Correlated activity favors synergistic processing in local cortical networks at synaptically-relevant timescales

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SUMMARY

Information processing by neural circuits is widely understood to depend on correlation in the activity of upstream neurons. However, whether correlation is favorable or not is contentious. Correlated activity can facilitate information transmission but also increases redundancy. Here, we sought to determine how correlated activity and information processing are related in cortical circuits. Using high-density 512-channel electrode arrays we recorded the spiking activity of hundreds of well-isolated neurons in organotypic cultures of mouse somatosensory cortex and asked whether mutual information between neurons that feed into a common third neuron increased synergistic information processing by the receiving neuron. We found that mutual information and synergistic processing were positively related when examined at synaptic timescales (0.05-14 ms), where mutual information values were generally low. This effect was mediated by increased information transmission that resulted as mutual information grew. However, at extrasynaptic windows (up to 3000 ms), where mutual information values were generally high, the relationship between mutual information and synergy became negative. In this regime, the further increases in mutual information resulted in a disproportionate increase in redundancy, outweighing incremental gains in information transmission. These results indicate that the relationship between input correlation and synergistic processing differs according to the correlation regime. In a low-correlation regime, synergistic processing increases with greater correlation, and in a high correlation regime, synergistic processing decreases with greater correlation.

KEYWORDS
Neural information processing; correlated activity; computation; networks; effective connectivity; cortex; information theory; synergy

INTRODUCTION

Is correlated activity among neurons in cortical microcircuits favorable or unfavorable for neural information processing? The answer to this question differs considerably between research communities, although it is not explicitly debated. Within the sensory processing and artificial neural networks communities, correlated activity is often equated with efficiency-reducing-redundancy and, thus, is considered unfavorable (Attneave, 1954; Barlow, 1961; c.f., Barlow, 2001). In contrast, within the cognitive rhythms community, correlated activity is associated with the coordination of distributed ensembles of neurons, facilitating information transmission, and, thus, is considered favorable (e.g., Lisman & Jenson, 2013; Fries, 2015). These perspectives dominate the thinking in their respective communities but are at apparent odds with each other. Here, we pit these perspectives against each other by asking, in organotypic cultures of cortical microcircuits, is correlated activity among upstream neurons associated with greater or lesser downstream neural information processing?

Neural information processing is comprised of information transfer, storage, and computation (Lizier et al., 2014; Wibral et al., 2017). We focus here on computation specifically. Computation refers to the synergistic combination of existing information to derive new information. Advances in information-theoretic analysis that enable analysis of multi-way interactions make it possible to decompose the encoded information into its constituent parts including the synergistic combination of information from the inputs (Williams & Beer, 2010). This enables formal quantification of the synergy that emerges when a given neuron integrates input from two other neurons (Timme et al., 2016; Wibral et al., 2017). Examples of high synergy computations include 'AND' and 'XOR,' wherein knowledge of the state of both upstream neurons is needed to predict the state of the receiving neuron (Timme et al., 2016). We refer to this as synergistic processing. This approach has been used effectively before, revealing that synergistic processing varies systematically with the maturation of neural cultures, with the number of connections of upstream neurons, and with the strength of rich-club topology (Wibral et al., 2017; Timme et al., 2016; Faber et al., 2019). Here, we leveraged this approach to determine whether correlated activity is favorable or unfavorable for synergistic processing.

The view that correlated neural activity is favorable for neural information processing is widely held within the cognitive rhythms community and is based on the idea that correlation facilitates both communication between circuits and orchestration of processing within circuits. Correlated neural activity is understood to generate the coherent rhythms that are observed in local field potentials, electrocorticography, and electroencephalography which have been theorized to subserve specific computational or cognitive mechanisms (e.g., Hasselmo et al., 2002; Ward 2003; Norman et al., 2006; Lisman & Jensen, 2013; Newman et al., 2014; Fries, 2015; Honey et al., 2017). A dominant and relevant theme among such theories is the importance of synchrony, a form of correlated activity, for enabling and organizing information transmission in cortical circuits. Ample empirical evidence derived from *in vitro*, *in silico*, and *in vivo* studies supports this idea (Salinas & Sejnowski, 2001; Azouz & Gray, 2003; Averbeck & Lee, 2004; Poulet & Petersen, 2008; Yu et al., 2008; Fries, 2015). The synchronization of neuronal spiking is indeed linked to higher order cognitive and behavioral processes (Vinck et al., 2015; Riehle et al.,1997; Grammont & Riehle, 1999). From this perspective, correlation is favorable for information processing. Yet, even within the cognitive rhythms community there is recognition that excess

correlation can be unfavorable and that, in some circumstances, desynchronization supports information processing better than synchronization (e.g., van Winsun et al., 1984; Hanslmayr et al., 2012; Bastos et al., 2015). The discrepancy between this and the standard view of the cognitive rhythms community warrants reconciliation (Hanslmayr, Staresina, & Bowman, 2016).

The view that correlated activity is unfavorable for neural information processing is widely held in the sensory processing and artificial neural network communities and is based on the idea that correlation is synonymous with redundancy and thus reduces efficiency (Attneave, 1954; Barlow, 1961; Gutnisky and Dragoi, 2008; Schneidman, Bialek & Berry, 2003; Shadlen & Newsome 1998). This bandwidth-limiting effect of correlation motivates the 'redundancy-reduction hypothesis' (Atick & Redlich, 1990; Attneave, 1954; Barlow, 1961; Shadlen & Newsome 1998). In this line of thinking, a normative goal of sensory information processing is to reduce the redundancy of neuronal signals (Atick and Redlich, 1992; Barlow, 1961; Field, 1987; Gutnisky and Dragoi, 2008; van Hateren, 1992; Laughlin, 1989; Rieke et al., 1995). This view is well supported. Many works, together, indicate that signal redundancy decreases from lower order sensory areas to higher order sensory areas (Berry et al., 1997; Chechik et al., 2006; Dan et al., 1998; Doi et al., 2012; Montani et al., 2007; Nirenberg et al., 2001; Puchalla et al., 2005; Reich et al., 2001; Reinagel and Reid, 2000; Zohary et al. 1994). From this perspective, correlation is unfavorable for information processing. Yet, as in the cognitive rhythms community, there is an indication that qualification is needed to this standard view, given recent empirical evidence that correlated activity can also increase processing (Nigam, Pojoga, & Dragoi, 2019).

Our aim with the work described here was to determine which of these two perspectives better accounts for the relationship between correlation and synergistic processing in cortical microcircuits at synaptic timescales and beyond. To accomplish this goal, we analyzed the spiking activity of hundreds of neurons recorded simultaneously from each of 25 organotypic cultures of mouse somatosensory cortex (Fig 1). From these recordings we identified hundreds of thousands of triads where individual neurons received significant functional input from two other unique neurons at synaptic timescales (< 14ms). Across these triads, we found that the overall correlation between the unique senders was low but that greater correlations were predictive of greater synergistic processing by the receiving neuron. When we extended the timescale of the analysis to identify significant triads at extrasynaptic windows (up to 3000ms), we observed a significant increase in the overall correlation between unique senders' activity. At the extrasynaptic timescales, we also observed a shift to a negative relationship between sender correlation and synergistic processing. Secondary analysis of the net information transmission and net redundancy in the same triads indicate that both perspectives are valid but become relevant in different correlation regimes. In the low-correlation regimes that we observed at synaptic timescales, correlated activity was positively related to both net information transmission and net redundancy, but the rate of increase of information transmission was greater than redundancy, and, we hypothesize, thereby enabling greater synergistic processing. In the high-correlation regimes that we observed at extrasynaptic timescales, correlated activity was not associated with greater net information transmission but remained positively related to redundancy, consuming bandwidth capacity, and, we hypothesize, thereby reducing synergistic processing.

Figure 1. Methodological approach taken to ask if correlated activity is favorable or unfavorable for synergistic processing in organotypic cultures of mouse cortex. (A) Hour-long recordings of spiking activity were collected *in vitro* from organotypic cultures of mouse somatosensory cortex. (B) Spike sorting yielded spike trains of hundreds of well-isolated individual neurons. (C) Effective connectivity between neurons was determined by quantifying transfer entropy between spike trains. The resulting effective networks were analyzed to identify all effective triads consisting of two effective connections to a common receiver. (D) For each triad, we quantified how correlated the activity of the senders was with mutual information (gray arrow) and decomposed the total information transmitted to the receiver (measured via multivariate transfer entropy, orange perimeter) into redundancy and synergy components (via partial information decomposition, indicated with purple and green areas respectively). (E-F) We sought to differentiate between two alternate hypotheses. (E) Predicted relationship between mutual information and synergy if correlated activity is favorable for computation. (2) Predicted relationship between mutual information and synergy if correlated activity is unfavorable for computation.

RESULTS

We asked whether correlated activity between neurons supports computation in cortical microcircuits by analyzing hour long recordings of spiking activity from organotypic cultures of mouse somatosensory cortex (n = 25) as summarized in Figure 1. Recordings contained between 98 and 594 well-isolated neurons (median = 310). We identified effective connections between neurons in each recording as those that had significant transfer entropy. For every effective triad consisting of one neuron receiving effective connections from two other neurons we quantified the amount of correlated activity between the sending neurons using mutual information. Mutual information was selected for its ability to detect nonlinear as well as linear

dependencies. Our findings were, however, not sensitive to the method for quantifying correlated activity (see Supplemental Materials for more information). The mutual information between senders (Sender$_{MI}$) was normalized to reflect the proportion of the maximum possible mutual information for that triad given the constituent neuron entropies (pMI^{max}). We quantified the amount of computation performed by the receiver on the inputs using 'synergy,' a term derived from partial information decomposition. Synergy was normalized to reflect the proportion of the receiving neuron entropy for which it accounted (pH^{rec}). Across triads, we asked whether synergy was positively or negatively correlated with mutual information. This analysis was repeated at varying timescales as determined by the granularity of the data binning and the delay between bins. All summary statistics are reported as medians followed by 95% bootstrap confidence intervals in brackets.

Correlated activity is associated with more synergy at synaptic timescales

To determine the relationship between Sender$_{MI}$ and synergy at timescales relevant for synaptic processing, we analyzed the functional dynamics at three timescales spanning 0.05 - 14 ms (centered on 3, 5, and 11 ms) for each of the 25 recordings, yielding 75 total functional networks. Each network had many effective triads (count = 806 [448 1350]). The median Sender$_{MI}$ across triads of individual networks was 0.008 [0.005 0.010], indicating that the median mutual information was ~0.8% of the maximum possible mutual information. Sender$_{MI}$ was highly variable around this median value within individual networks, varying across ~7.0 [6.7 7.2] orders of magnitude within individual networks. We then asked how this variability in Sender$_{MI}$ was correlated with variability in synergy.

Plotting synergy as a function of Sender$_{MI}$ across triads for each network revealed clear positive relationships (e.g., Fig 2A). To aggregate results across networks with differing numbers of triads and to maintain the ability to observe possible non-monotonic relationships between Sender$_{MI}$ and synergy, we collapsed results across triads based on Sender$_{MI}$ deciles for each network (Fig 2B). Sender$_{MI}$ and synergy were strongly positively correlated across deciles (Spearman *r* = 0.95 [0.93, 0.98]; $Z_{s.r.}$ = 7.53, n=75 networks, p < 1x10^{-13}; Fig 2C). The median slope over deciles in the log-log space was 0.46 [0.41 0.50] Δlog$_{10}$(pH^{rec}) / Δlog$_{10}$(pMI^{max}) (Fig 2D) indicating that synergy increases exponentially as a function of Sender$_{MI}$ with an exponent of ~0.46. This positive relationship indicated that greater synergistic processing emerges from integration of correlated activity at synaptic timescales.

Figure 2. Increased correlated activity predicts greater synergistic processing at synaptic timescales. (A) Synergy plotted as a function of Sender$_{MI}$ for a representative network shows a positive relationship. Grey dots indicate individual triads. Boundaries of deciles of Sender$_{MI}$ are depicted via dashed lines. Median synergy for each decile (red dots) increased across deciles. The black line shows the linear least squares fit of the black dots (rho = 0.99, slope = 0.39). (B) Synergy across Sender$_{MI}$ deciles for all 75 synaptic timescale networks are shown as red lines. The median synergy and Sender$_{MI}$ for each decile is shown by the black points with error bars indicating 95% bootstrap confidence intervals. (C) Histogram of Spearman rank correlation coefficients for synergy versus mutual information shown in B. A solid black line marks the median correlation coefficient across the 75 networks and the shaded region around the black line shows the 95% bootstrap confidence interval around the median. (D) Average regression fit line across the 75 linear regressions of synergy versus mutual information indicates consistently positive relationship. Shaded region indicates the 95% confidence interval.

Correlated activity is associated with greater gains in information transmission than redundancy at synaptic timescales

Theories regarding the favorability of correlated activity, or lack thereof, for neural computation are motivated by the impact of increasing correlation on information transmission and redundancy. To address these theories, we examined how information transmission and

redundancy covaried with $Sender_{MI}$ and how these relationships related to the generation of synergy. Information transmission was quantified as the multivariate transfer entropy (mvTE). We normalized mvTE to reflect the proportion of the entropy of the receiving neuron accounted for (pH^{rec}). Redundancy was quantified using the redundancy term derived from partial information decomposition and was also normalized to reflect the proportion of the entropy of the receiving neuron accounted for (pH^{rec}).

Theories that view correlated activity as favorable predict that correlated activity increases information transmission. Consistent with this, we found that mvTE was reliably positively correlated with $Sender_{MI}$ at synaptic timescales (Spearman r = 0.99 [0.98 1.00]; $Z_{s.r.}$ = 7.58, n=75 networks, p < 1×10^{-13}; slope = 0.35 [0.32 0.38] $\Delta\log_{10}(pH^{rec})$ / $\Delta\log_{10}(pMI^{max})$; Fig 3A; Table 1). Theories that view correlated activity as unfavorable predict that correlated activity increases redundancy. Supporting this, we found that redundancy was significantly positively related to $Sender_{MI}$ at synaptic timescales (Spearman r = 0.99 [0.98 0.99], $Z_{s.r.}$ = 7.56, n=75 networks, p < 1×10^{-13}; slope = 0.51 [0.47 0.57] $\Delta\log_{10}(pH^{rec})$ / $\Delta\log_{10}(pMI^{max})$; Fig 3A; Table 1). These results indicate that both hypotheses are well motivated with respect to the expected effect of increasing correlated activity.

Next, we related the changes in mvTE and redundancy observed over deciles of $Sender_{MI}$ to those observed in synergy. Consistent with the idea that correlated activity can support greater computation by facilitating information transmission, synergy and mvTE were reliably positively correlated across deciles of $Sender_{MI}$ (Spearman r = 0.95 [0.92 0.98]; $Z_{s.r.}$ = 7.53, p < 1×10^{-13}, n=75 networks; Table 1). Interestingly, synergy and redundancy were also reliably positively correlated across deciles of $Sender_{MI}$ (Spearman r = 0.99 [0.98 0.99]; $Z_{s.r.}$ = 7.56, p < 1×10^{-13}, n = 75 networks; Table 1). This positive correlation is contrary to the idea that redundancy impedes computation at synaptic timesales.

We then examined the *relative* influence of correlated activity on information transmission and redundancy. In a non-log-scaled space, the slope relating $Sender_{MI}$ to mvTE was significantly greater than the slope relating $Sender_{MI}$ to redundancy (1.41 [1.26 1.58] vs. 0.48 [0.45 0.55] (ΔpH^{rec} / ΔpMI^{max}) ; $Z_{s.r.}$ = 7.52, n=75 networks, p < 1×10^{-13}; Fig 3B). Note, though the slope relating $Sender_{MI}$ to mvTE was less than the slope relating $Sender_{MI}$ to redundancy in the log-log space, mvTE was offset vertically over redundancy, corresponding to a significantly larger y-intercept (0.017 vs. 0.003, $Z_{s.r.}$ = 7.52, n=75 networks, p < 1×10^{-11}; Fig 3A). This means that the exponential growth of mvTE was steeper than that of redundancy over the values of $Sender_{MI}$ observed at synaptic timescales. This can be seen by comparing the relationship between $Sender_{MI}$ and mvTE and redundancy without log-scaling (Fig 3B). Because mvTE increases faster than redundancy as a function of $Sender_{MI}$, the difference between the two also grew as a function of $Sender_{MI}$ (slope = 0.13 [0.06 0.19] $\Delta\log_{10}(pH^{rec})$ / $\Delta\log_{10}(pMI^{max})$; $Z_{s.r.}$ = 4.19, p < 1×10^{-4}, n=75 networks; Table 1; curve not shown). The growth of this difference could account for how correlated activity supports synergistic processing at synaptic timescales, as it was positively correlated with synergy across deciles of $Sender_{MI}$ (Spearman r = 0.88 [0.85 0.90]; $Z_{s.r.}$ = 7.52, p < 1×10^{-13}, n = 75 networks; Table 1).

Figure 3. Growth of information transmission (mvTE) is greater than growth of redundancy over deciles of Sender_MI at synaptic timescales. (A) Multivariate transfer entropy (mvTE) and redundancy (Red) increase with mutual information. Synergy data is replotted here from Figure 2B for ease of comparison. (B) Same data as shown in A without log-scaling to show rapid growth of mvTE relative to redundancy. For all plots, lines depict medians and shaded regions depict 95% bootstrap confidence intervals around the median.

Rho \ Slope	Synergy	Redundancy	mvTE	mvTE-Red
Synergy	0.95* \ 0.46*	0.90*	1.20*	1.26*
Redundancy	0.99*	0.99* \ 0.51*	1.34*	1.41*
mvTE	0.95*	0.98*	0.99* \ 0.35*	1.09*
mvTE-Red	0.89*	0.93*	0.99*	0.96* \ 0.31*

Table 1. Relationships between information term at synaptic timescales. Off diagonal: Median Spearman rank correlation coefficients (below diagonal) and linear regression slopes (above diagonal) for pairwise comparisons of synergy, redundancy, multivariate transfer entropy (mvTE), and the difference between mvTE and redundancy (mvTE-Red). Slopes are in units of $\Delta \log_{10}(p\mathrm{H}^{rec}) / \Delta \log_{10}(p\mathrm{H}^{rec})$. Along diagonal: Median Spearman rank correlation coefficients (left) and linear regression slopes (right) for each information term compared to mutual information. Slopes are in units of $\Delta \log_{10}(p\mathrm{H}^{rec}) / \Delta \log_{10}(p\mathrm{MI}^{max})$. * Indicate values that are significantly different from zero after Bonferroni-Holm correction (all p values < 0.001).

Activity becomes more correlated at extrasynaptic timescales, with negative returns for synergy

At synaptic timescales, (normalized) Sender_MI was generally low (~0.8% of maximum possible, as described above). From this, we reasoned that the observed positive relationship between

Sender$_{MI}$ and synergistic processing may have been due to synaptic processing operating in a regime of low overall correlation. To explore this further, we sought to test what happens in a regime of greater overall correlation.

We had observed that the median Sender$_{MI}$ increased progressively across the three synaptic timescales (pMI^{max} across timescales: 3 ms = 0.004 [0.002 0.005]; 5 ms = 0.008 [0.006 0.010]; & 11 ms = 0.019 [0.013 0.023]; Figure 4A), suggesting that extending the analysis to longer timescales would yield even greater Sender$_{MI}$. Examining median Sender$_{MI}$ in seven additional logarithmically spaced timescales, extending out to 3000 ms, showed that it indeed continued to increase (pMI^{max} across timescales: 23 ms = 0.03 [0.02 0.04]; 48 ms = 0.07 [0.05 0.08]; 104 ms = 0.12 [0.09 0.17]; 225 ms = 0.16 [0.10 0.23]; 485 ms = 0.20 [0.14 0.26]; 1044 ms = 0.22 [0.17 0.27]; 2250 ms = 0.25 [0.21 0.33]). All data is shown in Fig 4B.

For the sake of enabling statistical comparison between the patterns observed at longer timescales with those we reported for the synaptic timescale, we defined the timescales that were two orders of magnitude longer than those used to span the synaptic timescales as the 'extrasynaptic timescale' (i.e., those centered on 225, 485, & 1044 ms versus 3, 5, & 11 ms). Comparing Sender$_{MI}$ between these two timescales revealed that sender activity was significantly greater at extrasynaptic timescales than synaptic timescales (0.20 [0.16 0.23] vs. 0.008 [0.005 0.010] pMI^{max}, Z$_{r.s.}$ = 10.51, n = 150 networks, p < 1x10^{-25}; Fig 4C).

Analyzing the relationship between Sender$_{MI}$ and synergy at longer timescales revealed that the positive correlation observed at synaptic timescales was lost as the median Sender$_{MI}$ increased further (Fig 4D-G). At timescales beyond the synaptic timescales, the relationship between Sender$_{MI}$ and synergy inverted gradually. Numerically, this can be seen in the Spearman rank correlation coefficients relating Sender$_{MI}$ to synergy, which started positive and gradually shifted to negative across timescales (Fig 4F; Spearman r across timescales: 3 ms = 0.98 [0.94 0.99]**; 5 ms = 0.93 [0.88 0.96]**; 11 ms = 0.95 [0.88 0.96]**; 23 ms = 0.81 [0.65 0.95]**; 48 ms = 0.47 [0.09 0.70]**; 104 ms = 0.15 [-0.24 0.36]; 225 ms = -0.43 [-0.78 -0.03]**; 485 ms = -0.68 [-0.88 -0.39]**; 1044 ms = -0.96 [-1.00 -0.92]**; 2250 ms = -1.00 [-1.00 -0.99]**; ** = p < 0.05). Though the overall trend between Sender$_{MI}$ and synergy remained positive at the ~48 ms timescale, evidence of a saturation point emerged as synergy began to decrease for Sender$_{MI}$ values greater than ~ 0.07. Across networks, the saturation point was reliably around 0.07 [0.06 0.09]. At longer timescales, a greater percentile of triads had Sender$_{MI}$ values above 0.07. This resulted in diminishing returns of synergy as Sender$_{MI}$ grew further (Fig 4D-E). The relationship between Sender$_{MI}$ and synergy was significantly negative at timescales including and greater than 225 ms. Whereas Sender$_{MI}$ and synergy were positively correlated at synaptic timescales (as described above), Sender$_{MI}$ was significantly negatively correlated with synergy at extrasynaptic timescales (Spearman r = -0.77 [-0.88, -0.62]; Z$_{s.r.}$ = -6.57, n = 75 networks, p < 1x10^{-10}; slope= -0.16 [-0.21 -0.10] Δlog$_{10}$(pH^{rec}) / Δlog$_{10}$(pMI^{max}); Fig 4F-G). The slopes observed at the extrasynaptic timescales were significantly less than those observed at synaptic timescales (Z$_{r.s.}$ = -10.40, n = 150 networks, p < 1x10^{-24}).

These results were obtained using mutual information and synergy values that were normalized by the maximum possible values given the firing rates and bin sizes for each triad at each timescale. This was done because information terms such as mutual information and synergy are sensitive to the entropy of the data being analyzed, which is, in turn, sensitive to firing rates and bin sizes. The log-normal distribution of firing rates and the different timescales generated

variability in the total entropy and thus information terms. By normalizing, we minimized any effects that may have been due to changes in entropy within and across timescales. Critically, however, none of the qualitative results described here depended upon this normalization (see Supplemental Figure 6).

Figure 4. Greater correlated activity emerges at longer timescales with diminishing returns for synergistic processing. (A) Median Sender$_{MI}$ increases across synaptic timescales. (B) Median mutual information continues to increase at extrasynaptic timescales. (C) Median mutual information is significantly larger at extrasynaptic timescales than at synaptic

timescales. (D) Plotting synergy as a function of mutual information across timescales shows that the positive relationship between synergy and mutual information only exists at synaptic timescales where mutual information is relatively low. This relationship becomes negative at extrasynaptic timescales where mutual information is high. Note that mutual information, plotted along the x-axis, varies across sub-panels. A dashed vertical line where mutual information is 0.07 is included to facilitate visual alignment across panels. (E) Curves from D are replotted on the same axes here to show the overall relationship between synergy and mutual information. (F) Spearman rank correlation coefficients of synergy versus mutual information for all networks across timescales show that synergy and mutual information are positively related at shorter timescales and negatively related at longer timescales. (G) Synergy and mutual information are significantly positively correlated at synaptic timescales and significantly negatively correlated at extra-synaptic timescales. For all plots shown above, bars/solid lines indicate medians, shaded regions/error bars depict 95% bootstrap confidence intervals around the median, and * indicates $p < 0.05$.

Correlated activity is associated with greater gains in redundancy than information transmission at extrasynaptic timescales

The robust positive relationship between mvTE and $Sender_{MI}$ observed at synaptic timescales were lost at longer timescales (Fig 5A-B). This can be seen in the Spearman rank correlation coefficients relating mvTE to $Sender_{MI}$, which started positive and gradually shifted towards zero across timescales (Fig 5C; Spearman r across timescales: 3 ms = 0.99 [0.96 1.00]**; 5 ms = 0.98 [0.93 1.00]**; 11 ms = 0.99 [0.96 1.00]**; 23 ms = 0.98 [0.93 1.00]**; 48 ms = 0.90 [0.28 0.98]**; 104 ms = 0.95 [0.89 0.99]**; 225 ms = 0.99 [0.94 1.00]**; 485 ms = 0.88 [0.42 0.95]**; 1044 ms = 0.27 [-0.39 0.71]; 2250 ms = -0.25 [-0.72 0.54]; ** indicates $p < 0.05$). Consistent with the loss of a relationship between mvTE and $Sender_{MI}$ at longer timescales, mvTE ceased to be reliably correlated with synergy across deciles of $Sender_{MI}$ at extrasynaptic timescales (Spearman r = -0.19 [-0.41 0.03]; $Z_{s.r.}$ = -1.88, p = 0.06, n=75 networks; Fig 5D). The correlation between mvTE and synergy was significantly greater at synaptic compared to extra-synaptic timescales ($Z_{r.s.}$ = 9.99, $p < 1 \times 10^{-22}$, n = 150 networks; Fig 5D). These results indicate that the growth of information transmission with correlated activity that contributed to increased synergistic processing at synaptic timescales was lost at extrasynaptic timescales.

Redundancy remained significantly positively related with $Sender_{MI}$ at all timescales (Fig 5E; Spearman r across timescales: 3 ms = 0.98 [0.94 0.99]**; 5 ms = 0.98 [0.92 0.99]**; 11 ms = 0.99 [0.95 1.00]**; 23 ms = 0.99 [0.96 1.00]**; 48 ms = 0.95 [0.87 0.99]**; 104 ms = 0.99 [0.96 1.00]**; 225 ms = 1.00 [0.99 1.00]**; 485 ms = 1.00 [0.99 1.00]**; 1044 ms = 1.00 [0.98 1.00]**; 2250 ms = 1.00 [1.00 1.00]**; ** indicates $p < 0.05$). Though synergy and redundancy had been positively correlated at synaptic timescales (as described above), we found that they were negatively correlated at extrasynaptic timescales (Spearman r = -0.64 [-0.82 -0.53]; $Z_{s.r.}$ = -5.95, $p < 1 \times 10^{-8}$; n=75 networks; Fig 5G). The correlation between redundancy and synergy was significantly greater at synaptic compared to extra-synaptic timescales ($Z_{r.s.}$ = 10.55, $p < 1 \times 10^{-25}$, n = 150 networks; Fig 5G). This result indicates that, at extrasynaptic timescales, redundancy impeded synergistic processing.

Because redundancy, but not mvTE, continued to increase as a function of $Sender_{MI}$ at longer timescales, the difference between the two became smaller. This difference continued to be

Figure 5. Redundancy encroaches upon multivariate transfer entropy at longer timescales, accounting for decreasing synergy at those timescales. (A) Log-scaled multivariate transfer

entropy (mvTE), Redundancy (Red), and Synergy (Syn) versus mutual information, for all timescales. Growth of mvTE with respect to mutual information is steep at short timescales, but decreases across timescales. Redundancy grows with mutual information at all timescales. (B) MvTE curves in A plotted on the same axes. (C) Spearman rank correlation coefficients of synergy versus mvTE across timescales indicates that mvTE saturates at longer timescales. (D) Synergy and mvTE are significantly positively related at synaptic timescales, but not at extra-synaptic timescales. (E) Redundancy curves in A plotted on the same axes. (F) Spearman rank correlation coefficients of synergy versus redundancy across timescales shows how the two are positively related at shorter timescales and negatively related at longer timescales. (G) Synergy and redundancy are significantly positively related at synaptic timescales and significantly negatively related at extra-synaptic timescales. (H) Difference of MvTE and Red curves in A plotted on the same axes shows that the overall trend looks most similar to that of synergy versus MI in Figure 4E. (I) Spearman rank correlation coefficients of synergy versus mvTE-redundancy across timescales shows that the two are positively related at all timescales. (J) Synergy and mvTE-redundancy are significantly positively related at synaptic and extrasynaptic timescales. Synergy versus mutual information data has been replotted from Fig 4D here in A for ease of comparison. For all plots, solid/bold lines indicate medians and shaded regions/error bars depict 95% bootstrap confidence intervals around the median.

positively correlated with synergy at extrasynaptic timescales (Spearman r = 0.50 [0.32 0.66]; $Z_{s.r.}$ = 5.60, p < 1x10^{-7}; n=75 networks; Fig 5J). The correlation between mvTE-redundancy and synergy was significantly greater at synaptic compared to extra-synaptic timescales ($Z_{r.s.}$ = 6.57, p < 1x10^{-10}, n = 150 networks; Fig 5J), however, correlations were significantly positive at both timescales. This indicated that reduction of the gap between mvTE and redundancy across timescales could account for why correlated activity stops supporting synergistic processing at extrasynaptic timescales.

DISCUSSION

Our aim with the work described here was to determine whether correlated activity in cortical microcircuits is favorable or unfavorable for synergistic processing. By applying information theoretic analyses to the spiking activity of hundreds of simultaneously recorded neurons from organotypic cultures of mouse somatosensory cortex, we showed that correlated activity is favorable for synergistic processing when the overall level of correlations are low. We also showed that correlated activity is unfavorable for synergistic processing when overall correlation levels were an order of magnitude greater. Secondary analyses indicated that the relationship between correlated activity and synergistic processing varied as a function of the relative amount of information transmission and redundancy. When overall correlation levels were low, we observed that incremental increases in correlation were associated with larger increases in information transmission than redundancy. We hypothesize that this effectively left greater bandwidth available for synergistic processing. When overall correlation levels were high, incremental increases in correlation were associated with larger increases in redundancy than information transmission. We hypothesize that this effectively caused redundancy to consume the bandwidth available for synergistic processing.

Correlation regimes parse the favorability debate

These findings provide empirical support for each of two seemingly contradictory perspectives regarding the favorability of correlated activity for information processing. These distinct perspectives reflect the dominant perspectives in largely independent domains of research and are not often pitted against one another. The first perspective, held by many in the cognitive rhythms community, states that correlated activity is favorable for information processing because correlated activity facilitates information transmission (Fries, 2015; Fries, 2005; Averbeck & Lee, 2004; Salinas & Sejnowski, 2001; Lisman & Jensen, 2013). The second perspective, held by many in the sensory processing and artificial neural networks communities, states that correlated activity is unfavorable for information processing because correlated activity is viewed as equivalent to capacity-consuming redundancy (Attneave 1954; Barlow 1961). Yet, even within the respective communities there is recognition that the relationship between correlated activity and processing may not be simple. For example, within the cognitive rhythms community, Hanslmayr has explicitly argued that synchronized activity can either facilitate or impede processing (Hanslmayr et al., 2012; Hanslmayr, Staresina, & Bowman, 2016). Likewise, in the sensory processing community, there is evidence that correlated activity can also increase processing (e.g., Nigam, Pojoga, & Dragoi, 2019).

Figure 6. Neural computation can be expressed as a function of the correlation between inputs. When the correlation of inputs is low, synergistic processing benefits from increased correlation. In this regime, both information transmission and redundancy increase with greater correlation but information transmission grows faster than redundancy effectively increasing the bandwidth available for synergistic processing. When the correlation of inputs is high, synergistic processing is hurt by increased correlation. In this regime, redundancy and not information transmission increases with greater correlation reducing the bandwidth available for synergistic processing.

Each perspective, our data suggest, is relevant in distinct correlation regimes. This is summarized in Figure 6. In a low correlation regime, information transmission increases faster than redundancy, allowing correlated activity to support greater synergistic (information) processing. Conversely, in a high correlation regime, redundancy increases faster than information transmission, effectively consuming the available bandwidth and reducing

synergistic processing. Based on this framework, correlated activity can be favorable or unfavorable for synergistic processing, depending upon which regime is locally relevant.

The idea that the favorability of correlated activity for information processing varies non-monotonically can account for would-be inconsistencies with the respective bodies of work surrounding the separate perspectives. For example, while correlated activity is largely held as benefiting cognitive processing within the cognitive rhythms community (e.g., Fries, 2005; Lisman & Jensen, 2013), it can be that information processing requires decorrelation in higher correlation regimes (e.g., Hanslmayr et al., 2012). Indeed, it has been suggested that correlated activity serves distinct roles in distinct neural systems such as the cortex and hippocampus (Hanslmayr, et al., 2016). Consistent with the possibility for regional differences in the favorability of correlated activity, the present findings indicate that the key differentiating functional factor between areas is the correlation levels. Given this framework, we predict that the level of correlated activity in the hippocampus is significantly lower than in the cortex. Breaking from simple interregional differences, however, this framework would also predict that there can be systematic variability in the favorability of correlated activity even within a region. This is consistent with the finding that correlated activity improves synergistic coding in primary visual cortex (e.g., Nigam et al., 2019). As such, the present findings also serve to account for would-be inconsistencies in the sensory processing community.

'Signal' versus 'noise' correlations

The analysis of correlated activity used here differs from the analysis approach commonly used in sensory processing and artificial neural networks research in that we did not separately analyze 'signal correlations' and 'noise correlations.' In sensory processing and artificial neural networks research, in which neural responses to experimentally delivered stimuli are typically evaluated, it is possible to separate activity into what is stimulus-dependent (aka, signal correlations) and what is internally generated (aka, noise correlations) (Gawne & Richmond, 1993; Cohen & Kohn 2011). Here, no stimuli were delivered and the analysis integrated activity over the entire hour of the recording likening our analysis to one of noise correlations only. This does not mean, however, that the non-monotonic function relating correlated activity to synergistic processing need apply only to noise correlations. Though signal and noise correlations can be analytically separated, the same underlying physiological constraints should be expected to hold for both types of correlations. If there is an important difference between the activity comprising signal- and noise-correlations, it is, we argue, that correlations induced by extrinsic factors (e.g., delivered stimuli) reflect transient shifts in the statistics of the local processing dynamics. In this way, the perspective that redundancy reduction is important for sensory processing is consistent with the framework described here. Explicitly, external stimuli could cause a transient burst in correlated activity, necessitating redundancy reduction to free up processing capacity, in order to return the circuit to a regime better suited for synergistic processing. However, much of the activity and processing that takes place in the brain at any moment is self-driven, reflecting the endogenous reverberations recorded here, and resembling what is referred to as noise correlations by the sensory processing and artificial neural networks communities (Greicius et al., 2003; Buzsaki et al., 2014). To test how these results relate to signal and noise correlations, future work must test how synergistic processing relates to the level of correlated activity in response to delivered stimuli.

Related works

The present findings are consistent with prior analyses of synergistic processing and, we hypothesize, could account for previously reported topological determinants of synergistic processing. In a previous analysis of synergistic processing in organotypic cultures Wibral et al. (2017) asked how synergistic processing varied as a function of the maturity of an organotypic culture of cortex. They found that it increased initially but eventually collapsed. Notably, they also mapped the evolution of mutual information among the neurons across the same timeline and found it increased steadily. The underlying pattern, growth of synergistic processing paralleling increasing mutual information when the overall levels were low, and then eventual collapse of synergistic processing with further increases in mutual information once the overall levels were high, are consistent with the pattern observed here. Previous analysis of the topological determinants of synergistic processing found that synergistic processing was directly related to the 'out-degree' of the upstream neurons (Timme et al., 2016). That is, the more neurons that a given upstream neuron made effective connections with, the greater the resulting synergy was in the recipient neurons. In line with this observation, we have previously shown that neurons in the rich clubs of cortical micro-circuits do about twice as much synergistic processing as neurons outside of the rich clubs (Faber et al., 2019). Based on our present findings, we predict that (1) high out-degree neurons have greater correlated activity than low out-degree neurons, and (2) rich club neurons have greater correlated activity than neurons outside of the rich club.

Significance of optimal synergistic processing

The non-monotonic curve relating mutual information to synergy revealed by our analyses indicates that the most synergistic processing was observed when the activity of the sending neurons was correlated at ~7% of the maximum possible. It is unclear whether this reflects a universal optimum or if this value should be expected to vary as a function of the local circuit physiology. Physiology plays an important role in regulating the amount of correlation (e.g., Gutnisky and Dragoi, 2008; Minces et al., 2017). What is not clear based on existing work, however, is whether these changes shift processing relative to a fixed local optimum or whether the optimal correlation also shifts. To address this, future research must compare how the optimal value varies across brain regions, physiological conditions, and behavioral conditions, if at all.

Relevance of in vitro preparation

The use of organotypic cultures in the present work facilitated the recording of hundreds of neurons simultaneously. While organotypic cultures can be expected to differ from intact *in vivo* tissue, organotypic cultures exhibit synaptic structure and electrophysiological activity very similar to that found in vivo (Caeser et al., 1989; Bolz et al., 1990; Götz & Bolz, 1992; Plenz & Aertsen, 1996; Klostermann &Wahle, 1999; Ikegaya et al., 2004; Beggs & Plenz, 2004). For example, the distribution of firing rates observed in cultures is lognormal, as seen in vivo (Nigam et al., 2016), and the strengths of functional connections are lognormally distributed, similar to the distribution of synaptic strengths observed in patch clamp recordings (Song et al., 2005, reviewed in Buzsáki & Mizuseki, 2014). These features indicate that organotypic cortical cultures serve as a reasonable model system for exploring local cortical networks while offering accessibility to large neuron count and high temporal resolution recordings.

We believe the results obtained from these cultures broadly address fundamental questions regarding the nature of neural information processing. As such, beyond the relevance to the cognitive rhythms and sensory processing communities, we expect that our results will be impactful to research efforts seeking to understand neural coding, cognitive processing in symbolic systems, and sources of synergy that lead to emergent cognition. A key next step will be to understand the implications of our results in the context of a behaving brain. Beyond the brain, however, the present findings also have relevance in applied efforts to optimize the computational efficacy of engineered systems (e.g., artificial neural networks / deep learning). More broadly, our findings may reflect a general principle regarding the emergence of synergy in complex systems and, thus, could have relevance for systems beyond the brain (e.g., metabolic systems, societies, transportation networks, financial markets). Finally, our use of domain-general computational approaches enables direct replication of the analyses pursued here in other systems and could thus motivate and/or have implications for work in a variety of other fields.

Conclusions

We show, for the first time, that the relationship between correlated activity and synergistic processing is positive at synaptic timescales with low levels of overall correlation but negative at extrasynaptic timescales with high levels of overall correlation. We propose that the relationship between correlated activity and synergistic processing varies as a function of the overall correlation regime. The shift from a positive to a negative relationship between regimes, in this framework, is accounted for by a shift in the net effect of incremental increases in correlation on information transmission and on redundancy. In the low correlation regime, incremental increases in correlation increased information transmission faster than redundancy thereby increasing the effective bandwidth for synergistic processing. In the high correlation regime, incremental increases in correlation increased redundancy faster than information transmission thereby decreasing the effective bandwidth for synergistic processing. Both dynamics had been hypothesized to exist previously by separate frameworks within separate research communities. The present work serves to bridge across these disconnected domains of work to synthesize the two perspectives into a unified framework.

MATERIALS & METHODS

To answer the question of how correlation and computation are related in cortical circuits, we combined network analysis with information theoretic tools to analyze the spiking activity of hundreds of neurons recorded from organotypic cultures of mouse somatosensory cortex. Due to space limitations, here we provide an overview of our methods and focus on those steps that are most relevant for interpreting our results. A comprehensive description of all our methods can be found in the Supplemental Materials.

All procedures were performed in strict accordance with guidelines from the National Institutes of Health, and approved by the Animal Care and Use Committees of Indiana University and the University of California, Santa Cruz.

Electrophysiological recordings

All results reported here were derived from the analysis of electrophysiological recordings of 25 organotypic cultures prepared from slices of mouse somatosensory cortex. One hour long recordings were performed at 20 kHz sampling using a 512-channel array of 5 μm diameter electrodes arranged in a triangular lattice with an inter-electrode distance of 60 μm (spanning approximately 0.9 mm by 1.9 mm). Once the data were collected, spikes were sorted using a PCA approach (Ito et al., 2014; Litke et al., 2004; Timme et al., 2014) to form spike trains of between 98 and 594 (median = 310) well isolated individual neurons depending on the recording.

Network construction

Networks of effective connectivity, representing global activity in recordings, were constructed following the methods described by Timme et al. (2014, 2016). Briefly, weighted effective connections between neurons were established using transfer entropy (TE; Schreiber, 2000). Transfer entropy quantifies how much information about the prior state of neuron j decreased uncertainty about the current state of neuron i beyond simply knowing the prior state of neuron i itself. To consider synaptic interactions, we computed TE at timescales spanning 0.05 – 14 ms, to capture neuron interactions at timescales relevant to synaptic transmission. This was discretized into three logarithmically-spaced overlapping bins 0.05–3 ms, 1.6–6.4 ms and 3.5–14 ms (Table 2). Timescales were somewhat overlapping in order to ensure that all interactions were captured. Separate effective networks were constructed for each timescale resulting in three networks per recording (75 networks total). To consider extrasynaptic interactions, we computed additional networks at timescales spanning 7.5-3000 ms, discretized into overlapping bins of 7.5-30 ms, 16.15-64.6 ms, 34.8-139.2 ms, 75-300 ms, 161.6-646.4 ms, 348.1-1392.4 ms, and 750-3000 ms (Table 2). This resulted in an additional 7 networks per recording, or 175 networks (250 networks total). Only significant TE, determined through comparison to the TE values obtained with jittered spike trains (α = 0.001; 5000 jitters), were used in the construction of the networks. TE values were normalized by the total entropy of the receiving neuron so as to reflect the proportion of the receiver neuron's capacity that can be accounted for by the transmitting neuron.

Timescale	Bin size (ms)	Delay window (ms)	Delay window (bins)	Timescale Delay (~ms)
1	1	0.05–3	0–3	3
2	1.6	1.6–6.4	1–4	5
3	3.5	3.5–14	1–4	11
4	7.5	7.5–30	1–4	23
5	16.15	16.15–64.6	1–4	48
6	34.8	34.8–139.2	1–4	104
7	75	75–300	1–4	225

8	161.6	161.6–646.4	1–4	485
9	348.1	348.1–1392.4	1–4	1044
10	750	750–3000	1–4	2250

Table 2. Timescales. Bin sizes and delays were chosen to logarithmically span a broad range of neurologically relevant time scales. Timescales were somewhat overlapping in order to ensure that all interactions were captured. In addition, timescales beyond 1 used delays in order to prevent short timescale interactions from influencing long timescale dynamics. Values in the far right column were used to refer to timescales throughout the paper in an abbreviated fashion. For additional information about the binning structure, see Supplemental Figure 1.

Quantifying correlation

The degree of similarity between all pairs of neurons was quantified as mutual information (Shannon & Weaver, 1949; Cover & Thomas, 1991) :

$$MI_{norm}(I \leftrightarrow J) \ = \ \sum_{i,j} p(i,j) \, log \frac{p(i,j)}{p(i)p(j)} \, / \min \left(-\sum_i p_i \log \, p_i \, , \, -\sum_j p_j \log \, p_j \right)$$

(1)

Mutual information is a symmetric measure which quantifies how much uncertainty is reduced in one variable (I) by knowing another (J). All mutual information values were normalized by the maximum possible mutual information that could have occurred between each pair of neurons. The maximum possible mutual information for a given pair of neurons is equivalent to the minimum entropy of the two neurons (Gray & Shields, 1977). Using the normalized values allowed us to consider the proportion of the total possible mutual information that occurred between neurons and to control for differences in entropy across pairs of neurons, improving the interpretability of the numbers obtained. The results reported here are robust to the choice of similarity measure, as shown in Supplemental Figures 4 and 5.

Quantifying computation, redundancy, and information transmission

Computation was operationalized as synergy. Synergy measures the additional information regarding the future state of the receiver, gained by considering the prior state of the senders jointly, beyond what they offered individually, after accounting for the redundancy between the sending neurons and the past state of the receiver itself. Synergy was calculated according to the partial information decomposition (PID) approach described by Williams and Beer (2010, 2011). PID compares the measured bivariate TE between neurons $TE(J{\to}I)$ and $TE(K{\to}I)$ with the measured multivariate TE (the triad-level information transmission) among neurons $TE(\{J,K\}{\to}I)$ to estimate terms that reflect the unique information carried by each neuron, the redundancy between neurons, and the synergy (i.e., gain over the sum of the parts) between neurons. Redundancy was computed as per Supplemental equations 8-10. Synergy was then computed via:

$$Synergy(\{J,K\} \to I) = TE(\{J,K\} \to I) - TE(J \to I) - TE(K \to I) \\ + Redundancy(\{J,K\} \to I)$$

(2)

As with bivariate TE, synergy, redundancy and multivariate TE (mvTE) were normalized by the total entropy of the receiving neuron.

Although there are other methods for calculating partial information terms (Bertschinger et al., 2014; Pica et al., 2017; Wibral et al., 2017; Lizier et al., 2018), we chose this measure because it is capable of detecting linear and nonlinear interactions and it is currently the only measure that quantifies the amount of synergy that occurs in an interaction in which three variables (here, receiver past and pasts of the two transmitters) predict a fourth (receiver future). However, to address previously raised concerns that PID overestimates the redundancy term (Bertschinger et al., 2014; Pica et al., 2017), and consequently synergy, we also used an alternate implementation of PID that estimates synergy based on the lower bound of redundancy. In this implementation, the effective threshold for triads to generate synergy is higher. This approach yielded the same qualitative pattern of results at synaptic timescales (see Supplemental Figure 7). At extra-synaptic timescales, this alternate version of synergy remained positively related to $Sender_{MI}$. This is likely due to the fact that, in triads with sufficiently high synergy to be included in this analysis, redundancy had not effectively cannibalized the mvTE. As a result, the only triads left in this analysis were those with generally high synergy.

Note, we chose not to consider higher order synergy terms, for systems with more than two transmitting neurons, due to the increased computational burden it presented (in addition to the combinatorial explosion of increased numbers of inputs, the number of PID terms increases rapidly as the number of variables increases). However, based on bounds calculated for the highest order synergy term by Timme et al. (2016), it was determined that the information gained by including an additional input beyond two either remained constant or decreased. Thus, it was inferred that lower order (two-input) computations dominated.

Statistics

To aggregate results across networks with differing numbers of triads and to maintain the ability to observe possible non-monotonic relationships between sender mutual information and synergy, we collapsed synergy, redundancy and mvTE across triads based on deciles of sender mutual information for each network. That is, we calculated the median values of synergy, redundancy, and mvTE for each decile of sender mutual information. These values were used in all analyses. We obtained the same qualitative pattern of results when analyses are performed at the triad-level.

All values were log_{10} scaled in all analyses unless stated otherwise. This scaling was motivated by the inherent log-normality of these variables, as well as by the goodness-of-fit obtained for relationships in the log_{10} space compared to the linear space.

All results are reported as medians followed by the 95% bootstrap confidence limits (computed using 10,000 iterations) reported inside of square brackets. Accordingly, figures depict the medians with errorbars reflecting the 95% bootstrap confidence limits. Comparisons between conditions or against null models were performed using the nonparametric Wilcoxon signed-rank test, unless specified otherwise. The threshold for significance was set at 0.05, unless indicated otherwise in the text. Bonferroni-Holm corrections were used in cases of multiple comparisons.

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