Multi-trait random regression models increase genomic prediction accuracy for a temporal physiological trait derived from high-throughput phenotyping

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Abstract

Random regression models (RRM) are used extensively for genomic inference and prediction of time-valued traits in animal breeding, but only recently have been used in plant systems. High-throughput phenotyping (HTP) platforms provide a powerful means to collect highdimensional phenotypes throughout the growing season for large populations. However, to date, selection of an appropriate statistical genomic framework to integrate multiple temporal traits for genomic prediction in plants remains unexplored. Here, we demonstrate the utility of a multi-trait RRM (MT-RRM) for genomic prediction of daily water usage (WU) in rice (Oryza sativa) through joint modeling with shoot biomass (projected shoot area, PSA). Three hundred and fifty-seven accessions were phenotyped daily for WU and PSA over 20 days using a greenhouse-based HTP platform. MT-RRMs that modeled additive genetic and permanent environmental effects for both traits using quadratic Legendre polynomials were used to assess genomic correlations between traits and genomic prediction for WU. Predictive abilities of the MT-RRMs were assessed using two cross-validation (CV) scenarios. The first scenario was designed to predict genetic values for WU at all time points for a set of accessions with unobserved WU. The second scenario was designed to forecast future genetic values for WU for a panel of known accessions with records for WU at earlier time periods. In each scenario we evaluated two MT-RRMs in which PSA records were absent or available for time points in the testing population. Moderate to strong genomic correlations between WU and PSA were observed across the days of imaging (0.38-0.80). In both CV scenarios, MT-RRMs showed better predictive abilities compared to single-trait RRM, and prediction accuracies were greatly improved when PSA records were available for the testing population. In summary, these frameworks provide an effective approach to predict temporal 51 physiological traits that are difficult or expensive to quantify in large populations.

3 Background

High-throughput phenotyping (HTP) is an innovative tool in plant breeding. HTP provides precise and non-destructive estimation of multiple complex traits that describe growth and development (e.g., height, biomass, and flowering time) or environmental responses (e.g., chlorophyll fluorescence, canopy temperature, and water content) using non-destructive image-based phenotyping (Araus et al., 2018; Morota et al., 2019). These HTP data mitigate extensive costs associated with manual phenotyping, and can be used to better capture the plant's phenome. In the context of plant breeding and genetics, these data can be used to improve the prediction of breeding values for a target trait of interest, thereby improving the accuracy of selection, as well as provide insights into how secondary traits influence a trait of interest (Araus et al., 2018; Morota et al., 2019; Voss-Fels et al., 2019). For many genome-enabled breeding programs, developing phenotyping and statistical 64 approaches to improve prediction of breeding values and accelerate selection is the primary objective (Campbell et al., 2018; Juliana et al., 2019; Voss-Fels et al., 2019). In many breeding programs, the agronomic value of breeding materials is evaluated using multiple traits. These traits are often correlated at the genetic level. One standard approach for predicting breeding values is to jointly fit all phenotypes in a single model using a multi-trait (MT) approaches (Kadarmideen et al., 2003). These approaches capture the genetic covariances between traits, and have been shown to improve the prediction of breeding values compared to single trait approaches for phenotypes with limited records or low heritability (Calus and Veerkamp, 2011; Jia and Jannink, 2012; Guo et al., 2014). Thus, the MT framework can be particularly advantageous when the target trait has low heritability, but is correlated with a more heritable trait; or when the trait of interest is difficult or costly to evaluate and only incomplete data can be collected, and the trait of interest is correlated with a trait that is easier and cheaper to evaluate. Thus, in the context of HTP, MT genomic prediction approaches can accommodate the high-dimensional multi-trait data generated by these platforms. Moreover, secondary phenotypes recorded with HTP can be included in the prediction framework to improve prediction of a target trait such as yield. These applications
have been shown in a recent study by (Sun et al., 2017).

While several studies have highlighted the advantages of MT frameworks for genomic 82 prediction, HTP-derived MT data often introduce an additional level of complexity-the time axis. The standard MT framework may not be appropriate in cases where multiple phenotypes are recorded at regular intervals throughout the growing season or for the duration of the experiment. While MT frameworks can be fit to these data, the assumptions of the MT framework bring to question whether the conventional MT model should be used. For instance, one assumption is that each phenotype in the MT model is finite characteristic (Kirkpatrick et al., 1990). While this is certainly true for two phenotypes such as yield or protein content, this is certainly not the case for a phenotype recorded at two time points (Kirkpatrick et al., 1990). Temporal phenotypes are infinite-dimensional traits, meaning 91 that although there are only records for discrete time intervals, we expect that the phenotype will vary continuously with time between the two intervals. With these data, a more appropriate solution is to treat the temporal phenotypes as continuous characteristics and perform genetic analyses using random regression models (RRM).

RRM model the covariance between time points as a continuous function of time (Mrode, 2014). While several covariance functions can be utilized, Legendre polynomials or B-splines are routinely used (Schaeffer, 2004). With RRM, temporal phenotypes are partitioned into genetic, permanent environmental effects, and residuals (Mrode, 2014). With repeated measurements, it is assumed that there is additional resemblance between records of an individ-100 ual due to environmental factors or circumstances that affect the records of the individual 101 permanently (Mrode, 2014). Thus, the random permanent environment term captures this 102 non-genetic resemblance between time points. Covariance functions are used to model both 103 genetic and permanent environmental effects (Kirkpatrick et al., 1990; Schaeffer and Dekkers, 104 1994; Meyer and Hill, 1997; Schaeffer, 2004). Thus, the RRM prediction framework provides 105 solutions for random regression coefficients for random effects. Given coefficients for ran-106

dom genetic effects, the genetic values at any time point can be easily calculated. Recently, RRM have been used for genomic analyses of longitudinal image-based HTP traits in plants 108 (Campbell et al., 2018, 2019; Momen et al., 2019a). The ability of these frameworks to 109 forecast future phenotypes using the records at earlier time has been shown by Campbell 110 et al. (2018) and Momen et al. (2019a) based on a digital metric for shoot biomass, known 111 as projected shoot area (PSA). PSA is a digital metric derived from images taken of each 112 plant and is highly correlated with destructive measures of shoot biomass (Golzarian et al., 113 2011; Berger et al., 2010; Campbell et al., 2015). 114 However, given the capability of HTP to collect multiple temporal phenotypes, one un-115 resolved question in plant breeding is how to jointly model multiple temporal phenotypes. 116 To address this, we aimed to integrate the RRM framework for temporal traits into a MT 117 model. We utilized a data set in which PSA and water use (WU) was recorded daily over 118 a period of 20 days. The aim of the study was to evaluate the ability of multi-trait ran-119 dom regression model (MT-RRM) and a single-trait random regression model (ST-RRM) to 120 predict WU by borrowing information from PSA. The rationale is that WU is much more 121 difficult to evaluate in most studies compared to PSA and is likely to be more influenced 122 by environmental effects, and thus have lower heritability compared to shoot biomass. The 123

models were compared using several cross-validation (CV) scenarios.

Materials and Methods

Flant materials and greenhouse conditions

This study utilized HTP records from 357 of the 421 accessions of rice (*Oryza sativa*) diversity panel 1 (RDP1) (Zhao et al., 2011). Sixty four accessions were excluded due to lack of seed availability or poor germination. Seeds were treated with Thiram fungicide and germinated on moist paper towels in plastic boxes for three days. Three uniformly germinated seedlings were selected for each accession and transplanted to pots (150mm diameter x 200 mm height) filled with 2.5 kg of UC Mix. The plants were grown in saturated soil on greenhouse benches prior to phenotyping.

Plants were thinned to one seedling per pot seven days after transplant (DAT), and two 134 layers of blue mesh were placed on top of the pots to reduce evaporation. The plants were 135 loaded on to the imaging system at 13 DAT. The automated phenotyping system was set 136 to maintain all plants at 90% field capacity. The experiment followed a partially replicated 137 design (Cullis et al., 2006). The p-rep design was modified to accommodate the two water 138 treatments and allow comparison of treatments within each accession. Each accession was 139 assigned to two consecutive pots, and the water treatments were randomly assigned to each 140 pot. Each experiment consisted of 357 accessions from RDP1 and was repeated three times 141 from February to April 2016. The accessions were distributed across 432 pots positioned 142 across 24 lanes. In each experiment, 54 accessions were randomly selected and replicated 143 twice. All experiments were conducted at the Plant Accelerator Australian Plant Phenomics Facility, at the University of Adelaide, SA, Australia.

Phenotypic data

Beginning at 13 DAT all plants were phenotyped daily for shoot biomass and WU using the automated greenhouse system, and each plant was imaged daily over a period of 20 days using a visible (red-green-blue / RGB) camera (Basler Pilot piA240012 gc, Ahrensburg,

Germany). For each plant, three images were taken in each recording day: two side-view angles separated by 90 degree and a single top view. Plant pixels were extracted from RGB images using the LemnaGrid software, and the plant pixels from the three images were summed to obtain a digital measure of shoot biomass. We refer to this metric as PSA. Several studies have shown this to be an accurate proxy for shoot biomass (Golzarian et al., 2011; Campbell et al., 2015; Knecht et al., 2016).

After imaging, each plant was watered to a predefined weight to maintain 90% field capacity. The automated watering system collects the start weight, final weight and amount of water that was added for each pot. Thus, from these data we can estimate the amount of water that lost by evapotranspiration each day. WU was calculated as $WU_t = Potwt_{t-1} - Potwt_t$. Where $Potwt_{t-1}$ is the weight of the pot after watering on the previous day, and $Potwt_t$ is the weight of the pot on the current day prior to watering (Momen et al., 2019b).

Best linear unbiased estimators (BLUE) were obtained for each accession and day using the following model

$$y_{ij} = \mu + A_i + exp_j + rep_r + e_{ij}$$

where μ is the overall mean, A_i is the fixed effect of the i^{th} accession, exp_j is the random effect of the j^{th} experiment and rep_r is the random effect of the r^{th} replicate. After these processes, 7,140 records from 357 accessions were available for further analysis.

165 Genotypic data

All accessions were genotyped with a 44,000 single nucleotide polymorphisms (SNPs) array (Zhao et al., 2011). Genotypic data regarding the rice accessions can be downloaded from the rice diversity panel website (http://www.ricediversity.org/). SNPs with call rate ≤ 0.95 and minor allele frequency ≤ 0.05 were removed. Missing genotypes were imputed using Beagle software version 3.3.2 (Browning and Browning, 2007) following Momen et al. (2019b). A total of 34,993 SNPs remained for downstream analyses.

$_{72}$ Single-trait random regression model

Campbell et al. (2018) and Momen et al. (2019a) have applied ST-RRM for PSA. In this study, a similar statistical model was used to model WU. The model is given by

$$y_{jt} = \sum_{k=0}^{2} \phi(t)_{jk} b_k + \sum_{k=0}^{2} \phi(t)_{jk} u_{jk} + \sum_{k=0}^{2} \phi(t)_{jk} p_{jk} + e_{jt},$$

where y_{jt} is the BLUE of jth accession for WU at time point t, b_k is the kth fixed Legendre regression coefficients for overall mean, u_{jk} is the kth random regression coefficients for additive genetic effect, p_{jk} is the kth random regression coefficients for permanent environmental effect, e_{jt} is the vector of residuals, and $\phi(t)_{jk}$ is a time covariate coefficient defined by a kth Legendre polynomial evaluated at time point t belonging to the jth accession. We set quadratic Legendre polynomials of all the effects, based on the results of Momen et al. (2019a) which investigated the prediction accuracy of PSA using ST-RRM. The first order of the Legendre polynomial (i.e., an intercept) was standardized to 1 (Gengler et al., 1999). In matrix notation, the model is given by

$$\mathbf{v} = \mathbf{X}\mathbf{b} + \mathbf{Z}\mathbf{u} + \mathbf{Q}\mathbf{p} + \mathbf{e}.$$

where \mathbf{y} is the vector of observations for WU, \mathbf{b} is the vector of fixed effect, \mathbf{u} is the vector of random additive genetic effect, \mathbf{p} is the vector of random permanent environmental effect, \mathbf{e} is the vector of random residual effect, and \mathbf{X} , \mathbf{Z} , and \mathbf{Q} are corresponding incidence matrices. The covariance structures were defined as the following.

$$\operatorname{Var}\begin{bmatrix}\mathbf{u}\\\mathbf{p}\\\mathbf{e}\end{bmatrix} = \begin{bmatrix}\mathbf{C} \otimes \mathbf{G} & \mathbf{0} & \mathbf{0}\\ \mathbf{0} & \mathbf{D} \otimes \mathbf{I} & \mathbf{0}\\ \mathbf{0} & \mathbf{0} & \mathbf{I} \otimes \mathbf{R}\end{bmatrix},$$

where \mathbf{G} is a genomic relationship matrix calculated by $\mathbf{WW'}/m$ according to VanRaden (2008), \mathbf{W} is a centered and scaled matrix, m is the number of SNPs, \mathbf{I} is an identity matrix, \mathbf{C} and \mathbf{D} are covariance matrices of additive genetic and permanent environmental effects, \mathbf{R} is a diagonal matrix of heterogeneous residual variance at each time period, and \otimes is the Kronecker product. The covariance matrices \mathbf{C} and \mathbf{D} are defined as follows.

$$\mathbf{C} = \begin{bmatrix} v_u^0 & v_u^{01} & v_u^{02} \\ v_u^{10} & v_u^1 & v_u^{12} \\ v_u^{20} & v_u^{21} & v_u^2 \end{bmatrix}, \quad \mathbf{D} = \begin{bmatrix} v_p^0 & v_p^{01} & v_p^{02} \\ v_p^{10} & v_p^1 & v_p^{12} \\ v_p^{20} & v_p^{21} & v_p^2 \end{bmatrix},$$

where v_u^k and v_p^k are the variance components of kth order random regression coefficients for additive genetic and permanent environment effects, respectively, and v_u^{kl} and v_p^{kl} are the covariances between kth and lth order random regression coefficients for additive genetic and permanent environmental effects, respectively.

Multi-trait random regression model

For MT-RRM, the ST-RRM for WU described above is expanded to include PSA information as follows.

$$\begin{bmatrix} \mathbf{y_1} \\ \mathbf{y_2} \end{bmatrix} = \begin{bmatrix} \mathbf{X_1} & \mathbf{0} \\ \mathbf{0} & \mathbf{X_2} \end{bmatrix} \begin{bmatrix} \mathbf{b_1} \\ \mathbf{b_2} \end{bmatrix} + \begin{bmatrix} \mathbf{Z_1} & \mathbf{0} \\ \mathbf{0} & \mathbf{Z_2} \end{bmatrix} \begin{bmatrix} \mathbf{u_1} \\ \mathbf{u_2} \end{bmatrix} + \begin{bmatrix} \mathbf{Q_1} & \mathbf{0} \\ \mathbf{0} & \mathbf{Q_2} \end{bmatrix} \begin{bmatrix} \mathbf{p_1} \\ \mathbf{p_2} \end{bmatrix} + \begin{bmatrix} \mathbf{e_1} \\ \mathbf{e_2} \end{bmatrix},$$

where subscripts 1 and 2 refer to WU and PSA, respectively. The covariance structures of **C** and **D** were also expanded as follows.

$$\mathbf{C} = egin{bmatrix} \mathbf{C_1} & \mathbf{C_{12}} \\ \mathbf{C_{12}^T} & \mathbf{C_2} \end{bmatrix}, \quad \mathbf{D} = egin{bmatrix} \mathbf{D_1} & \mathbf{D_{12}} \\ \mathbf{D_{12}^T} & \mathbf{D_2} \end{bmatrix}$$

where C_1 and C_2 (D_1 and D_2) are 3×3 variance-covariance submatrices of random regression coefficients for each trait and C_{12} (D_{12}) is a 3×3 covariance submatrix of random regression coefficients between the traits. Thus, the whole C and D matrices take the form

$$\mathbf{C} = \begin{bmatrix} v_{u_1}^0 & v_{u_1}^{01} & v_{u_1}^{02} & v_{u_{12}}^{02} & v_{u_{12}}^{01} & v_{u_{12}}^{02} \\ v_{u_1}^{10} & v_{u_1}^{1} & v_{u_{12}}^{12} & v_{u_{12}}^{10} & v_{u_{12}}^{12} & v_{u_{12}}^{12} \\ v_{u_1}^{20} & v_{u_1}^{21} & v_{u_1}^{21} & v_{u_{12}}^{12} & v_{u_{12}}^{21} & v_{u_{12}}^{22} \\ v_{u_2}^{20} & v_{u_{21}}^{21} & v_{u_{21}}^{20} & v_{u_{22}}^{20} & v_{u_{22}}^{01} & v_{u_{22}}^{02} & v_{u_{22}}^{21} & v_{u_{22}}^{22} \\ v_{u_{21}}^{20} & v_{u_{21}}^{11} & v_{u_{21}}^{21} & v_{u_{22}}^{20} & v_{u_{22}}^{21} & v_{u_{22}}^{22} & v_{u_{22}}^{22} \\ v_{u_{22}}^{20} & v_{u_{21}}^{21} & v_{u_{21}}^{22} & v_{u_{22}}^{20} & v_{u_{22}}^{21} & v_{u_{22}}^{22} \\ v_{u_{22}}^{20} & v_{u_{21}}^{21} & v_{u_{21}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} \\ v_{u_{22}}^{20} & v_{u_{21}}^{21} & v_{u_{21}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} \\ v_{u_{22}}^{20} & v_{u_{21}}^{21} & v_{u_{21}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} \\ v_{u_{22}}^{20} & v_{u_{21}}^{21} & v_{u_{21}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} \\ v_{u_{22}}^{20} & v_{u_{21}}^{21} & v_{u_{21}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} \\ v_{u_{22}}^{20} & v_{u_{21}}^{21} & v_{u_{21}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} \\ v_{u_{22}}^{20} & v_{u_{21}}^{21} & v_{u_{21}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} \\ v_{u_{22}}^{20} & v_{u_{21}}^{21} & v_{u_{22}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} \\ v_{u_{22}}^{20} & v_{u_{21}}^{21} & v_{u_{21}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} \\ v_{u_{22}}^{20} & v_{u_{21}}^{21} & v_{u_{22}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} \\ v_{u_{22}}^{20} & v_{u_{21}}^{21} & v_{u_{22}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} \\ v_{u_{22}}^{20} & v_{u_{21}}^{21} & v_{u_{22}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} & v_{u_{22}}^{22} \\ v_{u_{22}}^{20} & v_{u_{21}}^{21} & v_{u_{22}}^{22} & v_{u_{22}}^{22$$

where $v_{u_1}^k$ and $v_{p_1}^k$ ($v_{u_2}^k$ and $v_{p_2}^k$) are variance components of kth order random regression coefficients for additive genetic and permanent environment terms for WU (PSA), $v_{u_1}^{kl}$ and $v_{p_1}^{kl}$ ($v_{u_2}^{kl}$ and $v_{p_2}^{kl}$) are covariances between kth and lth order random regression coefficients for additive genetic or permanent environmental effects within WU (PSA), and $v_{u_{12}}^{kl}$ and $v_{p_{12}}^{kl}$ are covariances between kth and lth order random regression coefficients for additive genetic and permanent environmental effects between WU and PSA, respectively. As with ST-RRM, we assumed the residual variance for each day of imaging was unique. Thus, a heterogeneous residual variance structure was used for MT-RRM. The matrix of residual variance at time t ($\mathbf{R}_{(\mathbf{t})}^*$) is presented as:

$$\mathbf{R}_{(\mathbf{t})}^* = \begin{bmatrix} v_{e_{1(t)}} & v_{e_{12(t)}} \\ v_{e_{21(t)}} & v_{e_{2(t)}} \end{bmatrix}$$

where $v_{e_{1(t)}}$ and $v_{e_{2(t)}}$ are residual variances for WU and PSA, respectively, and $v_{e_{12(t)}}$ ($v_{e_{21(t)}}$)
is the residual covariance between WU and PSA at time point t.

Estimation of genomic correlation at each time point

Genomic correlation between WU and PSA at each time point from MT-RRM was computed as follows.

$$\frac{t_iC_{12}t_i'}{\sqrt{t_iC_1t_i'}\sqrt{t_iC_2t_i'}},$$

where $\mathbf{t_i} = \phi_{ik}$ is the *i*th row vector of the 20 × 3 basis function matrix ($\mathbf{\Phi}$) with the kth order of fit (Mrode, 2014). Here, $\mathbf{\Phi}$ is given as $\mathbf{M}\mathbf{\Lambda}$, where \mathbf{M} is a matrix of second order polynomials of standardized time values and $\mathbf{\Lambda}$ is a matrix of coefficients for a second order Legendre polynomial (Kirkpatrick et al., 1990). We used the GIBBS3F90 program to estimate genetic parameters (Misztal et al., 2002).

We investigated the prediction performance of genetic values for WU from RRM using two

Cross-validation scenarios

CV scenarios as shown in Figure 1. For each CV scenario, we compared three models as 191 described below. 192 CV1: The objective of this scenario was to assess the ability of ST-RRM and MT-RRM to 193 predict WU for a set of new accessions without records on WU. To this end, the accessions 194 were split into testing and training sets with 245 accessions allocated to the training set and 195 112 allocated to the testing set. First, we fitted ST-RRM using genomic and phenotypic 196 data on the training subset and the genetic values of WU were predicted for all accessions 197 in the testing set. This ST-RRM served as a baseline to evaluate MT-RRM. We evaluated 198 two different types for MT-RRM. The first MT-RRM (MT-RRM1) can be thought of as 199 a conventional genomic prediction application in which a model is fitted using a training 200 population that has genomic data and phenotypic records for both traits. This model is 201 used to predict genomic values for WU in a testing population that has genotypic data, but 202 no records for either trait. In the second MT-RRM (MT-RRM2), complete PSA and WU 203 records were available for the training population, while only PSA phenotypes were available

for the testing population. The rationale for this scenario is that it is often much easier to obtain non-destructive measurements for shoot biomass compared to WU. Thus, this can be 206 thought of as a case in which a portion of the population has incomplete data. 207 Genetic values of testing individuals for WU at time t from ST-RRM and MT-RRM1 208 were calculated by $\hat{\mathbf{a}}_{tst}^t = \mathbf{G}_{tst,trn}\mathbf{G}_{trn,trn}^{-1}\hat{\mathbf{a}}_{trn}^t$, where $\mathbf{G}_{tst,trn}$ is the genomic relationship matrix 209 between testing and training individuals, $\mathbf{G}_{\mathrm{trn,trn}}^{-1}$ is the inverse of genomic relationship matrix 210 of training individuals, and $\hat{\mathbf{a}}_{\text{trn}}^t = \mathbf{\Phi}\hat{\mathbf{u}}_{1,\text{trn}}$ is the vector of genetic values at time t (Momen 211 et al., 2019a). On the other hand, the genetic values of testing individuals for WU from 212 MT-RRM2 can be directly obtained from best linear unbiased prediction (BLUP) solutions 213 because the model included the genomic relationship matrix of all accessions by fitting PSA 214 phenotypes for the testing individuals. Thus, the genetic values of WU for the testing 215 individuals at time t were computed by $\hat{\mathbf{a}}_{tst}^t = \mathbf{\Phi}\hat{\mathbf{u}}_{1,trn}$. 216 CV2: This cross-validation was designed to evaluate the ability of the MT-RRM and ST-217 RRM to predict genetic values of WU at future time points. Thus, it can be thought of as a 218 forecasting approach. The training dataset consisted of phenotypic records for 245 randomly 219 selected for the first 10 days of imaging. The models were used to predict genetic values for 220 days 11 to 20. As with the first scenario, we assessed their genomic predictions by using ST-RRM and two kinds of MT-RRM from the training data. MT-RRM1 used records of WU and PSA from day 1 to day 10 of imaging as training data, while MT-RRM2 used WU records from the first 10 days of imaging and PSA values from 1 to 20 to train the model. 224 We computed the genetic values of WU at day 11 to 20 as $\Phi_{11:20}\hat{\mathbf{u}}_{1,\mathrm{trn}}$ where $\Phi_{11:20}$ is the 225 basis function matrix at 11 to 20 days and $\hat{\mathbf{u}}_{1,\mathrm{trn}}$ is the vector of random additive genetic 226 effect for WU of testing individuals. 227 To assess prediction accuracy, Pearson correlation was calculated between predicted ge-228 netic values and BLUE of WU at each time point in the testing population. Each CV 229 scenario was repeated 10 times. We used the GIBBS3F90 program with a fixed variance 230 option to perform genomic prediction in all the CV scenarios.

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32 Results

Assessing temporal water use and shoot biomass trajectories in rice

To assess the temporal relationships between shoot biomass production and WU, a panel of 357 rice accessions was phenotyped over a period of 20 days using a non-destructive imagebased phenotyping platform. This system provides a means to non-destructively assess
plant growth and morphology, and allows WU to be assessed throughout the duration of the
experiment (Berger et al., 2010; Campbell et al., 2015; Fahlgren et al., 2015; Feldman et al.,
2018).

Figure 2 shows a boxplot of the BLUE after an adjustment by fixed effects for WU over 20 time days of imaging. WU exhibited an exponential trend over the 20 days of imaging and closely followed the temporal patterns exhibited by PSA.

Joint analysis of WU and PSA reveals shared additive genetic effects between traits

Genetic architectures of WU and PSA were dissected by estimating the proportion of captured additive genetic variances across 20 days of imaging using a ST-RRM. The RRM included a fixed second order Legendre polynomial to capture the overall mean trajectories for each trait, and additive genetic and permanent environmental effects were modeled using a second order Legendre polynomial. Figure 3 shows that PSA exhibited considerably higher narrow-sense heritability (h^2) compared to WU. For instance, h^2 ranged from 0.48 to 250 0.82 for PSA, while the values ranged from 0.28 to 0.69 for WU. We observed an increasing 251 trend over time with the lowest value observed on day 1 of imaging and the highest value 252 observed on day 19. PSA on the other hand showed the lowest h^2 values on day 1, but it 253 quickly increased and reached somewhat of a plateau from day 3 to 16. After day 16, h^2 254 slowly declined. Collectively, these results indicate that both traits are influenced by addi-255 tive genetic effects, and these effects vary throughout time. However, phenotypic variance is less influenced by non-genetic effects for PSA compared to WU. Moreover, additive genetic effects for WU show greater temporal variability compared to PSA.

To investigate genetic relationship between WU and PSA, we estimated genomic correla-259 tion at each time point. The MT-RRM used a second order polynomial to model the overall 260 mean trends for each trait, as well as the additive genetic and permanent environmental 261 effects for both traits. The genomic correlation between WU and PSA from MT-RRM is 262 shown in Figure 4. A moderate to strong positive genomic correlation between WU and 263 PSA was observed over 20 time periods. On average, the genomic correlation across all 264 time periods was 0.73. The genomic correlation was low for the first time point, but quickly 265 increased until the forth day of imaging. From day 4 to the final day of imaging, genomic 266 correlation showed a slight increasing trend. Genomic correlation ranged from 0.38 to 0.80, 267 with the highest value observed on the final day of imaging. These results indicate that WU 268 and PSA share similarity at the genetic level.

Predictive assessment using RRM by two CV scenarios

We next sought to evaluate the predictive performance of MT-RRM to predict genetic values 27 for WU. To this end, we employed two CV scenarios. The first is similar to a conventional 272 genomic prediction application in which the objective is to predict genetic values for a set 273 of individuals without phenotypic records. We used two different testing populations. The 274 first consists a set of 112 randomly selected accessions that have no phenotypic records for 275 PSA and WU. The second consists of a set of 112 accessions that have phenotypic records 276 for PSA, but lack records for WU. Thus, the latter scenario can be thought of as a case 277 where a subset of the population has incomplete data. The predictive ability of MT-RRM1 278 and MT-RRM2 was compared to a ST-RRM in which the model fitted using WU values 279 for 245 accessions and is used to predict genetic values for the remaining 112 accessions. In 280 all cases, the predictive ability was measured as the correlation between predicted genetic values and BLUE in the testing set at each time point.

The prediction accuracy for CV1 is shown in Figure 5. An increasing trend in prediction 283 accuracy over time for all models was observed in CV1. Prediction accuracy increased quickly 284 from day 1 to 13, and eventually plateaued from days 14 to 20. MT-RRM2 showed the highest 285 prediction accuracy of all models. On average the predictive ability for MT-RRM2 was 0.68, 286 while for MT-RRM1 and ST-RRM the prediction accuracies were 0.46 and 0.39, respectively. 287 These results indicate that the predictive ability can be improved using a MT-RRM when 288 records for one trait are available for individuals in the testing population. The predictive 280 ability for MT-RRM1 was similar to ST-RRM during the first five time points, but slightly 290 increased with 0.06 to 0.09 relative to ST-RRM from day 6 on ward. These results suggested 291 that MT-RRM approach can be more effective method for genomic prediction of WU. 292 The objective of the second CV scenario was to evaluate the abilities of MT-RRM1 and 293 MT-RRM2 to forecast genetic values at future time points using phenotypes recorded at 294 earlier time points. The design of two MT-RRM were similar to those described above 295 (Figure 1). The first MT-RRM, MT-RRM1, was fit using a training set with WU and PSA 296 data collected from the first 10 time points, and was used to predict genetic values for WU for 297 the subsequent time points. The second MT-RRM, MT-RRM2, was fit using PSA values for 298 all 20 time points and WU values for the first 10 time points, and was used to predict genetic values for WU for the last 10 time points. Figure 6 shows the predictive correlation of WU for each of the models evaluated. The prediction accuracy for each method was relatively constant over all days. However, the prediction accuracy of MT-RRM were greatly higher 302 than ST-RRM, indicating that inclusion of additional information from PSA can improve 303 the ability to forecast WU. For ST-RRM, prediction accuracy ranged from 0.48 to 0.54, while 304 values for MT-RRM1 and MT-RRM2 range from 0.72 to 0.80 and 0.80 to 0.89, respectively. 305 Collectively, these results indicate that joint analysis of PSA and WU with the MT-RRM 306

improves the ability to forecast future genetic values for WU.

Discussion

Advances in HTP has provided plant breeders with a new suite of tools to assess morphologi-300 cal and physiological traits in a non-destructive manner for large populations at frequent time 310 intervals throughout the growing season (Fahlgren et al., 2015). These platforms facilitate 311 the collection of data that provide important insights into the morpho-physiological basis of 312 complex traits. Thus, with these technologies complex traits such as drought tolerance can 313 be decomposed into component traits to better understand the basis of these traits and im-314 prove the development of varieties with increased resilience (Berger et al., 2010). Although 315 these platforms provide a powerful means to quantify complex traits in large populations, some physiological traits require specialized equipment or must be recorded during a specific 317 time of day (e.g., transpiration or chlorophyll fluorescence) (Tardieu et al., 2017). Thus, in 318 many cases these data may only be available for a subset of the population. 319

HTP is often used to record a number of traits on the same individuals. In some cases, 320 physiological traits that are difficult to measure may be correlated with traits that are more 321 accessible and can be recorded with greater ease. In such cases, MT genomic prediction 322 frameworks provide an excellent solution to utilize partial records and predict genetic val-323 ues for the physiological trait in individuals with missing data. Jia and Jannink (2012) 324 demonstrated that MT models improve prediction accuracy particularly for traits with low 325 heritability. In the current study, we utilized a MT approach in a RRM framework to pre-326 dict genetic values for WU, a difficult to measure trait with low heritability, by joint analysis 327 with PSA, which exhibits higher heritability and is easier to measure. Since WU shows a 328 positive correlation with PSA, we hypothesized that the MT-RRM framework can improve 329 predictions for WU.

Genetic components of HTP image traits

Since WU is difficult to quantify directly in cereals such as rice, few studies have measured 332 WU or water use efficiency, while most studies have sought to utilize indirect measurements 333 of WU or water use efficiency for genetic analyses (This et al., 2010; Rebolledo et al., 2013; 334 Feldman et al., 2018; Momen et al., 2019b). Consistent with the current study, Feldman 335 et al. (2018), which utilized a HTP platform to quantify temporal water use and plant size 336 in the C4 species Setaria grown in contrasting water regimes, reported moderate broad 337 sense heritability (H^2) values for WU, and higher H^2 for plant size. Moreover, Feldman 338 et al. (2018) showed that H^2 varied throughout the experiment with lower H^2 observed during the initial time points and higher H^2 values observed during the middle time points. In our study, h^2 values for WU in early time points were lower compared to those observed during the later time points. The plants in the current study were relatively small during 342 the initial time points and therefore less amount of water is lost each day. Thus, water 343 loss during these periods may be heavily influenced by environmental factors such as soil 344 temperature or irradiation. Similar temporal trends have been reported for plant height 345 in sorghum (Fernandes et al., 2018). Thus, given the moderate h^2 values for WU and the 346 temporal variability in h^2 , selection for this trait may be difficult in breeding programs. 347 Conversely, h^2 for PSA was relatively stable throughout the experiment, indicating that h^2 348 for PSA may be less affected by temporal environmental effects compared to WU. 340 Multi-trait approaches are particularly advantageous when one target trait has low her-350 itability and is correlated to a secondary non-target trait with higher heritability (Mrode, 351 2014). Joint analysis using a MT model can improve prediction of genetic values for low her-352 itability trait and thus improve selection in plant breeding programs. In the current study, 353 we showed a benefit of using MT-RRM for WU which had a positive genomic correlation 354 with PSA. Thus, we proposed that joint analysis of WU with PSA can improve predictions of genetic values for WU. In a recent study, Momen et al. (2019b) examined the relationships between single time point measurements of WU, root biomass, water use efficiency, and PSA. According to the result, WU showed a moderate to strong positive correlation with PSA, root biomass, and water use efficiency, ranging from 0.48 to 0.85 (Momen et al., 2019b). Although we utilized PSA as the indicator trait in this study, it is expected that root biomass and water use efficiency can be leveraged for genomic prediction for WU using the MT.

The MT-RRM framework offers several advantages over conventional single-trait genomic

⁶³ Predictive performance of MT-RRM

364

best linear unbiased prediction (ST-GBLUP) approaches. First, the random regression 365 framework provides a tractable means to predict genetic values for temporal traits. The RRM uses covariances functions to model the genetic and environmental covariance between 367 time points, and has been shown to improve prediction of genetic values compared to a 368 ST-GBLUP approach (Campbell et al., 2018). Secondly, because the covariance function 360 expresses the genetic covariance between time points using a continuous function, the RRM 370 can be used to predict genetic values at time points with no records (Momen et al., 2019a). 371 Thus, we can leverage the RRM framework to forecast future genetic values. Finally, as 372 mentioned above, the joint analysis of MT can improve prediction accuracy for traits with low heritability. In the current study, we designed two CV to evaluate the ability to predict genetic values in unobserved accessions for a trait with lower heritability, and assessed the ability of the MT-RRM to predict future genetic values for accessions with records. The first CV scenario was designed to evaluate the ability of MT-RRM to predict ge-377 netic values for WU in accessions without any records. Consistent with our expectations, 378 MT-RRM had a better predictive ability than ST-RRM. The predictive ability of the MT-379 RRM was further improved when PSA records were available for accessions in the testing 380 population. The effectiveness of MT genomic models have been investigated extensively and 381 have reported improved prediction accuracy compared to a ST model (Jia and Jannink,

2012; Guo et al., 2014; Okeke et al., 2017; Fernandes et al., 2018). For instance, Guo et al. (2014) compared prediction accuracy from ST- and MT-GBLUP using simulated data. MT-384 GBLUP showed better predictive performance when the target trait had lower heritability 385 compared to the non-target trait and when the target trait had a greater number of missing 386 observations (Guo et al., 2014). However, the majority of these studies have focused on 387 traits recorded at a single time point. In the current study, we used a MT approach for 388 prediction of bivariate traits with longitudinal records, and observed similar results. As sug-389 gested by the previous studies, an increase of prediction accuracy by MT-RRM in this study 390 may result from a relative lower heritability of WU than PSA and the high degree of shared 391 genetic signals with PSA (Momen et al., 2019b). The results of CV1 showed that prediction 392 accuracies from all the models were more stable at later time periods, which is similar to the 393 temporal trends in prediction accuracy observed for PSA reported by Momen et al. (2019a) 394 that was obtained using a ST-RRM. The accuracy of genomic prediction largely depends 395 on the heritability of the trait (Hayes et al., 2009). Thus, the lower predictions at the initial time points may be the result of the lower heritability observed during these periods. 397 Moreover, early observations are recorded on seedlings that have just started to tiller. At 398 this stage the plants may not have accumulated enough biomass and have low transpiration demands, to discern genotypic variation in water use from environmental variation. Genomic predictions based on small number of records are a major concern in many 401 practical applications, especially for a trait that is difficult or costly to measure because 402 it can reduce phenotyping costs. As expected, the MT approaches (MT-RRM1 and MT-403 RRM2) in CV2 resulted in improvements compared to the ST-RRM with gains of 0.25 and 404 0.33, on average, for MT-RRM1 and MT-RRM2, respectively. Our results suggest that 405 MT-RRM can be a powerful approach for forecasting future phenotypes using records from 406 earlier periods. In this study, we examined prediction accuracies from 11 to 20 days in CV2. 407 However, the trends in prediction accuracy were relatively stable across time points. Thus, 408 forecasting based on records at further earlier time periods could be implemented without a loss of prediction accuracy as reported by Momen et al. (2019a). However, the performance of these forecasting approaches will likely be highly dependent on the genomic correlation between the time points used to train the prediction model and the time points in which predictions will be made. Lastly, it should be noted that the best prediction performance delivered by MT-RRM2 in both scenarios may be due to the fact that the training-testing sets partitioning is not completely independent in a strict sense. However, a situation akin to this occurs in practice and an approach such as MT-RRM2 would be still worthwhile to test.

Conclusion

To our knowledge, this is the first study that applied the MT-RRM to HTP-derived temporal traits in plants. We demonstrated that MT-RRM is a robust and flexible approach that can be used to improve prediction accuracy for a trait with a limited number of records or low heritability. Thus, in the case of breeding for morpho-physiological traits, the MT-RRM can improve prediction accuracy for physiological traits that may have low heritability or are difficult to measure in large populations.

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431 to HW and GM, and Virginia Polytechnic Institute and State University startup funds to

432 GM. MTC and HW designed and conducted the experiments. TB and MM analyzed the

data. TB and GM conceived the idea and wrote the manuscript. MTC, MM and HW

discussed results and revised the manuscript. GM supervised and directed the study. All

authors read and approved the manuscript.

56 Figures

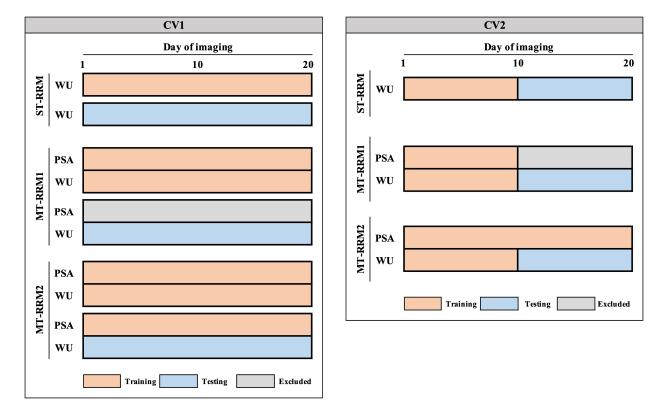


Figure 1: Two scenarios of cross-validation (CV) designed to investigate prediction accuracy of water use (WU) from single- and multi-trait random regression models (ST-RRM, MT-RRM1, and MT-RRM2). CV1: Prediction of WU for a set of 112 accessions without records on WU using 245 training accessions. ST-RRM: single-trait random regression model using WU of training accessions; MT-RRM1: multi-trait random regression model using WU and projected shoot area (PSA) of training accessions; MT-RRM2: multi-trait random regression model using WU and PSA of training accessions as well as PSA of testing accessions. CV2: Forecast future genetic values of WU belonging to 245 known accessions from records at earlier time periods. ST-RRM: single-trait random regression model for WU using the first 10 time points in training accessions; MT-RRM1: multi-trait random regression model for WU using the first 10 time points of WU and PSA information in training accessions; MT-RRM2: multi-trait random regression model for WU using WU from 1 to 10 time periods and PSA at all the time periods in training accessions.

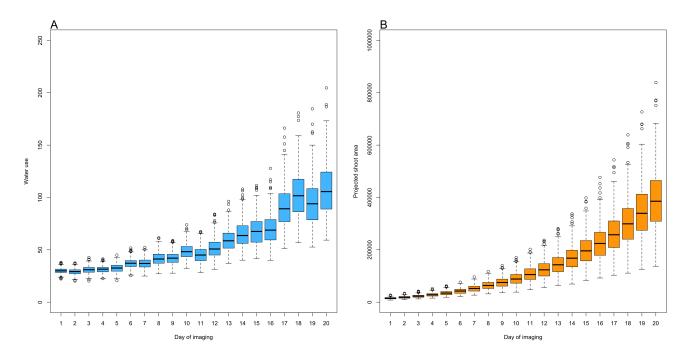


Figure 2: A boxplot of best linear unbiased estimator for water use (A) and projected shoot area (B) over 20 days of imaging.

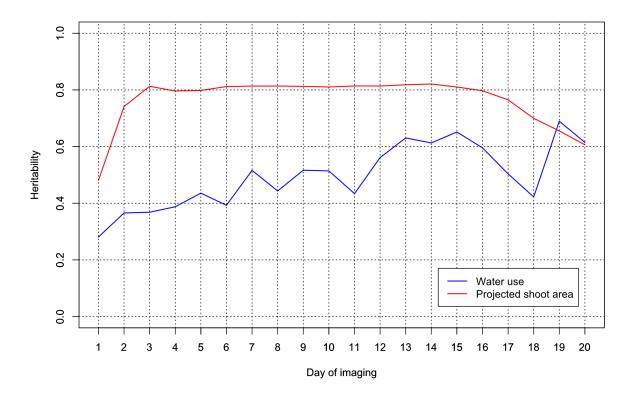


Figure 3: Heritability for water use and projected shoot area over 20 days of imaging using a single-trait random regression model.

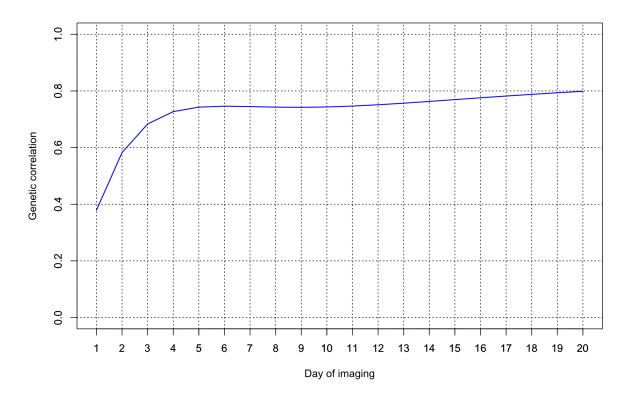


Figure 4: Genomic correlation between water use and projected shoot area over 20 days of imaging using a multi-trait random regression model.

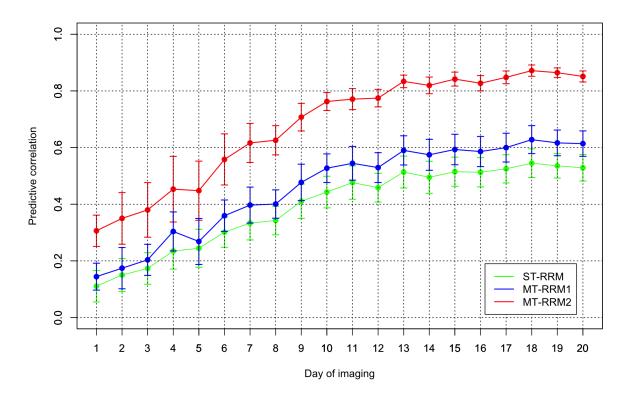


Figure 5: Pearson correlation of water use from cross-validation scenario 1. ST-RRM: single-trait random regression model; MT-RRM1: multi-trait random regression model using the water use and projected shoot area of training data; MT-RRM2: multi-trait random regression model using the water use and projected shoot area of training data as well as the PSA of testing data.

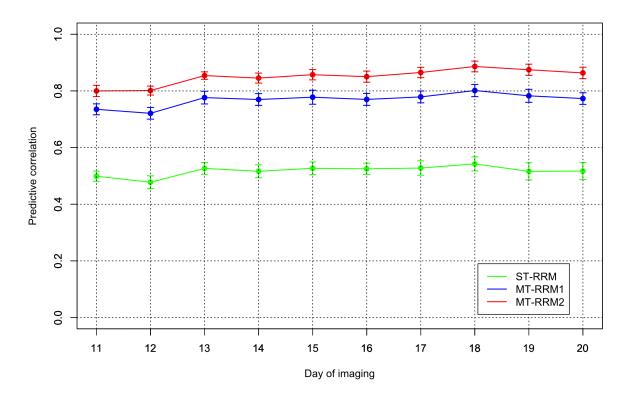


Figure 6: Pearson correlation of water use from cross-validation scenario 2. ST-RRM: single-trait random regression model; MT-RRM1: multi-trait random regression model using WU and PSA from 1 to 10 time periods in the training data; MT-RRM2: multi-trait random regression model using WU from 1 to 10 time periods and PSA at all the time periods in the training data.

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