Unifying intra- and inter-specific variation in tropical tree mortality

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Tree death is a fundamental process driving population dynamics, nutrient cycling, and evolution within plant communities. While past research has identified factors influencing tree mortality across a variety of scales, these distinct drivers are yet to be integrated within a unified predictive framework. In this study, we use a cross-validated Bayesian framework coupled with classic survival analysis techniques to derive instantaneous mortality functions for 203 tropical rainforest tree species at Barro Colorado Island (BCI), Panama. Specifically, we develop functions that not only integrate individual, species, and temporal effects, but also partition the contributions of growth-dependent and growth-independent effects on the overall instantaneous mortality rate. We show that functions that separate mortality rates into growth-dependent and growth-independent hazards, use stem diameter growth rather than basal area growth, and attribute the effect of wood density to growth-independent mortality outperform alternative formulations. Moreover, we show that the effect of wood density – a prominent trait known to influence tree mortality – explains only 22% of the total variability observed among species. Lastly, our analysis shows that growth-dependent processes are the predominant contributor to rates of tree mortality at BCI. Combined, this study provides a framework for predicting individual-level mortality in highly diverse tropical forests. It also highlights how little we know about the causes of species-level and temporal plot-scale effects needed to effectively predict tree mortality.

Rates of plant mortality are known to vary widely among individuals within species, among coexisting species, between forests, and from year-to-year \cite{1,2,3}. This variation has considerable consequences for forest structure and dynamics. For example, death of a single large tree can transfer up to 20,000 kg of carbon from living to decaying carbon pools \cite{4}. Furthermore it creates a gap in the canopy that can restart a successional race, during which 100’s of plants may die while competing for a spot in the sun. In models of forest dynamics, variation in mortality rates has been shown to have a larger impact on forest structure than variation in absolute growth rates \cite{5}. Improving our understanding of the mortality process is therefore a priority for making accurate predictions about population, carbon and nutrient dynamics of forests, especially in an era of rapid environmental change.

Two difficulties arise when studying tree mortality in tropical rainforests. The first is that large population sizes and long periods of observation are required to make inferences into how various factors affect mortality rates \cite{5}. This requirement arises in part because the observable outcome – alive vs. dead – is one step removed from the variable we ideally want to measure: \( \lambda_i(t) \), the instantaneous rate of mortality for individual \( i \) at time \( t \), also called the “hazard function”. In classic survival analysis \cite{6a}, the probability an individual dies between times \( t_2 \) and \( t_3 \) is a function of \( \lambda_i(t) \):

\[
 p_{i,t_2 \rightarrow t_3} = 1 - \exp \left( - \int_{t_2}^{t_3} \lambda_i(t) dt \right) .
\]

Here \( \int_{t_2}^{t_3} \lambda_i(t) dt \) is the “cumulative hazard” between \( t_2 \) and \( t_3 \) \cite{6a}. The observed survival outcome \( S_{i,t_2 \rightarrow t_3} \) (0 = alive, 1 = died) is then a realisation of this probability

\[
 S_{i,t_2 \rightarrow t_3} \sim \text{Bernoulli}(p_{i,t_2 \rightarrow t_3}).
\]

As trees are long-lived and we are trying to estimate the shape of a continuous hazard function (\( \lambda_i(t) \)) from binary data, large sample sizes are required. Detailed studies of tree mortality have thus only recently become possible, with the accumulation of growth and survival data from repeat surveys spanning several decades in plots containing thousands of individuals \cite{7}.

Another difficulty when studying mortality – similar to that faced in other fields like medicine and engineering – is determining the shape of hazard functions that skillfully predict.

**Significance Statement**

Tree mortality is a fundamental demographic process affecting forest dynamics and carbon cycling. Here, for the first time, we use over 400,000 observed survival records collected over a 15 year period from more than 180,000 individuals, to simultaneously estimate growth-dependent and growth-independent mortality across 203 tropical forest tree species. We found that growth-dependent mortality was the predominant factor influencing tree mortality rates at Barro Colorado Island. Furthermore, we found that while wood density influenced mortality rates by decreasing growth-independent mortality, wood density only accounted for a small fraction of the overall species variability in mortality rates, suggesting that there must be other species traits that strongly affect mortality.

D.F. conceived idea; all authors designed research; J.C & R.F. performed analysis in discussion with L.M, D.S. & M.W; R.C & S.W. collected data. J.C & D.F . wrote the manuscript.

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Data deposition: Code reproducing the results in this paper is available at github.com/tratecoco/mortality.bco. Data from BCI is available at DoIs 10.5479/data.bco.20130603., 10.5479/data.bco20140711.

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Towards a unified model of tree mortality

A specific challenge in developing hazard functions for plants is to estimate the relative contribution of growth-dependent and growth-independent hazards on an individual’s overall hazard. While plants die via many causes, these broadly fall into two categories. The first are growth-dependent hazards, where plants die because of insufficient carbon assimilation for growth and repair. The second are growth-independent hazards, where plants die because of stochastic events, irrespective of their growth rate, such as windfall or fire. An individual’s total hazard is the sum of growth-independent and growth-dependent components.

A further challenge in developing hazard functions for plants is to integrate the conflicting relationships observed within and across species between mortality and growth. Within species, mortality rates are lower for fast-growing individuals, presumably because those individuals have superior carbon budgets and are thus able to tolerate or repair diverse stresses [1, 12, 15]. Empirical studies broadly support this theory, with many indicating exponential declines in mortality with increased growth rate, \(X_i(t)\) [1, 11, 16]. By contrast, across species, there is a strong trade-off between growth and survival, with individuals from faster-growing species exhibiting higher mortality rates than individuals from slower-growing species [3, 9]. This trade-off may arise via traits with antagonistic effects, such as wood density. Denser wood—which is expensive to build and thus slows growth—reduces stem breakage [17, 18], embolism [19, 20], pathogen attack [21], and thereby mortality [3, 8, 9, 18].

Here, we attempt to reconcile intra- and inter-specific factors as well as partition instantaneous mortality rates into growth-dependent and growth-independent rates. We achieve this by evaluating the following, unified hazard function, incorporating individual-, species-, and censal-level effects:

\[
\lambda_i(t) = \left( \frac{\text{Growth independent}}{\gamma_s} + \frac{\text{Growth dependent}}{\alpha_s \cdot \delta_t} \right) \times X_i(t) \cdot \delta_t \quad \text{[3]}
\]

Eq. 3 allows for additive growth-independent and growth-dependent effects, includes a negative exponential effect of growth rate, and allows for mortality to vary among censuses, via the random effect \(\delta_t\). Further, the parameters \(\alpha_s\), \(\beta_s\), and \(\gamma_s\) vary by species, \(s\). Here we include an effect of a species trait (wood density, \(\rho\)), as well as a species random effect that captures any remaining species-level differences not accounted for by wood density (for details see Methods).

To validate this model, we fit a series of models with increasing complexity (eq. 3 being the most complex) and compare their skill in predicting patterns of tropical tree mortality for 180,509 individuals from 203 tree species at Barro Colorado Island (BCI), Panama (Fig. 1). The data are repeat censuses of stem diameter and tree status (alive vs. dead) taken over a 15 yr period (Fig. 1A). In total 427,468 observations were used to fit these models. We compare the skill of different hazard functions in predicting outcomes in novel data (i.e. not used in model fitting) via 10-fold cross-validation (Fig. 1D) [22, 23]. Evaluating models in this way is computationally expensive, making it impossible to run all possible model formulations. We therefore fit models across five iterative stages of model development. At each stage, the best model from the previous stage was taken as input for the next stage.

In stage 1, we ask whether mortality rates vary substantially between censuses, to establish whether a census effect is required. The null model is a constant, invariant with respect to species, growth rate, or year. In stage 2, we assess whether a hazard function including both growth-dependent and growth-independent terms outperform a function including only one of these. Species effects were excluded, so we are simply asking which of three functional forms for \(\lambda_i(t)\) (Fig. 1B) best predicts the data. The simplest form (Fig. 1B, left) assumes a constant growth-independent hazard rate. The second form (Fig. 1B, middle) assumes the risk of dying declines

![Fig. 1. Outline of methodology. A) Our data consist of repeat measures of stem diameter (D) and status (S, 0 = alive or 1 = dead) for individual trees at specific census dates (t1, t2, t3). B) We consider three alternative hazard functions: 1) a baseline hazard; 2) a growth-dependent hazard; and 3) a function that combines both baseline and growth-dependent hazards. The parameters of the models are biologically interpretable: \(\alpha\) defines the instantaneous mortality rate at low growth rate; \(\beta\) reflects the sensitivity of mortality rate to changes in growth rate; and \(\gamma\) is the asymptote, or baseline hazard. Combined \(\alpha\) and \(\beta\) capture growth-dependent mortality, while \(\gamma\) captures growth-independent mortality (e.g. windfall, fire) that kill a plant, irrespective of its growth rate. For each model form, we consider two alternative predictors of growth, \(X\) (basal area and stem diameter growth), as well as allowing for species-level effects on the parameters \(\alpha, \beta\), and \(\gamma\). C) Each model’s skill in predicting observed outcomes (S) is quantified via the log-loss function (eq. 5). D) The predictive skill of alternative models was evaluated via 10-fold cross validation. The entire dataset is split into 10 folds (F1, ..., F10). Alternative models were fit 10 times (M1, ..., M10), using different combinations of testing (1 fold; orange) and training (9 folds; green) data. Predictive capacity was assessed by averaging the log-loss obtained from the 10 test data predictions.](https://doi.org/10.1101/228361)
towards an asymptote of zero as growth increases. The third form (eq. Fig. 1B, right) is the summation of the two previous models; this allows $\lambda_i(t)$ to decrease exponentially with increasing growth rate, but, unlike a standard negative exponential, asymptoting at some baseline hazard $> 0$. Combined, these three models capture a variety of functional responses previously proposed, including effects represented in current vegetation models [14, 24], which have not previously been systematically compared. We also investigate which growth measure (stem diameter, stem area increment) more skillfully predicts growth-dependent mortality. In stage 3, we examine whether including wood density (a species-level trait) improved model skill, and if so, whether the effect of wood density was on growth-dependent, growth-independent, or both hazards. Finally, we fit a model that allowed parameters to vary by species-level variation that was otherwise not captured by wood density. This allowed us to ask what proportion of inter-specific hazard variability is explained by wood density. Using the final “best” model we also conducted post-hoc tests, to determine how species-level parameters were associated with their maximum size and light requirement.

Results

Mortality over time. Comparing the three 5-year intervals between censuses from 1995 to 2010, we found average mortality rates progressively decreasing over the time. The highest proportion of trees death occurred between 1995–2000 (16%) followed by 2000–2005 (13%) and 2005–2010 (12%). Consequently, when we allowed hazard rates to be scaled by census (i.e. adding term $\delta$) we observed a small, but significant, increase in predictive skill (Fig. 2A). Individual census effects can be found in Table S1.

Hazard functions. Comparing the three hazard functions in Fig. 1B, we found that the third function — with both growth-dependent and growth-independent terms, i.e. $(ae^{-\beta X_i} + \gamma)\delta_i$ — significantly outperformed both the growth-independent only (i.e. null) or growth-dependent only functions (Fig. 2A). Moreover, we found that predictive skill was higher when using stem diameter growth over stem-area growth (Fig. 2A).

A summary of hyper parameter estimates can be found in Table S1.

Wood density and other species effects. Including wood density as an effect on either growth-independent or growth-dependent parameters significantly improved model skill relative to a model without such effects (Fig. 2 A.B). The most parsimonious model, with highest predictive skill, was that attributing the wood density effect to the growth-independent hazard term ($\gamma$; Fig. 2 B). Specifically, we found that wood density was negatively correlated with a species’ baseline mortality rate, $\gamma$ (Fig. 3). This meant that fast growing individuals from a low wood density species had, on average, higher mortality rates (Fig. 4 A.B), and thus higher probability of death across a 1-yr period (Fig. 4 C.D), relative to fast growing individuals of high wood density species. For example, a species with a wood density of 0.3 g cm$^{-3}$ had an estimated mean probability of dying of 0.05 yr$^{-1}$ compared to 0.01 yr$^{-1}$ for a species with a wood density of 0.8 g cm$^{-3}$. Incorporating an additional species-level random effect to capture any additional inter specific differences substantially improved model
Discussion

Our Bayesian framework coupled with cross validation revealed that the most explanatory and parsimonious model of tropical tree death was that which: 1) partitioned mortality into growth-dependent and growth-independent hazards; 2) used stem diameter growth rather than basal-area growth; 3) attributed the effect of wood density to growth-independent mortality; and 4) incorporated temporal variability. Moreover, we found that rates of tropical tree mortality varied substantially between species and that wood density, a species level functional trait, explained only a limited proportion of the overall inter-specific variation.

The findings of this study provide empirical support for dynamic vegetation models that estimate mortality as the sum of growth-dependent and growth-independent hazards [14, 24, 25]. We show that regardless of growth measure, incorporating both hazards significantly improves model predictive skill. This is because the growth-dependent hazard allows for deaths associated with low carbon budgets, and as a consequence, incorporates intra-specific variability attributed to carbon related stresses (e.g. competition, parasites, herbivory). By contrast, the growth-independent hazard accounts for deaths caused by events that arise irrespective of an individual’s growth rate (e.g. windthrow, lightning strike).

Additionally, the partitioning of mortality into growth-dependent and growth-independent effects allowed us to estimate the proportion of variation attributed to each. Like many other studies [26–28], our analyses highlight the importance of light competition in influencing tropical tree demographic rates. Specifically, we found that the growth-dependent hazard accounted for 68% of the total predicted variability in mortality rates (Fig. 5). This suggests deficiencies in carbon budget are a major contributor to tree death on BCI.

Incorporating the effect of wood density on mortality rates also improved predictive performance. Our analyses revealed that the most parsimonious combination of wood density effects was when it was attributed to only the growth-independent hazard term. Specifically, high wood density species had lower baseline rates relative to low wood density counterparts. This finding corroborates the observed negative correlation observed between mortality and wood density reported elsewhere [8, 18]. More importantly, our analyses support the theory that wood density reduces mortality rates by decreasing a species’ vulnerability to growth-independent threats, such as windthrow, trampling and treefall [17, 18].

While wood density effects are now being incorporated in mortality algorithms of many vegetation models [24, 29], our analysis indicate that such effects are likely to only capture...
in shade (i.e. low gap index), supporting past findings [27].

We should also consider how the interval between censuses affects the estimation of growth-dependent and growth-independent hazards. Large census intervals may underesti-
mate growth-dependent mortality, as wide census intervals will not capture deaths due to rapid declines in growth, or events such as drought (although drought might also increase tree growth [34]). Consequently, we may overestimate the relative contribution of growth-independent hazards.

Here we showcase a new framework for modelling tropical tree mortality that unifies empirical evidence from within and between species studies. This framework also provides an approach for partitioning mortality rates into growth-dependent and growth-independent hazards. Our findings reveal that while wood density is an important trait affecting mortality rates, we are still only capturing a fraction of the overall species variability in mortality rates.

Materials and Methods

Data. We derived plant mortality models using individual growth and survival data collected from a relatively undisturbed 50-ha tropical rainforest plot on BCI, Panama (9.15°N, 79.85°W). The climate on the island is warm and rainfall is seasonal with most falling between April and November [34].

Within the 50-ha plot the diameter at breast height and survival status of all free-standing woody plants that were at least 1.3 m tall and had diameter ≥ 1 cm were recorded in 1981–1983, 1985, and every 5 years thereafter [34]. For the purpose of modelling mortality as a function of past growth, we discarded data collected prior to 1990. This was because diameter measurements were rounded to the nearest 5 mm for individuals with dbh < 55 mm, whereas in later censuses all individuals were measured to the nearest millimetre [33]. Consequently, we modelled tree mortality as a function of past growth for censuses 1995–2000, 2000–2005 and 2005–2010. We discarded species that do not exhibit secondary growth (e.g. palms and ferms), contained fewer than 10 individuals or did not contain an estimate of wood density. We also excluded individuals that: 1) did not survive at least two censuses (two being required to estimate growth rate); 2) were not consistently measured at 1.3 m above ground; 3) were multi-stemmed; 4) resprouted or seemingly “returned from the dead”; or 5) were extreme outliers—stems which grew more than 5 cm yr⁻¹ or shrank more than 25% of their initial diameter. In total 427,468 observations were used in this study comprising 180,509 individual trees and 203 species. Because of computational costs, the models fit in this study do not include individual random effects, as this would require estimation of an additional 180,509 parameters. Instead, our models assume that repeat measurements of an individual are independent of one another. We believe this is a reasonable assumption given that there is approximately 5-years between censuses.

Wood density for each species was estimated by coring trees located within 15 km of the BCI plot [9]. Cores were broken into pieces, each 5 cm long and specific gravity of each piece was determined by oven drying (100°C) and dividing by the fresh volume (as measured by water displacement).

Model fitting. Eqs. 1–3 were fit to the data using Bayesian inference and with covariates for growth rate in previous census and wood density.
density, as well as random effects. Growth rates were estimated from field measurements of diameter, which inevitably include observation error. In our dataset, 8% of estimated growth rates were negative. To ensure our mortality model was not biased by these unlikely values we first applied a probabilistic model to estimate “true growth”, taking into account measurement error and the distribution of growth rate across the community (see Supplementary Material S1 for details; Fig. S1). The parameters $\alpha_s$, $\beta_s$, and $\gamma_s$ were modeled as a function of both wood density (measured at species level) and a species-level random effect:

$$
\alpha_s = \alpha_{so} + \rho \alpha_{1},
$$

with similar formulations for $\beta_s$ and $\gamma_s$. Here $\alpha_{so}$ captures the effect of wood density $\rho$ on $\alpha_s$, while $\alpha_{1}$ captures any other species-level residual error not explained by wood density for species $s$. These random effects were modeled as random realisations from log-normal distributions. The form of eq. 4 ensures that parameters remain positive; and on a log scale this equates to an additive linear model centered around $\rho_s$. We also centered growth rate $X_s$ at the lower 5% quantile for both diameter increment and area growth (0.172 and 0.338, respectively), meaning $\alpha_s$ should be interpreted as the hazard rate when growth rate was very low. Weak priors on all hyper-parameters were set (see Supplementary Material S2 for details). Models were fit in R 3.4.1 using the package rstan 2.16.2 [55] and employing some numerical optimisations (see Supplementary Material S3-S4 for details). We executed three independent chains and in all cases modelled parameters converged within 2000 iterations. Convergence was assessed through both visual inspection of chains and reference to the Brooks-Gelman-Rubin convergence diagnostic [36]. After discarding the first 2000 iterations as ‘burn in’, a further 2000 iterations were taken from the joint posterior. Species parameter estimates from the final model are shown in Figs. S3-S5.

Evaluating model skill. Predictive skill was quantified by estimating the average log loss across 10-folds for held-out data, $L$ (Fig. 1C). Lower $L$ means a model, $\ell$, predicts the predicted probability is from the observed outcome, $y$, as a posterior distribution. We calculated a gap index as a measure of a species’ light dependence using annual canopy census data collected during 1985-1990 and 1990-1995. The canopy census recorded, in all 5 by 5 m subplots across the 50 ha plot, the presence of leaf in six different height layers (0-2.2-5.5-10.0-20.20-30.30-30.30 m). For each subplot, we calculated the number of strata > 2 m containing vegetation; and then transformed this to a light index ranging from 0 (dense shade) to 1 (gap). As light may penetrate into a subplot from the edge of a subplot, we rescaled this index to account for values in the eight immediate neighbouring subplots. Specifically, we used a weighted sum approach whereby the central subplot is assigned a weight of 8 and the eight neighbouring subplots are assigned a weight of 1. This meant that the contribution of the central plot was equivalent to the combined effect of all eight neighbouring plots. These weighted values were then summed and rescaled between 0 and 1 by dividing by the maximum value estimated across all subplots. The gap index for each species was estimated as the mean light index encountered by new saplings appearing in the census (Fig. S2).

Posthoc correlations. We calculated a global index as a measure of a species’ light dependence using annual canopy census data collected during 1985-1990 and 1990-1995. The canopy census recorded, in all 5 by 5 m subplots across the 50 ha plot, the presence of leaf in six different height layers (0-2.2-5.5-10.0-20.20-30.30-30.30 m). For each subplot, we calculated the number of strata > 2 m containing vegetation; and then transformed this to a light index ranging from 0 (dense shade) to 1 (gap). As light may penetrate into a subplot from the edge of a subplot, we rescaled this index to account for values in the eight immediate neighbouring subplots. Specifically, we used a weighted sum approach whereby the central subplot is assigned a weight of 8 and the eight neighbouring subplots are assigned a weight of 1. This meant that the contribution of the central plot was equivalent to the combined effect of all eight neighbouring plots. These weighted values were then summed and rescaled between 0 and 1 by dividing by the maximum value estimated across all subplots. The gap index for each species was estimated as the mean light index encountered by new saplings appearing in the census (Fig. S2).

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