A cascade of destabilizations: combining

Wolbachia and Allee effects to eradicate insect

pests

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# Summary

1. The management of insect pests has long been dominated by the use of chemical insecticides, with the aim of instantaneously killing enough individuals to limit their damage. To minimize unwanted consequences, environmentally-friendly approaches have been proposed that utilize biological control and

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take advantage of intrinsic demographic processes to reduce pest populations.

- 2. We address the feasibility of a novel pest management strategy based on the release of insects infected with *Wolbachia*, which causes cytoplasmic incompatibilities in its host population, into a population with a pre-existing Allee effect. We hypothesize that the transient decline in population size caused by a successful invasion of *Wolbachia* can bring the population below its Allee threshold and, consequently, trigger extinction.
- 3. We develop a stochastic population model that accounts for Wolbachia-induced cytoplasmic incompatibilities in addition to an Allee effect arising from mating failures at low population densities. Using our model, we identify conditions under which cytoplasmic incompatibilities and Allee effects successfully interact to drive insect pest populations toward extinction. Based on our results, we delineate control strategies based on introductions of Wolbachia-infected insects.
- 4. We extend this analysis to evaluate control strategies that implement successive introductions of two incompatible *Wolbachia* strains. Additionally, we consider methods that combine *Wolbachia* invasion with mating disruption tactics to enhance the pre-existing Allee effect.
- 5. We demonstrate that *Wolbachia*-induced cytoplasmic incompatibility and the Allee effect act independently from one another: the Allee effect does not modify the *Wolbachia*-invasion threshold, and cytoplasmic incompatibilities only have a marginal effect on the Allee threshold. However, the

interaction of these two processes can drive even large populations to extinc-

tion. The success of this method can be amplified by the introduction of

multiple Wolbachia cytotypes as well as the addition of mating disruption.

6. Our study extends the existing literature by proposing the use of Wolbachia

introductions to capitalize on pre-existing Allee effects and consequently

eradicate insect pests. More generally, it highlights the importance of tran-

sient dynamics, and the relevance of manipulating a cascade of destabiliza-

tons for pest management.

Keywords

biological control; cytoplasmic incompatibility; eradication; extinction; mating dis-

ruption; transient dynamics.

Introduction

Although most insect species provide crucial ecosystem services (Losey & Vaughan,

 $_{2}$  2006), a minority of taxa that we consider pests ( $\sim 1\%$ ) have an overwhelming

3 influence on the development of population management in theory and in practice.

4 Among the various environmentally friendly approaches that have been envisaged

5 to control unwanted species, we focus on a research avenue that proposes the

exploitation of Allee effects, i.e., the decrease in survival or reproduction at small

population sizes and the consequent reduction in population growth (Dennis, 1989;

Courchamp et al., 1999; Stephens et al., 1999; Berec et al., 2007; Liebhold & Tobin,

9 2008). The central ideas surrounding this work are twofold: management tactics

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could be combined in order to (1) reduce a population size down below the Allee threshold – the population size at which the per capita growth rate decreases (in the case of "weak" Allee effects) or becomes negative (in the case of "strong" Allee 12 effects) – which, in turn, increases the probability of stochastic extinction, and/or (2) amplify the mechanisms underpinning a pre-existing Allee effect to increase the Allee threshold itself (Tobin et al., 2011). Capitalizing on Allee effects to manage undesirable species is particularly advantageous because it drives populations into 16 extinction vortices without needing to eliminate every last individual. 17 Control methods centered on manipulating mating success as an alternative to 18 chemical pesticides have long been recognized as desirable (e.g. Knipling, 1955; 19 Baumhover et al., 1955). The application of such control methods has been con-20 sidered for managing many insect pests including the Oriental fruit fly (Steiner 21 et al., 1970), Indian meal moth and almond moths (Sower & Whitmer, 1977), and 22 Gypsy moths (Beroza & Knipling, 1972; Knipling, 1970). Importantly, mating disruption has been successfully used to control populations with pre-existing Allee effects. The Gypsy moth (Lymantria dispar), for example, is one of the few insect species for which both a component (mate-finding) and demographic Allee effect have been explicitly identified (Tobin et al., 2013, 2007; Johnson et al., 2006). The 27 Gypsy moth is an invasive forest pest in North America and triggered a major con-

tainment program to slow the spread toward the western United States (Sharov

et al., 2002a; Liebhold et al., 1992). Mating disruption has been a major tactic

used to control newly established low-density populations along the invasion front,

with evidence supporting that it is more efficient as well as economically cheaper

than classic treatments with the pesticide Bacillus thuringiensis (Sharov et al.,

2002a,b). This highlights the potential benefits of identifying other pest species

that have pre-existing Allee effects and determining whether environmentally desirable forms of control may similarly be effective. Several recent theoretical developments have focused on taking advantage of 37 Allee effects to promote pest eradication (e.g. Boukal & Berec, 2009; Liebhold & Bascompte, 2003; Blackwood et al., 2012; Yamanaka & Liebhold, 2009). These 39 models capture the underlying population dynamics of a pest and evaluate the success of population management tactics such as culling, release of sterile males, and 41 mating disruption to determine whether these methods can create or enhance pre-42 existing Allee effects (Fauvergue, 2013 provides a comprehensive review). While 43 there is evidence that such population management strategies will be successful for populations with pre-existing Allee effects, the range of species that might benefit 45 from these tactics may be much greater than currently known. In a meta-analysis focused on the presence of Allee effects in natural animal populations (Kramer 47 et al., 2009), terrestrial arthropods were found associated with the largest number 48 of studies (22) and the highest proportion (77%) exhibiting an Allee effect. Mating 49 failure at low density appeared as the most frequent mechanism. Additionally, Fauvergue (2013) found evidence supporting the presence of mate-finding Allee effects 51 in 19 out of 34 published studies that investigated the interplay of population size and mating success in insects. Indirectly, the central role of Allee effects in insect 53 population dynamics is supported by the efficiency of eradication programs based on the disruption of reproduction. Pest management based on the reduction of mating success via mass trapping, mating disruption with sex pheromones, or the

In this article, we investigate Wolbachia-induced cytoplasmic incompatibility

1955; Baumhover et al., 1955; Suckling et al., 2012, 2014; Krafsur, 1998).

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release of sterile males has indeed proved successful in several instances (Knipling,

(CI) as a novel method for triggering reproductive failures and consequently bringing a pest population below its Allee threshold. Wolbachia are endosymbiotic bacteria that infect at least 20% of all insect species and up to two thirds in some estimations (Hilgenboecker et al., 2008). Wolbachia have various effects on their insect hosts, the most widespread and prominent being cytoplasmic incompatibility (Stouthamer et al., 1999). Under CI, matings between an infected male and a female that is either uninfected or infected with an incompatible cytotype result in offspring mortality during embryonic development. Fitness advantages 67 of infected females as well as maternal inheritance are key features that promote 68 invasion of Wolbachia into a host population: above a threshold frequency, a given 69 Wolbachia strain is expected to invade until near-fixation (Barton & Turelli, 2011; 70 Hancock et al., 2011; Caspari & Watson, 1959; Hoffmann & Turelli, 1997; Turelli & 71 Hoffmann, 1991). As a result of the associated CI and subsequent reduction in reproductive rate, Wolbachia invasion via the release of infected hosts is a candidate 73 biological control agent against arthropod pests (Bourtzis, 2008). In practice, there are multiple ways to implement a management strategy cen-75 tered on inducing CIs via introduction of Wolbachia. For example, similar to the use of "Sterile Insect Technique" (SIT), males bearing a Wolbachia strain incom-77 patible with that of the target population can be released in large numbers. CIs arising from the mating of females and infected males would substantially limit 79 the total offspring in the subsequent generation, resulting in a decrease in overall population growth rate and thereby increasing the possibility of local population extinction (Laven, 1967; Zabalou et al., 2004; Atyame et al., 2015). Incompatible males can be obtained via transfection, even between completely different species 83 of host insects (e.g. Braig et al., 1994; Hoffmann et al., 2011). At the population

level, the conceptual underpinnings for mass-releases of incompatible males do not depart from that of SIT, for which interactions with the Allee effect have already been thoroughly analyzed (Boukal & Berec, 2009; Yamanaka & Liebhold, 2009; Fauvergue, 2013; Barclay & Mackauer, 1980; Barclay, 1982; Berec et al., 2016; Lewis & Van Den Driessche, 1993). An alternative management tactic using CI relies on the inoculation of a rela-90 tively small number of insects of both sexes with a Wolbachia strain incompatible with that of the target population. This method is investigated in the model introduced in Dobson et al. (2002), which combines insect population dynamics 93 with releases of individuals infected with Wolbachia. During a successful invasion of Wolbachia, a transient reduction in the insect population size occurs. This decline 95 results from the temporary increase in the fraction of incompatible matings, which peaks in the midst of the invasion process. Therefore, systematic introductions of different Wolbachia cytotypes could be applied to artificially sustain an unstable 98 coexistence of multiple incompatible infections within an insect population, allow-99 ing the population size to be reduced and maintained at low levels (Dobson et al., 100 2002). 101 Our goal is to determine when the latter implementation of Wolbachia in-102 troductions can drive a population to extinction in the presence of Allee effects. 103 Specifically, we derive a mathematical model built upon Dobson et al.'s (2002) 104 approach of CI management that additionally accounts for Allee effects as well as 105 environmental and demographic stochasticity. We also consider mating disruption 106 in our model as a potential complementary tactic. We use this model to address 107 three primary questions: (1) What is the influence of Allee effects present within 108 a host population on Wolbachia invasion dynamics? (2) What is the influence of cytoplasmic incompatibility on the demographic Allee effect? (3) What is the influence of a combination of *Wolbachia*-induced CI, Allee effects, mating disruption,
and stochasticity on the probability of host extinction?

## 13 Methods

### 114 Population model

Our model extends the framework introduced by Dobson et al. (2002) by accounting for pre-existing Allee effects, the release of pheromone sources as a method of 116 mating disruption, as well as both demographic and environmental stochasticity. In this section, we first introduce a model that considers the population dynamics 118 in the absence of individuals infected with Wolbachia. We considered populations such that the dynamics can be modeled in discrete 120 time with non-overlapping generations. The population model explicitly tracks the total population size at each time t, given by  $N_t$ . Our population model can 122 be expressed in terms of either census size or density and hereafter, we refer to 123 our model in terms of size. Therefore, while the deterministic model can take non-124 integer values, population sizes less than one are considered extinct. In contrast, 125 the stochastic model forces integer population sizes. We assume that each time 126 step can be broken into two stages: the first (at time t+0.5) captures reproduction, 127 and the second (at time t+1) captures density dependent survivorship of offspring 128 to adults. The total number of offspring is given by:

$$N_{t+0.5} = \tilde{m} F_t g_1(M_t) g_2(F_t) \tag{1}$$

where  $\tilde{m}$  is the maximum per capita female fecundity,  $F_t$  is the number of females in the population, and  $M_t$  is the number of males.  $g_1(M_t)$  captures a component Allee effect that results from the failure of mates finding one another at low densities such that:

$$g_1(M_t) = \frac{M_t}{M_t + \tilde{\theta}}. (2)$$

Here,  $\tilde{\theta}$  measures the strength of the Allee effect; a convenient interpretation of this term is that  $\tilde{\theta}$  represents the number of males at which half of the females 135 successfully find a mate or, equivalently, the maximum mating rate is reduced by 136 half (Boukal & Berec, 2009). 137 The function  $g_2(F_t)$  in Eqn. 1 captures the decline in fecundity resulting 138 from techniques to control populations via mating disruption. We assume that 139 pheromone sources are introduced into the environment and maintained in the 140 population at a fixed number  $\tilde{P}$  and only a fraction  $F_t/(F_t+\tilde{P})$  males successfully 141 find a mate (Fauvergue, 2013), or:

$$g_2(F_t) = \frac{F_t}{F_t + \tilde{P}}. (3)$$

We now assume that there is a 50:50 sex ratio (i.e.  $F_t = M_t = N_t/2$ ) and define constants  $m = \tilde{m}/2$  (which is now the overall per capita fecundity),  $\theta = 2\tilde{\theta}$ , and

 $P=2\tilde{P}$ . Now, we can write both  $g_1$  and  $g_2$  as functions of  $N_t$  and Eqn. 1 is now:

$$N_{t+0.5} = mN_t \frac{N_t}{N_t + \theta} \frac{N_t}{N_t + P}.$$
 (4)

For a simpler biological interpretation, we consider  $\theta$  relative to the carrying 143 capacity of the population in the absence of any control (denoted as K) as an 144 indicator of the intensity of the Allee effect (i.e.  $\theta/K$ ). Now, when  $\theta=K$  (or, 145 equivalently,  $\theta/K=1$ ) half of the total population successfully mates at its car-146 rying capacity. Hereafter, we refer to  $\theta/K$  as the "relative strength of the Allee 147 effect" and restrict its values to the range (0 - 0.5), with 0.5 likely on the upper end 148 of biologically reasonable values for  $\theta/K$ . Similarly, we consider P, the number of 149 pheromone sources, relative to K. 150 Finally, we assume that survivorship of offspring to adults is density dependent so 151 that: 152

$$N_{t+1} = N_{t+0.5} \, S_N \tag{5}$$

153 where

$$S_N = \frac{S_0}{1 + (\alpha N_{t+0.5})^{\gamma}} \tag{6}$$

and the constant  $\alpha$  is related to the carrying capacity (more details provided in the Supplementary Information S1),  $\gamma$  is related to intraspecific competition, and  $S_0$  is survivorship in the absence of intraspecific competition (Slatkin & Smith, 1979). Combining equations (4)-(7), we are left with the model:

$$N_{t+1} = mN_t \left(\frac{N_t}{N_t + \theta}\right) \left(\frac{N_t}{N_t + P}\right) \frac{S_0}{1 + (\alpha N_{t+0.5})^{\gamma}}.$$
 (7)

Our goal is to consider the dynamical consequences of population control methods (i.e. Wolbachia introductions and the release of pheromone sources). Therefore, we analytically determine the equilibrium values for the population model (7) in the absence of these management tactics (P=0). Throughout the remainder of the paper, we distinguish between the "maximum reproductive rate" (which is given by  $mS_0$  and therefore accounts for both fecundity and density independent survivorship) and the overall "reproductive rate" (which is the reproductive rate in the presence of all other demographic processes in our model, namely the Allee effect). As detailed in the Supplementary Information (S1), we find three equilibria (assuming the maximum reproductive rate is greater than one and setting  $\gamma=1$ ). The first equilibrium corresponds to population extinction, and the second two are given by:

$$\frac{mS_0 - 1 \pm \sqrt{(mS_0 - 1)^2 - 4\alpha m\theta}}{2\alpha m}.$$
 (8)

When Allee effects are not present ( $\theta = 0$ ) these equilibria collapse to a single equilibrium (the carrying capacity K). In contrast, for sufficiently large Allee effects these equilibria no longer exist and the reproductive rate is always less than one; consequently, the population will be driven to extinction independent of its initial size. However, when the value of  $\theta$  is between these extremes, the smaller equilibrium corresponds to the Allee threshold and the larger equilibrium

corresponds to the carrying capacity. The structure of these equilibria are integral 160 to the insect species that we are considering: there is a carrying capacity and a 161 strong Allee effect for positive values of  $\theta$  up to a threshold. We therefore conjecture 162 that an alternative form of density dependence that captures these properties will 163 yield qualitatively similar results. 164 Based on this deterministic framework, we build in environmental and demo-165 graphic stochasticity. We assume that environmental stochasticity leads to vari-166 ation in the population's fecundity between generations (Melbourne & Hastings, 167 2008). Therefore, we adapt the methods of Schoener et al. (2003) and account for 168

environmental stochasticity by rewriting Eqn. 4 as:

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$$N_{t+0.5} = m_t N_t g_1(N_t) g_2(N_t)$$
(9)

where the fecundity  $m_t$  is drawn at each generation from a normal distribution with mean m (that is truncated so that  $m \geq 0$ ) and variance  $(\sigma^2)$  that scales 171 with the mean. In the main text, we fix the variance so that it is equal to the mean; however, a sensitivity analysis of the magnitude of the variance is provided 173 in the Supplementary Information (S3). Further, we note that gamma-distributed 174 environmental stochasticity is a commonly used alternative choice; under our pa-175 rameterization, the probability density function (pdf) is nearly identical for both 176 normal- and gamma-distributed stochasticity and would therefore yield similar 177 results. 178

Demographic stochasticity results from variation in fecundity at the individual level (Melbourne & Hastings, 2008). In the absence of demographic stochasticity,

the total number of individuals that successfully reproduce is given by:

$$B = N_t g_1(N_t) g_2(N_t). (10)$$

We assume that each of these individuals at a given time t reproduces with fecundity  $m_t$  (as described above), and the total number of eggs produced is a Poisson random variable (Melbourne & Hastings, 2008). Since the sum of independent Poisson random variables is also a Poisson random variable, the total offspring of all adults is:

$$N_{t+0.5} \sim \text{Poisson}(m_t B)$$
. (11)

Finally, we include stochasticity in density dependent survivorship, again following Melbourne & Hastings (2008). Given that  $S_N$  (as defined in Eqn. 7) is the probability that offspring survive to adults, we assume that survivorship is binomially distributed so that:

$$N_{t+1} \sim \text{Binomial}\left(N_{t+0.5}, S_N\right). \tag{12}$$

#### 191 Infection dynamics

We consider the infection dynamics of up to two different cytotypes of Wolbachia (referred to as cytotypes X and Y) and denote the number of uninfected individuals

as W. Note that all variables and parameters with subscripts X (or Y) are related to cytotype X (or Y). This model is adapted from Dobson  $et\ al.\ (2002)$ ; therefore, we use similar notation throughout.

In the presence of a single cytotype of *Wolbachia*, there are only unidirectional cytoplasmic incompatibilities (CI); in contrast, in the presence of multiple cytotypes there may be bi-directional CI. We first introduce the case of a single cytotype and then extend the model to include two cytotypes. Below we describe the mathematical formulation of the infection dynamics, and Table 2 summarizes these processes.

204 One cytotype

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To capture the Wolbachia dynamics, we first determine the proportions of infected and uninfected individuals in the population at time t. For example, if there are  $W_t$  uninfected individuals and  $X_t$  infected with cytotype X then, under the assumption that there is a 50:50 sex ratio, the fraction of females infected with cytotype X at t + 0.5 is given by:

$$a_t = \frac{X_t}{W_t + X_t}.$$

Similarly, we find the fraction  $i_t$  of all males that are infected (where  $i_t = a_t$ ), the fraction  $q_t$  of all males that are uninfected, and the fraction  $c_t$  of all females that are uninfected (again  $q_t = c_t$ ).

Based on the proportions of uninfected and infected individuals in the population, we can now determine the fraction of offspring that are infected. Crosses be-

tween pairs with an infected female suffer a fecundity loss due to infection  $(1-F_X)$ ,
where  $F_X$  is the relative fecundity of infected individuals. Vertical transmission of
Wolbachia occurs maternally and we assume that transmission is successful with
probability  $(1 - \mu_X)$ , where  $\mu_X$  is the probability of transmission failure. In the
instance of Wolbachia-induced CIs, crosses between infected females and uninfected males in addition to crosses between infected males and infected females
give rise to infected offspring. The proportion of viable offspring that are infected
with cytotype X after reproduction (i.e. at time t + 0.5) is therefore given by:

$$x_{t+0.5} = a_t (1 - \mu_X) F_X (i_t + q_t)$$
(13)

where a lowercase x is used to denote proportion rather than number. Second, 223 we can identify the proportion of viable offspring that are uninfected  $(w_{t+0.5})$ . 224 Uninfected individuals can arise from crosses between both uninfected females and 225 uninfected males. Further, matings between both infected females and infected 226 males can yield viable uninfected offspring. This results from failure to vertically transmit Wolbachia to their offspring. When one type of Wolbachia is present 228 within a population, then only unidirectional cytoplasmic incompatibility (CI) is 229 possible. This type of CI occurs through matings between infected males and 230 uninfected females. Therefore, we assume that all but a fraction  $H_X$  of pairings between infected males and uninfected females undergo CI. Additionally, offspring 232 from pairings between infected males and infected females that fail to transmit Wolbachia are subject to CI-induced mortality. The proportion of viable offspring 234 that are not infected with Wolbachia following reproduction is therefore given by:

$$w_{t+0.5} = (\mu_X F_X a_t + c_t) \times (i_t H_X + q_t). \tag{14}$$

Notice that due to cytoplasmic incompatibilities and the fecundity cost due to infection with *Wolbachia*, the fraction of the offspring that are viable  $(x_{t+0.5} + w_{t+0.5})$  is less than one. Therefore, the total number of offspring as governed by Eqn. 4 can be rewritten as:

$$N_{t+0.5} = m \left( x_{t+0.5} + w_{t+0.5} \right) N_t \, g_1(N_t) \, g_2(N_t). \tag{15}$$

In other words, the product  $g_1(N_t)g_2(N_t)$  captures the total fraction of adults at time t who successfully find a mate, and the sum  $x_{t+0.5} + w_{t+0.5}$  is the fraction of all offspring that are viable. Finally, as described in the previous section, density dependent mortality limits the total number of adults at time t+1 (Eqn. 7).

Two cytotypes

In addition to releasing a single cytotype of Wolbachia, we consider a scenario in which a second cytotype is introduced. When two cytotypes of Wolbachia are present within a population, bidirectional CI occurs when a male with one cytotype mates with a female infected with an incompatible Wolbachia cytotype. Similar to the previous section, we assume that a fraction  $H_X$  (or  $H_Y$ , depending on the infection type of the male and female) of offspring survives. Offspring of pairings between infected males and females of either cytotype that fail to transmit are 253 again subject to CI-induced mortality.

Therefore, in the presence of two strains we rewrite Eqn. 13 as:

$$x_{t+0.5} = a_t (1 - \mu_X) F_X (i_t + j_t H_Y + q_t)$$
(16)

where  $j_t$  is the fraction of males infected with cytotype Y. Similarly, the proportion of viable offspring infected with cytotype Y following reproduction is given by:

$$y_{t+0.5} = b_t (1 - \mu_Y) F_Y (i_t H_X + j_t + q_t)$$
(17)

where  $b_t$  is the fraction of females infected with cytotype Y. The proportion of viable uninfected offspring is now given by:

$$w_{t+0.5} = (\mu_X F_X a_t + \mu_Y F_Y b_t + c_t) (i_t H_X + j_t H_Y + q_t). \tag{18}$$

#### 259 Parameterization

Here, we define the maximum reproductive rate as the product of the *per capita* fecundity and density independent survivorship (i.e.  $mS_0$ ). In other words, this is the reproductive rate in the absence of Allee effects and in the limit as the population size approaches zero. Our parameterization of the population model is based on both the parameterization used in Dobson *et al.* (2002) and common ranges for insect populations (see Table 1). For example, Hassell *et al.* (1976) cites

finite net rates of increase (defined as fecundity discounted by density independent mortality and therefore equivalent to  $mS_0$  here) ranging from 1.3-75 (with 22 267 of the 24 species investigated in the range 1.3 - 13.5) which is consistent with 268 our parameterization (e.g. see Fig. 2 caption and the associated results as  $mS_0$ 269 is varied). Additionally, several parameters vary for our analysis including the 270 strength of the Allee effect,  $\theta$ , and the initial population size. However, our results are intended to assess the general qualitative behavior of Wolbachia introductions 272 and consequently the actual implementation of such management tactics would 273 require a detailed analysis and parameterization specific to the target population 274 and cytotype. 275 Our parameterization for the infection dynamics is based on values that are rea-276 sonable for Wolbachia cytotypes (Hoffmann & Turelli, 1997; Dobson et al. (2002); 277 Charlat et al., 2005). In the main text, we assume that fecundity loss, trans-278 mission failure, and survival of CI are equal between all cytotypes. However, the 279 Supplementary Information (S3) provides an analysis of the dynamics when the 280 introduced cytotypes are not identical. S3 additionally provides sensitivity anal-281 yses for parameters related to the population model, including the strength of 282

## Results

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In the following sections we first test our model against well-established results related to *Wolbachia* invasion as a method of model validation, establish the relationship between *Wolbachia* and the strength of the Allee effect, and finally evaluate the potential for the release of infected insects to control a population.

environmental stochasticity and the maximum reproductive rate.

#### Model validation

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We first determine whether our model captures the same features of the important earlier work (Hoffmann et al., 1990; Turelli & Hoffmann, 1991; Hancock et al., 2011). Hoffmann et al. (1990) derived an analytic expression for the expected equilibrium infection frequencies. After adjusting their notation to match ours and simplifying, the equilibrium infection frequency (which we denote as p) for a single cytotype of Wolbachia X should satisfy the equation:

$$(1 - H_X)(1 - \mu_X F_X) p^2 + (F_X + H_X - 2) p + 1 - F_X(1 - \mu_X) = 0.$$

Their work predicts that there is an unstable equilibrium referred to as the

Wolbachia invasion threshold; cytotypes with initial infection frequencies above 297 this threshold will increase until reaching the higher stable equilibrium, indicating 298 a successful invasion. Following Charlat et al. (2005), we considered invasion dy-299 namics by estimating the infection frequency at generation t+1 as a function of 300 the frequency at generation t. Doing so allows us to create a simple graphical rep-301 resentation of the stable and unstable equilibria (Fig. 1). Unless stated otherwise, 302 the default parameter values are listed in Table 1. 303 Our simulation results are consistent with the analytically derived equilibrium 304 infection frequencies (Fig. 1). This verifies that our simulations are in line with 305 the behavior that we would like to capture from our model and are consistent with 306 the results observed in Charlat et al. (2005). This is not surprising given that our 307 model makes similar assumptions on the mechanisms driving Wolbachia invasion 308 dynamics (e.g. fecundity loss and cytoplasmic incompatibilities). In contrast to

earlier studies, our population model is dynamically different because of the inclu-310 sion of Allee effects and pheromones. Therefore, we determined the relationship 311 between the invasion threshold and these features of the model. We found that the 312 Wolbachia invasion threshold is not affected by Allee effects nor by the application 313 of pheromones to the host insect (not shown). This is important to note because 314 in all of our simulations and analyses, the invasion threshold does not vary as  $\theta$ 315 and P are adjusted. Finally, we note that the invasion threshold is not affected by 316 any of our demographic parameters (i.e.  $m, \alpha, \gamma,$  and  $S_0$ ; not shown.) 317

#### The effect of Wolbachia on the Allee threshold

To determine the dynamical effects of the presence of Wolbachia infection within a population, we find the Allee threshold in insect populations both in the presence 320 and absence of infection. In this section, we ignore stochasticity as well as the 321 release of pheromones (P=0). For a given proportion of infected individuals, we 322 calculate the reproductive rate between two consecutive generations (i.e.  $N_{t+1}/N_t$ ) 323 across all population sizes (Fig. 2). The equilibria for our population model occur 324 when  $N_{t+1} = N_t$ , and there are three equilibria for the parameters used to produce 325 this figure: the first corresponds to population extinction (stable), the second is the 326 Allee threshold (unstable), and finally the third is the carrying capacity (stable). 327 In addition to considering the population model in the absence of Wolbachia-328 infected individuals, we calculated the reproductive rates when the population is 329 comprised of 10%, 50%, and 90% infected individuals (Fig. 2). Given our pa-330 rameterization, the frequency of infected individuals is chosen to lie above the 331 invasion threshold (which is  $\sim 8.5\%$ ); therefore, this figure captures the dynamics 332

between two consecutive generations during the replacement process when the population contains the specified distribution of infected and uninfected individuals. 334 As a consequence of cytoplasmic incompatibilities, there is an increase in the Allee 335 threshold. Additionally, there is a slight decrease in the carrying capacity that 336 results from the fecundity loss associated with Wolbachia infection. Consequently, 337 the maximum reproductive rate decreases as the proportion of infected individuals 338 increases. Finally, the changes in reproductive rate are most significant during 339 the replacement process (e.g. when 50% is infected) and they diminish when the 340 infection is close to fixation (e.g. 90%). The proportion of Wolbachia-infected 341 individuals has a significantly smaller effect on the location of the Allee threshold 342 than the strength of the mate finding Allee effect itself (Fig. 2).

### Implications for population management

345 Deterministic results

In this section, we characterize implications for population management through 346 the release of Wolbachia-infected individuals into an insect population. As ob-347 served by Dobson et al. (2002), there should be a transient decline in the popu-348 lation size during the replacement of uninfected hosts by Wolbachia-infected indi-349 viduals. Therefore, we find the magnitude of this decline in the presence of Allee 350 effects to determine the conditions under which the replacement process brings 351 the population size below the Allee threshold in a deterministic setting, thereby 352 forcing extinction. This is achieved by running our model over a range of values 353 for the strength of the mate-finding Allee effect  $(\theta)$ . We assume that the initial 354 population size is at its carrying capacity (which is found analytically, as shown 355

in the Supplementary Information S1).

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We find the minimum population size (relative to K) over 50 generations fol-357 lowing the introduction of one cytotype (Fig. 3B) and two cytotypes (Fig. 3C). 358 Here, values of zero for the minimal population size indicate that the transient 359 reduction in population size brought the population below the Allee threshold, 360 therefore leading to deterministic extinction. The first cytotype is always released 361 in the second generation, and the release of the second cytotype is optimized so 362 that the release occurs in the generation that causes the largest decline in pop-363 ulation size (see Supplementary Information S2 for a detailed explanation of the 364 optimization scheme). While in the main text we assume that all cytotypes have 365 the same infection properties, this assumption is challenged in the Supplementary 366 Information (S3) and our qualitative results are unchanged. To ensure that the 367 introduction size is above the invasion threshold, in all simulations we assume that 368 the introduction is large enough so that the initial infection frequency is 10%. This 369 value lies just above the actual threshold of  $\sim 8.5\%$  associated with our parameter 370 values. Therefore, the number of infected individuals introduced in our simulations 371 directly depends on the current host population size.

To determine the success of releases under varying reproductive rates, we replicated the results for four different values of  $S_0$ . For all reproductive rates, the release of two incompatible cytotypes of *Wolbachia* is substantially more effective than a release of a single cytotype. In fact, release of a single cytotype is only effective in driving population extinction when reproductive rates are small. This observation holds more generally: the effectiveness of *Wolbachia* introductions increases as the maximum reproductive rate decreases (Fig. 3B-C).

These results suggest that CI management may fail in species with high repro-

ductive rates or alternatively in these species, complementary tactics that either 381 decrease the population size or increase the Allee threshold may be required to 382 amplify the effects of Wolbachia introductions. Therefore, we consider the use of 383 mating disruption through the release of sex pheromones (P) as a supplemental 384 management tactic (as in Eqns. (4) and (3)). We determine the minimum pop-385 ulation size following no introduction, one introduction, and the introduction of 386 two cytotypes while additionally assuming there is a fixed number of pheromone 387 sources present. These results suggest that combining both methods is significantly 388 more effective than either tactic alone (Fig. 3D-F). The associated dynamics can 389 be visualized by considering a plot of the population size with time (Fig. 4). 390

Stochastic results

391

The interplay of Allee effects and stochasticity can be especially important at low population sizes, when the population is at higher risk of stochastic extinction. Therefore, in this section we determine the ability of *Wolbachia* and mating disruption to drive populations with variable initial population sizes to extinction in the presence of Allee effects and stochasticity.

To achieve this, we determine the probability of extinction based on 500 real-397 izations of the stochastic model (i.e. Eqns. 9-12) over all relevant combinations 398 of the initial population size and strength of the Allee effect (i.e. the initial pop-399 ulation size is at most at 80% of carrying capacity and the relative Allee effect, 400  $\theta/K$  is no greater than 0.5). To determine the relative roles of environmental and 401 demographic stochasticity, we simulate the model while including both types of 402 stochasticity as well as demographic stochasticity alone. Further, we find the extinction probability under three scenarios: no introduction of Wolbachia-infected 404 individuals, introduction of one cytotype, and the introduction of two incompati-

ble cytotypes. As in the deterministic setting, we assume that the introduction of 406 the first cytotype occurs at the second generation. When two cytotypes are intro-407 duced, the generation of the second release is determined in the same way as it is 408 found in the deterministic setting: the second introduction is optimized for each 409 realization so that it occurs in the generation (up to 25 generations) that creates 410 the largest transient decrease in population size resulting from the Wolbachia in-411 troduction. The number of generations between releases increases as the strength 412 of the mate-finding Allee effect decreases (see Supplementary Information S2). As 413 before, each release is implemented so that the proportion of infected individuals 414 of a given cytotype is 10% (just above the invasion threshold). 415 Here, we consider populations with relatively high reproductive rates (max-416 imum reproductive rate 3.75); the Supplementary Information (S3) provides a 417 sensitivity analysis for lower reproductive rates. We find that the introduction of a single cytotype of Wolbachia leads to negligible increases in the extinction 419 probability across all values of the relative strength of the Allee effect (Fig. 5A-420 B). However, environmental stochasticity increases the uncertainty associated with 421 extinction near the Allee threshold, and there are more apparent increases in extinction probability for Wolbacia introductions for very strong Allee effects (Fig. 423 5D-E). As described in the previous section, the success of Wolbachia releases in-424 creases for lower reproductive rates. This finding holds in the stochastic setting 425 (see S3). 426 In contrast to a single introduction, the release of two incompatible cytotypes is 427 much more effective (Fig. 5C,F). Interestingly, when  $\theta$  is relatively high, Wolbachia introductions succeed in driving population extinction independent of the initial 429 population size. This result has the important implication that the success of Wolbachia introductions in driving extinction do not necessarily rely on having a

pest population at the initial stage, or at the front, of the invasion. Moreover, in 432 settings with high levels of environmental stochasticity, extinction is possible for 433 much smaller Allee effects than predicted by the deterministic model (Fig. 5F). 434 As explored in the deterministic framework, combining Wolbachia introduc-435 tions with other methods that increase the Allee threshold (e.g. mating disruption) will likely further increase the success of the overall management strategy. Here, 437 we perform a more global exploration of management options that combine both 438 Wolbachia introductions and pheromone releases. We again consider the popula-439 tion dynamics under three different management regimes: mating disruption only, 440 mating disruption and the introduction of one cytotype, and mating disruption 441 and the introduction of two cytotypes of Wolbachia. In this case, we assume that 442 the relative strength of the Allee effect is fixed and relatively low so that  $\theta/K$  is 0.1; under this condition, Wolbachia introductions alone do not drive the popu-444 lations to extinction in the deterministic setting (Fig. 3B-C). We again find that 445 environmental stochasticity increases the extinction probability for a smaller num-446 ber of pheromone sources and, importantly, utilizing both mating disruption and CI is much more effective than using mating disruption alone (Fig. 6). Therefore, 448 these two methods can serve as complementary tactics for pest management.

## Discussion

431

We investigated a population management strategy that considers *Wolbachia*induced cytoplasmic incompatibility in the presence of Allee effects. In particular,
we developed a stochastic population model, building upon the seminal approach

of Dobson et al. (2002) and the continuously expanding body of literature investigating the use of Allee effects for the eradication of pest species (Liebhold & Bas-455 compte, 2003; Tobin et al., 2011; Liebhold et al., 2016). Our model demonstrates 456 that the introduction of a relatively small number of incompatible individuals into 457 a pest population that has a strong pre-existing Allee effect can drive the pest 458 population to extinction with no further intervention. These methods are suc-459 cessful more broadly when multiple strains of Wolbachia are introduced. We also 460 demonstrate that extinction is possible for surprisingly large pest populations and 461 that combinations of more than one strain of Wolbachia and mating disruption via 462 sex pheromones work synergistically to increase the population's extinction risk. 463 Biological control has been studied for decades as an environmentally friendly al-464 ternative to pesticide use (e.g. Knipling, 1955; Baumhover et al., 1955; Murdoch 465 et al., 1985; Bale et al., 2008), and our study adds to this work by providing in-466 sight into ways that Wolbachia invasions can take advantage of intrinsic population 467 processes – that is, Allee effects – to manipulate and control pest populations. 468 An important first step of our modeling work was to uncover the basic inter-469 actions between Allee effects and cytoplasmic incompatibility (CI). We show that these interactions are weak or non-existent: the Wolbachia invasion threshold does 471 not depend on the strength of the Allee effect of its insect host, and the Allee threshold has only a marginal decrease in the presence of CI. Therefore, invasion 473 of a particular Wolbachia strain into a population only depends on the critical infection frequency above which invasion succeeds in a deterministic setting (Barton 475 & Turelli, 2011). This invasion threshold corresponds to a proportion of infected hosts above which infection spreads up to almost fixation, and is determined by 477 parameters such as the reduction in egg hatch-rate caused by CI, the fitness costs

of Wolbachia carriage, and the fraction of offspring that inherit the bacteria from an infected mother (Turelli, 1994). The invasion threshold found with our sim-480 ulation model is consistent with that derived analytically (Turelli & Hoffmann, 481 1991), and unaffected by the intensity of a mate-finding Allee effect. In addition 482 to adding validation to our model, this result holds interest because most theoret-483 ical approaches of Wolbachia invasion dynamics are purely genetic and consider 484 changes in infection frequency without considering host population dynamics. One 485 exception is the work of Hancock et al. (2011) which suggested that Wolbachia 486 invasion thresholds predicted analytically hold for closed populations. Our results 487 are consistent even when, as assumed here, host reproductive rate is affected by 488 both positive and negative density dependence. 489 In the presence of strong Allee effects a population below the Allee thresh-490 old will be forced to extinction in a deterministic setting, making the Allee effect 491 a central paradigm for conservation (Deredec & Courchamp, 2007; Stephens & 492 Sutherland, 1999), invasions (Taylor & Hastings, 2005), biological control intro-493 duction (Fauvergue et al., 2007, 2012), and as hypothesized in the present work, 494 eradication (Tobin et al., 2011). Whether an Allee effect is weak or strong (and the value of the Allee threshold in the latter case) depends on the strength of the un-496 derlying component Allee effect(s) relative to other density-dependent processes. Our simulations of various levels of cytoplasmic incompatibilities in a population 498 with a pre-existing mate finding Allee effect suggest that the Allee threshold is much less sensitive to variations in the frequency of Wolbachia-infected individu-500 als (0-90% infected individuals) than it is to variations in mating success (Fig. 2B). 501 Wolbachia-induced cytoplasmic incompatibility does decrease population growth 502 rate, as expected, but it has a minimal effect on the extinction threshold. Therefore, Wolbachia-induced CI may be considered a culling population management tactic where population size is temporarily decreased as a result of cytoplasmic incompatibilities.

Despite their initial apparent independence, cytoplasmic incompatibility and 507 the Allee effect yield interesting properties when acting in concert. Our first anal-508 ysis that considered the combined occurrence of Allee effects and CI in a determin-509 istic context reveals that the transient decrease in population size is large enough 510 to trigger extinction when the reproductive rate of the host species is relatively 511 low. Extinction caused by the introduction of a single Wolbachia cytotype in 512 populations with higher reproductive rates is only observed for very strong Allee 513 effects (Fig. 3A). However, the strength of the Allee effect required for extinction 514 lowers with the introduction of an additional incompatible Wolbachia strain. The 515 resulting insect extinction probability, estimated by simulating the model in the presence of stochasticity, confirmed the interaction between the two processes. In 517 the absence of Wolbachia, we determined the population's extinction probability 518 as it varies with its population size and the strength of the component Allee ef-519 fect (Fig 5A and 5D). Introducing infected individuals results in the extinction of populations that would have persisted otherwise (i.e., a population that is above 521 its Allee threshold can be brought to extinction). Introducing a second incompat-522 ible cytotype of Wolbachia increases CIs within the population and, consequently, 523 increases the extinction domain by reducing the severity of Allee effect necessary to trigger extinction (Fig 5). 525

Nonetheless, our model predicts that although Allee effects and CI combine to drive populations to extinction – even surprisingly large populations – these extinctions may occur for unrealistically severe Allee effects. For instance, after

the introduction of two incompatible Wolbachia strains into a population with a 529 maximum reproductive rate of 3.75, extinction is expected when  $\theta/K$  exceeds 0.25 530 (Fig. 5C-F); that is, extinction occurs if only 25% of all females successfully mate 531 when the population is at 50% of the carrying capacity. Field estimations of mate-532 finding Allee effects in insects are rare, but it is probable that mating failures only 533 occur at low densities. For instance, in the Gypsy moth Lymantria dispar, mating 534 failures occurred below a density of  $\sim 4$  (estimated via the rate of male captures 535 on sex-pheromone traps) whereas the carrying capacity was estimated similarly 536 around 800 (Tobin et al., 2007, 2013), so that estimation of  $\theta/K$  in this species 537 could be one or two orders of magnitude lower than that yielding extinction in our 538 model. 539

Our simulations demonstrate that eradication is much more likely if the intro-540 duction of Wolbachia-infected individuals is combined with mating disruption via the release of sex pheromone sources (Fig. 6). Interestingly, eradication is not 542 restricted to small populations, but also applies to populations that have reached 543 carrying capacity. Moreover, our results suggest that the two tactics act synergis-544 tically: the decrease in population size obtained when CI and mating disruption are combined is higher than the cumulative decrease obtained with each tactic 546 applied separately. Our model therefore supports previous studies that highlight the potential benefit of simultaneously using multiple complementary management 548 tactics (Blackwood et al., 2012; Suckling et al., 2012; Berec et al., 2016). If different tactics benefit from one another, additional methods for controlling a pest 550 population should also be considered. For example, other methods for popula-551 tion control such as parasitism or predation by native natural enemies may also 552 be complementary. Additionally, while our focus was on cytoplasmic incompatibilities, there is evidence that *Wolbachia* and other bacteria are capable of other reproductive manipulations including male-killing (Dyer, 2004; Richardson *et al.*, 2016). Similar conclusions were also made in the recent modeling study of Berec *et al.* (2016), who suggest that sterile insect technique is improved when combined with male-killing bacteria. This suggests the existence of additional avenues for utilizing *Wolbachia* in the context of pest management.

Theoretical models of population management are currently flourishing much 560 faster than empirical evidence can be obtained; therefore, it is important to dis-561 cuss the relevance of our predictions and the feasibility of our proposed methods. 562 First, we have shown that extinction in insect species with high reproductive rates 563 may not be feasible because extinction would require an unrealistic amount of sex 564 pheromone lures to successfully complement the Wolbachia-induced transient de-565 crease in population size. However, in the majority of our simulations we assigned the maximum reproductive rate a value of 3.75 or, equivalently, per capita fecun-567 dity as m=25 and density independent survivorship of larvae as  $S_0=0.15$ . This 568 value is just below the median of the reproductive rates estimated in Hassel et al. 569 (1976) across 24 different insect species. Therefore, we conjecture that these methods would still apply to a variety of pest species. Second, the reproductive rate is 571 just one of the parameters in our model. Although the main text is supplemented with sensitivity analyses, our work is not intended to provide robust quantitative 573 guidelines for a practical application of our proposed management strategies. Instead, our analysis provides general properties of the interactions between Allee 575 effects and cytoplasmic incompatibilities on the population dynamics of an insect pest species. Should our proposed management strategy be applied to a specific 577 insect pest that exhibits Allee effects, thorough investigations would be needed to better quantify parameters that dictate the strength of the processes that underpin the model, including *Wolbachia* diversity and incompatibility as well as component and demographic Allee effects.

To date, the potential use of Wolbachia-induced CI for pest management is 582 supported by a few but important studies on mosquitoes (Hoffmann et al., 2011; 583 Laven, 1967) and fruit flies (Zabalou et al., 2004). Furthermore, evidence for the 584 existence of both a component and a strong demographic Allee effect exists in 585 the Gypsy moth, which could explain the relative success of mating disruption 586 in this species (Tobin et al., 2013, 2007). Although such empirical advances are 587 indeed promising, they deserve a much stronger body of data and robust cause 588 and effect demonstrations (Fauvergue, 2013). From this perspective, our model 589 was not built as a predictive tool for a specific species. It was rather developed as 590 a heuristic theory yielding qualitative predictions which will hopefully encourage 591 future experimental approaches on the consequences of cytoplasmic incompatibility 592 and Allee effects on population extinction. 593

There is a long and prolific body of research in population dynamics that focuses on understanding the mechanisms stabilizing species near their carrying capacities (e.g. Hassell & May, 1973; Robert M. May, 1978; Bernstein, 2000). More recently, global climate change and the biodiversity crisis, including population declines, extinctions, or biological invasions, points towards the increasing relevance of nonequilibrium ecology (Rohde, 2006) and the biology of small populations (Fauvergue et al., 2012). Transient dynamics are increasingly emphasized (Hastings, 2004) and sometimes considered in the specific context of population management (Ezard et al., 2010; Kidd & Amarasekare, 2012). As first highlighted by Dobson et al. (2002), cytotype replacement which occurs in the course a suc-

cessful Wolbachia invasion yields a transient coexistence of incompatible infections
within a host population, and as a consequence, a transient decrease in reproductive rate and population size. Here, the transients only last a few generations and
this perturbation of the population's microbiome is the first step in a destabilizing cascade. We show here that the population can then be pushed toward a
second step of destabilization, triggered by a mate-finding Allee effect that can be
reinforced by the application of mating disruption, which potentially drives the
population to extinction.

# 612 Acknowledgements

We thank Fabrice Vavre for his enthusiasm in preliminary discussions, and Sylvain

614 Charlat for comments in earlier stages of this work. We also thank the Associate

Editor and two anonymous reviewers for their helpful and constructive feedback.

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## Tables

Parameter	Description	Value	Source
$\overline{N_0}$	initial population size	varies 1–K	
$m, m_t$	per capita fecundity (realized, expected)	25	
$\sigma^*$	standard deviation of fecundity	5	
$S_0^*$	survivorship in absence of competition	varies $0.08-0.2$	
$\alpha$	related to carrying capacity	0.00002	[1]
$\gamma$	related to intraspecific competition	1	[1]
$\mu_X^*, \mu_Y$	maternal transmission failure	0.03	[1]
$F_X^*, F_Y$	relative fecundity of infected individuals	0.95	[1]
$H_X, H_Y$	proportion of offspring surviving CI	0.05	[2]
$\theta$	strength of Allee effect	varies $1-0.5K$	
P	number of pheromone sources	varies $0$ – $0.15K$	

Table 1: List of model parameters. All figures use these parameter values, unless otherwise stated. Parameter values with a "\*" have associated sensitivity analyses (as discussed in the main text) in the Supplementary Information (S3). [1] refers to the reference Dobson *et al.* 2002, and [2] refers to Charlat *et al.* (2005).

Q O'	W	X	Y
W	$W: c_t q_t$	$W: H_X c_t i_t$	$W: H_Y c_t j_t$
	X: 0	X: 0	X: 0
	Y: 0	Y: 0	Y: 0
X	$W: \mu_X F_X a_t q_t$	$W: \mu_X F_X H_X a_t i_t$	$W: \mu_X F_X H_Y a_t j_t$
	$X: (1-\mu_X)F_X a_t q_t$	$X: (1-\mu_X)F_X a_t i_t$	$X: (1-\mu_X)F_XH_Ya_tj_t$
	Y: 0	Y: 0	Y: 0
Y	$W: \mu_Y F_Y b_t q_t$	$W: \mu_Y F_Y H_X b_t i_t$	$W: \mu_Y F_Y H_Y b_t j_t$
	X: 0	X: 0	X: 0
	$Y: (1-\mu_Y)F_Yb_tq_t$	$Y: (1-\mu_Y)F_YH_Xb_ti_t$	$Y: (1-\mu_Y)F_Yb_tj_t$

Table 2: Summary of Wolbachia transmission and its effects on reproduction in its host population. The first column states the maternal Wolbachia cytotype and the first row states the paternal Wolbachia cytotype. Each box in the table corresponding to a particular pairing between a female and male provides that proportion of the offspring from that pair that are uninfected (W), infected with cytotype X, and infected with cytotype Y.

## Figure captions

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Figure 1. Verification that our model accurately predicts the invasion threshold 804 as analytically determined in Hoffman et al. 1990. Here, we ignore Allee effects, 805 stochasticity, and assume P=0. The thick black curve is the frequency of infected 806 individuals at time t+1 given the frequency at t; equilibria occur when this curve 807 and the gray line (which corresponds to the case that the frequency at generations 808 t and t+1 are equal) intersect. When the black curve lies above the gray line, 809 the infection frequency is increasing; similarly, the infection frequency is decreas-810 ing when the black curve falls below the gray line. The dashed lines indicate the analytically predicted equilibrium. The smaller intersection is an unstable equi-812 librium that defines the invasion threshold: individuals introduced at a frequency higher than this threshold will successfully invade the population and approach 814 the higher stable equilibrium. In this figure, we use more extreme values for parameters related to CI to more clearly demonstrate the location of the invasion 816 threshold (specifically,  $\mu_X = 0.2$ ,  $H_X = 0.1$ ). Here,  $S_0 = 0.15$ .

Figure 2. Reproductive rate as a function of population size when  $\theta = 100$  (gray) and  $\theta = 1500$  (red). Values above one correspond to population growth, and values below one correspond to decline. The populations corresponding to the solid lines have no Wolbachia-infected individuals, populations with dashed lines have 10% of the population infected, dash-dotted lines have 50% of the population infected, and dotted lines have 90% of the population infected. Here,  $S_0 = 0.15$ .

<sup>6</sup> Figure 3. Deterministic results. (A) no control (so the population size remains

at K); (B) single Wolbachia introduction; (C) two introductions. Plot displays the 827 minimum population size relative to K over 50 generations assuming that  $N_0 = K$ 828 versus the relative strength of the Allee effect  $(\theta/K)$ . The solid line has  $S_0 = 0.08$ 829 (maximum reproductive rate of 2 in the absence of Allee effects as in Dobson et. 830 al, 2002), the dashed red line has  $S_0=0.15$  (maximum reproductive rate of 3.75 in 831 the absence of Allee effects), dash-dotted line has  $S_0 = 0.2$  (maximum reproductive 832 rate of 5 in the absence of Allee effects), and dotted line has  $S_0 = 0.25$  (maximum 833 reproductive rate of 6.25 in absence of Allee effects). (D)-(E) are identical to (A)-834 (C), respectively, but it is additionally assumed that pheromone sources are held 835 at a fixed level such that P/K = 0.1. In all plots, each release is created so the 836 initial infection frequency of that cytotype is 10%. The first release is at genera-837 tion one, and the second release is determined by the optimization scheme detailed 838 in Section S2 in the ESM. In (E)-(F), the absence of the solid line indicates that 839 extinction is achieved for all values of  $\theta/K$ . Curves corresponding to  $S_0 = 0.15$ , 840 the value used in all subsequent plots, are highlighted in red to further emphasize 841 the synergy between management tactics. 842

Figure 4. Sample trajectories of the population dynamics (relative to K) when two incompatible cytotypes of Wolbachia are introduced into a population when  $S_0 = 0.15$ . The relative strength of the Allee effect is set to  $\theta/K = 0.15$ , which corresponds to an Allee threshold of  $\sim 5.8\%$  of the carrying capacity (as indicated by the horizontal dashed gray line). The black dashed line assumes that there are no pheromone sources, and the solid line assumes that the relative number of pheromone sources P/K is 0.1. As also evidenced in Fig. 3 (e.g. by considering the dashed curve in Fig. 3A-B when  $\theta/K = 0.15$ ), intervention with Wolbachia

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introductions only under these parameter conditions is not successful. A combination of *Wolbachia* introduction and pheromone sources, however, is successful in achieving population extinction.

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Figure 5. The gray scale in each plot represents the extinction probability for 856 a given parameter combination based on 500 realizations of the model. In each 857 plot, the initial population size and the strength of the Allee effect  $\theta$ , both relative 858 to K, are varied. We note that the carrying capacity of the population in the 859 absence of Allee effects is 5500 with these parameters; therefore, the introduction 860 sizes – which adjust the population size so that there is a 10% infection frequency 861 - do not exceed  $\sim 612$  insects. Top row: demographic stochasticity only. Bottom 862 row: both demographic and environmental stochasticity. First column: no intro-863 duction. Second column: introduction such that infection frequency is at 10%. 864 Third column: two subsequent introductions, both of which ensure the infection 865 frequency is 10% for each cytotype at time of introduction (see Supplementary 866 Information S2 for generation of second introduction). The dashed gray curve is 867 the Allee threshold (i.e. initial populations below the gray curve go to extinction 868 in the deterministic model). Here,  $S_0 = 0.15$ . 869

Figure 6. Fixing the relative strength of the Allee effect  $\theta/K = 0.1$ , the gray scale in each plot represent the extinction probability for a given parameter combination based on 500 realizations of the model. In each plot, the initial population size and the number of pheromone sources (P) relative to K are varied. Top row: demographic stochasticity only. Bottom row: both demographic and environmental stochasticity. First column: no introduction. Second column: introduction such

that infection frequency is at 10%. Third column: two subsequent introductions.

Here,  $S_0 = 0.15$ .

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Figure 1:

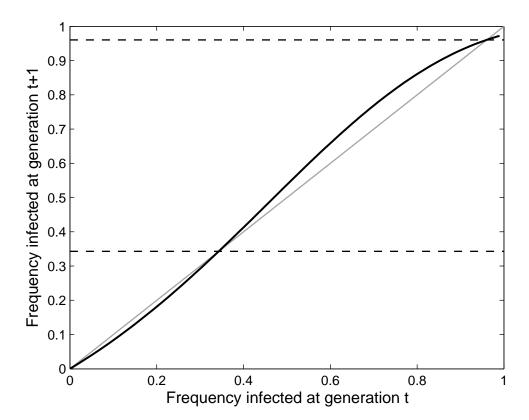


Figure 2:

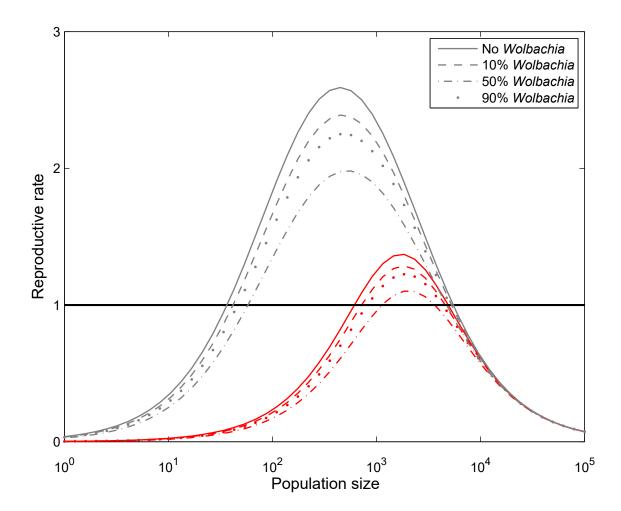


Figure 3:

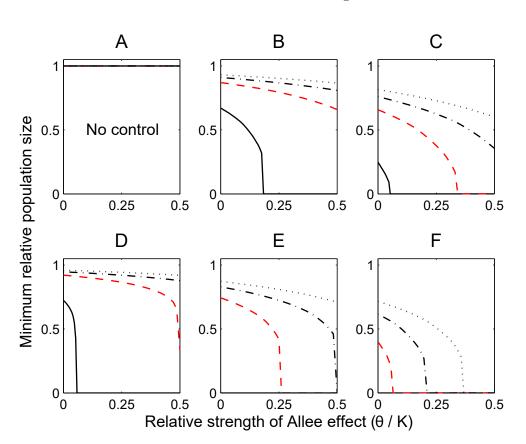


Figure 4:

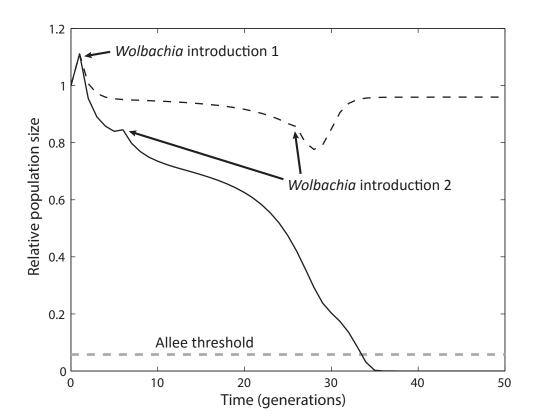


Figure 5:

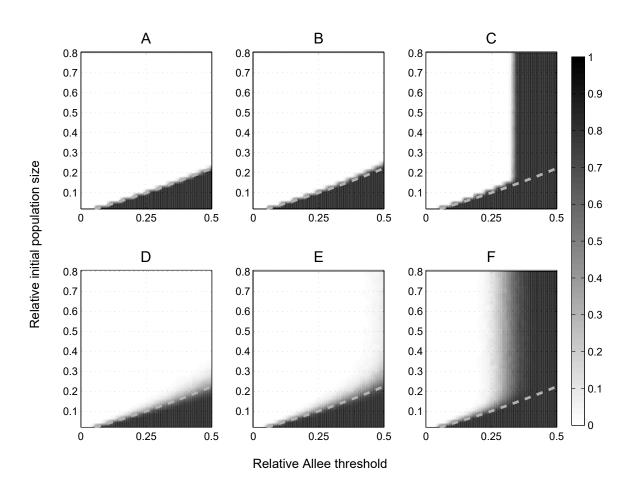


Figure 6:

