

Turning and twisting motion of chromosomes as an accelerating force to align homologous chromosomes during meiosis

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## Abstract

Homologous sets of parental chromosomes must pair during meiosis to produce recombined sets of chromosomes for their progeny. This is accompanied by nuclear oscillatory movements. This study aimed to elucidate the significance of these movements with a model, wherein external force was applied to the oscillating nucleus and via hydrodynamic interactions within the nucleus. Simulations revealed that a major force for aligning homologous chromosomes is length-dependent sorting during chromosomal turning and twisting, which occur when the nucleus reverses the direction of its movement.

Meiosis is an important process for eukaryotic organisms to generate inheritable haploid gametes from a diploid cell. During meiosis, homologous (paternal and maternal) chromosomes recombine; these recombined chromosomes are inherited by their progeny. For recombination of homologous chromosomes, side-by-side alignment of homologous loci along the chromosome is necessary [1]. During this alignment of homologous chromosomes, telomeres form a cluster beneath the nuclear envelope in various eukaryotic organisms [2].

Unicellular fission yeast *Schizosaccharomyces pombe* is a useful model system for studying the alignment of homologous chromosomes during meiosis [3, 4]. A meiotic cell of *S. pombe* contains 3 pairs of homologous chromosomes (chromosomes 1, 2, and 3 of 5.6, 4.6, and 3.5 Mb, respectively) [5]. During meiotic prophase, the nucleus elongates, oscillates between the cell poles, and shows drastic deformation, so-called “horsetail movement” [6], during which telomeres remain clustered at the spindle pole body (SPB) at the leading edge of the nuclear movement [6]. Telomere clustering and nuclear movements reportedly promote the alignment of homologous chromosomes [7,8,9].

To elucidate mechanisms underlying the alignment of homologous chromosomes, computer simulation strongly facilitates the examination and prediction of biological events under conditions that are never accomplished empirically. Various theoretical models of the pairing of homologous loci during meiosis have been proposed on the basis of telomere clustering [10, 11, 12, 13]. However, the role of the nuclear envelope, which confines the chromosomes, remains unknown in these models.

Studies are required to consider the role of the nuclear envelope in models of the meiotic nucleus of *S. pombe*, since its nucleus migrates and undergoes striking deformation during meiosis. During the horsetail movements, the nuclear envelope receives drag forces from the cytoplasm and from the nucleoplasm, while each chromosome receives drag forces only from the nucleoplasm. Thus, models of the meiotic nucleus of *S. pombe* would help describe the motion of the deformable nuclear envelope, direct collisions between the nuclear envelope and chromosomes, effects of the cytoplasm on the nuclear envelope, and effects of the nucleoplasm on chromosomes and the nuclear envelope, in addition to telomere clustering at the SPB. This study

aimed to investigate the role the horsetail nuclear movements in the alignment of homologous chromosomes via simulations of an initial model displaying the aforementioned nuclear membrane dynamics.

**Model construction:** A model of chromosomes confined within the nuclear envelope of *S. pombe* cells (Fig. 1(a)) was developed using the following methods. We described each chromosome as a chain and the nuclear envelope as a one-layered shell—both comprising particles with an excluded volume (Fig. 1(b)). A meiotic nucleus of *S. pombe* contains 3 homologous pairs of chromosomes; thus, the model contains 6 chains in total confined in the shell. To account for the effects of the SPB on chromosomal movement, we constructed a virtual sphere around the SPB (“the SPB sphere”), confining a limited area of the shell (nuclear envelope) extending toward the space inside the shell (Fig. 1(b)). To simulate telomere movement, which are clustered near the SPB during the horsetail movement, we assumed that ends of the chromosome chains move along the surface of the SPB sphere inside the shell.

To simulate the horsetail movements, we assumed that the SPB sphere oscillates periodically in the cell. Here, the drag force from the cytoplasm is exerted exclusively on the nuclear envelope. Since the cytoplasm can be considered a static intracellular fluid, we assumed that this drag force is proportional to the velocity of the nuclear envelope. However, the drag forces from the nucleoplasm to the nuclear envelope and chromosomes depend on the intranuclear velocity profile of the nucleoplasm, which is primarily determined on the basis of velocity profiles of chromosomes and the nuclear envelope. Thus, drag forces from the nucleoplasm could be described by the hydrodynamic interaction among particles in the chains and the shell.

These methods allowed for the generation of an appropriate model involving the effects indispensable for simulating the *S. pombe* meiotic nucleus.

**Model implementation:** We assumed that chromosomes 1, 2, and 3 consist of  $N_n$  particles ( $n = 1, 2, \text{ or } 3$ ) and the nuclear envelope consists of  $M$  particles with radii  $= r$ . The motion of the  $i$ -th particle is given as

$$m\ddot{\vec{x}}_i = -\gamma_i\dot{\vec{x}}_i - \nabla_i U(\{\vec{x}_i\}) + \sum_j \vec{F}_{ij} \quad (1)$$

where  $\vec{x}_i = (x_i, y_i, z_i)$  and  $m$  are the position and mass of the  $i$ -th particle, respectively.  $\gamma_i$  indicates the coefficient of a drag force from the cytoplasm where  $\gamma_i = 6\pi r\eta$  if the  $i$ -th particle is on the nuclear envelope and  $\gamma_i = 0$  if the  $i$ -th particle is on the chromosome. Here,  $\eta$  was assumed as the viscosity of cytoplasm.

In the second term of equation (1), the potential of the system  $U(\{\vec{x}_i\})$  is given as follows:

$$U(\{\vec{x}_i\}) = U_{cs} + U_{ms} + U_e \quad (2)$$

where  $U_{cs}$  is the contribution from the chain,  $U_{ms}$  is the contribution from the nuclear envelope, and  $U_e$  is the potential of the excluded volume effects.

The potential contribution from the chromosome chain  $U_{cs}$  is given as follows:

$$U_{cs} = \sum_i^{N_n-1} \frac{k_c}{2} (|\vec{x}_i - \vec{x}_{i+1}| - 2r)^2 + \sum_{i=telo} \frac{k'_c}{2} (|\vec{x}_i - \vec{X}_{SPB}| - (R_s + r))^2 \quad (3)$$

where the  $i$ -th particle is a part of the chain corresponding to  $n$ -th chromosome, and  $\vec{X}_{SPB}$  and  $R_s$  indicate the position of the center and the radius of the SPB sphere.

The potential contribution from the nuclear envelope  $U_{ms}$  is given as follows:

$$\begin{aligned} U_{ms} = & \sum_{i < j = near\ i} \frac{k_m}{2} (|\vec{x}_i - \vec{x}_j| - L_{i,j})^4 + \sum_{i\ in\ SPB} \frac{k'_m}{2} (|\vec{x}_i - \vec{X}_{SPB}| - L_{i,SPB})^2 \\ & + \frac{k_Y}{2} \left( \sum_i \frac{\pi r^2}{3} |\vec{x}_i - \vec{x}_{CM}| - V \right)^2 \\ & + \sum_i \theta((R_c - r) - \sqrt{x_i^2 + y_i^2}) \frac{k_w}{2} (\sqrt{x_i^2 + y_i^2} - (R_c - r))^2 \end{aligned} \quad (4)$$

where the  $i$ -th particle is a part of the nuclear envelope.  $\theta$  is Heaviside step function and  $L_{i,j}$  indicates the initial distance between the centers of the  $i$ -th and  $j$ -th particles constructing the nuclear envelope ( $L_{i,SPB}$ , the initial distance between the centers of the  $i$ -th particle and the SPB sphere). Here, the initial structure of the nuclear envelope is

indicated as a spherical shell with a thickness of one particle layer constructed by the rings along with  $y$ -axis with various radii consisting of particles (Fig. 1(c)), and initial position of the center of the SPB sphere is denoted as  $\overrightarrow{X_{SPB}} = (R_c, 0, 0)$  ( $R_c$  is the radius of the cell as described below). We used an unharmonic potential in the 1st term of  $U_{ms}$ , which provides tension between particles in the nuclear envelope since the nuclear envelope seems to be able to deform easily.

The second term of  $U_{ms}$  indicates the binding of the SPB to the nuclear envelope, where particles constituting the nuclear envelope and confined in the SPB sphere were connected tightly to the center of the SPB sphere. The third term of  $U_{ms}$  provides the force to sustain the volume of the cell nucleus where  $\overrightarrow{x_{CM}}$  and  $V$  indicate the position of the center of mass and the volume of the nucleus, respectively. Here,  $V$  is denoted by  $\sum_i \frac{\pi r^2}{3} |\overrightarrow{x_i} - \overrightarrow{x_{CM}}|$  with initial values of  $\overrightarrow{x_i}$ . The fourth term of  $U_{ms}$  indicates the excluded volume effect of the cell wall, where the cellular shape was assumed to be a parallel cylinder along the  $z$ -axis, with a radius  $R_c$ . Here, the central axis of this cylinder is denoted as  $(0, 0, z)$ , and  $\theta$  indicates the Heaviside function.

$U_e$  denotes the potential of the excluded volume effects among particles and the SPB sphere as follows:

$$U_e = \sum_{i < j} \theta(|\overrightarrow{x_i} - \overrightarrow{x_j}| - 2r) \frac{k_e}{2} (|\overrightarrow{x_i} - \overrightarrow{x_j}| - 2r)^2 + \sum_i \theta(|\overrightarrow{x_i} - \overrightarrow{X_{SPB}}| - (R_s + r)) \frac{k'_e}{2} (|\overrightarrow{x_i} - \overrightarrow{X_{SPB}}| - (R_s + r))^2 \quad (5).$$

In the third term of equation (1),  $\overrightarrow{F_{ij}}$  indicates the force of hydrodynamic effects from the  $j$ -th particle to the  $i$ -th particle, providing a drag force to each particle from the nucleoplasm. Herein, we employ the lubrication approximation [14, 15], which is denoted as follows:

$$\vec{F}_{ij} = \begin{cases} \frac{3}{2}r^2\pi\eta \frac{(\vec{x}_j - \vec{x}_i) \cdot \vec{n}_{ij}}{L_{ij} - 2r} \vec{n}_{ij} & (\text{if } |\vec{x}_j - \vec{x}_i| > 2.001r) \\ \frac{3}{2}r^2\pi\eta \frac{(\vec{x}_j - \vec{x}_i) \cdot \vec{n}_{ij}}{0.001r} \vec{n}_{ij} & (\text{if } |\vec{x}_j - \vec{x}_i| \leq 2.001r) \end{cases} \quad (6)$$

where  $r$  and  $\vec{n}_{ij}$  denoted the radius of the particle and a relative unit vector from the  $j$ -th particle to the  $i$ -th particle  $\vec{n}_{ij} = \frac{\vec{x}_i - \vec{x}_j}{|\vec{x}_i - \vec{x}_j|}$ , respectively. Nucleoplasm viscosity was assumed the same as the cytoplasm viscosity  $\eta$  in this model.

**Parameters for simulations:** In the simulations, we assumed a particle radius  $r = 0.084 \times 10^{-6} (m)$ , where each particle models a local region of chromatin of  $\sim 100$  kb. Here, chromosomes 1, 2, and 3 (5.6 Mb, 4.6 Mb, and 3.5 Mb, respectively) were described by the chains consisting of 56, 46, and 34 particles ( $N_1 = 56$ ,  $N_2 = 46$ , and  $N_3 = 34$ ; we considered  $N_3$  as an even number for convenience of analysis). The nuclear envelope was constructed using 994 particles with  $r = 0.084 \times 10^{-6} (m)$  ( $M = 994$ ). Here, the inner diameter of the initial spherical structure of the nuclear envelope was assumed to be  $2.7 \times 10^{-6} (m)$ , the initial distance between the center of the SPB sphere and that of the nucleus was assumed to be  $2.0 \times 10^{-6} (m)$ , and the radius of the SPB sphere was assumed  $R_s = 10r$  (Fig. 1(b)). In this case, the diameter of the cross-section where nucleus and the SPB sphere intersect was  $\sim 1.0 \times 10^{-6} (m)$ . The initial configurations of the chromosomes were randomized in this spherical shell.

The viscosity of nucleoplasm and cytoplasm  $\eta$  was  $\sim 0.64 (kg m^{-1} s^{-1})$  [12]. The elastic constants were assumed as appropriate values as  $k_c = k_w = k_e = k'_e = 2.77 \times 10^8 (kg s^{-2})$ ,  $k'_c = 6.22 \times 10^8 (kg s^{-2})$ ,  $k_m = 4.77 \times 10^{20} (kg s^{-2} m^{-2})$ ,  $k'_m = 8.12 \times 10^8 (kg s^{-2})$ , and  $k_v = \frac{150}{\pi} k_m$  for the present model to reproduce a similar shape variation of the nuclear envelope via horsetail movements. We also assumed  $m = 5.3 \times 10^{-10} (kg)$  to economize on the simulation cost, as smaller values of  $m$  incur a higher simulation cost. Herein, we selected a sufficiently small  $m$  with which the velocity of each particle relaxes rapidly with no overshooting motion. We confirmed that the following results were qualitatively unaffected by small changes in these parameters. Thus, we consider these parameters appropriate to simulate intracellular environment.

**Results:** To evaluate the effects of the horsetail movement, we simulated the following four cases of motions of the SPB sphere in the cylinder (cell) with radius  $R_c = 2 \times 10^{-6} (m)$  as shown in Fig. 2: (a) 3-d 8-shaped oscillatory motions as  $\overrightarrow{X}_{SPB} = (R_c - B(1 - \cos 4\pi wt), C \sin 4\pi wt, A \cos 2\pi wt)$ , (b) 3-d O-shaped oscillatory motions as  $\overrightarrow{X}_{SPB} = (R_c - B(1 - \cos 4\pi wt), C \sin 2\pi wt, A \cos 2\pi wt)$ , (c) 1-d motions as  $\overrightarrow{X}_{SPB} = (R_c, 0, A \cos 2\pi wt)$ , and (d) 1-d constant velocity linear motion as  $\overrightarrow{X}_{SPB} = (R_c, 0, \pi w A t)$ . Herein,  $A = 7.3 \times 10^{-6} (m)$  and  $w = \frac{1}{3} \times 10^{-2} (s^{-1}) (= 12 (h^{-1}))$

since the SPB completes 30 oscillations in 2 ~3 h from end to end in spheroid-shaped *S. pombe* cells [9]. Furthermore, we assumed  $B = 0.208 \times 10^{-6} (m)$ , and  $C = 0.67 \times 10^{-6} (m)$ . The results were qualitatively independent of the detail values of  $B$  and  $C$ .

Chromosomal behavior in the migrating nucleus was simulated under the aforementioned 4 conditions. Simulations were repeated with eight initial states for each condition (Figs. 3, 4, and Supplementary movies 1 and 2). Figure 3 shows typical snapshots for  $t = 75, 3375, \text{ and } 7950 (s)$  in an example of 8-shaped 3-d oscillatory motion. Elongation of the nuclear envelope (Supplementary movie 1) and switching of relative positions among chromosomes (Fig. 3, Supplementary movie 2) were observed during oscillatory motions of the SPB. The present results indicate the validity of our simulations.

To obtain a pictorial view of chromosomal movements, we plotted positions of the chromosomes as probability distributions along the x-y plane (Fig. 4). The plots were obtained from the 34 ( $= N_3$ ) nearest particles from the SPB sphere ( $N_3 / 2 = 17$  nearest particles from each end) along each of the 6 chromosomes (Fig. 4a). Figure 4b shows typical snapshots of the probability distributions of particles for  $t = 75, 3375, \text{ and } 7950 (s)$  in the 3-d 8-shaped oscillatory motion. The probability distributions of particles indicated that each homologous chromosome pair converged temporally and non-homologous chromosomes were separated from each other.

Figure 4 (c) – (d) show typical snapshots of the probability distributions of particles at  $t = 7950 (s)$  when the SPB sphere exhibits a 3-d O-shaped oscillatory motion, a 1-d



oscillatory motion, and a linear motion. As shown in Fig. 4 (a) and (c), the probability distributions of particles in each homologous pair of chromosomes converge temporally and non-homologous chromosomes separate from each other when the SPB sphere exhibits 3-d oscillatory motion involving twisting of chromosomes during turning.

However, when the SPB sphere exhibits 1-d oscillatory motion involving no twisting motion of chromosomes during turning, some homologous chromosome pairs often stay separated from each other (Fig. 4 (d); separation of non-homologous chromosomes was observed exceptionally only in one out of eight simulations). Furthermore, separation of non-homologous chromosomes was not apparent when the SPB sphere exhibits a linear motion involving no chromosomal turning or twisting (Fig. 4 (e)). These results suggest that chromosomal turning and twisting motion is crucial for shuffling of chromosomes for appropriate alignment of homologous chromosomes.

Non-homologous chromosomes are considered to separate owing to differences in chain lengths among non-homologous chromosomes. During the horsetail movement, the SPB movement reverses its direction periodically. Chromosomes receive drag forces from the nucleoplasm at every turn of the SPB, while no drag force is exerted on chromosomes and the nuclear envelope if SPB migrates linearly with a constant velocity. During reversal of SPB, the region distal from the SPB in longer chromosomes tends to be dragged by the slow (nearly stopped) motion of the rear region of the bent nucleus, while that in the shorter one tends to follow the SPB motion (Fig. 5). Thus, the relative positions of longer and shorter chromosomes tend to separate gradually from each other owing to reversal of the iterative direction of the SPB movement, resulting in the separation of non-homologous chromosomes. Owing to this separation, homologous chromosomes are aligned and stabilized during the periodic reciprocation of the SPB.

**Discussion:** Homologous chromosome pairing has received increasing attention in studies in physics, and several models have been proposed to describe its underlying mechanisms [10, 11, 12, 13, 16]. In the present simulations, separation of non-homologous chromosomes was achieved when the SPB sphere shows 3-d oscillations in the cell, but not when the SPB sphere exhibits only a linear motion. This result is further substantiated by previous experimental evidence regarding *S. pombe*: the efficiency of homologous recombination decreases drastically when the nucleus

does not exhibit the horsetail movement but just elongates [17]; the iterative reversals of the direction of the SPB movement during the horsetail movement are essential for the alignment of homologous chromosomes via separating non-homologous chromosomes [7, 9]. Our simulation reveals that a major force for the alignment and sorting of homologous/non-homologous chromosomes is the nucleoplasmic flow generated owing to SPB reversal and deformation of the nuclear envelope, involving direct collision and indirect hydrodynamic interactions between chromosomes and the nuclear envelope, which were previously unclear. The present model is the first, to our knowledge, to consider both direct collisions and indirect hydrodynamic interactions as essential mechanisms for the alignment of homologous chromosomes.

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## Figure legends

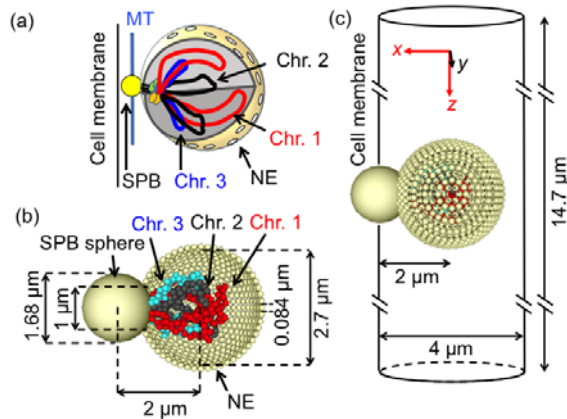


FIG. 1. (a) Illustration of the meiotic nucleus of *Schizosaccharomyces pombe* containing 3 homologous pairs of chromosomes (Chr. 1, 2, and 3), the nuclear envelope (NE), the spindle pole body (SPB), and microtubules (MT). (b) Illustration of the model composed of particle populations. (c) Illustration of the model of an intracellular region described as a cylindrical space, and the initial structure of the nuclear envelope constructed by combining particle rings (along dashed circles) along the vertical  $y$ -axis with various radii.

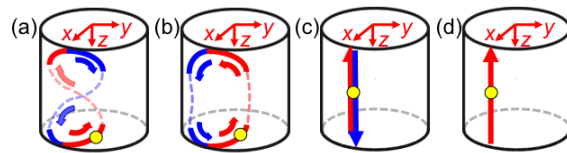


FIG. 2. Illustration of trajectories of the spindle pole body (SPB) sphere motions in the cell (cylindrical space). (a) 3-d 8-shaped oscillatory motions, (b) 3-d O-shaped oscillatory motions, (c) 1-d oscillatory motions, and (d) 1-d constant velocity linear motion. Yellow particle indicates the SPB sphere; red and blue arrows indicate the trajectory of downward and upward motion, respectively.

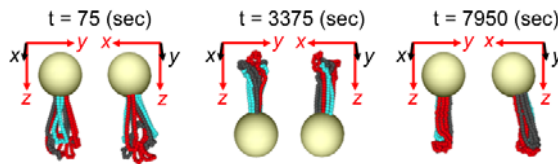


FIG. 3. Typical time course of chromosome dynamics in the case that the spindle pole body (SPB) sphere exhibits 3-d 8-shaped oscillation. Snapshots of chromosome configurations in the nucleus from two points of view (projected on  $y$ - $z$  and  $x$ - $z$  plane) at time  $t = 75$  s (after 0 oscillations), 3375 s (after 10 oscillations), and 7950 s (after 26 oscillations). The large sphere indicates the SPB sphere; red, black, and blue particle chains indicate Chr. 1, Chr. 2, and Chr. 3, respectively.

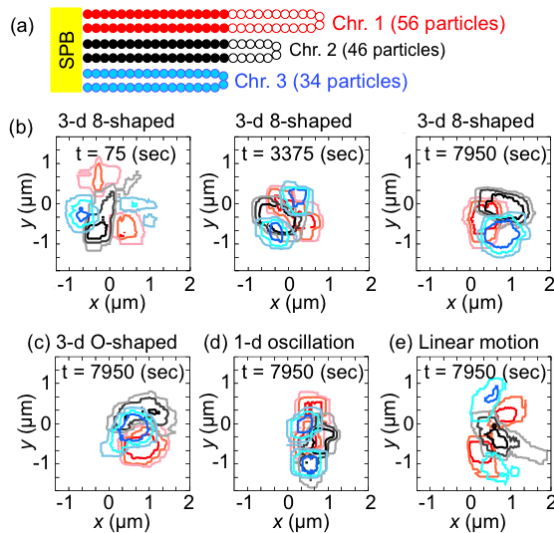


FIG. 4. Probability distributions of particles in each of the chromosome chains near the spindle pole body (SPB) sphere along the  $x$ - $y$  plane. (a) The 34 ( $= N_3$ ) nearest particles from the SPB sphere along each of the 6 chromosomes (filled particles) were used to estimate probability distributions. (b) Probability distributions of the 34 ( $= N_3$ ) nearest particles on each chromosome indicated as filled particles in (a). Curves represent contour lines of probability distributions of particles in the 3-d 8-shaped oscillation of the SPB sphere at  $t = 75$ , 3375, and 7950 s; red, black, and blue curves indicate Chr. 1,

Chr. 2, and Chr. 3, respectively. The intensity of the contour lines represents the probability values of 0.3, 0.5, and 0.75 in an increasing order of darkness. (c) – (e) Probability distributions at  $t = 7950$  s in (c) 3-d O-shaped oscillation, (d) 1-d oscillations, and (e) constant velocity linear motion of the SPB sphere. Colors of the contour lines represent probability distributions of each chain as in (b).

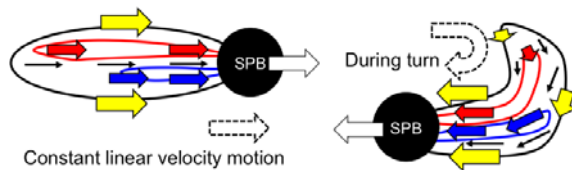


FIG. 5. Illustration of velocities of the spindle pole body (SPB; white arrow), long and short chromosomes (red and blue arrows, respectively), the nuclear envelope (yellow arrows), and the nucleoplasmic flow (black arrows). When the SPB exhibits a constant linear velocity motion, all regions of the nuclear envelope, the nucleoplasm, and chromosomes relax to the same velocity as the SPB (Left). During the turn of the SPB, the regions of the nuclear envelope, the nucleoplasm, and chromosomes at the nuclear front end (near the SPB) follow the motion of the SPB, while those at the nuclear rear end are almost stopped (Right). In the latter case, longer chromosomes tend to be dragged by the slow motion of the nuclear rear region, while shorter chromosomes tend to follow the motion of the SPB.