Precise coupling of the thalamic head-direction system to hippocampal ripples

Guillaume Viejo[1] and Adrien Peyrache[1,*]

[1]*Montreal Neurological Institute, McGill University, Montreal, QC, Canada;*
[*]Corresponding author: adrien.peyrache@mcgill.ca

Abstract

The anterior thalamus is a key relay of neuronal signals within the limbic system. During sleep, the occurrence of hippocampal sharp-wave ripples (SWRs), believed to mediate consolidation of explicit memories, is modulated by thalamocortical network activity, yet how information is routed around SWRs and how this communication depends on neuronal dynamics remain unclear. Here, by simultaneously recording ensembles of neurons in the anterior thalamus and local field potentials in the CA1 area of the hippocampus, we show that the head-direction (HD) cells of the anterodorsal nucleus are set in stable states immediately before SWRs. This response contrasts with other thalamic cells that exhibit diverse couplings to the hippocampus related to their intrinsic dynamics but independent of their anatomical location. Thus, our data suggest a specific and homogeneous contribution of the HD signal to hippocampal activity and a diverse and cell-specific coupling of non-HD neurons.

Introduction

Thalamocortical loops form the canonical circuits of the most complex cognitive functions [1, 2, 3, 4]. The dorsal thalamus (henceforth referred to as the thalamus for simplicity) is organized in a large family of cytoarchitectonically-defined nuclei [1]. Those of the anterior thalamic nuclei (AT) are located at the central stage of the Papez circuit [5] and play a key role in memory [6, 7], spatial navigation [8, 9, 10], and arousal states [11, 12]. However, the functional integration and dynamics of AT neurons in the limbic system remain elusive.

The role of AT in navigation is indicated by the presence of head-direction (HD) neurons, which discharge when the animal is facing a particular direction and are primarily located in the anterodorsal (AD) nucleus [8, 10]. HD cells of the AD are necessary for the establishment of higher level spatial representation in the brain's navigation system, for example the grid cells of the medial entorhinal cortex [9].

The relationship between neuronal activity and memory in the AT remains elusive. In contrast, this relationship has now been clearly established in the hippocampus. Non-Rapid Eye Movement (NREM) sleep is instrumental for memory consolidation [13]. During NREM sleep, the hippocampal activity patterns that form during exploration are replayed [14], thus recapitulating spatial trajectories in the environment [15, 16]. These replay events are associated with SWRs in local field potentials (LFPs) [17] and are necessary for memory [18, 19, 20]. However, it remains unclear whether this phenomemon is entirely generated within the hippocampus or is influenced by its inputs.

During NREM, the timing of SWRs is orchestrated by thalamocortical dynamics [21, 22, 23, 24], especially the thalamocortical slow oscillations that arise from the fluctuation of membrane potentials between UP and DOWN states (corresponding to active and silent states, respectively) [25]. The AD is a key hub for the propagation of the slow oscillation

[12], suggesting that HD cells play a role in coordinating neuronal activity within the limbic system during NREM.

The contribution of AD HD cells in offline processing of spatial signals is further demonstrated by the fact that HD cells remain coordinated during sleep [10, 26]) and that they lead their main cortical targets (in the post-subiculum), independent of brain states [27]. This suggests that during sleep, AD neurons continue conveying a coherent HD signal to the navigation system, including the hippocampus [28].

The role of the other AT nuclei in coordinating activity in the limbic system and how this activity relates to neuronal dynamics is still unclear. One challenge when investigating thalamic function is that, while each nucleus is characterized by specific connectivity with other brain areas, exact input/output patterns can differ across neurons from the same anatomically-defined nucleus [1, 29]. Furthermore, the firing of thalamic neurons is often believed to be homogeneous (e.g. burst firing during NREM sleep [30, 25]), yet variability in spike train dynamics has been previously reported [31, 32].

By simultaneously recording thalamic neuronal activity and hippocampal LFPs in freely moving and naturally sleeping mice, we first addressed the question of how AT neurons are coupled to SWRs, specifically HD cells in comparison to other AT neurons. Then, we examined how the variability in this coupling correlates with intrinsic properties of AT neurons, as determined from spike train dynamics across brain state and timescales. We show that HD cells were specifically coupled to SWRs, increasing their gain and settling into stable directions before SWRs. Furthermore, HD cells of the AD nucleus (the majority of cells in this nucleus) form a very homogeneous population of neurons, both in coupling to hippocampal dynamics as well as in intrinsic dynamics. Non-HD cells offer a striking contrast: their modulation by hippocampal SWRs and intrinsic dynamics were highly diverse and could tremendously vary even for proximal neurons of the same nucleus.

Results

The HD signal is precisely coupled to SWRs.

We performed recordings of the anterior thalamus (n=2016 AT neurons) in freely moving mice in an open environment, while they foraged for food, and in their home cages during sleep periods that preceded and followed exploration. Neurons were classified as HD cells by measuring the modulation of firing rate with respect to the direction of the head of the animal in the horizontal plane (n=161 HD cells; see Methods). The tuning curves of 24 simultaneously recorded HD cells are shown in **Fig. 1a**.

HD cells of the AT are believed to convey a coherent signal to the parahippocampal system during sleep [10, 27, 28]. We thus made the prediction that the HD system provides the hippocampus with a specific direction during SWRs in which place cell ensembles replay previously formed patterns associated with spatial trajectories [15, 16]. To this end, we simultaneously recorded LFPs in the pyramidal layer of the dorsal CA1.

Around the occurrence of SWRs only a subset of HD neurons fired, and these neurons demonstrated a similar preferred HD (**Fig. 1b**). To better visualize this effect, we first uncovered the topology of population firing using ISOMAP (see Methods) [26]. This non-linear dimensionality reduction method revealed the embedding of HD cell population vectors, and was computed without knowledge of the behavioral correlates (i.e. the HD tuning curves). During wakefulness, this topology had a ring structure with the relative angular position along the ring clearly mapping the animal's HD (**Fig. 1c**). While population activity was restricted to the ring during wakefulness (the center of the ring corresponds to 'forbidden states'), its intrinsic dimensionality increased during NREM activity, as seen by the scattering of population vector embeddings, in particular at the center of the ring.

Figure 1: Stability of head-direction decoding before SWRs. (**a**) Tuning curves of head-direction neurons recorded simultaneously from the AD nucleus. (**b**) Simultaneous recording of LFP in the CA1 pyramidal layer (*top*) and neuronal activity of the same neurons as in **a** around the time of SWRs during NREM sleep. Spikes from HD neurons are sorted according to their preferred direction during wakefulness (as in **a**). Red asterisks indicate SWRs. (**c**) Two-dimensional embeddings (using ISOMAP) of HD neuronal population activity during wakefulness (colored points) and around the times of SWRs (grey points) for the same session as in **a** and **b**. Lines display the embeddings of three examples from **b** (red asterisks as in **b**). (**d**) Average normalized radii (i.e. distance from embedding centers relative to shuffles) around times of SWRs (grey lines; n=7 session, 3 animals) and session-wide average (black line). (**e**) Same as (**d**) for angular velocity (i.e. angular displacement between two consecutive activity bins). (**f**) Average density of spikes (± sem) for simultaneously recorded HD (black) and non-HD (grey) neurons, and rate of occurrence of SWRs (red line) during DOWN and UP states (normalized time).

This apparent violation of the intrinsic topology resulted from the modulation of network activity by the slow oscillation [25, 26].

The population activity around times of SWRs correspond to trajectories within the projection space. In the three cases of **Fig. 1b**, activity started near the ring's center (corresponding to putative DOWN states) and settled on fixed points in the outer part of the ring (corresponding to "allowed" states during wakefulness) at the time of SWRs.

To quantify population states around SWRs and across sessions, the population vectors at each time bin were expressed in polar coordinates by taking the center of the ring as the reference point. We analyzed data sets that included more than 10 HD neurons recorded together and showed a clear ring topology during wakefulness (n=7 sessions, 3 animals, see **Supplementary Fig. 1**). For all sessions, the radius of the trajectories peaked around times of SWRs compared to baseline (see Methods) (**Fig. 1d**). The radii peaked before SWR peaks (-17ms ± 6ms; t=-2.82, p=0.03; t-test). Was the angular position stable or

was it drifting at these times? To address this question, we computed the relative angular velocity of the signal (i.e. angular displacement relative to a baseline). Angular velocity was minimal around SWRs (**Fig. 1e**), and, similar to the radius, reached its minimum before SWR peaks (-18ms $\pm$ 15ms; t=-2.88,p=0.02; t-test excluding SWRs occurring less than 100 ms after UP onset). Similar results were obtained upon using Bayesian decoding of angular position (i.e. a decoding based on HD tuning curves; see **Supplementary Fig. 2**) [33, 10].

It is possible that the stabilization of the network into particular states results from the increase of HD population firing. However, these two aspects of HD cell population activity seem independent as HD cell population outside of SWRs showed fast sweeps at high population firing rates (i.e. on the outer ring of the population activity topology) [26]. Hence, the increase in gain and the stabilization of the network into particular states is characteristic of epochs preceding SWRs.

The coupling between HD neuronal population and SWRs could result from non-specific coordination of SWRs with slow oscillations [23, 22, 34], in particular at the transition between DOWN and UP states. To test for this possibility, we first detected putative DOWN and UP states from ensemble activity (composed of HD and non-HD neurons) (**Fig. 1f**). We did not see any change in the probability of SWR occurrence around DOWN/UP transitions of AT activity, but instead saw a constant rate of SWR occurrence during UP states (**Fig. 1f**). If anything, SWRs were slightly less observed during early onset of UP states. Here, UP and DOWN state duration was normalized. When the modulation of SWRs by the slow oscillation was examined with a cross-correlation analysis, SWRs seemed more prominent at the beginning and end of the UP states (**Fig. 1f**, inset). However, this analysis primarily reflects the distribution of UP state duration and not a preferred phase within UP states. Finally, we asked whether the co-occurrence of SWRs and stable HD signal was biased by their relative position within UP states. SWRs were clustered according to the time elapsed since the UP state onset. No difference was observed in the time-lags of the radius peaks and minima of angular velocity relative to SWRs. The only exception was for SWRs occurring in the first 200 ms of UP state as the system which is certainly more governed by dynamics relative to the transition from the DOWN states (**Supplementary Fig. 1b-c**).

In conclusion, SWRs were specifically preceded by high-activity and stable HD population states, independent of the coordination between the thalamocortical slow oscillation and SWRs.

Thalamic HD cells are homogeneously coupled to SWRs.

The coupling of the HD network to SWRs raised the question of whether this was specific to HD neurons in the AT or not. Non-HD AT neurons were recorded at increasing dorsoventral depth from session to session (**Fig. 2a**), thus spanning most AT nuclei, not only the most dorsal nuclei adjacent to AD. Taking advantage of multiple channels and geometry of silicon probes, we were able to reconstruct the putative tracks of each shank across the AT (**Fig. 2b**). The position of the probes was calibrated along the dorso-ventral axis by the first appearance of spiking activity on at least one shank (indicating the dorsal border of the thalamus) and along the medio-lateral axis by matching the highest density of HD neurons with the AD nucleus [8, 10])(**Fig. 2b** and **Supplementary Fig. 3**).

As no particular behavioral correlates, and even less topology of the population activity could be assumed for non-HD neurons, we first analyzed neuronal activation around times of SWRs on a cell-by-cell basis. Similar to the potential caveat of HD cell population analysis (**Fig. 1**), a challenge when evaluating neuronal responses to SWRs with cross-correlation analysis is that SWRs are co-modulated with the slow oscillation [25, 23, 22, 21, 24]. To isolate the specific responses of neurons to SWRs, cross-correlograms were

Figure 2: Homogeneous coupling of HD, but not non-HD neurons to SWRs. (**a**) Histology of an example mouse (Mouse 17, DAPI staining). Note the tracks of the eight-shank silicon probe and lesion sites at the end of the tracks. Contour of the AD nucleus is shown in red. (**b**) Schematic of the AT (coronal plane) with recording sites (black dots) for the same animal as in **a**. Red dots indicate where HD neurons were detected. (**c**) *Top*, spikes for successive SWRs. *Middle*, mean firing rates. *Bottom*, z-scored modulation (see text) for one HD neuron (red) and 2 non-HD neurons (grey) differently modulated by SWRs. (**d**) Average SWRs modulation for HD (red) and non-HD neurons (black) for all sessions. *Middle,bottom* Matrix display of all SWRs modulation for both groups. Neurons were sorted according to the value of SWR modulation at zero-time lag. (**e**) Examples of SWR modulation for HD (*Top*) and non-HD neurons (*Middle*) recorded during the same sessions but within different shanks. The session anatomical localization is shown in (**b**) with an arrow. *Bottom* Pearson's correlation coefficients between SWRs modulation of pairs of neurons recorded on the same shanks. Red dots indicate pairs of HD neurons. (**f**) Distribution of Pearson's correlation coefficients between SWR modulation of pairs of HD (red) and non-HD (grey) neurons (similar to **e**) for all sessions. Abbrev. AD, anterodorsal; AM, anteromedial; AVd, anteroventral, dorsomedial part; AVv, anteroventral, ventrolateral part; IAD, interanterodorsal; LD, laterodorsal; MD, mediodorsal; PV, paraventricular; sm, stria medullaris; VA, Ventral anterior.

compared to a baseline expected in the condition of an absence of fast co-modulation between neuronal spikes and SWRs (within ± 150ms, corresponding to the typical duration of a sharp-wave; see Methods). Cross-correlograms were then expressed in a number of standard deviations (z) from these null distributions.

Three example neurons (including one HD neuron) showed different co-modulation with SWRs (**Fig. 2c**). The average SWR modulation of HD neurons shows a clear population response with a highly synchronized increase of firing before the SWRs (**Fig. 2d**), thus confirming the specific coupling of the HD signal to the SWRs (**Fig. 1**). On the contrary, non-HD cells showed various modulatory responses around the time of SWRs which resulted in a near-uniform average modulation. While this observation suggests that unlike HD cells, non-HD cells do not act as a synchronized population immediately before SWRs, the non-HD set was recorded from different nuclei of the AT (**Fig. 2b**). It is thus possible that, locally, some nuclei show the same coupling to SWRs as the HD neurons of AD. To rule out this possibility, we computed pairwise correlations of neurons recorded on the same shanks, assuming that those neurons were in most cases from the same nuclei. As shown in **Fig. 2e**, a session containing HD and non-HD neurons, SWR modulation of non-HD neurons was more heterogeneously distributed than for HD cells. This locally

inhomogeneous response of non-HD cell population to SWRs compared to HD neurons was confirmed by computing the distribution of pairwise correlation within all shanks and across sessions (**Fig. 2f**; n=7234 pairs, 58 sessions, t=-18.08, p=10^{-71}, t-test).

It can thus be concluded that HD neurons (and, by extension, neurons of the AD nucleus) play a specific and homogeneous role in the timing of SWRs. On the contrary, the activation of other neurons of the AT around the time of SWRs is highly variable, even within local networks (presumably within nucleus).

Temporal modulation with the hippocampus is brain-state invariant.

Figure 3: Relationship between temporal coupling of AT neurons to SWRs and modulation by theta oscillations. (**a**) Example of a simultaneous recording of LFP in the CA1 pyr. layer (*top*) and neuronal activity in the AT (*bottom*) during REM sleep. Red ticks indicate spikes from HD neurons, sorted according to their preferred direction during wakefulness. (**b**) *Top*, spikes for successive theta cycles. *Bottom*, histograms of spike density within theta cycles for three example neurons during REM sleep. (**c**) Theta modulation versus SWR energy for all neurons (red points indicates HD neurons). Side panels indicate distribution of each group. "Theta mod." (blue distributions) indicates the group of neurons significantly modulated by theta (p < 0.01). (**d**) Density map of theta-modulated neurons (min=0.016) for one mouse. Note the absence of theta modulation for AD. (**e**) Z-scored SWR cross-correlograms for all theta-modulated AT neurons (equivalent to the group theta-mod in **c**). Neurons are sorted according to their modulation at SWR peaks. (**f**) First two jPC vectors (black and grey) of SWR cross-correlograms. (**g**) Projection of individual SWR cross-correlograms onto the first two jPCs. Point colors indicate 0-lag modulation (same color code as in **e**). Grey arrows indicate corresponding SWR-jPCA phase for four example neurons (green points, *a* to *d*). Theta phase distributions for the same 4 neurons are shown at each corner. (**h**) SWR-jPCA phase as a function of Theta phase (r = 0.18, p<0.001, circular correlation). The four example neurons are shown in green.

What is the origin of the high variability in the coordination of AT neurons with SWRs? These interactions certainly depend on the input/output connections of each neuron. In the

case of a hard-wired network, we hypothesized that the coordination of AT neurons with hippocampal activity should not depend on brain states. During wakefulness and REM sleep, the hippocampus is dominated by theta oscillations (6-9 Hz) [35] which modulate neurons in the entire limbic system [35], including in the AT [36]. We thus tested for a relationship between SWR modulation (during NREM) and phase coupling to theta oscillation (during wakefulness and REM sleep) (**Fig. 3a**).

The firing of AT neurons relative to theta was analyzed, as commonly done, in terms of preferred phase and modulation amplitude. Three example AT neurons, recorded simultaneously but on different shanks of the probe, showed different modulations by theta, both in amplitude and preferred phase (**Fig. 3b**). Overall, 38% of all AT neurons were significantly modulated by theta rhythm during REM sleep (n=767/2016, p<0.001). This proportion was lower during wakefulness (n=333/2016, p<0.001).

How can theta modulation be compared to SWR responses? We first quantified the "SWR energy", defined as the variance of the normalized cross-correlograms (as in **Fig. 2**). SWR energy and theta modulation amplitude were correlated for the ensemble of AT neurons (**Fig. 3c**; r=0.81, p<0.014, Pearson's correlation). The similar modulation intensity with hippocampal dynamics across brain states possibly reflects the strength of inputs to each AT neuron from the parahippocampal area, potentially through multiple synaptic pathways. If so, this should also be reflected in the temporal response of each neuron.

Interestingly, HD neurons were overall not modulated by theta (only n=21/161 HD neurons). Thus showing once again that HD neurons of the AD nucleus form a homogeneous population of neurons, and certainly share the same input/output connectivity profile. Furthermore, the anatomical density of theta-modulated neurons revealed a clear segmentation: they can be found anywhere in AT except in the putative location of AD (**Fig. 3d**, see **Supplementary Fig. 2** for the three other mice).

Firing of AT neurons relative to SWRs cannot, overall, be trivially described (e.g. excited or inhibited). Rather, they show a wide range of temporal profiles (**Fig. 3e** for theta-modulated neurons). While modulation by oscillations is commonly characterized in terms of phase preference, such description for modulation by SWRs is lacking. To fully account for this variability, z-scored cross-correlograms of thalamic neurons relative to SWRs were projected onto a basis (jPCA, [37]) that captures the dynamical properties of the responses, assuming a quasi-oscillatory modulation in one sharp-wave cycle (**Fig. 3f**). In the two-dimensional jPCA projection space, each neuron can be attributed a "phase" that corresponds to the angle from the positive direction on the first jPC axis. The resulting phases were, for four example neurons, in good agreement with their preferred phase to theta oscillations (**Fig. 3g**, note that arrows point towards similar directions for theta and SWR phases). In the population of AT neurons that were significantly modulated by theta, theta phase was correlated with SWR phases (**Fig. 3h**; r=0.18, p=2.3 x 10^{-7}, circular correlation). Hence, AT neurons were similarly modulated, both in amplitude and in time, by hippocampal population dynamics in all brain states, thus revealing an invariant property at the circuit level.

A link between spike train dynamics and coordination with hippocampal activity.

Although the relationship between the modulation of individual AT neurons by hippocampal dynamics and their detailed connectivity profile is intractable *in vivo*, does this modulation depend on other intrinsic neuronal characteristics available from extracellular recordings? Spike train dynamics, which are well captured by auto-correlation functions (or "auto-correlograms"), reflect the complex interaction between morphological, input, and membrane properties. HD neurons exhibit quantitatively different auto-correlograms during wake, REM, and NREM sleep. Yet, as shown for two example HD neurons, response to

Figure 4: Covariation between single-cell spike train auto-correlograms and SWR cross-correlograms. (**a**) SWRs cross-correlograms (*top left*) and auto-correlograms across brain states (*bottom*) for two example HD neurons. Circular plots (*top right*) indicate HD tuning curves. (**b-c**) Same as **a** for three non-HD neurons recorded simultaneously on the same shank. *Top right,* average waveforms on the eight recording sites of the shank, from dorsal (**top**) to ventral (**bottom**) positions. The grey neuron is the same for both panels. Note that, although the cell bodies of the two neurons in **c** are close to each other (see waveforms), auto-correlograms and responses to SWRs are strikingly different. (**d**) Same as **a-c** but for three neurons recorded on different shanks and different sessions in the same animal. Their anatomical location is shown on the left-side map of the anterior thalamus. (**e**) PCA projections of first 20ms of auto-correlograms (*top*) and SWR cross-correlograms (*bottom*) for the three example neurons of **b-c**. (**f**) Correlation matrix between the two series of PCA weights (*left*) and for shuffled neuronal identities (*right*) for all neurons. ρ^2: total correlation. (**g**) Distribution of total correlation ρ^2 for actual (red line) and for random shuffling of cell identities (1000 times) between all cells irrespective of shank and recording days (black) and between cells recorded on the same shank on a given day (grey). (**h**) Distribution of total correlation ρ^2 for actual (vertical lines) and shuffled data between SWRs and auto-correlograms from wake (red), REM (light blue) and NREM (dark blue). Dashed line shows correlation between SWRs and stacked auto-correlograms of all epochs (same as in **g**). (**i**) Same as **h** but for cell identities shuffled within shanks.

SWRs and auto-correlograms are similar (only their firing rates, and thus absolute levels of auto-correlation are different; **Fig. 4a**). Examination of three non-HD example neurons recorded simultaneously and on the same shank illustrates that nearby neurons can share common properties, but can also be strikingly different (**Fig. 4b-c**). Specifically, a pair of simultaneously recorded neurons from a given shank had similar auto-correlograms and SWR cross-correlograms (**Fig. 4b**). On the same shank, a third nearby neuron (see anatomical distribution of waveforms), showed largely different spike train dynamics and opposite modulation by SWRs (**Fig. 4c**).

The previous examples suggest a high variability in both spike train dynamics and

response to SWRs, even within a given nucleus. Could these two properties of neuronal firing be related to each other? First, we asked the question of whether neurons showing the same response to SWRs across sessions (and, thus, anatomical locations) had similar auto-correlograms. This was indeed the case for the three example neurons shown in **Fig. 4d**. To further test for a possible relationship between individual spike train dynamics and SWR responses, we directly quantified the correlations between the two measures. To this end, principal component analysis (PCA) was used to reduce the dimensionality of the features (i.e. the number of time bins) of the first 20ms of auto-correlograms (from wake, REM and NREM epochs) and cross-correlograms with SWRs ($\pm$ 500ms). The first ten components were considered (explaining 99% and 91% of the variance of auto-correlograms and SWR cross-correlograms, respectively) (**Fig. 4e**). The correlation matrix of these weights had visibly more structure than the correlation matrix of PC weights in which neuron identities were shuffled (**Fig. 4f**) (the diagonal blocks of the full correlation matrix are not displayed because PCs are orthogonal to each other). In fact, the total correlation ρ^2 of PC weights was significantly higher than shuffles (**Fig. 4g**; $\rho^2 = 0.31$, p<0.001).

Shuffling neurons recorded simultaneously on a given shank led to a distribution of total correlation that was still significantly smaller than the actual total correlation (**Fig. 4g**), thus indicating that the relationship between spike train dynamics and response to SWRs is specific to each neuron rather than identical to nearby neurons. However, the within-shank shuffled correlations were higher than when cell identities were shuffled irrespective of recording days and shanks (t = -82; p = 10^{-10}), suggesting some similarity in both auto-correlation and SWR response within each nucleus. The strong correlation at the individual cell level cannot be accounted for by differences in firing rates ($\rho^2_{rate} = 0.3$ vs. $\rho^2 = 0.31$) nor in burstiness alone ($\rho^2_{burst} = 0.3$). Because SWR-associated firing could potentially bias the auto-correlograms during NREM, we repeated the analysis by considering auto-correlograms of only one brain state at a time. The total correlation remained significantly higher than shuffled data (p<0.001) when wake, REM, and NREM auto-correlograms were used separately (**Fig. 4h-i**). These results constitute a demonstration that intrinsic dynamics of individual AT neurons are directly related to their participation in circuit-level activity.

HD cells Have Unique Spike Train Dynamics While Non-HD AT Neurons Are Heterogeneous.

The link between spike train dynamics and coordination with SWRs, independent of the anatomical location of the neurons (except for HD cells), begs the question of whether there exists different sub-classes of neurons in the AT based solely on the distribution of spike train auto-correlograms. An example HD neuron (cell a in **Fig. 5a**) had a relatively short refractory period across brain states. It also showed a low level of burstiness, if any, during NREM (identified as a peak in the first 8 ms of the auto-correlogram; for the sake of simplicity, burstiness is reported only during NREM), in agreement with previous intracellular studies of AD neurons [32]. In contrast, example cell c in **Fig. 5a** showed a high level of burstiness, as expected for typical thalamic neurons during NREM [30, 25], and had a longer refractory period than the example HD neuron (cell a) during wakefulness and REM sleep. A third cell (cell b) showed intermediate properties, i.e. a long refractory period but a total lack of burstiness. We thus made the hypothesis that neurons can be segregated based on their auto-correlograms.

To visually determine the clustering of auto-correlograms, we used t-distributed stochastic neighbor embedding (t-SNE, [38]) to project the auto-correlograms from the three different brain states (i.e. three auto-correlograms per neuron) in a two-dimensional embedding. Instead of distinct groups, AT neurons were continuously distributed (along a gradient of

Figure 5: Variability and clustering of spike auto-correlograms in the AT. (**a**) Auto-correlograms of an HD (*a*), non-bursty (*b*) and bursty (*c*) neuron during wake, REM, and NREM epochs. (**b**) Clustering and t-SNE embedding of auto-correlograms (each point represents the stacked auto-correlograms from wake, REM and NREM of a neuron). HD neurons are marked with a white dot. The three example neurons from **c** are circled. K-means clustering of the auto-correlograms result in two clusters (see text). Cluster #2 is color-coded relative to burst index during NREM. (**c**) *Left,* 15 superimposed auto-correlograms of randomly selected cells from cluster #1 (normalized by the baseline between 50 and 100ms), during REM (*top*) and NREM (*bottom*) sleep. Color (white to dark red) indicates average firing rates (from low to high). Note the high similarity of auto-correlograms during REM sleep, independent of basal firing rates, and the mild variability during NREM sleep. (**d**) *Left,* density of cluster #1 (i.e. mostly HD neurons) and, *right,* mean burst index of cluster #2 over the anatomical schematics, for the same example mouse. (**e**) Distribution of Pearson's correlation coefficients between pairs of neurons recorded on the same shank showing the dynamical homogeneity of HD neurons compared to non-HD neurons. (**f**) Classification score of HD versus non-HD neurons (based on auto-correlograms) for increasing duration of auto-correlation. Score is relative to classifiers trained with shuffled data (0, chance level; 1, perfect classification).

burstiness, among other factors) with the exception of HD neurons that formed a separated "island" (**Fig. 5b**). To confirm this bimodal distribution, we applied the common clustering algorithm, K-means (with k=2), directly to the space of auto-correlograms. The first resulting cluster contained most of the HD neurons (99/127, p<0.001, binomial test). Within cluster #1, the shape of auto-correlograms was highly similar and independent of average firing rates (**Fig. 5c**). Moreover, the anatomical density of the neurons belonging to this particular cluster was concentrated around the putative location of the AD nucleus (**Fig. 5d**). These observations demonstrate that the dynamics of spike train emission, independent of excitability (i.e. firing rate), is sufficient to categorize HD neurons. There was not a direct match between cluster #2 and anatomy, as shown. For example, by the broad anatomical distribution of average burstiness. These observations were confirmed by the high level of correlation between auto-correlograms of neuronal HD pairs recorded on the same shanks. In contrast, pairs of non-HD neurons from the same shanks had less correlated auto-correlograms (**Fig. 5e**, t=18.32, p=10^{-73}, t-test).

How much information was sufficient to classify HD versus non-HD neurons? To address this question, we trained automatic classifiers, with auto-correlograms, to identify the distinction between HD and non-HD neurons. Specifically, we used gradient boosted trees (XGB, [39]), a robust and fast non-linear classifier, on a binary output (HD or non-HD). We train classifiers on auto-correlograms of various duration. Classification quality (or "score") was evaluated as a percentage from chance level (0%: chance level; 100%: perfect clustering). HD cells were labelled 50% above chance with only the first 6 ms of spike train auto-correlogram in each of the three brain states (**Fig. 5f**). This classification on such a

limited amount of information suggests that duration of the refractory period and level of burstiness are together unique to HD cells in the AT.

Together, these results provide evidence that HD neurons, in addition to their homogeneous response to hippocampal SWRs and unlike non-HD neurons, share common and specific dynamical properties. This further suggests that AD neurons are a distinct class of neurons in the anterior thalamus while non-HD neurons have broadly distributed properties, irrespective of their nucleus of origin.

Intrinsic slow dynamics of AT neurons distinguish HD and non-HD neurons.

Figure 6: Intrinsic slow dynamics during wakefulness and REM in the AT and its relation to fast dynamics during NREM. (**a**) Auto-correlograms of three neurons (HD and non-HD neurons) over long timescale (2.5 s) during wake. Dashed grey lines display exponential fit. (**b**) Decay time τ between wake and REM sleep. Red dots indicate HD neurons. Inset shows average ($\pm$ s.e.m.) decay time for HD and non-HD neurons during wakefulness and REM sleep. (**c**) Decay time τ during REM as a function of burst index during NREM (r = -0.374, p<0.001, Pearson's correlation). HD cells and non-HD cells are indicated by red and dark dots, respectively.

Although neurons showed a large spectrum of fast timescale dynamics (i.e. faster than 100ms), does that mean they were similarly activated during wakefulness on slow ("behavioral") timescales (i.e. on the order of seconds) [40]? These timescales correspond, for example, to the typical firing duration of an HD neuron as an animal rotates its head through the neuron HD tuning curves. For AT HD cells, these timescales are similar during wakefulness and REM sleep [10]. AT neurons showed a wide range of slow dynamics, not only during wakefulness, but also during REM sleep, as observed in the various decay times of their auto-correlograms (**Fig. 6a**). The characteristic timescale, τ, of auto-correlogram decay was well captured by an exponential fit [40]. These behavioral timescales were intrinsic markers of neurons. The average decay times during wake and REM sleep are significantly correlated across neurons (**Fig. 6b**; r=0.434, p<0.001, Pearson's correlation). HD cells, again, showed marked differences compared with other AT neurons: their intrinsic slow timescales were the slowest (**Fig. 6b**, inset; t=-0.23, p=10^{-18}, t-test for Wake; t=-0.37, p=10^{-41}, t-test for REM). In conclusion, neurons of the AT exhibited intrinsic behavioral timescale dynamics, thus possibly reflecting involvement in cognitive functions requiring different integration times [41, 40], which is another property that is a sufficient feature to distinguish HD from non-HD neurons.

Spike train dynamics, at fast and slow timescales, must result from complex interactions between intrinsic properties of neurons and network states. It is noteworthy that during wakefulness and REM sleep, thalamic neurons show very rare bursts [25]. Interestingly, burst index (calculated during NREM) was negatively correlated with slow dynamics during both wakefulness and REM (**Fig. 6c** during REM; during wakefulness: r=-0.24, p<0.001, data not shown). This relationship is potentially due to intrinsic properties that manifest at timescales that are orders of magnitude apart, and suggest that spike train

statistics at millisecond timescales recapitulate the firing properties of the neurons in processes taking place at behavioral timescales.

Discussion

We described how HD cells of the AT (almost exclusively from the AD nucleus) form a homogeneous and specific cell population that plays a key role in limbic processing: while HD cells obviously inform the brain's navigation system of the animal's current HD during wakefulness, they also point towards particular directions at times of hippocampal SWRs. Thus, they possibly constrain the dynamics of the hippocampus to allow for the generation of coherent replayed trajectories along certain directions. Other AT neurons were, on the contrary, non-homogeneous, even when recorded from the same nucleus. However, we revealed a link between the dynamics of spike trains and response to SWRs, thus revealing how intrinsic neuronal properties and circuit integration are certainly related in the AT.

Here, we used a non-linear dimensionality reduction technique, ISOMAP [42], to decode population states independent of their behavioral correlates [26]. We showed how the HD cell population of the AD nucleus, which normally drifts at high angular speed during NREM sleep [10, 26], stabilized at fixed points and at high gain immediately before SWRs. It remains to be shown whether HD cell firing in the AD can in fact orchestrate hippocampal activity. However, this transient gain increase in the HD cell population preceding SWRs was independent of the relative timing within the UP states. This suggests that the AD nucleus can rapidly influence hippocampal dynamics, and not only at the timescale of the slow oscillation [34, 23, 21, 24]. While the impact of AD firing on the timing of SWRs is indirect and through polysynaptic routes, the projection fields of AD neurons, including targets in the post-subiculum, retrosplenial cortex, and medial entorhinal cortex, suggest a broad contribution of AD neurons to the activity of the limbic system, as evidenced by their central role in synchronizing the slow oscillation during NREM sleep [12].

Not only do AD neurons exert a widespread influence on the limbic system during NREM sleep, they also convey a coherent message. Indeed, the population activity of HD neurons of the AD nucleus is still highly organized during NREM [10, 26] in such a way that an angle can be reliably decoded at any time, at the exception of DOWN states that correspond to a singularity in HD cell population dynamics. It is thus possible that spatially tuned neurons of the limbic system are also updated by the HD signal during NREM sleep. While the HD cell population shows fast "sweeps" during NREM [10, 26], the stabilization of the HD signal during SWRs suggests that the navigation system is transiently constrained in a particular direction. While our study did not include neuronal recordings in downstream structures, one prediction would be that replay events of the hippocampus [15, 16] correspond to linear bouts of possible trajectories. Following exploration of a two-dimensional environment, it was recently suggested that replayed trajectories follow random (and non necessarily linear) rather than previously experienced paths [16]. Whether the directions of the replayed trajectories, from start to end points, or the initial direction of the replayed trajectories correspond to the direction encoded by the HD network remains an open question. Another possibility is that the HD cells influence replay in the medial entorhinal cortex. Indeed, grid cells maintain their coordination during NREM sleep [43, 44] and replay previously formed trajectories [45, 46], possibly independent of the hippocampus [46]. Finally, the coherent HD signal provided by the AD nucleus may constitute a subcortical processes enabling the emergence during sleep of coordinated neuronal sequences that do not correspond to any experienced spatial trajectories [47, 16]. Paired recordings of AT HD neurons and place or grid cells will be necessary to test these predictions.

One outstanding question is whether the subcortical HD network itself is under the influence of an external signal related to SWR generation and content or not. Indeed, one view posits that the HD network, including the AD nucleus and upstream structures, randomly fluctuates during sleep by integrating noisy inputs [26]. A transient fluctuation in excitability would favor the occurrence of a SWR through polysynaptic pathways. Conversely, it is possible that such a state is controlled by cortical feedback: AD neurons, as well as their presynaptic neurons of the lateral mammillary nuclei, receive a feedback from the post-subiculum. However, post-subicular cells remain largely under the influence of the AD nucleus during NREM [27]. At any rate, AD alone is certainly not the only structure influencing SWRs. For example, auditory cortex neurons fire prior to SWR and predict the content of hippocampal replays [48].

While the exact input and output connectivity pattern of each AT neuron is intractable *in vivo*, their coordination with hippocampal activity is an opportunity to determine their functional integration in the circuit. Unlike HD neurons, the co-modulation with SWRs was broadly distributed for non-HD neurons, largely independent of their anatomical location. One prediction is that, at the exception of the AD nucleus, other cytoarchitecturally-defined AT nuclei are characterized by a large diversity of connectivity patterns from neurons to neurons, as previous anatomical studies have suggested [1, 29].

The flow of information in the limbic system, and in particular to and from the hippocampus, may vary with brain states, in particular between wakefulness and NREM sleep [49]. AT neurons showed similar response to SWRs (during NREM) and theta (during wakefulness and REM), thus suggesting that they play a role in routing information independent of brain states. Whether this results from specific coupling with the hippocampus or from modulation by other limbic structures (e.g. the medial septum) remains to be answered.

Surprisingly, spike train dynamics are another potential marker of the functional coupling of AT neurons with the hippocampus. In fact, we observed a strong relationship between spike train auto-correlograms across brain states and response to SWRs. While our study could not determine the intracellular properties of AT neurons, spike train dynamics directly reflect - at least in part - these intrinsic properties [50, 51]. Again, HD cells formed a highly homogeneous population of neurons that could be identified as separate from the non-HD cells. In contrast, non-HD cells showed a continuous spectrum of dynamics with graded burstiness and refractory periods, among other features. Furthermore, AT neurons show a wide range of slow (~1s) intrinsic timescale dynamics. The intrinsic nature of these timescales is suggested by the similar time constant of their spike train auto-correlogram during wakefulness and REM sleep, two activated states of the brain. HD cells show markedly longer behavioral timescales than other AT neurons. Taken together, these results suggest that the cytoarchitectural definition of AT nuclei is an insufficient level of description, at the exception of the AD nucleus in which neurons show homogeneous behavioral correlates, for functional coupling with the hippocampus and spike train dynamics. In support of this view, gene expression profile in the AD is unique in the thalamus, while other AT neurons are continuously distributed rather than clustered in cytoarchitecturally defined nuclei [52].

A growing body of evidence points towards an intimate link between gene expression, spontaneous activity, and circuit development in thalamocortical pathways [29, 53, 54, 55, 52]. It is thus possible that spike train dynamics and coupling to network activity are two facets of common processes that are directly related to the acquired (but not necessarily pre-configured) role that each neuron plays in the circuit and associated with a specific molecular makeup [52, 29, 53, 54, 55, 56, 57]. Whether the variability in spike train dynamics reflects specific processes for signal transmission to downstream readers remains an open question.

The AT is a key communication relay between structures of the limbic system [7]. Interactions between the thalamus, the hippocampus, and more generally the limbic system during learning and around SWRs (nested in slow and spindle oscillations, two NREM-specific thalamocortical rhythms) are believed to be crucial in supporting hippocampus-dependent memory consolidation processes at play during NREM [13, 12, 17, 58, 21, 22, 59, 28, 24]. Interestingly, while the HD cell population was stabilized at times of SWRs, it drifts at maximum speed during thalamocortical spindles [26]. Future work is necessary to characterize the processes controlling HD and non-HD cells of the AT, their contribution in determining hippocampal replay content, and their role in routing hippocampal signals across the structures of the limbic system. The analytical framework of our study provides a foundation for investigating the relationship between intrinsic neuronal properties at various timescales and functional integration in brain networks *in vivo*. It is possible that such relationship is an organizational principle of all thalamic neurons.

Acknowledgments

The authors thank G. Buzsaki, A. Adamantidis, F. P. Battaglia, M. D. Humphries, L. Sjulson, R. Chaudhuri, D. E. English and J.-P. Roussarie for critical reading of the manuscript, P. C. Petersen and M. M. Lacroix for help with the experiments, members of the Peyrache Lab for comments and for editing the manuscript. **Funding:** A.P. holds a Canadian Research Chair in Systems Neuroscience. This work was supported by CIHR Project Grant 155957 and NSERC Discovery Grant RGPIN-2018-04600.

Author contributions

A.P. conceived and designed the study. A.P. performed the experiments. G.V. and A.P. analyzed the data. G.V. and A.P. wrote the manuscript.

Declaration of interests

The authors declare no competing interests.

Supplemental information

Supplemental Information includes four figures and one table.

References

[1] Jones, E. *The Thalamus.* No. vol. 1 in The Thalamus (Cambridge University Press, 2007). URL https://books.google.ca/books?id=EtTvsgEACAAJ.

[2] Sherman, S. M. Thalamus plays a central role in ongoing cortical functioning. *Nature neuroscience* **19**, 533 (2016).

[3] Halassa, M. M. & Kastner, S. Thalamic functions in distributed cognitive control. *Nature neuroscience* **20**, 1669–1679 (2017).

[4] Mitchell, A. S. *et al.* Advances in understanding mechanisms of thalamic relays in cognition and behavior. *Journal of Neuroscience* **34**, 15340–15346 (2014).

[5] Papez, J. W. A proposed mechanism of emotion. *Archives of Neurology & Psychiatry* **38**, 725–743 (1937).

[6] Jankowski, M. M. *et al.* The anterior thalamus provides a subcortical circuit supporting memory and spatial navigation. *Frontiers in systems neuroscience* **7** (2013).

[7] Aggleton, J. P. *et al.* Hippocampal–anterior thalamic pathways for memory: uncovering a network of direct and indirect actions. *European Journal of Neuroscience* **31**, 2292–2307 (2010).

[8] Taube, J. S. Head direction cells recorded in the anterior thalamic nuclei of freely moving rats. *Journal of Neuroscience* **15**, 70–86 (1995).

[9] Winter, S. S., Clark, B. J. & Taube, J. S. Disruption of the head direction cell network impairs the parahippocampal grid cell signal. *Science* 1259591 (2015).

[10] Peyrache, A., Lacroix, M. M., Petersen, P. C. & Buzsáki, G. Internally organized mechanisms of the head direction sense. *Nature neuroscience* **18**, 569–575 (2015).

[11] Halassa, M. M. *et al.* State-dependent architecture of thalamic reticular subnetworks. *Cell* **158**, 808–821 (2014).

[12] Gent, T. C., Bandarabadi, M., Herrera, C. G. & Adamantidis, A. R. Thalamic dual control of sleep and wakefulness. *Nature neuroscience* 1 (2018).

[13] Diekelmann, S. & Born, J. The memory function of sleep. *Nature Reviews Neuroscience* **11**, 114 (2010).

[14] Wilson, M. A. & McNaughton, B. L. Reactivation of hippocampal ensemble memories during sleep. *Science* **265**, 676–679 (1994).

[15] Lee, A. K. & Wilson, M. A. Memory of sequential experience in the hippocampus during slow wave sleep. *Neuron* **36**, 1183–1194 (2002).

[16] Stella, F., Baracskay, P., O'Neill, J. & Csicsvari, J. Hippocampal reactivation of random trajectories resembling brownian diffusion. *Neuron* **102**, 450–461 (2019).

[17] Buzsáki, G. Hippocampal sharp wave-ripple: A cognitive biomarker for episodic memory and planning. *Hippocampus* **25**, 1073–1188 (2015).

[18] Girardeau, G., Benchenane, K., Wiener, S. I., Buzsáki, G. & Zugaro, M. B. Selective suppression of hippocampal ripples impairs spatial memory. *Nature neuroscience* **12**, 1222 (2009).

[19] Ego-Stengel, V. & Wilson, M. A. Disruption of ripple-associated hippocampal activity during rest impairs spatial learning in the rat. *Hippocampus* **20**, 1–10 (2010).

[20] Jadhav, S. P., Kemere, C., German, P. W. & Frank, L. M. Awake hippocampal sharp-wave ripples support spatial memory. *Science* **336**, 1454–1458 (2012).

[21] Siapas, A. G. & Wilson, M. A. Coordinated interactions between hippocampal ripples and cortical spindles during slow-wave sleep. *Neuron* **21**, 1123–1128 (1998).

[22] Sirota, A., Csicsvari, J., Buhl, D. & Buzsáki, G. Communication between neocortex and hippocampus during sleep in rodents. *Proceedings of the National Academy of Sciences* **100**, 2065–2069 (2003).

[23] Battaglia, F. P., Sutherland, G. R. & McNaughton, B. L. Hippocampal sharp wave bursts coincide with neocortical "up-state" transitions. *Learning & Memory* **11**, 697–704 (2004).

[24] Peyrache, A., Battaglia, F. P. & Destexhe, A. Inhibition recruitment in prefrontal cortex during sleep spindles and gating of hippocampal inputs. *Proceedings of the National Academy of Sciences* **108**, 17207–17212 (2011).

[25] Steriade, M., McCormick, D. A. & Sejnowski, T. J. Thalamocortical oscillations in the sleeping and aroused brain. *Science* **262**, 679–685 (1993).

[26] Chaudhuri, R., Gerçek, B., Pandey, B., Peyrache, A. & Fiete, I. The intrinsic attractor manifold and population dynamics of a canonical cognitive circuit across waking and sleep. *Nature neuroscience* 1–9 (2019).

[27] Viejo, G., Cortier, T. & Peyrache, A. Brain-state invariant thalamo-cortical coordination revealed by non-linear encoders. *PLoS computational biology* **14**, e1006041 (2018).

[28] Peyrache, A., Duszkiewicz, A. J., Viejo, G. & Angeles-Duran, S. Thalamocortical processing of the head-direction sense. *Progress in neurobiology* 101693 (2019).

[29] Clascá, F., Rubio-Garrido, P. & Jabaudon, D. Unveiling the diversity of thalamocortical neuron subtypes. *European Journal of Neuroscience* **35**, 1524–1532 (2012).

[30] Llinás, R. & Jahnsen, H. Electrophysiology of mammalian thalamic neurones in vitro. *Nature* **297**, 406 (1982).

[31] Pare, D., Steriade, M., Deschenes, M. & Oakson, G. Physiological characteristics of anterior thalamic nuclei, a group devoid of inputs from reticular thalamic nucleus. *Journal of Neurophysiology* **57**, 1669–1685 (1987).

[32] Sheroziya, M. & Timofeev, I. Global intracellular slow-wave dynamics of the thalamocortical system. *Journal of Neuroscience* **34**, 8875–8893 (2014).

[33] Zhang, K., Ginzburg, I., McNaughton, B. L. & Sejnowski, T. J. Interpreting neuronal population activity by reconstruction: unified framework with application to hippocampal place cells. *Journal of neurophysiology* **79**, 1017–1044 (1998).

[34] Isomura, Y. *et al.* Integration and segregation of activity in entorhinal-hippocampal subregions by neocortical slow oscillations. *Neuron* **52**, 871–882 (2006).

[35] Buzsáki, G. Theta rhythm of navigation: link between path integration and landmark navigation, episodic and semantic memory. *Hippocampus* **15**, 827–840 (2005).

[36] Tsanov, M. *et al.* Theta-modulated head direction cells in the rat anterior thalamus. *Journal of Neuroscience* **31**, 9489–9502 (2011).

[37] Churchland, M. M. *et al.* Neural population dynamics during reaching. *Nature* **487**, 51–56 (2012).

[38] Maaten, L. v. d. & Hinton, G. Visualizing data using t-sne. *Journal of machine learning research* **9**, 2579–2605 (2008).

[39] Chen, T. & Guestrin, C. Xgboost: A scalable tree boosting system. In *Proceedings of the 22nd acm sigkdd international conference on knowledge discovery and data mining*, 785–794 (ACM, 2016).

[40] Murray, J. D. *et al.* A hierarchy of intrinsic timescales across primate cortex. *Nature neuroscience* **17**, 1661 (2014).

[41] Chaudhuri, R., Knoblauch, K., Gariel, M.-A., Kennedy, H. & Wang, X.-J. A large-scale circuit mechanism for hierarchical dynamical processing in the primate cortex. *Neuron* **88**, 419–431 (2015).

[42] Tenenbaum, J. B., De Silva, V. & Langford, J. C. A global geometric framework for nonlinear dimensionality reduction. *science* **290**, 2319–2323 (2000).

[43] Trettel, S. G., Trimper, J. B., Hwaun, E., Fiete, I. R. & Colgin, L. L. Grid cell co-activity patterns during sleep reflect spatial overlap of grid fields during active behaviors. *bioRxiv* 198671 (2017).

[44] Gardner, R. J., Lu, L., Wernle, T., Moser, M.-B. & Moser, E. I. Correlation structure of grid cells is preserved during sleep. *bioRxiv* 198499 (2017).

[45] Ólafsdóttir, H. F., Carpenter, F. & Barry, C. Coordinated grid and place cell replay during rest. *Nature neuroscience* **19**, 792 (2016).

[46] O'Neill, J., Boccara, C. N., Stella, F., Schönenberger, P. & Csicsvari, J. Superficial layers of the medial entorhinal cortex replay independently of the hippocampus. *Science* **355**, 184–188 (2017).

[47] Dragoi, G. & Tonegawa, S. Preplay of future place cell sequences by hippocampal cellular assemblies. *Nature* **469**, 397 (2011).

[48] Rothschild, G., Eban, E. & Frank, L. M. A cortical–hippocampal–cortical loop of information processing during memory consolidation. *Nature neuroscience* **20**, 251 (2017).

[49] Hasselmo, M. E. The role of acetylcholine in learning and memory. *Current opinion in neurobiology* **16**, 710–715 (2006).

[50] Fuzik, J. *et al.* Integration of electrophysiological recordings with single-cell rna-seq data identifies neuronal subtypes. *Nature biotechnology* **34**, 175 (2016).

[51] Cadwell, C. R. *et al.* Electrophysiological, transcriptomic and morphologic profiling of single neurons using patch-seq. *Nature biotechnology* **34**, 199 (2016).

[52] Phillips, J. W. *et al.* A single spectrum of neuronal identities across thalamus. *bioRxiv* 241315 (2018).

[53] Martini, F. J., Moreno-Juan, V., Filipchuk, A., Valdeolmillos, M. & López-Bendito, G. Impact of thalamocortical input on barrel cortex development. *Neuroscience* **368**, 246–255 (2018).

[54] Molnár, Z. & Blakemore, C. How do thalamic axons find their way to the cortex? *Trends in neurosciences* **18**, 389–397 (1995).

[55] Frangeul, L. *et al.* A cross-modal genetic framework for the development and plasticity of sensory pathways. *Nature* **538**, 96 (2016).

[56] Harris, K. D. & Shepherd, G. M. The neocortical circuit: themes and variations. *Nature neuroscience* **18**, 170 (2015).

[57] Cembrowski, M. S. & Spruston, N. Heterogeneity within classical cell types is the rule: lessons from hippocampal pyramidal neurons. *Nature Reviews Neuroscience* (2019). URL https://doi.org/10.1038/s41583-019-0125-5.

[58] Peyrache, A., Khamassi, M., Benchenane, K., Wiener, S. I. & Battaglia, F. P. Replay of rule-learning related neural patterns in the prefrontal cortex during sleep. *Nature neuroscience* **12**, 919–926 (2009).

[59] Maingret, N., Girardeau, G., Todorova, R., Goutierre, M. & Zugaro, M. Hippocampo-cortical coupling mediates memory consolidation during sleep. *Nature neuroscience* **19**, 959–964 (2016).

[60] Paxinos, G. & Keith B. J. Franklin, M. *The Mouse Brain in Stereotaxic Coordinates* (Elsevier Science, 2007). URL https://books.google.ca/books?id=5MdpQgAACAAJ.

[61] Royer, S. *et al.* Control of timing, rate and bursts of hippocampal place cells by dendritic and somatic inhibition. *Nature neuroscience* **15**, 769 (2012).

Material and Methods

Surgery and experimental design

All experiments were approved by the Institutional Animal Care and Use Committee of New York University Medical Center. Details of the surgeries were described previously [10]. Briefly, four male mice weighing approximately 30g (3-6 months) were implanted under isoflurane anesthesia with silicon probes (Neuronexus) above the anterior thalamus (AP: −0.6 mm; ML:−0.5 to −1.9 mm; DV: 2.2 mm, with a 10–15° angle, the shanks pointing toward midline). Hippocampal wire bundles were implanted above CA1 (AP: −2.2 mm; −1 to −1.6 mm ML; 1 mm DV). The probes consisted of 8 shanks separated by 200-μm and each shank had 8 recording sites (160 μm^2 each site, 1–3-MΩ impedance) that were staggered to provide a two-dimensional arrangement (20-μm vertical separation). In all experiments ground and reference screws or 100-μm diameter tungsten wires were implanted in the bone above the cerebellum.

Electrophysiological data acquisition

The animals were recorded over several days for successive epochs of pre-sleep (1-2 Hrs), food foraging in a circular arena (sweetened cereals or regular food pellets) for 30 min, and post-sleep (1-2 Hrs). Overall, sessions lasted on average 5 hours (± 0.94 s.d.). Electrophysiological signals were acquired continuously at 20 kHz on a 256-channel Amplipex system (Szeged; 16-bit resolution, analog multiplexing). The broadband signal was down sampled to 1.25 kHz and used as LFPs.

To track the position of the animals in the open maze and in their home cage during rest epochs, two small light-emitting diodes (LEDs; 5-cm separation), mounted above the headstage, were recorded by a digital video camera at 30 frames per second. The LED locations were detected online and resampled at 39 Hz by the acquisition system. Spike sorting was performed semi-automatically, using KlustaKwik (http://klustakwik.sourceforge.net/). This was followed by manual adjustment of the waveform clusters using the Klusters software.

Sleep scoring

As previously described [10], stages of sleep were identified semi-automatically based on the CA1 LFP spectrogram and on animal movements that were continuously tracked with the LEDs, as during behavior. Overall, sleep was defined as a long period of immobility. Within each sleep episode, NREM sleep was defined as periods with high delta (1-4Hz) and spindle (10-15Hz) activity. REM sleep was defined as periods with strong power in the theta (5-12Hz) range and low delta.

UP and DOWN state detection

UP and DOWN states were detected by computing the total firing rate of all simultaneously recorded neurons in bins of 10 ms, smoothed with a Gaussian kernel of 20 ms s.d.. Epochs during which total firing rate was lower than 20% of the maximum firing rate were considered as DOWN epochs. Epochs shorter than 30 ms and longer than 500 ms were discarded. UP states were defined as the epochs between each DOWN states.

SWR detection

To detect SWRs, CA1 LFP was first bandpassed between 80 and 300 Hz with a Gaussian filter. The squared signal was then smoothed using a digital filter with a window length of 11 and z-scored using mean and standard deviation. The normalized squared signal was then thresholded between 3 and 7 standard deviations yielding a first set of candidate

ripples. The set was then reduced by keeping only candidates with a duration between 25 ms and 350 ms (in some sessions with lower amplitude ripples, the thresholds were lowered to 2 and 5 s.d., respectively, and rippled detection was validated by visual inspection). Ripples closer than 30ms were merged and considered a unitary event.

Head-direction classification

For each session, the direction of the head of the animal in the horizontal plane was calculated by the relative orientation of a blue and red LED located on top of the head. Head-direction neurons were detected by computing tuning curves i.e. the ratio between the histogram of angular direction associated to each spike divided by the total time spent by the animal in each angular bins. Similar to [10], a Rayleigh test was performed to test for the null hypothesis of uniformly distributed firing in all angular directions, and neurons were classified as HD cells if peak firing rates of the tuning curves was larger than 1, a probability of non-uniform distribution smaller than 0.001 and a concentration parameter (i.e. inverse of the variance of the tuning curves) larger than 1.

ISOMAP projection and decoding

ISOMAP projections (**Fig. 1** and **Supplementary Fig.1**) were performed for sessions containing at least 10 HD neurons (8 sessions in total from 3 different animals). First, spike trains were binned during wakefulness and around time of SWRs. As such dimensionallity reduction techniques are computationally heavy, we included in the analysis only the first 15 min of exploration and a period of 1 second around SWRS ($\pm$ 500ms). The duration of the bins was 400 ms and 30 ms (with a 50% overlap) during wakefulness and around SWR occurrence times, respectively (different bins were used to capture the different timescales of the HD signal during wakefulness and NREM). To visually inspect the topology of HD cell population vectors (**Fig. 1c** and **Supplementary Fig. 1a**), we used a bin size of 200 ms for wakefulness and 100 ms (with a overlap of 75%) around SWRs. To quantify the change in radii and angular velocity across sessions, ISOMAP projections were compared to a baseline taken around randomly selected events during NREM sleep. Similar to [26], we computed the square root of the rates to normalize for the variance in firing rates. Binned firing rates were smoothed with a Gaussian kernel of 3 bin standard deviation (independent of absolute bin duration).

In each condition (wakefulness, SWR and controls), binned firing rates were stacked together, yielding a rate matrix $R \in \mathbb{R}^{T \times N}$, where N is the number of neurons and T is the total number of time points. This rate matrix was then projected to a two dimension plane $I \in \mathbb{R}^{T \times 2}$ using ISOMAP [42]. The number of neighbors was set to 200. To further reduce the computational requirement for long spike trains (i.e. typically more than 30000 time bins), we repeated the ISOMAP projection using a random subset of 150 SWRs and 150 random NREM time bins at each iteration for baseline quantification, yielding a total of 300 events during NREM.

Angular direction and radius (i.e. ring size) was decoded during SWRs by computing the element-wise arc tangent and Euclidean norm of each time point. Angular velocity was then evaluated by computing the angular difference between two consecutive time points. The same procedure was performed for randomly selected events during NREM that projected within the same ISOMAP embedding. Radius and angular velocity (as shown in **Figs. 1d-e**) are thus the ratio $(\bar{X}_{SWRs} - \bar{X}_{random})/\bar{X}_{random}$ with $\bar{X}$ deonting average values).

Bayesian decoding

To validate the decoding in the embedding space (**Fig.1**), we used Bayesian decoding to predict angular velocity during SWRs (**Fig.2**). Let $\mathbf{n} = (n_1, n_2, ..., n_N)$ be the number of spikes fired by the HD neurons within a given time window (30 ms) and Φ be the animal's head direction or, during sleep, the angle of the internal HD signal. The goal of this decoder is to compute the *posterior* probability $P(\Phi|\mathbf{n})$, which can be achieved using Bayes' rule of conditional probabilities:

$$P(\Phi|\mathbf{n}) = \frac{P(\mathbf{n}|\Phi)P(\Phi)}{P(\mathbf{n})} \tag{1}$$

Assuming that (i) neuronal firing is independent from each other and (ii) spike counts follow Poisson distributions, the probability $P(\mathbf{n}|\Phi)$ is equal to [33]:

$$P(\mathbf{n}|\Phi) = \prod_{i=1}^{N} P(n_i|\Phi) = \prod_{i=1}^{N} \frac{(\tau f_i(\Phi))^{n_i}}{n_i!} exp^{-\tau f_i(\Phi)} \tag{2}$$

where τ is the bin size and $f_i(\Phi)$ the average firing rate of cell i for the direction Φ during wakefulness (i.e. the HD tuning curve at angle Φ). The decoded direction is the value Φ associated with the highest posterior probability $P(\Phi|\mathbf{n})$.

Similar to ISOMAP decoding, angular velocity was evaluated as the ratio $(\bar{v}_{SWRs} - \bar{v}_{random})/\bar{v}_{random}$ with $\bar{v}_{SWRs}$ being the average angular velocity during SWRs and $\bar{v}_{random}$, the average angular velocity for randomly selected events during non-REM sleep. We used bin size of 30 ms with 50% overlap and angular bins of 6 degrees.

Map alignment

To align the position of the electrodes with their putative anatomical location, we used the following procedure. First, after each session, the probe was lowered by 70-140 μm. Relative position was estimated from the first day of recording when the probe entered the thalamus (appearance of spiking activity on 1-2 shanks). This yielded a relative depth for each session while the horizontal distance between shanks was kept constant (200 μm). This two-dimensional grid of recording sites was then rotated by 15 degrees clockwise corresponding to the angle of penetration of the silicon probe. Then, the relative position of recording sites was aligned to the anatomical map (from bregma -0.82 mm; Figure 38 in [60]) by matching the relative configuration of the electrodes with the putative location of the AD nucleus (shanks on which large number of head-direction neurons were recorded) [10]. Note that the anatomical map from the atlas was enlarged by 10% (it is commonly accepted that slices used for anatomy are shrunk by approximately this amount). As shown in **Figs.** 2 and **S2**, the density of HD neurons matched well with the estimated anatomical position of the antero-dorsal nucleus.

SWRs cross-correlograms

The SWR modulation was computed for each neuron by estimating cross-correlograms (average firing rates in 5 ms bins, $\pm$ 500ms from SWR peak time). Because neuronal discharge and SWRs are both co-modulated by the slow oscillation [21, 22, 24, 23], cross-correlograms were normalized relative to their expected values under the null hypothesis of no short timescale coupling between neuronal discharge and SWR occurrence. To this end, SWR cross-correlograms were convolved with Gaussian windows of 150 ms s.d. (a process similar to low-pass filtering the firing rates). The value of 150ms was chosen as it corresponds to the upper bound duration of SWRs. From this distribution of low-pass filtered ("expected") rates around the time of SWRs, we inferred an "expected," standard deviation under the assumption of a Poisson process (i.e. the square root of the expected

rate at a given time bin). For each time bin, we subtracted the expected rate from the observed rate, and then divided the difference by the expected standard deviation. The observed cross-correlograms were thus expressed in z-values from the expected distribution under the null hypothesis of no short timescale coupling. This method enables us to extract the specific and fast modulation of a neuron by SWRs, independent of the co-modulation of the SWRs with the thalamo-cortical slow oscillations [25, 22, 24, 23]. In mathematical terms, we thus obtained a set of time series $\mathbf{z}(t) = [z_1(t), ..., z_N(t)]$ where N is the number of neurons. Note that the z values are not a typical z-score, but correspond to deviation in z from the null hypothesis. Note that the mean and s.d. of the resulting z-transforms are not normalized. To describe the amplitude of SWR modulation, we introduced SWR $energy$, defined as the total power of the z-scored cross-correlograms: $|z_i| = \sqrt{\sum_{t=1}^{T} z_i(t)^2}$.

Theta modulation

Theta modulation for each neuron was computed separately for epochs of wake and REM sleep. Using continuous wavelets transform, a phase was assigned to each theta cycle and histograms of spike counts between 0 and 2π were then computed for each neuron as shown in **Fig. 3b**. A Rayleigh test was then performed with the null hypothesis of uniformly distributed firing rates during a theta cycle.

jPCA

To describe SWR modulation in term of phases, we used the jPCA method [37]. First, PCA was used to reduce the dimensionality of the ensembles of cross-correlograms ($K = 6$ principal components were considered, as in [37]). Overall, the goal of jPCA is to describe temporal response profiles, assuming that the data are governed by a linear dynamical system of the form: $\dot{\mathbf{x}} = M\mathbf{x}$ with $M \in \mathbb{R}^{K,K}$ (or $M \in \mathbb{R}^{N,N}$ if no dimension reduction is applied first). The matrix M can be split into its symmetric and anti-symmetric matrix $M = M_{sym} + M_{anti}$, related to expansion/contraction and rotational dynamics, respectively. The latter matrix has pure imaginary eigenvalues, hence its association with rotational dynamics. To capture phase response in the rotational space, it is thus sufficient to find the best fit for the matrix $M_{anti} \in \Gamma^{k \times k}$. This can be done by minimizing the error made on predicting $\dot{X}$ from MX, which can be expressed as $M_{anti}^* = argmin_{M \in \Gamma}||\dot{X} - MX||_F$, where F denotes the Froebenius norm (see [37] for additional details on the methods). Finally, jPCA entails the decomposition of M_{anti}^* into its eigenvectors made (by definition) of complex conjugate pairs. A suitable pair of projection vectors $U = (u_1, u_2) \in \mathbb{R}^{T,2}$ can be obtained by combining complex conjugate pairs (v_1, v_2) such that $u_1 = v_1 + v_2$ and $u_2 = i(v_1 - v_2)$.

The last step consists in projecting SWR cross-correlograms onto the first two jPCs (u_1 and u_2): $\mathbf{y} = Z^T\mathbf{u} \in \mathbb{R}^{N,2}$. The SWR phase was defined as the angle from origin in this 2D space: $\phi_{SWR} = atan2(y_2, y_1)$.

Auto-correlograms

For each neuron, three auto-correlograms were computed separately for the epoch of wake, REM and NREM sleep respectively. The short auto-correlograms shown in **Figs. 4-5** were computed using a bin size of 0.5 ms while the long auto-correlograms in **Fig. 6** were computed using a bin size of 5 ms.

Embedding of the auto-correlograms in a 2D map (**Fig. 5b**) was performed with the t-SNE algorithm [38] by concatenating only the part corresponding to positive time lag (i.e. the right part of the auto-correlograms). Given $A_{2ms \to 40ms}^{epoch} \in \mathbb{R}^N$ the auto-correlogram

vector of one epoch for one neuron, each point in the t-SNE projection is thus a mapping $f : X_i \in \mathbb{R}^{3N} \to Y_i \in \mathbb{R}^2$ with $X_i = [A_{2ms \to 40ms}^{wake} A_{2ms \to 40ms}^{REM} A_{2ms \to 40ms}^{NREM}]$ for each neuron i.

In **Fig. 5f**, neurons were classified (HD versus non-HD) with gradient boosted trees using the XGBoost package [39]. Inputs given to the classifier is the same as the t-SNE algorithm (i.e. stacked auto-correlograms of wake, REM and NREM episodes). Classifier was trained with 1000 iterations, using default parameters and a 10-fold cross-validation procedure. Chance levels were determined from a thousand classifications obtained with random shuffling of the neuron labels. For N neurons and C classes, classification score was defined as:

$$s = \frac{\sum_{i=1}^{N} 1(c_i = \hat{c}_i) - \sum_{i=1}^{N} 1(c_i = \hat{c}_i^s)}{N - \sum_{i=1}^{N} 1(c_i = \hat{c}_i^s)}$$

with $1(x)$ the indicator function, $\hat{c}_i$ the class predicted for the ith neuron and $\hat{c}_i^s$ the labels predicted with a classifier trained on shuffled data. A score of 0 indicates chance level (compared to shuffles) and a score of 1 indicates perfect classification.

Burst index

For each epoch, bursts were defined as groups of spikes with interspike intervals (ISI) between 2ms and 9ms. Burst index [61] was then computed as the ratio between the observed count $N_{2ms < ISI < 9ms}$ and the count expected from a homogeneous process with the same average firing rate: $\bar{N}_{\tau_1 < ISI < \tau_2} = T(exp(-\tau_1 \times r) - exp(-\tau_2 \times r))$ with T the duration of the epoch, r the mean firing rate during this epoch, $\tau_1 = 2$ ms and $\tau_1 = 9$ ms.

Total correlation between auto-correlograms and SWR cross-correlograms

To compute the correlation between SWR cross-correlograms and auto-correlograms (**Figs. 4e**, **f** and **g**), auto-correlograms were first stacked across brain states (as done for the t-SNE projection, see above). We used PCA to reduce the dimensionality of each matrix (of either SWRs cross-correlograms or stacked autocorrelograms) and we kept the first 10 components accounting for respectively 91% and 99% of the variance. We computed the 20-by-20 correlation matrix C for the 10 SWR PCs and 10 auto-correlogram PCs. The matrix is diagonal for the upper-left and bottom right 10-by-10 blocks as PCs from a given dataset are perpendicular to each other. We thus show only the off-diagonal matrix in **Fig. 4f**. We then defined the total correlation as $\rho_{total}^2 = 1 - |C|$ with $|C|$ being the determinant of the correlation matrix (if only one PC was considered for auto-correlograms and SWR cross-correlograms, then total correlation would be the linear correlation between the two PCs). From a geometrical perspective, this measure captures the fraction of state-space volume occupied by both measures. The null correlation was determined by shuffling the identity of the neurons in both datasets (1000 times).

We controlled for correlation between neurons belonging to the same nucleus by shuffling neurons within groups recorded on the same shank and session (1000 times). The correlation between SWR cross-correlograms and auto-correlograms was further tested for possible correlation by common underlying factors (firing rates or burstiness). The correlation r_{ij} between the ith auto-correlogram PC and the jth SWR PC was replaced by the partial correlation (correlation knowing factor f): $r_{ij|f} = \frac{r_{ij} - r_{if} r_{jf}}{\sqrt{1 - r_{if}^2} \sqrt{1 - r_{jf}^2}}$ where r_{kf} ($k = i$ or j) is the correlation between PC weights and the external factor f (firing rates or burstiness).

Quantification and statistical analysis

Analyses were done using customized code written in MATLAB (MathWorks) and Python (3.5) with the following libraries: numpy, scipy and scikit-learn.

Data and software availability

Some of the data are available at http://dx.doi.org/10.6080/K0G15XS1. We used animals labelled Mouse17, Mouse12, Mouse20 and Mouse32 in the dataset. The entire dataset will be made available upon request. Code is available at https://github.com/PeyracheLab/ThalamusPhysio.

Supplemental information

Supplementary Figures 1-3

Supplementary Figure 1: ISOMAP embeddings and decoding. (**a**) ISOMAP embeddings for sessions with at least 10 HD neurons (see **Fig.**1). Only one session was excluded (Mouse17-130129) as it showed no ring topology. (**b**), *left* Average normalized radii around times of SWRs as a function of the time-lag from UP onset. (*right*) Average ISOMAP radius around SWRs occurring at various time intervals during the UP state (each of the four groups contains the same number of SWRs) (**c**) Same as (**b**) for angular velocity.

Supplementary Figure 2: Bayesian decoding during SWRs. (**a**) Angular velocity around SWRs using bayesian decoding for sessions with more than 10 HD neurons. Black line shows average. (**b**) Same as **a** for sessions with more than 5 HD neurons.

Supplementary Figure 3: Alignment of Recordings with Anatomical Locations. (**a**) Neuron count for each session and each shank for mouse 17. (**b**) Neuron density for mouse 17 after interpolation (i.e. given the distance between shanks and between sessions) and spatial smoothing. (**c**) Neuron count for each recording position. (**d**) Position of the interpolated neuronal density map (as in **b**). (**e**) Recording areas for each mouse. (**f**) Neuron count for all mice. (**g** - **i**) Recording locations, neuron count, cluster #1 (HD) and cluster #2 (burstiness) density maps (see Figure 5) for mice 12, 20 and 32.