1

Robustness and universality in organelle size control

Kiandokht Panjtan Amiri[1, *], Asa Kalish[1,*], Shankar Mukherji[1,2,3,†]

[1]Department of Physics, Washington University in St. Louis, St. Louis, MO

[2]Department of Cell Biology & Physiology, Washington University School of Medicine,
St. Louis, MO

[3]Center for the Science and Engineering of Living Systems, McKelvey School of
Engineering, Washington University in St. Louis, St. Louis, MO

* These authors contributed equally

[†] Correspondence to: smukherji@wustl.edu

ABSTRACT

One of the grand challenges in quantitative cell biology is understanding the precision
with which cells assemble and maintain subcellular organelles. A critical property that
governs organelle function is its size. Organelle sizes must be flexible enough to allow
cells to grow or shrink them as environments demand, yet be maintained within
homeostatic limits. Despite identification of numerous molecular factors that regulate
organelle sizes we lack insight into the quantitative principles underlying organelle size
control. Here we examine organelle sizes from *Saccharomyces cerevisiae* and human iPS
cells with mathematical theory to show that cells can robustly control average fluctuations
in organelle size. By demonstrating that organelle sizes obey a universal scaling
relationship we predict theoretically, our framework suggests that organelles grow in
random bursts from a limited pool of building blocks. Burst-like growth provides a general
biophysical mechanism by which cells can maintain on average reliable yet plastic
organelle sizes.

INTRODUCTION

Among the most critical scales of biological organization in the eukaryotic cell is its compartmentalization into organelles. Organelle biogenesis, among the most complex tasks the eukaryotic cell performs, is the result of the coordinated synthesis of tens to hundreds of protein and lipid macromolecular species, each of which is potentially subject to stochastic fluctuations intrinsic to their production. How these molecular-scale fluctuations propagate to organelle-scale functional properties remains an outstanding question in quantitative cell biology (Chang and Marshall 2017, Vagne and Sens 2018, Sachadeva 2016, Bauer 2020). We have previously shown that organelle copy number statistics exhibit substantial cell-to-cell variability (Mukherji and O'Shea 2014), though the root mechanisms of this variability remain subject of much debate (Craven 2016, Choubey 2019). Here we turn our attention to the ability of the eukaryotic cell to control a closely linked biophysical property that determines organelle function: organelle size.

Pioneering work on a wide variety of organelles has focused on characterizing average organelle sizes and begun to unravel the molecular mechanisms underpinning this size control (Marshall 2016). The physiological importance of controlling organelle size is highlighted by their massive expansion upon increased demand for their outputs. The volume of the endoplasmic reticulum, for example, is upregulated to support elevated protein secretion by mature B cells through activation of the unfolded protein response (Shaffer 2004, Taubenheim 2012). Similarly, mitochondrial volume increases to support elevated respiration in myocytes following prolonged exercise (Jornayvaz and Shulman 2010). Peroxisome and lipid droplet volumes increase upon cellular exposure to environments enriched in very long chain fatty acids (Smith and Aitchison 2013, Thaim 2013). The importance of controlling organelle size is further suggested by the many scaling relationships that have shown both fixed relative sizes of various organelles compared to their host cells in a variety of organisms and developmental contexts (Levy and Heald 2012), including for the nucleus (Levy and Heald 2010, Chen 2019) and vacuole (Chan 2016), and nontrivial relationships such as maximal mitochondrial activity in intermediate sized cells (Miettinen and Bjorklund 2016). Dysfunctional organelle size control has been linked to a wide variety of metabolic, developmental, and neurodegenerative disorders (Hatch 2013, Shahmoradian 2019, Mourelatos 1990, Chang 2017). Uncoordinated regulation of organelle size can lead to severe phenotypic defects, such as impaired *Chlamydomonas reinhardtii* motility in uncoordinated flagellar length control (McVittie 1972), inappropriately sized secretory vesicles due to variability in Golgi size (Ferraro 2014), and impaired metabolism due to defects in mitochondrial (Toda 2016) and peroxisomal (Waterham 2007) fission among others. What remains underexplored, as also highlighted by complementary work simultaneous to our own documenting the coupling between organelle size and fluctuations (Bauer 2020), is development of a quantitative understanding of the precision with which organelle size variability is controlled, particularly for organelles that exist in multiple copies per cell.

Drawing on a combination of the theory of stochastic processes and quantitative fluorescence imaging, we directly examine two questions: how precisely the does the cell control the sizes of its organelles and what, if any, overarching quantitative principles collectively describe the patterns of observed organelle sizes despite the vastly different molecular mechanisms that implement size control?

RESULTS

Organelle size control appears to be constrained by a limiting pool of building blocks

In order to decipher the quantitative principles governing organelle size control, we reasoned that
we could use a mathematical model of organelle biogenesis to interpret endogenous stochastic
fluctuations in organelle size. Our first task in building a mathematical framework to quantify
organelle size control was to be able to distinguish between the three general limits organelle
growth is thought to fall into (Marshall 2016). In the first limit, termed constant growth, organelle
growth occurs at a constant rate. In the second limit, termed negative feedback control, the cell
constrains organelle growth rates to drive them towards a target size. In the third limit, termed the
limiting pool, we assume that organelle sizes are constrained by a limited pool of building blocks
from which they are assembled. In each limit, organelle size is affected by both size-specific
processes, such as growth and disassembly, as well as number changing processes such as
fission and fusion (Rafelski 2008, Lowe 2007). We therefore derived a stochastic model of
organelle biogenesis that tracks the joint probability distribution of organelle numbers and sizes
in single simulated cells. In this model organelles can be created de novo, decay, undergo fission
and fusion, grow in size, and shrink (**Fig.1A**). Using the Gillespie algorithm (Gillespie 1977) we
solve our model for the three general limits that organelle growth can take. The simulation is
performed by tracking the number and sizes of organelles in a single cell until they reach steady
state. We repeat these simulations for 1000 cells and extract organelle number and organelle
sizes from each simulated cell (**Fig. S1**).

Inspired by physiologically-relevant cases, we focused the simulations on three different regimes
of number changing dynamics: in the late Golgi (Bevis 2002, Rossanese 1999) and lipid droplet
(Pol 2014, Wilfling 2014, Walther 2017) relevant case in which number dynamics are governed
by de novo synthesis and first order decay (**Fig. 1B**), in the peroxisome relevant limit of when
organelle numbers change through de novo synthesis, first order decay, and fission (Hoepfner
2005, van der Zand 2012, Motley and Hettema 2007, **Fig. 1C**), and lastly in the mitochondria
relevant limit of when the abundance of organelles changes solely through fission and fusion
(Diaz 2008, **Fig. 1D**). For each number changing regime we see that the correlation between
organelle number and average organelle size is diagnostic for whether organelles grow at a
constant rate or are constrained by either negative feedback or a limiting pool of building blocks.
Most importantly, in the limiting pool limit we observe a negative correlation between organelle
number and average organelle size in both de novo synthesis and fission dominated organelle
number controlling regimes; these correlations are robust to variations in the detailed parameters
used in the simulation (**Fig. S2**). This contrasts with the constant growth regime, in which average
organelle size is constant in simulated cells with different organelle numbers when organelles are
made de novo. Intuitively, this is because in the constant growth regime with de novo synthesized
organelles, the organelles within a given cell grow independently of each other and each attain a
steady state size set only by the rates of assembly and disassembly irrespective of how many
other organelles are in that given cell. Finally, we note that in the case of fission and fusion
dominated organelle numbers, the constant growth and limited pool limits both reduce to the same
picture as the fission and fusion processes conserve biomass, leading to an inherent tradeoff
between organelle number and size. The model thus leaves us well positioned to use
experimental data to infer which growth limit describes a given organelle.

To experimentally measure joint organelle number versus size distributions so as to infer
organelle growth rules with our model, we analyzed the endogenous stochastic fluctuations in
organelle numbers and sizes in the budding yeast *Saccharomyces cerevisiae*. To visualize the
various organelles we examine, we fuse the fluorescent protein monomeric Kusibara Orange2
(mKO2) to organelle membrane resident proteins (**Fig. S3-5**). We obtain joint single cell average
organelle size versus organelle number probability distributions of fluorescently labelled late Golgi
(labelled with Sec7-mKO2), lipid droplets (Erg6-mKO2), peroxisomes (Pex3-mKO2), and
mitochondria (Tom70-mKO2). From these joint distributions we plot the average organelle size

as a function of organelle number. For each of the organelles we examine, we observe a
significant negative correlation between organelle number and average organelle size (**Fig. 1E-**
1H). In the case of late Golgi and lipid droplets, which we expect are dominated by de novo
synthesis, the negative correlation is inconsistent with the constant growth and negative feedback
limits of the general stochastic growth model. In the case of the mitochondria, whose copy
numbers are a result of fission and fusion, the observed negative correlation is inconsistent with
negative feedback. In the case of the peroxisome, the negative correlation is consistent with both
constant growth with fission and the limiting pool limits. In order to distinguish between these
pictures, we note that reducing peroxisome fission should flatten the curve relating organelle size
to number if peroxisome growth occurs in the constant growth limit while it should remain
negatively correlated in the limiting pool limit. We genetically deleted the peroxisome fission
factors *DNM1, FIS1,* and *VPS1* (Kuravi 2006, Mukherji 2014, **Fig. S6A-C**) and observe the
persistence of a negative correlation between average organelle size and organelle number. Our
measurements suggest that the sizes of the four organelles under study are all constrained by a
limited pool of building blocks.

Cells exhibit robust average intracellular variability in organelle size

Among the most attractive hypotheses arguing for the utility of the limiting pool model of organelle
growth is that it achieves a stable organelle size in the absence of feedback. However, it has been
shown theoretically that growing multiple organelles from a limited pool of building blocks can lead
to remarkably severe size fluctuations between organelles within the same cell (Mohapatra 2017,
Fai 2019), potentially impairing cellular-scale physiological function. To quantify how intracellular
fluctuations in organelle size behave in our model, we plot the average coefficient of variation
(CV) in organelle size as a function of organelle size. We focus on cells simulated in the limiting
pool limit of the model. As expected for a Poisson-type process, we observe that for decreasing
organelle size (which corresponds to increasing organelle number) the intracellular organelle size
CV increases. This suggests that cells face a fundamental tradeoff in their ability to achieve
organelle size homeostasis. We then use our experimental joint distributions of organelle number
and size for the late Golgi, lipid droplets, mitochondria and peroxisomes to directly measure the
CV of organelle sizes within single cells (**Fig. 1I-L, Fig. S7**). Contrary to our theoretical expectation
(**Fig. 1I-L**, insets), we see that the average intracellular CV of the late Golgi, lipid droplets and
peroxisomes remain constant with varying average organelle size. Thus, despite organelles
changing in size by 2-fold, cells are able to robustly maintain the fluctuations in sizes to within a
factor of 0.5 (peroxisomes) to 0.6 (late Golgi and lipid droplets) of the mean organelle size, thereby
avoiding a rise in intracellular fluctuations when the mean organelle size shrinks. Only the average
intracellular CV of mitochondria appears to increase when the cell creates more, smaller copies
of this organelle.

Burst-like organelle growth model derived to explain robust organelle size control unifies
description of endomembrane organelle size statistics

To address the discrepancy between the noise profile resulting from our model versus the noise
profile of organelles observed experimentally, we consider a fundamental revision to how
organelle growth proceeds in our mathematical framework. Building on previous observations that
subcellular structures can grow from bursts of random sizes of building blocks (Ludington 2013)
we constructed a model in which organelles grow from a limited pool of building blocks in
exponentially distributed bursts of random size β that occur at random times characterized by a
burst frequency α (**Fig. 2A**). In the model, changes in organelle size arise from modulation of the
burst size β, which is proportional to the free pool of building blocks available for organelle growth.

If the limited pool of building blocks is not exhausted and allows organelle sizes to fluctuate
independently of each other, and if copy number changes are slow compared to size changes,
then the resulting organelle sizes from cells that contain a defined number of organelles follow a
gamma distribution with mean size $\alpha\beta$ (**Fig. 2B**). Crucially, the average intracellular organelle size
fluctuations depend only on the burst frequency α but is independent of the burst size β (Friedman
2006). This allows the cell to decouple the average fluctuations in intracellular organelle size from
the mean organelle size (**Fig. 2C**) as we observe experimentally, allowing robust tuning of
organelle sizes.

The model predicts that if the pool of building blocks is not depleted, we should observe two types
of data collapses upon rescaling organelle sizes (**Fig. 2D, Fig. S8A-G**). First, since the model
holds that organelle sizes change only through modulation of burst sizes, rescaling organelle
sizes by their corresponding burst sizes should collapse them onto unifying gamma distributions
specific to each organelle. Second, by further rescaling these organelle-specific size distributions
by their organelle-specific burst frequencies, our whole collection of late Golgi, lipid droplet, and
peroxisome sizes should collapse onto the universal curve $f(s) = e^{-s}/s$, where s is the
dimensionless rescaled organelle size (**Methods**).

To test our predictions from the burst-like organelle growth model we first construct a measure of
pool depletion. To measure pool depletion, we measure the total volume of all copies of a given
organelle in each cell, and assume all cells have roughly equal amounts of the limiting pool.
Plotting the total organelle volume as a function of organelle number, if the total volume increases
linearly with the number of organelles, we conclude that the pool has not depleted. However, if at
higher organelle numbers the total organelle volume plateaus then we conclude that the limited
pool has depleted. We plot the total organelle volume versus organelle number for late Golgi, lipid
droplet, and peroxisomes (**Fig. 2E-G, insets**). We observe that while each organelle appears to
grow from a limited pool, the pool of building blocks does not appear to deplete.

To test our prediction that modulation of burst size alone can explain changes in organelle sizes,
we first use our experimental data to obtain burst size values for each late Golgi, peroxisome and
lipid droplet size distribution. Mathematically, the burst size is the product of the mean organelle
size and the square of the average intracellular CV, both of which we measure experimentally.
We then rescale late Golgi, peroxisome, and lipid droplet sizes by their experimentally inferred
burst sizes and plot the resulting rescaled size distribution. We see that late Golgi, lipid droplet,
and peroxisome sizes collapse onto single gamma distributions (**Fig. 2E-G**). Further rescaling the
organelle-specific rescaled size histograms by their experimentally calculated burst frequencies
α, we see that despite the starkly different molecular mechanisms by which their sizes are
controlled, late Golgi, lipid droplet, and peroxisome size distributions further collapse onto the
single theoretically predicted universal curve $f(s) = e^{-s}/s$ (**Fig. 2H**). This fitting parameter-free data
collapse strongly suggests that our mathematical model of organelle biogenesis has captured an
essential, unifying feature of endomembrane organelle growth regulation.

Depletion of limited pool of building blocks breaks robust organelle size control

According to our model, sufficient capacity in the limited pool of building blocks allows organelles
to grow and fluctuate in size independently of each other and allow for robust intracellular size
control. Our model also predicts, however, that if the available amount of building blocks for
growth depletes enough to be similar to the typical burst size (**Fig. 3A,B**) then intracellular
organelle size fluctuations will become anti-correlated. Anti-correlated fluctuations, in turn, will
lead to a rise in the average intracellular CV (**Fig. 3C**).

To test our prediction that organelle growth from a limited pool with no spare capacity leads to an
elevated intracellular CV, we examine the case of mitochondria, whose sizes are a balance
between biomass conserving fission and fusion. We plot total organelle volume vs. organelle
number for mitochondria and observe a flat line (**Fig. S9A**), consistent with the idea that cells
largely rearrange an existing a fixed pool of mitochondrial biomass when changing mitochondrial
number through fission and fusion. The resulting organelle size distributions are consistent with
our model (**Fig. S9C-I**) and with our observation of an increasing intracellular CV with decreasing
mitochondria size (**Fig. 1L**).

Next we test our prediction that downregulating size growth bursts will increase average
intracellular size fluctuations. We reason that inhibiting Golgi vesicular traffic could reduce large
bursts of size changes, leading to a narrower distribution of burst sizes that would mimic
deterministic growth steps, or reduce the burst frequency. Both changes would lead to depletion
of the available supply of building blocks and a predicted increased average intracellular Golgi
CV. To test this idea, we analyze the late Golgi in cells lacking the vesicular traffic regulator *ARF1*
(Bhave 2014). We observe, in agreement with our hypothesis, that upon deletion of *ARF1* the
average intracellular Golgi size CV increases as the average Golgi size decreases (**Fig. 3D,E**).
Moreover, we observe a concomitant increase in cell size variability upon increased Golgi size
variability (**Fig. S10**).

Finally, to test our prediction that pool depletion leads to an elevated intracellular organelle size
CV, we turn to lipid droplets and peroxisomes. Lipid droplets and peroxisomes are dynamic
organelles whose sizes and copy numbers increase upon cellular exposure to long chain fatty
acid-rich environments (Wilfling 2014, Walther 2017, Mast 2010). We hypothesized that culturing
cells in an oleic acid rich environment could expose capacity constraints in lipid droplet and
peroxisome biogenesis given our previous observation that these organelles appear to grow from
a limited pool of building blocks. We observe that when grown in glucose, neither lipid droplets
nor peroxisomes deplete the limited pool of building blocks, however, when grown in medium rich
in oleic acid, total organelle volume plateaus (**Fig. 3F,H**), suggesting that the pool has depleted.
Concomitantly, we observe that the lipid droplet and peroxisome average intracellular organelle
size CV increases with decreasing mean organelle size (**Fig. 3G,I**). Importantly, we observe the
elevation of the average intracellular peroxisome size CV in oleic acid even upon deletion of the
primary peroxisome fission factor *VPS1*, (**Fig. 3I**) suggesting that capacity constraints from the
limited pool of building blocks, and not elevated fission, are responsible for the increased noise
in peroxisome sizes.

Pattern of organelle size robustness is conserved to human induced pluripotent stem cells

To establish the evolutionary conservation of our observed pattern of robustness in organelle size,
we leveraged single cell imaging data from human induced pluripotent stem cells (iPSC) whose
Golgi apparatus and mitochondria are labelled available from the Allen Cell Atlas (Roberts 2017).
With single cell organelle size distributions from populations of iPSCs, we are able to construct
datasets of both average organelle size versus organelle number and the average intracellular
organelle size CV as we have done for budding yeast. Both the Golgi apparatus and mitochondria
yield negative sloping average organelle size versus organelle number curves consistent with a
limited pool model constraining their growth (**Fig. 4A,C**). Most significantly, we observe that the
average intracellular organelle size CV exhibits the same pattern in human iPSCs as seen for
budding yeast: a robust, invariant organelle size CV as a function of average organelle size for
the Golgi (**Fig. 4B**) and a sensitive, inverse correlation between organelle size CV and average
organelle size for the mitochondria (**Fig. 4D**).

DISCUSSION

In order to explain our observed invariance of average organelle size fluctuations to changing mean organelle size, we propose a model in which organelle growth proceeds in a burst-like fashion from a limited pool of building blocks. The pattern of organelle size robustness is shared between budding yeast and human iPS cells. The underlying molecular mechanisms producing these bursts are yet to be fully elucidated and are likely to be organelle-specific and potentially species-specific: Golgi size, for example, is likely influenced by both small increases in size from non-vesicular traffic as well as the sudden, large increases in size from vesicle fusion as we have shown here, while lipid droplet size bursts may result from burst-like expression of genes such as those encoding neutral lipid synthesis enzymes. However, the size statistics of a diverse array of organelles appear to be well described by a single unifying model that can be used to interpret future studies on the mechanistic underpinnings of organelle size control and a basis for more sophisticated modeling efforts to more accurately capture details suppressed here (Craven 2016, Choubey 2019, Banerjee and Banerjee 2020) as well as comparison to universal growth phenomena in seemingly unrelated biological systems (Iyer-Biswas 2014). More generally, the robust organelle size control we observe here may play a significant role in cellular homeostasis and aid in efforts to engineer organelle size to rationally control cellular metabolism. Suppression of average intracellular organelle size variability in principle allows the organelles within the cell to be functionally interchangeable with each other, avoiding fluctuations in phenotype that could arise from variability from one organelle to another within the same cell arising solely due to increased number of that organelle. Establishing the limits of the ability of the cell to suppress size fluctuations, which we demonstrated in the case of Golgi, peroxisomes and lipid droplets and complementary work in flagellar length control in *Chlamydomonas reinhardtii* showing a coupling between flagellar length and length fluctuations (Bauer 2020), may provide important clues for how to design organelles to control cellular phenotypes. Our results point to the potentially general principle that that robust size control can, remarkably, be the result of random burst-like assembly of subcellular structures.

REFERENCES

Banerjee, D.S. & Banerjee, S. Size regulation of multiple organelles competing for a shared subunit pool. bioRxiv doi: https://doi.org/10.1101/2020.01.11.902783 (2020).

Bauer, D., Ishikawa, H., Wemmeber, K.A., Marshall, W.F. Biological noise in an organelle size control system. bioRxiv doi: https://doi.org/10.1101/2020.08.31.276428 (2020).

Bevis, B. J., Hammond, A. T., Reinke, C. A. & Glick, B. S. De novo formation of transitional ER sites and Golgi structures in Pichia pastoris. Nature Cell Biology 4: 750 (2002).

Bhave, M. et al. Golgi enlargement in arf-depleted yeast cells is due to altered dynamics of cisternal maturation. J Cell Sci 127: 250–257 (2014).

Chan, Y.M., Reyes, L., Sohail, S.M., Tran, N.K., Marshall, W.F. Organelle size scaling of the budding yeast vacuole by relative growth and inheritance. Curr. Biol. 26(9): 1221-1228 (2016).

Chang, A.Y. & Marshall, W.F. Organelles - understanding noise and heterogeneity in cell biology at an intermediate scale. *Journal of Cellular Science* 130(5): 819-826 (2017).

Chen, P., Tomschik, M., Nelson, K.M., Oakey, J., Gatlin, J.C., Levy, D.L. Nucleoplasmin is a limiting component in the scaling of nuclear size with cytoplasmic volume. J. Cell Biol. 218(12): 4063-4078 (2019).

Choubey, S., Das, D. & Majumdar, S. Cell-to-cell variability in organelle abundance reveals mechanisms of organelle biogenesis. Physical Review E 100: 022405 (2019).

Craven, C. J. Evaluation of predictions of the stochastic model of organelle production based on exact distributions. eLife 5: e10167 (2016).

Diaz, F. & Moraes, C. T. Mitochondrial biogenesis and turnover. Cell calcium 44: 24–35 (2008).

Fai, T.G., Mohapatra, L., Kar, P., Kondev, J., & Amir, A. Length regulation of multiple flagella that self-assemble from a shared pool of components. eLife 8: e42599 (2019).

Ferraro, F., Kriston-Vizi, J., Metcalf, D.J., Knight, A.E., Ketteler, R., & Cutler, D.F. A Two-Tier Golgi-Based Control of Organelle Size Underpins the Functional Plasticity of Endothelial Cells. Developmental Cell 29(3): 292-304 (2014).

Friedman, N., Cai, L. & Xie, X. S. Linking stochastic dynamics to population distribution: an analytical framework of gene expression. Physical Review Letters 97: 168302 (2006).

Gillespie, D. T. Exact stochastic simulation of coupled chemical reactions. The journal of physical chemistry 81: 2340–2361 (1977).

Hatch, E.M., Fischer, A.H., Deerinck, T.J., & Hetzer, M.W. Catastrophic nuclear envelope collapse in cancer cell micronuclei. Cell 154: 47–60 (2013).

Hoepfner, D., Schildknegt, D., Braakman, I., Philippsen, P. & Tabak, H. F. Contribution of the
endoplasmic reticulum to peroxisome formation. Cell 122: 85–95 (2005).

Iyer-Biswas S, Crooks GE, Scherer NF, Dinner AR. Universality in stochastic exponential growth.
Phys Rev Lett. 113(2): 028101 (2014).

Jornayvaz, F.R., Shulman, G.I. Regulation of mitochondrial biogenesis. Essays Biochem. 47:
10.1042/bse0470069 (2010).

Kuravi, K. et al. Dynamin-related proteins Vps1p and Dnm1p control peroxisome abundance in
saccharomyces cerevisiae. Journal of Cell Science 119: 3994–4001 (2006).

Levy, D.L., Heald, R.D. Nuclear size is regulated by Importin α and Ntf2 in Xenopus. Cell 143(2):
288-298 (2010).

Levy, D.L., Heald, R.D. Mechanisms of intracellular scaling. Ann. Rev. Cell Dev. Biol. 28: 113-
135 (2012).

Lowe, M. & Barr, F. A. Inheritance and biogenesis of organelles in the secretory pathway. Nature
Reviews Molecular Cell Biology 8: 429 (2007).

Ludington, W. B., Wemmer, K. A., Lechtreck, K. F., Witman, G. B. & Marshall, W. F. Avalanche-
like behavior in ciliary import. Proceedings of the National Academy of Sciences 110: 3925–3930
(2013).

Marshall, W.F. Cell geometry: how cells count and measure size. Annual Reviews of Biophysics
45: 49-64 (2016).

Mast, F. D., Fagarasanu, A., Knoblach, B. & Rachubinski, R. A. Peroxisome biogenesis:
something old, something new, something borrowed. Physiology 25: 347–356 (2010).

McVittie, A. Flagellum mutants of Chlamydomonas reinhardtii. Journal of General Microbiology
71: 525-540 (1972).

Miettinen, T.P., Bjorklund, M. Cellular allometry of mitochondrial functionality establishes the
optimal cell size. Dev. Cell 39: 370-382 (2016).

Mohapatra, L., Lagny, T. J., Harbage, D., Jelenkovic, P. R. & Kondev, J. The limiting-pool
mechanism fails to control the size of multiple organelles. Cell Systems 4: 559–567 (2017).

Motley, A. M. & Hettema, E. H. Yeast peroxisomes multiply by growth and division. The Journal
of cell biology 178: 399–410 (2007).

Mourelatos, Z., Adler, H., Hirano, A., Donnenfeld, H., Gonatas, J.O., & Gonatas, N.K.
Fragmentation of the Golgi apparatus of motor neurons in amyotrophic lateral sclerosis revealed
by organelle-specific antibodies. Proc. Natl. Acad. Sci. U S A 87(11): 4393–4395 (1990).

Mukherji, S. & O'Shea, E. K. Mechanisms of organelle biogenesis govern stochastic fluctuations
in organelle abundance. eLife 3: e02678 (2014).

Pol, A., Gross, S. P. & Parton, R. G. Biogenesis of the multifunctional lipid droplet: lipids, proteins,
and sites. J. Cell Biol 204: 635–646 (2014).

Rafelski, S. M. & Marshall, W. F. Building the cell: design principles of cellular architecture. Nature
Reviews Molecular Cell Biology 9: 593 (2008).

Roberts, B., Haupt, A., Tucker, A., Grancharova, T., Arakaki, J., Fuqua, M.A., Nelson, A.,
Hookway, C., Ludmann, S.A., Mueller, I.A., Yang, R., Horwitz, R., Rafelski, S.M., Gunawardane,
R.N. Systematic gene tagging using CRISPR/Cas9 in human stem cells to illuminate cell
organization. Mol. Biol. Cell 28(21): 2854-2874 (2017).

Rossanese, O. W. et al. Golgi structure correlates with transitional endoplasmic reticulum
organization in pichia pastoris and saccharomyces cerevisiae. The Journal of Cell Biology 145:
69–81 (1999).

Sachadeva, H., Barma, M., Rao, M. Nonequilibrium description of de novo biogenesis and
transport through Golgi-like cisternae. Scientific Reports 6: 38840 (2016).

Shaffer, A.L., et al. XBP1, downstream of Blimp-1, expands the secretory apparatus and other
organelles, and increases protein synthesis in plasma cell differentiation. Immunity 21(1): 81-93
(2004).

Shahmoradian, S.H., et al. Lewy pathology in Parkinson's disease consists of crowded organelles
and lipid membranes. Nature Neuroscience 22: 1099–1109 (2019).

Smith, J.J., Aitchison, J.D. Peroxisomes take shape. Nat. Rev. Mol. Cell Biol. 14(12): 803-817
(2013).

Taubenheim, N. Tarlinton, D.M., Crawford, S. Corcoran, L.M., Hodgkin, P.D., Nutt, S.L. High rate
of antibody secretion is not integral to plasma cell differentiation as revealed by XBP-1 deficiency.
J. Immunol. 189(7): 3328-3338 (2012).

Thaim, A.R., Farese Jr, R.V., Walther, T.C. The biophysics and cell biology of lipid droplets. Nat.
Rev. Mol. Cell Biol. 14(12): 775-786 (2013).

Toda, C., Kim, J.D., Impellizzeri, D., Cuzzocrea, S., Liu, Z.W., & Diano S. UCP2 Regulates
Mitochondrial Fission and Ventromedial Nucleus Control of Glucose Responsiveness. Cell
164(5): 872-83 (2016)

Vagne, Q. and Sens, P. Stochastic model of maturation and vesicular exchange in cellular
organelles. Biophysical Journal 114(14): 947-957 (2018)

Van Der Zand, A., Gent, J., Braakman, I. & Tabak, H. F. Biochemically distinct vesicles from the
endoplasmic reticulum fuse to form peroxisomes. Cell 149: 397–409 (2012).

Walther, T. C., Chung, J. & Farese Jr, R. V. Lipid droplet biogenesis. Annual review of cell and
developmental biology 33: 491–510 (2017).

Waterham, H.R., Janet Koster, J., van Roermund, C.W.T., Mooyer, P.A.W., Wanders, R.J.A., &
Leonard, J.V. A Lethal Defect of Mitochondrial and Peroxisomal Fission. *New England Journal of*
Medicine 356: 1736-1741 (2007).

Wilfling, F., Haas, J. T., Walther, T. C. & Farese Jr, R. V. Lipid droplet biogenesis. Current opinion
in cell biology 29: 39–45 (2014).

ACKNOWLEDGEMENTS

We thank D. Laman Trip, T. Maire, and H. Youk for critically reviewing our manuscript. K.A. was
supported by a fellowship from the Center for Science and Engineering of Living Systems at
Washington University in St. Louis.

AUTHOR CONTRIBUTIONS

S.M. conceptualized the project. K.A. performed the computational simulations and imaging
experiments, assisted by A.K. A.K. analyzed the image data, assisted by K.A., and prepared the
manuscript figures. K.A., A.K., and S.M. wrote the manuscript.

COMPETING INTERESTS

None declared.

METHODS
409
410 **Mathematical framework for growth with deterministic step sizes**

411 In our mathematical framework (**Fig. 1A**), solve for the dynamics of the probability of a state of
412 organelles in a single cell that undergo the following changes:

413 I. De novo synthesis of organelles from a given source of constituents within the cell with a
414 constant rate k_{denovo}

$$P(N, \vec{S_i}) \xrightarrow{k_{denovo}} P(N+1, \vec{S'}_{i+1})$$

416 II. Decay of organelles due to inheritance, maturation, autophagy, etc. at a rate γ per organelle
417 per time:

$$P(N, \vec{S_i}) \xrightarrow{N_\gamma} P(N-1, \vec{S'}_{i-1})$$

419 III. Creation of two organelles from a single organelle through fission at a rate $k_{fission}$ per organelle
420 per time:

$$P(N, \vec{S_i}) \xrightarrow{N k_{fission}} P(N+1, \vec{S'}_{i+1})$$

422 IV. Creation of a single organelle through the fusion of two organelles at a rate k_{fusion} per organelle
423 per squared time:

$$P(N, \vec{S_i}) \xrightarrow{N(N-1)k_{fusion}} P(N-1, \vec{S'}_{i-1})$$

425 V. Organelle size growth at a rate r_{growth} per time:

$$P(N, \vec{S_i}) \xrightarrow{r_{growth}} P(N, \vec{S'}_i)$$

427 VI. Organelle size decay at a rate k_{decay} per number of organelle constituents (size s) per time:

$$P(N, \vec{S_i}) \xrightarrow{s k_{decay}} P(N, \vec{S'}_i)$$

We initially assume that organelles grow in deterministic increments (packet sizes). In all three
limits, we assume that the rates of decay, fission, fusion, and shrinking are $N\gamma$, $Nk_{fission}$, $N(N$
$-1)k_{fusion}$, and $S_i k_{shrink}$ respectively, in which N is the number of organelles and S_i is the size of the
i^{th} organelle and S' refers to the size of each organelle in the new probability state. In the case of

constant growth, we assume that the growth and de novo synthesis rates are equal to their rate
constants respectively (i.e., $r_{denovo} = k_{denovo}$ and $r_{grow} = k_{grow}$). In the negative feedback model, we
assume that the de novo synthesis rate is equal to its rate constants, however the growth rate is
constrained by a feedback term

$$r_{growth} = \frac{(target\ size)^h}{1 + (target\ size)^h} k_{growth}$$

in which target size = $\frac{k_{growth}}{k_{decay}}$ and h is the Hill coefficient. Lastly, in the k_{decay} limiting pool model we
characterize the rate for de novo synthesis and organelle growth as $R_{denovo} = k_{denovo}N_{pool}$ and R_{grow}
= $k_{grow}N_{pool}$ respectively, in which N_{pool} is the free pool available for the organelles. Additionally,
we assume that the pool is replenished by the process of organelle decay and shrinking.

In **Fig. S1A-F** we plot the trajectories of a single cell reaching steady-state for the three limits of
our framework, in a regime where the abundance of organelles change through de novo
synthesis, fission, and first order decay, and in a regime in which organelle abundance changes
solely through fission and fusion.

To obtain additional insight about the three limits of our model, we sweep through a large
parameter space and simulate 1000 cells. From each simulation we obtain the slope of the plot
of average organelle sizes vs. organelle abun- dance. Finally, we plot the histogram of the
recorded slopes by increasing fission rate (purple represents a fission rate of zero and red
represents the highest fission rate in our simulations). Comparing the slope histograms, we
observe a zero slope for almost all parameter sets in the negative feedback model and a negative
slope for all parameter sets used to simulate the limiting pool model. However, we notice that in
the constant growth model, the slopes become increasingly negative as fission rates increase
(**Fig. S2G-2I**). We implement this information to learn about peroxisomal growth. In wildtype
yeast, we consider peroxisomes to undergo de novo synthesis, fission, and first order decay. Our
measurement of the wildtype data results in a negative correlation between average size and
abundance of peroxisomes (**Fig. 1**). However, this can only help us rule out the negative feedback
control model, as we expect a negative correlation between number and average organelle size
at high fission rates in the constant growth model. In order to determine the correct model to
describe peroxisomes, we engineered strains of yeast with their peroxisomal fission factors
deleted, while grown in medium rich in long chains of fatty acid. Peroxisomes undergo fission
when grown in oleic acid. We observe that even in the strain with the *VPS1* gene deleted (*VPS1*
being the quantitatively most significant of all fission factor deletes, Ref. 1), the correlation
between the abundance and average peroxisome size is still negative in **Fig. S6**. This argues
against constant growth as the underlying mechanism for peroxisomal growth, suggesting that
peroxisomes grow from a limited pool of building blocks.

Experimental methods

<u>Strains</u>

Saccharomyces cerevisiae strain BY4742 was obtained as a kind gift from H. Zaher. Cells were
transformed by standard lithium acetate methods to fluorescently labelled indicated organelles
with monomeric Kusibara Orange 2 (mKO2) obtained from Addgene (Cambridge, MA).

Peroxisomes in strains engineered with deletions of *DNM1, FIS1,* and *VPS1* were visualized as
in Ref. 1.

For glucose medium, strains were grown to mid-log phase at 30°C in standard synthetic medium
containing 2% glucose and subsequently imaged. For oleic acid medium, strains were grown to
mid-log phase at 30°C in standard synthetic medium containing 2% glucose, washed twice, and
resuspended in medium containing 0.3% yeast extract, 0.6% peptone, 0.1% glucose, 0.1%
Tween40, and 0.2% oleic acid, cultured for 20 hours in the oleic acid rich medium, and
subsequently imaged.

Imaging Conditions

482 Wildtype strains were imaged with a Nikon Ti2 microscope using a Hamamatsu Orca Flash v3
483 scientific CMOS camera with standard TRITC emission and excitation filter cubes. The exposure
484 time for the samples ranged from 50 - 250ms. Strains engineered with deletions of *DNM1, FIS1,*
485 and *VPS1* were imaged as in Ref. 1.

Image Processing

Custom Matlab code was written to segment, filter, binarize, and compute sizes of all organelles.
Cellular segmentation was semi-automated and varied between datasets. For the confocal
images, segmentation was performed by hand with ImageJ. For the camera images, cell
segmentation was performed by labeling the cellular cytoplasm with YFP, whose image was
binarized to identify those pixels belonging to each cell. Following cell segmentation, 3D images
of organelles were extracted from the field of view to be measured individually and deconvolved
(**Fig. S3**). Two thresholding processes were used, dependent upon the morphology of the
organelle. For the globular structures (lipid droplets, peroxisome, and Golgi) the filtering began
with a weak Gaussian blur followed by taking the Laplacian of the image. Ultimately, the threshold
for binarization was picked by hand and confirmed by eye. For the tubular structures
(mitochondria) we used the Hessian based "Frangi Vesselness" filter (available on
mathworks.com); the threshold was again picked by hand and confirmed by eye. After applying
the filters corresponding to the given structure's morphology (globular or tubular), the organelle
images from each cell are binarized one z-slice at a time (**Fig. 1B**). Z-slices are then reconstructed
to form a 3D image of the cell and built-in Matlab functions are used to identify individual
organelles and count their voxels (**Fig. S3**).

To test the robustness of the analysis pipeline to choice of threshold, we perform two analyses.
First we show that the measured average intracellular CVs for a population of the given organelle
type where Threshold 2 is 10% greater than Threshold 1 are highly correlated between the
thresholds (**Fig. S7**). Second, we observe no correlation between the average pixel intensity of a
given organelle and its size, eliminating a possible source of artefactual size variation due to
differences in fluorescent protein concentration; shown here is data on the late Golgi (**Fig. S4**).
Finally, to test that our spatial resolution following deconvolution was sufficient to detect variation
in organelle size and not be truncated by diffraction, we measured the fraction of organelles in
our dataset that were indistinguishable in size from a diffraction limited, 100nm Tetraspeck bead
(Thermo Fisher T7279), whose image data was processed in the same way outlined in
Supplementary Fig. 6, with the modification of being carried out without the cell segementation

step. For the images collected with a camera, we report the proportion of organelles from all cells
that fall at the diffraction limit (**Fig. S5**). In the vast majority of cases, this proportion is below 10%
(**Fig. S5**, numbers above individual violin plots).

Mathematical framework for growth with burst-like step sizes

In the revised mathematical framework describing burst-like steps of organelle growth, the
number changing processes (Equations I-IV above) and the organelle shrink process (Equation
VI above) from the initial model remain unchanged. The growth process has two modifications:
first the rate of growth is given as a constant "burst frequency" parametrized by α, second the
growth increment is itself a random quantity described by an exponential distribution parametrized
by a "burst size" β. As shown by Friedman et al. (Ref. 2), the steady state distribution of organelle
sizes resulting from these stochastic processes, assuming that the number dynamics are slow
compared to the size dynamics, is a gamma distribution:

$$p(S) = \frac{1}{\Gamma(\alpha)\beta^\alpha} S^{\alpha-1} e^{-S/\beta}$$

In the model, we note the burst size itself varies according to how much free pool of building
blocks is available for growth; namely $\beta = \beta_0 N_{pool}$. Intuitively, therefore, an increased number of
organelles will lead to a smaller average organelle size as the fraction of building blocks held in
organelles and away from the pool is greater, thereby reducing the burst size.

In order to collapse the data onto organelle-specific gamma distributions, we can rescale the
organelle sizes by their corresponding burst sizes. We define a new random variable

$$\tilde{S} = S/\beta$$

534   Then by the chain rule:

$$p(\tilde{S}) = \frac{1}{\Gamma(\alpha)} \tilde{S}^{\alpha-1} e^{-\tilde{S}}$$

536   where each organelle-specific gamma distribution is parametrized by its organelle-specific burst
537   frequency alpha. In order to further collapse all organelle data onto a universal master curve, we
538   can rescale $p(\tilde{S})$ by multiplying by a factor of $\Gamma(\alpha)/\tilde{S}^\alpha$ to remove any dependence of the right-
539   hand size on α. The resulting scaling relationship is the dimensionless curve plotted in **Fig. 2H**:

$$f(\tilde{S}) = e^{-\tilde{S}}/\tilde{S}$$

541   <u>Figure schematics</u>

542   Figure schematics in Fig. 2A and Fig. 3A were performed using images from BioRender.

Fig. 1: A) Schematic of mathematical framework. De novo synthesis of organelles, fission, fusion, organelle growth, shrink, and organelle decay occur at rate constants k_{denovo}, $k_{fission}$, k_{fusion}, k_{grow}, k_{shrink}, and γ respectively. Mean organelle sizes vs. number of organelles from 1000 simulated cells at steady state in a regime where organelle abundances change through **B**) de novo synthesis and first order decay, **C**) de novo synthesis, fission, and first order decay, and **D**) fission and fusion. The red, green, and blue dots correspond to the constant growth, negative feedback, and limiting pool regime of our model. Experimental measurements of mean organelle size vs. number of organelles for fluorescently labelled **E**) Golgi body, **F**) lipid droplets, **G**) peroxisomes, and **H**) mitochondria. Average intracellular coefficient of variation (CV) of organelle sizes for **I**) late Golgi, **J**) lipid droplets, **K**) peroxisomes, and **L**) mitochondria; insets represent the predicted CV from our limiting pool model, and the blue stars correspond to the measured CV of diffraction-limited fluorescently labelled 100nm Tetraspeck microspheres.

Fig. 2: A) Schematic depicting model of burst-like growth in organelle size in the limit of large number available of building blocks for organelle growth compared to the typical size of growth bursts. **B)** Organelle size distributions predicted from burst-like organelle growth model under either modulation of burst frequency (purple histograms) or burst size (orange histograms). **C)** Organelle size fluctuations as a function of mean organelle size under burst frequency (purple curve) or burst size (orange curve) modulation. **D)** Histograms of experimentally measured late Golgi, lipid droplet, and peroxisome sizes. **E)** Histograms of late Golgi, **F)** lipid droplet, and **G)** peroxisome sizes from (**D**) rescaled by their experimentally derived organelle-specific burst sizes β; insets are the corresponding total organelle size as a function of number of organelles. **H)** Histogram of organelle size distributions rescaled by both experimentally derived organelle-specific burst sizes β and burst frequencies α; black curve is the theoretically predicted scaling relationship from the model, $f(s) = e^{-s}/s$.

Fig. 3: A) Schematic depicting model of burst-like growth in organelle size in the limit of a similar number of available building blocks for organelle growth compared to the typical size of growth bursts. **B)** Theoretical prediction of total organelle size V as a function of the number of organelles in the limits where the pool is exhausted (pink line) versus non-exhausted (maroon line) **C)** Average intracellular CV of organelle sizes in 1000 simulated cells from burst-like model, when pool is not depleted versus when pool is depleted. Total organelle size **D)** and **E)** average intracellular size CV of late Golgi from populations of wildtype (maroon) and *ΔARF1* (purple) cells. **F)** Total organelle size and **G)** average intracellular size CV of lipid droplets from populations of wildtype cells grown in glucose (maroon) and in medium with 0.2% oleic acid (pink). **H)** Total organelle size and **I)** average intracellular size CV of peroxisomes from populations of wildtype cells grown in glucose (maroon) and of wildtype (pink) and *ΔVPS1* (purple) cells grown in medium with 0.2% oleic acid.

Fig. 4: A) Average Golgi size versus number of Golgi from images of single induced pluripotent stem cells taken from the Allen Cell Atlas. **B)** Average Golgi intracellular size CV versus average Golgi size. **C)** Average mitochondrial size versus number of mitochondria from images of single induced pluripotent stem cells taken from the Allen Cell Atlas. **D)** Average mitochondrial intracellular size CV versus average mitochondrial size.

FIGURE SUPPLEMENTS

Fig. S1. In the regime where organelle abundances change through de novo synthesis, fission
and first order decay **A**) trace of a simulated single cell in the limit of constant growth **B**)
negative feedback control, and **C**) limiting pool, from t=0 (circle) to steady-state (square). In the
regime where organelle abundances change through fission and fusion **D**) trace of a simulated
single cell in the limit of constant growth **E**) negative feedback control, and **F**) limiting pool, from
t=0 (circle) to steady-state (square).

613
614
615 **Fig. S2.** Histograms of slopes relating average simulated organelle size and organelle number
616 obtained from sweeping through a large parameter space from kfission = 0 to high fission rates
617 for **A**) the constant growth, **B**) negative feedback, and **C**) limiting pool model.
618

627
628
629
630 **Fig. S3. A**) After semi-automated segmentation, individual cells are extracted from a given field
631 of view. **B**) After applying the filters corresponding to the given structure's morphology (globular
632 or tubular), each cell is binarized one z-slice at a time. **C**) Z-slices are then reconstructed to
633 form a 3D image of the cell and built-in Matlab functions are used to identify individual
634 organelles and count their voxels.
635
636

637
638 **Fig. S4.** Scatter plot of late Golgi, labelled by Sec7-mKO2, average pixel intensity versus
639 measured late Golgi size.
640
641

644 **Fig. S5.** Proportion of organelles fall at the diffraction limit (computed by measuring the size of a
645 diffraction-limited 100nm Tetraspeck microsphere bead). Floating numbers above data points
646 are proportion of organelles from cells in a subpopulation with defined number of organelles that
647 falls at the diffraction limit.

650
651
652
653

A **B** **C**

654
655
Fig. S6. Average of mean peroxisome sizes as a function of peroxisome number in strains grown in medium rich in oleic acid with their peroxisomal fission factors **A**) *DNM1* , **B**) *FIS1* , and **C**) *VPS1* deleted.

659
660

661
662
663
664 **Fig. S7.** Sensitivity analysis of measured average intracellular coefficient of variation to choice
665 of threshold. Threshold 1 is the threshold used for image analysis whose results are presented
666 in Fig. 1, 2, and 3. Threshold 2 is a 10% higher pixel intensity threshold. **A**) Tom70-mKO2, **B**)
667 Sec7-mKO2, **C**) Sec7-mKO2 Δ*ARF1*, **D**) Erg6-mKO2, **E**) Erg6-mKO2 (oleic acid), **F**) Pex3-
668 mKO2, **G**) Pex3-mKO2 (oleic acid), **H**) Pex3-mKO2 Δ*VPS1*
669
670
671

Fig. S8. Single organelle size distributions and corresponding gamma distribution fits to the **A)** late Golgi apparatus in Sec7-mKO2 strains, **B**) late Golgi in Sec7-mKO2 strain with *ARF1* deleted, **C**) lipid droplets in Erg6-mKO2 strains grown in glucose, and **D**) in medium rich in oleic acid, **E**) peroxisomes in Pex3-mKO2 strains grown in glucose, **F**) in medium rich in oleic acid, and **G**) strain with *VPS1* deleted and grown in medium rich in oleic acid.

683
684

685
686
687 **Fig. S9.** Total organelle volume vs. number of organelles plot of **A**) mitochondria (red) and **B**)
688 result of bursty model (blue) with organelle numbers changing through fission and fusion. **C**-**L**)
689 distribution of mitochondria (red) and simulated organelles (blue) sizes from subpopulations of
690 cells with defined mitochondrial copy numbers.

692
693
694 **Fig. S10.** Comparison of cell size coefficient of variation in the wildtype strain versus a strain
695 carrying a deletion of *ARF1*, which exhibits an increased average intracellular coefficient of
696 variation in late Golgi sizes. Cells were binned into 3 quantiles according to their average late
697 Golgi size, their sizes were estimated using their area as measured by a YFP fluorescent
698 marker for their cytoplasm, and the CV was computed from the resulting cell size distributions.