Characterizing functional consequences of DNA copy number alterations in breast and ovarian tumors by spaceMap

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Abstract

Motivation: We propose a novel conditional graphical model — **spaceMap** — to construct gene regulatory networks from multiple types of high dimensional omic profiles. A motivating application is to characterize the perturbation of DNA copy number alterations (CNA) on downstream protein levels in tumors. Through a penalized multivariate regression framework, **spaceMap** jointly models high dimensional protein levels as responses and high dimensional CNA as predictors. In this setup, **spaceMap** infers an undirected network among proteins together with a directed network encoding how CNA perturb the protein network. **spaceMap** can be applied to learn other types of regulatory relationships from high dimensional molecular profiles, especially those exhibiting hub structures.

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Results: Simulation studies show **spaceMap** has greater power in detecting regulatory relationships over competing methods. Additionally, **spaceMap** includes a network analysis toolkit for biological interpretation of inferred networks. We applied **spaceMap** to the CNA, gene expression and proteomics data sets from CPTAC-TCGA breast (n=77) and ovarian (n=174) cancer studies. Each cancer exhibited disruption of ‘ion transmembrane transport’ and ‘regulation from RNA polymerase II promoter’ by CNA events unique to each cancer. Moreover, using protein levels as a response yields a more functionally-enriched network than using RNA expressions in both cancer types. The network results also help to pinpoint crucial cancer genes and provide insights on the functional consequences of important CNA in breast and ovarian cancers.

Availability: The R package **spaceMap** — including vignettes and documentation — is hosted at <https://topherconley.github.io/spacemap>

Keywords:

integrative genomics, proteogenomics, conditional graphical models, network analysis

1. Introduction

Relative to high-throughput genomic assays, only recently has quantitative mass-spectrometry-based proteomics become available for large-scale studies. The collaboration between the Clinical Proteomic Tumor Analysis Consortium (CPTAC) (Paulovich et al., 2010; Ellis et al., 2013; Zhang et al., 2016) and The Cancer Genome Atlas (TCGA) is among the first to produce

7 large-sample cancer studies integrating deep proteomic and genomic quanti-
8 tative profiling. Naturally this proteogenomic combination enables the study
9 of how and to what extent genetic alterations impacted protein levels in can-
10 cer. Specifically, the CPTAC Breast/Ovarian Cancer Proteogenomics Land-
11 scape Study (BCPLS/OCPLS) identified proteomic signaling consequences
12 of DNA copy number alterations (CNA) based on 77 and 174 high-quality
13 breast and ovarian cancer samples, respectively (Mertins et al., 2016; Zhang
14 et al., 2016). Identifying which CNAs impact downstream protein activities
15 and how they do so can lead to better understanding of disease etiology and
16 discovery of new biomarkers as well as drug targets (Akavia et al., 2010;
17 Greenman et al., 2007).

18 However, the full extent of biomedical information in multiple-omic stud-
19 ies like BCPLS/OCPLS cannot be realized without effective integrative anal-
20 ysis tools. These tools must characterize interactions among different bi-
21 ological components operating in different cellular contexts. For the BC-
22 PLS/OCPLS data and other proteogenomic data like it, this requires exam-
23 ining relationships between a large number of protein levels in one context
24 and CNA events in another context. Studying a pair of features at a time
25 may not be sufficient, as cancer is overwhelmingly complex; molecules from
26 many parallel signal transduction pathways are affected by the disease, and
27 their activities appear to be controlled by multiple factors. Therefore, we
28 need to jointly consider all players in the system. Recent advances in graph-
29 ical models for high-dimensional data provide a powerful “hammer” for this
30 “nail” (Meinshausen and Bühlmann, 2006; Yuan and Lin, 2006; Friedman
31 et al., 2008; Peng et al., 2009).

Graphical models infer interactions among features (e.g., genes/proteins) based on their dependency structure, for it is believed that strong interactions often result in significant dependencies. Compared to approaches using pairwise correlation to characterize and infer interacting relationships (e.g. (Butte et al., 2000)), graphical models learn more direct interactions through investigating *conditional dependencies*. Many methods have been proposed in the past decade to infer *genetic regulatory networks (GRNs)* based on high-throughput molecular profiling through graphical models (Li et al., 2013; Friedman et al., 2008; Peng et al., 2009; Wang et al., 2011; Cheng et al., 2014; Danaher et al., 2014; Schäfer and Strimmer, 2004). However, when applying graphical models for the proteogenomic integrative analysis, we encounter new challenges that are not fully addressed by existing methods. First, integrative analysis necessarily involves multi-layer biological components, but we may only be interested in a subset of all possible interactions. For example, we may be interested in how CNAs regulate protein levels, but not the dependency structure among CNAs. Second, although many data types may be reasonably modeled by Normal distributions, some data types, such as DNA mutation and SNP, can not be modeled by Gaussianity.

To bridge these gaps we propose a conditional graphical (CG) model, **spaceMap**, which learns the conditional dependencies between two types of nodes through a penalized multivariate regression framework. Specifically, **spaceMap** infers an undirected graph among response variables (e.g., protein levels) in tandem with a directed graph encoding perturbations from predictor variables (e.g., CNAs) on the response network. In addition, we use cross-validation and a model aggregation technique called **Boot.Vote** to

improve reproducibility. Moreover, we develop a network analysis toolkit to facilitate biological interpretation. These lead to an integrative -omics analysis pipeline illustrated in Figure 1.

Peng et al. (2010) proposed the **remMap** model for integrative analysis of gene expressions and CNA. Specifically, **remMap** utilized a penalized multi-variate regression model and introduced a so called MAP penalty through combining both l_1 and column-wise- l_2 norm of the coefficient matrix to encourage the selection of *master* predictors that have influence on many responses. However, unlike **spaceMap**, **remMap** does not reveal how the expressions interact with each other in the presence of perturbations from CNAs.

Another straight forward approach to handle two types of data is to fit one graphical model without distinguishing the two types of nodes and then subset only those interactions of interest. For example, a model like **space** (Peng et al., 2009) can be used to infer an undirected network where CNAs and protein levels are not explicitly distinguished during model fitting. The inferred conditional dependencies amongst CNAs can then be ignored, while CNA-protein and protein-protein interactions could be retained for further investigation. However, since there are often thousands of CNA regions, such an approach suffers from inefficiency by wasting many degrees of freedom in estimating interactions among CNAs that we are not interested in. On the contrary, **spaceMap** aims at learning the conditional dependencies among a set of response nodes (e.g., protein levels) and the perturbations from a set of predictor nodes (e.g., CNAs). By conditioning on the predictor nodes, these are free to have any distribution and the interactions among the predictors need not be modeled and estimated. Such an approach is expected to exhibit

82 gains in statistical power and computational efficiency.

83 Recently, Zhang and Kim (2014) proposed a model called **scggm** to fit con-
 84 ditional Gaussian graphical models through an l_1 penalized conditional log-
 85 likelihood. In several genetical genomics simulations, **scggm** showed higher
 86 precision-recall curves (i.e. accuracy) in learning the network structure than
 87 competing methods including **MRCE** (Rothman et al., 2010) and **graphical**
 88 **lasso** (Friedman et al., 2008). Although **spaceMap** and **scggm** target the
 89 same type of response-predictor and response-response interactions, they are
 90 very different in terms of modeling approaches. **spaceMap** uses a regression-
 91 based approach through pseudo-likelihood approximations with a penalized
 92 least squares criterion, while **scggm** is based on penalized conditional like-
 93 lihood. Peng et al. (2009) conducted a comprehensive comparison between
 94 regression-based and likelihood-based graphical models and found that regression-
 95 based methods often perform better in the presence of hubs and are more ro-
 96 bust to violations of distributional assumption. Moreover, **spaceMap** adopts
 97 the MAP penalty from **remMap** (Peng et al., 2010) for the response-predictor
 98 interactions, making it more powerful in detecting master predictors. In a
 99 simulation study involving networks with hub nodes, **spaceMap** is shown to
 100 outperform both **space** and **scggm** in terms of edge and hub detection.

101 The rest of the paper is organized as follows. In Section 2, we first present
 102 simulation results to demonstrate the performance of **spaceMap** and then
 103 apply **spaceMap** to the BCPLS data and OCPLS data to learn the (CNA-
 104 protein, CNA-RNA, and protein-protein) regulatory networks. We summa-
 105 rize the conclusions in Section 3. In Section 4, we describe the **spaceMap**
 106 model, simulation settings, BCPLS/OCPLS applications, and a network

analysis toolkit. Additional details are given in the Supplementary Material.

2. Results

2.1. Simulation

Figure 2 shows the results of the three methods, namely **spaceMap**, **space** and **scggm**, under the **hub-net** simulation (see Section 4.2). **spaceMap** has the highest MCC and the highest power across all edge types while maintaining a low FDR. Particularly, **spaceMap** has considerably more power in CNA–protein edge detection than the other two methods. **space** is least powerful in CNA–protein edge detection, though it also has the lowest FDR. The differences in power and MCC are significant, whereas those in FDR are not always significant. See Supplementary Table S.1 for more details.

Moreover, all methods have 100% power in identifying all 15 CNA-hubs. Note that, the CNA-hub power is defined as the power to detect at least one CNA-protein interaction. Since each hub has a fair number of such interactions, this power is expected to be high for all reasonable methods. On the other hand, **spaceMap** has the lowest CNA-hub detection FDR (0.67%) and **scggm** has the highest CNA-hub detection FDR (12.6%).

The performance of the three methods under the **power-net** simulation (see Section 4.2) is shown in Figure S.1 with numerical summaries given in Table S.2 of the Supplementary Material. **spaceMap** achieves the highest MCC score across all edge types followed with a close second by **space**, and a distant third by **scggm**. **spaceMap** dominates **space** and **scggm** in CNA–protein edge detection power at the cost of slight FDR inflation. **scggm** has

the highest power in protein–protein edge detection, however with extremely high FDR. All methods exhibit (near) 100% power in CNA-hub detection. Remarkably, **spaceMap** has an CNA-hub FDR of 0, while the other two methods have CNA-hub FDR above 20%. In summary, **spaceMap** is able to find the true source of perturbation to the response network. On the other hand, the other two methods exhibit a tendency to report false CNA-hubs.

We also apply the **Boot.Vote** procedure (with $B = 1000$ bootstrap resamples) described in Section 4.1 to **spaceMap** to further reduce FDR. **Boot.Vote** under the **hub-net** simulation leads to very similar results as **CV.Vote**, probably due to the already low FDR in this setting. On the other hand, **Boot.Vote** under the **power-net** simulation leads to reduced FDR compared to **CV.Vote**. In short, **Boot.Vote** is an effective procedure in (further) reducing FDR. It is especially useful for real data applications, which often suffer from low signal-to-noise ratio and complicated noise structure and consequently high FDR and low reproducibility of the fitted networks.

2.2. BCPLS application

2.2.1. *prot-net*

We first focus on protein levels because protein activities are expected to have a more direct impact on cell phenotypes than RNA. The goal is to identify major CNA events disrupting biological pathways at the protein level while accounting for the conditional dependency structure among proteins themselves. To this end **spaceMap** learns a network from CNA and protein levels — hereafter called **prot-net** — built under the 10-fold CV-selected tuning parameters and the **Boot.Vote** ($B = 1000$) aggregation process.

prot-net has 585 CNA–protein edges, 954 protein–protein edges and 11

156 CNA-hubs (Table 1). The top three ranked CNA-hubs are listed in Table 2
 157 and the complete list is provided in Table S.4. Network analysis reveals 10
 158 modules of size 15 or more. GO terms enriched in each module are listed
 159 in Supplementary Table S.5. Three of the 10 modules contain at least one
 160 CNA-hub that directly perturbs at least five proteins within the module.
 161 Figure 3 illustrates the topology of these three modules.

162 One of the three modules contains a CNA-hub on 17q12 (Figure 3 upper-
 163 left), which cis-regulates multiple genes in this region including ERBB2,
 164 GRB7, and PNMT. ERBB2, the epidermal growth factor receptor 2, is a
 165 well-known breast cancer oncogene for Her2-subtype of breast cancer. Ac-
 166 tivities of Her2, the protein coded by ERBB2, influence multiple pathways
 167 regulating cell growth, survival, migration and proliferation that have a key
 168 role in cancer development. Her2 has been used as a drug target in current
 169 clinical treatment of breast cancer patients (Wolff et al., 2013; Sahlberg et al.,
 170 2013). Recent research studies also suggest that expression of other genes
 171 in the 17q12 amplicon, such as GRB7 and PNMT, may function together
 172 with ERBB2 to sustain the growth of breast cancer cells (Sahlberg et al.,
 173 2013). Thus, identifying CNA in 17q12 as a hub in CNA-protein regulatory
 174 network suggest that **spaceMap** is able to reveal known important regulations
 175 underlying the disease system.

176 In addition to 17q12, **spaceMap** also identified another prominent CNA
 177 regulatory hub on the same chromosome in 17q21.32 (Figure 3, bottom).
 178 Loss of 17q21.32 has been widely reported in breast cancer studies. For
 179 example, in a recent paper of invasive ductal breast cancer study, loss in
 180 17q21.32 were observed at a very high frequency (80%), suggesting potential

181 tumor suppressor genes harbored in this region (Dimova, 2015). However,
 182 it remains unclear what functional consequences these deletions may lead to
 183 in tumor cells. To address this question, we investigated the subset of pro-
 184 teins regulated by the CNA-hub on 17q21.32. We identify a tightly linked
 185 group of 10 proteins from the family of P-type cation transport ATPases,
 186 which are integral membrane proteins responsible for establishing and main-
 187 taining the electrochemical gradients of Na and K ions across the plasma
 188 membrane. Increasing evidence suggests that ion channels and pumps play
 189 important roles in cell proliferation, migration, apoptosis and differentiation,
 190 and therefore is involved in aberrant tumor growth and tumor cell migra-
 191 tion (Li and Langhans, 2015). For example, Na, K-ATPase proteins are
 192 associated with various signaling molecules, including Src, phosphoinositide
 193 3-kinase (PI3K), and EGFR thereby activating a number of intracellular
 194 signaling pathways, including MAPK and Akt signaling, to modulate cell
 195 polarity, cell growth, cell motility and gene expression (Haas et al., 2002;
 196 Barwe et al., 2005). In addition, it has been hypothesized that targeting
 197 overexpressed Na(+)/K(+)-ATPase alpha subunits might open a new era in
 198 anticancer therapy and bring the concept of personalized medicine from aspi-
 199 ration to reality (Mijatovic et al., 2008). Our network analysis result further
 200 suggests that high frequency deletion of 17q21.32 might serve as an upstream
 201 regulating event for Na, K-ATPase proteins in breast cancer cells. Further
 202 study of this region could lead to new discoveries of tumor suppressor genes
 203 controlling ion channels and pumps (Litan and Langhans, 2015). Addition-
 204 ally, 17q21.32 acts in cis on LRRC59, which has been shown to modulate cell
 205 motility, aid in EMT, and is a necessary factor for oncogene FGF1 to enter

206 the nucleus for regulatory activity (Maurizio et al., 2016).

207 Loss of 5q is a common feature of basal-like breast tumors (Cancer Genome
208 Atlas Network et al., 2012). In the network inferred by **spaceMap**, a CNA of
209 a region on 5q34 is found to influence the largest number of proteins (Figure
210 3, upper-right). This observation is consistent with previously reported result
211 based on pairwise correlation analysis on the same data set (Mertins et al.,
212 2016). Applying GO enrichment analysis to the network module containing
213 the 5q34 CNA-hub reveals the biological process of “regulation of transcrip-
214 tion from RNA polymerase II promoter” is significantly enriched, including
215 the well-known breast cancer oncogenes ESR1, GATA3, FOXA1 and many
216 others. No doubt that gene transcription mediated by RNA polymerase II
217 (pol-II) is a key step in gene expression, as the dynamics of pol-II moving
218 along the transcribed region influence the rate and timing of gene expres-
219 sion. Specifically, in breast cancer cell lines, it has been confirmed that the
220 predominant genomic outcome of estrogen signaling is the post-recruitment
221 regulation of pol-II activity at target gene promoters, likely through specific
222 changes in pol-II phosphorylation (Kininis et al., 2009). Another recent work
223 also demonstrate that pol-II regulation is impacted during activation of genes
224 involved in the epithelial to mesenchymal transition (EMT), which when ac-
225 tivated in cancer cells can lead to metastasis (Samarakkody et al., 2015).
226 These findings together with our results from **spaceMap** analysis imply that
227 DNA copy number alterations of 5q34 plays important role in breast tumor
228 initiation and progression.

229 Mertins et al. (2016) reported 6 trans- association hubs at chromosomal
230 arm level, namely, 5q, 10p, 12, 16q, 17q, and 22q. **spaceMap** identified CNA-

hubs in all six arms except for 22q. On the other hand, **spaceMap** identified additional tran-hubs in 15q13.1-15.1, 11q13.5-14.1, 12q21.1. These details are provided in Table S.14. **spaceMap** further pinpointed new cis-regulation between the CNA-hub in 17q12 and MIEN1 as well as KAT2A. Migration and invasion enhancer 1 (MIEN1) is an important regulator of cell migration and invasion. In a recently reported study, MIEN1 is found to drive breast tumor cell migration by regulating cytoskeletal-focal adhesion dynamics, and targeting MIEN1 is suggested to be a promising means to prevent breast tumor metastasis (Kpetemey et al., 2016). KAT2A, also known as histone acetyltransferase GCN5, is reported to play an essential role in the HBXIP-enhanced migration of breast cancer cells by wound healing assay, and thus is also an important player in tumor metastasis of breast cancer (Li et al., 2015).

To have a more direct comparison with the marginal correlation based approach, we built a network (referred to as the marginal network) using the same set of nodes as in **prot-net** (Table 1) whose edges were determined by significant Pearson's correlation with global FDR control at 0.05. There are 2103 CNA hubs in the marginal network with 47.9 percent of them having only one degree. In contrast, there are 15 CNA hubs in **prot-net** and only one of them has degree being one. The mean degree of the CNA hubs in the marginal network is 4, while for **prot-net** it is 39. Thus **spaceMap** is more likely to be able to narrow down the region of potential cancer drivers. This is due to **spaceMap** targeting direct interactions instead of marginal correlations, as well as utilizing group selection techniques. Moreover, by the module analysis described in Section 4.4, **prot-net** yielded 45 significant

GO terms compared to 9 for the marginal network and thus is more functionally enriched. These observations imply that **spaceMap** is a useful addition to conventional pairwise correlation based analysis in integrating proteomics and CNA profiles and pinpointing important disease-relevant regulatory relationships.

Finally, among the CNA-protein edges in **prot-net**, the CNA profiles are positively correlated with their cis-regulated protein levels; whereas for trans-regulation, we did not observe a significant preference towards either positive regulation or negative regulation.

We also fit **scggm** to the CNA and protein levels of the BCPLS data set, but find evidence of high variability and instability. We first use 10-fold CV to choose **scggm**'s tuning parameters. However, this leads to a large number of protein-protein edges and very few CNA-protein edges (first column of Table S.6). This is consistent with the observations from the simulation results of Section 2.1 and is likely due to high FDR in edge detection and lack of power in CNA-hub detection. In order to facilitate comparison with **spaceMap**'s **prot-net**, we instead choose **scggm**'s tuning parameters such that the resulting **Boot.Vote** network would have a similar size as **prot-net**. This leads to a network with 967 protein-protein edges, 574 CNA-protein edges (third column of Table S.6). There are many more edges if **CV.Vote** instead of **Boot.Vote** had been applied under these same tuning parameters (second column of Table S.6). This again indicates instability of the inferred network topology due to excess variability and overfitting. On the contrary, network topology inferred by **spaceMap** is reasonably stable: The number of protein-protein edges and CNA-protein edges are 1147 and 772, respectively,

281 under `CV.Vote`; and 954 and 585 under `Boot.Vote`. We analyze `scggm`'s
282 `Boot.Vote` network in more detail in Section S.3.2.

283 2.2.2. *RNA-net* vs. *prot-net*

284 The protein and mRNA expressions are not jointly modeled due to limited
285 sample size. Instead, we apply `spaceMap` to learn a separate RNA network,
286 referred to as **RNA-net**. To facilitate comparison, `spaceMap` learned **RNA-net**
287 through `Boot.Vote` ($B = 1000$) in such a way to produce similar edge sizes
288 as **prot-net**; this resulted in 1010 RNA–RNA edges, 622 CNA–RNA edges,
289 and 14 CNA-hubs. The list of the top-ranked CNA-hubs are shown in Table
290 2 and the complete list of the 14 CNA-hubs are provided in Table S.9. Mod-
291 ule analysis reveals 13 modules (of size 15 or more) in **RNA-net**, with their
292 enriched GO terms annotated in Table S.10.

293 **RNA-net** and **prot-net** share 6 common CNA-hubs (see boldfaced lines
294 from Tables S.4 and S.9). Both identify the 17q12 amplicon as a major hub
295 with shared cis regulatory elements such as ERBB2, GRB7, and PNMT.
296 The common hub 5q34 has the largest out-degree in both networks. Other
297 common CNA are 10p15.1-15.3, 15q13.1-15.1, 16q22.1-22.2, and 8q21.2-22.1.
298 The CNA-hubs do not share many common targets, which is expected since
299 there are less than 16% of common nodes (i.e., nodes corresponding to the
300 same genes) in these two networks. There are 33 overlapping edges in to-
301 tal: 20 of them are CNA–expression edges, and 13 are expression–expression
302 edges.

303 **prot-net** is more functionally-enriched compared to **RNA-net**, having 11
304 out of 15 CNA-hubs belonging to a module with at least one enriched GO
305 term compared to only 2 out 17 for **RNA-net**. In addition, 45 GO terms

are significantly enriched in **prot-net** modules, whereas only 24 enriched GO terms are detected in **RNA-net** modules. GO terms enriched in both networks include (innate) immune response, collagen catabolism, and extracellular matrix (ECM) organization. The last two are interesting as abnormal collagen fibers in the ECM are known to play roles in invasive breast tumor activity (Grossman et al., 2016). The *GO-neighbor percentages* of CNA-hub neighborhoods also tend to be higher for **prot-net** (mean 63.25%) than **RNA-net** (mean 42.25%), as evidenced in Figure S.1.

2.3. OCPLS application

From Table 1, it can be seen that, compared with the breast cancer networks, the ovarian networks tend to have smaller CNA hubs. This is consistent with the marginal correlation based results from Mertins et al. (2016) and Zhang et al. (2016) for breast cancer and ovarian cancer, respectively. Moreover, the **prot-net** of ovarian cancer has 71 significant GO terms, whereas the **RNA-net** has none (Table S.12). This confirms the observation from the breast cancer application that the protein network tends to be more functionally enriched than the RNA network.

The network modules corresponding to the two leading CNA hubs — 20q11.22-.23 and 8q24.23-24.3 — in the ovarian CNA-protein network are illustrated in Figure S.7. Interestingly, two GO terms that are enriched in the two leading breast cancer CNA-hub modules, namely, RNA polymerase II promoter and ion transmembrane transport, are also enriched in these two ovarian cancer CNA-hub modules (compare Figures 3 and S.7). The differences are, in breast cancer network, RNA polymerase II promoter genes are regulated by CNA in 5q34; and ion transmembrane transport genes are

331 regulated by CNA in 17q21. These results suggest that crucial tumor related
332 biological processes are triggered by different genetic alternation mechanisms
333 in different types of cancers.

334 Among the four genes cis-regulated by the CNA-hub in 20q11.22-.23,
335 RPRB1B, a novel gene also called CREPT and K-h, belongs to the RNA
336 polymerase II promoter GO category. Specifically, RPRB1B increases cyclin
337 D1 transcription during tumorigenesis, through enhancing the recruitment of
338 RNAPII to the promoter region as well as chromatin looping (Lu et al., 2012).
339 Another recent study further suggests the crucial role of RPRB1B in promot-
340 ing repair of DNA double strand breaks and the potential of using RPRB1B
341 as a biomarker to facilitate patient-specific individualized therapies (Pati-
342 dar et al., 2016). Indeed, the specificity of the monoclonal antibody against
343 CREPT has been recently characterized for preparation of industrial produc-
344 tion (Ren et al., 2014). The fact that we successfully pin-point this important
345 protein through our network analysis convincingly demonstrates the utility
346 of **spaceMap** in revealing relevant and important biological information.

347 The other leading CNA-hub sits in 8q24.23-24.3, which is the only genome
348 region that have shown frequent focal chromosome copy number gains in all
349 four female cancer types, including ovarian, breast, endometrial and cervical
350 cancers, in a very recent Pan-Cancer study (Kaveh et al., 2016). However,
351 the functional consequences of copy number gain of this region remain largely
352 unclear. Could the result of **spaceMap** network give us insights of the bio-
353 logical role of this important CNA region? Indeed, in the inferred ovarian
354 CNA-protein network, we identified 11 cis-regulated proteins of this CNA-
355 hub. The fact that this CNA-hub has the largest number of cis-regulations

among all CNA-hubs in both the breast and ovarian CNA-protein networks also implies the uniqueness of this CNA region. Among the 11 cis-regulated proteins, three —TSTA3, NAPRT, and CYC1 — are from the Metabolic pathway. Specifically, TSTA3 controls cell proliferation and invasion and has been reported to exert a proto-oncogenic effect during carcinogenesis in breast cancer (Sun et al., 2016). NAPRT has been observed to promote energy status, protein synthesis and cell size in various cancer cells, and NAPRT-dependent NAD⁺ biosynthesis contributes to cell metabolism as well as DNA repair process, so that NAPRT has been recently suggested to be used to increase the efficacy of NAMPT inhibitors and chemotherapy (Piacente et al., 2017). CYC1 plays important roles in cell proliferation and comedo necrosis through elevating oxidative phosphorylation activities, and has been recently suggested to serve as a biomarker to predict poor prognosis in breast cancer patients (Han et al., 2016; Chishiki et al., 2017). All these are useful pieces of information to help to figure out the functional consequences of the amplification of the CNA-hub on 8q24.23-24.3, which then could lead to detection of novel drug targets or biomarkers for ovarian cancer.

3. Discussion

The proposed model **spaceMap** (Section 4.1) can successfully address many of the challenges inherent to learning networks from multiple -omic data types. Statistical efficiency is gained by discarding irrelevant interactions through a conditional graphical model framework. Moreover, pseudo-likelihood approximations and the MAP penalty increase power of CNA-hub

380 detection compared with a likelihood-based CG model `scggm`. This has been
 381 convincingly shown by the simulation results in Section 2.1 as well as the
 382 BCPLS and OCPLS applications in Sections 2.2 and 2.3. Providing biolog-
 383 ical interpretation is another challenge after a network is learned. For this
 384 purpose, we develop a network analysis toolkit that facilitates the researchers
 385 to interpret their results and integrates with visualization software (Section
 386 4.4).

387 We engineer the `spaceMap` R package to be computationally efficient.
 388 Model fitting steps are implemented with *Rcpp* and *RcppArmadillo* C++
 389 bindings to R (Eddelbuettel, 2013; Eddelbuettel and Sanderson, 2014). Model
 390 selection procedures `CV.Vote` and `Boot.Vote` leverage R’s parallel processing
 391 backends. Detailed documentation and vignettes of the `spaceMap` R pack-
 392 age and the network analysis toolkit are hosted on [https://topherconley.](https://topherconley.github.io/spacemap/)
 393 [github.io/spacemap/](https://topherconley.github.io/spacemap/). Details of the BCPLS application is illustrated in
 394 the *neta-bcpls* repository on GitHub ([https://topherconley.github.io/](https://topherconley.github.io/neta-bcpls/)
 395 [neta-bcpls/](https://topherconley.github.io/neta-bcpls/)).

396 In the applications of breast and ovarian cancers, protein level data re-
 397 sults in more functionally enriched networks than RNA expression data for
 398 both cancer types, suggesting that protein data could be more informative for
 399 characterizing functional consequences of genetic alterations. While differ-
 400 ent sets of CNA-hubs and network modules are identified in the breast and
 401 ovarian CNA-protein networks, respectively, the leading modules in both
 402 networks are enriched with genes from the same GO categories, namely, ion
 403 transmembrane transport and regulation from RNA polymerase II promoter.
 404 This suggests a hypothesis that, although different cancers show large tumor

405 heterogeneity in terms of genomic alterations, these distinct alteration events
 406 may eventually contribute to the same set of crucial biological processes.
 407 Therefore, identifying and characterizing the downstream crucial biological
 408 processes might be the key to design effective diagnosis and treatment strate-
 409 gies to overcome the challenges due to tumor heterogeneity in clinical prac-
 410 tice. And network-based-system-learning approaches, like the one proposed
 411 in this paper, would be essential for such a goal.

412 Due to the small sample sizes, here we focus only on the most robust
 413 signals in the data and our top priority has been to control false discovery
 414 rate of the inferred networks. Although we are not expecting to capture all
 415 important regulatory patterns in such a way, we can be reasonably confident
 416 with those that are identified. In the future, with more proteomics samples
 417 available for cancer studies, we expect that **spaceMap** will be able to draw
 418 more insights on driver genes and genomic events in cancer.

419 Since **spaceMap** infers conditional dependency relationships, we expect
 420 that the interactions inferred by **spaceMap** are more direct than those in-
 421 ferred by marginal analysis. Specifically, compared to the results of marginal
 422 analysis using the same data by **spaceMap**, we find that **spaceMap** is more
 423 advantageous in narrowing down to small genome regions as tran-hub and
 424 thus could shed more lights on regulatory mechanisms of CNA on protein
 425 or RNA. However, this is at the cost of a more complicated model and con-
 426 sequently demands both more samples and computational efforts to fit the
 427 model.

428 In principle, **spaceMap** may also be used to conduct eQTL analysis using
 429 protein levels or RNA expressions (as response) and SNV (as predictor). Due

430 to the large number of SNV, one may need to reduce the set of SNV through
431 filtering and/or grouping.

432 4. Materials and Methods

433 4.1. *spaceMap* Model

434 Graphical models provide compact and visually intuitive representations
435 of interactions (conditional dependency relationships) among a set of nodes
436 (random variables). For example, CNAs and protein levels may be the nodes,
437 while the edges may encode interactions among these molecular entities.
438 Graphical models carry an advantage over relevance networks based on pair-
439 wise correlations by being able to distinguish marginal dependency from con-
440 ditional dependency. For instance, protein_j and protein_k may be marginally
441 dependent because they are co-regulated by CNA_l . But after conditioning on
442 the effect of CNA_l , they may become conditionally independent. Thus the
443 interactions inferred by graphical models are more direct interactions com-
444 pared with those based on marginal statistics such as pairwise correlations.

The goal is to learn the graph structure (ie. the set of edges) based on the observed data. In the following, we use $\mathbf{x} = (x_1, \dots, x_P)^T$ to denote one type of nodes, e.g., CNAs, and $\mathbf{y} = (y_1, \dots, y_Q)^T$ to denote another type of nodes, e.g., protein levels. Let $\mathbf{z} = (\mathbf{x}^T, \mathbf{y}^T)^T$ and assume that the random vector $\mathbf{z}$ has mean $\boldsymbol{\mu} = (\boldsymbol{\mu}_x^T, \boldsymbol{\mu}_y^T)^T$ and a joint covariance matrix

$$\Sigma = \begin{pmatrix} \Sigma_{xx} & \Sigma_{xy} \\ \Sigma_{yx} & \Sigma_{yy} \end{pmatrix},$$

where $\boldsymbol{\mu}_x$, $\boldsymbol{\mu}_y$ are the mean vectors of $\mathbf{x}$ and $\mathbf{y}$, respectively; Σ_{xx} , Σ_{yy} are the covariance matrices of $\mathbf{x}$ and $\mathbf{y}$, respectively; and $\Sigma_{xy} = \Sigma_{yx}^T$ is the covariance

between $\mathbf{x}$ and $\mathbf{y}$. Furthermore, the inverse of the joint covariance matrix, referred to as the *concentration matrix*, can be partitioned accordingly:

$$\Sigma^{-1} := \Theta = \begin{pmatrix} \Theta_{xx} & \Theta_{xy} \\ \Theta_{yx} & \Theta_{yy} \end{pmatrix}.$$

445 The off-diagonal entries of Θ are proportional to the *partial correlations*,
 446 i.e., the correlations between pairs of variables after removing linear effects of
 447 the rest of the variables. Under Gaussianity, partial correlations are the same
 448 as conditional correlations and thus zero entries in Θ mean that the respec-
 449 tive pairs of random variables are conditionally independent given the rest
 450 of the variables. In contrast, a nonzero entry of Θ means conditional depen-
 451 dency and corresponds to an edge in the graph. Therefore, the goal of graph
 452 inference can be achieved by identifying nonzero entries of the concentration
 453 matrix Θ .

454 When there are two types of nodes, sometimes we are only interested in
 455 certain subsets of interactions. In the following, assume that we are only
 456 interested in the interactions among the $\mathbf{y}$ variables and those between the $\mathbf{y}$
 457 variables and the $\mathbf{x}$ variables, but not the interactions among the $\mathbf{x}$ variables.
 458 Then there is no need to learn the entire concentration matrix Θ . Note that
 459 for $l \neq q$, $\theta_y^{lq} = \Theta_{yy}(l, q)$ is proportional to ρ_y^{lq} which denotes the partial
 460 correlation between y_l and y_q given $\{x_p\}_{p=1}^P$ and $\{y_{q'} : q' \neq l, q\}$; and in
 461 parallel, $\theta_{xy}^{pq} = \Theta_{xy}(p, q)$ is proportional to ρ_{xy}^{pq} which denotes the partial
 462 correlation between y_q and x_p given $\{x_{p'} : p' \neq p\}$ and $\{y_{q'} : q' \neq q\}$.
 463 Therefore, we only need to elucidate the zero patterns of Θ_{yy} and Θ_{xy} . Models
 464 for such a purpose are referred to as conditional graphical (CG) models.

For simplicity of notation, hereafter, assume that the mean vectors $\boldsymbol{\mu}_x =$

$\mathbf{0}, \boldsymbol{\mu}_y = \mathbf{0}$. In Zhang and Kim (2014), it is assumed that given $\mathbf{x}$, the conditional distribution of $\mathbf{y}$ is :

$$\mathbf{y}|\mathbf{x} \sim N\left(-\Theta_{yy}^{-1}\Theta_{yx}\mathbf{x}, \Theta_{yy}^{-1}\right).$$

Parameters Θ_{yy} and Θ_{yx} are then learned by minimizing the negative conditional log-likelihood with ℓ_1 penalties on Θ_{xy}, Θ_{yy} to encourage sparsity. This method is called **scggm** (Sparse Conditional Gaussian Graphical Model).

In the following, we propose an alternative approach, called **spaceMap**, which uses regularized multivariate regression with sparsity- and hub-inducing penalties (Peng et al., 2010) to learn the zero patterns of Θ_{yy} and Θ_{xy} . Unlike **scggm**, **spaceMap** does not rely on the conditional Gaussianity assumption for model fitting.

Peng et al. (2009) show partial correlations can be an efficient parameterization for graphical model learning. This is done through the connection between partial correlations and the regression coefficients while regressing each variable to the rest of the variables. This formulation can also be motivated through pseudo-likelihood approximations. Peng et al. (2009) further show this regression-based approach achieves higher power in edge detection compared to a likelihood-based approach when the true network exhibits hub structures, which is often the case for a GRN.

In **spaceMap**, we extend this regression framework to learn CG models. Note that, while regressing y_q to the rest of the nodes, we have:

$$y_q = \sum_{l:l \neq q} \beta_{lq} y_l + \sum_{p=1}^P \gamma_{pq} x_p + \epsilon_q, \quad q = 1, \dots, Q, \quad (1)$$

where the residual ϵ_q is uncorrelated with $\{x_p\}_{p=1}^P, \{y_l : l \neq q\}$, and the

regression coefficients follow:

$$\beta_{lq} = \rho_y^{lq} \sqrt{\theta_y^{ll} / \theta_y^{qq}} = -\frac{\theta_y^{lq}}{\theta_y^{qq}}$$

$$\gamma_{pq} = \rho_{xy}^{pq} \sqrt{\theta_x^{pp} / \theta_y^{qq}} = -\frac{\theta_{xy}^{pq}}{\theta_y^{qq}}.$$

483 Since the diagonal entries $\theta_y^{qq} = \Theta_{yy}(q, q)$ are positive, identifying nonzero
 484 entries of Θ_{yy} and Θ_{xy} is equivalent to identifying nonzero regression coef-
 485 ficients in (1). Also note that, equation (1) holds without the Gaussianity
 486 assumption.

487 We propose to minimize the following penalized ℓ_2 loss criterion with
 488 respect to $\boldsymbol{\rho}_y = (\rho_y^{12}, \rho_y^{13}, \dots, \rho_y^{Q-1, Q})^T$, $\boldsymbol{\theta}_y = (\theta_y^{qq})_{q=1}^Q$, and $\boldsymbol{\Gamma}_{P \times Q} = ((\gamma_{pq}))$:

$$\begin{aligned} L(\boldsymbol{\rho}_y, \boldsymbol{\theta}_y, \boldsymbol{\Gamma}; \lambda_1, \lambda_2, \lambda_3) = & \\ \frac{1}{2} \sum_{q=1}^Q & \left\| \mathbf{Y}_q - \sum_{l:l \neq q} \rho_y^{lq} \sqrt{\frac{\theta_y^{ll}}{\theta_y^{qq}}} \mathbf{Y}_l - \sum_{p=1}^P \gamma_{pq} \mathbf{X}_p \right\|_2^2 \\ & + \lambda_1 \|\boldsymbol{\rho}_y\|_1 + \lambda_2 \sum_{p=1}^P \|\boldsymbol{\Gamma}_p\|_1 + \lambda_3 \sum_{p=1}^P \|\boldsymbol{\Gamma}_p\|_2, \end{aligned}$$

489 where $\mathbf{Y}_q = (y_q^1, \dots, y_q^N)^T$ and $\mathbf{X}_p = (x_p^1, \dots, x_p^N)^T$ are observed samples
 490 of the nodes y_q and x_p , respectively; $\boldsymbol{\Gamma}_p$ denotes the p th row of $\boldsymbol{\Gamma}$; $\|\cdot\|_1, \|\cdot\|_2$
 491 denote ℓ_1 and ℓ_2 norms, respectively; and $\lambda_1 > 0, \lambda_2 > 0, \lambda_3 > 0$ are tuning
 492 parameters.

493 The ℓ_1 norm penalty on $\boldsymbol{\rho}_y$ encourages sparsity in $y - y$ interactions:
 494 When λ_1 is sufficiently large, only some pairs of y nodes (but not all) will
 495 have the corresponding partial correlations estimated to be nonzero, thus
 496 having an edge in the inferred $y - y$ network. By imposing regularization

on the partial correlations ρ_y instead of on the $y - y$ regression coefficients β_{lq} 's, we not only reduce the number of parameters by nearly a half, but also ensure the *sign consistency*, due to $\rho_y^{lq} = \rho_y^{ql}$. Moreover, since ρ_y^{lq} are on the same scale, the amount of regularization is comparable for different pairs of y nodes.

The combination of ℓ_1 norm and ℓ_2 norm penalties imposed on the $x - y$ regression coefficients $\mathbf{\Gamma}$ encourages both sparsity in $x - y$ interactions as well the detection of x -hubs: The ℓ_1 penalty induces overall sparsity of x nodes influencing the y nodes, while the ℓ_2 penalty encourages the selection of x nodes that have connections with many y nodes (i.e, x -hubs).

This model is referred to as **spaceMap** as it may be viewed as a hybrid of the **space** model (Peng et al., 2009) and the **remMap** model (Peng et al., 2010). Specifically, when $\lambda_2 = \lambda_3 = 0$, **spaceMap** reduces to a partial **space** model where only the $y - y$ and $x - y$ interactions are being fitted (but not the $x - x$ interactions). On the other hand, the penalties on $\mathbf{\Gamma}$ is the same as the **MAP** penalty used in the **remMap** model which encourages the selection of x -hubs. **spaceMap** can be fitted through a *coordinate descent algorithm* similarly as in **space** and **remMap** by alternatively updating ρ_y , θ_y and $\mathbf{\Gamma}$.

For tuning parameters selection, we use K-fold cross validation (CV) to choose the optimal tuning parameters and adopt a sequential search strategy to efficiently navigate the 3D tuning grid. More details are given in section S.1 of the Supplementary Material. We then apply the **CV.Vote** procedure proposed in Peng et al. (2010) where only edges appearing in a majority of the cross validation networks are retained. The purpose of **CV.Vote** is to reduce the number of false positive edges. In application to real data, however, the

false discovery rate (FDR) could still be high even after **CV.Vote** due to low signal-to-noise ratios and complicated noise structure. Therefore, we also consider a bootstrap-based aggregation procedure where we fit a network on each of the B bootstrap resamples of the data. We then only retain edges appearing in at least half of these networks (i.e., using a majority voting rule). We refer to this procedure as **Boot.Vote**. A similar strategy has been studied in Li et al. (2013) and is shown to be effective in reducing FDR. Compared to **CV.vote**, as shown by the simulation results, **Boot.Vote** better controls FDR at the expense of computation and a small cost in power.

4.2. Simulation

We conduct two simulation studies to examine how well **spaceMap**, **space**, and **scggm** perform at network inference. In each simulation, one hundred independent replicates with sample size $N = 250$ are generated from a zero-mean multivariate Gaussian distribution. Each method is applied to each replicate to infer a network, where model tuning parameters are selected through 10-fold cross validation. The final network inference uses aggregation techniques **CV.Vote** and **Boot.Vote** to control the false discovery rate (FDR); The inferred networks are then compared with the true network to obtain power and FDR in terms of edge detection across all replicates. Moreover, *Matthew's correlation coefficient (MCC)* is calculated to summarize the confusion matrix (Baldi et al., 2000); or in other words, the power-FDR tradeoff. MCC ranges from -1 to 1, where 1 corresponds to perfect match and -1 corresponds to perfect mismatch.

In the first simulation, referred to as **hub-net**, we generate a network with $P = 35$ CNA nodes, $Q = 485$ protein nodes and 577 total edges, following the

547 hub network simulation from Peng et al. (2009) (with small modifications).
 548 Among the CNA nodes, 15 of them have at least 11 edges (CNA-hubs), and
 549 the rest has no edge (background nodes). The protein–protein network con-
 550 sists of five disjoint modules with around 100 nodes in each module since
 551 many real-world large networks exhibit modular structures. Moreover, the
 552 node degree follows a power-law distribution. The non-zero partial corre-
 553 lations fall in $(-0.67, -0.1] \cup [0.1, 0.67)$, with two modes around -0.28 and
 554 0.28, respectively. Details on how the partial correlations are generated can
 555 be found in the Supplementary Material.

556 In the second simulation, referred to as **power-net**, we generate a network
 557 with more complicated structure: It has about 10 times as many non-hub
 558 CNA nodes and each module has roughly double the number of edges. This
 559 renders a power law network with the power parameter approximately 2.6.
 560 Specifically, there are 700 nodes ($P = 210$ CNA nodes and $Q = 490$ pro-
 561 tein nodes) and 1257 edges. There are 10 CNA-hubs perturbing a subset of
 562 the 490 proteins. Among the 200 non-hub CNA nodes, 28 are confounders,
 563 meaning that they are correlated with a CNA-hub; 172 are background nodes,
 564 meaning that they are *not* connected to the rest of the CNA nodes and the
 565 protein nodes, although the background nodes are correlated among them-
 566 selves. Further details of network generation and construction of the corre-
 567 sponding precision matrix Θ are given in Supplementary Section S.2.

568 4.3. Application: breast cancer and ovarian cancer proteogenomics

569 We apply **spaceMap** to the BCPLS data (Mertins et al., 2016) and the
 570 OCPLS data (Zhang et al., 2016) to demonstrate **spaceMap**’s ability in
 571 identifying major functional consequences of DNA copy number alterations

572 in a sample-size limited and biologically-heterogeneous context.

573 Protein abundance levels of 77 breast cancer tumor samples were obtained
574 from the supplementary table of (Mertins et al., 2016). Protein levels of 174
575 ovarian cancer tumor samples were obtained from the supplementary table 2,
576 sheet 2, of (Zhang et al., 2016). The corresponding level-three RNA-seq and
577 segmented DNA copy number profiles were downloaded from TCGA web
578 site (<http://tcga-data.nci.nih.gov/tcga/>). Global normalization were then
579 performed to both the protein level and gene expression data sets.

580 Due to the relatively small sample sizes, genome-wide network reconstruc-
581 tion is not advisable. Instead, we focus on the most robust signals afforded
582 in the data. This is accomplished by filtering out features with high missing
583 rate and then selecting the most highly variable features, resulting in 1595
584 proteins and 1657 RNA expressions for breast cancer and 2097 proteins and
585 2236 RNAs for ovarian cancer, respectively. We also clustered CNAs into
586 1662 and 1349 larger genomic segments for breast cancer and ovarian can-
587 cer, respectively, using the fixed order clustering method proposed in Wang
588 (2010), which helps to reduce multicollinearity among CNA features due to
589 physical proximity (see section S.8).

590 4.4. *Network interpretation toolkit*

591 To facilitate biological interpretation, we built a toolkit to derive bio-
592 logical insights from the inferred networks. The application of the toolkit
593 is illustrated under 'Network Analysis' of Figure 1. The toolkit utilizes R
594 package *igraph* (Csardi and Nepusz, 2006) to map user-supplied annotations
595 onto the network and perform a rich suite of network analysis options. If
596 the annotation contains gene coordinates, the toolkit also identifies cis/trans

regulatory information. In our analysis, we define cis regulation to be within a $\pm 4\text{Mb}$ window. In literature, there is not a standard window size for defining cis regulation. A large range of window sizes varying from 100k to 10Mb has been used in the past (Blackburn et al., 2015). Here we chose 4Mb as a trade-off between an overly liberal cis window and the risk of missing a cis regulation. The toolkit can conduct two types of analysis, one based on hubs and another based on modules.

In the hub analysis, we define any CNA node with at least one edge to an expression node (protein or RNA) as a *CNA-hub* and its corresponding *CNA-hub neighborhood* consists of all expression nodes that are directly connected to the CNA-hub by an edge. The toolkit prioritizes CNA-hubs based on a stability metric by calculating the average degree rank across the networks built on bootstrap resamples of the data (by the **Boot.Vote** procedure). Higher priority CNA-hubs have higher average rank, meaning that they have consistently high degree across the network ensemble. Next, the toolkit reports the number of cis/trans regulations found in each CNA-hub neighborhood and the number of protein/RNA nodes in cis with this CNA-hub from the entire network (referred to as *potential # of cis regulations*); see Table 2.

The hub analysis is enhanced if the annotation includes a functional mapping from databases like Gene Ontology (GO) to expression nodes. In our analysis, we construct a GO universe where each GO biological process term is required to have at least 15 participating genes in the network analysis, but no more than 300; for breast cancer, there are 167 and 129 biological processes meeting this criteria for protein and RNA, respectively; while for

ovarian cancer there were 184 (protein) and 193 (RNA) biological processes. The toolkit reports the functional enrichment of a CNA-hub neighborhood through its *GO-neighbor percentage*: the percent of expression nodes in the neighborhood that share a common GO term with at least one other expression node neighbor; see Figure S.2.

Regarding module analysis, the toolkit evaluates which GO terms are significantly enriched in pre-specified network modules. In our analysis of the BCPLS data, we detect modules based on edge-betweenness (Newman and Girvan, 2004) using *igraph* — but other module-finding algorithms can be used. Modules with at least 15 nodes are subjected to GO enrichment testing through a hypergeometric test. GO terms are required to have at least 5 members in a module to be enriched. The FDR of GO enrichment is controlled at 0.05 (Benjamini and Hochberg, 1995). Significantly-enriched modules, as well as any CNA-hub members of the modules, are organized into an accessible report as in Table S.5.

Taken together, the toolkit enables fast network analysis with well-organized results that is easily exported to other tools like *Cytoscape* (Shannon *et al.*, 2003), which rendered Figure 3.

5. Acknowledgments

Data used in this publication were generated by the National Cancer Institute Clinical Proteomic Tumor Analysis Consortium (CPTAC). This work has been supported by the Floyd and Mary Schwall Fellowship in Medical Research and grants NIH R01-GM082802, R01-GM108711, R01-CA189532 and NSF DMS-1148643. This work was also partly supported by grant U24

646 CA 210093, from the National Cancer Institute Clinical Proteomic Tumor
647 Analysis Consortium (CPTAC).

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Figure 1: **spaceMap integrative analysis pipeline**. Predictors (e.g., CNA) and responses (e.g., protein abundance) data are inputs to the model fitting stage, where the model is tuned by cross validation and aggregated across 1000 bootstrap ensemble networks through the Boot.Vote procedure. The Boot.Vote network is input to the network analysis stage, where biological function is layered onto the network. Finally the network is visualized with Cytoscape.

Figure 2: **hub-net simulation**: Edge-detection performance summarized by MCC, power, and FDR, across 100 replicates. The overall performance is further decomposed into response subnetwork PROT-PROT and the predictor→response subnetwork CNA→PROT. `spaceMap.CV`, `space` and `scggm` are learned under `CV.Vote` and `spaceMap.boot` is learned under `Boot.Vote`. All tuning parameters are chosen by 10-fold CV.

Table 1: Summary statistics of **prot-net** and **RNA-net** by **spaceMap**. For CNA-hubs and GO-neighbor percentage, statistics are computed on CNA-hubs with at least degree 10 (prior to manually merging a few highly correlated CNA-hubs).

Statistic	Breast cancer		Ovarian cancer	
	prot-net	RNA-net	prot-net	RNA-net
# CNA nodes	1662	1662	1349	1349
# expr nodes	1595	1657	2097	2236
# expr-expr edges	954	1010	1657	1735
# CNA-expr edges	585	622	1284	1231
# CNA-hubs (median size)	11 (36)	9 (55)	6 (10)	44 (17.5)
median GO-neighbor %	71.43	57.90	50.0	52.77

Figure 3: **BCPLS application:** Three GO-enriched modules from spaceMap prot-net . Large circles denote proteins belonging to enriched GO terms: cell proliferation (blue), transcription from RNA polymerase II promoter (orange) and ion transmembrane transport (purple). Rectangles denote CNA-hubs.

Table 2: **BCPLS/OCPLS applications:** Top three CNA-hubs for **prot-net** and **RNA-net** of breast cancer and ovarian cancer, respectively. Within each CNA-hub, we report the number of cis- and trans- edges and the potential number of cis regulations (i.e., the number of protein/RNA nodes in cis with this CNA-hub from the entire network). We also list which genes are found to be in cis with the CNA-hub.

Cytoband	# cis/ # trans	Potential # cis	cis- proteins
Breast cancer			
prot-net			
17q21.32 (46-46 Mb)	1 / 98	14	LRRC59
5q34 (160-170 Mb)	0 / 129	0	–
17q12 (38-38 Mb)	5 / 47	34	ERBB2, GRB7, MIEN1 PNMT, KAT2A
Breast cancer			
RNA-net			
5q34 (160-170 Mb)	0 / 189	4	–
10p15.1-15.3 (0.42-4 Mb)	0 / 55	7	–
17q12 (38-38 Mb)	4 / 36	24	ERBB2, GRB7, PNMT, TCAP
Ovarian cancer			
prot-net			
22q13.1-.31 (39-46 Mb)	5/5	26	TSPO, ACO2, TTLL12, CYB5R3, ARFGAP3,
20q11.22-.23 (32-36 Mb)	3/16	20	NFS1, RPRD1B, CPNE1
8q24.23-24.3 (140-150 Mb)	11/3	16	C8orf82, GSDMD, CYC1, TSTA3,KHDRBS3, THEM6, OPLAH, PYCR3, EPPK1, MROH1, NAPRT
Ovarian cancer			
RNA-net			
22q13.1-13.31 (39-46 Mb)	3 / 103	11	KDELR3, APOBEC3B, APOL6
20q11.22-11.23 (32-36 Mb)	1 / 103	3	ID1
8q22.1-23.3 (98-120 Mb)	3 / 46	11	NCALD, TNFRSF11B, TRPS1