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The rise and fall of the new variant of *Chlamydia trachomatis* in Sweden: mathematical modelling study

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Contents

S1: Model description.....	2
Overview.....	2
Sexual mixing and force of infection	3
Model parameterisation.....	5
S2: Data.....	6
S3: Basic reproduction number	8
S4: Sensitivity analysis: fitness affects duration of infection	8
S5: Proportion of infected people that is treated	10
References	12

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S1: Model description

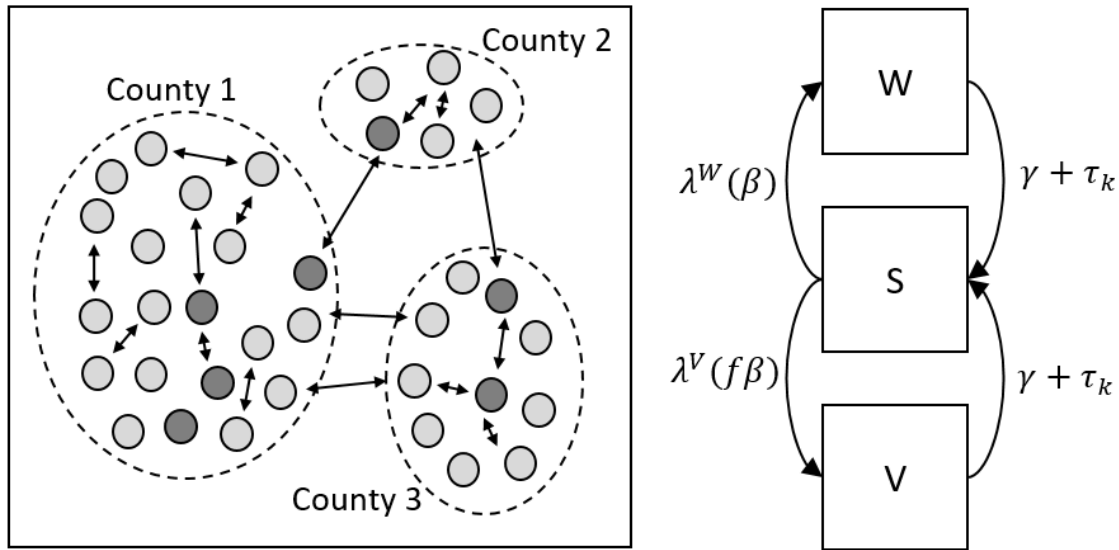


Figure S1 A) Representation of a meta-population model for sexually active heterosexual people of lower sexual activity class (light grey) and of a higher sexual activity class (dark grey) in three different counties. The proportion of high-activity individuals is the same in all counties. Partnerships are represented as two-head arrows. (B) Structure of infection transmission model. Individuals have three infection states: uninfected and susceptible (S), infected with wtCT (W) and infected with nvCT (V). Arrows represent transitions between infection states. Transition rates: $\lambda^W(\beta)$ force of infection for becoming wtCT infected, depending on transmission probability β ; $\lambda^V(f\beta)$ force of infection for becoming nvCT infected, depending on transmission probability β and fitness for nvCT (f); γ natural clearance rate; τ_k treatment rate, depending on type of county k (AR/BD). All rates except γ are also time-dependent.

Overview

We developed a mathematical model to describe heterosexual *C. trachomatis* transmission and the spread of the nvCT in Sweden (Figure S1). We implemented the spatial structure of Sweden consisting of 21 counties as a meta-population model. We modeled the population of 15-29 year old Swedish sexually experienced adults, subdivided into a low and a high sexual activity class. In the model, people can be susceptible people (S), infected with the wtCT (W) and infected with the nvCT (V). We assumed that wtCT is representative of all CT strains that are co-circulating with nvCT. We used the following system of ordinary differential equations (ODE):

$$\frac{dS_{j,k}}{dt} = -(\lambda_{jk}^W + \lambda_{jk}^V) S_{jk} + \gamma(W_{jk} + V_{jk}) + \tau_k(t)(W_{jk} + V_{jk}),$$

SUPPLEMENTARY MATERIAL

$$\frac{dW_{jk}}{dt} = \lambda_{jk}^W S_{jk} - \gamma W_{jk} - \tau_k(t) W_{jk},$$

$$\frac{dV_{jk}}{dt} = \lambda_{jk}^V S_{jk} - \gamma V_{jk} - \tau_k(t) V_{jk}.$$

Here subscripts j denotes sexual activity class and k the county. Susceptible people can be infected with the wtCT or the nvCT at rate λ_{jk}^W and λ_{jk}^V , respectively (the forces of infection). Infected people clear infection naturally at rate γ , or may be treated for infection at rate $\tau_k(t)$, dependent on time, county and on whether they were infected with the wtCT or with the nvCT. We assume in the model that before October 2006, in all counties wtCT infected people were treated at a fixed rate τ . In counties using AR tests, nvCT infected people were not treated, whereas nvCT infected people were treated at the same rate τ in counties using BD tests. We assume that after October 2006, both wtCT and nvCT can be diagnosed and treated. The increased number of tests done directly after 2006 (Fig. S2) suggests a higher treatment rate after the nvCT was discovered. We model this by assuming that $\tau_k(t)$ was a certain percentage point (π) higher than τ in October 2006, and that this percentage linearly decreased to zero within 3 years after this month. Therefore, $\tau_k(t)$ is parameterized as follows:

$$\tau_k(t) = \begin{cases} \tau & \text{if } k = BD \text{ and } t < 2007 \\ 0 & \text{if } k = AR \text{ and } t < 2007 \\ \tau + \pi\tau(1 - 1/3(t - 2007)) & \text{if } k \in \{AR, BD\} \text{ and } 2007 \leq t < 2010 \\ \tau & \text{if } k \in \{AR, BD\} \text{ and } t \geq 2010 \end{cases}$$

Sexual mixing and force of infection

In our model, the time-dependent forces of infection exerted by the wtCT (λ_{jk}^W) and nvCT (λ_{jk}^V) depend on assumptions about transmission rates and sexual contact preferences between individuals from different sexual activity classes and counties. We model them as:

$$\lambda_{jk}^W = c_j \beta \sum_i \sum_l M_{kl} (\epsilon \delta_{ij} + (1 - \epsilon) \frac{c_i N_{il}}{\sum_i c_i N_{il}}) \frac{W_{il}}{N_{il}},$$

$$\lambda_{jk}^V = c_j f \beta \sum_i \sum_l M_{kl} (\epsilon \delta_{ij} + (1 - \epsilon) \frac{c_i N_{il}}{\sum_i c_i N_{il}}) \frac{V_{il}}{N_{il}}.$$

SUPPLEMENTARY MATERIAL

Here c_j is the sexual partner change rate and β the per partnership transmission probability. Parameter f denotes the relative fitness of the nvCT compared to the wtCT, where we assume that a potential fitness difference between the wtCT and the nvCT increases or decreases the per partnership transmission probability, rather than the duration of infection.

We model a certain degree of assortative mixing with respect to activity classes i and j by parameter ϵ , which takes values between 0 and 1. Here, δ_{ij} is the Kronecker delta, which equals 1 if $i = j$ and 0 otherwise. Therefore, $\epsilon = 0$ corresponds to proportional (random) mixing where sexual partners are chosen in proportion to the size of their sexual activity class; $\epsilon = 1$ corresponds to fully assortative mixing where people only have sexual contacts with people from the same sexual activity class.

Sexual mixing between individuals from counties k and l was modeled through matrix M_{kl} , containing the conditional probabilities that somebody from county k has a sexual contact with somebody from county l . We assumed here that there are more sexual contacts between counties with large population sizes compared to counties with smaller populations. Further, we assume that the number of sexual contacts is inversely related to the distance between counties. By these assumptions, we defined a gravity matrix Φ with entries

$$\Phi_{kl} = \frac{N_k N_l}{d_{kl}^\rho},$$

where N_k is the population size of county k , and d_{kl} is the distance between the geographical centers of counties k and l , as a proxy for the average distance of all contacts in these counties. Parameter ρ controls the dependence of sexual mixing on distance between people living in different counties. Using Φ only, mixing within counties as compared to mixing between counties is still undefined. Therefore, we used algebraic manipulations proposed by Riesen et al¹ to reconstruct the mixing matrix M from Φ . We rescaled Φ by a scaling factor s and weighted all columns with the inverse of the population size of a county:

$$M_{kl} = s \frac{\Phi_{kl}}{N_k}.$$

SUPPLEMENTARY MATERIAL

We then replaced the diagonal entries of M_{kl} with the sum of all entries outside county k :

$$M_{kk} \rightarrow 1 - \sum_{l \neq k} M_{kl}.$$

We chose the scaling factor s such that the proportion of new sexual contacts made within a county, weighted across the county population sizes, equals model parameter α . Then

$$\sum_k M_{kk} \frac{N_k}{\sum_k N_k} = \alpha.$$

Model parameterisation

Model parameters are shown in Table 1 of the main text. We use data from Natsal-2² specifying the number of new sexual partners per year to parametrize parameters c_j and q_j . We assumed that the distribution of reported number of new heterosexual partners is the sum of two Poisson distributions with means c_j , weighted by the proportion of individuals in each sexual activity class, q_j (with $q_1 = 1 - q_2$).³ Fitting to the data was performed with maximum likelihood estimation methods. The duration of asymptomatic untreated infection ($1/\gamma$) was taken from an evidence synthesis study.⁴ We inferred the values of the variable parameters using Markov Chain Monte Carlo (MCMC), by comparing the time-dynamic model trajectories to the empirical data. We ran three separate MCMC chains each simulating 50.000 MCMC steps, using the R package BayesianTools. In the MCMC algorithm we assumed a binomial likelihood for the data about proportions of the nvCT. For the diagnoses data, we assumed a negative binomial likelihood with parameters $\mu(\theta)$ (the model computed number of diagnoses, as function of the model parameters θ) and var (the variance of number of diagnoses). The parametrization $NegBin(\mu, var)$ is sometimes referred to as the “ecological parametrization” of the negative binomial distribution⁵, p. 165. It is a more dispersed distribution than the Poisson distribution through the factor $disp \geq 1$. If $disp = 1$ then this distribution is equal to the Poisson distribution. The relation with the original parametrization of the Negative Binomial distribution ($NegBin(r, p)$) is $r = \frac{\mu^2}{var - \mu}$ and $p = \frac{var - \mu}{var}$. So we take

$$var = \frac{\mu(\theta)^2}{\mu(\theta) * disp - \mu(\theta)} = \frac{\mu(\theta)}{disp - 1}.$$

SUPPLEMENTARY MATERIAL

The dispersion parameter *disp* is not inferred in the mcmc sampling algorithm but, instead, a value of $10^{0.5}$ is assumed for this parameter, reflecting a moderate dispersion. By this choice of dispersion, the data about proportions of the nvCT get a similar weight in the posterior log-likelihood as the diagnoses data.

Convergence of the MCMC chains was checked by computing the Gelman-Rubin convergence diagnostic.⁶

S2: Data

In Tables S1 and S2 we have tabulated the data used in the MCMC simulations to infer the variable model parameters.

Table S1 Data used in the model on the proportion of the nvCT in different counties and years (isolates of genotype nvCT / all isolates)

County	2006	2007	2008	2010	2014
Blekinge	7/106	-	-	-	-
Dalarna	520/812	104/204	42/172	64/253	18/292
Halland	140/584	-	-	-	-
Kalmar	38/188	-	-	-	-
Norrbottn	12/115	31/231	35/185	33/297	19/361
Örebro	63/162	97/261	55/233	34/151	25/374
Södermanland	36/119	-	-	-	-
Skåne	455/1896	-	-	-	-
Stockholm	26/115	-	-	-	-
Uppsala	50/263	62/230	37/206	31/262	18/336
Västra Götaland	24/93	-	-	-	-

Table S2 Data used in the model on the number of diagnoses in different counties and years

County	2004	2006	2007	2008	2009
Dalarna	1037	907	2446	1579	1293
Norrbottn	964	1023	967	991	969

SUPPLEMENTARY MATERIAL

Örebro	875	854	1294	1245	1282
Uppsala	1194	1353	1611	1490	1218

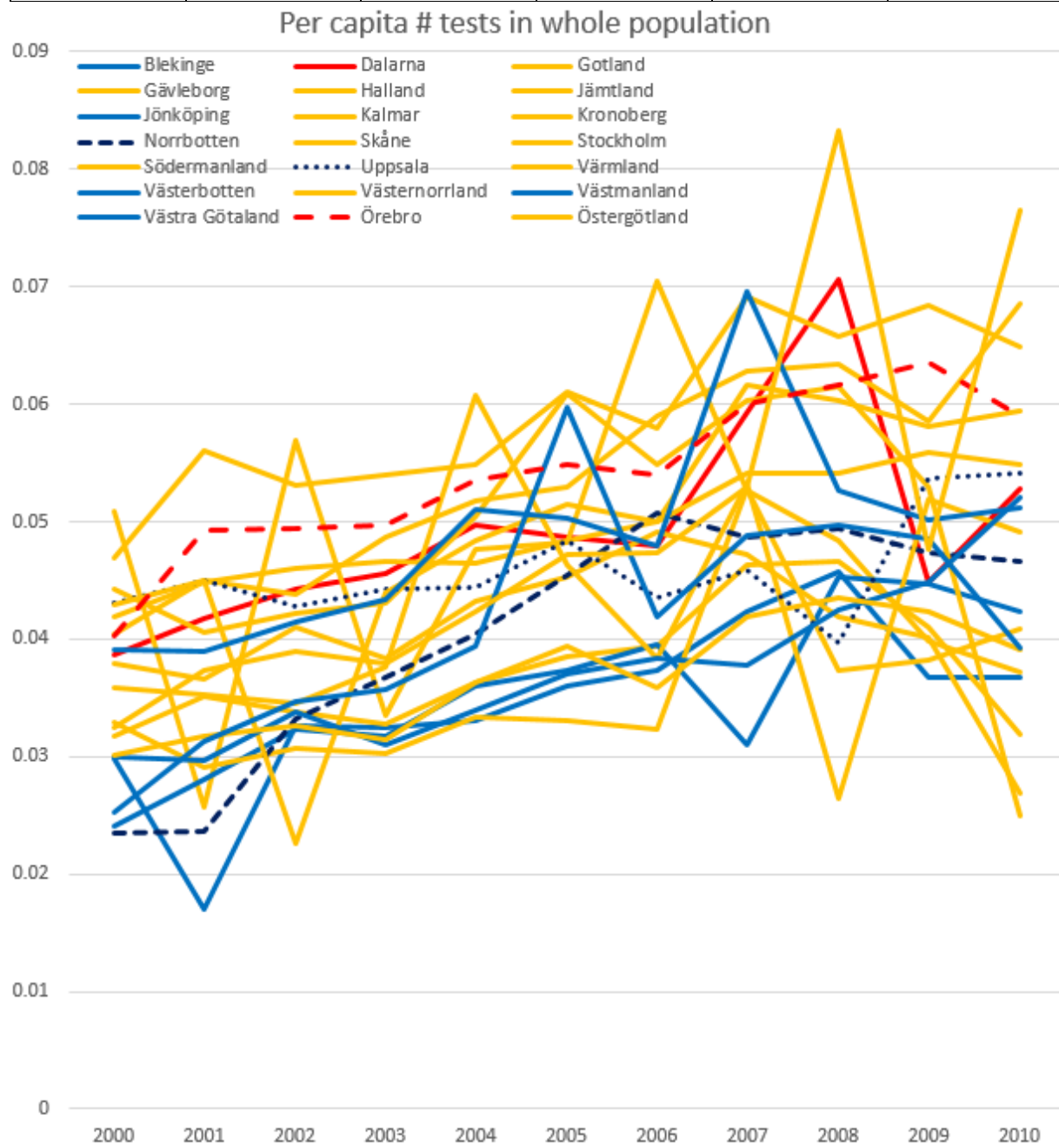


Figure S2 Per capita number of tests in the whole population (data not used in the model)

SUPPLEMENTARY MATERIAL

S3: Basic reproduction number

The basic reproduction number, R_0 , can be calculated using the next-generation matrix method as described by Diekmann et al.^{7,8} It is different for the wtCT, the nvCT before discovery and the nvCT after discovery. As we did not consider sex-specific differences in sexual behavior or the natural history of chlamydia, and assumed that the sexual behavior of individuals is the same across all Swedish counties, we can simplify the model into a single population with two different sexual activity groups. For wtCT, the transmission matrix T is given by

$$T = \begin{bmatrix} \beta c_l \rho_{ll} N_l / N_l & \beta c_l \rho_{lh} N_l / N_h \\ \beta c_h \rho_{hl} N_h / N_l & \beta c_h \rho_{hh} N_h / N_h \end{bmatrix}.$$

For nvCT, the transmission matrix is equal before and after discovery. It is given by fT , where f is the difference in fitness between wCT and nvCT.

The transition matrix Σ for wCT and nvCT after discovery is given by

$$\Sigma = \begin{bmatrix} -(\gamma + \tau) & 0 \\ 0 & -(\gamma + \tau) \end{bmatrix}.$$

The transition matrix Σ for nvCT before discovery is given by

$$\Sigma = \begin{bmatrix} -\gamma & 0 \\ 0 & -\gamma \end{bmatrix}.$$

R_0 is defined as the dominant eigenvalue of the next-generation matrix $K = -T \Sigma^{-1}$.

S4: Sensitivity analysis: fitness affects duration of infection

Table S1 shows the prior and posterior distributions of the model parameters if we assumed that a difference in fitness between the wtCT and the nvCT affects the duration of infection, rather than the per partnership transmission probability (Table 1 main text). For the nvCT, parameter γ is replaced by γ/f in the model equations.

SUPPLEMENTARY MATERIAL

Table S3 Description of fixed and variable model parameters, and model derived quantities (mean and 95% CI of posterior distributions). Only results for the model in which we assumed that nvCT emerged in Dalarna (M1) are shown. Assumed: difference in fitness between wtCT and nvCT affects duration of infection.

Fixed parameters		Value	Source
q_j	Proportion in risk group	0.93, 0.07	²
c_j	Partner change rates	0.59, 6.57	²
γ	Chlamydia clearance rate (per year)	0.73	⁴
C	County where nvCT emerged	1-21	Methods
Variable parameters		Prior	Posterior*
ρ	Between-county mixing dependency on distance	unif(0,2)	1.12 (0.87-1.34)
α	Average fraction of new contacts inside of county	unif(0,1)	0.75 (0.72-0.77)
β	Per partnership transmission probability	unif(0,1)	0.93 (0.84-1.00)
ϵ	Assortativity index risk groups	unif(0,1)	0.04 (0.00-0.16)
f	Relative fitness of nvCT compared to wtCT (affects duration of infection)	unif(0.7,1.3)	0.18 (0.16-0.19)
τ	Treatment rate (wtCT) per year	unif(0,3)	2.31 (1.97-2.70)
π	Maximal increase of treatment rate τ after October 2006	unif(0,0.25)	0.00 (0.00-0.02)
Δ	Number of months that the nvCT remained undiscovered until October 2006	unif(36,144)	44 (37-52)
Model derived quantities		Posterior*	
Year of emergence		Jan '03 (Nov '02-Aug '03)	
Proportion treated**		0.76 (0.73-0.79)	
Prevalence before emergence		1.03 (0.85-1.21)	
Max prevalence***		3.01 (2.62-3.55)	
R_0 wtCT		1.07 (1.06-1.08)	
R_0 nvCT before discovery		3.66 (3.27-4.08)	
R_0 nvCT after discovery		1.01 (1.00-1.02)	

* (median, 95% credible interval). ** Computed as $\tau/(\tau + \gamma)$. *** Prevalence in Dalarna, October 2006.

SUPPLEMENTARY MATERIAL

S5: Proportion of infected people that is treated

We found a posterior distribution for the (wtCT) treatment rate τ that implies that 75% (72-77%) of infected people is treated (Table 1 main text). We cannot use the model itself to verify whether this is a realistic finding, because the model does not include explicitly all processes by which people are treated, including asymptomatic screening. To further analyze how credible the posterior distribution of the treatment rate is, we do the following calculations.

Infected people can become susceptible again by natural recovery (at rate γ), by receiving treatment for symptoms (at rate ξ , not considered in the model) or by asymptomatic screening (at rate σ , not considered in the model). Probably, asymptomatic screening rates are higher in infected compared to susceptible people, because infected people tend to have more risky sexual behavior. Screening campaigns may therefore be more targeted towards infected people, and infected people are more likely to be screening through notified, infected partners. We define η as the ratio of screening rates in infected compared to that in susceptible people. Then, the fraction of the population that is screened per year is:

$$f_{screened} = (1 - prev) * (1 - e^{-\sigma/\eta}) + prev * (1 - e^{-\sigma}).$$

We solve this equation for σ . We have data on the fraction of the population that is screened per year (0.25)⁹ and the (model-computed) prevalence in the population aged 15-29 that is considered in the model (0.01). However, η is not well known, so we make assumptions about η instead (we consider a range of values between 1 and 10).

Further, suppose that there was no screening. Then only symptomatically infected people would be treated:

$$f_{symp} = \frac{\xi}{\xi + \gamma}.$$

We can also solve for ξ , using $\gamma=0.73$ ⁴ and considering a range of values between 0 and 1 for f_{symp} . Then we compute the proportion of infections that is treated as:

$$f_{treat} = \frac{\sigma + \xi}{\sigma + \xi + \gamma}.$$

SUPPLEMENTARY MATERIAL

We then verify which values for η and f_{symp} values are consistent with f_{treat} between 0.72 and 0.77 (red area in Figure S3). These computations show that if η is around 5, and f_{symp} between 30-60%, the model-computed value for f_{treat} is not unlikely. We deem such values for η and f_{symp} in a credible range.^{10,11}

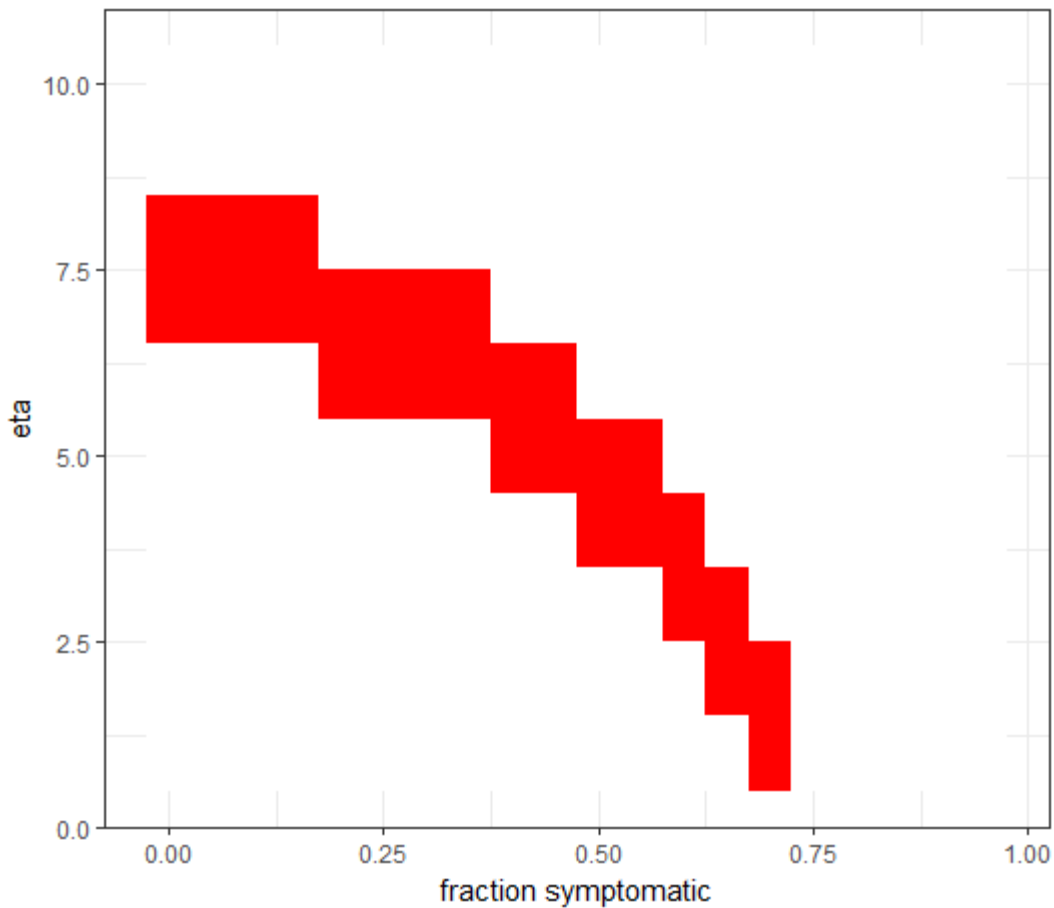


Figure S3 Red area: values for η (ratio of screening rates in infected compared to susceptible people) and f_{symp} (proportion symptomatic) when the prevalence is 0.01 and the proportion of infected people that is treated is between 0.72 and 0.77.

SUPPLEMENTARY MATERIAL

References

1. Riesen M, Garcia V, Low N, Althaus CL. Modeling the consequences of regional heterogeneity in human papillomavirus (HPV) vaccination uptake on transmission in Switzerland. *Vaccine* 2017;**35**(52):7312-7321.
2. British National Surveys of Sexual Attitudes and Lifestyles. Natsal. <http://www.natsal.ac.uk>.
3. Althaus CL, Heijne JC, Herzog SA, Roellin A, Low N. Individual and population level effects of partner notification for Chlamydia trachomatis. *PLoS One* 2012;**7**(12):e51438.
4. Price MJ, Ades AE, Angelis DD, Welton NJ, Macleod J, Soldan K, Turner K, Simms I, Horner PJ. Mixture-of-exponentials models to explain heterogeneity in studies of the duration of Chlamydia trachomatis infection. *Stat Med* 2013;**32**(9):1547-60.
5. Bolker B. *Ecological Models and Data in R, Ch. 4.5.1.3*. Princeton/Oxford: Princeton University Press, 2008.
6. Brooks SP, Gelman A. General methods for monitoring convergence of iterative simulations. *Journal of Computational and Graphical Statistics* 1998;**7**(4):434-455.
7. Diekmann O, Heesterbeek JAP, Metz JAJ. On the Definition and the Computation of the Basic Reproduction Ratio R_0 in Models for Infectious-Diseases in Heterogeneous Populations. *Journal of Mathematical Biology* 1990;**28**(4):365-382.
8. Diekmann O, Heesterbeek JAP, Roberts MG. The construction of next-generation matrices for compartmental epidemic models. *Journal of the Royal Society Interface* 2010;**7**(47):873-885.
9. Löfdahl M, Rydevik G, Blaxhult A, Herrmann B. Chlamydia infection among Swedish women. Contact tracing and reporting routines must be improved. *Lakartidningen* 2008;**105**(44):3116-20.
10. Davies B, Anderson SJ, Turner KM, Ward H. How robust are the natural history parameters used in chlamydia transmission dynamic models? A systematic review. *Theor Biol Med Model* 2014;**11**:8.
11. Smid JH, Althaus CL, Low N. Immunity and increased testing of uninfected people may have limited the impact of chlamydia screening in England. submitted.