TITLE

Cerebellar patients have intact feedback control that can be leveraged to improve reaching

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ABSTRACT

It is thought that the brain does not simply react to sensory feedback, but rather uses an internal model of the body to predict the consequences of motor commands before sensory feedback arrives. Time-delayed sensory feedback can then be used to correct for the unexpected—perturbations, motor noise, or a moving target. The cerebellum has been implicated in this predictive control process. Here we show that the feedback gain in patients with cerebellar ataxia matches that of healthy subjects, but that patients exhibit substantially more phase lag. This difference is captured by a computational model incorporating a Smith predictor in healthy subjects that is missing in patients, supporting the predictive role of the cerebellum in feedback control. Lastly, we improve cerebellar patients' movement control by altering (phase advancing) the visual feedback they receive from their own self movement in a simplified virtual reality setup.

INTRODUCTION

Humans normally rely on a balance of feedback and predictive control mechanisms to make smooth and accurate movements. Proprioceptive and visual feedback are necessary for determining body postures at the beginning and end of a movement and can be used to guide slow movements accurately. However, feedback is time delayed, and thus it never represents the current state of the body during movement. Because of this, it is thought that we depend on internal models of the body that are built based on prior experience. These models can be rapidly accessed and thus provide a fast internal prediction system to estimate how a movement will unfold, enabling us to better understand where our limbs are at any given moment. This allows us to make fast and accurate movements despite long-latency feedback.

People with cerebellar damage show a characteristic pattern of incoordination during movement that is referred to as ataxia. When reaching, they make curved movements that miss intended targets and require multiple corrections. This pattern of over- and undershooting a target (dysmetria) and oscillatory corrections (intention tremor) are hallmarks of cerebellar ataxia. One hypothesis that might explain ataxia is that the predictive estimation and control provided by cerebellar circuits is dysfunctional or lost (Wolpert, Miall, and Kawato 1998; R. Chris Miall et al. 2007).

Normally, the estimation of limb state (i.e., position and velocity) benefits from integrating proprioceptive measurements with an internal predictive control model during a movement (Paillard and Brouchon 1974; Adamovich et al. 1998; Fuentes and Bastian 2010). However, patients with cerebellar damage do not seem to receive this benefit (N. H. Bhanpuri, Okamura, and Bastian 2013; Weeks, Therrien, and Bastian 2017). Worse, it is possible that their predictive model actually conveys incorrect state information during active movements, which could corrupt rather than enhance proprioceptive estimation of limb state. This difficulty of predicting the future state of limbs during active movement leads to movements that are poorly directed and scaled, requiring ongoing corrections to reach a goal location.

Patients with cerebellar ataxia may rely more heavily on visual feedback to correct dysmetric movements (Beppu, Nagaoka, and Tanaka 1987; Beppu, Suda, and Tanaka 1984; Day et al. 1998). A drawback of visual feedback is that it is slower than proprioception; intention tremor in these patients' movements is thought to stem from dependence on time-delayed visual

feedback to make corrections (Day et al. 1998). However, it is not known how well they

incorporate this visual feedback into their movements. Is visual feedback control impaired? Or

does the dysmetria stem solely from errors in predictive (i.e., feedforward) control (M. Manto,

Godaux, and Jacquy 1994; Nasir H. Bhanpuri, Okamura, and Bastian 2014; M. A. Smith and

Shadmehr 2005)? A gait study by Morton and Bastian suggested that cerebellar patients could

use feedback information to make reactive corrections during split-belt treadmill walking in

order to maintain stability, but lacked the ability to adapt their predictive motor patterns (Morton

and Bastian 2006). Other studies have indirectly supported the notion that patients can

incorporate some level of visual feedback control in reaching (M. Smith, Brandt, and Shadmehr

2000; Day et al. 1998).

In this study, we used behavioral experiments and computational modeling to test for any

impairment in visual feedback control (correction based on measured error) and disambiguate it

from previously described impairments in feedforward control (Broersen et al. 2016; Bares et al.

2007). Subjects performed a visuomotor task which required them to track an unpredictable

target (Roth et al. 2011). This method allowed us to determine that cerebellar patients can

integrate visual feedback control similarly to healthy, age-matched control subjects. We then

hypothesized that we could exploit intact feedback control to reduce dysmetria by dynamically

altering visual feedback closed-loop in a simplified virtual reality setting. Specifically, we

provided an acceleration-dependent alteration to visual feedback of a hand cursor to compensate

for time delays and allow patients to use feedback more effectively. This real time controller

successfully reduced patients' dysmetria.

METHODS

EXPERIMENTAL MODEL AND SUBJECT DETAILS

A total of 17 patients with cerebellar deficits and 14 age-matched controls were tested in one or more of the following experiments. Patients were excluded if they had any clinical or MRI evidence of damage to extra-cerebellar brain structures, or clinical evidence of dementia, aphasia, peripheral vestibular loss, or sensory neuropathy. The age-matched controls were clinically screened for any neurological impairments. Experiments 1-2 tested 11 cerebellar patients (7 male, 4 female) and 11 age-matched controls (4 male, 7 female). Patient and control ages were within +/-3 years of age. The one exception is a pairing of a 78 year old patient with a 71 year old control. Experiment 3 tested 12 cerebellar patients (8 male, 4 female) and 12 age-matched controls (3 male, 9 female), and all patient and control ages were within +/-3 years of age. Subjects gave informed consent according to the Declaration of Helsinki. The experimental protocols were approved by the Institutional Review Board at Johns Hopkins University School of Medicine. Each subject used his or her dominant arm for all tasks. The only exception was one unilaterally affected cerebellar patient who was instructed to use her affected, non-dominant, hand. We quantified each subject's ataxia using the International Cooperative Ataxia Rating Scale (ICARS) (Trouillas et al. 1997). Because this study involves upper limb reaching behavior, we calculated an Upper Limb ICARS sub-score comprising the sum of the upper-limb kinetic function elements of the test. The results of the ICARS as well as demographic information for all patients are shown in Table 1.

EXPERIMENTAL APPARATUS AND TASK INSTRUCTIONS

For all experiments, subjects were seated in a KINARM exoskeleton robot (BKIN Technologies Ltd., Kingston, Ontario, Canada), shown in Figure 1A, which provided gravitational arm support while allowing movement in the horizontal plane. A black video screen occluded the subjects' view of their arm movements. The shoulder position was fixed at a 75 degree angle, as shown in Figure 1C. The wrist joint was also fixed; therefore, the elbow joint was the only freely mobile joint. Data were recorded at 1 kHz. The KINARM system exhibits a cursor delay. Using a high-speed camera, we measured this delay (0.048s) and took the delay into account in modeling the human control system.

A 1 cm diameter white dot (cursor) was projected onto the display to indicate the subject's index fingertip position. The display was calibrated so that the projected dot position aligned with the subject's fingertip position. Subjects performed three experiments: sum-of-sines task (Experiment 1), single-sines task (Experiment 2), and discrete reaches (Experiment 3).

For Experiments 1 and 2, subjects were instructed to try to keep the cursor in the center of the target, a 1.5 cm diameter green dot (Figure 1C). The target angle followed a pseudorandom sum-of-sines (Figure 1D) or single-sine pattern. Each trial was 100 seconds long. We tested three different Feedback Gain conditions in the sum-of-sines (Experiment 1) task: 1.35 (cursor moves 35% farther than hand), 0.65 (cursor motion is attenuated by 35%) and 1.0 (veridical feedback; Figure 1B). Subjects were not informed that there was a gain change.

111   For Experiment 3, the robot moved the arm to align the cursor with the red dot start

112 position (55 degree elbow angle) before each reach. After approximately 2 seconds, the red dot

113 disappeared, and a green target dot (1.5 cm diameter, at 85 degree elbow angle) appeared

114 elsewhere on the screen. Subjects were instructed to bring the white cursor dot to the center of

115 the green target dot (a 30 degree flexion movement) as smoothly and accurately as possible

116 without over or undershooting the target. If the fingertip did not reach within 1.75 of the target

117 within 800 ms, the green dot changed to blue and subjects were instructed to complete the reach

118 (trials were not repeated); the subjects were also asked to try to move faster on the next trial. The

119 next trial started after the subject kept the fingertip in the target dot for two continuous seconds.

121   Healthy control subjects performed five practice trials and patients performed 10 practice

122 trials to familiarize themselves with the procedure. If subjects were still confused about the

123 procedure after the practice trials, they were given more practice trials until they were

124 comfortable with the procedure.

126   Control subjects performed blocks of five reaches of each of the following Acceleration-

127 Dependent Feedback Gain conditions, where the cursor angle was set to follow the elbow angle

128 plus an acceleration-dependent term:

129     $$\text{CursorAngle(t)} \; = \; \text{ElbowAngle(t)} + k_a \frac{d^2}{dt^2}\text{ElbowAngle(t)}$$

130 The 8 gain conditions tested were k_a = 0, 0.005, 0.010, 0.015, 0.020, −0.005, −0.010, −0.015,

131 and −0.020. Subjects were given five trials of one Feedback Gain before being exposed to the

132 next Feedback Gain on the list. This was to encourage subjects to focus on the white dot

position. Trial order was not randomized because in pilot experiments, when the gains were

randomized, the subjects seemed to focus on their proprioception rather than the visual feedback.

Cerebellar patients performed blocks of 10 reaches with a single Acceleration-Dependent

Feedback Gain. Patients started with an Acceleration-Dependent Feedback Gain of 0 (veridical

feedback). Individual reaches were categorized as hypometric, on-target, or hypermetric. Based

on the mode of this categorization for the 10 reaches, the Acceleration-Dependent Feedback

Gain was increased, remained the same, or decreased. The amount by which the Acceleration-

Dependent Feedback Gain was altered was determined using the Parameter Estimation by

Sequential Testing (PEST) algorithm (see Implementation of the PEST Algorithm (Experiment

3)) (Taylor and Creelman 1967). We also tested six of the twelve cerebellar patients on the

control subject task (blocks of 5 trials on the 8 gains listed above); others could not due to time

constraints.

Some subjects completed only a subset of the experiments due to time constraints. For

every experiment, between trials, subjects were told to relax while the robot moved the subject's

hand to bring the cursor to the start position.

EXPERIMENTAL DESIGN AND STATISTICAL ANALYSIS

Generating the Sum-of-Sines Target Trajectory (Experiment 1)

The goal of Experiment 1 was to determine how well patients and controls could track an

unpredictable sum-of-sines stimulus and probe their ability to use visual feedback for movement

control. The target trajectory comprised 15 sine waves whose frequencies were prime multiples

of 0.05 Hz, namely 0.1, 0.15, 0.25, 0.35, 0.55, 0.65, 0.85, 0.95, 1.15, 1.45, 1.55, 1.85, 2.05, 2.15,

and 2.35 Hz. Phases of each sinusoid were randomized. Each trial was 100 s long, comprising

five replicates of the sum-of-sines trajectory. The sinusoids were scaled so that the *angular*

velocity of each sinusoid never exceeded 720 degrees per second while the *positional* amplitude

of each sine wave never exceeded 2 degrees. The non-harmonic relation of the component

sinusoids created a temporally complex target motion with 45 degrees of freedom (amplitude,

phase, and frequency for 15 sinusoids) that repeats every 20 s; a portion of the trajectory is

shown in Figure 1D, wherein it can be observed that the signal trajectory includes multiple

seemingly random turn-arounds within even very short timescales. This complexity, coupled

with the long period, makes this target motion far less predictable than a simple single-sine

motion (Roth et al. 2011). Lastly, the dramatic increase in tracking phase lag presented in this

paper (see Results) for sum-of-sine responses recapitulates the main finding of (Roth et al. 2011),

confirming that from a practical point of view subjects were less able to predict the movement

trajectories. Nevertheless, this signal design allowed good signal-to-noise ratio at each frequency

while avoiding excessively large or fast motions of the target, making it well suited as a probe

signal for tracking behavior (Roth et al. 2011). The normalized magnitude of Fourier spectrum of

our input signal is shown in the top half of in Figure 1E. Five trials were conducted for each

condition tested.

Estimating Frequency Response from the Sum-of-Sines Data (Experiment 1)

All analysis was performed using custom scripts in MATLAB (The Mathworks Inc.,

Natick, MA, USA). To obtain the steady-state frequency response of the subject, the first period

(20 seconds) was discarded as transient, leaving four periods per trial. The data were manually

inspected for unusual activities that were not representative of the subject's typical behavior. For

example, if the subject turned away from the screen to cough or talk, movement would cease for

a few seconds and the data from those few seconds were removed from further analysis. The

movement trajectories for a given subject were then averaged across trials at each time instant,

excluding any deleted data. The averaged data were linearly detrended and converted to the

frequency domain via the discrete Fourier transform (DFT). An example of the result of this

process for a cerebellar patient is shown in Figure 1F (the frequency domain data is complex

valued at each frequency so only the magnitude is shown). To estimate a subject's frequency

response, we calculated the ratio of the DFT of the subject's movement to the DFT of the

underlying target trajectory at each of the 15 frequencies in the sum-of-sines. The result of this

calculation is 15 complex numbers, called *phasors*, representing the frequency response estimate

for a given subject. The magnitude of each phasor is the *gain* and the angle is the *phase* of the

subject's response at that frequency.

Phasor Plot

To visualize the frequency response, we used Phasor Plots as shown in Figure 2A. In

these plots, the gain is the radial distance from the origin, and phase lag is the clockwise angle of

the data with respect to the horizontal axis. Perfect tracking at a given frequency corresponds to

unity gain and zero phase lag, as illustrated by the large blue dot in Figure 2B. The distance

between any point on the phasor plot and this blue dot provides a measure of the amplitude of the

(sinusoidal) error signal at that particular frequency as a proportion of the input signal amplitude.

Additionally, this visualization can be enhanced with a circle with a 0.5 radius centered at

+0.5 along the horizontal axis as shown in blue in Figure 2B. Points on this circle correspond to

the ideal response gain for minimizing error given a particular phase lag (Roth et al. 2011).

Points on this circle represent the gain values that minimize error assuming the subject cannot

further minimize phase lag. Points outside the circle indicate the subject is moving too much for

a given phase lag, i.e., if they moved with a lower amplitude they would achieve a lower tracking

error. Points within the circle may represent striking a balance between effort and error in that

the subject is not moving enough to fully minimize their error given a certain phase lag. Lastly,

points that lie on the unit circle, traced in bold black in Figure 2C, would indicate that the subject

is replicating the sinusoidal component exactly, albeit at a phase shift.

Phasor Plot Scaling

If a subject were to "fully" respond to an applied visual gain, the subject would need to

scale his or her movement so that the visual output appeared the same as it did in the veridical

feedback condition, although there is no constraint (or instruction) to do so. In reality a subject

may scale his or her movements more than this, less than this, or even not at all. To quantify this,

we fit a Scaling Factor that, when multiplied by the frequency response phasors for a given

Feedback Gain condition, best aligned the phasors with those of the veridical condition. We only

included the five lowest frequencies in this calculation because at these frequencies subjects

generally appeared to have robust responses (based on visual inspection of the data). At high

frequencies, however, response magnitudes were low and therefore fitting the Scaling Factor

could be dominated by noise.

Scaling Factor (dependent measure) was analyzed using a 2-way ANOVA, testing for the

effects of two independent variables, group (patient vs. control) and Feedback Gain (0.65 and

1.35). If a main effect was found to be significant, we calculated an effect measure (η_p^2) using

the Measures of Effect Size toolbox for Matlab (Hentschke and Stüttgen 2011).

Model Fitting and Model Selection

To capture the visuomotor tracking response of both cerebellar patients and age-matched

healthy controls, we adapted the classic McRuer gain-crossover model: a delayed, scaled

integrator which specifically assumes that the subject is responding to an unpredictable stimulus

(McRuer and Krendel 1974). We hypothesized that the patient and control models would be

equivalent except for the magnitude of the feedback delay. To test this, we considered a more

general class of models that allows for distinct parameters for the healthy subjects and controls,

and includes the possibility of distinct delays on the visual measurement of target motion from

that of self-movement feedback (which can incorporate for example, proprioception, which

generally incurs a lower latency than visual). To determine the simplest combined model of

patients and controls which provided both a good and consistent fit without overfitting, we used

a model selection process similar to that described in (Madhav et al. 2013) based on Experiment

1 data (sum-of-sines). In the most flexible model, all patient and control parameters were

allowed to vary independently with eight free parameters: $k_{patient}$, $k_{control}$, Visual Gain$_{patient}$, Visual

Gain$_{control}$, Visual Delay$_{patient}$, Visual Delay$_{control}$, Feedback Delay$_{patient}$, and Feedback Delay$_{control}$.

The following model selection procedure aimed to determine which of those eight parameters

should be free and which should be yoked together. Different combinations of yoked parameters

were tested as well as different model structures. Some of these model structures allowed for the

elimination of one or more of the blocks within the model structure.

249   The following procedure was repeated for each possible model. For each subject, we

represented their frequency response as an array of 15 complex numbers (one for each of the

frequencies tested in the sum-of-sines experiment). We began by pulling 10 of the 11 age-

matched patient–control pairs from the full dataset. Then, we took the average of those 10

patients' (and, separately, controls) frequency responses at each tested frequency. Using the

MATLAB function 'fminsearch,' we used these average frequency response functions to fit the

current model parameters to the average data by minimizing the frequency-domain (FD) error:

$$\text{FD-error} = \|\text{control}_{\text{left out}} - \text{control}_{\text{model fit}}\|^2 \; + \; \|\text{patient}_{\text{left out}} - \text{patient}_{\text{model fit}}\|^2 \qquad (1)$$

where *control* and *patient* in the above equation were arrays with 15 complex values,

corresponding respectively to frequency responses of healthy control subjects and patients at the

15 frequencies tested. This was repeated 100 times with different initial parameter values

selected for the 'fminsearch' function, increasing the likelihood of finding a global minimum.

The model parameters that generated the lowest overall error were kept (as well as the magnitude

of the error). This was repeated for each patient–control pair, yielding 11 sets of model

parameters and 11 leave one out error values.

267   The leave one out error values were averaged together to create the gross leave one out

error for that model structure. This was our gauge for the ability of the model to capture the

responses. The maximum singular value of all 11 sets of the model parameters for that particular

model was used as our gauge for model consistency. This was repeated for all potential models.

We then selected a best model based on the tradeoff of model fit, model consistency, and number

of free parameters. Finally, we used bootstrapping to generate confidence intervals for the

parameter values in our best model.

We validated the frequency-domain fits in the time domain. We converted each

frequency-domain model (which includes patient and control submodels) to state space in

Matlab, and simulated the model pair using the lsim command (Figure 4S2). The input was the

sum-of-sines target angle trajectory used in experiments. The model output produced a distinct

prediction for the elbow-angle trajectory for each group (patients and controls; Figure 4C). These

simulated elbow-angle responses were compared to subject responses as follows. We averaged

across trials for each subject to compute a single time-domain response for each patient and each

age-matched control; we then averaged across subjects in each group to compute a mean elbow-

angle response for patients and a mean elbow-angle response for controls. Given the simulated

model responses and actual patient and control mean responses, the time-domain (TD) error was

calculated as follows:

$$\text{TD-error} = \int_{20}^{100}(\text{control}(t)_{\text{mean}} - \text{control}(t)_{\text{model}})^2 + (\text{patient}(t)_{\text{mean}} - \text{patient}(t)_{\text{model}})^2 dt$$

where the integration is taken over the last 80 seconds of the 100s trial period. The TD-error was

normalized so that the maximum error was 1 for visualization purposes.

Generating the Single-Sines Trajectory (Experiment 2)

In Experiment 2, we wanted to determine how well patients and controls could track a

predictable single sine wave. Every other frequency tested in the sum-of-sines condition was

tested as a single, standalone sine wave: 0.1, 0.25, 0.55, 0.85, 1.15, 1.55, 2.05, and 2.35 Hz. The

amplitude of each sine wave matched (component-wise) the sum-of-sines experiments. Subjects

were once again instructed to keep the cursor in the target dot as much as possible. The order of

presentation of the stimuli was randomized for each subject.

Processing the Single-Sines Data (Experiment 2)

The processing of the data for the single-sine condition was identical to the processing of

the sum-of-sines data, except that there was no averaging across trials and no manual

inspection/filtering of the data for unusual activities. This is because we were only looking at one

frequency from each sine wave trial, and any error caused by an unusual, aperiodic activity (such

as pausing) would introduce very little power at any individual frequency.

Comparing Phase Lags between Sum-of-Sines and Single-Sine Conditions (Experiments 1 & 2)

We tested whether the cerebellar group showed a different pattern of phase lag across

frequencies compared to controls. Specifically, we compared the phase lag for the lowest

common frequencies (0.10, 0.25, 0.55, 0.85, 1.15) in the sum-of-sines and single-sine conditions

across the two groups. We hypothesized that the control group would be able to use prediction

and follow the single sine wave with little phase lag compared to the cerebellar patients. We

expected that there would be less of a difference between groups when they followed the sum-of-

sines. We used a parametric two-way ANOVA for circular data called the Harrison-Kanji test for

this analysis (Berens 2009).

 Implementation of the Acceleration-Dependent Feedback Gain for Experiment 3

In Experiment 3 we attempted to improve dysmetria for discrete reaching by individually

optimizing visual feedback gains. Using the KINARM's real-time computer, we calculated the

average of the previous 100 elbow angular acceleration values (at 1 kHz sampling, this resulted

in a ∼ 50 ms delay) as an approximation of the instantaneous acceleration. This instantaneous

acceleration was multiplied by the Acceleration-Dependent Feedback Gain (k_a), added to the

real elbow angle, and the position of the cursor was displayed on the Kinarm screen at this new,

slightly shifted angle.

Quantification of Dysmetria for Experiment 3

We quantified dysmetria in this single-joint task by measuring the elbow angle at which

the subject made his or her first correction. In a smooth and accurate reach, the ratio between the

angle of first correction and the goal angle would be 1. We determined the angle of the first

correction by finding when the velocity crossed zero after the initiation of the reach. The angle of

the elbow at this time point is the angle of the first correction. This angle was divided by the goal

angle of 30 degrees. If the result was greater than 1.03, the reach was categorized as hypermetric,

and likewise, if the result was less than 0.97, the reach would be categorized as hypometric.

Results between 0.97 and 1.03 were classified as "on target" reaches.

Implementation of the PEST Algorithm (Experiment 3)

The Parameter Estimation by Sequential Testing (PEST) algorithm was used to

iteratively determine the best Acceleration-Dependent Feedback Gain values to apply in

Experiment 3 by analyzing the history of the responses to different applied values (Taylor and

Creelman 1967). If the mode of the initial set of reaches was hypermetric, the Acceleration-Dependent Feedback Gain would be decreased. Likewise, it would be increased if the mode of the set was hypometric. The initial step size used for the PEST algorithm was 0.01. The maximum step size for the PEST algorithm was limited to 0.01 and the minimum step size was 0.0035. The maximum Acceleration-Dependent Feedback Gain was set to +/-0.02. The PEST algorithm was terminated when two blocks of the same Acceleration-Dependent Feedback Gain yielded a mode of reaches classified as "on target." Alternatively, if this portion of the experiment took longer than approximately 20 minutes or the subject was experiencing fatigue, the most successful Acceleration-Dependent Feedback Gain was selected based on those which had already been tested. To show the effects of the full spectrum of Acceleration-Dependent Feedback Gains on cerebellar patients, we also had 7 cerebellar patients complete the control task in addition to the PEST block.

RESULTS

Experiment 1: Cerebellar Patients and Age-Matched Controls Respond Similarly to Rescaling of Visual Self-Motion Feedback

To probe participants' ability to use visual feedback, we challenged cerebellar patients and age-matched controls to keep a cursor within a target dot that was following an unpredictable trajectory. The normalized Fourier spectrum (magnitude only) of the target trajectory is shown in Figure 1E and the spectrum of a single subject's response is shown in Figure 1F. Note that this subject had clear peaks at all of the frequencies of target movement in the veridical condition (1x).

Subjects also were exposed to two Feedback Gain conditions where the cursor was

presented at 0.65x or 1.35x. A phasor plot for each Feedback Gain condition is shown for a

single cerebellar patient in Figure 3A. Points with the smallest phase lag (~30°) are responses

from the lowest frequencies (0.1 Hz). Responses at the five lowest frequencies are marked with

solid dots. As the input frequency increases, the phase lag increases and the plotted points move

progressively clockwise around the origin. At the lowest frequencies, note from Figure 3A that

the subject scales his movement in response to the Feedback Gain applied. For the 0.65

Feedback Gain condition, he increases the scaling of his movement in comparison to the

veridical condition, as expected. Similarly, in the 1.35 Feedback Gain condition, he decreases the

scaling of his movement in comparison to the veridical condition.

For each patient, we computed a Scaling Factor based that best scaled responses at the

lowest 5 frequencies (Methods); to visualize how well this Scaling Factor represents our data, the

Response Gain data from the cerebellar patient in the 1.35 Feedback Gain condition shown in

Figure 3A is multiplied by its scaling factor to yield the corresponding line in Figure 3B. If the

scaling factor is a good fit for the data, the data should rest on top of the veridical line. Note that

the phase is not modified by this scaling computation, so we should not expect to see an

improvement in phase alignment in this second plot.

Figure 3C shows the Scaling Factors for all subjects for each Feedback Gain condition.

We conducted a one-sided t-test to determine whether patients scaled their gain in the

hypothesized direction against the null hypothesis that patients' scaling factors would be 1 (i.e.,

they would not respond to the applied feedback gain). Both groups scaled up (patients: p=0.03,

t=-2.1, DOF=10; controls: p=4×10^{-6}, t=-8.3, DOF=10) or scaled down (patients: p=0.005, t=3.23,

DOF=10; controls p=0.0002, t=5.3, DOF=10) their movement, commensurate with the

respective decrease or increase of the cursor Feedback Gain. We performed a two-way ANOVA,

confirming that the effect of Feedback Gain (0.65 vs. 1.35) on Scaling Factor was highly

significant ($F(1,40)$=59.7, p=2×10^{-9}, η_p^2=0.7), whereas the effect of group (patient vs. control) on

Scaling Factor was not significant ($F(1,40)$=0.05, p=0.83), with no significant interaction

between group and gain ($F(1,40)$=3.57, p=0.07). We accounted for the samples being dependent

on one another because each subject was exposed to both the 0.65 and 1.35 gain conditions. The

effect size was computed using the Hentschke and Stüttgen toolbox (Hentschke and Stüttgen

2011).

Note that the Scaling Factor in for the gain of 1.35 was typically approximately 1.2.

Intuitively, this indicates that subjects rescaled their movements as if to compensate perfectly for

an experimentally applied Feedback Gain of 1.2, i.e., they did not fully compensate for the

change in gain. Likewise, for a Feedback Gain of 0.65, the Scaling Factor was typically

approximately 0.8, again implying that subjects compensated, albeit not fully, for the visual

rescaling (Figure 3). Critically, the patients' responses to the feedback scaling were comparable

to that of age-matched controls, suggesting that they were able to use visual feedback in a

substantively similar manner.

 Cerebellar Patient Performance Best Captured by Long Latency Closed-Loop Model

In computational terms, one can interpret the data from Experiment 1 to mean that

cerebellar patients had a functional feedback loop in their control system. Here we asked if they

are using the same "control structure" (i.e., a model of the interplay between sensory feedback,

external sensory input, and motor output) as age-matched controls. Because the cerebellar and

age-matched control groups scaled their movements similarly in Experiment 1, one might

hypothesize that they were using a similar control structure. However, the scaling was measured

relative to each subject's baseline movement in the veridical condition and was not a measure of

their overall error performance on the task; for example, issues of phase lag would not be

captured by the scaling analysis. Thus, here we use our findings from Experiment 1 along with

the model selection procedure described by Madhav et al. (2013) to determine any differences in

control structures used by patients and age-matched controls.

Consider the hypothesized model depicted in Figure 4A. In this model, the brain

calculates the error between perceived elbow angle and target angle, as shown in the subtraction

calculation in the feedback diagram. The model merges the cascade of the subject's internal

controller and mechanical plant (arm and robot dynamics); the combined plant and controller is

treated as a classic McRuer gain-crossover model—a scaled integrator—a model based on the

assumption that the subject is responding to an unpredictable stimulus (McRuer and Krendel

1974). Our hypothesis is that all model parameters would be equivalent between patients and

age-matched controls, except that patients would have a feedback delay commensurate with their

visual processing time (~140-250 ms) and controls would have a lower-latency feedback delay

commensurate with their proprioceptive feedback processing time (~110-150 ms) (Cameron, de

la Malla, and López-Moliner 2014; N. H. Bhanpuri, Okamura, and Bastian 2013). This is

because we expect that patients would rely more on (slower) visual feedback to compensate for

their deficient estimation of limb state.

To test this hypothesized model, we performed model fitting and model selection based

on 60 related models (Figure 4S1A,B). Our hypothesized model was just one possibility and the

parameter values of the models were not constrained *a priori*. The models were compared based

on joint consideration of model consistency and model fit. Model fitting and selection produced

four models (called Models W, X, Y, and Z) that were nearly equivalent in their trade-off

between model inconsistency and model fitting error (Figure 4S1C). Moreover, three of the four

models (Models X, Y, and Z) were extremely similar in their structure and parameters (Figure

4S1D and Table 2). One of these, Model Y, matched our hypothesis (Figure 4A) except that

feedback delay from control subjects was shorter than we hypothesized (30ms, see Table 2).

Model W differs slightly in model structure and parameters but also exhibits a smaller feedback

delay for controls than patients. Indeed, in all four top models, the feedback delay was

substantially shorter for control subjects than cerebellar patients. This suggests that controls can

rely on an internal model of their hand position and/or proprioceptive feedback to make

corrections for their future movements while cerebellar patients must rely on delayed visual

feedback (see Discussion). We selected Model Z as the Best Model on the basis of it having the

fewest free parameters of the top four models (Figure *4*B). This Best Model closely matches our

hypothesis except that it does not include any feedback delay for control subjects.

In addition to the parameter values having consistent values across the top four models,

they also have intuitively plausible values (Table *2*). While the true parameters have biological

limitations, we did not restrict their values during the fitting procedure. This provides a useful

diagnostic tool, since unrealistic parameter fits would indicate inadequate model structure. In

three of the models (Models X, Y, and Z) Visual Delays were found to be 170 ms, which is

biologically plausible. The tight consistency of visual delay is likely a reflection of the fact that

model fitting accuracy is expected to be quite sensitive to phase differences, and in our model,

delay has the biggest impact on phase, so that parameter is expected to be highly constrained by

the data. Model W exhibited a low Visual Delay of 110ms for controls, equal to the feedback

delay for controls. One possible explanation for this model is that the sum-of-sines trajectory was

not completely unpredictable and subjects were able to reduce feedforward latency with partial

anticipation. Visual Gain values were all approximately 0.40 which also seems reasonable given

a visual inspection of the data: subjects do not appear to be attempting to replicate the full

magnitude of the signal, but some smaller portion of the signal.

As a final test of our modeling approach, we examined how our Best Model's (Model Z)

parameters changed when we applied variations in Feedback Gain as shown in Table 3. Recall

that in the 1.35 Feedback Gain condition, the dot moves more than the person's hand position;

therefore, we expect the subject to move slightly less than they do in the veridical feedback

condition because they do not need to move as much to get the same visual output (i.e., we

expect k to decrease). Similarly, we expect the subject to attempt to replicate a greater portion of

the signal because it is easier to do so. Thus, we expect the Visual Gain (the amount of the input

signal that the subject is trying to reproduce) to increase with respect to the veridical condition.

Recall that the Visual Gain affects the *input* to the visual error computation. We expect the

opposite trend for the 0.65 Feedback Gain condition, as is detailed in Table 3. Given that we

believe the delays are biologically limited based on transmission time of visual information, we

expect the delay magnitudes to stay the same between Feedback Gain conditions. Indeed, the

model parameters change in the hypothesized manner when different Feedback Gains were

applied. The results from fitting the Best Model to the data from each of the different Feedback

Gains yields the parameter values shown in Table 4. The visual feedback delays are nearly

identical between Feedback Gain conditions, and the k and Visual Gain values increase and

decrease as hypothesized in Table 3. The one difference between the hypothesis and these model

values is in the lack of a feedback delay for the control subjects. This discrepancy is addressed in

the Discussion section.

Lastly, we used bootstrapping to generate confidence intervals for the parameter values in

our Best Model. Making one change to the fitting procedure described earlier, after the leave-

one-out step, we randomly sampled ten times with replacement from the remaining ten subjects.

This was repeated 1000 times to generate 1000 sets of parameter values. From these values, we

found the 95% confidence intervals for our best model to be: 2.4-2.7 for $k_{patient}$ and $k_{control}$; 0.38 -

0.41 for Visual Gain$_{patient}$ and Visual Gain$_{control}$; and 0.16-0.18 for Visual Delay$_{patient}$, Visual

Delay$_{control}$, and Feedback Delay$_{patient}$.

Experiment 2: Poor Tracking of Simple Oscillatory Trajectories Highlights Cerebellar Patients' Predictive Deficit

We validated the sinusoidal tracking paradigm by quantifying a known behavioral deficit in cerebellar visuomotor control. In this predictable task, we expected healthy participants would be efficient, exerting less than or equal to the amount of effort required to minimize error for a given phase lag. Where subjects lie relative to this tradeoff can be visualized on a phasor plot; efficient tracking would yield points on or inside the effort/error tradeoff circle (Figure 2B, Methods). We hypothesized that patients with impaired prediction may in some cases exert more effort than needed to minimize error, resulting in phasor points outside the effort/error tradeoff circle. We also hypothesized that patients would generate larger tracking errors.

At the five lowest frequencies tested, all of the control responses landed in/on the circle, whereas only 31% of patient responses landed in/on the circle (Figure 5). Additionally, patients generated larger tracking errors: 70% of patient responses exhibited larger error magnitude than the respective age-matched control responses. Furthermore, we created an aggregate tracking error for the single-sines experiment by calculating the sum of the tracking errors for the lowest five frequencies. We compared the aggregate tracking error between patients and age-matched controls by calculating the difference for each pair and testing those differences against 0 using a two-sided sign test. The null hypothesis for a two-sided sign test is that there was no difference between patients and their age-matched controls. The alternative hypothesis is that the controls may be either better or worse than patients. When we compared the difference between the aggregate tracking errors for each patient/control pair to 0, controls were significantly better than patients at single-sines tracking with 10 out of 11 controls performing better than their age-

matched counterpart (p=0.012). These results illustrate cerebellar patients' poor predictive

ability. Importantly, note that this analysis does not distinguish what portion of their errors

stemmed from poor prediction of the stimulus trajectory versus poor control of the arm.

For comparison, we also included the results from the task where the stimulus was

unpredictable (sum-of-sines from Experiment 1) in Figure 5. For this experiment, we expected

that patients would be less impaired relative to controls because neither group would be able to

predict the target trajectory. Indeed, patient and control behaviors were more similar in this

condition: for the five lowest frequencies tested in the sum-of-sines condition, 72% of control

responses and 64% of patient responses were in/on the circle. Note, however, that there is an

increased phase lag of the cerebellar patients (relative to controls), particularly as the frequency

of the stimulus increases, which would be expected if the patients were dependent primarily on

time-delayed visual feedback (feedback delay introduces greater phase lag at higher frequencies).

Specifically, 73% of individual patient frequency responses were more phase lagged than the

responses of the age-matched control (as computed on an individual frequency basis).

As expected, we also observed a reduction in tracking error from the sum-of-sines task to

the single-sines task. We calculated the magnitude of the tracking error for each subject for each

frequency (i.e., for the frequencies that were tested in both conditions) and then compared the

errors between the conditions. 93% of controls' and only 75% of patients' tracking errors were

reduced in the single-sine task in comparison to his or her performance in the sum-of-sines task.

Again, we computed the aggregate tracking error for the sum-of-sines task, as described earlier,

using the same five frequencies used in the single-sines aggregate tracking error calculation. We

then used a two-sided sign test to determine that patients ($p=9x10^{-4}$) and controls ($p=9x10^{-4}$)

were better at tracking single-sines than sum-of-sines, with all patients and all controls having

less tracking error for single-sines than sum-of-sines.

To specifically look at phase lag between groups (cerebellar vs. controls) and conditions

(single- vs. sum-of-sines), we used a circular statistical approach. Figure 6 shows polar

representations of the phase lags from the single-sine and sum-of-sines conditions (Figures 6A,

C) and an example time series from a control and cerebellar subject tracking the 0.85 Hz sine

wave (Figures 6B, D). The example control subject showed little phase lag suggesting that this

individual could make use of an internal prediction of the dot movement and their arm

movement. In contrast, the example cerebellar subject showed a systematic phase lag suggesting

that their ability to use prediction is impaired. The pattern of lag can be visualized across

frequencies in the polar plots. As a group, controls show a small increase in lag as the frequency

increases in the single-sine condition, whereas the cerebellar group shows large lags (Figures 6A

and C, compare purple vectors). Circular ANOVA for the single-sine condition showed that the

cerebellar group had greater lags compared to controls (Group effect, $p=1x10^{-8}$), that the lags

increased with frequency (Frequency effect, $p=7x10^{-11}$) and an interaction such that the

cerebellar group lags increased more than controls across frequency (Interaction effect, $p=2x10^{-6}$

). In the sum-of-sines condition, the difference in lags across frequency was qualitatively greater

when comparing cerebellar and control groups (Figures 6A and C, compare black vectors).

Overall the cerebellar group showed greater phase lags compared to controls (Group effect,

p=0.02), and there was a statistically significant effect of Frequency (Frequency effect, $p=7x10^{-30}$

). Group x Frequency interaction (Interaction effect, p=0.03), was weaker than that seen in the

single-sine condition.

Experiment 3: Virtual Reality Feedback Visual Feedback Reduces Dysmetria

The results from Experiment 1 indicated that cerebellar patients' feedback control may be

intact. In Experiment 3, we leveraged this intact element of their control system to reduce

dysmetria. Our goal was to provide each cerebellar patient with customized visual position

feedback information that took into account their controller's mismatched feedforward model.

This altered visual feedback would help them generate the correct motor command for a simple

elbow movement (30 degrees flexion) by accounting for their actual arm dynamics.

Here we used a motor task that requires subjects make a discrete movement to a target

that is stepped to a new position. This was chosen so that we could compare our data to

previously published results using the same task with cerebellar patients. Subjects were asked to

make a 30 degree elbow flexion movement from a home target to a stepped target. The task was

completed with both veridical visual feedback and with altered visual feedback that was

designed to reduce their dysmetria.

Bhanpuri et al. theorized that cerebellar patients have a static mismatch between their

controller's internal model of their limb inertia and the actual limb inertia for elbow flexion

movements (Nasir H. Bhanpuri, Okamura, and Bastian 2014). Critically, for single-joint elbow

flexion or extension, an inertial mismatch causes an acceleration-dependent error in the internal

dynamic model because inertia and acceleration are kinematically yoked. Thus, we predicted that

an Acceleration-Dependent Feedback Gain (block diagram inset in Figure 7A) could provide

corrective feedback to enhance reaching performance of cerebellar patients. Specifically, we

took a subject's estimated acceleration (see Methods), multiplied this by the Feedback Gain, and

then added it to the position of the subject's cursor. We predicted that positive Acceleration-

Dependent Feedback Gains would make a subject more hypermetric and negative Acceleration-

Dependent Feedback Gains would make a subject more hypometric. Thus, we expected

hypometric patients would experience a reduction in dysmetria with a positive Acceleration-

Dependent Feedback Gain. Similarly, we expected hypermetric patients would experience a

reduction in dysmetria when a negative Acceleration-Dependent Feedback Gain was applied.

Subjects completed 30 degree elbow flexion reaching movements in the Kinarm

exoskeleton robot. Reaches were categorized as hypometric, hypermetric, or on-target based on

the angle where they made their first correction to their movement. Acceleration-Dependent

Feedback Gains were applied to the visual feedback provided on the Kinarm screen. For more

details on the implementation and instructions of this task, see Methods.

When an appropriate Acceleration-Dependent Feedback Gain was applied, dysmetria was

reduced. The effect of this Acceleration-Dependent Feedback Gain on the displayed trajectory is

shown in Figure 7A, where the dashed green line shows the altered visual feedback given to the

subject and the solid green line shows the subject's actual reach to the target for a single

Feedback Gain condition. Increasing the Acceleration-Dependent Feedback Gain magnitude had

a graded effect on the trajectory profile, as shown by the decreasing amplitude of the solid traces

in Figure 7A. Applying this Acceleration-Dependent Feedback Gain shifted the angle of first

correction in the way we predicted, as shown in both Figure 7B and C (control subjects also

respond similarly, Figure 8). Namely, positive Acceleration-Dependent Feedback Gain made

patients more hypermetric and negative Acceleration-Dependent Feedback Gain made patients

more hypometric. Thus, subject-specific Acceleration-Dependent Feedback Gain was needed to

best reduce dysmetria. In general, increased Acceleration-Dependent Feedback Gain magnitude

was needed to ameliorate greater dysmetria.

DISCUSSION
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We found that cerebellar patients can use visual feedback control in a manner similar to

control subjects. This was assessed during a sum-of-sines visuomotor tracking task by subtly

changing the gain of the visual cursor feedback (i.e. hand) and measuring the degree to which an

individual subject could modulate the gain of his or her corrective movements. Our modeling

corroborated this finding: the structure and parameters differed between patients and controls

only in the feedback delay term. The patients relied on time delayed cursor feedback of their

hand position, whereas controls appeared to be able to generate predictions of their hand

position.

We also saw increases in phase lag for patients versus controls when following

predictable sine waves. While patients showed large phase lags that increased with frequency in

both conditions, controls only showed large phase lags in the sum-of-sines condition when the

stimulus was unpredictable. We interpret this to mean that the control subjects could predict the

movement of the hand *and stimulus* in the single-sine condition, but the cerebellar patients could

not.

The above results are significant as it has previously been difficult to assess visual

feedback control in these patients due to their clear impairments in feedforward control of

movement. In Experiment 3, we tested whether patients' intact visual feedback could be

exploited to benefit their targeting performance in a reaching task. Indeed, we found that

cerebellar patients could leverage their intact, albeit delayed, feedback control ability to improve

their movement when we manipulate their visual feedback to assist them.

Delay in Patients but not in Healthy Controls

Cerebellar patients are thought to make faulty state estimates of arm motion due to a

damaged internal model, which adversely affects their proprioceptive estimates during active

movement (N. H. Bhanpuri, Okamura, and Bastian 2013). Thus, we expect them to increase their

reliance on visual feedback, which is time delayed compared to proprioceptive feedback. Here

we hypothesized that our patients' feedback control system would have an increased delay in

comparison to controls. This hypothesis is supported by work that showed that healthy subjects

normally rely more on proprioception than vision for feedback control (Crevecoeur, Munoz, and

Scott 2016). Based on the Crevecoeur et al. (2016) model, increased variability of the

proprioceptive information would lead to increased weighting of visual feedback (Crevecoeur,

Munoz, and Scott 2016; Weeks, Therrien, and Bastian 2017).

Our modeling results reveal that patients have a delay in their feedback loop that

approximates what one would expect from visual feedback, while controls appear to have little-

to-no feedback delay. One interpretation of the control data is that they are relying on a

predictive internal model of their arm dynamics. This would allow them to make corrections

even faster than they could using purely proprioceptive feedback. In other words, healthy

controls can make corrections for current target movements based on a prediction of the present

limb state from outdated measurements and known motor commands, rather than waiting on

delayed sensory feedback.

We think that the cerebellar patients' deficits are best explained by their dependence on

time-delayed visual feedback, though it is theoretically possible that delays in motor execution

could contribute. Previous studies have shown that some patients with cerebellar damage exhibit

longer than usual reaction time delays when asked to make discrete, rapid movements (Vilis and

Hore 1980; Holmes 1917; Beppu, Suda, and Tanaka 1984; Beppu, Nagaoka, and Tanaka 1987;

Day et al. 1998). These reaction time studies aimed to quantify a movement initiation delay as

opposed to a feedback delay. Here, we specifically assessed the timing of the in-flight trajectory

alterations made while tracking an unpredictable stimulus. While our feedback delay is a type of

"reaction time" because this task requires making corrections on the fly, the neural mechanisms

underlying these corrections may differ from those responsible for planning and initiation of a

rapid movement.

Lastly, while the confluence of data and modeling presented here seems to indicate that

patients rely disproportionately on delayed feedback from vision for this tracking task, we cannot

rule out the possibility that the control signal may nevertheless include some reliance, albeit

weaker, on prediction and proprioception that is not captured by our simplified model.

Modeling Results Support the Cerebellum as a Smith Predictor

Sensorimotor tasks are naturally analyzed using control systems theory and system

identification (Roth, Sponberg, and Cowan 2014), and because cerebellar patients' dysmetria

resembles a poorly tuned control system, many researchers have analyzed cerebellar behavior

using control theory (Luque et al. 2011; Mario Manto 2009; R C Miall et al. 1993; Porrill, Dean,

and Anderson 2013).

Our modeling results indicate that control subjects make corrections based on prediction

of a future limb state measurement. While there is some controversy on this (Pelisson et al. 1986;

Wolpert, Miall, and Kawato 1998), previous work has proposed that the cerebellum might

function in a manner consistent with a Smith Predictor (R C Miall et al. 1993). Essentially, a

Smith Predictor is a control architecture that compensates for self-movement feedback delay. To

achieve this requires a simulation of the plant in order to predict sensory consequences of motor

output, and a simulated delay that "stores" the plant simulation for comparison with delayed

feedback. In order to understand the consequences of incorporating a Smith Predictor, consider

the generic feedback block diagram of sensorimotor control depicted in Figure 9 (top) and model

the brain as either a controller *with* (Figure 9, left) or *without* (Figure 9, right) a Smith Predictor.

Surprisingly, upon simplification, we find the exact structures yielded by our modeling results:

the patient model matches the simplified block diagram without a Smith Predictor and the age-

matched control model matches the simplified block diagram which one. This suggests that an

intact cerebellum may be approximated as a Smith Predictor.

Perhaps the increased feedback delay in the cerebellar patients is unavoidable if one

assumes the patients' control systems lack the essential capabilities of a Smith Predictor (making

and storing predictive plant simulations). Thus, the apparent increased reliance on visual

feedback seen in cerebellar patients may not be a compensatory mechanism at all—perhaps all

subjects rely on delayed visual feedback, but healthy subjects disguise the delay using

predictions of future measurements of limb state. Patients may simply lack this capability and it

is not that they *compensate* for their deficit by relying *more* on visual feedback but instead that

the loss of the sensory prediction and storage reveals the visual feedback delay inescapably

present in both groups. This would provide some clarity on how cerebellar patients could "learn"

to "compensate" in this way even when their cerebellum was damaged.

At its core, the Smith Predictor has to do with simulating the mechanical plant (and

appropriate delay) in order to mitigate the effect of *feedback* delay. But notice that in our model

there is a large visuomotor delay on the reference input even with the Smith Predictor in place. In

order to compensate for the delayed visual measurement of the stimulus, the brain would need to

be able to predict reference motions. To avoid this confound of stimulus prediction, and focus on

feedback delay compensation, we fit our models using responses to unpredictable (sum-of-sine)

target motions.

But, what if the target motion were predictable? Previously, it was shown in another

species (weakly electric fish) that target predictability can indeed improve tracking performance,

and it was hypothesized that this was based on an internal model of predictable reference motion

(Roth et al. 2011). Here, we extend this to healthy human subjects who show marked

improvement in the single-sine (predictable) tracking task. Cerebellar patients exhibit much more

modest improvement in tracking predictable stimuli, suggesting that they may have impairment

in both their own plant model predictions and predictions of external sensory references (see

Results, Experiment 2). Further data and experiments would be needed to better isolate the

effects of cerebellar damage on these potentially disparate functions of the cerebellum.

Lastly, even if a healthy cerebellum helps "cancel" expected cursor feedback, this does

not imply that visual cursor feedback goes unused: any errors in visual feedback, i.e., cursor self-

motion feedback that is not precisely anticipated by the cerebellum, could be highly informative,

and recent evidence (Yon et al. 2018) suggests that a predictive model of action–perception

could heighten perceptual sensitivity, making self-motion (in this case, cursor) feedback more

nuanced and precise.

Potential for Real-World Application

In Experiment 3, we were successfully able to reduce the dysmetria of both the

hypermetric and hypometric cerebellar patients in an elbow flexion task. Our visual feedback-

control-based intervention was developed based on a control model which represented dysmetria

as a mismatch between the patient's internal model of their limb inertia and the actual limb

inertia (Nasir H. Bhanpuri, Okamura, and Bastian 2014). Thus, the success of our intervention

provides support to this inertial mismatch theory. However, recent evidence based on the

application of limb weights suggest that the inertial mismatch theory may be insufficient to

explain dysmetria in multi-joint movements (Zimmet, Cowan, and Bastian 2018). Thus,

feedback enhancement of multi-joint movements will likely require modifications of the simple

acceleration-based controller tested in this paper.

Though our intervention successfully reduces the initial over or undershooting

component of the reach, our method does not attempt to correct all aspects of dysmetria. Patients

with cerebellar ataxia also typically exhibit increased movement variability. Application of this

visual feedback gain does not attempt to reduce the variability of patient reaches. Secondly, our

intervention does not completely eliminate the oscillations experienced by the subject after this

first correction is made. Moreover, our modeling work does not characterize or explain this

increased variability directly. Mild oscillations after the first correction can be seen in Figure 7A.

It is possible that adding a damping term to the feedback intervention might be able to address

this oscillatory behavior.

Our results provide an encouraging foundation for future studies because they show that

cerebellar patients are capable of using their own intact visual feedback control system to make

accurate reaches. Further study is needed to determine whether this intact feedback control

system could be leveraged therapeutically to reduce dysmetria without need for a virtual reality

system. Alternatively, it is possible that wearable sensory augmentation (for example, tendon

vibration or skin stretch) could be used as a surrogate for the vision-based sensory shift provided

here. These alternatives are especially important because drug therapy for cerebellar ataxia is not

currently viable, leaving rehabilitative and assistive therapies alone as the primary means of

treatment for these patients. In any case, we hope that by identifying these intact movement

control mechanisms we might help move treatment possibilities forward.

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We have no competing financial interests to disclose.

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CODE/DATA REPOSITORY

The dataset and code used in this paper will be uploaded to Dataverse and made publicly available.

FIGURES

Figure 1 – Experimental Setup

Figure 1 *The experimental paradigm*. **A** The Kinarm Exoskeleton robot system (BKIN Technologies Ltd.) where all tasks are executed. Image is taken from (Mostafavi et al. 2015). **B** This block diagram shows our experimental paradigm for experiment 1. The actual elbow angle (orange in C) is multiplied by a feedback gain to compute the shown elbow angle (white dot in C). **C** A schematic view of the Kinarm screen in the 0.65 Feedback Gain condition. The subject's shoulder is locked at a 75° angle. The green dot is the target dot. The green dot oscillates according to the sum-of-sines pattern along an arc with a radius equivalent to the forearm + hand + finger length. The sum-of-sines pattern is centered about the 0° angle. This 0° centerline is at a 65° angle from the subject's straight arm position. The subject could not see their fingertip (orange dot) or arm position. The angle of the white dot (visible to the subject) is equal to 0.65 times the actual fingertip angle in orange (0.65 · 30° = 19.5°). **D** Sample data (20 s) for a single cerebellar patient showing the angles traversed by the target dot during the sum-of-sines task (green) and by the fingertip (orange, averaged over 5 trials). **E** The normalized Fourier spectrum of the input sum-of-sines signal (green trace in D). **F** The spectrum of the response by a single cerebellar patient over five trials (orange trace in D).

905 Figure 2 – Interpreting Phasor Plots

906
Figure 2 *Interpreting Phasor Plots*. **A-C** Brief explanation of phasor plots, which are explained in depth in Methods in "Phasor
Plot." **A** Illustration of the relationship between the real and imaginary components of the complex numbers and the gain and
phase lag. **B** The bold black circle illustrates the gains that minimize error given a particular phase lag (veridical feedback
condition only). **C** Points on the bold black circle illustrate a different control strategy than what was asked of our subjects.
Points on this circle replicate the input signal without minimizing error between the input and output signals (veridical feedback
condition only) due to the phase lag.

Figure 3 – Motion Rescaling under Different Feedback Gains

Figure 3 *Motion Rescaling under Different Feedback Gains*. **A** Sample phasor plot data from a single cerebellar patient under all
three feedback gain conditions. The dots represent the frequency response at the lowest five frequencies. The solid line traces
through the responses at all tested frequencies. The dimmed lines show the frequency responses at the other frequencies
tested beyond the five lowest frequencies. **B** Scaled phasor plot data from the same single cerebellar patient. The gain value
from D has been multiplied by the scaling factor shown in the legend here to create an overlaid phasor plot. The higher the
Scaling Factor, the less effort (in terms of movement magnitude) the subject expended in that condition. Outliers are marked
with an x. The outlier subject with the highest Scaling Factor in the 0.65 condition was from the same subject who had the
lowest Scaling Factor in the 1.35 condition. **C** Patients and controls respond similarly to the applied Feedback Gain, indicating
that they incorporate visual feedback similarly. The higher the Scaling Factor, the less effort (in terms of movement magnitude)
the subject expended in that condition. Outliers are marked with an x.

925 ## Figure 4 – Modeling

Figure 4 *Modeling*. **A** Our modeling framework was based on the McRuer Crossover model (McRuer and Krendel 1974). This
simple model structure lumps the controller and plant as a scaled integrator, and assigns different delays to the measurement
of the target from that of self-movement feedback. We hypothesized that the patient and control models would be equivalent
except for the magnitude of the feedback delay. The Visual Gain is necessary because, given the complexity and speed of the
signal, participants were unable to match the full magnitude of the signal. **B** After our model selection procedure, the Best
Model structure was determined to be very similar to our hypothetical model, but with one small difference: the feedback
delay for the controls was determined to be zero instead of equivalent to the proprioceptive delay. **C** Time domain visualization
of subject and model responses for a typical 15 second time window of our experiments. The same visual target trajectory
(green) was played to all patients and controls, and was used in simulation. Individual time-domain elbow-angle responses
(light gray) are shown for the 11 control subjects (top plot) and 11 patients (bottom plot). The average subject responses
(orange, solid) match with reasonable accuracy the simulated model responses (orange, dashed).

Figure 4 Supplemental 1 – Model Fitting and Model Selection

Figure 4S1 *Model Fitting and Model Selection*. We used sum-of-sine data to fit the parameters of a modified McRuer Crossover
model (McRuer and Krendel 1974). **A** In the most flexible setting, there are a total of eight free parameters, allowing for
patients and controls to have completely independent model parameters. **B** In the model fitting and model selection process,
we tested many variations of this model structure. For example, some model structures yoke parameters together or eliminate
parameters, and some yoke variables together across patient and control models. This color table specifies all 60 model
configurations tested. Each row describes an individual model configuration. Variables with the same color within that row are
yoked together for that model configuration. White indicates that the specified variable was removed from the model. The
total number of free parameters is shown in the left column. X, Y, and Z in the rightmost column refer to the corresponding top
3 models described in (D). **C** Results of model selection procedure. (Some of the 60 models had model inconsistency values that
were orders of magnitude greater than what is shown here, indicating over-parameterization; this figure is truncated to only
show the most relevant models). The best four models, highlighted in the red circle, provide the best trade-off between
minimizing model inconsistency (i.e., minimizing parameter variability and over-fitting) and minimizing error (improving model
fit). The best four models are labeled W, X, Y, and Z. These top four models had nearly equivalent performance according to the
model selection criteria. **D** Model W shares the same parameters between patients and controls, except for delay, for which
there is a single group-specific parameter for both the feedforward and feedback delay. Model X allows for freedom between

the patient and control models in the visual gain terms. No feedback delay is present in the control subject model. Model Y is
our hypothesized model. The cerebellar patient feedback delay is yoked to the visual feedback delay, while the control
feedback delay is a free, non-zero parameter. Model Z requires only 3 free parameters and was therefore determined to be our
Best Model. No feedback delay is present in the control subject model here as well. The best fit parameter values are shown for
this Best Model, Model Z.

Figure 4 Supplemental 2 – Time Domain Validation

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963 Figure 4S2 *Time Domain Validation*. As in Figure 4S1C, we plotted error versus model inconsistency, but here we used the time-
964 domain error (see Methods). Critically, the time-domain data were not used directly for model fitting, and yet the four top
965 models in the frequency domain are also the four top models in the time domain, validating that our frequency-domain model
966 selection process selected the models that were best in the best time-domain.
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968   Figure 5 –Single-Sine and Sum-of-Sines Phasor Plots

969
970   Figure 5 *Patients and controls have categorically different responses to single-sine and sum-of-sine stimuli*. Each data point is
971   the response at a single frequency (magnitude and phase) of a single subject. The patient data in both the single and sum-of-
972   sines conditions are more variable than that of the control subjects. In the single-sines condition, control subjects are able to
973   consistently remain inside the effort/error circle at low frequencies, balancing the tradeoff between effort and error, while
974   patients are not. This result is consistent with previous studies that show patients have impaired prediction.

Figure 6 – Comparison of Phase Lags

Figure 6 *Phase lags show different patterns between groups.* Polar plot representations showing phase lag for the 5 lowest
frequencies common to the single-sine and sum-of-sines conditions. **A.** Control group phase lags. Individual subjects are
represented as lighter colored unit vectors and the group mean vector is plotted in bold. Purple indicates the single-sine
condition and black represents the sum-of-sines condition. Note that only phase lag is represented on the polar plot (gain is not
represented). The Control group is able to track the single-sine stimuli with little or no phase lag, but shows phase lags that
increase with frequency in the sum-of-sines condition. **B.** Example response from a control subject tracking a 0.85 Hz single-sine
stimuli. The target sine wave is represented in green and the subject performance in orange. Note that this control could
predict the single-sine and track it with little or no phase lag. **C.** Cerebellar group phase lags plotted as in A. The Cerebellar
patients were able to track the two slowest single-sine stimuli with little phase lag (purple, 0.10 and 0.25 Hz) but then shows
increasing phase lags as a function of frequency. Note that 0.10 and 0.25 Hz are extremely slow frequencies that could be
followed using only visual feedback control. In the sum-of-sines condition, the cerebellar group shows phase lags that increase
with frequency. **D.** Example response from a cerebellar subject tracking a 0.85 Hz single-sine stimuli. In contrast to the control
subject, this cerebellar patient shows phase lags relative to the target.

Figure 7 – Acceleration-Dependent Feedback Reduces Dysmetria

Figure 7 *Acceleration-dependent feedback reduces dysmetria*. **A** The trajectories from a single cerebellar patient for different
Acceleration-Dependent Feedback Gain conditions. The solid lines are average trajectories (across trials for a single subject) at a
given Acceleration-Dependent Feedback Gain value. A decrease in the angle of first correction is apparent as the Acceleration-
Dependent Feedback Gain decreases. The best Acceleration-Dependent Feedback Gain for this subject was determined to be -
0.0025, and the resulting movement trajectory is shown as a solid green line. The dashed green line illustrates the trajectory
that is displayed to the subject on the screen for the -0.0025 condition. This example also shows that oscillation around the
target remains with Acceleration-Dependent Feedback Gain. The block diagram in the lower right shows how the Acceleration-
Dependent Feedback Gain was applied to the visual representation of the fingertip position. **B** The reduction in dysmetria
exhibited by patients when the best Acceleration-Dependent Feedback Gain was applied. Each line represents a single
cerebellar patient. Lines are color coded to indicate the best Acceleration-Dependent Feedback Gain for that subject. **C**
Increasing Acceleration-Dependent Feedback Gain causes increased hypermetria. Again, each line represents a single cerebellar
patient. At the highest gain values, the visual feedback diverged enough from the fingertip position so that some subjects
paused mid-reach, presumably due to the conflicting visual feedback. This yielded the observed drop in median angle of first
correction seen in some subjects in the higher gain conditions. This figure shows only the cerebellar patients. Control subject
data is shown in Figure 8.

Figure 8 – Acceleration-Dependent Feedback: Control Subjects

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1012   Figure 8 *Acceleration-dependent feedback also affects single reaches in control subjects.* Control subjects' median angle of first
1013   correction when completing thirty-degree flexion movements. The expected upward trend in median angle of first correction is
1014   visible across subjects. At the largest Acceleration-Dependent Feedback Gains, there is a slight drop off in median angle of first
1015   correction. At high gain values, the discrepancy between the cursor and the fingertip became more apparent, causing some
1016   subjects to pause mid-reach, resulting in a lower median angle of first correction for these high gain conditions.

 Figure 9– Smith Predictor

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Figure 9 *Our modeling results agree with the theory of the cerebellum as a Smith Predictor*. A basic model for the control system is shown in the top panel. In our experiment, the plant, P, represents the entire mechanical arm system, including the robot exoskeleton arm. A single visual delay block delays the input from both the reference signal and the feedback information. A visual gain scales the amount of the input the subject will attempt to replicate. The brain, illustrated by a dashed box, can be modeled as containing just a controller, C, as shown on the right side. Or, the brain can be modeled as a controller with an accompanying Smith Predictor, as shown on the left side. When these two alternate structures are simplified, we are left with the exact model structures yielded by our previous modeling results.

Subject No.	Patient Age	Sex	Pathology	ICARS	Upper Limb ICARS	Experiments
P1	44	M	SCA8	62	17	1,2,3
P2	52	M	ADCAIII	28	8	3
P3	53	M	Sporadic	59	19	1,2,3
P4	55	F	SCA8	41	17	3
P5	55	M	OPCA	46	14	1,2
P6	60	M	MSA-C	63	14	1,2,3
P7	62	F	Sporadic	36	16	1,2
P8	62	M	SCA6/8	62	19	1,2,3
P9	63	M	SCA6	41	10	3
P10	64	F	SCA6	58	13	1,2
P11	64	M	ADCAIII	11	3	1,2,3
P12	65	M	Idiopathic	34	10	3
P13	66	F	SCA6	41	11	1,2
P14	67	F	Left Cerebellar Stroke	27	10	1,2,3
P15	69	F	ADCAIII	52	13	3
P16	72	F	SCA6	49	18	3
P17	78	M	Sporadic (Vermis Degen.)	39	6	1,2

1027 Table 1 The cerebellar patient population that was tested. Not all subjects completed all experiments. Some subjects completed
1028 the experiments over two visits. Upper Limb ICARS contains the sum of the upper-limb kinetic function elements of the test
1029 (ICARS subsections 10-14, out of 20).

Model	$k_{patient}$	$k_{control}$	Visual Gain$_{Patients}$	Visual Gain$_{Controls}$	Visual Delay$_{Patients}$ (s)	Visual Delay$_{Controls}$ (s)	Feedback Delay$_{Patients}$ (s)	Feedback Delay$_{Controls}$ (s)
W	2.4	2.4	0.38	0.38	0.18	0.11	0.18	0.11
X	2.6	2.6	0.38	0.41	0.17	0.17	0.17	0
Y	2.5	2.5	0.39	0.39	0.17	0.17	0.17	0.030
Z	2.5	2.5	0.40	0.40	0.17	0.17	0.17	0

1030 Table 2 Model parameters for the four best fit models. Models X, Y, and Z are quantitatively similar; for these models, the
1031 McRuer gain (k), visual gain, and visual delay deviated by no more than 5% between patients and controls across all three
1032 models, while the feedback gain was consistently equal to the visual delay for the patients, and small (≤30ms) for controls.
1033 Model W differs somewhat in model structure and parameters, but also exhibits a smaller feedback delay for controls than
1034 patients.

Feedback Gain	k	Visual Gain	Visual Delay (s)	Feedback Delay$_{Patients}$ (s)	Feedback Delay$_{Controls}$ (s)
1.0		<1	Visual Delay	Visual Delay	Proprioceptive Delay
1.35	Decrease	Increase	Unchanged	Unchanged	Unchanged
0.65	Increase	Decrease	Unchanged	Unchanged	Unchanged

Table 3 This is our hypothesis of how we expect the model parameter values indicated in the bottom two rows (1.35 and 0.65
Feedback Gain) will change (with respect to the value obtained in the veridical Feedback Gain condition, Feedback Gain=1.0)
with changing Feedback Gains. We expect Visual Delay of approximately 140 to 250 ms, and Proprioceptive Delay
approximately 110 to 150 ms (Cameron, de la Malla, and López-Moliner 2014). We also expect Visual Gain to be less than one
in the veridical feedback condition because we do not expect the subjects to attempt to replicate the full magnitude of the
signal, given that it is a challenging, fast, and unpredictable task.

1041

Feedback Gain	$k_{patient}$	$k_{control}$	Visual Gain$_{Patients}$	Visual Gain$_{Controls}$	Visual Delay$_{Patients}$ (s)	Visual Delay$_{Controls}$ (s)	Feedback Delay$_{Patients}$ (s)	Feedback Delay$_{Controls}$ (s)
1	2.5	2.5	0.40	0.40	0.17	0.17	0.17	0
1.35	2.0	2.0	0.45	0.45	0.17	0.17	0.17	0
0.65	3.3	3.3	0.33	0.33	0.17	0.17	0.17	0

1042   Table 4 The model parameters changed with different applied Feedback Gains in a manner consistent with our prediction.

AUTHOR CONTRIBUTIONS

All three of the authors conceived of the experiments, contributed to the analysis, and participated in the writing. Amanda Zimmet conducted the experiments and collected data.