. Y and X are latitudinal and longitudinal coordinates of the
492 US National Atlas projection, TEMP.SEAS is temperature seasonality, S.POOL is the regional species
493 pool, MANAGED is forest management, lnNPP is MODIS-derived NPP, lnN is the number of

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495 individuals, $\ln \text{BIOMASS}$ is biomass, $\ln \text{AREA}$ is area of the spatial unit, ELEV.RANGE is elevation
496 range, ANN.TEMP is mean annual temperature, ANN.PREC is mean annual precipitation, and AGE is
497 forest age. For explanation of variables see Table S1.

498

499 Discussion

500 The first important result is the similar magnitude of the $S \rightarrow \text{NPP}$ (Grace *et al.*, 2016) and $\text{NPP} \rightarrow S$
501 (Mittelbach *et al.*, 2001; Hawkins *et al.*, 2003; Šímová *et al.*, 2011) relationships at all grains. This
502 reflects, in part, that both productivity and species richness have many environmental and geographical
503 drivers in common (Lavers & Field, 2006), which complicates distinguishing correlation from causation,
504 even when using SEMs (Grace *et al.*, 2010; Shipley, 2016). There are two possible interpretations of this
505 result: (i) it may indicate that diversity's causal effects on productivity and productivity's causal effects
506 on diversity operate simultaneously, which was suggested by (Grace *et al.*, 2016), but never demonstrated
507 on observational data from large spatial grains. Alternatively (ii), if only one direction of the diversity-
508 productivity relationship is real and causal, it may be possible to fit another model assuming the opposite
509 direction because of multicollinearity in the data or non-identifiability of the causal direction (Petersen &
510 van der Laan, 2014). Without large-grain experiments that manipulate diversity in ways that mimic
511 biodiversity change (i.e. species gains and losses) in real-world ecosystems (Loreau *et al.*, 2001; Wardle,
512 2016; Hillebrand *et al.*, 2018; Manning *et al.*, 2019; Gonzalez *et al.*, 2020), we see little hope for
513 resolving this with contemporary data and approaches.

514 Our second important result is that both $S \rightarrow \text{NPP}$ and $\text{NPP} \rightarrow S$ strengthen from the fine to the intermediate
515 grain, and in the case of the SEM both relationships continue strengthening towards the coarsest grain.

516 While grain-dependent shifts are often expected (Table 1), this had not been shown previously with
517 empirical data for $S \rightarrow \text{NPP}$ using spatial grains coarser than several hectares (Luo *et al.*; Chisholm *et al.*,
518 2013; Hao *et al.*, 2018). If the $S \rightarrow \text{NPP}$ direction is the real causal one, then our results from SEM and RF
519 analyses support several theoretical expectations (Table 1) and give further impetus to efforts quantifying
520 biodiversity effects in naturally assembled ecosystems at broad spatial scales (Isbell *et al.*, 2018). If the

NPP \rightarrow S direction is the real causal one, then our results are in line with (Lavers & Field, 2006; Field *et al.*, 2009), but are in contrast with (Storch *et al.*, 2005; Belmaker & Jetz, 2011), particularly when upscaling from the fine grain to intermediate grain, where both the SEM and RF analyses give congruent results. Intriguingly, a third possibility is that both NPP \rightarrow S and S \rightarrow NPP are real and that they operate simultaneously, as suggested by our SEM results. In this case, we are unaware of any theory that considers how this reciprocal relationship would be expected to change with increasing spatial grain. The one caveat applicable to interpreting any direction of diversity-productivity relationships is that of demographic stochasticity (mechanism I in Table1), which may weaken both NPP \rightarrow S and S \rightarrow NPP, or their synergistic interplay, at fine spatial grains. In our study, the strong local effect of demographic stochasticity appears plausible given the small area of the forest plots (672 m²) and small population sizes (12.24 \pm 0.02 trees per plot; range = 1- 157 trees per plot) therein. This would suggest that temporal changes in local scale biodiversity (Dornelas *et al.*, 2014; Magurran *et al.*, 2018) may have under-appreciated effects on ecosystem function (Bannar-Martin *et al.*, 2018).

The third key result is that other predictors, such as temperature and biomass, were particularly influential in all our analyses. That is, the grain dependence of the relationship between S and NPP was coupled with a clear increase in the combined effect of annual temperature and precipitation on both S and NPP towards coarse grains, which supports the notion that either temperature-dependent diversification (Rohde, 1992; Allen *et al.*, 2002), niche conservatism (Qian & Ricklefs, 2016), or ecological limits (Šímová *et al.*, 2011) shape diversity at these spatial grains. The weaker (relatively to temperature) effect of precipitation is expected since we focus on forests, which only grow above certain precipitation thresholds (Whittaker, 1975). The clear importance of temperature, biomass, longitude, and other predictors such as forest age, temperature seasonality, or species pool (Figs. 4 & 6) highlights that even when the NPP \rightarrow S relationship holds across grains, other drivers are considerably more important in predicting both (e.g., Ratcliffe *et al.*, 2017). Hence, integrating the environmental context surrounding ecological communities into modeling diversity-productivity relationships is a necessary step towards

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546 making robust predictions of either biodiversity or ecosystem functioning at any spatial grain.

547 Our results reveal that mechanisms associated with one direction of diversity-productivity relationships

548 may provide insight to observed patterns of either direction, despite being initially formulated at a

549 different spatial grain. For example, the strong effect of the East-West spatial coordinate on both S and

550 NPP at the fine spatial grain (Fig. 6) suggests that biogeographical history may play a role in shaping the

551 diversity and ecosystem functioning of plant communities, which was initially tested at larger spatial

552 grains (e.g., Hawkins *et al.*, 2011; Conradi *et al.*, 2020). Increasingly, macroecological mechanisms such

553 as speciation gradients (Schluter & Pennell, 2017) and water-energy variables are being examined in

554 small-grain experimental grasslands to explore their role in mediating niche-based processes (Zuppingen-

555 Dingley *et al.*, 2014) and biodiversity effects (Wagg *et al.*, 2017), respectively. Similarly, efforts to

556 upscale biodiversity effects on productivity - developed initially to identify local scale mechanisms

557 (Loreau & Hector, 2001; Turnbull *et al.*, 2016) - may identify new mechanisms that underpin spatial

558 variation in ecosystem functioning at large spatial scales (Gonzalez *et al.*, 2020). An emerging challenge

559 to these efforts is the creation of data products that capture similar processes across spatial scales and are

560 independent (Supplemental Note 2 and Table S3); many of the variables used in this study share similar

561 data sources (e.g. MODIS and LANDSAT sensors), but are ultimately derived from different types of

562 intermediate products. Rather than uniquely focusing on the direction and strength of S-NPP once

563 accounting for other factors, our results show that mechanisms associated with $S \rightarrow NPP$ and $NPP \rightarrow S$

564 likely underpin the context dependency of diversity-productivity relationships across spatial grains (Table

565 1). These recent developments in BEF research and macroecology suggest that conceptual integration

566 between these two disciplines is just beginning (Craven *et al.*, 2019), yet further efforts to bridge

567 disciplinary gaps are essential to deepen current understanding of mechanisms that underpin the shifts in

568 diversity-productivity relationships across spatial scales.

569 To conclude, we show that the relationship between diversity and productivity strengthens toward coarse

570 grains. This result is in line with expectations from both BEF theory, and some (but not all) expectations

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571 from macroecological studies on NPP → S, and highlights the potential of demographic stochasticity and
 572 sampling effects to distort or mask diversity-productivity relationships at fine grains. Moreover, we find
 573 similar support for both directions of diversity-productivity relationships across spatial grains, revealing
 574 that biodiversity and productivity can be both cause and effect. Future research on this relationship needs
 575 to move from fine-grain experiments and observational studies to coarse grains in order to fully
 576 understand and predict the impacts of anthropogenic biodiversity change on ecosystem function.

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