Phase i trials in melanoma: A framework to translate preclinical findings to the clinic

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One Sentence Summary:

We propose a computational framework to implement phase i trials (virtual/imaginary yet informed clinical trials) in cancer, using an experimentally calibrated mathematical model of melanoma combination therapy, that can readily capture observed heterogeneous clinical outcomes and be used to optimize future clinical trial design.
Abstract

We present a, mathematical model driven, framework to implement virtual or imaginary clinical trials (phase i trials) that can be used to bridge the gap between preclinical studies and the clinic. The trial implementation process includes the development of an experimentally validated mathematical model, generation of a cohort of heterogeneous virtual patients, an assessment of stratification factors, and optimization of treatment strategy. We show the detailed process through application to melanoma treatment, using a combination therapy of chemotherapy and an AKT inhibitor, which was recently tested in a phase 1 clinical trial. We developed a mathematical model, composed of ordinary differential equations, based on experimental data showing that such therapies differentially induce autophagy in melanoma cells. Model parameters were estimated using an optimization algorithm that minimizes differences between predicted cell populations and experimentally measured cell numbers. The calibrated model was validated by comparing predicted cell populations with experimentally measured melanoma cell populations in twelve different treatment scheduling conditions. By using this validated model as the foundation for a genetic algorithm, we generated a cohort of virtual patients that mimics the heterogeneous combination therapy responses observed in a companion clinical trial. Sensitivity analysis of this cohort defined parameters that discriminated virtual patients having more favorable versus less favorable outcomes. Finally, the model predicts optimal therapeutic approaches across all virtual patients.
Introduction

Significant advances have been made in understanding mechanisms that provoke tumor initiation and progression, and often this knowledge has been translated into the development of targeted agents that selectively disable the mutated, activated and/or overexpressed oncoproteins manifest in tumor cells (1). Most of these targeted agents have been tested in clinical trials either alone or in combination with other treatments (2), and though some are clinically effective (e.g., small molecule BRAF kinase inhibitors (3)), the majority are not (4-6) despite the fact that such agents have potent activity in preclinical cancer cell and animal model studies. The leading cause of failure tends to be lack of efficacy, in part due to lack of robust predictive models that consider patient heterogeneity, and poorly designed clinical trials (6-9). This inconsistency is also partly due to difficulties in predicting the long-term effectiveness of a cancer therapy using time-limited in vitro (typically < 1 month) or in vivo (often < 3 months) models systems.

We reasoned that an appropriately defined and parameterized mathematical model, based on observations in cell and animal studies and clinical trials, might reveal insights regarding the design of improved and informed therapeutic approaches for treating cancer patients. To test this notion we used a mathematical model of melanoma that was generated based on data from in vitro experiments and a distribution of treatment responses (Fig 1A) from a comparable clinical trial. More specifically, the recently completed multi-arm phase 1 trial of the MK2206 AKT inhibitor (AKTi) in combination with standard chemotherapy (chemo) with advanced solid tumors, including melanomas (10) was used for these studies. To investigate potential mechanisms of treatment efficacy, a mathematical model comprised of a system of ordinary differential equations was
developed to describe the dynamics of melanoma cells exposed to four treatment conditions, no treatment, chemo, AKTi and combination of chemo and AKTi. Cell culture experiments were then used to parameterize the model. The calibrated model was further validated using results from an extensive series of cell culture experiments that consider twelve different drug combinations and timings. This validated model was then used to predict the long-term effects of the twelve treatments on melanoma cells, which revealed that all treatments eventually fail, but do so at significantly different rates.

To investigate the long-term effects of therapy in a more clinically relevant setting, we varied model parameters to generate virtual patients that had a heterogeneous mix of responses similar to typical clinical trial outcomes (Fig. 1A and (10)). We employed a heuristic search algorithm (genetic algorithm (GA)) to generate a diverse virtual patient cohort consisting of over 3,000 patients. Treatment responses for this patient cohort were simulated and optimized, and the schedules of AKTi therapy were combined with chemotherapy. This strategy allowed implementation of a “virtual clinical trial” (phase i trial), where the model guides optimal treatment strategies for selected patient cohorts (11). Similar virtual clinical trials have been made to simulate clinical trials of cardiovascular disease, hypertension, diabetes (www.entelos.com), and acute inflammatory diseases (12). There have also been some previous studies that employed modeling approaches to predict outcomes of clinical trials (13, 14). Statistical approaches based on clinical drug metabolism (e.g., dose-concentration relationships) have also been developed to design virtual clinical trials (reviewed in (15)) that detect significant differences between treatments (for example, placebo vs. treatment). Here we rather sought to translate biological findings coming from in vitro and clinical studies, using
melanoma combination therapy, into a phase i trial - with the goal that this approach could be easily adapted to other cancers.

Results

Responses of melanoma treated with combination therapy

We reported unexpectedly long-term responses (of up to 15 months) to the combination therapy of chemo and AKTi in two BRAF-wild type melanoma patients in the trial (NCT00848718) (16). Although little was known regarding why this combination therapy was successful, we reasoned this reflected differential effects on inducing autophagy that were observed in Figure 1B. Autophagy represents a cancer cell-intrinsic mechanism of resistance that allows cells to survive times of drug-induced stress (17, 18) or, if uncontrolled, can deplete key cellular components and provoke tumor cell death (19, 20). Differential autophagic responses to the chemo plus AKTi combination and accompanying effects on tumor cell growth and survival were manifest in melanoma cells (Fig. 1B) (16).

Mathematical model development

Motivated by these experimental results, we formulated a mathematical model comprised of three phenotypic compartments (Fig. 2A(a)), a non-autophagy compartment (N) and two autophagy compartments (P and Q). We divided the autophagy compartment into two, physiological autophagy (P) and quiescent autophagy (Q) compartments, based on studies showing that some cells where autophagy is manifest continue to maintain normal cell homeostasis whereas others did not (21-24). Figure 2A shows the interactions between the
N, P and Q compartments within the four different environments: (a) no-treatment, (b) chemo, (c) AKTi, and (d) combination therapy (chemo+AKTi) (see the Materials and Methods section for a detailed description of model development).

To calibrate model parameters, two melanoma cell lines (M257 and WM3918) were treated with the four different conditions for 8 days and the results were compared with the model predictions. Using an optimization technique to minimize the difference between predicted and actual growth curves (see Materials and Methods) we obtained two suites of parameters that produced good fits ($R \geq 0.8$, for all cases) for the growth of each cell line (Fig. 2B). Chemo reduced growth rates of both WM3918 and M257 (Fig.2B, Chemo panels) and continuous application of AKTi increased the proportion of the non-autophagy (N) to physiological autophagy (P) phenotype (Fig. 2B, AKTi panels, increasing green lines). The combination of AKTi and chemo generally induced the quiescent autophagy (Q) phenotype (Fig. 2B, combination panels, increase of red lines), which arose following the rapid transition of a non-autophagy to physiological autophagy phenotype (Fig. 2B, combination panels, a sharp increase in the green line < day 1). The number of cells in the total cell population treated with the combination therapy continued to decrease as a result of cell death of the Q phenotype (Fig. 2B, combination panels, decreasing red lines).

**Model prediction and validation with preclinical data**

The calibrated model was used to predict the effects of twelve treatment schedules that differed in the timing and order of chemo, AKTi and combination therapy across a 16-day period (Fig. S1, Materials and Methods). The expected treatment responses are summarized in Fig. 2C (red bars). One application of chemo decreased the tumor cell
population by 30-65% (#2) and two applications reduced the population by 50-90% (#3). One application of AKTi had limited impact on tumor cell growth (approximately 20% reduction from #1 to #4). Continuous application of the AKTi reduced the tumor cell population size by 40-70% (#5). The M257 melanoma cell line was more sensitive to both chemo and AKTi than WM3918 melanoma cells. Combination therapies were substantially more effective than mono-therapies. In general, concurrent therapies with chemo and AKTi (#6 and #7) were more successful than all sequential therapies (#8-#12). Concurrent therapy #6 reduced the tumor cell population size by up to 90%, and concurrent therapy #7 nearly eradicated all of the tumor cells (Fig. 2C, #7, nearly invisible red bars). Sequential therapy decreased the tumor cell population size by 50-90% (Fig 2C #8-#12).

To validate these predictions, an extensive series of in vitro experiments were performed and the numbers of viable tumor cells were quantified on day 16 (Fig. S1B) using the Matlab Image Analysis toolbox. We then compared the total experimental melanoma cell numbers with those predicted by the models (Fig. 2C, blue vs. red bars). In general, the predictions matched well with the experimental results, as all predicted values (red bars) were within one standard error deviation from the mean value of the experimental results (blue bars). Thus, this mathematical model accurately describes and predicts treatment outcomes obtained in vitro.

**Long-term response of treatments**

Having established a successfully validated model, the longer-term effects of the therapies were assessed. Surprisingly, the best proposed strategy (#7) failed by day 40 (WM3918 cells) or day 50 (M257 cells), where the physiological autophagy phenotype developed
resistance to the therapy population (green lines, Fig. S2). This finding highlights a key shortcoming of in vitro experiments; i.e., the limited timescale. To test this prediction long-term cell culture studies were performed. Perhaps unsurprisingly, as the model predicted, a 30-day treatment of strategy (#7) failed to eradicate some of the melanoma cell lines in colony formation assay experiments (16).

**Phase I trial: virtual cohort generation**

Under the assumption that our underlying model mechanism is relevant to the clinic, and there is some evidence to support this (25), it was important to advance such analyses beyond homogeneous cell lines to the heterogeneous patient population. More specifically, in order to predict long-term treatment responses in a more clinically relevant scenario, treatments for model parameters that are more representative of real patients were simulated. The same treatment schedules as in the clinical trial (10) were used, with five cycles of first-day chemo in a 21-day cycle, and two different treatment arms of AKTi schedules (Q3W, QOD). In the first AKTi schedule (arm 1: Q3W), the drug is administered on the first day of the 21-day cycle for five cycles, and thereafter is given on the first day of every week (weekly maintenance therapy). In the second schedule (arm 2: QOD), the drug is administered on days 1, 3, 5 and 7 of the 21-day cycle, and is then given weekly as maintenance therapy.

To generate virtual patient cohorts that exhibit the diversity of responses observed in the clinic, adaptive heuristic search Gentetic Algorithms (GA, built in Matlab) were used, which are based on the evolutionary principle of natural selection (26, 27). A solution \( P = [g_N, g_p, d_Q, d_t, r_p, r_N, b_p, c_p, c_Q, a_N, c_N] \) was searched that minimized our objective
function, \( F(P) = \frac{2}{\sqrt{V(P) - V_T^2}} \), using the difference between tumor volume with a parameter \( V(P) \) and the target tumor volume \( V_T \). The \( V_T \) was randomly selected from three categories \( (V_C, V_P, V_S) \) based on response criteria (28), where subscript \( C \) denotes complete response (CR; tumor diameter < 1 mm), subscript \( P \) denotes partial response (PR; at least 30% reduction in tumor diameter) and subscript \( S \) denotes stable disease (SD; up to 20% increase in tumor diameter). Our GA found 1293 sets of parameters in the case of arm 1 \((P_1)\) and found 2098 sets of parameters for arm 2 \((P_2)\).

**Phase i trial: Stratifying treatment outcomes via clinically measurable parameters**

To characterize this virtual cohort, it was first divided into four sub-cohorts \((C_1-C_4, \text{Fig. 3A(a)})\) according to the clinically measurable variables \( c_N \), chemo-sensitivity (29, 30), and \( a_N \), autophagy marker staining (31, 32). The hope being that this division might stratify best and worst responders. We compared a distribution of best tumor volume change responses of the 24 patients in the trial with that of 500 virtual patients sampled from our virtual cohort (3391 virtual patients) (Fig. 3A(b)). To test if two distributions are from the same continuous distribution, we performed a two-sample Kolmogorov-Smirnov test (Matlab statistics toolbox) (33). The test determined that we can not reject the null hypothesis at 5% significance (\( H = 0, P > 0.05, \text{test statistic} = 0.14 \)). In addition, empirical cumulative distribution functions of the two overlap each other (Fig. 3A(b)). This implies that the best tumor volume responses of these 500 virtual patients can recapitulate real patients’ tumor volume response well. To validate the agreement further, we used Lin’s concordance correlation coefficient \((\rho)\) (34, 35). We repeatedly sampled 24 virtual patients with an approximated probability density function of best tumor volume changes of real
patients (Fig.1A) 1000 times. For each sample, we calculated ρ of two measurements, best tumor volume changes of both real patients and the sample, using an R package (epiR)(36) (Fig. S3). The resulting distribution of ρ shows that the two measurements are highly concordant (Fig. S3, ρ > 0.8).

The native doubling time (i.e., without any treatment) of each sub-cohort (C₁-C₄) in each patient group (P₁ and P₂) was compared assuming exponential tumor growth, which is reasonable for metastatic disease, and the exponent of the best-fit curve was determined. Doubling times were in the range of 7 to 110 days (Fig. 3A(c) top P₁, Fig. 3A(c) bottom for P₂), which were similar to values observed in patients with cutaneous melanoma (37). Overall, tumors in the P₂ group grew much faster than those in P₁ (mean of ~30 days vs. mean of ~60 days, respectively). In P₁, tumors in C₁ (dark blue) and C₂ (dark green) that had slightly increased autophagy following AKT inhibition treatment grew faster than those in C₃ (orange) and C₄ (pink) that had highly increased levels of autophagy (50 days vs. 70 days). In contrast, there were no significant differences in the doubling times between the sub-cohorts in P₂.

Phase i combination therapy was simulated for 6 months with the two arms to predict treatment responses in the virtual cohorts. Patients in P₁ treated with arm 1 had diverse responses to the therapy, where CR, PR and SD were observed in 30 randomly selected subjects (Fig. 3B(a), waterfall plot). For example, some patients in C₁ were expected to be complete responders (CR, dark blue bars of nearly -100%), while others in the same cohort were expected to be in SD (dark blue bars of 40-60%). When comparing the expected tumor volume changes in each cohort (Fig 3B(a), middle boxplot), there were no significant differences in outcomes between C₁ and C₂ or between C₃ and C₄. However,
the $C_2$ and $C_3$ cohorts showed a significant difference ($P < 0.01$, Student’s $t$-test). Thus, one of the parameters, specifically the physiological autophagy phenotype ($a_N$), defines outcome. The histogram of all subjects in each cohort also showed a shift in treatment responses from the cohort $C_{1-2}$ (skewed toward responsive) to $C_{3-4}$ (uniformly distributed tumor volumes).

Similarly, subjects in $P_2$ treated with arm 2 also showed diverse responses to therapy (Fig. 3B(b)). However, unlike subjects in $P_1$ (Fig. 3B(a)), none of the metrics determined outcomes of subjects in $P_2$, as the mean tumor volume responses in the four cohorts did not show significant differences (Fig. 3B(b), boxplot). Accordingly, the histograms only showed a slight shift of responses when $C_{1-3}$ was compared to $C_4$ (Fig. 3B(b)).

We also randomly assigned a treatment arm (either arm 1 or arm 2) to all virtual patients in both $P_1$ and $P_2$. Tumor volume was checked at the beginning of each cycle (every 21 days), and subjects were removed from treatment if the tumor volume had more than doubled; this resulted in the removal of a total of 1473 subjects. Random assignment of the treatment arms produced even greater variations in expected outcomes (Fig. 3B(c)), but might more accurately reflect how an actual population responds. Specifically, the expected tumor volume changes showed a large variation, where the 9-99% bar in the boxplot increased in all sub-cohorts, and in both arms. The physiological autophagy phenotype ($a_N$) distinguished outcomes between $C_2$ and $C_3$ only when patients were treated with arm 2 (Fig. 3B(c), boxplot, $P < 0.05$). There was no shift in the distribution of responses between the cohorts (Fig. 3B(c), histograms). Interestingly, the outcomes were almost uniformly distributed in patients treated with arm 1, while the distributions of
patients treated with arm 2 were skewed toward smaller final tumor volumes (more responsive to the therapy). Thus, the physiological autophagy phenotype defines outcomes in diverse virtual cohorts.

**Phase i trial: Assessing stratification factors by sensitivity analysis**

Rather than focusing solely on the clinically quantifiable parameters, the nine remaining model parameters were also assessed to identify sub-cohorts that are most or least likely to benefit from the combination therapy. To identify the key parameters a sensitivity analysis of the effect of each parameter on tumor volume after 6 months of treatment was performed. After dividing the patient group into CR, PR, and SD (based on their tumor volume at 6 months), each parameter value from each group was compared and the Student’s t-test was used to determine if the mean values of a parameter differed between two groups (CR vs. PR and PR vs. SD) (Fig. S4-S6). In patients in P1, the two autophagy-associated phenotypes, physiological and quiescent ($a_N, b_P$), were significantly different between CR and PR and between PR and SD (Fig. S4). Compared with the previous partition (Fig. 3A), the new partitioning of P1 according to the value of $a_N$ and $b_P$ (Fig. 4A) discriminated the expected treatment outcomes more clearly. Unlike the previous partition result (Fig. 3B(a)), each sub-cohort ($C_{1-4}$) now showed significantly different mean response to therapy (Fig. 4A, boxplot). The new sub-cohort $C_1$ (cyan) is most likely to benefit from the treatment, while the likelihood decreased gradually in $C_2$ (blue), $C_3$ (yellow), and $C_4$ (red). There is also a clear shift in the distribution of treatment response from $C_1$ to $C_4$ (Fig. 4A, waterfall plot).
Similarly, our sensitivity analysis on P_2 (Fig. S5) revealed another key parameter set \((g_N, g_P)\), the growth rates of both the non-autophagy and physiological autophagy phenotypes. P_2 was divided based on the parameter values (C_1-C_4) (Fig. 4B, table). Unlike the previous partitioning (Fig. 3B(b)), these parameters successfully segregated patients according to the expected outcomes (Fig. 4B, boxplot). C_1 was revealed as the best responding sub-cohort, where almost all tumor volumes in this group (99%) were reduced by at least 20% (Fig. 4B, cyan boxplot). The next best responders were both C_2 and C_3, where more than 75% of the cohorts showed at least a 30% reduction in tumor volume; the expected outcomes in C_2 and C_3 significantly differed from those in C_1 (P < 0.01). The expected outcomes in C_4 were slightly worse than those in C_1.C_3, as the mean outcome was worse with some tumors from C_4 having an increased tumor size of up to \(\sim 70\%\) (Fig. 4B, red boxplot). The waterfall plots in Fig. 4B show inter-patient variation in tumor volume changes even within the same sub-cohort and shifting of the treatment response from C_1 to C_4.

With random treatment assignment of either arm 1 or arm 2 to all patients in both P_1 and P_2, as would be done in a real trial, our analysis identified the key parameters \(g_N\) and \(a_N\) as potential predictive factors of the treatment outcomes (Fig. S6). The new cohorts (C_1*-C_4*, Table in Fig. 4C) exhibit significantly different mean responses to therapy (Fig. 4C, boxplots). The new partition also showed a tendency of increasing tumor volumes from C_1* to C_4* in both arms (Fig. 4C, boxplots and waterfall plots), and defined the most sensitive sub-cohort (C_1*), who are predicted to be the most likely to benefit from treatment using either arm 1 or arm 2. In summary, sensitivity analysis allows one to select potential
predictive factors for each treatment strategy, which could be used as a guide for selecting specific therapies for a given patient.

**Phase i trial: Optimizing AKTi treatment to minimize toxicity for each sub-cohort**

For the new virtual sub-cohorts (C_{i^*}-C_{4^*}) optimal therapy recommendations were derived using implicit filtering (38). Notably, the schedule of chemo was fixed, as it was in the clinical trial (10), with the goals of identifying the AKTi schedule that reduced the initial tumor volume by at least 30% after 6 months of therapy, and that used as few AKTi applications as possible to provide an effective and less toxic treatment strategy. Optimized schedules of AKTi are summarized in Table 1. For the patients in C_{1^*}, optimum therapy recommended 1 day of AKTi treatment on the first day of the 42-day cycle, a treatment holiday for five cycles and then from day 168, 1 day of treatment on the first day of a 7-day cycle (weekly maintenance). For the patients in C_{2^*}, the optimal schedule was to administer AKTi on the first and third days of a 21-day cycle for five cycles, followed by weekly maintenance. For the patients in C_{3^*}, optimization recommended that AKTi be taken on the first, third, and fifth days of each 19-day cycle for five cycles, followed by administration on the first day of each week from day 95. The optimal schedule for cohort C_{4^*} is to administer AKTi on the first, third, and fifth days of each 19-day cycle for five cycles, followed by administration on the first and third days of a 9-day cycle from day 96.

To understand the relative impact of these alternate therapies we compared the 2-year survival probability of patients on the different therapies. The therapies included optimized therapy, treatment arm 1 and arm 2, and two mono-therapies of AKTi only (i.e., AKTi treatment only from either arm 1 or arm 2), and chemo (Fig. 5). The initial number of
tumor cells was set at one billion and the melanoma was considered fatal when the number of tumor cells reached \(10^{13}\) cells. We also compared the cumulative drug concentration of each therapy to determine the toxicity of the treatment at two time points, immediately after the five-cycles of combination therapy of AKTi with chemo (105 days) and at the completion of therapy (2 years) (see Materials and Methods for calculations of plasma concentration).

As expected, the probability of 2-year survival decreased after 6 months if the patients in the cohort \(C_1^*\) were not treated with any therapy (Fig. 5A, black line). Survival of the chemo-alone \(C_1^*\) cohort had only minimal improvement (Fig. 5A, yellow line). In contrast if the \(C_1^*\) patients were treated with any type of AKTi, their probability for 2 year survival remained over 0.9 (Fig. 5A, red, pink, blue, cyan and green lines), which was expected as this cohort is the most sensitive (Fig. 4C, cyan boxplots, tumor volume at 6 months < -60%). Regarding toxicity, the optimal therapy was the least toxic to patients, as the cumulative drug concentration was minimal (Fig. 5A, green bars), except the \(C_1^*\) chemo cohort (Fig. 5A, nearly invisible yellow bar).

The probability of 2-year survival of patients in cohort \(C_2^*\) also decreased after 6 months if patients were not treated with any therapy (Fig. 5B, black line) and chemo again slightly increased the probability of survival (Fig. 5B, yellow line). Also, like the cohort \(C_1^*\), the probability of 2-year survival was relatively high (> 0.9) when patients were treated with any of the AKTi schedules (Fig. 5B). The combination AKTi with chemo and the optimized therapy slightly increased survival probability (Fig. 5B, cyan, blue, and green lines). Regarding toxicity, arm 2 (cyan) was the most toxic, followed by AKTi (QOD, pink), the optimized therapy (green bar), and arm 1 (blue bar), at both days 105 and 720 (2
years) (Fig. 5B bar graphs). Interestingly, the most optimized therapy is substantially less toxic than both arm 2 and AKTi (QOD) at day 105.

For patient cohort C3*, the survival probability decreased rapidly to zero by 6 months if the patients were untreated (Fig. 5C, black line) and chemo again had little-to-no. impact on survival (Fig. 5C, yellow line). The AKTi monotherapies and treatment arm 1 significantly improved patient survival (Fig. 5C, AKTi: pink and red lines and arm 1: blue line). However, the most optimized therapy and arm 2 clearly provided the best probability for survival, and again the optimized therapy was less toxic than arm 2 (Fig. 5C, green vs. cyan bars).

Finally, like the C3* cohort, the probability of survival of C4* patients decreased sharply if they were untreated or treated with chemo only (Fig. 5D, black and yellow line), and again the AKTi monotherapies improved survival (Fig. 5D, red line (Q3W), and pink line (QOD)). Both treatment arm 1 and arm 2 also increased the probability of survival (Fig. 5D, blue line: arm 1 and cyan line: arm 2). Notably, the optimized therapy significantly improved the probability of survival (Fig. 5D, green line) compared to arm 2 (P < 0.05), and was also less toxic than arm 2 at day 105 right after the five cycles of combination of chemo with AKTi, although it became more toxic at year 2 (Fig. 5D bar graphs).
Discussion

The integrated approach applied herein shows that treatment-induced autophagy phenotypes is certainly one factor driving the long-term effects of treating patients with chemo in combination with AKTi. The mathematical model hypothesizes that two distinct states of autophagy exists (physiological and quiescent states), and indicates that improved patient outcomes are associated with the quiescent autophagy phenotype. The model also predicts that therapy drives the transition from the non-autophagy to the physiological autophagy phenotype, which provides a transient escape route from treatments. In contrast, the model indicates that a persistent quiescent autophagy state is detrimental to overall fitness and thus this represents a desired outcome of therapy.

Implementing a phase I trial allows one to translate models to a clinically relevant setting. The key components of such a trial are an experimentally calibrated mathematical model and a cohort of virtual patients that mirror responses observed in an actual clinical trial. When developing mathematical models to facilitate clinical decisions, an important constraint is the number of measurable parameters of the patient. As patient data are generally limiting, this inevitably leads to simpler models, where the data dictate model inputs and consequently, model outputs. The model presented herein is an excellent example, as it is constructed by integrating experimental findings for a given cancer (e.g., melanoma) with the clinical reality. An extensive cohort having widely distributed parameters is another key element of the phase I trial, and the cohort should be representative of inter-patient variability, which drives the diversity of the response (i.e., the spectrum of the response and resistance to a given therapy) that is observed in the clinic. Using a GA and employing response criteria used in the clinic, one can easily
generate a relatively large cohort of diverse virtual patients who are treated using the same treatments given to patients in a clinical trial and statistically reproduce the same responses.

To stratify treatment outcomes according to clinically measurable variables, the cohort was divided based on chemo-sensitivity and the induction of autophagy in tumor samples. The rate of transition to the physiological autophagy phenotype was a predictive factor of treatment outcome for arm 1, where higher rates of physiological autophagy resulted in unfavorable outcomes. Interestingly in another melanoma study using different treatments, an increased autophagy response was associated with resistance to BRAF inhibitors (25). In treatment arm 2, neither of the two variables selected for more sensitive or resistant individuals. However, after randomly assigning treatment of either arm 1 or arm 2 to each virtual patient, the autophagy phenotype again discriminated sensitive vs. non-sensitive sub-cohorts. Interestingly, some of the good responders to arm 2 became non-responders when their treatment was switched to arm 1 (Fig. 3B(c), 100% dark blue bars on the far left), highlighting the importance of knowing the most appropriate patients to be assigned to each treatment arm.

Sensitivity analysis of the simulated cohort was superior at defining predictive factors in each treatment arm, which discriminated between CR, PR and SD. The ability of non-autophagic melanoma cells to become either physiological or quiescent autophagic determined patient outcomes for arm 1, whereas the growth rates of proliferating tumor cells (non-autophagy vs. autophagy phenotypes) were the determinants of outcomes for arm 2. Further, when randomly assigning to either arm 1 or arm 2 the transition to the quiescent autophagy phenotype and the growth rate of non-autophagy cells discriminated
outcomes. Thus, key parameters for cases having more or less favorable outcomes can be defined for each treatment schedule, demonstrating the utility of phase $i$ trials in aiding patient selection.

Optimizing the AKTi schedule for each cohort provided the most benefit. Notably, mathematically informed drug scheduling can positively impact overall outcome, including using a lower drug dose in some cohorts. Indeed, changing the temporal protocol influenced the dynamics of the system significantly. Interestingly, another melanoma study showed that using unconventional (discontinuous) dosing schedules of melanoma cells with $BRAF$ inhibitors could prevent resistance (39). This idea is now being explored in a phase II clinical trial of $BRAF$-mutant melanoma patients (SWOG: 1320). We submit that the simulation of optimized schedules and comparing outcomes across virtual patients can assist clinical treatment planning to improve overall outcomes (10).

The underlining mechanisms, parameterization and validation of our model were based on data from a preclinical in vitro study. However, as demonstrated Leder and colleagues an integrated approach can be also achieved using in vivo preclinical studies (40). To bridge the divide between our in vitro study and the clinic the assumption was made that the same mechanisms of therapy resistance apply. Although there are a multitude of potential resistance mechanisms in patients, we consider one (autophagy) that we characterized using our integrated approach of mathematical modeling with in vitro experiments. We also assume that the variability in patients' responses to treatment can be characterized by variability in this autophagy mechanism, although there are certainly more sources of variability including but not limited to the variation in patient age, size and the genetic composition of an individual tumor, and immune responses.
Whilst it would certainly be possible to incorporate both additional resistance mechanisms and sources of variability into our model, and given appropriate experimental controls to calibrate and validate our model, ultimately the methodology would be the same, albeit with many more parameters to generate virtual cohorts. What is clear, regardless of the model complexity or cancer system, is that using a validated mathematical model (with pre-clinical data) to generate a virtual patient cohort (that matches the distribution of clinically observed outcomes) will allow us to carry out phase I trials that can be broadly applied to improve the safety and efficacy of future phase I-IV trials, as well as patient outcomes.
Materials and Methods

Mathematical modeling

Untreated melanoma cells proliferate (rate: $g_N$), and following treatment can acquire either a physiological autophagy phenotype (transition rate: $a_p$) or a quiescent autophagy phenotype (transition rate: $b_Q$). Physiological autophagy cells grow (rate: $g_P$) and can revert to non-autophagy cells (returning rate: $r_P$), or enter a quiescent/senescent state (rate: $q_P$). Tumor cells having the quiescent autophagy phenotype do not divide, yet such these cells can either reacquire a physiological autophagy phenotype (rate: $r_Q$) or a non-autophagy phenotype (rate: $r_N$) state. Cells in each compartment die at some rate ($d_{N,P,Q}$). To model increased cell deaths on days 6-9 (Fig. 1B(b)), we included the delayed cell deaths of quiescent/senescent autophagy cells ($\tau$).

The effects of chemo, AKTi and their combination (Fig. 2A(b)-(d)) were incorporated into the model. It was assumed that the drug reaches its maximum concentration immediately after administration and remains at that level until the beginning of the treatment break. Although the chemotherapeutic agents (paclitaxel and carboplatin) are detectable in patients for 24 hours, the half-life in serum is relatively short, in the range of 5.6 – 11.1 hr (41, 42); we assumed that the concentration of the chemotherapeutic agents were maintained for only 1 day after administration and became zero at the beginning of the treatment break. As the plasma concentration of AKTi (MK2206) is known to be constant for approximately 48 hr (with a long terminal elimination half-life of 40-100 hr) (43), we assumed that a 1-day application of AKTi to cells or patients corresponds to a 2-day application to cells or patients in silico. Notably, drug doses were not modulated in this study, where a fixed dose was assumed for both chemo and AKTi. As cell culture experiments showed that chemo triggered cell death with negligible effects on autophagy (Fig. 1B(a)), it was assumed that chemo only augmented cell death. Further, as chemo is effective only in proliferating melanoma populations, we assumed that the therapy increases the death rate of the two proliferating phenotypes, non-autophagy ($d_N$) and physiological autophagy cells ($d_P$)(Fig. 2B(b),
black arrows). We also assumed that the frequency with which cells became quiescent/senescent \( (q_P) \) increased with chemo (Fig. 2B(b), black lines). \textit{In vitro} studies showed that while AKTi did not augment cell deaths or effectively inhibit melanoma cell growth (Fig. 1B(a)-(b) and (16)), it did induce autophagy (Fig. 1B(c) and (16)); thus, we assumed that AKTi increases the rate of transitioning to the autophagy phenotypes, \( a_P \) and \( b_Q \) (Fig. 2B(c), black arrows). As combination therapy does not augment cell death compared with chemo, nor significantly increase autophagy relative to AKTi, the combination of the two treatments was modeled by adding the effects of chemo and AKTi (Fig. 2B(d), black arrows and crosses). Finally, it was assumed that no cells with a given phenotype revert to their original states while any treatment is being applied. The schematic representation of this compartment model (Fig. 2A(a) to (d)) converts readily into a system of ordinary differential equations:

\[
\begin{align*}
\dot{N} &= (g_N - d_N)N - (a_P + b_Q)N + [1 - A(t)][r_P P + (1 - C(t)) r_N Q] \\
\dot{P} &= (g_P - d_P)P - q_P P + a_P N + [1 - A(t)][-r_P P + (1 - C(t)) r_Q Q] \\
\dot{Q} &= -\left(\frac{d_Q}{1 + e^{-t_1 - t}}\right)Q + b_Q N + q_P P - [(1 - A(t))(1 - C(t))](r_N + r_Q)Q
\end{align*}
\]

where \( d_N = d_0 + c_N C(t) \), \( d_P = d_0 + c_P C(t), q_P = q_0 + c_q C(t), a_P = a_0 + a_N A(t) \), and \( b_Q = b_0 + b_P A(t) \). In equation (1), \( A(t) \) and \( C(t) \) model time schedules of AKTi and chemo, respectively. To model the treatment schedules, we used Heaviside function \( H(t - \theta) \) defined by

\[
H(t - \theta) = \begin{cases} 
0 & t < \theta, \\
1 & t \geq \theta.
\end{cases}
\]

Assuming alternative application of the AKTi over a period of time at each cycle, the schedule of AKTi was modeled by \( A(t) = \sum_{k=0}^{n_a} \sum_{i=0}^{n_a - 1} \left(H(t - (kt_i + 2i)) - H(t - (kt_i + 2(i + 1)))\right) \), where \( n \) is the number of AKTi applications at each cycle, \( n_a \) is the number of AKTi treatment cycles, and \( t_i \) is the length of each AKTi treatment cycle. Similarly, the schedule of chemo was modeled by \( C(t) = \sum_{k=0}^{n_c} \left(H(t - kt_m) - H(t - (kt_m + t_C))\right) \), where \( n_c \) is the number of chemo cycles, \( t_m \) is the length of
each chemo-cycle, and $t_c$ is the duration of chemo. The equation (1) was solved using a Matlab ODE solver (ode15s).

**Parameter estimation**

Two melanoma cell lines (M257 and WM3918) were treated with chemo on the first four days (day 0-4) and with AKTi on every other day (days 0, 2, 4, and 6). We measured the number of melanoma cells at days 4, 6 and 8. We assumed that all of the initial tumor cell population was the non-autophagy phenotype (100% of non-autophagy cells on day 0). Both initial cell populations and the growth rate of non-autophagy cells ($g_N$) are estimated by assuming an exponential growth of untreated cells and finding both the initial value and exponent of the best-fit curve. We used an optimization algorithm called implicit filtering (38), a steepest descent algorithm for problems with bound constraint, to determine the best remaining parameter set $H$ (except $g_N$) that minimized the difference between predicted number of cells ($N_p$) and experimental result ($N_E$) in four conditions: no treatment ($n$); chemo ($c$); AKTi ($a$); and combination ($m$). The mathematical definition of our problem is:

$$\min_{H \in \Omega} f(H) = \min_{H \in \Omega} \sqrt{\sum_{t \in \{n,c,a,m\}} (N_{p_t}(H) - N_{E_t})^2},$$

where the goal is to minimize the objective function $f$ subject to the condition that $H \in \mathbb{R}^N$ is in the feasible region:

$$\Omega = \{H \in \mathbb{R}^N | L_j \leq H_j \leq U_j \},$$

where and $L_j$ and $U_j$ are the upper and lower bound on the $j$th component $H_j$ of the vector $H$. The estimated parameters for each cell line are summarized in Table S1.

**Synopsis of 12 different schedules over 16 days tested to validate the model**

The schedules (Fig. S1) included: #1, no-treatment; #2, two types of mono-therapies with chemo
only (one time chemo for the first four days, days 0-4); #3, two chemos for both the first four days (days 0-4) and the last four days (days 12-16); #4, AKTi mono-therapy (one time AKTi for the first four days (days 0-4), #5: AKTi mono-therapy, alternative day administration of AKTi.

We considered both concurrent and sequential combination therapies. The two concurrent combination therapy schedules are #6 and #7, where #6 was one time treatment of concurrent therapy for the first four days (day 0-4), and where #7 was one time treatment of chemo for the first 4 days (days 0-4) and alternative administration of AKTi.

The four single agent sequential therapy schedules (#8-#12) included different ordering of chemo and AKTi. Some schedules set chemo treatment first, where #8 was chemo from day 0 to day 4 and then AKTi from day 0 to day 4, whereas #9 was chemo on day 0-4 and then alternating administration of AKTi. The other schedule administrated AKTi first, where #10 was AKTi first for day 0-4 and then chemo day 0-4. Finally, there were alternative applications of chemo and AKTi twice, where #11 was chemo first for the first four days, followed by AKTi treatment for 4 days, and where #12 was AKTi for the first four days, followed by 4-day application of chemo.

**Optimization of AKTi schedules**

In the model AKTi was initially administered with chemo for five cycles and then administered without chemo (AKTi maintenance), as in the clinical trial. For each AKTi application, we assumed a 1-day application time. The scheduling parameter $S$ consists of 5 variables, number of 1-day applications ($N_c$) at each cycle with chemo, length of treatment holiday at each cycle ($L_c$), starting day of AKTi maintenance ($M_s$), number of applications ($N_s$) in AKTi maintenance phase and the length of treatment holiday ($L_s$) each week since the stating day $A_s$. Our objective function to identify an optimal schedule of the AKTi is $f_k(S) = \sqrt{\sum_{i \in \mathbb{C}_k}(V_i(S) - 0.7V_0)^2}$, where $k = 1,2,3,4$ denotes each cohort $C_{1-4}$ and $V_0$ is the initial number of tumor cells ($10^9$ cells). We employed the implicit filtering method to find the optimal $S$ for each cohort.
Toxicity treatment: cumulative drug concentration of AKTi and chemo

The plasma concentration of AKTi was determined by solving a differential equation \( \frac{dx}{dt} = -\lambda X(t) + A(t) \), where \( \lambda \) is a decay rate of AKTi and \( A(t) \) (defined in the above Mathematical modeling section) denotes the application of AKTi. We assumed that the decay rate of AKTi is 0.35 per day based on pharmacokinetic study of AKTi in patients (43). Similarly, plasma concentration of chemo was obtained by solving a differential equation \( \frac{dy}{dt} = -\mu Y(t) + C(t) \), where \( \mu \) (= 0.7 per day) is a decay rate of chemo and \( C(t) \) denotes the application chemo (see Mathematical modeling section). The cumulative drug concentration at time \( T \) is obtained by adding the areas under the curve of \( X(t) \) (AKTi) and \( Y(t) \) (chemo) from 0 to \( T \).

Cell culture

Melanoma cell lines were a gift from Dr. Meenhard Herlyn (The Wistar Institute, Philadelphia, PA, USA) and were grown in RPMI-1640 media (Corning, Pittsburgh, PA, USA) supplemented with 5% FBS (Sigma, St. Louis, MO, USA). M257 cells were a gift from Dr. Antoni Ribas (UCLA, Los Angeles, CA, USA).

Statistical analysis

Matlab statistics toolbox was used to perform the Student’s \( t \)-test where no significance (ns) denotes \( > 0.05 \), ** denotes \( P < 0.05 \), and *** denotes \( P < 0.01 \).
Acknowledgments

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Conflict of interest: None.
References and Notes


**Figure Legends:**

**Figure 1.** Acquisition of historic clinical and biological data.

A, typical clinical data obtained from a clinical trial. Waterfall plots of the best responses in a clinical trial (10). The percentage change from baseline for the best result is shown here. Adapted from Molife et al (10), published in the Journal of Hematology & Oncology, copyright 2014 BioMed Central.

B, biological data that may explain the underlying mechanisms in treatment responses. (a) Assessment of cell death (WM3918 cells, annexin-V) after 72 hr treatment with chemo (carboplatin and paclitaxel), AKTi (MK2206), and the combination of chemo and AKTi. (b) The measurement of cell death (WM3918) in a panel of 3D collagen-implemented spheroids. Cells were treated with AKTi and chemo (carboplatin and paclitaxel) for 3, 6, and 9 days. Green, viable cells; red, dead cells. Magnification 10x. (c) Treatment induces autophagy in cells. Left, fluorescence imaging of WM3918 cells treated as indicated for 72 hr and stained with acridine orange (AO). Orange: aggregated AO, green: diffuse AO. Right, Quantification of staining. Adapted from Rebecca et al (16) published in Pigment Cell & Melanoma Research, copyright 2014. John Wiley & Sons.
Figure 2. Mathematical model development and validation.

A, Mathematical model development. (a) Schematic of a compartmental model composed of three compartments, non-autophagy (blue), physiological autophagy (green), and quiescent autophagy (red). (b) Schematic that incorporates the responses to chemo. Black arrows, increased rates during chemo; black crosses, the removal of the interaction during therapy. (c) AKTi increases the transition rate from non-autophagy to both autophagy phenotypes (black arrows) and blocks the transition from the autophagy to the non-autophagy phenotype (black crosses). (d) Schematic of the combination of chemo and AKTi.

B, Model calibration. Predicted non-autophagy (blue), physiological autophagy (green), quiescent autophagy (red), total population (black line), and experimental cell counts (black dots) on days 4, 6 and 8, under four conditions: no treatment; chemo (day 0-4, cyan bars), AKTi (days 0, 2, 4 and 6, pink bars) and combination therapy (chemo on days 0-4 and AKTi on days 0, 2, 4 and 6) in cell lines WM 3918 (left) and M257 (right) melanoma cells. R-values are reported for each case.

C, Validation. In a total of 12 different conditions (Fig. S1), each of the predicted total populations (red bars) are compared with of the each experimental results (blue bars).
Figure 3. Virtual cohort generation and clinical trial simulation

A, Virtual cohort generation. (a) Graphical representation of virtual patients partitioned based on the cell death rate of the non-autophagy tumor population under chemo \((c_N)\) and the induction of the autophagy from non-autophagy to physiological autophagy populations following exposure to AKTi \((a_N)\). Both rates were low in patients in sub-cohort \(C_1\) (dark blue dots). \(c_N\) was low but \(a_N\) was high in \(C_2\) (dark green). Both rates were high in patients in \(C_3\) (orange). The tumor cells in patients in \(C_4\) (pink) had a higher rate of \(a_N\) but a lower rate of \(c_N\). (b) Empirical cumulative distribution functions of patients (black line) and virtual patients (green line). The maximum difference between two distributions is 0.14. Inlet: Box-Whisker plots of patients (left) and sampled 500 virtual patients (right). x: mean, -: median, box: 25% - 75%, upper and lower horizontal bar (-): 91-99%. (c) Mean doubling time of untreated tumor volume in virtual patients from group \(P_1\) (top), \(P_2\) (bottom). Dark blue: \(C_1\); dark green, \(C_2\); orange, \(C_3\); and pink, \(C_4\).

B, Simulation of 6-month treatments in all of the virtual patients. (a) Waterfall plots of final tumor volumes in 30 randomly selected patients from \(P_1\) treated with arm 1. Box whisker plot of the expected 6-month treatment outcomes in each sub-cohort \(C_{1-4}\) (x: mean, -: median, box: 25% - 75%, upper and lower horizontal bar (-): 91-99%). **, \(P < 0.05\); ***, \(P < 0.01\). Histogram shows expected tumor volumes at the final day of treatment (day 180). (b) Waterfall plots of final tumor volume in 30 randomly selected patients from \(P_2\) treated with arm 2. Box whisker plot of the expected 6-month treatment outcomes in each sub-cohort \(C_{1-4}\) Histogram of expected tumor volumes. (c) Waterfall plots of tumor volume response in 30 randomly selected patients from both \(P_1\) and \(P_2\) treated with either arm 1 or arm 2 (randomly selected treatment). Box whisker plot of the expected 6-month treatment outcomes in each sub-cohort \(C_{1-4}\). Histogram of expected tumor volumes (day 180).
Figure 4. Potential predictive factors of the therapy to virtual patients.

A, Re-partitioning of P₁ based on the rate of autophagy induction in the transition from the non-autophagy to physiological autophagy phenotypes under AKTi (aₙ), and the rate of transition from the non-autophagy to quiescent autophagy phenotypes (bₚ). Box whisker plot of the expected 6-month treatment outcomes in the new sub-cohorts C₁-C₄ of P₁ (x: mean, -: median, box: 25%-75%, upper and lower horizontal bar (-): 91-9%). Cyan, C₁; blue, C₂; yellow, C₃; and red, C₄. **, P < 0.05; ***, P < 0.01. Waterfall plots of final tumor volumes in 40 randomly selected patients from P₁. The vertical line indicates no change in volume (0%) after therapy.

B, Re-partitioning of P₂ based on two growth rates, those of non-autophagy (gₙ) and physiological autophagy phenotype cells (gₚ). Box whisker plot of the expected 6-month treatment outcomes in the new sub-cohorts C₁-C₄ of P₂. Waterfall plots of final tumor volumes in 40 randomly selected patients from P₂.

C, Re-partitioning of all virtual patients based on the growth rate of non-autophagy tumor cells (gₙ) and the transition rate from non-autophagy to quiescent autophagy phenotype (bₚ). Box whisker plot of the expected 6-month treatment outcomes in the new sub-cohorts C₁*-C₄*. Waterfall plots of the final tumor volumes in 40 randomly selected 40 patients treated with either arm 1 or arm 2 (random assignment).
### Table A

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**Figure 5.** Treatment optimization and predicted 5-year survival analysis

Kaplan-Meier curves in patients from cohort (A: C₁*, B: C₂*, C: C₃*, D: C₄*) when eight different treatments were applied for 2 years, no treatment (black), five cycles of chemo only (yellow), AKTi monotherapy following the Q3W schedule (red), AKTi monotherapy following the QOD schedule (pink), combination therapy with arm 1 (blue) or arm 2 (cyan), and the optimum therapy (green). Inlet bars, sum of cumulative drug (both AKTi and chemo) concentrations at day 105 (first bar graph, same color scheme as in the survival curves) and year 2 (second bar graph).
Table 1. Optimized AKTi schedule for sub-cohort C1-4* (unit: day)

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<th>5 cycles of combination</th>
<th>After 5 cycles of combination (AKTi only)</th>
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<td>Cycle length</td>
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<td>C1*</td>
<td>1</td>
<td>42</td>
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<td>C2*</td>
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Supplementary Information

Phase $i$ trials in melanoma: An integrated model to translate preclinical findings to the clinic

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Supplementary Materials includes:

Supplementary Materials and Methods.
Supplementary Figures S1-S6
Supplementary Table S1.
Supplementary Materials and Methods

Supplementary Figure Legends

Figure S1. A, graphical representation of the 12 different schedules. B, representative image of cells (WM3918 and M257) on day 16 treated with the schedules. The melanoma cell lines were treated with vehicle, MK-2206 (5 μM), Carboplatin (1 μM), Paclitaxel (3 nM) or the combination of all three agents for 16 days. After this time, colonies were fixed and photographed. Photographs are representative of three independent experiments.
**Figure S2.** The long-term effects of the therapy (#7).

![Graph showing the long-term effects of the therapy](image)

**Figure S3.** Histogram of Lin’s concordance correlation coefficients and estimated densities based on 1000 samplings from the virtual cohort.

![Histogram of Lin's concordance correlation coefficients](image)
**Figure S4.** Predictive factors of treatment response arm 1 to the patient cohorts P₁. For each parameter, a Students’ *t*-test was performed to assess if there is a significant difference in the mean of each model parameter between complete responder (CR), partial responder (PR) and stable diseases (SD). Statistical significance is indicated where ns denotes > 0.05, ** denotes $P<0.05$ and *** denotes $P < 0.01$. Among 11 parameters, $b_P$ and $a_N$ discriminate CR, PR and SD in $P₁$ most significantly.

Initial diameter = 1 cm
CR: diameter < 0.1 cm
PR: diameter < 0.7 cm
SD: diameter < 1.2 cm

**p value < 0.05**
***p value < 0.01**
Figure S5. Predictive factors of treatment response arm 2 to the patient cohorts P₂. Parameter $g_N$ and $g_P$ discriminated CR, PR and SD most significantly.
Figure S6. Predictive factors of treatment response either arm 1 or arm 2 to all patients (both P₁ and P₂). Parameter $g_N$ and $b_P$ discriminated CR, PR and SD most significantly.
Table S1. Estimated parameters (unit: 1/day)

<table>
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<th>Name</th>
<th>Description</th>
<th>M257</th>
<th>WM 3918</th>
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<tr>
<td>$g_N$</td>
<td>Growth rate of non-autophagy cells ($N$)</td>
<td>0.238</td>
<td>0.198</td>
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<tr>
<td>$a_0$</td>
<td>Autophagy transition rate $N \rightarrow P$</td>
<td>0.015</td>
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<tr>
<td>$b_0$</td>
<td>Autophagy transition rate $N \rightarrow Q$</td>
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<td>0.01</td>
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<tr>
<td>$r_p$</td>
<td>Recovery rate $P \rightarrow N$</td>
<td>0.5</td>
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<tr>
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<td>Recovery rate $Q \rightarrow N$</td>
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<tr>
<td>$g_P$</td>
<td>Growth rate of physiological autophagy cells ($P$)</td>
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<td>0.195</td>
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<tr>
<td>$q_P$</td>
<td>Transition rate $P \rightarrow Q$</td>
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<td>Recovery rate $Q \rightarrow P$</td>
<td>0.09</td>
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<tr>
<td>$c_N$</td>
<td>Increased non-autophagy cell death rate under chemo</td>
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<td>Increased physiological autophagy ($P$) cell death rate under chemo</td>
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A natural death rate ($d_0$) was set to be $d_0 = 0.01$. 