Assessing the Operational Feasibility of Evolutionary Therapy in Metastatic Non-Small Cell Lung Cancer

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Abstract

Evolutionary cancer therapy (ECT) applies principles of evolutionary game theory to prolong the effectiveness of cancer treatment by curbing the development of treatment resistance. It was shown to increase time to progression while decreasing the cumulative drug dose. ECT individually tailors treatment schedules for patients based on their cancer dynamics and, thus, requires regular follow-up and precise measurements of the cancer burden. The current literature on ECT often overlooks clinical realities, such as rather long intervals between tests, possible appointment delays and measurement errors, in the development of the treatment protocols. In this study, we assess the clinical feasibility of ECT for metastatic non-small cell lung cancer (NSCLC). We create virtual patients with cancer dynamics described by the polymorphic Gompertzian model, based on data from the START-TKI clinical trial. We assess the effects of longer test intervals, measurement error and appointment delays on the expected time to progression under the evolutionary therapy protocols. We show that a higher containment level, although it increases time to progression in the model's predictions, may lead to premature treatment failure in the presence of measurement error and appointment delay. Further, we show that the ECT protocol with a single containment bound is more robust to the clinical realities than the protocol with two bounds. Finally, we show that a dynamically adjusted treatment protocol can be beneficial for individual patients, but requires a thorough follow-up. This study contributes to the design of a clinical trial and the future clinical implementation of evolutionary therapy for NSCLC.

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1 Introduction

Evolutionary cancer therapy (ECT), also known as adaptive therapy, applies principles of evolutionary game theory to optimize treatment in metastatic cancer (Gatenby, 2009; Gatenby et al., 2009b; Stanková et al., 2019; West et al., 2020; Wölfl et al., 2021; West et al., 2023). It presents an alternative to the current standard of care in metastatic cancer, which aims at complete eradication of cancer applying maximum tolerable dose (MTD), either continuously or in repeated pre-defined treatment cycles. In metastatic cancer, eradication is rare, and the MTD approach typically promotes rapid development of treatment resistance, causing therapy failure and subsequent progression (Gatenby et al., 2009b; Gatenby, 2009; Dujon et al., 2021; Staňková, 2019; West et al., 2023). ECT typically delays or forestalls the development of treatment-induced resistance by exploiting competition between different types of cancer cells - those sensitive and resistant to treatment - in the treatment design (Gatenby et al., 2009b; Staňková, 2019; West et al., 2023). ECT is typically guided by evolutionary game-theoretic models of tumor growth calibrated with patient data (Zhang et al., 2022; Strobl et al., 2023; West et al., 2023; Jansén-Storbacka et al., 2026; Beckman et al., 2020). Single-treatment evolutionary therapies typically involve lower doses of treatment than MTD and/or periods without treatment. Because the cumulative dose of ECT is lower than that of MTD, ECT usually has lower toxicity and a higher patient quality of life than standard of care (Zhang et al., 2017, 2022; Cunningham et al., 2018).

The first ECT clinical trial, a small Zhang et al.'s trial in metastatic castrate-resistant prostate cancer (mCRPC), was initiated in 2015 (Zhang et al., 2017, 2022). The patients were treated with MTD of the drug Abiraterone until the tumor burden measured through prostate-specific antigen (PSA), a biomarker used as a proxy for overall tumor burden, decreased to 50% of its initial level. At that point, the treatment was paused to allow the tumor burden to regrow. When the initial level of PSA was reached again, the treatment was resumed and a new treatment cycle began (Zhang et al., 2017). As a result of the clinical trial, time to progression (TTP) increased to 33.5 months compared to 14.3 months in the standard of care group, while the cumulative drug dose was decreased by half (Zhang et al., 2022). The success of this initial trial led to a growing interest in evolutionary cancer therapy with multiple studies published on theoretical analysis of (potential) mathematical models that could guide ECT (Viossat & Noble, 2021; Alvarez & Viossat, 2024), validation of these models with real-world data (Kaznatcheev et al., 2019; Ghaffari Laleh et al., 2022; Soboleva et al., 2025b; Garjani et al., 2025), development of different ECT approaches, including dose stabilization (Hockings et al., 2023; Salvioli et al., 2024; Cunningham et al., 2020b), intermittent dosing (Yu et al., 2017; De Iuliis et al., 2016), extinction therapy (Gatenby et al., 2019), and the double-bind therapy (Gatenby et al., 2009a; Basanta et al., 2012). Moreover, evolutionary cancer therapy is being evaluated in an increasing number of clinical trials across cancers, including prostate (NCT05393791), ovarian (NCT05080556), melanoma (NCT03543969), and skin cancers such as basal cell carcinoma (NCT05651828).

Many studies have applied optimal control and related optimization techniques to evolutionary game theoretic (EGT) models, as well as to other mathematical models of eco-evolutionary cancer dynamics under treatment, to derive therapeutic protocols that delay resistance, prolong time to progression, and improve patient quality of life (Martin et al., 1992; Tomlinson, 1997; Carrère, 2017; Cunningham et al., 2018; Brady-Nicholls & Enderling, 2022; Wang & Lei, 2025; Gluzman et al., 2020; Stanková et al., 2019) These efforts are part of the broader and rapidly expanding field of mathematical oncology, in which optimization and evolutionary modeling are increasingly integrated into clinical decision-making (Scibilia et al., 2025; Pradelli et al., 2026; Soboleva et al., 2025a). Such approaches span a spectrum from purely theoretical analyses to optimization of models calibrated and validated against experimental and/or clinical data.

An alternative to Zhang et al.'s protocol is the containment strategy. Unlike the original approach, which maintains tumor burden within two predefined bounds, the containment protocol relies on a single threshold. Treatment is suspended once the tumor burden decreases below this threshold and resumed when it exceeds it again. The key challenge is, therefore, how this containment level should be optimally determined. It has been theoretically shown that a higher containment level can prolong time to progression (Viossat & Noble, 2021). However, this potential benefit comes with risk, as a higher tumor burden may increase the probability of new mutations, the likelihood of metastatic spread, and the severity of patient symptoms, thereby reducing quality of life (Joseph et al., 2018; He et al., 2025;

Lommen et al., 2026; Howard et al., 2011). To address this trade-off, Gallagher et al. derived the containment threshold using competition-based tumor growth models, requiring that under discrete monitoring intervals the tumor cannot grow from the containment level to the progression threshold between successive tumor measurements (Gallagher et al., 2025).

The applications of ECT for metastatic non-small cell lung cancer (NSCLC) are currently being evaluated (Jansén-Storbacka et al., 2026), based on fitting *in vitro* and *in vivo* data to mathematical models (Kaznatcheev et al., 2019; Ghaffari Laleh et al., 2022; Soboleva et al., 2025b; Garjani et al., 2025). The state-of-the-art treatment for metastatic NSCLC patients with known driver mutations is targeted therapy with tyrosine kinase inhibitors (TKIs). In EGFR-mutated NSCLC, third-generation TKIs such as osimertinib significantly improve progression-free and overall survival compared to earlier-generation inhibitors (Ramalingam et al., 2020). However, despite these advances, resistance inevitably emerges and tumor regrowth occurs. Clinical and molecular analyses of patients progressing on EGFR TKIs reveal substantial heterogeneity in resistance mechanisms, including secondary EGFR alterations, MET amplification, and alternative bypass pathways, reflecting the dynamic evolutionary nature of the disease (van der Wel et al., 2025; Steendam et al., 2020; Rolfo et al., 2021).

Prospective studies combining tumor tissue and circulating tumor DNA analyses further demonstrate that single-modality testing may miss clinically relevant resistance mechanisms, underscoring spatial and temporal heterogeneity during treatment (van der Wel et al., 2025). These findings support the view that resistance development in metastatic NSCLC is an evolutionary process occurring within a heterogeneous tumor ecosystem (Gatenby & Vincent, 2003), a perspective that has motivated both eco-evolutionary modeling and optimization-based approaches to adaptive therapy.

From a theoretical perspective, mathematical models of tumor growth and resistance evolution suggest that continuous maximum tolerated dose therapy may promote competitive release of resistant cell populations. In contrast, containment-based strategies aim to maintain a controlled tumor burden by preserving a population of treatment-sensitive cells that suppress the expansion of resistant phenotypes. Analytical and computational studies of competition-based tumor growth models demonstrate that containment protocols can prolong time to progression across a broad range of biologically plausible parameter regimes (Viossat & Noble, 2021; Alvarez & Viossat, 2024). Recent data-driven modeling of longitudinal NSCLC tumor burden, incorporating density-dependent growth and frequency-dependent interactions, further indicates that evolutionary therapy protocols may theoretically extend progression-free survival compared to continuous treatment (Jansén-Storbacka et al., 2026).

However, clinical implementation of ECT for metastatic NSCLC is challenging because it requires careful monitoring of disease progression (Soboleva et al., 2025a). Unlike prostate cancer, NSCLC does not have an easily measured serum biomarker, and the disease is usually monitored through imaging using computed tomography (CT), magnetic resonance imaging (MRI) and positron emission tomography (PET) scans (Molnárová et al., 2025). The lesions on the images are often difficult to measure, which leads to high variation of the estimated tumor volume and potential disagreements between measurements made by different radiologists (Oxnard et al., 2011b; Zhao et al., 2009).

Another challenge is the long interval between assessments. In current clinical practice, radiological response evaluation in metastatic NSCLC is typically performed every 6–12 weeks (Hendriks et al., 2023). In evolutionary therapy, where patients may have treatment vacations, such long intervals can be risky because clinically relevant regrowth may occur between scans. Moreover, in routine care, imaging and follow-up appointments may be delayed (e.g., due to scheduling constraints or patient-related factors), further increasing the effective interval between measurements (Iwsakul & Geater, 2025).

In this study, we evaluate the feasibility of the common evolutionary therapy protocols - Zhang et al.'s, containment and dynamic containment protocols - in clinically realistic conditions through simulations. Based on time-series volumetric patient data from the START-TKI trial (NCT05221372), we utilize frequency-dependent polymorphic Gompertzian model to simulate virtual patients corresponding to the patient cohort of metastatic NSCLC treated with tyrosine kinase inhibitor osimertinib. For these virtual patients, we compare time to progression under the considered evolutionary therapy protocols and the continuous MTD treatment under assumptions of varying measurement errors and appointment delays. We then summarize our findings as suggestions for the best evolutionary osimertinib protocol for metastatic NSCLC, accounting for the clinical realities.

2 Methods

2.1 The frequency-dependent Gompertzian model

We assumed that cancer eco-evolutionary dynamics follow the polymorphic frequency-dependent Gompertzian model with competition between sensitive and resistant cancer cell populations and log-kill osimertinib-induced death rate. The model was selected as it demonstrated the highest accuracy when fitted to the NSCLC patient data in previous studies (Soboleva et al., 2025b; Jansén-Storbacka et al., 2026). The model describes the eco-evolutionary dynamics of treatment-sensitive and treatment-resistant cancer cell populations denoted by $S(t)$ and $R(t)$, respectively, as follows:

$$\begin{cases} \dot{S}(t) = \rho_S\,S(t)\,\ln\left(\frac{K}{S(t)+\alpha_{SR}\,R(t)}\right) - \lambda\,S(t)\,C(t), \\ \dot{R}(t) = \rho_R\,R(t)\,\ln\left(\frac{K}{\alpha_{RS}\,S(t)+R(t)}\right), \end{cases} \tag{1}$$

where ρ_S and ρ_R are growth rates of sensitive and resistant populations, respectively, K is carrying capacity representing cancer cell population limit to growth due to space and resource constraints, α_{RS} and α_{SR} capture the competitive effect of sensitive population on the resistant one and vice versa, respectively, λ reflects how strongly treatment affects sensitive population, and $C(t)$ indicates the drug dose at time t. The total cancer population $N(t)$ at time t is defined as $N(t) = S(t) + R(t)$.

2.2 Virtual patients

The frequency-dependent Gompertzian model was parametrized using patient data from 37 patients with metastatic non-small cell lung cancer treated with first-line tyrosine kinase inhibitor osimertinib from the START-TKI trial (NCT05221372). The dataset comprises longitudinal volumetric measurements extracted from three-dimensional imaging, with CT scans used for lung lesions and MRI for brain metastases. The tumor burden $N(t)$ at every measured point was estimated as the sum of volumes of all measured lesions. We fitted parameters ρ_S, ρ_R, α_{SR}, α_{RS}, K, and λ of the frequency-dependent polymorphic Gompertzian model (1) individually to each patient's tumor burden trajectory by minimizing the mean squared error (MSE), obtaining one patient-specific parameter set per patient (37 in total). The empirical distribution of the fitted parameters was used to estimate a multivariate normal distribution, from which virtual patient parameter sets were sampled. These simulated patients were then used to compare containment-based evolutionary strategies with MTD therapy in terms of time to progression, defined as the first occurrence of total tumor burden exceeding $1.2N(0)$ (a 20% increase over baseline). In this framework, treatment effects were modeled exclusively through the treatment variables $C(t)$ and λ, while intrinsic growth and interaction parameters were assumed to be independent of the dosing schedule. This assumption allows us to simulate alternative treatment approaches and compare them to MTD. More information on the data and the fitting procedure is available at Appendix A1.

Based on the 37 parameter sets, we constructed a multivariate normal distribution from which we sampled 100 virtual patients, each representing a cancer dynamics described by an individually parametrized polymorphic Gompertzian model. We simulated the treatment dynamics by solving the ODE system 1 with the Runge–Kutte 45 method from the `solve_ivp` module in the `scipy.integrate` library in Python. To ensure realism of the virtual patients' dynamics, we only included the once with predicted time to progression under MTD protocol ($C(t) = 1\,\forall t$) below 3000 days. Furthermore, we did not include non-responders - virtual patients whose tumor size had not decreased below half of the initial size in the first 120 days of the treatment. Using virtual patients allowed us to explore a wider range of potential tumor dynamics.

2.3 Tested treatment protocols

In our study, we tested different evolutionary therapy protocols and assessed the outcomes in terms of time to progression. We defined progression as an increase in tumor burden by more than 20% of its initial tumor burden, following previous modeling studies (Viossat & Noble, 2021; Strobl et al., 2021; Gallaher et al., 2018). We considered binary on–off treatment protocols, in which the dose is fixed at MTD when administered and zero otherwise. In the model (1), the medication variable is

$C(t) \in \{0, 1\}$, where $C(t) = 1$ corresponds to the standard osimertinib dose of 80 mg. In the treatment protocols considered, the decision to stop or resume medication can be changed daily, reflecting the clinical reality of osimertinib administered as a daily pill. We assume that the test that measures tumor burden and the doctor appointment, at which the decision to stop or resume treatment is made, occur on the same day.

Let $\mathcal{T} = \{t_0, t_1, \ldots\}$ denote the discrete testing times with $t_0 = 0$ and $t_{i+1} > t_i$. Define the (continuous) time of progression as $\tau_{\mathrm{prog}} = \min\{t \geq 0 : N(t) > N_{\mathrm{prog}}\}$. Progression is observed at $t_K = \min\{t_i \in \mathcal{T} : t_i \geq \tau_{\mathrm{prog}}\}$. In simulations, treatment decisions are updated only at testing times and the simulation is terminated once progression is observed at t_K. We report τ_{prog} as the time to progression (TTP). In the simulations, we consider the following treatment protocols:

- **Continuous MTD treatment.** The current standard of care. Under this protocol, patients receive the constant treatment dose daily until progression. In the model, it is reflected as:

$$C(t) = 1 \, \forall t \tag{2}$$

- **Zhang et al.'s evolutionary protocol.** Patients receive a constant treatment dose until the tumor burden reaches the established lower threshold N_{min} (in the initial clinical trials $N_{\mathrm{min}} = 0.5 \, N(0)$ (Zhang et al., 2017, 2022)). The treatment is then paused until the tumor burden regrows to the upper threshold N_{max}, at which point it is resumed. This is repeated until progression. At each testing time point t_i, the treatment is set for the next interval between tests $(t_i, t_{i+1}]$ according to

$$C(t) = \begin{cases} 1, & \text{if } i = 0 \text{ or } N(t_i) \geq N_{\mathrm{max}}, \\ 0, & \text{if } N(t_i) \leq N_{\mathrm{min}}, \\ C(t_i), & \text{otherwise}, \end{cases} \qquad t \in (t_i, t_{i+1}]. \tag{3}$$

- **Containment protocol.** Unlike in Zhang et al.'s protocol, this protocol has a single threshold N_{cont}. The patient is treated at a constant dose until the tumor burden decreases below N_{cont}; then, treatment is paused. The treatment is resumed when the tumor size exceeds N_{cont}. At each testing point t_i, the treatment for the next interval is set as

$$C(t) = \begin{cases} 1, & \text{if } i = 0 \text{ or } N(t_i) \geq N_{\mathrm{cont}}, \\ 0, & \text{if } N(t_i) < N_{\mathrm{cont}}, \end{cases} \qquad t \in (t_i, t_{i+1}]. \tag{4}$$

2.4 Effect of appointment delay and measurement error

We incorporated appointment delays into the simulations to reflect clinical reality, where appointments are often postponed due to the doctor's scheduling conflicts, vacations, public holidays, worsening of the patient's condition, etc. The time to the next test was determined as the interval specified in the treatment protocol plus an additional delay sampled from a Poisson distribution (in days). The next testing moment is defined as the following:

$$t_i = t_{i-1} + \Delta t + \delta \tau, \tag{5}$$

where Δt is the established interval between tests and $\delta \tau$ is a random appointment delay in days, with $\delta \tau \sim \mathrm{Poisson}(\lambda)$. The delay was sampled independently at each testing point and was constrained to be non-negative, reflecting that appointments may be postponed but not advanced. We considered different mean values λ of the Poisson distribution ($\lambda \in \{2, 5, 7, 10, 15\}$), up to 15 days, corresponding to half of a standard 30-day testing interval. For each value of λ, we ran 1000 simulations to account for the stochastic nature of the delay process and analyzed the resulting distributions of TTP.

To account for measurement uncertainty in radiological assessments, we modeled the observed tumor volume at each testing point as the model-predicted tumor size multiplied by a stochastic error term drawn from a log-normal distribution:

$$N_{\mathrm{mes}}^i = N(t_i)\varepsilon_i, \tag{6}$$

where N_{mes}^i denotes the observed tumor burden at time t_i, $N(t_i)$ is the model-predicted tumor size at the time point t_i and $\varepsilon_i \sim \mathrm{LogNormal}(0, \sigma^2)$ represents multiplicative measurement error, sampled from log-normal distribution.

We modeled measurement error as multiplicative uncertainty relative to the model-predicted tumor size at the time point. In the log-normal distribution, we set $\mu = 0$ and considered $\sigma \in \{0.02, 0.05, 0.1, 0.2, 0.3\}$. These values correspond to increasing levels of variability, ranging from a minimal error of 2% to a high variability of 30%. The measurement error can both increase and decrease the actual tumor burden.

Because the error is sampled independently at each measurement time point, its cumulative effect on the treatment trajectory and the resulting TTP is stochastic and varies across simulation runs. Therefore, for each patient and each value of σ, we performed 1000 simulations to characterize the distribution of outcomes under measurement uncertainty.

We then assessed the joint effect of measurement error and appointment delay. We assumed error and delay to be independent, and for all combinations of λ for the appointment delay and σ for the measurement error, we ran 1000 simulations per patient and analyzed the distributions of TTPs.

2.5   Dynamically adjusted treatment protocol

We also simulated a dynamic containment protocol in which the containment threshold N^* is updated during treatment based on the tumor burden growth rate observed during medication-free intervals. The objective of this protocol is to maintain the containment level as high as possible to maximize the potential TTP benefit, while ensuring that the tumor burden cannot reach the progression threshold between successive evaluations. The protocol is inspired by the method proposed by Gallagher et al. (Gallagher et al., 2025), who derived the optimal threshold as the maximum level from which the untreated tumor cannot grow to the progression threshold within one testing interval.

In clinical practice, it is not feasible to reliably identify and parametrize a specific tumor growth model from sparse longitudinal measurements. Therefore, we employ a linear growth estimate to avoid model-specific assumptions and to assess the feasibility of dynamic containment under realistic clinical conditions.

To reduce the risk of premature failure due to growth-rate misestimation, we restrict the containment threshold to $N^* \in [0.4\,N(0), 0.8\,N(0)]$. The containment threshold cannot exceed 80% of the initial tumor burden to avoid an erroneous growth rate estimate, leading to a too-high containment threshold and premature failure. It also cannot be lower than 40% of the tumor burden, as in this case, the risk of resistance development is high and would undermine the concept of evolutionary therapy. The containment threshold N^* is determined at the end of each treatment-free interval as

$$N^* = N_{\mathrm{prog}} - g_i * \Delta t, \tag{7}$$

where Δt is the established interval between tests (not accounting for the appointment delay) and g_i is a linear growth rate at the ith measurement, calculated as

$$g_i = \frac{N_{\mathrm{mes}}(t_i) - N_{\mathrm{mes}}(\tau_i)}{t_i - \tau_i}, \text{ if } N_{\mathrm{mes}}(t_i) > N_{\mathrm{mes}}(\tau_i) \text{ and } C(t_i) = 0, \tag{8}$$

where t_i is the time of the ith measurement, $N_{\mathrm{mes}}(t_i)$ is the corresponding measured tumor burden, τ_i is the time of the last treatment pausing decision prior to t_i, $\tau_i = \max\{t_j < t_i : C(t_j) = 1\}$ and $N_{\mathrm{mes}}(\tau_i)$ is the tumor size measurement at this point. Note that we used the measured tumor burden $N_{\mathrm{mes}}(t_i)$ that may contain an error and not the model-predicted one $N(t_i)$ to estimate the growth rate.

For the dynamic containment protocol, we also implemented appointment delay and measurement error and assessed their effect on the model-predicted TTPs. The virtual patients' data, simulations, and the analysis code are available at: https://gitlab.tudelft.nl/evolutionary-game-theory-lab/clinical-feasibility.

Figure 1: **The cancer dynamics under constant treatment, Zhang et al.'s and containment protocols and Zhang et al.'s protocol with 30, 60 and 90 days intervals between tests.** Blue, orange and black lines indicate the dynamics of sensitive, resistant, and total cell populations, respectively. The yellow and green dotted lines show $N_{\max}$ and $N_{\min}$ levels of Zhang et al.'s protocol. The red dashed line indicates the progression threshold, denoted $1.2N(0)$. When the cancer burden reaches this threshold, the treatment protocol has failed. The gray areas indicate the periods during which the treatment was in effect. **A.** For all three protocols in these simulations, the decisions are made daily. Both Zhang et al.'s and containment protocols significantly increase time to progression compared with the constant-treatment protocol. The containment protocol yields a slightly higher TTP than Zhang et al.'s protocol, due to the higher containment level. **B.** Blue crosses indicate the points of measurement. The 90 days test interval leads to premature failure of the treatment protocol.

3 Results

3.1 Trade-off of the protocol threshold levels and the length of test intervals

We first simulated an unrealistic scenario of daily testing. Figure 1A illustrates the tumor burden dynamics under MTD, Zhang et al.'s and the containment protocols in such settings. The on/off medication cycles are repeated until progression, defined as tumor size exceeding $1.2\,N(0)$. Under Zhang et al.'s protocol, the patient undergoes extended periods of treatment and treatment holidays, whereas under the containment protocol, treatment is adjusted almost daily. Both Zhang et al.'s and the containment protocols result in a substantial increase in TTP compared to continuous treatment, in accordance with the theoretical results of Viossat and Noble that showed that both the containment and the intermittent containment (containment between two bounds as in Zhang et al.'s protocol) outperform MTD in terms of time to progression in cancer dynamics described by the Gompertzian model (Viossat & Noble, 2021).

We varied the upper bound $N_{\max}$ in Zhang et al.'s protocol and the containment level N_{cont} in the containment protocol. The benefits in terms of TTP were present across all patients at all threshold levels, but were more pronounced at higher thresholds. For more conservative bounds of $N_{\max} = 0.7$ for Zhang et al.'s protocol and $N_{\text{cont}} = 0.5$ for the containment protocol, the benefit in terms of TTP ranged among patients from 1.02 to 37.6, with a median of 2.07 for Zhang et al.'s protocol and from 1.01 to 37.6, with a median of 1.69, for the containment protocol. The TTP increase varies significantly between patients, but even if it is minimal, patients can still benefit from reduced medication use and the associated reduction in side effects. The patients, in general, were off medication for 40% of the treatment trajectory under Zhang et al.'s protocol and 33% under the containment protocol.

As daily follow-ups are unrealistic in clinical practice, in our simulations of the impact of different

treatment protocols, we considered monthly (30 days), bimonthly (60 days), and trimonthly (90 days) evaluations of tumor progression (see Figure 1B). In such settings, the tumor volume can decrease significantly below the lower bound of Zhang et al.'s protocol during the treatment period, and significantly exceed the upper bound during the treatment holidays. In the containment protocol, the cycling of the tumor burden also becomes less frequent, making it qualitatively similar to Zhang et al.'s protocol in reality.

The main risk of longer test intervals is the premature failure of the treatment protocol. Progression is premature if the tumor burden exceeds the progression threshold during the treatment holidays (see Figure 1B with a 90-day test interval). In this case, the sensitive cancer population may still be present, and the medication can still be effective, but the progression is declared, according to the definition of 20% increase from the initial size. The percentage of premature failures across virtual patients depends both on the intervals between tests and the bounds of evolutionary therapy protocols. However, even with low containment interval $N_{\text{cont}} = 0.5N(0)$, the 60-day interval between tests leads to premature failure for 78% of patients, and a 90-day interval for 90% of patients. We therefore fixed the interval between tests to 30 days and varied the bounds of the evolutionary therapy protocols. The increase in TTP with higher protocol thresholds is minimal, whereas it significantly increases the number of cases of premature failures (see Appendix A2). We therefore continue the analysis with Zhang et al.'s protocol with $N_{\text{min}} = 0.5N(0)$ and $N_{\text{max}} = 0.7N(0)$, and the containment protocol with $N_{\text{cont}} = 0.5N(0)$.

When tumor burden is evaluated at discrete time intervals, progression can only be detected at those measurement time points. As a result, the observed time to progression is effectively rounded up to the nearest evaluation time and therefore depends on the length of the testing interval. To avoid this discretization artifact, we report the actual time to progression (TTP), defined as the first time at which the tumor burden exceeds the progression threshold in the continuous model simulation.

With the established test interval and protocols' bounds, 44 out of 100 virtual patients demonstrated premature failure under both Zhang et al.'s and containment protocols. Essentially, those cases demonstrated growth from $0.5N(0)$ to $1.2N(0)$ in less than 30 days. In real clinical practice, such growth would be very unlikely. We therefore excluded these 42 cases from further analysis. Additionally, three patients experienced premature failure with Zhang et al.'s protocol but not with the containment protocol. This can be explained by Zhang et al.'s protocol's upper bound being higher than the containment threshold, making it riskier with longer test intervals. Furthermore, 15 virtual patients resulted in a TTP of 5000, which was the simulation time limit. Those virtual patients demonstrated unrealistically slow resistance development and were therefore excluded from further analysis. The parameter sets that result in unrealistic dynamics stem from limitations in the clinical data and the fitting procedure. As the virtual patients were sampled from the distribution based on the real patient fitted data, they also carry these abnormalities (see Appendix A1 for the details). The following steps were performed with 38 remaining virtual patients. These selected patients match the disease dynamics observed in clinical practice and add additional variation in regrowth rate and pattern, as well as in TTP under continuous treatment. We decided to continue the analysis with 38 virtual patients, to keep the number of cases manageable and convenient for visualization.

For 27 out of 38 virtual patients, the TTP under Zhang et al.'s protocol is higher than that under the containment protocol with 30-day test interval. This is explained by the higher tumor burden allowed in Zhang et al.'s protocol ($N_{\text{max}} = 0.7N(0)$), which results in higher TTP (Viossat & Noble, 2021).

3.2 Effect of appointment delay

Appointment delays can alter the treatment trajectory of evolutionary therapy protocols and lead to a decrease in the TTP. Figure 2A-B shows the principles of how a delayed testing moment can reduce TTP. Delays during the off-medication period are risky for patients with rapidly progressing cancer, as they may lead to premature failure within the same treatment cycle (Figure 2A). Delay during the on-medication period does not result in immediate protocol failure, but a prolonged on-medication interval kills more sensitive cells, allowing the resistant population to proliferate freely (Figure 2B). As a result, the tumor becomes resistant earlier, and TTP is shorter. In specific cases, appointment delays can be beneficial by allowing the tumor burden to grow above or decrease below the protocol bounds.

Figure 2: **The effect of the appointment delay on the TTP under Zhang et al.'s protocol.**
A-B Red, yellow, and green dashed horizontal lines demonstrate the progression threshold, upper and lower bounds of Zhang et al.'s protocol, respectively. The black line shows the total tumor burden up to the point of delay occurrence; after that, it shows the total tumor volume dynamics with delay, and the dashed line shows the dynamics without it. The orange circles indicate the measurement points along the treatment trajectory without delay, and the blue crosses indicate those with delay. Dashed blue and orange lines show the dynamics of the sensitive and resistant populations under the treatment trajectory without delay and the solid ones show the same for the treatment trajectory with delay. **A** The delay of appointment during the off-medication period leads to premature failure of the treatment protocol as the resuming of treatment is postponed. **B** The delay during the on-medication period leads to "overtreatment" - eradication of more sensitive cells and thus earlier emergence of resistance, leading to earlier progression. **C** The graph shows the medians of TTPs of 1000 simulations across increasing expected delay λ, normalized to the TTP under continuous treatment for the same patient. The crosses show the median TTPs for each value of λ and the shaded areas show the interquartile range. The patients demonstrate a range of sensitivity to the appointment delay. Patient 1009 shows only a slight decrease in median TTP, never falling below the MTD baseline. Patients 1062 and 1069 are robust to small expected delays, but the TTP decreases significantly with large appointment delays of more than a week. Patients 1020 and 1027 are extremely sensitive, as even a small expected delay leads to premature failure of the protocol.

This way, the delay prevents another interval without treatment, which would lead to premature failure or another interval on treatment, which would lead to earlier development of resistance (see Appendix A3).

Due to the stochastic nature of the delay in the simulations, the TTP across simulation runs can vary significantly. We used median TTP and interquartile ranges (IQR) for each patient and each λ value to assess the main tendency. The median and IQR were chosen over the mean and standard deviation because the distributions of TTPs are often non-normal and skewed. In the majority of virtual patients (24 out of 38 for Zhang et al.'s and 21 for containment), the median TTP decreased with increasing expected delay λ. For the remaining virtual patients, the median TTP either fluctuated or remained constant across mean delay values. The intensity of the decrease of the median TTP differs significantly across patients. Figure 2C demonstrates the decrease of the median TTPs under Zhang et al.'s protocol with the increase of the expected delay values λ for five patients. Patients 1027 and 1020 are very sensitive to delays, and even a 2- or 5-day expected delay leads to premature failure

of Zhang et al.'s protocol. For patients 1069 and 1062, Zhang et al.'s protocol is robust to short expected delays of up to a week, but the median TTP drops below the MTD baseline for sufficiently large values of λ. Finally, for the patient 1009, the median TTP decreases slightly but does not drop below the MTD baseline. This indicates that the risk of premature failure is low and the decrease in TTPs is attributed to earlier emergence of resistance due to longer periods of medicating. There is no significant difference in the sensitivity of Zhang et al.'s and the containment protocols to appointment delays. In the majority of cases, the median TTP of Zhang et al.'s protocol remains higher than that of the containment protocol across all tested values of λ (see Figure A3).

3.3 Effect of measurement error

Measurement error can affect treatment decisions at the testing point by making the measured tumor volume higher or lower than the protocol bounds. Figure 3 describes the ways measurement error can affect the treatment trajectory. For example, if the actual tumor burden is slightly above $N_{\max}$ (or N_{cont} for the containment protocol) and thus the treatment should be resumed, the error can make the measurement smaller, leading to another interval without treatment and potentially premature failure (see Figure 3B). If the true cancer burden is close to the progression threshold, an error making the measurement larger can lead to premature declaration of treatment failure (see Figure 3A). Further, an erroneous measurement can be higher than $N_{\min}$ (or N_{cont}), leading to an additional interval on medication, even though the actual tumor burden is below the threshold (see Figure 3C). Unnecessary treatment period in these cases promotes the development of resistance.

On the other hand, measurement error can lead to higher TTP in certain cases. For example, if the measurement is close to the upper bound but has not yet reached it, the error can cause it to exceed the upper bound and trigger resuming treatment. In this case, we avoid leaving a patient for another 30 days without treatment, during which the tumor burden might cross the progression threshold. Similarly, measurement error can help avoid an unnecessary treatment interval, which could have led to earlier resistance development.

In the simulations, measurement error decreased median TTPs for all patients under both Zhang et al.'s and the containment protocol, indicating that the negative effects of measurement errors outweigh any potential benefits as the error magnitude increases. However, errors lead to substantial variation in outcomes for the same patient. Figure 4B shows the distribution of TTPs across simulation runs for different log-scale standard deviation σ values for three patients. Median TTP decreases with increasing σ, but the interquartile ranges are wide. Two density peaks around a higher and a lower TTP value indicate two potential trajectories of treatment - one with almost no negative effect of errors and another with a very detrimental effect. For example, for patient 1045, Zhang et al.'s protocol with $\sigma = 0.1$ can result in a TTP close to the protocol baseline (significantly higher than under MTD) or below the MTD baseline. However, with higher values of σ, there is much lower variability in results. Most simulation runs result in TTPs lower than under MTD, thereby eliminating the benefits of Zhang et al.'s protocol.

We observed that Zhang et al.'s protocol is more sensitive to the measurement error than the containment protocol. While without error, the TTP of Zhang et al.'s protocol is not lower than that of the containment protocol for all the virtual patients, with $\sigma = 0.3$ this is true only for 9 out of 38 patients. In many cases, the decrease in the median TTP with increasing variance determined by σ is sharper for Zhang et al.'s than for the containment protocol (see Figure 4 A). This is explained by Zhang et al.'s having a higher upper bound than the containment protocol. Therefore, if the actual measurement is above $N_{\max}$ but, because of the error, the treatment was not resumed, in Zhang et al.'s protocol, the tumor burden is more likely to overgrow the progression threshold before the next testing moment.

3.4 Interaction between error and delay

For each combination of λ for appointment delay and σ for measurement error, we repeated the simulations 1000 times and obtained the TTPs. Because the distributions of TTPs for the same patient under the same conditions are often non-normal and skewed, we focused the analysis on the median TTP for each combination. The heatmaps show the changes of the median TTPs with increasing σ and λ values for each patient 5. The median TTPs are normalized to the protocol baseline, which is

Figure 3: **The logic of measurement error affecting the TTP of Zhang et al.'s protocol.**
Red, yellow, and green dashed horizontal lines demonstrate the progression threshold, upper and lower
bounds of Zhang et al.'s protocol, respectively. The black line shows the total tumor burden up to the
point of error occurrence; after that, it shows the total tumor volume dynamics with error, and the
dashed line shows the dynamics without it. The orange circles indicate the measurement points along
the treatment trajectory without error, and the blue crosses indicate those with error. Dashed blue
and orange lines show the dynamics of the sensitive and resistant populations under the treatment
trajectory without error and the solid ones show the same for the treatment trajectory with error.
A If the volume almost reaches the progression threshold during the period without treatment, an
error can increase the measurement and lead to the declaration of the treatment failure. **B** Error
decreases the actual tumor measurement, which has already reached $N_{\max}$. As a result, the treatment
is not resumed when it should have been, leading to another interval without medication during which
the tumor burden exceeds the progression threshold. **C** The top graph shows the treatment dynamic
without an error and the bottom graph - with a measurement error at 30 days test point. The error
raised the measurement above $N_{\min}$. The treatment is thus continued for another 30 days, leading to
a resistant population overgrowing the sensitive one. This results in the loss of one treatment cycle
and reduces TTP.

the TTP under the protocol for the patient without error or delay. The patients are classified into
4 clusters using K-Means clustering implemented in `scikit-learn` Python library (Pedregosa et al.,
2011). The virtual patients are clustered based on their sensitivity decomposition, which quantifies
the magnitudes of the effects of error, delay and their combination on each patient's median TTP (see
Appendix A4). The four clusters, the sensitivity decomposition and the median TTP change heatmaps
for 38 virtual patients under Zhang et al.'s protocol are presented in Figure 5.

The largest cluster (cluster 1) contains virtual patients for whom the measurement error plays the
major role in the variance of the median TTP. Those patients are almost unaffected by appointment
delays, but an error changes the median TTP significantly. In the heatmaps, the differences between
columns are more apparent than between rows. This is especially evident in cases of large values of
$\sigma = 0.2$ or $\sigma = 0.3$. For the virtual patients in cluster 0, in contrast, the appointment delay plays a
more significant role but does not have as much impact as the measurement error in cluster 1. For
many patients in this cluster, delays result in a notable drop in median TTPs. For the virtual patients
in cluster 2, the combination of errors and delays is prevalent in the sensitivity decomposition. The

Figure 4: **Effects of the increasing mean measurement error on the median and distribution of TTP for selected virtual patients. A.** Zhang et al.'s protocol is more susceptible to the measurement error than the containment protocol. The blue line and shaded area show the median TTP and interquartile range for patients under the Zhang et al protocol. The orange line and the shaded area show the same for the containment protocol. For the four illustrated patients, Zhang et al.'s protocol has a higher TTP without measurement error but decreases faster with higher measurement error variability σ. **B.** Higher values of σ result in high variability of TTP across simulations. Violin plots show distributions of TTPs across 1000 simulation runs for each value of σ.

heatmaps of median TTP changes indicate that these are extremely sensitive patient dynamics, for which even small measurement errors or delays result in premature failure of the treatment protocol. Finally, cluster 3 consists of patients for whom the error plays an important role, as in cluster 1, but delay also contributes. The error and delay intensify each other. For the same value of λ, a higher value of σ leads to a lower median TTP, and vice versa. For some patents in this cluster, while both components affect the median TTP, the magnitude of the effect is moderate (patients 1017 and 1073). They present a favorable case in which neither error nor delay eliminates the benefits of ECT. Overall, for the majority of patients, the effect of measurement error on median TTP is greater than that of appointment delay.

For the containment protocol, K-means clustering of the median TTP variance decomposition yields the same cluster categories (see Figure 6). The heatmaps show the changes in median TTPs, normalized to the patient's TTP under the containment protocol without error or delay. Compared with Zhang et al.'s protocol, the changes in median TTP are less significant. We then compare the median TTPs under Zhang et al.'s and the containment protocols for each combination of λ and σ for all patients. Table 1 shows the percentage of patients (out of 38) for whom the median TTP under Zhang et al.'s protocol is not lower than under the containment protocol for a combination.

A significant decrease in median TTP with an increase of λ and σ does not necessarily imply that the median TTP drops below that under MTD. As TTP under Zhang et al.'s is higher than that under the containment protocol without error or delay for the majority of patients, a more apparent relative decrease in median TTPs does not necessarily indicate the protocol's failure for higher values of λ and σ. To assess how probable the premature failure of the evolutionary therapy protocols is with an increase in error variability and expected delay, we compared the fraction of simulation runs out of 1000 that resulted in TTP exceeding that under MTD for each combination of λ and σ. Figure 7 compares the number of simulation runs that outperform MTD for two protocols for an example patient 1069. Low values of λ and σ have little effect on the outcomes of evolutionary protocols, whereas higher values lead to failure in the majority of cases. For the majority of the combinations, the containment protocol has more simulations with TTP higher than under MTD than Zhang et al.'s protocol.

Figure 5: **The change of the median TTP normalized to a protocol baseline under Zhang et al.'s protocol for 38 virtual patients divided into four clusters based on their sensitivity decomposition of the variation in the median TTP.** The heatmaps show the change in median TTP, normalized to Zhang et al.'s baseline (the TTP under no delay, no error conditions), across combinations of expected delay λ and error variance determined by σ. Each heatmap corresponds to a virtual patient. The virtual patients are divided into four clusters based on their sensitivity decomposition of the median TTP variance. The blue, orange and green bars indicate the fractions of the variation attributed to delay, error and their interaction.

To explore the role of the individual tumor growth rate in the resulting sensitivity of the cancer dynamics to delay and error, we simulated a 30-day unmedicated tumor growth period at the start of therapy and calculated the linear growth rates for all patients (see Figure A7). Figure A5 shows the changes in the fraction of simulations with TTP higher than under MTD across combinations of λ and σ for all 38 virtual patients, sorted by increasing linear unmedicated growth rate. The virtual patients with a lower growth rate are generally less affected by appointment delay and measurement error, but this does not explain all the variability of results (see Figure A5 and Figure A6).

3.5   Dynamically adjusted containment level

We then implemented the dynamically adjusted containment protocol, which estimates the tumor volume's linear growth rate without medication and adjusts the containment level to the maximum possible level, ensuring that the tumor volume does not exceed the progression line during the interval between tests. As linear estimation of the growth rate can be imprecise, in 5 patients, the dynamic containment protocol led to premature failure even without error or delay. In the remaining 33 out of 38 patients, the dynamic containment resulted in a TTP not lower than the containment protocol. In 13 of those patients, the resulting TTP was higher than under other evolutionary protocols, and in 19 patients, it was equal to that of Zhang et al.'s (which is always not lower than the containment

Figure 6: **The change of the median TTP of the virtual patients under containment protocol across delay and error combinations divided into four clusters based on the fraction of the variation attributed to delay error and their interaction.** The heatmaps show the change in median TTP under the containment protocol with increasing expected delay λ and error variance determined by σ. Each heatmap corresponds to a virtual patient. The median TTPs are normalized to the TTP under the containment protocol in no-delay, no-error conditions for this patient. The virtual patients are divided into four clusters based on the decomposition of median TTP variance. The blue, orange and green bars indicate the fractions of the variation attributed to delay, error and their interaction.

protocol in no delay, no error conditions).

The higher TTP of the dynamic containment protocol is attributed to the higher containment level that it aims to set. However, there is an increased risk of premature failure. Firstly, the dynamic containment protocol sets the containment bound as high as possible, but so that the tumor size does not exceed the progression threshold between tests. The linear growth rate used for that might not be a sufficiently accurate estimation and could overestimate a safe containment level. Secondly, in the calculations, the interval between tests is assumed without delays. Therefore, the protocol is sensitive to unexpected appointment delays. Lastly, the growth rate is estimated from tumor size measurements, which may contain errors. If the previous measurement was overestimated and the next is underestimated, the calculated growth rate can be much lower than the actual one, and the suggested containment bound is dangerously high. In this case, the error not only affects the treatment decision at each measurement point but also interferes with the protocol design.

To assess the safety of the dynamic containment protocol in clinically realistic conditions, we compared how the fraction of simulation runs with TTP higher than under MTD changes with increasing values of λ and σ, and compared it with constant-schedule evolutionary therapy protocols. Figure 8 shows the effect of measurement error and appointment delay on the fraction of TTPs higher than under MTD of the 7 patients under the three evolutionary therapy protocols. The heatmaps show the

	σ					
λ	0.00	0.02	0.05	0.10	0.20	0.30
0	100	97	89	71	34	26
2	97	97	87	53	34	21
5	89	92	76	47	37	29
7	84	84	71	34	34	26
10	87	79	79	53	42	32
15	84	87	71	50	45	34

Table 1: **The percentage of patients out of 38 with the median TTP under the containment protocol lower than that under Zhang et al.'s protocol across the values of expected appointment delay λ and measurement error variance determined by σ.** The columns indicate the values of log-scaled standard deviation σ of measurement error and the rows indicate the mean values of the appointment delay λ in days. While the TTP under Zhang et al.'s is not lower than under containment for almost all virtual patients with small σ and λ values, the fraction decreases as these values increase, indicating that the containment protocol is more robust to clinical conditions.

number of simulation runs (out of 1000) that resulted in TTP higher than under MTD, indicating the success of the evolutionary therapy protocol. The patients are arranged in order of increasing linear growth rate of the untreated tumor over 30 days (see Figure A7). The virtual patient with the lowest presented growth rate has a low risk of premature failure and only with large errors indicated by high values of σ. The higher linear growth rate corresponds to a larger effect of error and delay, with the last patient being affected even by small λ and σ. We can observe that the dynamic protocol has a rapidly increasing number of simulation runs resulting in premature failure with the increase of error and delay, especially noticeable in patients 1071, 1069. The dynamic containment protocol is more sensitive to errors and delays than constant protocols.

4   Discussion

In our study, we simulated clinically realistic conditions with monthly test intervals, appointment delays and measurement error and assessed the effects of these factors on the outcomes of evolutionary cancer therapy protocols. We demonstrated that longer delays and larger errors can undermine the benefits of the evolutionary therapy, however, the negative effects can be partially countered by the design of the treatment protocol. With our findings, we aim to aid the discussion between physicians and evolutionary therapy modelers by projecting the predictions of cancer growth models to more realistic clinical conditions and to support the design of clinical trials.

An especially prominent risk to consider is premature failure of ECT protocols due to the rapid growth of cancer burden during treatment holidays. In the simulations, progression was defined as tumor burden exceeding its initial size by 20% regardless of whether the medication is on or off at the time. It differs from the definition of progression used in an ongoing clinical trial on prostate cancer, where the progression can only be declared if the treatment is on. Using this definition would improve simulation outcomes in cases where the tumor burden slightly exceeds the progression threshold, but the sensitive population is still present, and the next treatment cycle is possible. However, tumor burden exceeding the progression threshold remains undesirable, as it may worsen cancer-related symptoms for patients and increase the likelihood of tumor mutations (He et al., 2025; West et al., 2023). The number of simulated patients was predicted to progress during the first treatment cycle because of the rapid growth of the untreated tumor. These cases are challenging to identify before treatment starts, as the information on the individual cancer dynamics is not collected. This necessitates especially frequent and thorough follow-up during the first treatment cycle. Another way to address the challenge would be to add a test on the day of the medication start. As this day is usually more than 4 weeks later than the diagnostic test, it would allow to estimate the growth rate of the untreated tumor, which is crucial for the safety of ECT protocols.

Appointment delay affects treatment outcomes by prolonging either the treatment-free interval, leading to premature failure, or the on-medication interval, enabling the growth of a resistant popu-

Figure 7: **The number of simulation runs out of** 1000 **across the combinations of** λ **and** σ **that resulted in a TTP higher than the MTD baseline for patient** 1069 **under Zhang et al.'s and the containment protocol.** In general, the containment protocol has a higher fraction of simulations that outperform MTD across the simulated conditions.

lation. If the delay during the treatment-free interval does not lead to premature failure, it would be considered beneficial in the modeling framework, as it allows for a higher containment level, which, in the model with the cost of resistance, promotes higher fitness of the sensitive population and thus prolongs the effectiveness of the treatment. However, in clinical practice, a higher tumor burden would likely mean more discomfort and more prevalent cancer symptoms for the patient, which would be a motivation to also avoid the delays during the off-medication period.

While an appointment delay only postpones a treatment decision, a measurement error can change the decision itself. This leads to an unnecessary interval (30 days in our simulations) with either medication administered, in which case it promotes resistance development, or without medication, in which case there is a risk of the tumor growing too large, leading to premature treatment failure or unwanted symptoms for the patient.

In simulation scenarios with both delay and error, the two factors often amplify each other. A higher error with the same mean delay would result in both a lower median TTP and a higher occurrence of premature failure, and vice versa. We observed that the error has a larger effect on decreasing the median TTP and increasing occurrences of premature failure. Furthermore, in clinical practice, we have less control over the measurement error than over appointment delay. When a delay occurs, we know its length and can account for it in the treatment design. With error, we cannot know the actual measurement and must always assume some level of it is present. In the simulation, small values of error variability $\sigma \leq 5\%$ have a minor effect on the outcomes of evolutionary therapy for the majority of virtual patients. Therefore, limiting measurement error would allow for the clinical implementation of evolutionary therapy. The use of technical advances, such as computer vision tools, can improve the accuracy and reduce the time required for lung lesion volume estimation (Xie et al., 2021; Primakov et al., 2022). Alternatively, the development of a less invasive and more easily quantifiable biomarker for NSCLC, such as ctDNA, can allow for more frequent and precise monitoring of disease progression. It is also important to consider that the error is usually higher in smaller lesions, as they are more difficult to measure in imaging and, thus, there is a larger uncertainty and disagreements between radiologists' measurements (Oxnard et al., 2011a; McNitt-Gray et al., 2015; Goodman et al., 2006; Henschke et al., 2016). At the same time, other differences in the response of larger tumors versus smaller tumors to ECT can be present (Gallaher et al., 2022), highlighting the importance of the individual cancer composition in the design of therapy.

Figure 8: **Comparison of Zhang et al., containment and dynamic containment protocols under increasing expected appointment delay (λ) and measurement error variability (σ).** The heatmaps show the fraction of 1000 simulation runs resulting in TTP higher than that under MTD across combinations of λ and σ for 7 patients under three treatment protocols. In general, the dynamic containment protocol is especially susceptible to errors and delays, while the containment protocol is the most robust.

Zhang et al.'s protocol results in higher TTP than the containment protocol in all patients under no-delay, no-error conditions, due to a higher containment level. However, the median TTP decreases sharply once errors and delays are introduced. The reason is that a higher upper bound in combination with appointment delays and measurement errors leads to a high risk of premature failure. To partially mitigate this risk, we implemented dynamically adjusted test intervals (see Appendix A5). The idea is to update the intervals between tests based on the decrease and regrowth rates of the tumor burden to better keep it within the bounds of Zhang et al.'s protocol. In the case of insignificant error and delay, this approach performs worse than Zhang et al.'s protocol with a constant schedule, as the resulting average containment level is lower, but it is more robust to higher errors and longer delays and might be preferred in clinical practice because it provides greater control over tumor size. The containment protocol, however, was demonstrated to be "safer" than Zhang et al.'s protocol even with a dynamic schedule. In the simulations, the containment protocol resulted in premature failure less often across combinations of error and delay. A protocol with a single containment bound is more robust to real clinical conditions of long intervals between tests. The tumor volume cycles around the bound and can grow or shrink further from it. As the difference between a measurement and the established threshold is larger, there is a lower risk that error will shift the measurement relative to the bound and affect the treatment decision.

We also tested the dynamically adjusted containment protocol, in which the containment bound is determined based on the tumor's linear growth rate during the medication-free interval. As the protocol aims to set the containment level as high as possible, it led to higher TTPs than those under Zhang et al.'s and the containment protocols in 19 out of 38 patients in the no-delay, no-error setting. However, with a large error and long delay, it performs worse than the constant-schedule protocols in terms of TTP. The estimated containment level is highly affected by measurement errors, because the growth rate is calculated from the erroneous measurements, and by appointment delays, because the tumor burden is supposed to grow to progression lines between tests, but does not account for unexpected delays. As a result, an imprecise growth rate estimate and a subsequent overly high containment level lead to premature failure.

There is a trade-off between a larger TTP benefit from maintaining a higher cancer burden and greater safety from keeping the tumor burden lower. When dealing with a fast-growing type of cancer and accounting for clinically realistic intervals between tests, avoiding tumors going untreated for a long time should be a priority. As individual cancer dynamics play a crucial role in ECT outcomes, starting with a conservative threshold of 50% of the initial tumor burden would be preferred. For

patients with a high rate of tumor regrowth, careful follow-up should be a priority. This can include high-resolution scans to reduce measurement error, more strategic appointment planning and avoiding delays. If the rate of regrowth is moderate, the focus can be on maximizing TTP benefit by setting the containment level higher. However, it is important to recognize the risks of such an approach, as it is particularly sensitive to errors and unexpected delays.

The proposed modeling framework provides an opportunity to evaluate potential clinical scenarios of evolutionary cancer therapy for NSCLC and assess its clinical feasibility before real-world implementation and resource allocation. Nevertheless, several limitations of the modeling approach should be considered. First, the study relies on virtual patients based on clinical cancer dynamics observed under continuous MTD treatment. The cancer dynamics under evolutionary therapy protocols were then predicted by the model and may not fully reflect those of real patients. Further, the resistant cell population was assumed to be almost absent at the beginning of treatment, based on clinicians' observations that patients rarely have preexisting resistance to the first-line treatment. A larger initial resistant population would likely change the predicted evolutionary dynamics and treatment outcomes.

The linear growth rate estimation used in the dynamic containment protocol and for dynamic test scheduling represents a simplified approximation of tumor dynamics. Incorporating a cancer growth model can more accurately suggest an optimal containment threshold. However, in practice, it is not clear which of the various cancer growth models to use or how to properly parameterize them with the scarce medical data. Further, such a modeling task would likely require a multidisciplinary team involved in designing a patient's treatment trajectory, which is not feasible in wide clinical practice. Linear growth cannot be safely applied to high-precision protocols and scheduling tailoring, but if the aim is simply to identify slow and fast growers, it can be sufficient. Finally, we only considered binary evolutionary therapy protocols, in which the treatment is either on or off at each time point, and not dose-modulation ECT protocols (Cunningham et al., 2020a; Hockings et al., 2023; Salvioli et al., 2024). Such protocols may be a preferable option for rapidly growing cancers, where complete treatment interruption for a prolonged period may be undesirable. However, the dose-modulation protocols would likely require even more accurate tracking of disease progression and more frequent follow-up, potentially including the development of biomarkers. The feasibility of such treatment protocols in clinical realities should be evaluated in future studies.

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A1 Parameterizing the cancer dynamics model with patient data and creating virtual patients

In the study, we used data from the START-TKI trial (NCT05221372). The START-TKI trial is conducted in accordance with the Declaration of Helsinki. Ethical approval for the trial was granted by the Medical Ethics Review Committee (METC) of Erasmus Medical Center, Rotterdam, The Netherlands (MEC 16-643) in accordance with the Dutch Medical Research Involving Human Subjects Act (WMO). Informed consent was obtained from all patients prior to enrollment in the trial. This study does not use any identifiable or individual-level patient data from START-TKI trial.

All patients are patients with metastatic non-small cell lung cancer treated with osimertinib. The data consist of time-series measurements of the tumor's longest diameters across three projections. We defined tumor volumes as volumes of ellipsoids with radii equal to the observed measurements. We calculated the total tumor burden as the sum of all measured lesions at every time point. If measurements of different lesions were performed within a week of each other, we assumed they were taken on the day of the primary lung lesion measurement. As we are interested in tumor response to osimertinib treatment, tumor measurements obtained after switching to a different medication were excluded.

The polymorphic Gompertzian model was fitted to the time-series data for total tumor volume for 37 patients. As the patients were treated with first-line osimertinib, we assumed almost no preexisting resistance and set the initial total tumor burden to be $N(0) = S(0) + R(0)$, with the initial resistant and sensitive populations set to $R(0) = 5 \cdot 10^{-6} \cdot N(0)$ and $S(0) = N(0) - R(0)$. The remaining model parameters were estimated using Python 3.12.3 with the differential evolution algorithm (Storn & Price, 1997) implemented in the `scipy.optimize` library. Differential evolution (DE) is a global optimization algorithm designed for continuous, non-linear problems. The model was fitted to the data by solving the differential equations with the Runge–Kutte 45 method from the `solve_ivp` module in the `scipy.integrate` library.

In the fitting procedure, we applied the following bounds for the parameter values. For the growth rates ρ_R and ρ_S the bounds are 0.0001 and 0.06. We set treatment sensitivity λ to be between 0.0001 and 0.2.The lower and upper bounds for the competition coefficients α_{SR} and α_{RS} were set at 0.1 and 10, respectively. The bounds for the carrying capacity K were set individually for each patient as $1.3N(0)$ and $5*10^5$. The parameter bounds and the fitting procedure are analogous to the previous study on similar patient data (Jansén-Storbacka et al., 2026).

Due to imperfections in the data and potentially limitations of the fitting procedure, some of the obtained parameter values were on the bounds, resulting in unrealistic cancer dynamics under treatment. Some patient records showed no tumor regrowth because the patients were still in treatment, or only slight regrowth, which, however, was sufficient to declare progression under RECIST criteria. According to RECIST, progression is declared when there is a 20% increase in one of the longest diameters from its minimum size (Eisenhauer et al., 2009b). In the total tumor volume, such an increase can be very small and may be ignored during model fitting. In these cases, the model estimates that resistance develops very slowly, resulting in TTP above 3000 days. Another abnormality in the data is the extremely rapid tumor growth without treatment, which likely stems from the model's growth rate values being too high. As the model is fitted to tumor dynamics under continuous treatment, extreme growth rate values are compensated by the treatment variable and only become apparent in the protocols with treatment holidays.

To avoid these abnormalities and broaden the range of potential dynamics to consider, we created virtual patients by sampling parameters from a multivariate normal distribution derived from the fitted models. We applied the same parameter bounds that were used in the fitting procedure. To ensure clinical realism, we only sampled patients with TTP below 3000 days under continuous treatment.

A2 Choosing the optimal protocols' bounds

For Zhang et al.'s protocol, we tested various values of $N_{\max} = k_{\max}N(0)$ with $k_{\max} \in \{0.6, 0.7, 0.8, 0.9, 1.0\}$). For the containment protocol, we tested containment levels $N_{\text{cont}} = k_{\text{cont}}N(0)$ with $k_{\text{cont}} \in \{0.5, 0.6, 0.7, 0.8, 0.9, 1.0\}$. For each level, we simulated treatment trajectories for all 100 virtual patients and assessed TTPs and the percentage of premature failures (cases in which the tumor burden exceeds the progression threshold during the treatment-free interval). Table A2 presents the number of cases when the given threshold value leads to the maximum TTP across all $N_{\max}$ and the percentage of premature failure for each of the threshold values. We considered both indicators to determine the optimal thresholds. For the containment protocol $N_{\text{cont}} = 0.5$ has the highest percentage of the best results and the lowest percentage of the premature failures. We therefore decided to focus on this value in the main analysis of the study. In Zhang et al.'s protocol, $N_{\max} = 0.7$ has the second highest percentage of the best TTPs (only 1 percent lower than the maximum) and a significantly lower percentage of premature failures than $N_{\max} = 0.8$. This level was chosen as optimal for Zhang et al.'s protocol for further simulation.

	Zhang et al.			Containment	
$N_{\max}$	% best results	% premature failure	N_{cont}	% best results	% premature failure
–	–	–	0.5	67	43
0.6	75	44	0.6	57	51
0.7	79	45	0.7	60	55
0.8	80	53	0.8	58	63
0.9	79	63	0.9	58	71
1.0	69	74	1.0	51	82

A3 Increase of TTP due to appointment delay

In a few particular cases, appointment delay can increase TTP under Zhang et al.'s protocol. Three patients who demonstrated premature failure under Zhang et al.'s protocol but not under the containment protocol showed an increase in median TTP with increasing mean appointment delay (see Figure A1). This reflects the disadvantage of the strict upper bound in Zhang et al.'s protocol. If the current measurement is close to the upper bound but has not yet reached it, the treatment pause continues for an additional 30 days until the next test, during which the tumor burden grows to the progression level. In this case, a one-week delay of the appointment would lead to the restart of the treatment at the current appointment, thereby prolonging or avoiding premature failure (see Figure A1).

Figure A1: **Appointment delay can help to avoid the premature failure of Zhang et al.'s protocol.** The graph on the left shows the dynamics of the median TTP for three virtual patients for whom Zhang et al.'s protocol, but not the containment protocol, resulted in premature failure in the delay-free conditions. The shaded area reflects the interquartile ranges. Median TTP increases with the appointment delay for these patients. The right side shows the treatment dynamic of patient 1081 under constant 30 days test intervals (top) and one of the simulation runs with the mean appointment delay of 15 days (bottom). In the first case, the cancer burden does not reach $N_{\max}$ after 30 days without medication, leading to the continuation of the treatment pause for another 30 days, during which it exceeds the progression threshold. With the appointment delay, the initial interval without treatment is longer than 30 days, allowing the cancer burden to grow beyond $N_{\max}$ but not beyond N_{prog}. The treatment is renewed at this time point, resulting in a delay of premature failure and higher TTP.

A4 Sensitivity decomposition of the median TTP values

For each virtual patient, we obtained a 6-by-6 matrix of median TTPs $Y \in \mathbb{R}^{6 \times 6}$ as the results of 1000 simulation runs. The rows and columns of the matrix correspond to the mean appointment delay λ and measurement error σ, respectively. For each patient and each treatment protocol (Zhang et al.'s and containment), we quantified the variability in median TTPs arising from delay, error, and their combination. For this, we implemented the following procedure, based on the two-factor ANOVA variance decomposition. A full parametric ANOVA was not performed because the simulated outcomes do not meet the normality assumption required for the test. Our focus in this analysis was on variance attribution to delay and error rather than on hypothesis testing.

We first calculate the overall mean across all delay-error combinations as

$$\mu = \frac{1}{36} \sum_\lambda \sum_\sigma Y_{\lambda,\sigma}; \tag{9}$$

and then the total variance as the mean squared deviation from the overall mean:

$$V_{\text{tot}} = \frac{1}{36} \sum_\lambda \sum_\sigma \left(Y_{\lambda,\sigma} - \mu\right)^2. \tag{10}$$

We then compute the variance attributed to delay as:

$$V_{\text{delay}} = \frac{1}{6} \sum_\lambda \left(\bar{Y}_\lambda - \mu\right)^2, \tag{11}$$

where $\bar{Y}_\lambda$ is the average over measurement error for each mean delay value:

$$\bar{Y}_\lambda = \frac{1}{6} \sum_\sigma Y_{\lambda,\sigma}. \tag{12}$$

Similarly, the variance attributable to measurement error is

$$V_{\text{error}} = \frac{1}{6} \sum_\sigma \left(\bar{Y}_\sigma - \mu\right)^2, \tag{13}$$

where $\bar{Y}_\sigma$ is the average over delay for each mean measurement error value:

$$\bar{Y}_\sigma = \frac{1}{6} \sum_\lambda Y_{\lambda,\sigma}. \tag{14}$$

We then normalized the variances attributed to the delay and error to the total variance:

$$S_{\text{delay}} = \frac{V_{\text{delay}}}{V_{\text{tot}}}, \qquad S_{\text{error}} = \frac{V_{\text{error}}}{V_{\text{tot}}}. \tag{15}$$

The remaining proportion of variance was assigned to the interaction of delay and error:

$$S_{\text{inter}} = 1 - S_{\text{delay}} - S_{\text{error}}. \tag{16}$$

For each patient and each protocol, we calculated what fraction of the variance is attributed to delay, error and their combination ($S_{\text{delay}}, S_{\text{error}}, S_{\text{inter}}$). Based on these values, the virtual patients were clustered into 4 clusters using K-Means clustering implemented in `scikit-learn` Python library (Pedregosa et al., 2011).

A5 Zhang et al.'s protocol with dynamic test schedule

We tested the scenario where the time of the next follow-up under Zhang et al.'s protocol is determined based on the rate of tumor burden progression. The dynamic scheduling uses linear estimation of tumor growth without medication and tumor decline under treatment to determine how long it would take for the tumor burden to grow to $N_{\max}$ or to shrink to $N_{\min}$. Based on this information, the test intervals are updated. In clinical practice, an interval of less than a month is unlikely to be feasible. At the same time, not performing a follow-up for longer than 3 months is dangerous for cancer patients. We therefore enforced the intervals calculated from the linear growth/decline rate to be between 30 and 90 days.

We implemented rounding up in the dynamic scheduling. If at the test point it is observed that the tumor burden decreased under medication but has not yet reached $N_{\min}$, the time needed to reach the threshold is calculated based on the tumor burden's linear decline rate. If it would require less than 14 days, roughly half the standard test interval, the treatment is resumed. Similarly, if the tumor burden at the end of a treatment-free interval has not reached $N_{\max}$ but is estimated to do so within 14 days, the treatment is resumed. This allows to avoid the situations where the tumor burden almost reaches $N_{\min}$ or $N_{\max}$, but has to go another 30 days with or without medication, respectively. That can lead to either overtreating or a higher risk of premature failure and symptoms related to higher tumor burden. From a medical perspective, it is undesirable to allow the tumor burden to reach the initial size or exceed it. Optimizing test scheduling helps maintain tumor burden within the bounds set by Zhang et al.'s protocol, thereby improving therapy outcomes for some patients. At the same time, for some patients, the required test frequency under dynamic scheduling would be lower than every 30 days, thereby decreasing the cost of treatment and the burden on healthcare facilities.

A5.1 Dynamic test scheduling algorithm

Let $t_0 = t(0) < t_1 < \ldots < t_K = \min t : N(t) > N_{\text{prog}}$ denote the discrete testing time points at which tumor burden is assessed, repeated until progression, and $N_{\text{mes}}(t_i)$ the corresponding tumor burden. The treatment status at time t is denoted by $C(t) \in \{0, 1\}$, where $C(t) = 1$ indicates treatment on and $C(t) = 0$ treatment off. At each measurement time t_i, we estimate the linear rate of change of tumor burden over the previous interval based on the medication on/off status.

Rate estimation. Let τ_i be the most recent time prior to t_i at which the treatment status was switched, $\tau_i = \max \{t_j < t_i \ : \ C(t_j) \neq C(t_i)\}$, and $N_{\text{mes}}(\tau_i)$ the tumor burden at that time.

- If $C(t_{i-1}) = 1$ (treatment on) and $N_{\text{mes}}(t_i) < N_{\text{mes}}(t_{i-1})$, the decline rate is estimated as

$$g_{\downarrow}^i = \frac{N_{\text{mes}}(\tau_i) - N_{\text{mes}}(t_i)}{t_i - \tau_i}. \tag{17}$$

- If $C(t_{i-1}) = 0$ (treatment off) and $N_{\text{mes}}(t_i) > N_{\text{mes}}(t_{i-1})$, the growth rate is estimated as

$$g_{\uparrow}^i = \frac{N_{\text{mes}}(t_i) - N_{\text{mes}}(\tau_i)}{t_i - \tau_i}. \tag{18}$$

Prediction of the bound crossing.

- If $C(t_{i-1}) = 1$ and $N_{\text{mes}}(t_i) > N_{\min}$, the predicted time until reaching $N_{\min}$ is

$$dt_i = \frac{N_{\text{mes}}(t_i) - N_{\min}}{g_{\downarrow}^i}. \tag{19}$$

- If $C(t_{i-1}) = 0$ and $N_{\text{mes}}(t_i) < N_{\max}$, the predicted time until reaching $N_{\max}$ is

$$dt_i = \frac{N_{\max} - N_{\text{mes}}(t_i)}{g_{\uparrow}^i}. \tag{20}$$

Figure A2: **The treatment trajectory of an example patient 1079 under Zhang et al.'s protocol with the constant test schedule (top) and dynamically adjusted test schedule (bottom).** Red, yellow, and green dashed horizontal lines indicate the progression threshold, upper and lower bounds of Zhang et al.'s protocol, respectively. The black line shows the total tumor burden, and the blue and orange lines show the dynamics of sensitive and resistant cancer populations. The blue crosses indicate the measurement points along the treatment trajectory. The dynamic test schedule decreases the length of on-medication periods and thus delays the development of resistance. **TTP** - time to progression. **Mean int** - mean length of the intervals between tests.

Treatment switching and scheduling. If the predicted time to reach the bound satisfies $dt_i < 14$ days, the treatment is switched at t_i, i.e.

$$C(t_i) = 1 - C(t_{i-1}), \tag{21}$$

and the next appointment is scheduled based on the rate corresponding to the new regime.

If $dt_i \geq 14$ days, the time to the next appointment is set as

$$dt = \min\big(\max(dt_i, 30), 90\big), \tag{22}$$

ensuring that the next test occurs no earlier than 30 days and no later than 90 days.

A5.2 Results

When simulated in no error, no delay conditions, Zhang et al.'s protocol with dynamic scheduling outperforms MTD in terms of TTP for all 38 patients. Further, for 30 patients, the TTP is not lower than that of the containment protocol, and for 10 is higher than that of Zhang et al.'s protocol with a constant schedule. Figure A2 shows an example of virtual patient 1079, for whom the dynamically adjusted test schedule led to an increase in TTP under Zhang et al.'s protocol. The medication periods were adjusted to a single longer interval rather than two standard intervals, resulting in less time on medication and, thus, postponed development of resistance.

We applied appointment delay and measurement error, as previously done for the protocols with constant schedules. For each delay-error combination, we compared the median TTPs between Zhang et al.'s protocol with the dynamic schedule and the constant schedule. Table A1 shows the percentage of virtual patients for whom the median TTP was higher under Zhang et al.'s protocol with the constant schedule than with the dynamic schedule (left) and for whom the median TTP under the

Zhang et al. vs dyn sched Zhang et al.							Containment vs dyn sched Zhang et al.					
	σ							σ				
λ	0.00	0.02	0.05	0.10	0.20	0.30	λ	0.00	0.02	0.05	0.10	0.20	0.30
0	74	66	50	47	39	32	0	45	34	24	26	79	82
2	76	71	68	39	26	32	2	34	26	29	29	74	82
5	74	76	68	39	39	32	5	39	37	42	42	79	74
7	68	68	58	39	39	32	7	42	42	42	45	74	82
10	71	66	63	55	37	34	10	45	42	42	50	71	74
15	58	63	53	50	55	37	15	47	50	45	47	74	76

Table A1: **Percentage of virtual patients for whom the median TTP is higher under Zhang et al.'s protocol with the constant test schedule than with the dynamic schedule (left) across delay and error combinations.** The left part of the table shows the percentage of virtual patients for whom the TTP under Zhang et al.'s protocol with a constant schedule was higher than that with a dynamic schedule. The right part of the table shows the percentage of virtual patients for whom the median TTP under the containment protocol with a constant schedule was higher than under Zhang et al.'s protocol with a dynamic schedule. The rows indicate the mean delay λ in days, and the columns - the mean measurement error σ as a fraction of the actual measurement. Zhang et al.'s protocol with a constant schedule yields the highest TTP for the majority of patients with no or little error, but if the error is large, the dynamically adjusted schedule outperforms the constant schedule, but the containment protocol is still preferred over the Zhang et al.'s protocol.

containment protocol was higher than under Zhang et al.'s protocol with dynamic schedule (right) for each combination of λ and σ.

When the measurement error variability, denoted by σ, is small, Zhang et al.'s protocol with the constant schedule results in a higher median TTP than Zhang et al.'s protocol with the dynamic schedule for the majority of virtual patients. This is explained by longer treatment-free intervals allowing the tumor burden to grow to a larger size, thereby increasing TTP in the model's predictions. However, with large values of σ, the median TTPs for most virtual patients are higher under the dynamic-schedule Zhang et al.'s protocol. At the same time, the percentage of virtual patients for whom the containment protocol results in a higher median TTP than the dynamic-schedule Zhang et al.'s protocol increases significantly with higher values of σ. This indicates that when a large measurement error is present, the containment protocol performs better than Zhang et al.'s protocol, even with a dynamically adjusted schedule.

A6   Figures

Figure A3: **The dynamics of the median and interquartile range of TTPs with increasing expected appointment delay for** 38 **virtual patients under both Zhang et al.'s and containment protocol.** The blue crosses indicate the median TTP of 1000 simulation runs under Zhang et al.'s protocol. The blue-shaded area shows the interquartile range. The orange crosses and shaded area show the same for the containment protocol. The TTPs are normalized by the MTD baseline - TTP under the MTD protocol without delay, which is indicated by the red dashed line.

Figure A4: **The dynamics of the median and interquartile range of TTPs with increasing measurement error variability (σ) for 38 virtual patients under both Zhang et al.'s and containment protocols.** The blue crosses indicate the median TTP of 1000 simulation runs under Zhang et al.'s protocol. The blue-shaded area shows the interquartile range. The orange crosses and shaded area show the same for the containment protocol. The TTPs are normalized by the MTD baseline - TTP under the MTD protocol without error, which is indicated by the red dashed line.

Figure A5: **Heatmaps of the fraction of the simulation runs resulting in TTP higher than the MTD baseline under Zhang et al.'s protocol, containment and dynamic containment protocols for all** 38 **patients.** The virtual patients are sorted in accordance with increasing unmedicated growth rate (see Figure A7).

Figure A6: **The change in median TTP with increase of measurement error variability** **(σ) and expected appointment delay (λ) normalized to the protocol baseline (TTP in no** **error, no delay conditions) under Zhang et al.'s, containment and dynamic containment** **protocols for all 38 patients.**

Figure A7: **The unmedicated linear growth rate of** 38 **virtual patients.** The linear growth rate was estimated by simulating tumor volume growth in the absence of treatment at the start of treatment. The patients marked in orange are those for which heatmaps of the fraction of simulations with TTP higher than under MTD are presented in Figure 7.