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Guiding dose selection of monoclonal antibodies using a new parameter (AFTIR) for characterizing ligand binding systems

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Abstract Guiding the dose selection for monoclonal antibody oncology drugs is often done using methods for predicting the receptor occupancy of the drug in the tumor. In this manuscript, previous work on characterizing target inhibition at steady state using the AFIR metric [1] is extended to include a “target-tissue” compartment and the shedding of membrane-bound targets. A new potency metric AFTIR (Average Free Tissue target to Initial target ratio at steady state) is derived, and it depends on only four key quantities: the equilibrium binding constant, the fold-change in target expression at steady state after binding to drug, the biodistribution of target from circulation to target tissue, and the average drug concentration in circulation. The AFTIR metric is useful for guiding dose selection, for efficiently performing sensitivity analyses, and for building intuition for more complex target mediated drug disposition models. In particular, reducing the complex, physiological model to four key parameters needed to predict target inhibition helps to highlight specific parameters that are the most important to estimate in future experiments to guide drug development.

Graphical Abstract

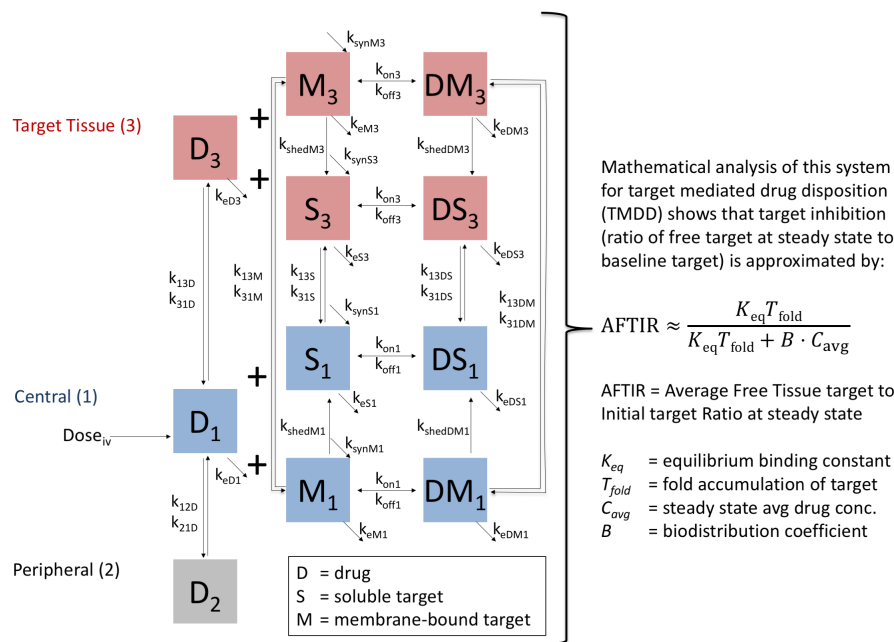


Fig. 1 Graphical Abstract

1 Introduction

During biologic drug development, prediction of target engagement at the site of action plays a critical role in dose regimen selection [2]. Because target engagement measurements at the site of action are often impossible to obtain, model-based predictions of target engagement at the site of action are often used to help justify the dose regimen selection. The methods used to predict target engagement vary significantly in their assumptions and in their level of complexity. For example, consider the model-based dose selection of pembrolizumab and atezolizumab.

For the PD-1 inhibitor pembrolizumab, a physiologically based model for antibody distribution and target engagement was developed to predict the dose needed to achieve target engagement and tumor suppression [3]. This model involved many assumptions about a large number of parameters and how these parameters scale from mice to humans. For the PD-L1 inhibitor atezolizumab, a much simpler approach was taken to guide the dosing regimen [4]. The tumor biodistribution coefficient (B) and in vivo binding affinity (K_d) were chosen based on preclinical data. The steady state trough concentration (C_{trough}) was estimated from clinical observations. The receptor occupancy (RO) formula in Equation 1 was then used to identify the dosing regimen needed to achieve 95% target occupancy. This approach made fewer assumptions about model parameters than in [3]. However, in choosing this simple model, many implicit assumptions were made about the system. For example, this simple model assumes that the rate of PD-L1 internalization does not change when it is bound to atezolizumab.

$$RO = B \cdot C_{\text{trough}} / (B \cdot C_{\text{trough}} + K_d) \quad (1)$$

The complex, mechanistic model used for pembrolizumab, captures more details of the underlying physiological processes. However, this model was more difficult to analyze due to its complexity; it also had a large number of unknown parameters which were difficult to estimate. The simple model used for atezolizumab was easier to analyze and had fewer unknown parameters to estimate. However this model required certain implicit assumptions which do not necessarily hold.

In this paper, a mathematical analysis of a physiologically-based model for drug distribution and target turnover is performed to derive a simple potency factor for characterizing target engagement. This theoretical calculation is validated using simulations of the model. All assumptions made in deriving this formula are explicitly stated. This paper extends previous work that focused on target engagement in circulation, as characterized by the Average Free target to Initial target Ratio (AFIR) at steady state in circulation [1].

2 Theory

In this section, an expression for the Average Free Tissue target to Initial target Ratio in tissue (AFTIR) is derived for the model in Figure 2.

2.1 Model Description

The model in Figure 2 is based on the standard target mediated drug disposition (TMDD) model [5], where a drug (D) binds its target. The model is extended to include the following processes:

- Shedding of the membrane-bound target (M) to form soluble target (S).
- Binding of the drug to both the membrane-bound target and the soluble target to form complexes DM and DS , respectively.
- Distribution of drug, target, and complexes from central (1) to tissue (3) compartment via either passive processes (soluble target) or active processes such as cell-trafficking (membrane-bound target).

As with the standard TMDD model, the peripheral compartment (2) contains the drug only; it is included so that the two-compartment pharmacokinetics of the drug can be described. The ordinary differential equations for describing this system are given by Equations (2) - (12).

$$\begin{aligned} \frac{dD_1}{dt} = & \frac{1}{V_C} \text{Dose}_{iv}(t) - k_{12D}D_1 + \frac{V_{D_2}}{V_{D_1}}k_{21D}D_2 - k_{13D}D_1 \\ & + \frac{V_{D_3}}{V_{D_1}}k_{31D}D_3 - k_{eD_1}D_1 - k_{on1}D_1 \cdot S_1 + k_{off1}(DS_1) \\ & - k_{on1}D_1 \cdot M_1 + k_{off1}(DM_1) \end{aligned} \quad (2)$$

$$\frac{dD_2}{dt} = k_{12D} \frac{V_{D_1}}{V_{D_2}} D_1 - k_{21D}D_2 \quad (3)$$

$$\begin{aligned} \frac{dD_3}{dt} = & \frac{V_{D_1}}{V_{D_3}}k_{13D}D_1 - k_{31D}D_3 - k_{eD_3}D_3 - k_{on3}D_3 \cdot M_3 + k_{off3}(DM_3) \\ & - k_{on3}D_3 \cdot S_3 + k_{off3}(DS_3) \end{aligned} \quad (4)$$

$$\begin{aligned} \frac{dM_1}{dt} = & k_{synM_1} - k_{shedM_1}M_1 - k_{13M}M_1 + \frac{V_{M_3}}{V_{M_1}}k_{31M}M_3 - k_{eM_1}M_1 \\ & - k_{on1}D_1 \cdot M_1 + k_{off1}(DM_1) \end{aligned} \quad (5)$$

$$\begin{aligned} \frac{dM_3}{dt} = & k_{synM_3} - k_{shedM_3}M_3 + \frac{V_{M_1}}{V_{M_3}}k_{13M}M_1 - k_{31M}M_3 - k_{eM_3}M_3 \\ & - k_{on3}D_3 \cdot M_3 + k_{off3}(DM_3) \end{aligned} \quad (6)$$

$$\begin{aligned} \frac{dS_1}{dt} = & k_{synS_1} + k_{shedM_1}M_1 - k_{13S}S_1 + \frac{V_{S_3}}{V_{S_1}}k_{31S}S_3 - k_{eS_1}S_1 \\ & - k_{on1}D_1 \cdot S_1 + k_{off1}(DS_1) \end{aligned} \quad (7)$$

$$\begin{aligned} \frac{dS_3}{dt} = & k_{synS_3} + k_{shedM_3}M_3 + \frac{V_{S_1}}{V_{S_3}}k_{13S}S_1 - k_{31S}S_3 - k_{eS_3}S_3 \\ & - k_{on3}D_3 \cdot S_3 + k_{off3}(DS_3) \end{aligned} \quad (8)$$

$$\begin{aligned} \frac{d(DM_1)}{dt} = & -k_{shedDM_1}DM_1 - k_{13DM}(DM_1) + \frac{V_{DM_3}}{V_{DM_1}}k_{31DM}(DM_3) \\ & - k_{eDM_1}DM_1 + k_{on1}D_1 \cdot M_1 - k_{off1}(DM_1) \end{aligned} \quad (9)$$

$$\begin{aligned} \frac{d(DM_3)}{dt} = & -k_{shedDM_3}DM_3 + \frac{V_{DM_1}}{V_{DM_3}}k_{13DM}(DM_1) - k_{31DM}(DM_3) \\ & - k_{eDM_3}DM_3 + k_{on3}D_3 \cdot M_3 - k_{off3}(DM_3) \end{aligned} \quad (10)$$

$$\begin{aligned} \frac{d(DS_1)}{dt} = & k_{shedDM_1}DM_1 - k_{13DS}DS_1 + \frac{V_{DS_3}}{V_{DS_1}}k_{31DS}DS_3 \\ & - k_{eDS_1}(DS_1) + k_{on1}D_1 \cdot S_1 - k_{off1}(DS_1) \end{aligned} \quad (11)$$

$$\begin{aligned} \frac{d(DS_3)}{dt} = & k_{shedDM_3}DM_3 + \frac{V_{DS_1}}{V_{DS_3}}k_{13DS}DS_1 - k_{31DS}DS_3 \\ & - k_{eDS_3}(DS_3) + k_{on3}D_1 \cdot S_3 - k_{off1}(DS_3) \end{aligned} \quad (12)$$

The initial conditions for all variables are zero except for the free target concentrations M_1 , M_3 , S_1 , S_3 . The equations used to determine these four initial concentrations are provided in Appendix A.1.1.

2.2 AFTIR derivation

2.2.1 AFTIR definition

Average Free Tissue target to Initial target Ratio (AFTIR) is defined as

$$\text{AFTIR} := \frac{1}{\tau} \int_{t_{ss}}^{t_{ss}+\tau} \frac{T_3(t)}{T_{30}} dt = \frac{T_{3\text{avg,ss}}}{T_{30}} = \left(\frac{T_{3\text{avg,ss}}}{T_{3\text{tot,ss}}} \right) \left(\frac{T_{3\text{tot,ss}}}{T_{30}} \right). \quad (13)$$

This equation applies for both membrane-bound (M) and soluble (S) targets, where $T_3(t)$ is the time series target concentration in the tumor compartment, T_{30} is the baseline target, $T_{3\text{avg,ss}}$ is the average free target concentration at steady state, and $T_{3\text{tot,ss}}$ denotes the total target concentration at steady state. AFTIR gives a measure of target inhibition in the tissue of interest (compartment 3) where the lower the AFTIR value, the greater the inhibition. The objective of this section is to derive the following estimate for AFTIR:

$$\text{AFTIR} \approx \frac{K_{\text{eq}} \cdot T_{\text{fold}}}{K_{\text{eq}} \cdot T_{\text{fold}} + B \cdot C_{\text{avg}}}, \quad (14)$$

where K_{eq} is an equilibrium constant measuring how fast the drug and target bind to form complexes, T_{fold} is the fold-change in the target levels at steady state compared to baseline, B is the biodistribution coefficient (i.e. the fraction of the drug from circulation that is found in the tissue of interest), and C_{avg} is the average drug concentration in circulation. Expressions for each of these terms are derived below.

2.2.2 K_{eq} definition

Three different equilibrium constants are defined below. (1) *The quasi-equilibrium approximation* for both membrane and soluble target is [6]

$$K_{\text{d}} := \frac{k_{\text{off}3}}{k_{\text{on}3}} \quad (15)$$

(2) *The quasi-steady state approximation* for soluble targets is [6]

$$K_{\text{ss,sol}} := \frac{k_{\text{off}3} + k_{\text{e}DS3}}{k_{\text{on}3}}. \quad (16)$$

For membrane-bound targets, the formula is similar, though shedding needs to be taken into account as well:

$$K_{\text{ss,mem}} := \frac{k_{\text{off}3} + k_{\text{e}DM3} + k_{\text{shed}DM3}}{k_{\text{on}3}}. \quad (17)$$

(3) A new equilibrium constant is introduced in this paper, called the *quasi-steady-state with distribution constant*, denoted K_{ssd} . This new equilibrium constant outperforms K_{d} and K_{ss} in terms of accuracy of approximating AFTIR.

The derivation of K_{ssd} for membrane-bound targets is shown below, and a similar process is followed for the soluble target version. To begin, assume a constant infusion of drug and that the system has reached steady state. Setting Equation (10) to zero and rearranging terms gives

$$k_{\text{on}3}D_3 \cdot M_3 = k_{\text{shed}DM_3}(DM_3) + k_{31DM}(DM_3) + k_{eDM_3}(DM_3) + k_{\text{off}3}(DM_3) + \frac{V_{DM_1}}{V_{DM_3}}k_{13DM}(DM_1) \quad (18)$$

Dividing each side by $k_{\text{on}3} \cdot DM_3$ gives

$$\frac{D_3 \cdot M_3}{DM_3} = \frac{k_{\text{shed}DM_3} + k_{31DM} + k_{eDM_3} + k_{\text{off}3}}{k_{\text{on}3}} + \frac{V_{DM_1}}{V_{DM_3}} \frac{DM_1}{DM_3} \frac{k_{13DM}}{k_{\text{on}3}}. \quad (19)$$

We then define K_{ssd} (for membrane-bound target and soluble target) as

$$K_{\text{ssd},\text{mem}} := \frac{k_{\text{shed}DM_3} + k_{31DM} + k_{eDM_3} + k_{\text{off}3}}{k_{\text{on}3}}, \quad (20)$$

$$K_{\text{ssd},\text{sol}} := \frac{k_{31DS} + k_{eDS} + k_{\text{off}3}}{k_{\text{on}3}}. \quad (21)$$

Substituting Equation (20) into Equation (19) gives

$$\begin{aligned} \frac{D_3 \cdot M_3}{DM_3} &= K_{\text{ssd},\text{mem}} + \frac{V_{DM_1}}{V_{DM_3}} \frac{DM_1}{DM_3} \frac{k_{13DM}}{k_{\text{on}3}} \\ &= K_{\text{ssd},\text{mem}} + \frac{\text{Amt}_{DM_1}}{\text{Amt}_{DM_3}} \frac{k_{13DM}}{k_{\text{on}3}}, \end{aligned}$$

where $\text{Amt}_{DM_1} = V_{DM_1} \cdot DM_1$ is the amount of complex in the central compartment, and $\text{Amt}_{DM_3} = V_{DM_3} \cdot DM_3$ is the amount of complex in the tissue compartment. If the membrane-bound target is unable to move to the central compartment (i.e., $k_{13DM} = k_{31DM} = 0$), or if the amount of complex is much larger in the tissue than in circulation such that $\text{Amt}_{DM_1}/\text{Amt}_{DM_3} \approx 0$, then

$$\frac{D_3 \cdot M_3}{DM_3} = K_{\text{ssd},\text{mem}}. \quad (22)$$

And similarly for soluble targets,

$$\frac{D_3 \cdot S_3}{DS_3} = K_{\text{ssd},\text{sol}}. \quad (23)$$

Regardless of which K_{eq} is used, the following approximation is assumed to hold:

$$K_{\text{eq}} = \frac{D_3 \cdot T_3}{DT_3} \quad (24)$$

2.2.3 T_{fold} , B , and C_{avg} definition

The total target in tissue is defined as $T_{3\text{tot}} := T_3 + DT_3$. The fold-accumulation of the target in tissue at steady state is defined as

$$T_{\text{fold}} := \frac{T_{3\text{tot,ss}}}{T_{30}}. \quad (25)$$

The analytical formula for T_{fold} is derived in Appendix (A.1).

For large drug concentrations at steady state, the biodistribution coefficient (B) gives the the ratio of the drug concentration in tissue to that in circulation. The average steady state circulating concentration is defined as $C_{\text{avg}} := D_{1\text{avg,ss}}$. Thus, the biodistribution coefficient can also be defined as,

$$B := \frac{D_{3\text{avg,ss}}}{D_{1\text{avg,ss}}} = \frac{D_{3\text{avg,ss}}}{C_{\text{avg}}}. \quad (26)$$

The analytical formula for B is derived in Appendix (A.2).

2.2.4 Putting it all together

Using the definitions of $T_{3\text{tot}}$ and K_{eq} , substituting the equation $DT_3 = T_{3\text{tot}} - T_3$ into the equation $K_{\text{eq}} = D \cdot T / (DT)$, and solving for $T_3 / T_{3\text{tot}}$ gives

$$\frac{T_3}{T_{3\text{tot}}} = \frac{K_{\text{eq}}}{K_{\text{eq}} + D_3} \approx \frac{K_{\text{eq}}}{D_3} \approx \frac{K_{\text{eq}}}{D_{3\text{tot}}}. \quad (27)$$

The first approximation holds when $D_3 \gg K_{\text{eq}}$, and the second approximation holds when $D_{3\text{tot}} \approx D_3$, which occurs when drug is dosed in vast molar excess to the target, as is the case for most monoclonal antibody (mAb) drugs at the approved dosing regimen.

Using Equations (25) and (27) gives

$$\frac{T_3}{T_{30}} = \left(\frac{T_3}{T_{3\text{tot}}} \right) \left(\frac{T_{3\text{tot}}}{T_{30}} \right) \approx \frac{K_{\text{eq}} \cdot T_{\text{fold}}}{D_{3\text{tot}}}. \quad (28)$$

Integrating this ratio over one dosing cycle at steady state gives

$$\text{AFTIR} = \frac{1}{\tau} \int_{t_{\text{ss}}}^{t_{\text{ss}}+\tau} \frac{T_3(t)}{T_{30}} dt \approx \frac{1}{\tau} \int_{t_{\text{ss}}}^{t_{\text{ss}}+\tau} \frac{K_{\text{eq}} \cdot T_{\text{fold}}}{D_{3\text{tot}}(t)} dt \quad (29)$$

When the drug is given as an infusion at a rate Dose/τ , then the steady-state drug concentration is a constant ($D_{3\text{tot,ss}}$), giving

$$\text{AFTIR} \approx \frac{K_{\text{eq}} \cdot T_{\text{fold}}}{D_{3\text{avg,ss}}}. \quad (30)$$

Substituting the biodistribution expression from Equation (26) gives what we call a simple expression for AFTIR.

$$\text{AFTIR}_{\text{simple}} \approx \frac{K_{\text{eq}} \cdot T_{\text{fold}}}{B \cdot C_{\text{avg}}}. \quad (31)$$

2.2.5 TEC_{50} definition

In deriving the above formula for the AFTIR metric, which we call the “simple” AFTIR formula, large drug concentrations are assumed. However, for arbitrarily small drug concentrations, $AFTIR_{\text{simple}}$ is unbounded:

$$\lim_{\text{Dose} \rightarrow 0} AFTIR_{\text{simple}} = \infty.$$

Realistically, AFTIR should approach one for arbitrarily small drug concentrations since the average free tissue target at steady state should approach the baseline tissue target concentration. Motivated by [7], we then modify the AFTIR approximation by adding an additional factor to the denominator:

$$AFTIR \approx \frac{K_{\text{eq}} \cdot T_{\text{fold}}}{K_{\text{eq}} \cdot T_{\text{fold}} + B \cdot C_{\text{avg}}} = \frac{TEC_{50}}{TEC_{50} + B \cdot C_{\text{avg}}}, \quad (32)$$

where the approximate concentration for 50% target engagement (TEC_{50}) is given by

$$TEC_{50} := K_{\text{eq}} \cdot T_{\text{fold}}. \quad (33)$$

TEC_{50} is equivalent to the “L50” parameter in [7]. With this reformulation, we have

$$\lim_{\text{Dose} \rightarrow 0} AFTIR = 1.$$

This new formulation still converges to the previously derived formula such that

$$\lim_{\text{Dose} \rightarrow \infty} AFTIR = AFTIR_{\text{simple}}.$$

Both the TEC_{50} and simple formulas for AFTIR are checked against numerical simulations in the Results section. We attempted to derive the above expressions for AFTIR by extending the work from [7], but the derivation proved difficult for the model shown here. Thus, we instead posit that this approximation holds and will check it in the following sections.

2.2.6 Definition of TFTIR

Besides AFTIR, another quantity that can be used to guide dosing regimen is TFTIR (the Trough Free Tissue target to Initial target Ratio). It measures the minimum ratio of the free tissue target (e.g. within a tumor) to the initial tissue target at steady state and is defined as

$$TFTIR := \frac{T_{3,\text{trough}}}{T_{30}} \quad (34)$$

Like AFTIR, TFTIR can be approximated by

$$TFTIR \approx \frac{K_{\text{eq}} \cdot T_{\text{fold}}}{K_{\text{eq}} \cdot T_{\text{fold}} + B \cdot C_{\text{trough}}} \quad (35)$$

From [8], C_{trough} is given by

$$C_{\text{trough}} = \text{Dose} \cdot \left(\frac{C_1 \cdot \exp(-\alpha \cdot \tau)}{1 - \exp(-\alpha \cdot \tau)} + \frac{C_2 \cdot \exp(-\beta \cdot \tau)}{1 - \exp(-\beta \cdot \tau)} + \frac{C_3 \cdot \exp(-\gamma \cdot \tau)}{1 - \exp(-\gamma \cdot \tau)} \right),$$

where all constants can be computed from the model parameters [9]. We will numerically check whether this approximation for TFTIR is accurate in the next section.

2.2.7 Linear PK and CL

In the case that the PK is linear, and there is no elimination from the tumor compartment (i.e., $k_{eD3} = 0$), one can write C_{avg} in terms of the dosing regimen and the parameters governing the pharmacokinetics: bioavailability (F), clearance (CL), and dosing interval (τ). It is given by

$$C_{\text{avg}} = \frac{F \cdot \text{Dose}}{CL \cdot \tau}. \quad (36)$$

If there is elimination from the tumor (i.e., $k_{eD3} \neq 0$), then the formula above does not apply with $CL = k_{eD1}/V_{D1}$. However, a similarity transform can be applied where k_{eD3} can be forced to be zero, and all the other PK parameters k_{12D} , k_{21D} , k_{13D} , k_{31D} , k_{eD1} , CL can be transformed such that the concentration time profiles for $D_1(t)$ and $D_3(t)$ do not change. See Appendix A.3 for this similarity transformation. Thus, once CL is estimated by fitting a compartmental model, the formula above for C_{avg} holds whether or not there is elimination from the tissue compartment.

3 Methods

Under the assumption of large doses and a constant infusion of drug, we have arrived at the following expression for AFTIR:

$$\text{AFTIR} \approx \frac{K_{\text{eq}} \cdot T_{\text{fold}}}{K_{\text{eq}} \cdot T_{\text{fold}} + B \cdot C_{\text{avg}}} \quad (37)$$

We hypothesize that this expression also holds for TFTIR, replacing C_{avg} with C_{trough} .

To check the accuracy of this formula, we compare the theoretical AFTIR to the simulated AFTIR. The theoretical AFTIR is computed by Equation (37) for a given set of parameters. The simulated AFTIR is computed directly by simulating Equations (2) - (12) for the same set of parameters and then taking the ratio of the steady state average (or trough) free target concentration to the baseline target concentration. This is done for four mAbs used to treat cancer: trastuzumab (anti-HER2), atezolizumab (anti-PD-L1), pembrolizumab (anti-PD-1), and bevacizumab (anti-VEGF). Key properties

of these drugs are summarized in Table (1), and the specific parameters used in this analysis and the references for these parameters are provided in the supplementary material. An overview for how the parameters are selected is provided below.

3.1 Parameter Selection

The PK parameters (k_{eD1} , k_{12D} , k_{21D} , V_{D1} , V_{D2}) are taken from PopPK model fits from the literature. The volumes for the target tissue are assumed to be $0.1L$. The binding affinity (K_d or K_{ss}) is also taken from the literature, and when needed, a typical value for k_{off3} between $1 - 100/d$ is assumed [10, figure 12]. The binding and unbinding rates are assumed to be the same in both the central and tissue compartments. For baseline soluble and membrane-bound target levels, data from the literature is used. For membrane-bound targets, target expression (M_{10} , M_{30}) is provided in terms of receptors per cell (N), which is then converted to nanomolar concentration with

$$M_{i0}[\text{nM}] = N \cdot \rho_i \cdot \phi \cdot \frac{10^9}{6.02 \cdot 10^{23}}, \quad (38)$$

where $i = 1, 3$ refer to the central and target tissue compartments respectively. Here ρ_i is the cell density of the tissue of interest ($\rho_1 = 6 \cdot 10^9$ cells/L in blood for targets expressed on white blood cells, and $\rho_3 = 3 \cdot 10^{11}$ cells/L for targets expressed in tumor tissue [11]), and ϕ is the fraction of cells in the tissue of interest expressing the target, assumed to be $0.1 - 1$.

The target elimination and shedding rates are chosen to have reasonable values ($1 - 10/d$) [12], and the synthesis rates are chosen so that baseline target levels matched the estimates for M_{i0} above.

It is assumed that the rates of distribution of drug into the tumor are proportional to the rates of distribution into the peripheral tissue, scaled by the ratio of tissue volumes:

$$k_{13D} = k_{12D} \cdot \frac{V_{D3}}{V_{D2}}.$$

The biodistribution coefficient (B) is assumed to be around 30% [4], and assuming no elimination of drug from the tumor, k_{31D} is estimated by assuming that at steady state, the transit rates into and out of the tumor are equal:

$$\begin{aligned} k_{31D} \cdot D_3 \cdot V_{D3} &= k_{13D} \cdot D_1 \cdot V_{D1}, \\ k_{31D} \cdot (B \cdot D_1) \cdot V_{D3} &= k_{13D} \cdot D_1 \cdot V_{D1}, \\ k_{31D} &= \frac{k_{13D}}{B} \cdot \frac{V_{D1}}{V_{D3}}. \end{aligned}$$

Soluble targets are then assumed to distribute two times faster than the drug, and soluble drug-target complexes are assumed to distribute two times slower than the drug. It is recognized that this approach is empirical, and as a check,

these rates were found to be comparable to the rates estimated using the Krogh cylinder approach for modeling tissue distribution [13].

For membrane-bound targets where immune trafficking may occur (pembrolizumab, atezolizumab), it is assumed that the rate of distribution of cells expressing those targets into and out of tissue is $k_{13M} = 0.048/d$, and $k_{31M} = 5.5/d$ [14, Table 4, parameter k_{in} and k_{out}].

3.2 Sensitivity Analysis

In the above definition of AFTIR, three different approximations are used for the equilibrium binding constant K_{eq} : quasi-equilibrium (K_d), quasi-steady-state (K_{ss}), and the newly derived constant, quasi-steady-state with distribution (K_{ssd}). The accuracy of each of these constants over a range of doses is compared for the four drugs above.

To further check the accuracy of the AFTIR approximation, sensitivity analyses are performed on a few of the 47 model parameters:

- k_{13D} - the rate of distribution of the drug from the central compartment to the tissue compartment. This will impact the biodistribution (B) of drug in the tissue.
- k_{13DT} - the rate of distribution/trafficking of the drug-target complex from the central compartment to the tissue compartment. This parameter is included because it is often excluded from TMDD models and it was found to impact AFTIR.
- k_{synT3} - the rate of target synthesis in the tissue compartment. This will impact whether the drug at a particular dose is in excess to its target.
- $k_{shedDM3}$ - the rate of shedding of the drug-target complex from membrane-bound to soluble. This parameter is included because it is also often excluded from TMDD models.

For pembrolizumab, atezolizumab, and trastuzumab, T denotes the membrane-bound target, and for bevacizumab, T denotes the soluble target.

To explore the importance of an accurate estimate for the soluble target accumulation in the tissue of interest, we also perform a sensitivity analysis for the parameter k_{eS3} for bevacizumab, as this parameter has a significant impact on $T_{fold} = S_{3tot,ss}/S_{30}$.

4 Results

The AFTIR calculated by simulation is compared to the theoretical formula in Equation (37). The results are shown in Figures (3) and (4). Figure (3) shows comparisons of the approximations over a range of doses using the three equilibrium constants, K_d , K_{ss} , and K_{ssd} . In general, K_{ssd} , the new equilibrium constant derived here, best matches the model simulation. Note, however, that for trastuzumab, the drug with the highest target levels, the theory does not

match the simulation at all. This is because the AFTIR approximation requires the assumption that the drug is in vast excess to its target. Similar findings are also observed for TFTIR (see supplementary material).

Figure (4) shows the sensitivity of AFTIR to other parameters, namely the rate of trafficking of the drug from the central compartment to the tissue compartment (k_{13D}), the rate of trafficking of the drug-target complex from the central compartment to the tissue compartment (k_{13DT}), the rate of shedding of the drug-target complex from membrane-bound to soluble ($k_{shedDM3}$), and the rate of target synthesis in the tissue compartment (k_{synT3}). For bevacizumab, pembrolizumab, and atezolizumab, there is generally good agreement between theory and simulation. For trastuzumab, the theory does not match the simulation due to the very high target concentration. Aside from trastuzumab, the parameter for which there is the greatest discrepancy between theory and simulation is k_{synT3} . At low k_{synT3} values, the theory overpredicts the AFTIR value, while for high k_{synT3} values, the theory underpredicts the AFTIR value. The reason for the discrepancy at high k_{synT3} values is that the target expression becomes so high that the drug is no longer in excess to the target, as in the trastuzumab case. The reason for the discrepancy at low k_{synT3} values is that the assumption of negligible complex transport from circulation into the tissue of interest no longer applies. And so the approximation for deriving K_{ssd} in Equation (20) is no longer accurate. As a check of this phenomenon, we set k_{13DT} to zero. As a result, there is better agreement between theory and simulation in Figure (S1).

In Figure (6), it is shown that for a drug (bevacizumab) with a soluble target (VEGF), the fold-accumulation of the target is a critical factor in predicting the amount of target inhibition in the tissue of interest. This is also observed in Equation (30), where AFTIR is directly proportional to T_{fold} .

5 Discussion

5.1 Review of key AFTIR parameters

The key insight from this work is that under many clinically relevant scenarios, AFTIR can be estimated using four parameters, a binding constant (K_{eq}), the fold-change in target levels upon binding to drug (T_{fold}), the average drug concentration in circulation (C_{avg}), and the biodistribution coefficient for the drug to the tissue of interest (B):

$$\text{AFTIR} = \frac{K_{eq} \cdot T_{fold}}{K_{eq} \cdot T_{fold} + B \cdot C_{avg}}.$$

This simple formula provides intuition for how changing the dosing regimen, improving the binding affinity of the drug, or enhancing tissue penetration would be expected to alter target inhibition. For example, at large drug concentrations, when $\text{AFTIR} \approx \text{AFTIR}_{\text{simple}} = K_{eq} \cdot T_{fold} / (B \cdot C_{avg})$, one can see that either halving the dosing interval, halving the binding affinity (with

a more potent drug), or doubling the tissue accessibility (with a drug that enhances tissue penetration) would reduce the free target concentration by approximately 50%. Even though the model in Figure (2) has many parameters, some of which are difficult to estimate, the AFTIR formula shows that under many practical scenarios, predicting the target inhibition can be done with an estimate of only four lumped parameters. The method for estimating each of these parameters is described below.

The **drug concentration** (C_{avg} or C_{trough}) is estimable from PK data from Phase 1 clinical trials. For monoclonal antibodies, it can also be readily predicted from preclinical data [15].

The **biodistribution coefficient** (B) has been estimated for many tissues in monkeys [16], where it ranges from 5 – 15% in the total tissue or 15 – 45% in the tissue interstitial fluid (assuming that 1/3 of the tissue is interstitial fluid). In mouse tumors, $B = 30\%$ [4], and this is similar in human skin for secukinumab [17]. However, others have used predictions of tumor distribution based on rates of extravasation and diffusion to predict that the antibody concentration in a tumor should be only 0.1–1% [18]. Due to this disagreement in estimates for B and the limited data in the literature, further work in estimating biodistribution would be of value [19].

The **binding affinity** (K_d , K_{ss} or K_{ssd}) can either be estimated in vitro with surface plasmon resonance and cell binding assays, or in the clinic with a model-based analysis of soluble target data [1] or receptor occupancy assays [20]. Often there is good agreement between the in vitro and in vivo estimates, though it is critical that the assays be carefully validated as there have been instances of 1000-fold differences between the in vitro and in vivo estimates [21, Figure 8]. Also, assays measuring free or bound target concentrations, rather than total target concentrations, can be difficult to validate [22].

The **fold-change in target concentration** (T_{fold}) in the tissue of interest can be estimated from in vitro experiments for membrane-bound targets by estimating the internalization rates of bound and unbound receptors. It is generally around $T_{\text{fold}} = 0.5$ [23], [24, page 15]. Care must be taken when interpreting biopsy staining data from immunohistochemistry (IHC) assays to estimate T_{fold} . If staining for the target increases during therapy, it may be because the number of receptors per cell has increased due to drug binding, or it may be because the number of cells expressing the target in the tissue has increased. These two effects impact the AFTIR formula differently. If the number of receptors per cell doubles, T_{fold} will also double, and the fraction of free receptors on the cell surface will also double. But if it is the number of cells that doubles with the number of receptors per cell held constant, this instead potentially affects the assumption that the drug is in excess to its target; if this assumption still holds, then AFTIR will not be affected.

For soluble targets, T_{fold} is often directly measured in circulation [1], but to our knowledge, it has only been measured once in tissue, namely for IL-6 in mouse synovial fluid [25]. This data was difficult to interpret since many measurements were below the limit of quantification of the assay. Therefore, a significant challenge in applying this formula to soluble targets is that the extent

of target-accumulation in the tissue of interest is not known. The importance of measuring the target in the tissue of interest was previously highlighted by [26].

5.2 Review of assumptions and caveats

The following assumptions are needed for the theoretical estimate of AFTIR to be accurate.

The drug concentration is much larger than the target concentration. This assumption can be checked by comparing estimates of target expression in the tissue of interest to estimates of the drug concentration in that tissue.

The tissue can be treated as homogeneous. One check of this approximation is whether the Thiele Modulus is less than one [18]. In terms of the model parameters used here, the Thiele Modulus is given by $\phi^2 = (k_{\text{shedDM3}} + k_{\text{eDM3}}) \cdot M_{3\text{tot}} / (k_{31D} \cdot B \cdot C_{\text{avg}})$ [11], which was found to be less than one for atezolizumab and pembrolizumab, but greater than one for trastuzumab.

Distribution of the drug-target complex from circulation into the tissue is relatively small. This assumption was required for the calculation of K_{ssd} . If distribution of the complex from circulation into the tissue of interest plays a significant role, then the AFTIR formula may not apply. One instance where it may need to be checked is for a soluble target that accumulates 100–1000 times in circulation but not in the tissue of interest. This assumption is difficult to check and requires knowledge of the underlying biology. If it is known that the target is primarily expressed in the tumor, or if its a membrane-bound target that doesn't move from circulation into the tumor, then this assumption would be reasonable.

The degree of inhibition needed for efficacy is known. Often, 90-95% inhibition is assumed to be needed [27], though for a drug that works by stimulating the immune system to attack the tumor, much less inhibition may be needed. Examples include trastuzumab, which may also work via antibody dependent cell-mediated cytotoxicity and bispecific T-cell engagers like blinatumomab, which facilitates the interaction between T cells and cancer cells.

Competition for target binding sites between drug and endogenous ligand. If the binding between a target and its endogenous ligand is much lower than the binding affinity of the drug, the formulas derived here may not be applicable because the drug may not be disrupting the interactions between the target and its endogenous ligand.

5.3 Applications

Phase 2 dose selection. A key application of this work is to provide an updated methodology for guiding Phase 2 dose selection for biologics when

the safety, efficacy, and biomarker data are insufficient to guide dose selection. With this approach, one uses a PopPK model based on Phase 1 PK data to predict the steady state trough concentration of the drug. Then, together with estimates for the binding affinity, fold accumulation of target upon treatment, and biodistribution of drug to tissue, one can apply the AFTIR or TFTIR equation to identify the dose at which say 90% of patients are expected to achieve 90% target inhibition. While a similar methodology was used previously for atezolizumab [4], K_{ssd} and T_{fold} were not explicitly accounted for.

Rapid assessment of drugs. The AFTIR potency metric also allows for a rapid assessment of new drugs without a need for extensive simulations. In particular, given that $AFTIR_{simple} = (K_{eq} \cdot T_{fold} \cdot CL \cdot \tau) / (F \cdot B \cdot Dose)$, this formula shows how changing the dosing regimen, clearance, and binding affinity would impact target engagement.

Moreover, rather than specify every rate constant of the complex system of Figure (2), or an even more complex physiological model, it is sufficient in many scenarios to provide estimates for only four parameters: K_{eq} , T_{fold} , B , and C_{avg} , all of which can in principle be measured directly.

5.4 Conclusions

In summary, we have extended previous work to develop potency metrics AFTIR and TFTIR that characterize target inhibition in a tissue, such as a tumor. These metrics predict the target inhibition at steady state under a repeated dosing regimen using four quantities: the average (or trough) drug concentration at steady state, the biodistribution of drug to its target, the equilibrium binding constant, and the fold-accumulation of the target. AFTIR and TFTIR provide intuition for how various physiological properties of the system impact target engagement. In addition, AFTIR and TFTIR can be used for rapid assessment of new targets and exploration of the binding affinity, half-life, bioavailability, and dosing regimen needed for a second-generation drug to achieve comparable or superior efficacy to a marketed compound.

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A Appendix

A.1 Fold-Accumulation (T_{fold})

Recall that the fold-accumulation of target is given by

$$T_{\text{fold}} := \frac{T_{3\text{tot,ss}}}{T_{30}}, \quad (39)$$

where $T_{3\text{tot,ss}}$ denotes drug-target complex concentration at steady state, and T_{30} denotes target concentration at the initial state. In the sections below, we solve for the baseline target and the steady state target (for large drug concentrations) using similar approaches. Then, we compute T_{fold} as the ratio of the two.

A.1.1 Baseline target (T_{10} and T_{30})

Before the drug is given, the system is at steady state. And we have $D_1 = D_2 = D_3 = DM_1 = DM_3 = DS_1 = DS_3 = 0$. Using the ODE system, we solve for the nonzero initial membrane-bound targets. Setting Equations (5) and (6) to zero, we get a system of two linear equations,

$$\begin{pmatrix} 0 \\ 0 \end{pmatrix} = \frac{d}{dt} \begin{pmatrix} M_1 \\ M_3 \end{pmatrix} = \begin{pmatrix} -(k_{\text{shed}M_1} + k_{13M} + k_{eM1}) & (V_T/V_C)k_{31M} \\ (V_C/V_T)k_{13M} & -(k_{\text{shed}M_3} + k_{31M} + k_{eM3}) \end{pmatrix} \begin{pmatrix} M_1 \\ M_3 \end{pmatrix}_0 + \begin{pmatrix} k_{\text{syn}M1} \\ k_{\text{syn}M3} \end{pmatrix}.$$

Rearranging yields

$$\begin{pmatrix} (k_{\text{shed}M_1} + k_{13M} + k_{eM_1}) & -(V_T/V_C)k_{31M} \\ -(V_C/V_T)k_{13M} & (k_{\text{shed}M_3} + k_{31M} + k_{eM_3}) \end{pmatrix} \begin{pmatrix} M_1 \\ M_3 \end{pmatrix}_0 = \begin{pmatrix} k_{\text{syn}M_1} \\ k_{\text{syn}M_3} \end{pmatrix}$$

Then, using the formula for inverting a 2D matrix gives

$$M_{10} = \frac{(k_{\text{shed}M_3} + k_{31M} + k_{eM_3})k_{\text{syn}M_1} + (V_T/V_C)k_{31M}k_{\text{syn}M_3}}{(k_{\text{shed}M_1} + k_{13M} + k_{eM_1})(k_{\text{shed}M_3} + k_{31M} + k_{eM_3}) - k_{31M}k_{13M}}, \quad (40)$$

$$M_{30} = \frac{(V_C/V_T)k_{13M}k_{\text{syn}M_1} + (k_{\text{shed}M_1} + k_{13M} + k_{eM_1})k_{\text{syn}M_3}}{(k_{\text{shed}M_1} + k_{13M} + k_{eM_1})(k_{\text{shed}M_3} + k_{31M} + k_{eM_3}) - k_{31M}k_{13M}}. \quad (41)$$

To solve for the nonzero initial soluble targets, we set Equations (7) and (8) to zero, resulting in a system of two linear equations,

$$\begin{pmatrix} 0 \\ 0 \end{pmatrix} = \frac{d}{dt} \begin{pmatrix} S_1 \\ S_3 \end{pmatrix} = \begin{pmatrix} -(k_{13S} + k_{eS_1}) & (V_T/V_C)k_{31S} \\ (V_C/V_T)k_{13S} & -(k_{31S} + k_{eS_3}) \end{pmatrix} \begin{pmatrix} S_1 \\ S_3 \end{pmatrix}_0 + \begin{pmatrix} k_{\text{syn}S_1} + k_{\text{shed}M_1} \\ k_{\text{syn}S_3} + k_{\text{shed}M_3} \end{pmatrix}.$$

Similar to above, we get

$$S_{10} = \frac{(k_{31S} + k_{eS_3})(k_{\text{syn}S_1} + k_{\text{shed}M_1}M_{10}) + (V_T/V_C)k_{31S}(k_{\text{syn}S_3} + k_{\text{shed}M_3}M_{30})}{(k_{13S} + k_{eS_1})(k_{31S} + k_{eS_3}) - k_{31S}k_{13S}}, \quad (42)$$

$$S_{30} = \frac{(V_C/V_T)k_{13S}(k_{\text{syn}S_1} + k_{\text{shed}M_1}M_{10}) + (k_{13S} + k_{eS_1})(k_{\text{syn}S_3} + k_{\text{shed}M_3}M_{30})}{(k_{13S} + k_{eS_1})(k_{31S} + k_{eS_3}) - k_{31S}k_{13S}}, \quad (43)$$

where M_{10} and M_{30} are given by (40) and (41).

A.1.2 Steady State Value

After the drug is given, the system reaches steady state. We assume that the drug is in vast excess to the amount of target so that almost all of the target is bound to the drug. Then we have $M_1 = M_3 = S_1 = S_3 \approx 0$, $M_{3\text{tot,ss}} = M_3 + DM_3$, and $S_{3\text{tot,ss}} = S_3 + DS_3$. Using the ODE system, we solve for the nonzero steady state of the total membrane-bound targets. Adding the equations for the target and complex, Equations (5) and (6) added to Equations (9) and (10), respectively, gives differential equations for the total target that are similar to that when no drug is on board. We set these differential equations to zero, resulting in a system of two linear equations. We solve as in the previous section to get

$$M_{1\text{tot,ss}} = \frac{(k_{\text{shed}DM_3} + k_{31DM} + k_{eDM_3})k_{\text{syn}M_1} + (V_T/V_C)k_{31DM}k_{\text{syn}M_3}}{(k_{\text{shed}DM_1} + k_{13DM} + k_{eDM_1})(k_{\text{shed}DM_3} + k_{31DM} + k_{eDM_3}) - k_{31DM}k_{13DM}}, \quad (44)$$

$$M_{3\text{tot,ss}} = \frac{(V_C/V_T)k_{13DM}k_{\text{syn}M_1} + (k_{\text{shed}DM_1} + k_{13DM} + k_{eDM_1})k_{\text{syn}M_3}}{(k_{\text{shed}DM_1} + k_{13DM} + k_{eDM_1})(k_{\text{shed}DM_3} + k_{31DM} + k_{eDM_3}) - k_{31DM}k_{13DM}}. \quad (45)$$

Likewise, the nonzero steady state of total soluble targets are given by

$$S_{1\text{tot,ss}} = \frac{(k_{31DS} + k_{eDS_3})(k_{\text{syn}S_1} + k_{\text{shed}DM_1}DM_{1\text{tot,ss}}) + (V_T/V_C)k_{31DS}(k_{\text{syn}S_3} + k_{\text{shed}DM_3}DM_{3\text{tot,ss}})}{(k_{13DS} + k_{eDS_1})(k_{31DS} + k_{eDS_3}) - k_{31DS}k_{13DS}}, \quad (46)$$

$$S_{3\text{tot,ss}} = \frac{(V_C/V_T)k_{13DS}(k_{\text{syn}S_1} + k_{\text{shed}DM_1}DM_{1\text{tot,ss}}) + (k_{13DS} + k_{eDS_1})(k_{\text{syn}S_3} + k_{\text{shed}DM_3}DM_{3\text{tot,ss}})}{(k_{13DS} + k_{eDS_1})(k_{31DS} + k_{eDS_3}) - k_{31DS}k_{13DS}}, \quad (47)$$

where $M_{1\text{tot,ss}}$ and $M_{3\text{tot,ss}}$ are given by (44) and (45).

A summary of all the equations is provided below. To calculate T_{fold} , one then uses the formulas below to compute $M_{3\text{tot,ss}}/M_{30}$ or $S_{3\text{tot,ss}}/S_{30}$.

$$M_{10} = \frac{(k_{\text{shed}M_3} + k_{31M} + k_{eM_3})k_{\text{syn}M_1} + (V_T/V_C)k_{31M}k_{\text{syn}M_3}}{(k_{\text{shed}M_1} + k_{13M} + k_{eM_1})(k_{\text{shed}M_3} + k_{31M} + k_{eM_3}) - k_{31M}k_{13M}} \quad (48)$$

$$M_{30} = \frac{(V_C/V_T)k_{13M}k_{\text{syn}M_1} + (k_{\text{shed}M_1} + k_{13M} + k_{eM_1})k_{\text{syn}M_3}}{(k_{\text{shed}M_1} + k_{13M} + k_{eM_1})(k_{\text{shed}M_3} + k_{31M} + k_{eM_3}) - k_{31M}k_{13M}} \quad (49)$$

$$S_{10} = \frac{(k_{31S} + k_{eS_3})(k_{\text{syn}S_1} + k_{\text{shed}M_1}M_{10}) + (V_T/V_C)k_{31S}(k_{\text{syn}S_3} + k_{\text{shed}M_3}M_{30})}{(k_{13S} + k_{eS_1})(k_{31S} + k_{eS_3}) - k_{31S}k_{13S}} \quad (50)$$

$$S_{30} = \frac{(V_C/V_T)k_{13S}(k_{\text{syn}S_1} + k_{\text{shed}M_1}M_{10}) + (k_{13S} + k_{eS_1})(k_{\text{syn}S_3} + k_{\text{shed}M_3}M_{30})}{(k_{13S} + k_{eS_1})(k_{31S} + k_{eS_3}) - k_{31S}k_{13S}} \quad (51)$$

$$M_{1\text{tot,ss}} = \frac{(k_{\text{shed}DM_3} + k_{31DM} + k_{eDM_3})k_{\text{syn}M_1} + (V_T/V_C)k_{31DM}k_{\text{syn}M_3}}{(k_{\text{shed}DM_1} + k_{13DM} + k_{eDM_1})(k_{\text{shed}DM_3} + k_{31DM} + k_{eDM_3}) - k_{31DM}k_{13DM}} \quad (52)$$

$$M_{3\text{tot,ss}} = \frac{(V_C/V_T)k_{13DM}k_{\text{syn}M_1} + (k_{\text{shed}DM_1} + k_{13DM} + k_{eDM_1})k_{\text{syn}M_3}}{(k_{\text{shed}DM_1} + k_{13DM} + k_{eDM_1})(k_{\text{shed}DM_3} + k_{31DM} + k_{eDM_3}) - k_{31DM}k_{13DM}} \quad (53)$$

$$S_{1\text{tot,ss}} = \frac{(k_{31DS} + k_{eDS_3})(k_{\text{syn}S_1} + k_{\text{shed}DM_1}DM_{1\text{tot,ss}}) + (V_T/V_C)k_{31DS}(k_{\text{syn}S_3} + k_{\text{shed}DM_3}DM_{3\text{tot,ss}})}{(k_{13DS} + k_{eDS_1})(k_{31DS} + k_{eDS_3}) - k_{31DS}k_{13DS}} \quad (54)$$

$$S_{3\text{tot,ss}} = \frac{(V_C/V_T)k_{13DS}(k_{\text{syn}S_1} + k_{\text{shed}DM_1}DM_{1\text{tot,ss}}) + (k_{13DS} + k_{eDS_1})(k_{\text{syn}S_3} + k_{\text{shed}DM_3}DM_{3\text{tot,ss}})}{(k_{13DS} + k_{eDS_1})(k_{31DS} + k_{eDS_3}) - k_{31DS}k_{13DS}} \quad (55)$$

A.2 Biodistribution (B)

For very large infusion where the target concentration is negligible, we can write the three equations for the drug (D_1 , D_2 , D_3) from Equations (2), (3), and (4) as below to solve for steady state.

$$\begin{aligned} - \begin{pmatrix} k_{\text{inf}} \\ 0 \\ 0 \end{pmatrix} &= \frac{d}{dt} \begin{pmatrix} D_1 \\ D_2 \\ D_3 \end{pmatrix} \\ &= \begin{pmatrix} -(k_{eD_1} + k_{12D} + k_{13D}) & (V_P/V_C)k_{21D} & (V_T/V_C)k_{31D} \\ (V_C/V_P)k_{12D} & -k_{21D} & 0 \\ (V_C/V_T)k_{13D} & 0 & -(k_{eD_3} + k_{31D}) \end{pmatrix} \cdot \begin{pmatrix} D_1 \\ D_2 \\ D_3 \end{pmatrix} \\ &= A \cdot \begin{pmatrix} D_1 \\ D_2 \\ D_3 \end{pmatrix}. \end{aligned}$$

B is given by the ratio of $D_{3,ss}/D_{1,ss}$ where ss denotes steady state, such that when the drug concentration is large

$$D_{3\text{tot,avg}} = B \cdot D_{1\text{tot,avg}} = B \cdot C_{\text{avg}}, \quad (56)$$

where we define $C_{\text{avg}} := D_{1\text{tot,avg}}$.

B is computed as follows:

$$\begin{aligned} \begin{pmatrix} D_1 \\ D_2 \\ D_3 \end{pmatrix}_{ss} &= A^{-1} \cdot \begin{pmatrix} -k_{\text{inf}} \\ 0 \\ 0 \end{pmatrix} \\ &= \frac{-k_{\text{inf}}}{\det A} \begin{pmatrix} a_{22}a_{33} - a_{23}a_{32} \\ a_{23}a_{31} - a_{21}a_{33} \\ a_{21}a_{32} - a_{22}a_{31} \end{pmatrix} = \frac{-k_{\text{inf}}}{\det A} \begin{pmatrix} k_{21D}(k_{eD3} + k_{31D}) \\ k_{21D}(V_P/V_C)(k_{eD3} + k_{31D}) \\ k_{21D}(V_C/V_T)k_{13D} \end{pmatrix}. \end{aligned}$$

Thus the biodistribution coefficient for the tissue compartment is given by

$$B := \left(\frac{D_3}{D_1} \right)_{ss} = \frac{k_{21D}(V_C/V_T)k_{13D}}{k_{21D}(k_{eD3} + k_{31D})} = \frac{V_C}{V_T} \cdot \frac{k_{13D}}{(k_{eD3} + k_{31D})}.$$

For drugs dosed with linear PK at regular intervals, drug concentration much larger than target concentration, and free drug elimination occurring only in the central compartment, we have $D_{1\text{tot,avg}} = \text{Dose}/(CL \cdot \tau)$, where $CL = k_{eD1} \cdot V_C$ is the drug clearance. As shown in Section A.3, we can derive a similar formula with coefficient matrix A' in which $k_{eD3} = 0$, while D'_1 and D'_3 in the new model are the same as D_1 and D_3 in the original model. From Section A.3, we have

$$A' = \begin{pmatrix} -(k_{13D} + k_{12D} + k_{eD1}) & \frac{V_P}{V_C}k_{21D} & \frac{V_T}{V_C}(k_{eD3} + k_{31D}) \\ \frac{V_C}{V_P} \left(k_{12D} - \frac{k_{13D}k_{eD3}}{k_{21D}} \right) & -k_{21D} & -\frac{V_T}{V_P} \left(k_{eD3} - \frac{k_{31D}k_{eD3}}{k_{21D}} - \frac{k_{eD3}^2}{k_{21D}} \right) \\ \frac{V_C}{V_T}k_{13D} & 0 & -(k_{31D} + k_{eD3}) \end{pmatrix}.$$

Then, as above,

$$\begin{aligned} \begin{pmatrix} D'_1 \\ D'_2 \\ D'_3 \end{pmatrix}_{ss} &= \frac{-k_{\text{inf}}}{\det A'} \begin{pmatrix} a_{22}a_{33} - a_{23}a_{32} \\ a_{23}a_{31} - a_{21}a_{33} \\ a_{21}a_{32} - a_{22}a_{31} \end{pmatrix} \\ &= \frac{-k_{\text{inf}}}{\det A'} \begin{pmatrix} k_{21D}(k_{31D} + k_{eD3}) \\ (V_C/V_P)(k_{12D}k_{31D} + \frac{k_{12D}}{k_{eD3}} + \frac{k_{13D}}{k_{eD3}}) \\ (V_C/V_T)k_{21D}k_{13D} \end{pmatrix} \end{aligned}$$

And the biodistribution coefficient for the tissue compartment is given by

$$B' := \left(\frac{D'_3}{D'_1} \right)_{ss} = \frac{(V_C/V_T)k_{21D}k_{13D}}{k_{21D}(k_{31D} + k_{eD3})} = \frac{V_C}{V_T} \cdot \frac{k_{13D}}{(k_{31D} + k_{eD3})},$$

which is the same as B in the original model above.

A.3 Similarity Transform

We consider the model in Figure (2). A drug (D) binds to its target (M) to form a complex (DM). It has three compartments, central, tissue, and peripheral.

The drug and target dynamics are modeled with the following system of ordinary differential equations

$$\begin{aligned} \frac{dD_1}{dt} = & \frac{1}{V_C} \text{Dose}_{iv}(t) - k_{12D} D_1 + \frac{V_P}{V_C} k_{21D} D_2 - k_{13D} D_1 \\ & + \frac{V_T}{V_C} k_{31D} D_3 - k_{on1} D_1 \cdot M_1 + k_{off1}(DM_1) - k_{eD1} D_1 \end{aligned} \quad (57)$$

$$\frac{dD_2}{dt} = k_{12D} \frac{V_C}{V_P} D_1 - k_{21D} D_2 \quad (58)$$

$$\frac{dD_3}{dt} = \frac{V_C}{V_T} k_{13D} D_1 - k_{31D} D_3 - k_{on3} D_3 \cdot M_3 + k_{off3}(DM_3) - k_{eD3} D_3 \quad (59)$$

$$\begin{aligned} \frac{dM_1}{dt} = & k_{syn1} - k_{13M} M_1 + \frac{V_T}{V_C} k_{31M} M_3 - k_{on1} D_1 \cdot M_1 + k_{off1}(DM_1) \\ & - k_{eM1} M_1 \end{aligned} \quad (60)$$

$$\begin{aligned} \frac{dM_3}{dt} = & k_{syn3} + \frac{V_C}{V_T} k_{13M} M_1 - k_{31M} M_3 - k_{on3} D_3 \cdot M_3 + k_{off3}(DM_3) \\ & - k_{eM3} M_3 \end{aligned} \quad (61)$$

$$\begin{aligned} \frac{d(DM_1)}{dt} = & -k_{13DM}(DM_1) + \frac{V_T}{V_C} k_{31DM}(DM_3) + k_{on1} D_1 \cdot M_1 - k_{off1}(DM_1) \\ & - k_{eDM1}(DM_1) \end{aligned} \quad (62)$$

$$\begin{aligned} \frac{d(DM_3)}{dt} = & \frac{V_C}{V_T} k_{13DM}(DM_1) - k_{31DM}(DM_3) + k_{on3} D_3 \cdot M_3 - k_{off3}(DM_3) \\ & - k_{eDM3}(DM_3) \end{aligned} \quad (63)$$

We will calculate $D_{3\text{tot,avg}}$, which is the average drug concentration at steady state in the tissue compartment. We have $D_{3\text{tot,avg}} = B \cdot D_{1\text{tot,avg}}$, where $D_{1\text{tot,avg}}$ is the average drug concentration at steady state in the central compartment, and B is the antibody biodistribution coefficient. Assume that drug elimination only occurs in the central compartment, i.e., $k_{eD3} = 0$. Then for drugs dosed with linear PK at regular intervals and concentration much larger than target concentration, we have $D_{1\text{tot,avg}} = \text{Dose}/(CL \cdot \tau)$, where $CL = k_{eD1} \cdot V_C$ is the drug clearance [8].

For the model with drug elimination in both the central and tissue compartments, we will derive an alternative model with $k_{eD3} = 0$ that is indistinguishable from the existing model by using the similarity transform technique [28]. We consider drug concentration large enough that target binding does not affect drug distribution. Then the model equations for the drug can be written as

$$\frac{d\mathbf{D}}{dt} = A \cdot \mathbf{D}(t) + B \cdot \text{Dose}_{iv}(t), \quad (64)$$

with measurement

$$\mathbf{m}(t) = C \cdot \mathbf{D}(t), \quad (65)$$

where

$$\mathbf{D} = \begin{pmatrix} D_1 \\ D_2 \\ D_3 \end{pmatrix}, \quad (66)$$

$$A = \begin{pmatrix} -(k_{13D} + k_{12D} + k_{eD1}) & \frac{V_P}{V_C} k_{21D} & \frac{V_T}{V_C} k_{31D} \\ \frac{V_C}{V_P} k_{12D} & -k_{21D} & 0 \\ \frac{V_C}{V_T} k_{13D} & 0 & -(k_{31D} + k_{eD3}) \end{pmatrix}, \quad (67)$$

$$B = \begin{pmatrix} 1 \\ \frac{1}{V_C} \\ 0 \\ 0 \end{pmatrix}, \quad (68)$$

$$C = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}. \quad (69)$$

We transform this model into an indistinguishable model with coefficient matrices A' , B' , and C' such that $k'_{eD3} = 0$. This is accomplished with the similarity transform

$$A' := TAT^{-1}, \quad B' := TB, \quad C' := CT^{-1}, \quad (70)$$

for some transformation matrix

$$T = \begin{pmatrix} t_{11} & t_{12} & t_{13} \\ t_{21} & t_{22} & t_{23} \\ t_{31} & t_{32} & t_{33} \end{pmatrix}, \quad T^{-1} = \begin{pmatrix} \hat{t}_{11} & \hat{t}_{12} & \hat{t}_{13} \\ \hat{t}_{21} & \hat{t}_{22} & \hat{t}_{23} \\ \hat{t}_{31} & \hat{t}_{32} & \hat{t}_{33} \end{pmatrix}. \quad (71)$$

Alternatively, one can get this similarity transform with the change of variables $\mathbf{D} = T^{-1}\mathbf{D}'$. Then from (64) and (65), we have

$$\frac{d(T^{-1}\mathbf{D}')}{dt} = A \cdot (T^{-1}\mathbf{D}')(t) + B \cdot \text{Dose}_{iv}(t), \quad \mathbf{m}(t) = C \cdot (T^{-1}\mathbf{D}')(t). \quad (72)$$

Multiplying the first equation in (72) on the left by T yields

$$\frac{d\mathbf{D}'}{dt} = TAT^{-1} \cdot \mathbf{D}'(t) + TB \cdot \text{Dose}_{iv}(t). \quad (73)$$

Then we have the new model equation and measurement

$$\frac{d\mathbf{D}'}{dt} = A' \cdot \mathbf{D}'(t) + B' \cdot \text{Dose}_{iv}(t), \quad \mathbf{m}(t) = C' \cdot \mathbf{D}'(t), \quad (74)$$

where A' , B' , and C' are given by (70).

Regardless of model formulation, the same dose is given to D_1 , that is,

$$B' = B. \quad (75)$$

From this and (70), we get $t_{11} = 1$, $t_{21} = 0$, and $t_{31} = 0$. Regardless of model formulation, we measure D_1 and D_3 , that is,

$$C' = C. \quad (76)$$

From this and (70), we get $\hat{t}_{11} = 1$, $\hat{t}_{12} = 0$, $\hat{t}_{13} = 0$, $\hat{t}_{31} = 0$, $\hat{t}_{32} = 0$, and $\hat{t}_{33} = 1$. For a 3×3 matrix, the inverse is given by

$$T^{-1} = \frac{1}{\det T} \begin{pmatrix} t_{22}t_{33} - t_{23}t_{32} & t_{13}t_{32} - t_{12}t_{33} & t_{12}t_{23} - t_{13}t_{22} \\ t_{23}t_{31} - t_{21}t_{33} & t_{11}t_{33} - t_{13}t_{31} & t_{13}t_{21} - t_{11}t_{23} \\ t_{21}t_{32} - t_{22}t_{31} & t_{12}t_{31} - t_{11}t_{32} & t_{11}t_{22} - t_{12}t_{21} \end{pmatrix}, \quad (77)$$

with the determinant given by

$$\det T = t_{11}(t_{22}t_{33} - t_{23}t_{32}) - t_{12}(t_{21}t_{33} - t_{23}t_{31}) + t_{13}(t_{21}t_{32} - t_{22}t_{31}). \quad (78)$$

Putting the above findings into T^{-1} yields $t_{12} = 0$, $t_{13} = 0$, $t_{32} = 0$, and $t_{33} = 1$. From $TT^{-1} = I$, we get $t_{22} = 1$. Then we have

$$T = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & t_{23} \\ 0 & 0 & 1 \end{pmatrix} \quad T^{-1} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & -t_{23} \\ 0 & 0 & 1 \end{pmatrix}. \quad (79)$$

Putting this into (70) yields

$$A' = \begin{pmatrix} -(k_{13D} + k_{12D} + k_{eD1}) \frac{V_P}{V_C} k_{21D} & -\frac{V_P}{V_C} k_{21D} t_{23} + \frac{V_T}{V_C} k_{31D} \\ \frac{V_C}{V_P} k_{12D} + \frac{V_C}{V_T} k_{13D} t_{23} & -k_{21D} & (k_{21D} - k_{31D} - k_{eD3}) t_{23} \\ \frac{V_C}{V_T} k_{13D} & 0 & -(k_{31D} + k_{eD3}) \end{pmatrix}. \quad (80)$$

Now we impose

$$k'_{eD3} := -a'_{33} - \frac{V_C}{V_T} a'_{13} = 0, \quad (81)$$

from which we get $t_{23} = -(V_T/V_P)(k_{eD3}/k_{21D})$. After putting this last piece into A' , we have

$$A' = \begin{pmatrix} -(k_{13D} + k_{12D} + k_{eD1}) \frac{V_P}{V_C} k_{21D} & & \frac{V_T}{V_C} (k_{eD3} + k_{31D}) \\ \frac{V_C}{V_P} \left(k_{12D} - \frac{k_{13D} k_{eD3}}{k_{21D}} \right) & -k_{21D} & -\frac{V_T}{V_P} \left(k_{eD3} - \frac{k_{31D} k_{eD3}}{k_{21D}} - \frac{k_{eD3}^2}{k_{21D}} \right) \\ \frac{V_C}{V_T} k_{13D} & 0 & -(k_{31D} + k_{eD3}) \end{pmatrix}. \quad (82)$$

We get k'_{eD1} from

$$\begin{aligned} k'_{eD1} &= -a'_{11} - \frac{V_P}{V_C} a'_{21} - \frac{V_T}{V_C} a'_{31} \\ &= k_{eD1} - \frac{k_{13D} \cdot k_{eD3}}{k_{21D}}. \end{aligned} \quad (83)$$

Thus $CL' = k'_{eD1} \cdot V_C$, with k'_{eD1} given by (83). And finally we get $D_{\text{tot,avg1}} = \text{Dose}/(CL' \cdot \tau)$, and $D_{\text{tot,avg3}} = B \cdot D_{\text{tot,avg1}}$.

Remark: In the similarity transform, we measure D_1 and D_3 , which is indicated by C . As a result of imposing $C' = C$, the original model and the transformed model output the same values for these variables. D'_2 , however, differs from D_2 .

B Figures and Tables

Drug	Bevacizumab	Pembrolizumab	Atezolizumab	Trastuzumab
Target Type	Soluble	Membrane-Bound	Membrane-Bound	Membrane-Bound
Target	VEGF	PD-1	PD-L1	HER-2
Baseline Target (nM)	0.01	0.2	3	800

Table 1 Summary of drugs in this analysis. Details on all model parameters is provided in the Supplementary Material

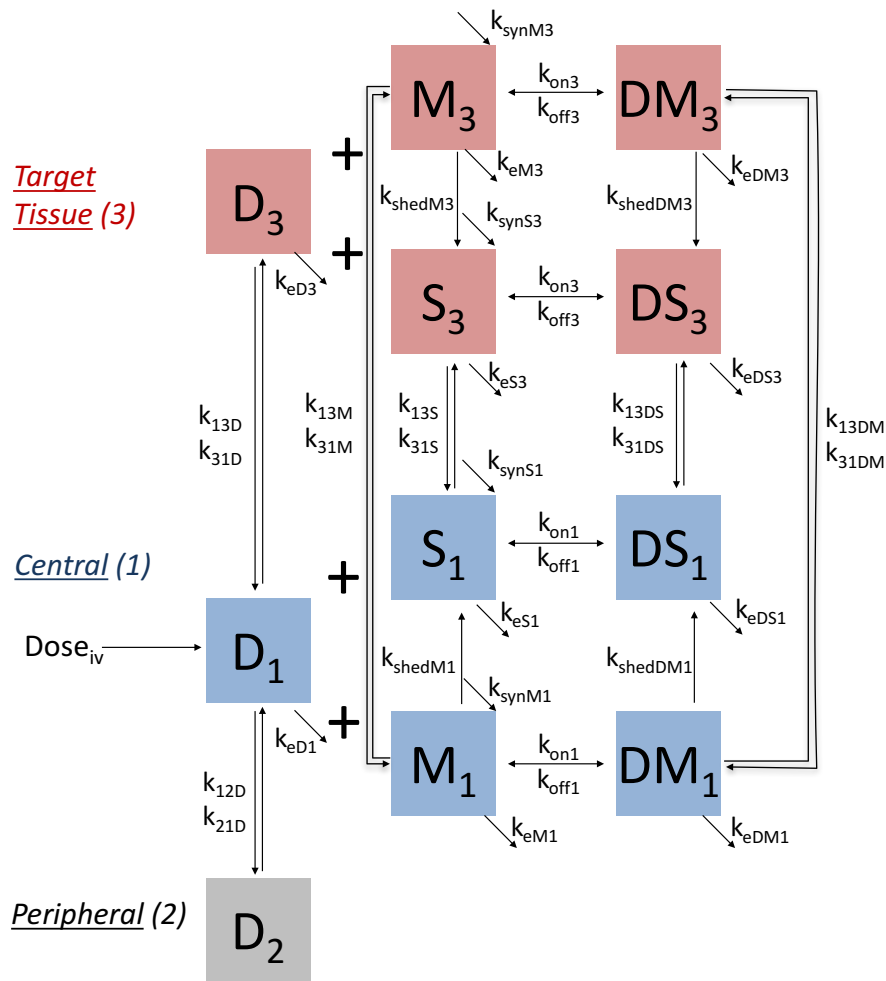


Fig. 2 The extended target mediated drug disposition model. Vertical arrows represent distribution, horizontal arrows represent dosing and binding, and diagonal arrows represent synthesis and elimination.

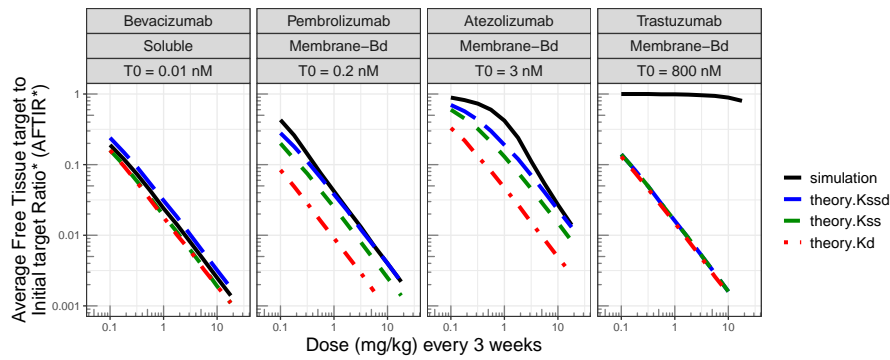


Fig. 3 Average Free Tissue target to Initial target Ratio (AFTIR) for four drugs with different baseline target expression levels (T_0) over a range of doses. The K_{ssd} approximation matched the simulation better than K_{ss} and K_d . Note that except in the case of very high target expression levels (Trastuzumab) the theory matched the simulation.

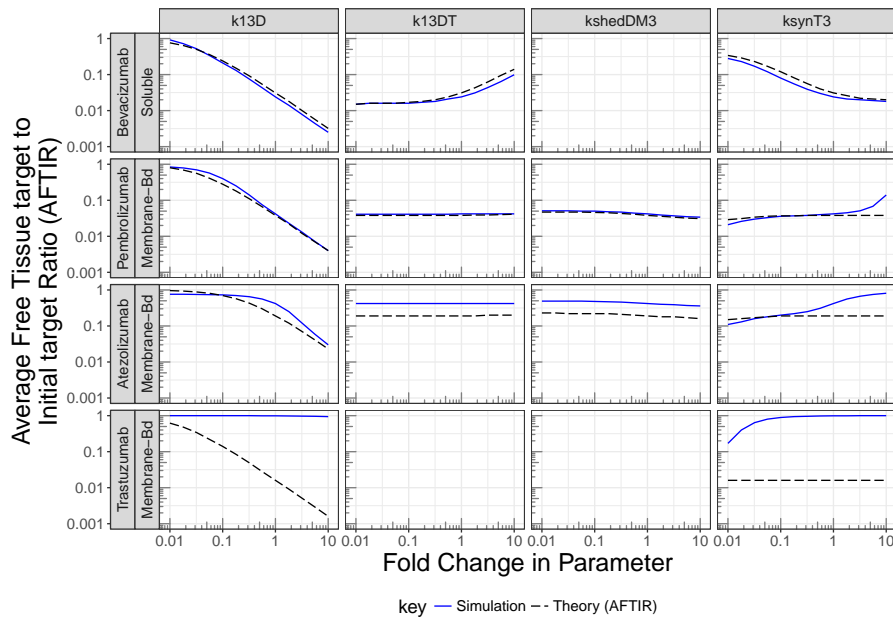


Fig. 4 Sensitivity analysis where the parameter at the top of each column is changed from 0.01x to 10x from its baseline value. There is in general good agreement between theory and experiment, except for trastuzumab, when the target expression is high. Kssd approximation.

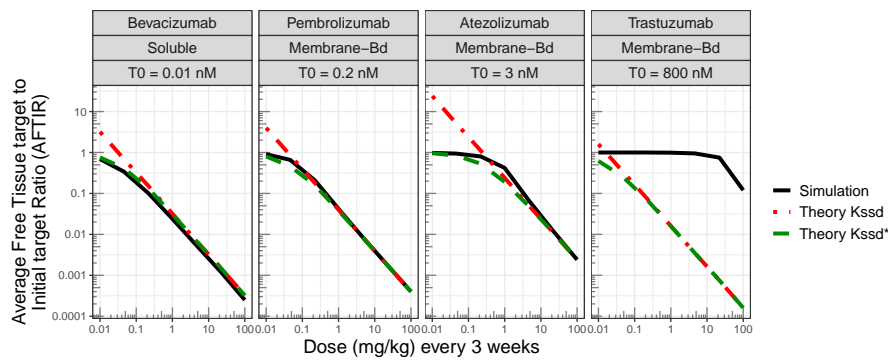


Fig. 5 Average Free Tissue target to Initial target Ratio (AFTIR) for four drugs with different baseline target expression levels (T_0) over a range of doses. The AFTIR approximation better matches the simulation than the AFTIR approximation for very small doses. For small doses, the simulation and AFTIR asymptotically approach 1, whereas AFTIR is unbounded.

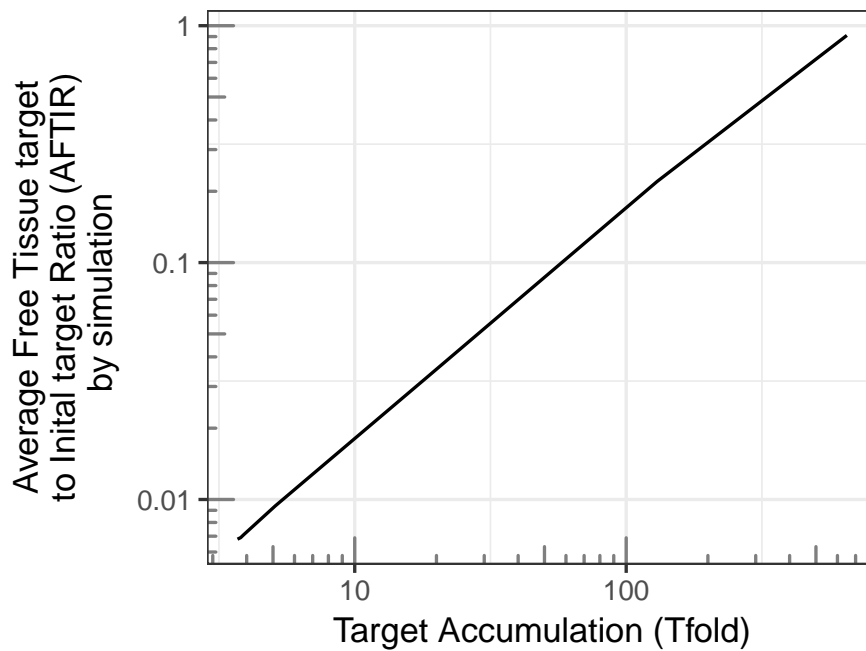


Fig. 6 Average Free Tissue target to Initial target Ratio (AFTIR) as a function of fold change in target (T_{fold}) for Bevacizumab.

C Supplementary Material

C.1 AFTIR Simulations

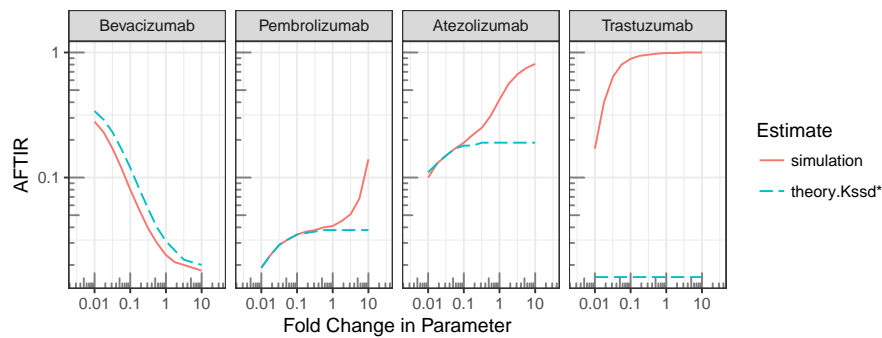


Fig. S1 Sensitivity analysis k_{13DT} has been set to zero gives better agreement for k_{synT3} . Here, the parameter at the top of each column is changed from 0.01x to 10x from its baseline value. There is in general good agreement between theory and experiment, except for trastuzumab, when the target expression is high. The agreement Sensitivity analysis when $k_{13DT} = 0$ shows

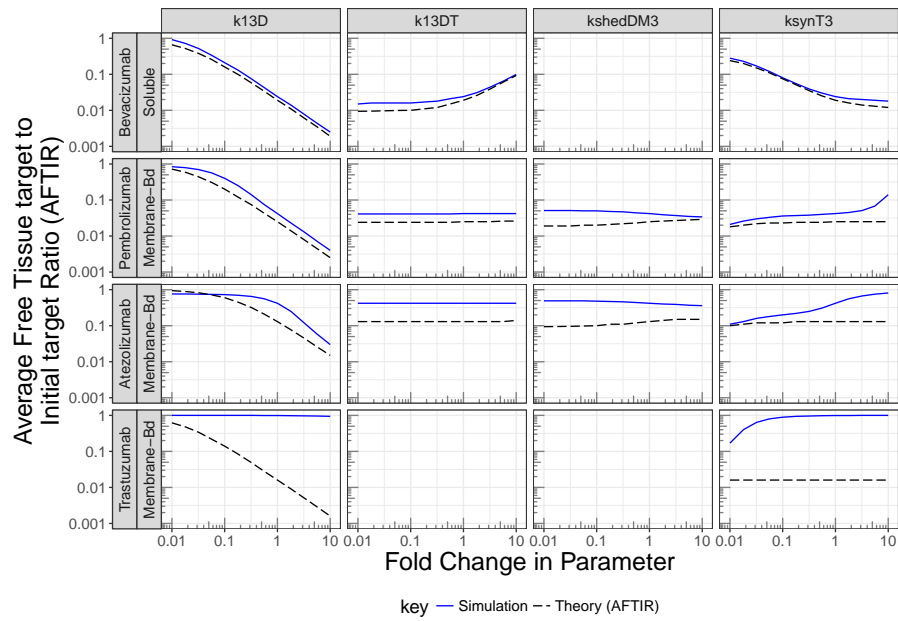


Fig. S2 Sensitivity analysis where the parameter at the top of each column is changed from 0.01x to 10x from its baseline value. There is in general good agreement between theory and experiment, except for trastuzumab, when the target expression is high. Kss approximation.

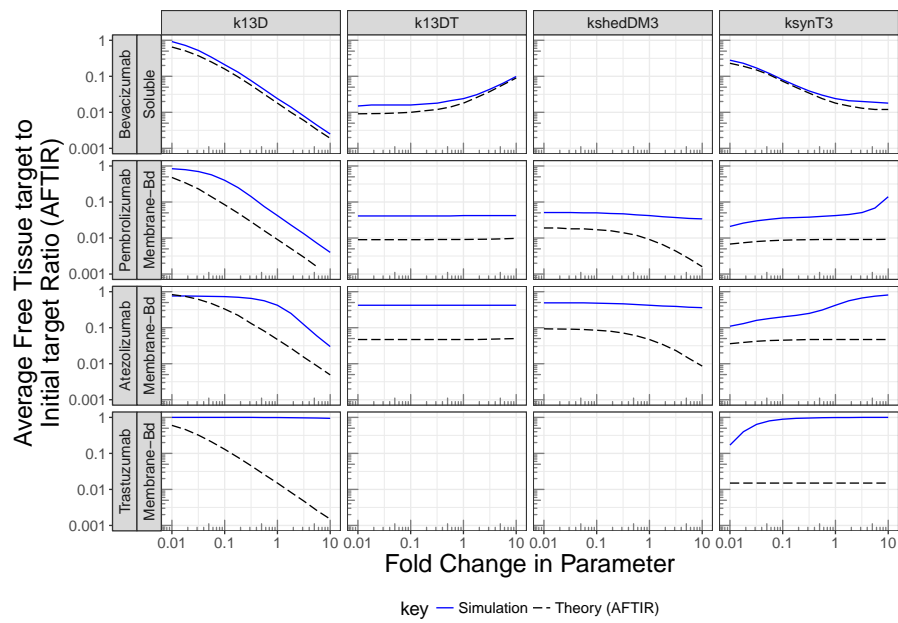


Fig. S3 Sensitivity analysis where the parameter at the top of each column is changed from 0.01x to 10x from its baseline value. There is in general good agreement between theory and experiment, except for trastuzumab, when the target expression is high. Kd approximation.

C.2 TFTIR simulations

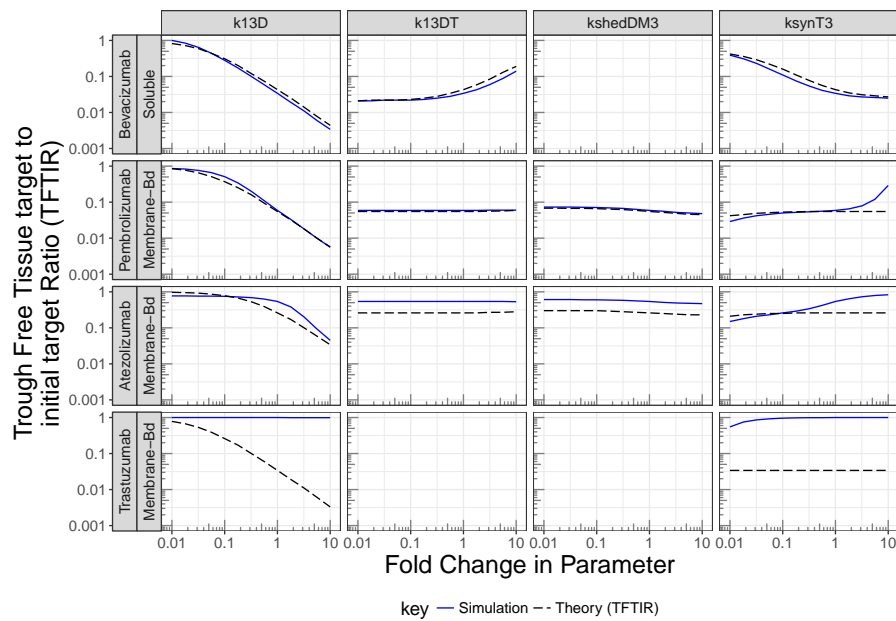


Fig. S4 Sensitivity analysis where the parameter at the top of each column is changed from 0.01x to 10x from its baseline value. There is in general good agreement between theory and experiment, except for trastuzumab, when the target expression is high. Kssd approximation.

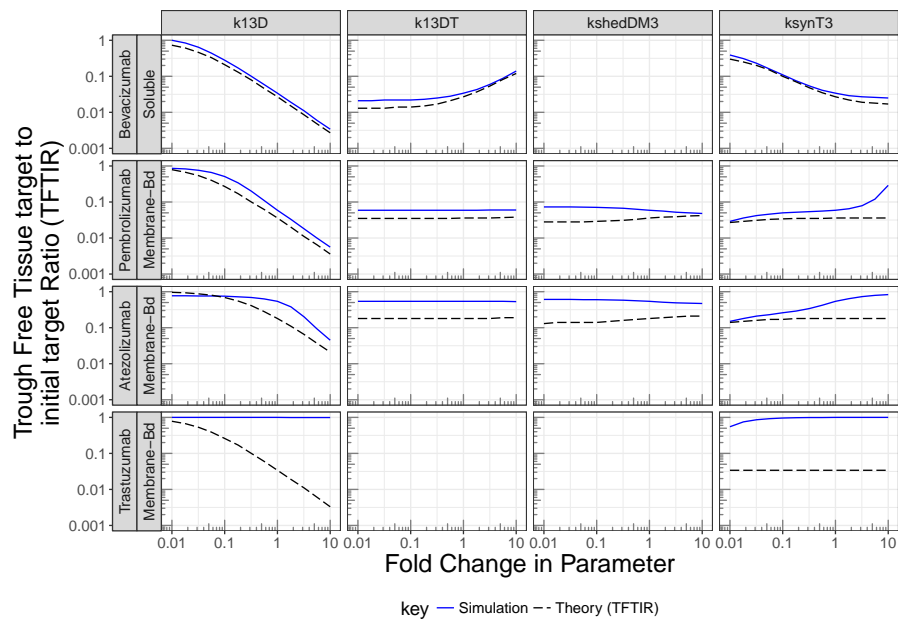


Fig. S5 Sensitivity analysis where the parameter at the top of each column is changed from 0.01x to 10x from its baseline value. There is in general good agreement between theory and experiment, except for trastuzumab, when the target expression is high. Kss approximation.

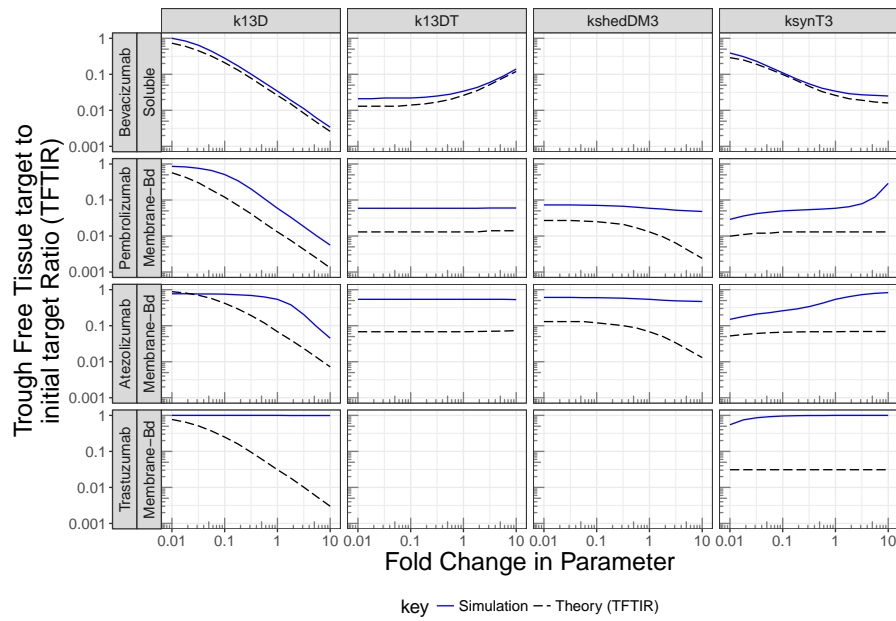


Fig. S6 Sensitivity analysis where the parameter at the top of each column is changed from 0.01x to 10x from its baseline value. There is in general good agreement between theory and experiment, except for trastuzumab, when the target expression is high. Kd approximation.