

1 **Title : Is adaptation limited by mutation? A timescale dependent effect of genetic**  
2 **diversity on the adaptive substitution rate in animals.**

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## 8 ABSTRACT

9 Whether adaptation is limited by the supply of beneficial mutations is a long-standing question of  
10 evolutionary genetics, which more generally relates to the determination of the adaptive substitution  
11 rate and its relationship with the effective population size  $N_e$ . The empirical evidence so far is  
12 equivocal, with some but not all studies supporting a higher adaptive substitution rate in large- $N_e$   
13 than in small- $N_e$  species.

14 We gathered coding sequence polymorphism data and estimated the adaptive amino-acid  
15 substitution rate  $\omega_a$ , in 50 species from ten distant groups of animals with markedly different  
16 population mutation rate  $\theta$ . We reveal the existence of a complex, timescale dependent relationship  
17 between species adaptive substitution rate and genetic diversity. On the one hand, we report a  
18 positive relationship between  $\omega_a$  and  $\theta$  among closely related species, indicating that adaptation is  
19 indeed limited by the supply of beneficial mutations, but this was only true in relatively low- $\theta$  taxa.  
20 On the other hand, we uncovered a weak negative correlation between  $\omega_a$  and  $\theta$  at a larger  
21 taxonomic scale. This result is consistent with predictions of Fisher's geometrical model and  
22 suggests that the proportion of mutations that are beneficial scales negatively with species long-  
23 term  $N_e$ .

24 **Key words:** adaptive substitution rate, beneficial mutations, effective population size, Mc-Donald  
25 and Kreitman, animals.

## 26 INTRODUCTION

27 It is widely accepted that adaptation is more efficient in large populations. Firstly, because they  
28 produce a greater number of mutants per generation, large populations are more likely than small  
29 ones to newly find the required alleles, if missing from the gene pool. Secondly, because they tend  
30 to be genetically more diverse, large populations are more likely to carry the alleles needed to  
31 respond to environmental changes (1). Lastly, the fixation probability of beneficial mutations is  
32 higher in large than in small populations due to a weaker effect of genetic drift in the former. So, be  
33 it from standing variation or from *de novo* mutations, one would intuitively expect to observe a  
34 higher rate of accumulation of adaptive changes, on average, in large than in small populations (2).

35 Under a simple population genetic model, in a population of effective size  $N_e$ , mutations of  
36 selection coefficient  $s \gg 1/N_e$  should accumulate at rate  $\sim 4N_e\mu_a s$ , where  $\mu_a$  is the adaptive mutation  
37 rate – i.e., the adaptive substitution rate should scale linearly with  $N_e\mu$  (where  $\mu$  is the total mutation  
38 rate) (3).

39 This rationale implicitly assumes that the rate of adaptation is limited by the supply of new  
40 mutations, i.e., the population mutation rate  $\theta=4N_e\mu$  (4). It might be, however, that the amount of  
41 genetic diversity available in all or most existing populations is sufficient for adaptation, and/or that  
42 the ability to adapt to environmental changes is determined in the first place by factors independent  
43 from the effective population size, such as the magnitude or frequency of perturbations, the finite  
44 set of possible genotypes an organism can reach, or the ability of populations to combine favorable  
45 alleles across loci via recombination (5–10). Finally, it has been suggested that the rate of adaptive  
46 mutation,  $\mu_a$ , might be negatively correlated with  $N_e$ , which further complicates the situation. This is  
47 because small populations tend to accumulate deleterious mutations, and the resulting load could  
48 offer the opportunity for adaptive, compensatory mutations to appear and spread irrespective of  
49 environmental perturbations (9). Theoretical models, therefore, can predict either a positive, a  
50 negative, or a lack of relationship between population size and adaptive rate, depending on the  
51 underlying assumptions.

52 Molecular data offer an unique opportunity to empirically evaluate the correlation between the rate  
53 of adaptation and  $\theta$ , and thus to test whether adaptation is indeed limited by mutation. More  
54 efficient adaptation in large populations should manifest itself by an increased rate of protein  
55 evolution, which can be estimated from coding sequence alignments. The ratio of non-synonymous  
56 (i.e. amino-acid changing, dN) to synonymous (i.e. amino-acid conservative, dS) substitution rates,  
57 often called  $\omega$ , is a measure of the protein evolutionary rate that controls for the effects of  
58 divergence time and mutation rate.  $\omega$ , however, is not only influenced by adaptation, but also by the  
59 strength and efficiency of purifying selection against deleterious alleles. To account for this,  
60 McDonald and Kreitman (1991, MK) (10) suggested including within-species polymorphism in the  
61 analysis. Because adaptive mutations are rare and not particularly long-lived, they are expected to  
62 contribute negligibly to the pool of segregating alleles. The ratio of non-synonymous to  
63 synonymous polymorphism, therefore, provides an estimate of the expected  $\omega$  under near-neutrality,  
64 i.e., in absence of adaptation, called  $\omega_{na}$  (for non-adaptive). Subtracting the nearly-neutral

65 expectation  $\omega_{na}$  from the observed  $\omega$  provides an estimate of the adaptive rate,  $\omega_a$ , and the  
66 proportion of adaptive substitution rate,  $\alpha$  (11).

67 Subsequent improvements of the MK method were intended to account for a number of factors  
68 potentially confounding the estimation of  $\omega_{na}$ , including the prevalence of slightly deleterious  
69 segregating alleles and recent demographic effects (14–21). Improved methods explicitly model the  
70 distribution of fitness effect (DFE) of non-synonymous mutations, and take information not only  
71 from the number of synonymous and non-synonymous single nucleotide polymorphisms (SNPs),  
72 but also from the distribution of allele frequencies across SNPs – the so-called site frequency  
73 spectra (SFS). The  $\omega_a$  statistics has a high sampling variance (22) and its estimation can be biased  
74 by various factors, such as fluctuating population size (12,23,24) and GC-biased gene conversion  
75 (25–27). In particular, one key assumption of the MK approach is that the long-term  $N_e$ , which  
76 determines  $\omega$ , is equal to the short-term  $N_e$  and can therefore be estimated from polymorphism data.  
77 This appears unlikely to be generally true, and ancient fluctuations in  $N_e$  could in principle fault the  
78 MK rationale (12,23,24). Eyre-Walker (24) theoretically considered the problem of a single ancient  
79 change in  $N_e$  and showed that an expansion in population size, even if old, could lead to  
80 overestimation of the adaptive substitution rate, a bias that could create spurious positive correlation  
81 between  $\omega_a$  and  $N_e$  and that we need to keep in mind when interpreting this type of estimates.

82 The first applications of the MK method to large-scale data sets indicated that the adaptive rate is  
83 higher in *Drosophila* than in humans (11,13,14), consistent with the prediction of more efficient  
84 adaptation in large populations and with the hypothesis that mutation limits adaptation. These  
85 studies, however, were focusing on the  $\alpha = \omega_a / (\omega_a + \omega_{na})$  statistics, i.e., the proportion of amino-acid  
86 substitutions that result from adaptation.  $\alpha$ , however, is influenced by  $\omega_{na}$  as well as  $\omega_a$ , and a lower  
87  $\alpha$  in humans than in *Drosophila* might mainly reflect a higher rate of non-adaptive amino-acid  
88 substitution in the former. Indeed, purifying selection against deleterious mutations is expected to  
89 be less effective in small populations due to increased genetic drift (28). Comparative studies  
90 focusing on  $\omega_a$  have only revealed tenuous positive effects of  $\theta$  on the adaptive rate in mammals,  
91 flies and plants (29–31). The largest analysis of this sort used 44 pairs of non-model species of  
92 animals occupying a wide range of  $\theta$  (18). This study reported a significantly positive relationship  
93 between  $\theta$ -related life history traits and  $\alpha$ , consistent with previous literature, but this was entirely  
94 due to the non-adaptive component. Galtier (18) failed to detect any effect of  $\theta$  on  $\omega_a$ , despite using  
95 various models for the distribution of fitness effects and accounting for a number of potential

96 confounding factors - a result that does not support the hypothesis that adaptation is limited by  
97 mutation. Of note, the species sampled in this study belong to divergent families and phyla of  
98 animals. They differ much in terms of ecology and genome architecture, which might confound the  
99 relationship between  $\omega_a$  and  $\theta$  (18).

100 So, the evidence so far regarding the relationship between adaptive rate and population mutation  
101 rate is equivocal. Existing comparative studies have adopted distinctive methodological approaches,  
102 both in terms of species sampling and estimates of the adaptive rate. In particular, these studies have  
103 been conducted at different evolutionary scales, which might contribute to explain their somewhat  
104 discordant results. In the short term, an increase in  $N_e$  is expected to boost the adaptive substitution  
105 rate if the supply of new mutations is limiting. In the long run, differences in  $N_e$  could also lead to  
106 changes in the DFE, and particularly the proportion of beneficial mutations, due to small- $N_e$  species  
107 being pulled away from their fitness optimum via genetic drift (11,18,32). How these two opposing  
108 forces interact and combine to determine the relationship between  $\omega_a$  and  $\theta$  is still unknown, in  
109 absence of a multi-scale study.

110 In this study, we propose to test the effect of evolutionary scale on the relationship between the  
111 adaptive substitution rate ( $\omega_a$ ) and the population mutation rate ( $\theta$ ). For this, we gathered coding  
112 sequence polymorphism data in 4 to 6 species from each of ten distant groups of animals with  
113 markedly different  $\theta$ . Our results reveal that the relationship between  $\omega_a$  and  $\theta$  varies depending on  
114 the considered taxonomic scale, i.e. depending on whether we compare closely related species or  
115 distantly related taxa. We report a positive relationship between  $\omega_a$  and  $\theta$  within groups, the strength  
116 of which weakens as  $\theta$  increases, indicating that adaptation is limited by beneficial mutations in  
117 small- $\theta$  species of animals. At a larger taxonomic scale, in contrast, we report a weak negative  
118 correlation between  $\omega_a$  and  $\theta$ , with primates and ants showing a higher adaptive substitution rate  
119 than mussels and fruit flies, for instance. This is consistent with the hypothesis that long-term  $N_e$   
120 influences the DFE, and particularly the proportion of adaptive mutations.

## 121 RESULTS

### 122 1. Data sets

123 We assembled a data set of coding sequence polymorphism in 50 species from ten taxonomic  
124 groups, each group including 4 to 6 closely-related species (**Table S1**). The ten taxa we analyzed are  
125 Catharrhini (Mammalia, hereafter called “primates”), Passeriformes (Aves, hereafter called  
126 “passerines”), Galloanserae (Aves, hereafter called “fowls”), Muroidea (Mammalia, hereafter called  
127 “rodents”), Lumbricidae (Annelida, hereafter called “earth worms”), *Lineus* (Nemertea, hereafter  
128 called “ribbon worms”), *Mytilus* (Mollusca, hereafter called “mussels”), Satyrini (Lepidoptera,  
129 hereafter called “butterflies”), *Formica* (Hymenoptera, hereafter called “ants”), and *Drosophila*  
130 (hereafter called “flies”).

131 Data for five groups (primates, passerines, fowls, rodents and flies) were obtained from public  
132 databases. Data for the other five groups were newly generated via exon capture in a total of 242  
133 individuals from 22 species (**Table 1**) and we obtained sufficient data for 216 of them (~89%). The  
134 average coverage was of 9X in ants, 23X in butterflies, 10X in earth worms, 28X in ribbon worms  
135 and 26X in mussels (average of median coverage per species). The percentage of targeted coding  
136 sequences for which at least one contig was recovered varied from 31.9% to 88.2% across species  
137 (median=78.8%, **Table 1**).

Species	Group	Targeted transcripts	Recovered transcripts	Percentage of recovered among targeted transcripts
<i>Formica fusca</i>	ants	1810	1427	78.8
<i>Formica sanguinea</i>	ants	1810	1396	77.1
<i>Formica pratensis</i>	ants	1810	1398	77.2
<i>Formica cunicularia</i>	ants	1810	1406	77.7
<i>Maniola jurtina</i>	butterflies	2235	1921	86.0
<i>Melanargia galathea</i>	butterflies	2235	1713	76.6
<i>Pyronia tithonus</i>	butterflies	2235	1823	81.6
<i>Pyronia bathseba</i>	butterflies	2235	1864	83.4
<i>Aphantopus hyperanthus</i>	butterflies	2235	1772	79.3
<i>Allolobophora chlorotica</i> L1	earth worms	2955	2293	77.6
<i>Allolobophora chlorotica</i> L2	earth worms	2955	2315	78.3
<i>Allolobophora chlorotica</i> L4	earth worms	2955	1732	58.6
<i>Aporrectodea icterica</i>	earth worms	2955	2321	78.5
<i>Lumbricus terrestris</i>	earth worms	2955	943	31.9
<i>Lineus sanguineus</i>	ribbon worms	1725	1251	72.5
<i>Lineus ruber</i>	ribbon worms	1725	1521	88.2
<i>Lineus lacteus</i>	ribbon worms	1725	1516	87.9
<i>Lineus longissimus</i>	ribbon worms	1725	1505	87.2
<i>Mytilus galloprovincialis</i>	mussels	2181	1820	83.4
<i>Mytilus edulis</i>	mussels	2181	1721	78.9
<i>Mytilus trossulus</i>	mussels	2181	1740	79.8
<i>Mytilus californianus</i>	mussels	2181	1808	82.9

138 **Table 1: Summary of the number of targeted transcripts recovered in the capture experiment.**

139 We assessed contamination between samples from distinct species using the software CroCo (33).  
140 Overall, inter-groups connections in **Figure S1** indicates a low level of cross-contamination: when  
141 there are connections between taxonomic groups, they concern on average 38 contigs identified as  
142 contaminants, the worst case being the 172 contigs identified as contaminants between the assembly  
143 of *Lineus sanguineus* and *Mytilus galloprovincialis*. The connections between assemblies from  
144 closely related species are very likely to be false positive cases, especially since the intensity of the  
145 within-group connections is congruent with the phylogenetic distance between species within taxa.

144 Regardless, all the contigs identified as potential contaminants were excluded from the dataset in  
145 downstream analyzes by safety.

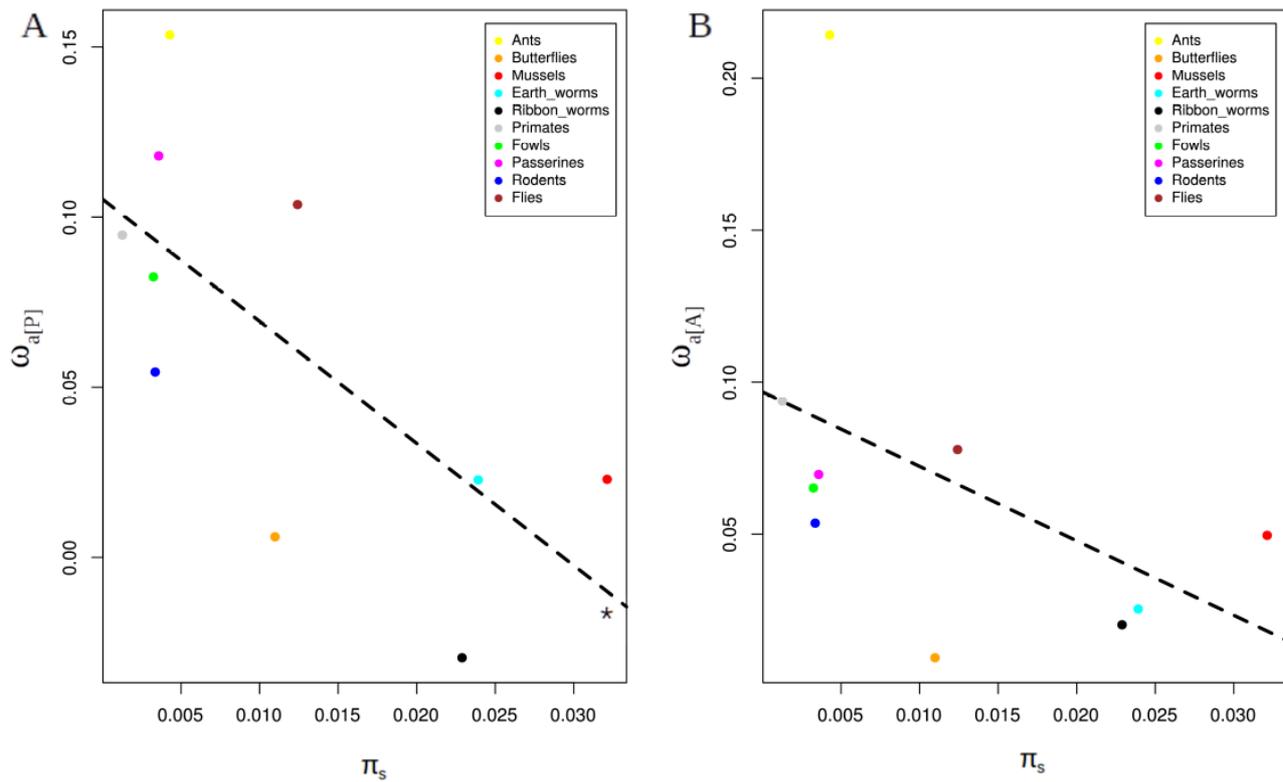
146 Within each group, we focused on orthologous contigs (**Table S2**), predicted open reading frames,  
147 and called the diploid genotypes of individuals at every coding position. SNPs counts obtained  
148 after genotyping are summed up in **Table S3**. Only in two species did we obtain less than a  
149 thousand SNPs, the minimum being 153 for *Lineus longissimus*, for which we could recover data  
150 for only six individuals.

151 We recovered an average of 8,459 SNPs per species in ants, 7,950 in butterflies, 4,763 in earth  
152 worms, 8,347 in ribbon worms, 19,750 in mussels, 10,191 in primates, 25,534 in rodents, 40,870 in  
153 passerines, 8,488 in fowls and 195,398 in flies.

154 In conclusion, the capture experiment seems to be suitable to recover population coding sequences  
155 data for several closely related species - here, the maximum divergence between species within a  
156 taxonomic group was 0.2 subst./site, i.e. the divergence between *Lumbricus terrestris* and  
157 *Allolobophora chlorotica* L1.

## 158 **2. Between-groups relationship between the population mutation rate ( $\theta$ ) and the adaptive** 159 **substitution rate ( $\omega_a$ )**

160 Two strategies were adopted to combine SFS information from distinct species in a group-level  
161 estimate of  $\omega_a$ , thus accounting for the problem of phylogenetic non-independence between species.  
162 For both strategies, we first calculated the dN/dS ratio  $\omega$  at the group-level, i.e., averaging across all  
163 branches of the tree (see Material and Methods). The first one, which we call  $\omega_{a[P]}$ , was obtained by  
164 pooling the SFS from distinct species within a group, separately for synonymous and non-  
165 synonymous SNPs (as in (34)), before fitting the model and estimating the parameters. We then  
166 computed the relationship between  $\omega_{a[P]}$  estimates and the across-species average nucleotide  
167 diversity,  $\pi_s$ , taken as an estimate of  $\theta$ . We detected a significant negative relationship between  $\omega_{a[P]}$   
168 and the across-species average nucleotide diversity,  $\pi_s$ , taken as an estimate of  $\theta$  (regression test,  
169  $r^2=0.4$ , p-value=0.029) (**Figure 1A**).



170 **Figure 1: Relationship between group-level  $\omega_a$  and group-level  $\pi_s$ .**

171 A:  $\omega_a$  is estimated by pooling SFS across species within a group ( $\omega_{a[P]}$ ).

172 B:  $\omega_a$  is estimated via the averaging of  $\omega_{na}$  across species within a group ( $\omega_{a[A]}$ ).

173 Group level  $\pi_s$  is estimated by averaging species-level  $\pi_s$  across closely related species. The dotted lines represent the  
174 regression across taxonomic groups and \* symbols indicate when it is significant.

175 Recent studies focusing on birds and more recently on primates indicate that GC-biased gene  
176 conversion (gBGC) may lead to an overestimation (25,26) or an underestimation of  $\omega_a$  (27).  
177 Interestingly, gBGC does not affect genomic evolution with the same intensity in all organisms  
178 (35). To avoid biases in the estimation in species where gBGC is active, we restricted the SNPs and  
179 substitution data to GC-conservative changes, which are not influenced by gBGC. Here again, the  
180 correlations, even if not significant, were in line with a negative relationship between  $\omega_{a[P]GC\text{-conservative}}$   
181 and proxies of the long-term  $N_e$  (**Figure S2**).

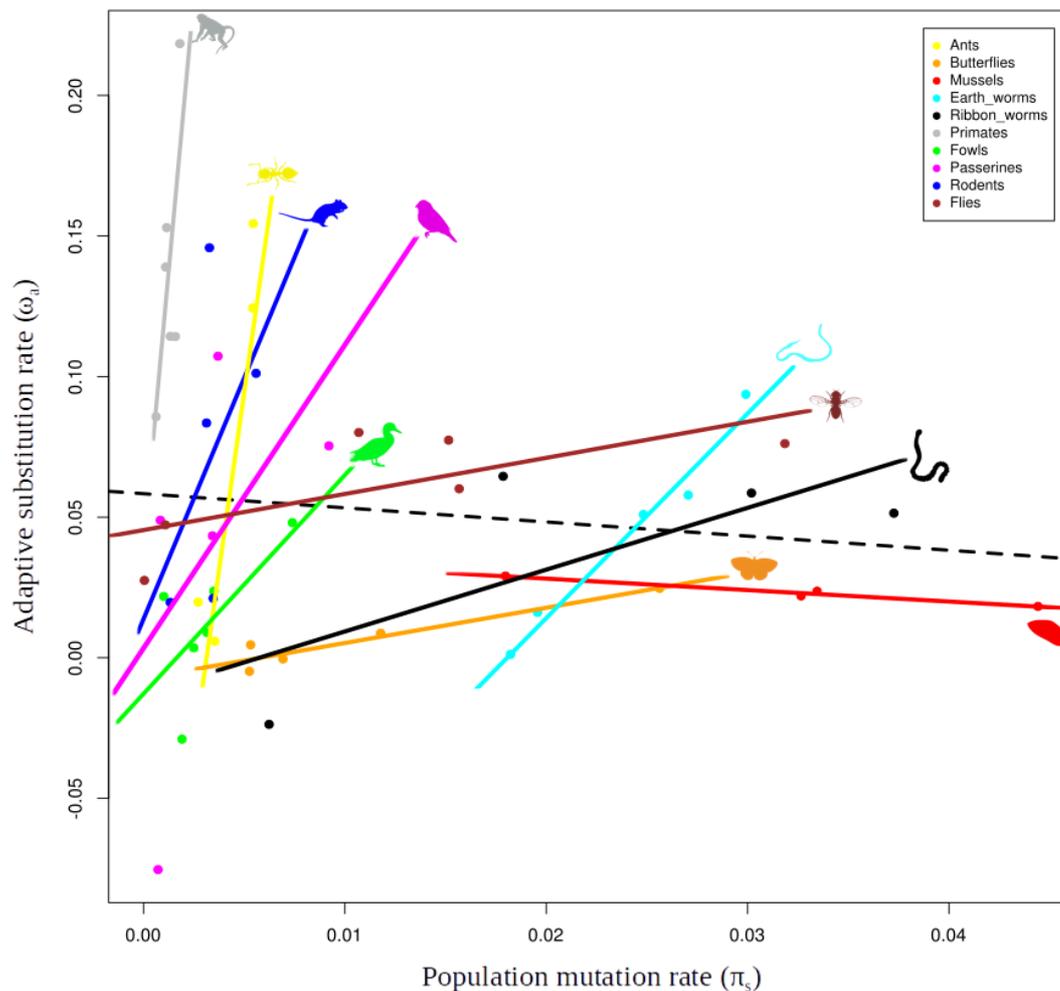
182 Our second estimate of the adaptive rate at group-level, which we called  $\omega_{a[A]}$ , was obtained by  
183 calculating the across-species arithmetic mean of  $\omega_{na}$  within a group, then subtracting this average  
184 from  $\omega$ . It can be shown that  $\omega_{a[A]}$  is an unbiased estimate of the adaptive rate with fluctuating

185 population size if the pace of fluctuations is sufficiently slow (Supplementary Material **Box S1**). We  
186 found a non significant negative correlation between  $\omega_{a[A]}$  and  $\omega_{a[A]GC-conservative}$  and  $\pi_s$  (**Figure 1B and**  
187 **Figure S3**). Overall, the between-group analysis confirmed the absence of a positive relationship  
188 between  $\omega_a$  and  $\theta$  at the between-phyla scale in animals, and even suggested the existence of a  
189 weak, negative relationship.

### 190 **3. Within-group relationship between $\theta$ and $\omega_a$**

191 To assess the within-group effect of  $\pi_s$  on  $\omega_a$ , we performed an analysis of covariance (ANCOVA)  
192 with taxonomic group as a categorical independent variable, as in (29). The principle of this  
193 analysis is to fit a set of parallel lines (one for each taxonomic group) and test whether their  
194 common slope is significantly different from zero. Additionally, we tested if the relationship  
195 between  $\omega_a$  and  $\pi_s$  or life history traits differs between taxonomic groups by testing whether the  
196 lines have different intercepts.

197 Using this strategy, we found that  $\omega_a$  and both  $\pi_s$  and  $\log_{10}(\pi_s)$  are significantly positively correlated  
198 when using only GC-conservative mutations (ANCOVA p-value=0.028 and 0.0031, respectively)  
199 (**Figure 2**).  $\omega_a$  is only marginally positively correlated to  $\log_{10}(\pi_s)$  when using all mutations  
200 (ANCOVA p-value=0.076). We also found that there is a significant variation between the intercepts  
201 (ANCOVA p-value<0.001), as well as a significant interaction between the dependent variable and  
202 categorical independent variable (ANOVA p-value=0.016). Those results support the existence of a  
203 positive relationship between  $\omega_a$  and  $\theta$  within groups, with the slope of the relationship differing  
204 between groups. This is consistent with the hypothesis that within a group, higher- $\theta$  species are  
205 more likely to find and fix adaptive substitutions than low- $\theta$  species, in line with the hypothesis that  
206 mutation limits adaptation. **Figure 2** shows that the slopes of the within-group  $\omega_a/\theta$  correlations  
207 decrease with group-level  $\pi_s$ , and we actually find a significant negative correlation between these  
208 two quantities (Spearman correlation coefficient=-0.77 p-value=0.014). This interestingly suggests  
209 that the limitation of adaptation by the income of adaptive mutations is effective and strong in  
210 small- $\theta$  groups (e.g. primates, rodents, ants), but not in high- groups of animals (e.g. flies, mussels,  
211 butterflies), where the  $\omega_a/\theta$  relationship is essentially flat. (**Figure 2**).



212 **Figure 2: Relationship between species-level  $\omega_a$  and  $\pi_s$ .**

213  $\omega_a$  is estimated using only GC-conservative mutations. The dotted line represents the regression across all species, and  
214 full lines represent the regression within each taxonomic groups.

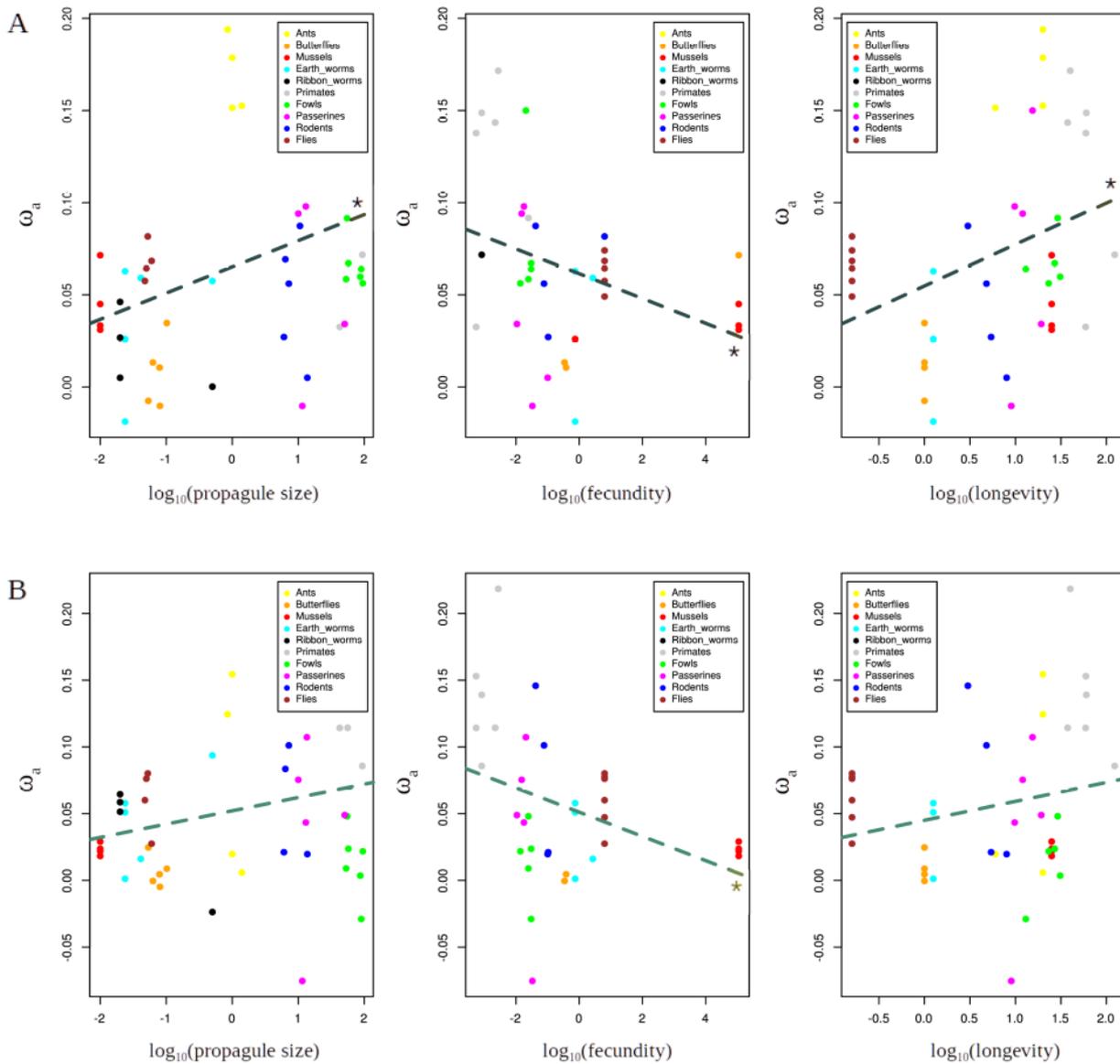
215 When analyzing the per-species non-adaptive substitution rate in the same manner, we found a  
216 global negative relationship between  $\omega_{na}$  (using both all mutations and only GC-conservative  
217 mutations) and  $\pi_s$  (regression test  $r^2=0.33$ ,  $p$ -value= $7.7e-6$ ), and also a significantly negative  
218 relationship within groups (ANCOVA  $p$ -value=0.0018) (**Figure S4**). This is consistent with the  
219 expectations of the nearly neutral theory of evolution (28), and with previous empirical results  
220 (18,36). The estimated ratio of adaptive to total non-synonymous substitutions,  $\alpha$ , behaved more or  
221 less similarly to  $\omega_a$  (**Figure S5**).

#### 222 4. Control for fluctuations in $N_e$

223 We were concerned that the correlation between  $\omega_a$  and  $\pi_s$  might have arisen as an artifact generated  
224 by past fluctuations in population size (23,24). To test this, we simulated coding sequence evolution  
225 under several demographic scenarios with four regimes demographic fluctuations, with a three or  
226 thirty-fold ratio between the low and high  $N_e$ , and a high or low long-term  $N_e$  (see Material and  
227 Method and **Figure S6**). We found that the only scenario where demographic fluctuations could  
228 lead to a detectable positive correlation between  $\omega_a$  and  $\pi_s$  is the one with the highest long-term  $N_e$   
229 and highest difference between the low and high  $N_e$  (see **Figure S7 panel B**, regression test  $r^2=0.07$ ,  
230  $p$ -value=0.0095). The correlation disappeared when we used a ten-fold smaller long-term  $N_e$ ,  
231 whereas we empirically observed that the correlation between  $\omega_a$  and  $\pi_s$  is stronger for small long-  
232 term  $N_e$  groups (**Figure 2**). These simulations therefore suggest that ancient demographic  
233 fluctuations cannot explain our finding of a positive within-group correlation between  $\omega_a$  and  $\pi_s$  in  
234 low- $\theta$  groups.

#### 235 5. Relationship with life history traits

236 We used several life history traits known to be correlated with species long-term effective  
237 population size (37). In our data set, all life history traits are indeed correlated with  $\pi_s$  (Spearman  
238 correlation  $p$ -value, propagule size: 1.1e-12, adult size: 0.00043, longevity: 0.055, body mass:  
239 0.0047, fecundity: 9.4e-6). When estimating per-group  $\omega_a$ , we did not find any significant  
240 relationship with life history traits, but the sign of correlation coefficients were indicative of a  
241 negative relationship between the long-term  $N_e$  and both  $\omega_a$  and  $\omega_{a[GC-conservative]}$  (**Figure S2 and S3**).  
242 When considering all mutations and all 50 species, we found a negative relationship between  $\omega_a$  and  
243  $\log_{10}$  transformed fecundity (regression test,  $r^2=0.094$ ,  $p$ -value=0.038), as well as a positive  
244 relationship with  $\log_{10}$  transformed longevity (regression test,  $r^2=0.10$ ,  $p$ -value=0.022),  $\log_{10}$   
245 transformed propagule size (regression test,  $r^2=0.13$ ,  $p$ -value=0.0073) (**Figure 3**). When using only  
246 GC-conservative mutations, the relationships were similar, while only significant with fecundity  
247 (regression test,  $r^2=0.11$ ,  $p$ -value=0.0026) (**Figure 3**). When controlling for phylogenetic inertia,  
248 those relationships lost significance.



249 **Figure 3: Relationship between species-level  $\omega_a$  and life history traits.**

250 A:  $\omega_a$  is estimated using all mutations.

251 B:  $\omega_a$  is estimated using only GC-conservative mutations.

252 The dotted lines represent the regression across all species and \* symbols indicate when the regression is significant.

253 We also found a significant positive relationship between  $\omega_{na}$  and fecundity (regression test  $r^2=0.31$ ,  
 254  $p$ -value=0.00028), and a significant negative relationship between  $\omega_{na}$  and propagule size  
 255 (regression test  $r^2=0.13$ ,  $p$ -value=0.0072) and body mass (regression test  $r^2=0.10$ ,  $p$ -value=0.024),  
 256 which was also true when using only GC-conservative mutations: significant negative relationships  
 257 between  $\omega_{na[GC-conservative]}$  and propagule size (regression test  $r^2=0.21$ ,  $p$ -value=0.0006802), longevity

258 (regression test  $r^2=0.12$ ,  $p$ -value=0.016), body mass (regression test  $r^2=0.08$ ,  $p$ -value=0.045) and a  
259 significant positive relationship with fecundity (regression test  $r^2=0.36$ ,  $p$ -value=6.236e-05) (**Figure**  
260 **S4**).

## 261 **DISCUSSION**

### 262 **1. Influence of $\theta$ on $\omega_a$ : a two-scale mechanism**

263 In this study, we analyzed a novel, 50-species population genomic data set to evaluate the  
264 relationship between the adaptive substitution rate and the population mutation rate and test the  
265 hypothesis that mutation limits adaptation in natural populations of animals. Using an exon capture  
266 strategy, we were able to generate large-scale synonymous and non-synonymous SFS data in 22  
267 non-model species from five groups of non-vertebrates, which were added to five existing datasets  
268 in mammals, birds and flies. In all ten groups we started from raw data and *de novo* performed  
269 genome/transcriptome assembly, read mapping, SNP/genotype calling, and population genetic  
270 analyses.

271 We found that the relationship between  $\omega_a$  and  $\theta$  depends on the considered timescale. On the one  
272 hand, at a recent evolutionary scale (i.e., neutral divergence  $<0.2$  subst./site), we found a significant  
273 positive correlation between  $\omega_a$  and  $\pi_s$  (**Figure 2**). Interestingly, the slope of the relationship differed  
274 significantly among taxonomic groups, and this slope itself was negatively correlated with the  
275 group average  $\pi_s$ . On the other hand, estimations of the adaptive substitution rate at group level  
276 revealed a weak but consistently negative relationship between  $\omega_a$  and  $\pi_s$  - and life history traits  
277 correlated with the long-term  $N_e$  (**Figure 1 and 3**). This time scale-dependent behavior of the  $\omega_a/\theta$   
278 relationship is here demonstrated via the analysis of a single, multi-scale dataset, somehow  
279 reconciling earlier taxon-specific studies on the subject (4,8,18,29–31,38).

### 280 **2. Relationship between $\theta$ and $\omega_a$ : a real causative link or an artifact ?**

281 Using an ANCOVA analysis, we found that the slopes of the relationship between  $\omega_a$  and  $\pi_s$  within  
282 each taxonomic group were significantly different from zero, demonstrating the existence of a  
283 positive link between  $\omega_a$  and  $\pi_s$  within groups (**Figure 2**). We were concerned that this relationship  
284 may result from a bias of the MK approach, instead of a true biological signal. Indeed, the MK

284 approach implicitly assumes that the regime of selection/drift has been constant over the considered  
285 time period, i.e. since the divergence between the focal and outgroup species. However, if the  
286 selection/drift regime had changed (via a change in effective population size, for instance) between  
287 the period during which divergence was built and the period during which polymorphism was built,  
288 this could lead to overestimation or underestimation of  $\omega_a$  (23,24). Here, we used the so-called  $r_i$ 's  
289 nuisance parameters (39) to control for recent changes in  $N_e$ .

290 In contrast, ancient  $N_e$  changes that affect coding sequence divergence are virtually impossible to  
291 trace – an ancient bottleneck, for instance, is expected to result in an increased dN/dS ratio due to  
292 the accumulation of deleterious substitutions, similarly to an episode of positive selection. We  
293 showed in a previous study based on simulations that ancient demographic fluctuations can lead to  
294 severely overestimated  $\alpha$  and  $\omega_a$ , an upward bias which is exacerbated when the true adaptive  
295 substitution rate is low (23). Additionally, it has been shown by modeling single changes in  $N_e$  that  
296 in presence of slightly deleterious mutations, an increase in  $N_e$  in the past could yield spurious  
297 evidence for positive selection, which can lead to a spurious positive correlation between  $\omega_a$  and  $\pi_s$   
298 (24).

299 We used simulations to test if demographic fluctuations could lead to such a correlation. We  
300 simulated several scenarios of demographic fluctuations with different periods of fluctuations, two  
301 levels of severeness of fluctuations (two different ratios between low and high  $N_e$  phases) and two  
302 levels of long-term  $N_e$ . We found that the only scenario where a positive relationship between  $\omega_a$   
303 and  $\pi_s$  is detected is the one with the highest long-term  $N_e$  and the highest difference between low  
304 and high  $N_e$ . In contrast, our empirical data analysis revealed that the relationship between  $\omega_a$  and  $\pi_s$   
305 weakens when the group average  $\pi_s$  increases, which suggests that long-term fluctuations are not  
306 responsible for the positive link between  $\omega_a$  and  $\pi_s$  we report. Additionally, the gradual decrease of  
307 the slope of the relationship with per-group average  $\pi_s$  is also consistent with the fact that the  
308 relation is genuine, because (i) we do not expect the regime of demographic fluctuation to correlate  
309 with the average  $\pi_s$  of the group, and (ii) there is no relationship between the inter-group variation in  
310  $\pi_s$  and the average  $\pi_s$  of the group (Spearman correlation test: p-value=0.47).

311 A recently developed method allows the estimation of  $\alpha$  and  $\omega_a$  using polymorphism data alone  
312 (20), thus avoiding the assumption of time constancy of the regime of drift and selection. However,  
313 estimates of  $\alpha$  and  $\omega_a$  by this method have a meaning that differs from the usual one, as they  
314 represent the rate of adaptive evolution of the species during its very recent history, and not the one

315 of its long-term history. This method requires high quality datasets and highly polymorphic species,  
316 and was not applicable to our dataset, in which species and groups differ widely in terms of  
317 numbers of SNPs (**Table S3**).

### 318 **3. Mutation limits adaptation within taxonomic groups in small- $\theta$ animals**

319 Our analysis therefore supports the existence of a genuine link between the adaptive substitution  
320 rate and  $\theta$ , which is consistent with the hypothesis that, in several groups of animals, the rate of  
321 adaptation is limited by the supply of beneficial mutations. The slope of the relationship is  
322 particularly steep in ants, fowls, passerines, rodents and primates (**Figure 2**). For instance, the  
323 estimated adaptive rate in rhesus macaque *Macaca mulatta* ( $\pi_s=0.0018$ ) is more than three time  
324 higher than that of our own species, *Homo sapiens* ( $\pi_s=0.0006$ ). Note that this interpretation relies  
325 on the assumption that different species from a given taxonomic group share the same DFE and, in  
326 particular, the same proportion of beneficial mutations. This result is consistent with previous  
327 analyses of the relationship between  $\omega_a$  and  $\pi_s$  at a relatively recent time scale (27,29). It is also  
328 consistent with the finding that strong selective sweeps are more abundant in great apes with large  
329 population size (4).

330 Interestingly, we found that the relationship between  $\omega_a$  and  $\pi_s$  is significantly stronger in low-  
331 diversity than high-diversity groups. In flies, a high-diversity group, the slope of the linear  
332 regression between the two variables was only 1.3, whereas it was between 7.8 and 77 in the four  
333 groups of vertebrates. In mussels, the taxonomic group with the highest average diversity in our  
334 dataset, we detected no significant relationship between  $\omega_a$  and  $\pi_s$ , the slope being very close to zero  
335 (-0.4). It is possible that in such organisms the rate of adaptive evolution is not limited by the supply  
336 of beneficial mutations: the standing variation and/or the rate of apparition of new mutations are  
337 sufficient for proteins to find the required alleles. This is consistent with the results of (8), who  
338 showed that patterns of adaptation to insecticides in natural populations of *Drosophila*  
339 *melanogaster* are incompatible with the hypothesis that adaptation is limited by the income of  
340 adaptive mutations. This is also consistent with the results of Jensen and Bachtrog (40), who found  
341 very similar rates of adaptation between two *Drosophila* species with different  $N_e$ . Finally, this  
342 corroborates theoretical predictions indicating that when  $N_e$  is sufficiently large, it is the species  
343 ability to combine beneficial alleles across loci that limits adaption rather than the strength of

344 selection or mutation supply (9). Our results suggest that this situation applies to large- $N_e$  groups of  
345 animals, such as *Drosophila*, but not to small- $N_e$  ones, such as primates.

#### 346 **4. What are the determinants of $\omega_a$ across distantly related taxa?**

347 We used two approaches to estimate the adaptive substitution rate at group level. Both supported a  
348 negative among-groups relationship between  $\omega_a$  and  $\pi_s$ , and between  $\omega_a$  and life history traits that  
349 have been shown to be linked to long-term effective population size (37) (**Figure 1, S2, S3 and 3**).  
350 As different sets of genes have been used in the different groups of animals, gene content might  
351 influence our results. Indeed, Enard et al. (41) showed that genes interacting with viruses  
352 experience a significantly higher adaptive substitution rate, illustrating the importance of gene  
353 content. In the exon capture experiment, a subset of genes have been randomly sampled from  
354 existing transcriptome reference, whereas in the other species, all available genes (providing that  
355 they were present in all species within a group) were used. We do not see any particular reason why  
356 the gene sample would be biased with respect to virus interacting proteins in some specific groups,  
357 and we did not detect any effect of data type (i.e. exon capture vs. genome-wide) on  $\omega_a$ . Our results  
358 are consistent with the results of Galtier (16), who analyzed the relationship between  $\omega_a$  and  $\pi_s$  in a  
359 transcriptomic dataset of 44 distantly related species of animals. Indeed, the main analysis in Galtier  
360 (18) revealed no significant correlation between  $\omega_a$  and  $\pi_s$ , but various control analyses (using GC  
361 or expression restricted datasets in particular) yielded a significantly negative correlation between  
362 the two variables.

363 This suggests that the mutation limitation hypothesis does not predict well the variation of  $\omega_a$  at a  
364 large taxonomic scale, i.e., that factors other than  $\theta$  must be at work here. Below, we discuss a  
365 number of such potential factors in the light of Fisher's geometrical model (FGM), which provides  
366 a convenient framework under which to think about the determinants of the adaptive substitution  
367 rate.

368 Simulations under FGM and a moving optimum showed that the adaptive substitution rate is  
369 primarily determined by the rate of environmental change (32,42). This relates to our result as we  
370 may speculate that species with a longer generation time may undergo a higher environmental  
371 change per generation, and generation time is (presumably) negatively correlated to population size  
372 in animals (37).

373 Second, Lourenço et al. (32) suggested that organismal complexity, represented by the  
374 dimensionality of the phenotypic space in FGM, affects the adaptive substitution rate more strongly  
375 than does the effective population size, the adaptive substitution rate being an increasing function of  
376 complexity. This is because the probability for a new mutation to be in the optimal direction  
377 decreases as the number of potential directions increases, such that the average adaptive walk takes  
378 more steps in a high-dimension than a low-dimension space (32,43). Complexity *sensus* FGM,  
379 however, is very hard to quantify in a biologically relevant way, and whether primates and birds  
380 would be more complex than mussels and worms appears anything but meaningful at organismal  
381 level. Different measures of complexity have been thought of at molecular or cellular level, such as  
382 genome size, genes or proteins number, number of protein-protein interactions, number of cell  
383 types, and these seem to point towards a higher complexity in mammals than insects, for instance  
384 (37,38). This would be consistent with the idea of a greater complexity of species with smaller  $N_e$ .  
385 Fernández and Lynch (46) suggested that the accumulation of mildly deleterious mutations in  
386 populations of small size induces secondary selection for protein-protein interactions that stabilize  
387 key gene functions, thus introducing a plausible mechanism for the emergence of molecular  
388 complexity (46). If the number of protein-protein interactions is a relevant measure of proteome  
389 complexity, then this might contribute to explain our report of a higher rate of adaptive substitution  
390 in low- $\theta$  than in high- $\theta$  groups.

391

392 Finally, the variation of  $\omega_a$  across distantly related taxa could be modulated by the long-term  $N_e$  via  
393 the mean distance of the population to the fitness optimum. Indeed, under FGM, the proportion of  
394 beneficial mutations increases with the distance to the optimum. Groups of species evolving under  
395 small long-term  $N_a$  are further away from their optimum, compared to larger- $N_e$  groups, due to an  
396 increased rate of fixation of deleterious mutations at equilibrium, so they are predicted to undergo a  
397 larger proportion of beneficial, compensatory mutations. Empirical analyses of SFS based on large  
398 samples in humans and flies are consistent with the hypothesis that humans are on average more  
399 distant to their optimum than flies (11).

400 To sum up, our results suggest that factors linked to species long-term effective population size  
401 affect the DFE, making the proportion and rate of beneficial mutation non-independent from the  
402 long-term  $N_e$ . We suggest that the proteome is probably more complex and further away from its  
403 optimal state in small- $N_e$  than in large- $N_e$  groups of animals, which might contribute to increase the

404 steady-state adaptive rate in the former, masking the effect of mutation limitation in across-groups  
405 comparisons.

## 406 CONCLUSION

407 In this study, we sampled a large variety of animals species and demonstrated the existence of a  
408 timescale-dependent relationship between the adaptive substitution rate and the population mutation  
409 rate, that reconciles previous studies that were conducted at different taxonomic scales. We  
410 demonstrate that the relationship between the adaptive substitution rate and  $\theta$  within closely related  
411 species sharing a similar DFE is shaped by the limiting supply of beneficial mutations, whereas the  
412 between-groups pattern probably reflects the influence of long-term population size on the  
413 proportion of beneficial mutations. Our results provide empirical evidence for mutation-limited  
414 adaptive rate at whole proteome level in small- $N_e$  groups of animals, and emphasize the fact that the  
415 DFE is not independent from the long-term effective population size – a crucial factor that must be  
416 properly accounted for in large-scale comparative population genomic analyses.

## 417 MATERIAL & METHODS

### 418 1. Data set

419 Genomic, exomic and transcriptomic data from primates, passerines, fowls, rodents and flies were  
420 retrieved from the SRA database. Detailed referenced, bioprojects and sample sizes are provided in  
421 **Table S1**. The minimal sample size was five diploid individuals (in *Papio anubis*) and the  
422 maximum was 20 (in seven species).

423 Exon capture data were newly generated in ants, butterflies, mussels, earth worms and ribbon  
424 worms. We gathered tissue samples or DNA samples for at least eight individuals per species and  
425 four or five species per group. Reference transcriptomes were obtained from previously published  
426 RNA-seq data in one species per taxonomic group (37,47,48). Details of the species and numbers of  
427 individuals are presented in **Table S1**.

## 428 2. Multiplexed target capture experiment

429 DNA from whole animal body (ants), body section (earth worms, ribbon worms), mantle (mussels)  
430 or head/thorax (butterflies) was extracted using DNAeasy Blood and Tissue kit (QIAGEN)  
431 following the manufacturer instructions. About 3 µg of total genomic DNA were sheared for 20 mn  
432 using an ultrasonic cleaning unit (Elmasonic One). Illumina libraries were constructed for all  
433 samples following the standard protocol involving blunt-end repair, adapter ligation, and adapter  
434 fill-in steps as developed by (49) and adapted in (50).

435 To perform target capture, we randomly chose contigs in five published reference transcriptomes  
436 (*Maniola jurtina* for butterflies (47), *Lineus longissimus* for ribbon worms (37), *Mytilus*  
437 *galloprovincialis* for mussels (37), *Allobophora chlorotica L1* for earth worms (37), and *Formica*  
438 *cunicularia* for ants (48)) in order to reach 2Mb of total sequence length per taxon (~2000 contigs).  
439 100nt-long baits corresponding to these sequences were synthesized by MYbaits (Ann Arbor, MI,  
440 USA), with an average cover of 3X.

441 We then performed multiplexed target capture following the MYbaits targeted enrichment protocol:  
442 about 5 ng of each library were PCR-dual-indexed using Taq Phusion (Phusion High-Fidelity DNA  
443 Polymerase Thermo Scientific) or KAPA HiFi (2× KAPA HiFi HotStart ReadyMix  
444 KAPABIOSYSTEMS) polymerases. We used primers developed in (51). Indexed libraries were  
445 purified using AMPure (Agencourt) with a ratio of 1.6, quantified with Nanodrop ND-800, and  
446 pooled in equimolar ratio. We had a total of 96 combinations of indexes, and two Illumina lanes, for  
447 a total of 244 individuals. This means that we had to index two (rarely three) individuals with the  
448 same combination to be sequenced in the same line. When this was necessary, we assigned the same  
449 tag to individuals from distantly related species (i.e. from different groups). Exon capture was  
450 achieved according to the Mybaits targeted enrichment protocol, adjusting the hybridization  
451 temperature to the phylogenetic distance between the processed library and the baits. For libraries  
452 corresponding to individuals from the species used to design baits, we used a temperature of 65°C  
453 during 22 h. For the other ones we ran the hybridization reactions for 16 h at 65°C, 2 h at 63°C, 2 h  
454 at 61°C and 2 h at 59°C. Following hybridization, the reactions were cleaned according to the kit  
455 protocol with 200 µL of wash buffers, and hot washes were performed at 65°C or 59°C depending  
456 on the samples. The enriched solutions were then PCR-amplified for 14 to 16 cycles, after removal  
457 of the streptavidin beads. PCR products were purified using AMPure (Agencourt) with a ratio of

458 1.6, and paired-end sequenced on two Illumina HiSeq<sup>®</sup> 2500 lines. Illumina sequencing and  
459 demultiplexing were subcontracted.

### 460 **3. Assembly and genotyping**

461 For RNA-seq data (i.e. fowls and two rodents), we used trimmomatic (52) to remove Illumina  
462 adapters and reads with a quality score below 30. We constructed *de novo* transcriptome assemblies  
463 for each species following strategy B in (53), using Abyss (54) and Cap3 (55). Open reading frames  
464 (ORFs) were predicted using the Trinity package (56). Contigs carrying ORF shorter than 150 bp  
465 were discarded. Filtered RNA-seq reads were mapped to this assembly using Burrow Wheeler  
466 Aligner (BWA) (version 0.7.12-r1039) (57). Contigs with a coverage across all individual below  
467 2.5xn (where n is the number of individuals) were discarded. Diploid genotypes were called  
468 according to the method described in (58) and (59) (model M1) via the software reads2snps  
469 (<https://kimura.univ-montp2.fr/PopPhyl/index.php?section=tools>). This method calculates the  
470 posterior probability of each possible genotype in a maximum likelihood framework. Genotypes  
471 supported by a posterior probability higher than 95% are retained, otherwise missing data is called.  
472 We used version of the method which accounts for between-individual, within-species  
473 contamination as introduced in (48), using the -contam=0.1 option, which means assuming that up  
474 to 10% of the reads assigned to one specific sample may actually come from a distinct sample, and  
475 only validating genotypes robust to this source of uncertainty.

476 For primates, rodents, passerines and flies, reference genomes, assemblies and annotations files  
477 were downloaded from Ensembl (release 89) and NCBI (**Table S1**). We kept only 'CDS' reports in  
478 the annotations files, corresponding to coding exons, which were annotated with the automatic  
479 Ensembl annotation pipeline, and the havana team for *Homo sapiens*. We used trimmomatic to  
480 remove Illumina adapters, to trim low-quality reads (i.e. with an average base quality below 20),  
481 and to keep only reads longer than 50bp. Reads were mapped using BWA (57) on the complete  
482 reference assembly. We filtered out hits with mapping quality below 20 and removed duplicates,  
483 and we extracted mapping hits corresponding to regions containing coding sequences according to  
484 the annotated reference assembly. This was done to avoid calling SNPs on the whole genome,  
485 which would be both time consuming and useless in the present context. We called SNPs using a  
486 pipeline based on GATK (v3.8-0-ge9d80683). Roughly, this pipeline comprised two rounds of  
487 variant calling separated by a base quality score recalibration. Variant calling was first run on every

488 individuals from every species using HaplotypeCaller (`--emitRefConfidence GVCF`  
489 `--genotyping_mode DISCOVERY -hets 0.001`). The variant callings from all individuals of a given  
490 species were then used to produce a joint genotype using GenotypeGVCFs. Indels in the resulting  
491 vcf files were then filtered out using vcfutils. The distributions of various parameters associated  
492 with SNPs were then used to set several hard thresholds (i.e. Quality by Depth < 3.0; Fisher Strand  
493 > 10; Strand Odds Ratio > 3.0; MQRootMeanSquare < 50; MQRankSum < -0.5; ReadPosRankSum  
494 < -2.0) in order to detect putative SNP-calling errors using VariantFiltration. This erroneous SNPs  
495 were then used for base quality score recalibration of the previously created mapping files using  
496 BaseRecalibrator. These mappings with re-calibrated quality scores were then used to re-call  
497 variants (HaplotypeCaller), to re-produce a joint genotype (GenotypeGVCFs, `--allsites`) and to re-  
498 set empirical hard thresholds (i.e. same values as above, except for Quality by Depth < 5.0). The  
499 obtained vcf files were converted to fasta files (i.e. producing two unphased allelic sequences per  
500 individual) using custom python scripts while discarding exons found on both mitochondrial and  
501 sexual chromosomes and while filtering out additional SNPs: we removed SNPs with a too high  
502 coverage (thresholds were empirically set for each species), with a too low coverage (i.e. 10x per  
503 individual) and with a too low genotype quality per individual (i.e. less than 30).  
504 For reads generated through target capture experiment, we cleaned reads with trimmomatic to  
505 remove Illumina adapters and reads with a quality score below 30. For each species, we chose the  
506 individual with the highest coverage and constructed de novo assemblies using the same strategy as  
507 in fowls. Reads of each individuals were then mapped to the newly generated assemblies for each  
508 species, using BWA (57). Diploid genotypes were called using the same protocol as in fowls. We  
509 used a version of the SNP calling method which accounts for between-individual, within-species  
510 contamination as introduced in (48) (see the following section). As the newly generated assemblies  
511 likely contained intronic sequences, the predicted cDNAs were compared to the reference  
512 transcriptome using blastn searches, with a threshold of e-value of 10e-15. We used an in-house  
513 script to remove any incongruent correspondence or inconsistent overlap between sequences from  
514 the transcriptomic references and the predicted assemblies, and removed six base pairs at each  
515 extremity of the resulting predicted exonic sequences. These high-confidence exonic sequences  
516 were used for downstream analyses.

### 517 **3. Contamination detection and removal**

518 For the newly generated data set, we performed two steps of contamination detection. First, we used  
519 the software tool CroCo to detect inter-specific contamination in the *de novo* assembly generated  
520 after exon capture (33).

521 CroCo is a database-independent tool designed to detect and remove cross-contaminations in  
522 assembled transcriptomes of distantly related species. This program classifies predicted cDNA in  
523 five categories, “clean”, “dubious”, “contamination”, “low coverage” and “high expression”.

524 Secondly, we used a version of the SNP calling method which accounts for between-individual,  
525 within-species contamination as introduced in (48), using the `-contam=0.1` option. This means  
526 assuming that up to 10% of the reads assigned to one specific sample may actually come from a  
527 distinct sample, and only validating genotypes robust to this source of uncertainty.

### 528 **4. Orthology prediction and divergence analysis**

529 In primates, we extracted one-to-one orthology groups across the six species from the OrthoMaM  
530 database (60,61).

531 In fowls, passerines, rodents and flies, we translated the obtained CDS into proteins and predicted  
532 orthology using OrthoFinder (62). In fowls, full coding sequences from the well-annotated chicken  
533 genome (Ensembl release 89) were added to the dataset prior to orthology prediction, then  
534 discarded. We kept only orthogroups that included all species. We aligned the orthologous  
535 sequences with MACSE (Multiple Alignment for Coding SEquences (63)).

536 In each of earth worms, ribbon worms, mussels, butterflies and ants, orthogroups were created via a  
537 a `blastn` similarity search between predicted exonic sequences reference transcriptomes. In each  
538 taxon, we concatenated the predicted exonic sequences of each species that matched the same ORF  
539 from the reference transcriptome and aligned these using MACSE. We then kept alignments  
540 comprising exactly one sequence per species or if only one species was absent.

541 We estimated lineage specific dN/dS ratio using `bppml` (version 2.4) and `MapNH` (version 2.3.2)  
542 (64), the former for estimating each branch length and the latter for mapping substitutions on  
543 species specific branches.

544 Tree topologies were obtained from the literature (**Table S4**). In passerines, fowls, rodents, flies and  
545 primates, we kept only alignments comprising all the species. In the other groups we also kept  
546 alignments comprising all species but one.

547 We also estimated dN/dS ratios at group level by adding up substitution counts across branches of  
548 the trees, including internal branches.

549 To account for GC-biased gene conversion, we modified the MapNH software such that only GC-  
550 conservative substitutions were recorded (26). We estimated the non-synonymous and synonymous  
551 number of GC-conservative sites per coding sequence using an in-house script. We could then  
552 compute the dN/dS ratio only for GC-conservative substitutions.

## 553 **5. Polymorphism analysis**

554 For each taxon, we estimated ancestral sequences at each internal node of the tree with the Bio++  
555 program SeqAncestor (64). The ancestral sequences at each internal node were used to orientate  
556 single nucleotide polymorphisms (SNPs) of species that descend from this node. We computed non-  
557 synonymous ( $\pi_n$ ) and synonymous ( $\pi_s$ , i.e.  $\theta$ ) nucleotide diversity, as well as  $\pi_n/\pi_s$  using the software  
558 dNdSpiNpiS\_1.0 developed within the PopPhyl project ([https://kimura.univ-](https://kimura.univ-montp2.fr/PopPhyl/index.php?section=tools)  
559 [montp2.fr/PopPhyl/index.php?section=tools](https://kimura.univ-montp2.fr/PopPhyl/index.php?section=tools)) (using `gapN_site=4`, `gapN_seq=0.1` and median  
560 transition/transversion ratio values estimated by `bppml` for each taxonomic group). We also  
561 computed unfolded and folded synonymous and non-synonymous site frequency spectra both using  
562 all mutations and only GC-conservative mutations using an in-house script as in (18).

## 563 **6. Mc-Donlad-Kreitman analysis**

564 We estimated  $\alpha$ ,  $\omega_a$  and  $\omega_{na}$  using the approach of (16) as implemented in (18) (program Grapes  
565 v.1.0). It models the distribution of the fitness effects (DFE) of deleterious and neutral non-  
566 synonymous mutations as a negative Gamma distribution, which is fitted to the synonymous and  
567 non-synonymous site frequency spectra (SFS) computed for a set of genes. This estimated DFE is  
568 then used to deduce the expected dN/dS under near-neutrality. The difference between observed and  
569 expected dN/dS provides an estimate of the proportion of adaptive non-synonymous substitutions,  
570  $\alpha$ . The per mutation rate of adaptive and non-adaptive amino-acid substitution were then obtained as  
571 following:  $\omega_a = \alpha(\text{dN/dS})$  and  $\omega_{na} = (1-\alpha)(\text{dN/dS})$ . We computed these statistics for each species

572 using the per branch dN/dS ratio, using either all mutations and substitutions, or only GC-  
573 conservative mutations and substitutions.

574 We used three different distributions to model the fitness effects of mutations that have been shown  
575 to perform the best in (18). We then averaged the estimates of the three models using Akaike  
576 weights as follows:

$$\begin{aligned}\bar{\alpha} &= \alpha_{GammaZero} * AICw_{GammaZero} + \alpha_{GammaExpo} * AICw_{GammaExpo} + \alpha_{ScaledBeta} * AICw_{ScaledBeta} \\ \bar{\omega}_a &= \alpha_{GammaZero} * AICw_{GammaZero} + \omega_a_{GammaExpo} * AICw_{GammaExpo} + \omega_a_{ScaledBeta} * AICw_{ScaledBeta} \\ \bar{\omega}_{na} &= \omega_{na_{GammaZero}} * AICw_{GammaZero} + \omega_{na_{GammaExpo}} * AICw_{GammaExpo} + \omega_{na_{ScaledBeta}} * AICw_{ScaledBeta}\end{aligned}$$

577 where AICw stands for akaike weights that were estimated using the `akaike.weights` fonction in R  
578 (<https://www.rdocumentation.org/packages/qpcR/versions/1.4-1/topics/akaike.weights>).

579 When estimating DFE model parameters, we accounted for recent demographic effects by using  
580 nuisance parameters, which correct each class of frequency of the synonymous and non-  
581 synonymous SFS relative to the neutral expectation in an equilibrium Wright–Fisher population  
582 (39).

583 We also estimated  $\alpha$ ,  $\omega_a$  and  $\omega_{na}$  at group level. Two approaches were used. Firstly, we pooled  
584 species specific SFS from each group, and used the dN/dS ratio of the total tree of each taxon. We  
585 did so following the unweighted and unbiased strategy of (34), which combines polymorphism data  
586 across species with equal weights. Briefly, we divided the synonymous and non-synonymous  
587 number of SNPs of each category of the SFS of each species by the total number of SNPs of the  
588 species, then we summed those normalized numbers across species and finally we transformed  
589 those sums so that the total number of SNPs of the pooled SFS matches the total number of SNPs  
590 across species. The resulting estimate was called  $\omega_{a[PI]}$ . Secondly, we calculated the arithmetic mean  
591 of  $\omega_{na}$  across species within a taxonomic group to obtain a non-adaptive substitution rate at the  
592 group level. We then subtracted this average from the dN/dS ratio calculating across the whole tree  
593 of each taxon to obtain an estimate of the adaptive substitution rate at group level (called  $\omega_{a[A]}$ ).

## 594 **7. Life history traits variables**

595 Five life history traits were retrieved from the literature for each species: adult size (i.e. the average  
596 length of adults), body mass (i.e. the mean body mass of adults' wet weights), fecundity (i.e. the

597 number of offspring released per day), longevity (i.e. the maximal recorded longevity in years), and  
598 propagule size (i.e. the size of the juvenile or egg or larva when leaving parents or group of  
599 relatives) (**Table S5**). In the case of social insects and birds, parental care is provided to juveniles  
600 until they reach adult size so in these cases, propagule size is equal to adult size.

## 601 **8. Simulations**

602 In order to evaluate whether our method to estimate the adaptive substitution rate could lead to a  
603 spurious correlation between  $\pi_s$  and  $\omega_a$ , we simulated the evolution of coding sequences in a single  
604 population undergoing demographic fluctuations using SLIM V2 (65). We considered panmictic  
605 populations of diploid individuals whose genomes consisted of 1500 coding sequences, each of 999  
606 base pairs. We set the mutation rate to  $2.2e-9$  per base pair per generation, the recombination rate to  
607  $10e-8$  per base (as in (23)) and the DFE to a gamma distribution of mean -740 and shape 0.14 for  
608 the negative part, and to an exponential distribution of mean  $10^{-4}$  for the positive part (those DFE  
609 parameters correspond to the DFE estimated from the pooled SFS of primates). We simulated  
610 several demographic scenarios with four regimes of frequency of the fluctuations, as well as four  
611 regimes of intensity of the fluctuations (see **figure S5**). We sampled polymorphism and divergence  
612 for 20 individuals at several time points during the simulations, evaluated  $\pi_s$  and  $\omega_a$  and measured  
613 the correlation between the two variables.

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621 Fisher's geometrical model predictions.

622 **Data accessibility:**

623 Illumina raw reads of the capture experiment are deposited under the Bioproject PRJNA530965 in  
624 the SRA database.

625 **Supplementary tables and figures legends:**

626 **Table S1 : Details of the species used in this study and numbers of individuals for each species.**

627 **Table S2 : Number of orthogroups for each taxonomic group.**

628 The differences in terms of number of orthogroups comes from the fact that we not only kept orthogroups with all  
629 species but also orthogroups with all species but one to estimate dN/dS value for each terminal branches in order to  
630 maximize the number of substitutions for data sets generated by exon capture.

631 **Table S3: SNPs counts for each species.**

632 SNPs counts are not integers because they corresponds to SNPs that are present in our SFS, where we chose a sample  
633 size (i.e. the number of categories of the SFS) lower that  $2*n$ , where  $n$  is the number of individuals. This is to  
634 compensate the uneven coverage between individuals that results in some sites in some individuals not to be genotyped.  
635 We chose sample sizes that maximize the number of SNPs in each SFS.

636 **Table S4: Sources of the tree topologies of each taxonomic group used to estimate branch  
637 length and map substitutions.**

638 **Table S5: Values and sources of the life history traits used in this study.**

639 **Figure S1: Cross contamination network for de novo assemblies from exon capture.**

640 Circles represent the assemblies, and arrows and their corresponding numbers represent the number of cross  
641 contaminants. Most cross contamination events occur between closely-related species and are therefore likely false  
642 positive cases.

643 **Figure S2: Relationship between  $\omega_{a[P]}$  and  $\pi_s$  and  $\log_{10}$  transformed life history traits.**

644  $\omega_{a[P]}$  is estimated using all mutations and substitutions (A) or using only GC-conservative mutations and substitutions  
645 (B). Group level  $\pi_s$  and life history traits are estimated by averaging species level estimates across closely related  
646 species. The lines represent the regression across groups and \* symbols indicate when it is significant.

647 **Figure S3: Relationship between  $\omega_{a[A]}$  and  $\pi_s$  and  $\log_{10}$  transformed life history traits.**

648  $\omega_{a[A]}$  is estimated using all mutations and substitutions (A) or using only GC-conservative mutations and substitutions  
649 (B). Group level  $\pi_s$  and life history traits are estimated by averaging species level estimates across closely related  
650 species. The lines represent the regression across groups and \* symbols indicate when it is significant.

651 **Figure S4: Relationship between species-level  $\omega_{na}$  and  $\pi_s$  and  $\log_{10}$  transformed life history  
652 traits.**

653  $\omega_{na}$  is estimated using all mutations and substitutions (A) or using only GC-conservative mutations and substitutions  
654 (B). The dotted lines represent the regression across all species and \* symbols indicate when it is significant.

655 **Figure S5: Relationship between species-level  $\alpha$  and  $\pi_s$ .**

656  $\alpha$  is estimated using only GC-conservative mutations. The dotted line represents the regression across all species, and  
657 full lines represent the regression within each taxonomic groups.

658 **Figure S6: Design of the simulations of fluctuation of population size.**

659 A: three fold ratio between low and high population size and high long-term population size.

660 B: thirty fold ratio between low and high population size and high long-term population size.

661 C: three fold ratio between low and high population size and low long-term population size.

662 D: thirty fold ratio between low and high population size and low long-term population size.

663 **Figure S7: Relationship between  $\omega_a$  and  $\pi_s$  in simulated scenarios of fluctuating population  
664 size.**

665 A: three fold ratio between low and high population size and high long-term population size (scenario A in figure S1)

666 B: thirty fold ratio between low and high population size and high long-term population size (scenario B in figure S1)

667 C: three fold ratio between low and high population size and low long-term population size (scenario C in figure S1)

668 D: thirty fold ratio between low and high population size and low long-term population size (scenario D in figure S1)

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