

DESCRIPTION OF ADDITIONAL SUPPLEMENTARY MATERIALS

Supplementary Movie 1: Live-cell time-lapse confocal microscopy showing multiple Rad52 foci (Rad52-YFP) engaging in dripping behaviour in a representative cell that was treated with 0.03% MMS to induce DNA damage. Scale bar, 1 μm .

Supplementary Movie 2: Live-cell time-lapse confocal microscopy reveals that Rad52 foci (Rad52-YFP) can fuse with each other in a representative cell that was treated with 0.03% MMS to induce DNA damage. Two fusion events are seen on the right. Scale bar, 1 μm .

Supplementary Movie 3: Live-cell time-lapse confocal microscopy showing multiple smaller Rad52 foci (Rad52-YFP) bumping into one larger central droplet in a yeast cell that was treated with 0.03% MMS to induce DNA damage. Scale bar, 1 μm .

Supplementary Movie 4: Live-cell time-lapse confocal microscopy from a FLIP experiment. Rad52 droplet (Rad52-YFP) intensity rapidly decreases upon photobleaching of a nucleoplasmic point outside the Rad52 focus. Yeast cells were treated with 0.03% MMS to induce DNA damage.

Supplementary Movie 5: Light microscopy showing the fusion of Rad52 droplets assembled *in vitro*.

Supplementary Movie 6: Live-cell time-lapse confocal microscopy revealing dynamic pti-DIMs inside the nucleus. Cells were treated with 0.03% MMS to induce DNA damage. GFP-Tub1 (α -Tubulin) and Nup49-GFP (nuclear pore complexes) are shown in cyan. Scale bar, 1 μm .

Supplementary Movie 7: Time-lapse from Supplementary Movie 6 overlaid with the corresponding Rad52 droplet signal (Rad52-YFP shown in magenta). Scale bar, 1 μm .

Supplementary Movie 8: Representative computational flow dynamics simulation in which pti-DIM extension-shortening cycles resulted in the fusion of two Rad52 droplets. The line connecting the droplets in their initial position was perpendicular to the velocity exerted by the pti-DIMs at the centre of the Y-axis. The parameters used in this simulation were $r = 046$, $\rho = 1014 \text{ Kg/m}^3$, $\sigma = 1.4 \text{ uN/m}$, $\mu = 0.005$, $\Theta = 90^\circ$, $u = 41 \text{ nm/s}$, and $f = 1000 \text{ Hz}$ as shown in Supplementary Figure 2.

Supplementary Movie 9: Representative computational flow dynamics simulation in which pti-DIM extension-shortening cycles failed to result in the fusion of two Rad52 droplets. The line connecting the droplets in their initial position was rotated clockwise by 20° compared to the position in Supplementary Movie 8, thereby changing Θ to 110° . Other simulation parameters were identical to those used in that movie.

Supplementary Movie 10: Live-cell time-lapse confocal microscopy showing a large Rad52 droplet with an internally concentrated tubulin focus that is captured by and travels along a stable DIM. Cells were treated with 0.03% MMS to induce DNA damage. GFP-Tub1 (tubulin) and Nup49-GFP (nuclear envelope) are shown in cyan and Rad52-YFP in magenta. Scale bar, 1 μm .