

1 Title:

2 Allometric scaling strengthens the relationship between eDNA particle concentration and
3 organism abundance in nature

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5 Running title:

6 Allometry and eDNA particle concentration

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16

17 **Abstract**

18 *Organism abundance is a critical parameter in ecology, but its estimation is often challenging.*
19 *Approaches utilizing eDNA to indirectly estimate abundance have recently generated substantial*
20 *interest. However, preliminary correlations observed between eDNA concentration and*
21 *abundance in nature are typically moderate in strength with significant unexplained variation.*
22 *Here we apply a novel approach to integrate allometric scaling coefficients into models of eDNA*
23 *concentration and organism abundance. We hypothesize that eDNA particle production scales*
24 *non-linearly with mass, with scaling coefficients < 1 . Wild populations often exhibit substantial*
25 *variation in individual body size distributions; we therefore predict that the distribution of mass*
26 *across individuals within a population will influence population-level eDNA production rates. To*
27 *test our hypothesis, we collected standardized body size distribution and mark-recapture*
28 *abundance data using whole-lake experiments involving nine populations of brook trout. We*
29 *correlated eDNA concentration with three metrics of abundance: density (individuals/ha),*
30 *biomass (kg/ha), and allometrically scaled mass (ASM) ($\sum(\text{individual mass}^{0.73})/\text{ha}$). Density and*
31 *biomass were both significantly positively correlated with eDNA concentration (adj. $R^2 = 0.59$*
32 *and 0.63, respectively), but ASM exhibited improved model fit (adj. $R^2 = 0.78$). We also*
33 *demonstrate how estimates of ASM derived from eDNA samples in ‘unknown’ systems can be*
34 *converted to biomass or density estimates with additional size structure data. Future experiments*
35 *should empirically validate allometric scaling coefficients for eDNA production, particularly*
36 *where substantial intraspecific size distribution variation exists. Incorporating allometric scaling*
37 *may improve predictive models to the extent that eDNA concentration may become a reliable*
38 *indicator of abundance in nature.*

39

40 Keywords:

41 environmental DNA, eDNA, Abundance, Density, Biomass, Allometry, Allometric scaling

42 **Introduction**

43 Developing methods to estimate animal abundance in nature has attracted the attention of
44 researchers and managers alike for over a century (Schwarz & Seber, 1999). Abundance is a
45 fundamental population parameter in ecology, conservation, and natural resource management
46 (Luikart, Ryman, Tallmon, Schwartz, & Allendorf, 2010), with direct impacts on ecological
47 interactions (Krebs, 2009), ecosystem functioning (Schaus et al., 2010), population persistence
48 and adaptability (Jamieson & Allendorf, 2012), as well as ecosystem services/resources (Immell
49 & Anthony, 2008; Schwarz & Seber, 1999). Methodologies to estimate animal abundance
50 represent a well-developed field of empirical research in ecology that has progressed remarkably
51 (Schwarz & Seber, 1999; Seber, 1986). Yet despite this success, the estimation of abundance in
52 nature is often challenging; obtaining robust estimates in natural populations using traditional
53 methods can be time-consuming, costly, labor intensive, or even impossible to obtain for some
54 populations (Luikart et al., 2010; Ovenden et al., 2016; Yates, Bernos, & Fraser, 2017).

55 The recent development of novel molecular tools has renewed interest in utilizing genetic
56 information to indirectly estimate abundance in difficult-to-sample natural populations
57 (Goldberg, Strickler, & Pilliod, 2015; Luikart et al., 2010). Molecular techniques that quantify
58 the concentration of environmental DNA (eDNA) particles represent a promising tool, with
59 recent studies demonstrating support for a correlation between eDNA concentration and
60 abundance (Pilliod, Goldberg, Arkle, & Waits, 2013; Takahara, Minamoto, Yamanaka, Doi, &
61 Kawabata, 2012; Thomsen et al., 2012). For example, laboratory studies have demonstrated a
62 strong correlation between eDNA concentration and abundance (Eichmiller, Miller, & Sorensen,
63 2016; Klymus, Richter, Chapman, & Paukert, 2015), exhibiting a mean correlation coefficient of
64 0.9 ($R^2 = 0.81$) (Yates, Fraser, & Derry, 2019). Studies in nature, however, have generally found

65 weaker correlations than laboratory studies, with a mean correlation coefficient of 0.71-0.75 (R^2
66 = 0.51-0.57) (Yates et al., 2019). Although correlations remain moderately strong in nature,
67 much of the variation in eDNA particle concentration across environments often remains
68 unexplained. As a result, the extent to which eDNA could be used to reliably infer abundance in
69 nature remains limited without significant improvements in modelling or technology.

70 In nature, organismal abundance is typically quantified by evaluating individual density
71 (i.e. individuals/unit area) or biomass density (i.e. kg/unit area). While both metrics of abundance
72 appear to correlate equally well with species-specific eDNA particle concentration in the wild,
73 processes involved in the production of eDNA particles in natural environments are unlikely to
74 scale linearly with either biomass or density. Although eDNA production tends to increase with
75 individual mass (Maruyama, Nakamura, Yamanaka, Kondoh, & Minamoto, 2014), individuals
76 with a large biomass often produce fewer eDNA particles than equivalent biomass of smaller
77 conspecifics (Maruyama et al., 2014; Mizumoto, Urabe, Kanbe, Fukushima, & Araki, 2017;
78 Takeuchi, Iijima, Kakuzen, Watanab, & Yamada, 2019). As such, eDNA particle concentration
79 would be expected to vary, for example, between environments that contain equal densities of
80 individuals but with varying biomass. Similarly, environments with equal biomass but varying
81 densities would also be likely to vary in observed eDNA particle concentration. Wild populations
82 often exhibit substantial inter-population variation in the distribution of individual biomass
83 (Donald, Anderson, Mayhood, Anderson, & Correlations, 1980; Guernon, Yates, Fraser, &
84 Derry, 2018; Millien et al., 2006; Sebens, 1987), which may in turn scale to affect overall
85 population-level rates of eDNA production (Maruyama et al., 2014) and partially account for the
86 substantial unexplained variation observed between eDNA concentration and traditional metrics
87 of abundance (e.g. density and biomass) in nature (Yates et al., 2019).

88 Here, we extend models of physiological allometric scaling to organismal eDNA particle
89 production to provide a framework through which differences in density, total biomass, and the
90 distribution of individual biomass can be integrated into models of eDNA production in natural
91 populations. Excretory processes (urine, fecal matter, etc.) and shedding (from scales, skin,
92 mucous, etc.) are thought to be the two major physiological processes that contribute to the
93 production of eDNA particles (Jo, Murakami, Yamamoto, Masuda, & Minamoto, 2019; Stewart,
94 2019). The metabolic theory of ecology (MTE) provides a robust, empirically validated
95 framework through which allometry in metabolic processes (including excretion) can be
96 modelled. The MTE posits that metabolic processes scale non-linearly with body size according
97 to the power function:

$$98 \qquad I = I_0 * M^b$$

99 where I = metabolic rate, I_0 = a normalization constant, M = organism body mass, and b = an
100 allometric scaling coefficient (Allegier, Wenger, Rosemond, Schindler, & Layman, 2015;
101 Brown, Gillooly, Allen, Savage, & West, 2004; Vanni & McIntyre, 2016). The value of b varies
102 depending on the physiological process; metabolic rates typically scale to the power of 0.75
103 (Brown et al., 2004; Isaac & Carbone, 2010), whereas values for consumptive or excretory rates
104 are often lower (Post, Parkinson, & Johnston, 1999; Vanni & McIntyre, 2016). Nevertheless,
105 metabolic theory predicts that larger organisms tend to exhibit disproportionately lower rates
106 (relative to their mass) for metabolically linked processes such as excretion (Allen & Gillooly,
107 2009; Vanni & McIntyre, 2016). While shedding from mucous, scales, or skin may also be
108 linked to metabolic rates, shedding rates are also likely a function of the surface area of an
109 organism. In many aquatic organisms (particularly fish) the allometric relationship between body
110 mass and surface area follows a similar mathematical form as metabolic processes; salmonids,

111 for example, exhibit mass-scaling coefficients for surface area between 0.59 and 0.65 (Shea,
112 Fryer, Pert, & Bricknell, 2006).

113 Metabolic rates, excretory rates, and surface area (via shedding) are likely to collectively
114 impact eDNA production, yet all follow a similar allometric form; as a result, we hypothesize
115 that eDNA production can also be modelled as a power function of individual mass and an
116 exponential scaling coefficient with a value less than 1. This hypothesis has important
117 consequences for ecosystem-level processes; the utility of integrating allometric scaling in
118 ecosystem-level models of ecological stoichiometry (Allen & Gillooly, 2009), animal excretion
119 (Vanni & McIntyre, 2016), consumption (Post et al., 1999), and nutrient cycling (Schaus et al.,
120 2010; Schindler & Eby, 1997), for example, has long been acknowledged with broad empirical
121 support. We therefore further hypothesize that, when scaled to the level of an entire population,
122 allometric scaling in eDNA production will also have a substantial effect on overall population-
123 level production of eDNA. We consequently predict that the incorporation of mass scaling
124 coefficients to account for inter-population variation in density, biomass, and the distribution of
125 biomass across individuals will improve modelling efforts linking eDNA particle concentration
126 and abundance across natural ecosystems.

127 To test our hypothesis, we collected standardized individual biomass data and used
128 classic mark-recapture experiments to enumerate abundance in nine populations of brook trout in
129 the Rocky Mountains of Canada while simultaneously collecting eDNA samples in each lake.
130 Study populations exhibited substantial variation in individual density (63 - 1177 individuals/ha),
131 biomass density (12.6 - 52.4 kg/ha), and mean body size (43.0 - 405.9 g/individual). We applied
132 these data to specifically test two key predictions: i) brook trout eDNA particle concentration
133 will correlate with traditional metrics of abundance (density and biomass) across the nine study

134 lakes; and ii) incorporating allometric scaling coefficients to estimates of brook trout abundance
135 (e.g. $\sum(\text{individual biomass}^{0.73})/\text{ha}$, or “allometrically scaled mass” (ASM)) will substantially
136 improve models of abundance and eDNA particle concentration.

137 ASM estimates derived from known eDNA concentrations in novel systems lacking
138 abundance data cannot be directly converted to traditional metrics of abundance (e.g. density and
139 biomass) because multiple density/biomass configurations (e.g. many small fish or a small
140 number of large fish) can produce equivalent ASM values. However, using a real-world
141 example, we also demonstrate how ASM estimates derived from known eDNA concentrations
142 for systems that lack abundance data on a target species can be converted into traditional
143 estimates of abundance with additional size structure data.

144 **Materials and Methods**

145 *Study species and system*

146 Nine brook trout populations introduced in the early 20th century to lakes located in
147 Kootenay, Banff, and Yoho national parks (Figure S1) were monitored to determine population
148 size (number of individuals > 80mm) and individual biomass distributions. Study populations
149 experience little recreational fishing pressure due to no-take policies implemented within the
150 National Parks.

151

152 *Mark-recapture surveys and size structure estimates*

153 Mark-recapture studies were conducted in 2018 between May 27th and June 30th, except
154 for Cobb lake where isolated marking events occurred until September 12th (Figure S2). Fish
155 were captured using a combination of fyke nets, angling, and backpack electrofishing (Table 1).
156 Large (1 m hoop diameter, 2 cm mesh) and small (0.7 m hoop diameter and 0.8 cm mesh) fyke
157 nets were distributed around the perimeter of lakes with the lead attached to shore and the end of
158 the trap facing the center of the lake. Nets were checked daily to reduce stress to fish and
159 possible cannibalism. Angling was used to supplement fish capture efforts at sites where fyke
160 catchability was low (predominantly Cobb). Marks were also assigned to fish captured by
161 electrofishing the shore and inlets/outlets of lakes with a backpack electrofisher (Smith-Root,
162 Vancouver, Washington, USA)

163 Captured fish were anesthetized using clove oil and measured for fork length (\pm 1mm)
164 and mass (\pm 0.1g). Any unmarked fish were gastrically tagged with a BioMark HPT8 pre-loaded
165 Passive Integrated Transponder (PIT) tag (Boise, Idaho, USA). Only fish greater than or equal to
166 80 mm were tagged to reduce tagging mortality. The tag number of any recaptured fish was

167 recorded. All fish were processed in the shade with aerators to avoid unnecessary stress.
168 Recovered fish were released in the center of the lake to standardize release location and
169 promote mixing (e.g. if released near shore, fish may have been recaptured in an adjacent net,
170 biasing mark recapture data). Marking ceased once recapture ratios approached twenty five
171 percent for several consecutive days.

172 Size structure estimates aimed to obtain a representative snapshot of the size structure of
173 each population and was conducted between July 27th and September 1st, with the exception of
174 Cobb where size structure assessments continued to October 12th (Figure S2). Fish were captured
175 in large and small sinking mixed mesh gillnets with clear monofilament. Large mixed-mesh
176 gillnets were 15.6 m long, 1.8 m deep and had an equal area of 64-51-89-38-76 mm mesh panels.
177 Small mixed-mesh gillnets were 12.5 meters long, 1.8 meters deep, and consisted of an equal
178 area of 32-19-38-13-25 mm mesh panels. Index nets are widely used in North America for size
179 structure assessments (Bonar, Hubert, & Willis, 2009; Hubert, Pope, & Dettmers, 2012; Johnson,
180 1983; Post et al., 1999; Ward, Askey, Post, Varkey, & Mcallister, 2012) as these attempt to
181 capture a representative size/age structure of the population (Morgan, 2002). Nets were checked
182 daily and moved if they were being reset. Sampling ceased when approximately five to ten
183 percent of the population was captured, apart from Cobb lake where size structure assessment
184 captured approximately 71% of individuals (Table 1). Captured fish were euthanized with clove
185 oil, PIT tags were recorded, and length/mass data were collected as described for the marking
186 period.

187

188 *Population size estimation*

189 Schnabel population size estimates, which utilize sequential marking/recapture events,
190 were used to determine the number of fish in a lake (Schnabel, 1938). All size structure
191 assessment removals were pooled together into one final sampling event for the population
192 estimates which controlled for the removal of marks at large (M). Note that population estimates
193 only account for fish greater the minimum tagging size (80 mm fork length). All population
194 estimates were conducted in R (R Development Core Team, 2017) with the *mrClosed* function
195 from the Fisheries Stock Assessment package FSA (Ogle, 2016). Confidence intervals for
196 Schnabel population estimates followed recommendations from (Seber, 2002) as implemented in
197 the FSA package.

198 *Density calculation*

199 To link eDNA particle concentration with fish abundance, three metrics of density were
200 calculated: (i) individual density (individuals/ha); (ii) biomass density (biomass/ha); (iii) and
201 allometrically scaled mass (ASM/ha). Individual density was estimated by dividing the
202 population size estimate by lake size (ha). Biomass density was calculated according to the
203 following formula:

204
$$\text{biomass per ha} = \frac{\sum_{i=1}^{N_{SA}} \text{mass}_{SA} \cdot \hat{N}}{N_{SA} \cdot \text{area (ha.)}}$$

205 Where $\sum_{i=1}^{N_{SA}} \text{Mass}_{SA}$ is the sum of the masses captured in the index net during size structure
206 assessment, N_{SA} is the number of fish captured in the index nets, \hat{N} is the estimated population
207 size. This methodology assumes that the size structure assessment was representative of the
208 population.

209 ASM was calculated by replacing the mass measure with $\text{mass}^{0.73}$ according to the

210 formula:

$$211 \quad ASM \text{ per ha} = \frac{\sum_{i=1}^{N_{SA}} (mass_{SA}^{0.73})}{N_{SA}} \cdot \hat{N}$$

212 *area (ha.)*

213 This density metric was included to account for the relative decline in mass-specific eDNA
214 production or excretion rates typically observed as individual organismal mass increases
215 (Maruyama et al., 2014; Takeuchi et al., 2019; Vanni & McIntyre, 2016). Scaling coefficients
216 can vary substantially depending on the physiological process, taxonomy or environment
217 (Allegier et al., 2015; Glazier, 2005). In the absence of data on allometric scaling in eDNA
218 production, data on allometric scaling in metabolic or excretory rates for the same study species
219 can represent useful starting points. Data on allometry in excretory rates were unavailable for
220 brook trout, so the metabolic scaling coefficient obtained from (Hartman & Cox, 2008) was
221 used: data extracted using the R package *digitizer* (Poisot, 2011) and back-transformed from
222 figure one in (Hartman & Cox, 2008) indicate an allometric metabolic scaling factor of
223 approximately 0.73 (0.03 SE).

224 In difficult to sample populations, estimates of relative abundance are often obtained
225 using CPUE metrics. As a result, most previous studies examining eDNA particle concentration
226 and abundance utilize similar metrics (Yates et al., 2019). To evaluate the utility of CPUE as a
227 ‘proxy’ metric of abundance in our study system, CPUE for each lake was quantified as the
228 mean catch per-unit effort of a large and small index gillnet.

229

230 *eDNA sample collection*

231 eDNA samples were collected between June 30 and July 13th, 2018. Sampling was
232 equidistantly distributed around each lake and included four littoral and four pelagic samples.
233 Littoral samples were collected approximately 1-3 m from shore at a depth of least 12 inches but
234 six inches above the bottom to avoid the unintentional collection of sediments. Pelagic samples
235 were collected from each lake by drawing a line through the center of the lake along its longest
236 axis; samples were collected along this axis at equidistant intervals at a depth of approximately
237 0.5m. To avoid between-lake contamination all eDNA samples were collected either from an
238 inflatable kayak that was decontaminated 48h prior in a 2% bleach solution for 15 minutes
239 (including paddle and life-jacket) or from a canoe assigned to sample a single specific lake.
240 Water samples were collected using sterile Whirl-PakTM bags (Uline, Ontario, Canada).

241 Samples were immediately filtered on the lakeshore using two chlorophyll filtering
242 manifolds bleached in a 30% household bleach solution for ten minutes 2-12h prior to collection.
243 All samples were stored in the shade prior to filtration in plastic washbasins bleached with a 30%
244 solution for ten minutes, and all filtering was conducted in the shade under a tarp. Manifolds
245 were transported in a Polar BearTM backpack cooler (Polar Bear Coolers, Georgia, USA) whose
246 interior was wiped with a 30% bleach solution for ten minutes. Manifold components were
247 stored after bleaching and transported individually in sealed plastic zippered bags to limit
248 contamination. Pencils and markers were also wiped with a 30% bleach solution.

249 One L of sample water from each site was filtered through a 0.7 μ m-pore glass fibre filter
250 (GE Healthcare Life Sciences, Ontario, Canada) using a vacuum hand pump (Soil Moisture,
251 California, USA); each vacuum pump was decontaminated between lakes by wiping with a 30%
252 bleach solution and resting for ten minutes. All littoral samples were filtered on one manifold

253 and all pelagic samples were filtered on the other. Prior to filtering lake water samples, 1 L of
254 distilled water was filtered through each manifold as a negative control. Filters were handled
255 using two metal forceps bleached in a 30% solution for ten minutes and transported in individual
256 bags; one forceps was used for littoral samples and another forceps was used for pelagic samples.
257 After filtering, filters were folded and placed directly in a sterile 2 ml microcentrifuge tube filled
258 with 700µl AL buffer (Qiagen, Maryland, USA) which was then labelled and individually sealed
259 in a plastic zippered bag and placed in a 2nd cooler that was decontaminated by wiping with a
260 30% bleach solution and resting for ten minutes. This cooler contained two frozen freezer-gel
261 packs decontaminated in a 30% bleach solution for ten minutes. If a filter became clogged (i.e. <
262 1 L of water was filtered) the final volume of water filtered was recorded and the sample was
263 stored in buffer. Filters were immediately transported to and stored in a -20 °C freezer (wiped
264 with 30% bleach and soaked for ten minutes) at Kootenay Crossing. Filters were stored on dry
265 ice for transportation to Montreal where they were stored in a -80 °C freezer.

266 *eDNA extraction and analysis*

267 Each filter was extracted using a Qiagen DNeasy Blood and Tissue™ kit and
268 Qiashredder™ spin column following a modified extraction protocol (see Appendix S1 for
269 details). Final DNA product was eluted into 130 µl of AE buffer and stored in a clean -20 °C
270 freezer dedicated to the sole storage of eDNA samples. To avoid cross-contamination between
271 lakes extractions were conducted on batches from a single lake, with a single extraction blank of
272 700 µL AL buffer included as an extraction control. Decontamination procedures were identical
273 for both manifolds, so only a single negative control was extracted per lake. All extractions were
274 conducted in an extraction room dedicated to the handling of sensitive eDNA samples. This
275 room receives weekly cleaning with a 10% bleach solution and is free of PCR products or high-

276 concentration DNA. All individuals entering the extraction room were required to wear nitrile
277 gloves, hair nets, shoe covers, and dedicated, clean lab coats. All lab surfaces were soaked with a
278 20% bleach solution for ten minutes before and after extractions. PCR Clean Wipes™ (Thermo
279 Scientific, Massachusetts, USA) were also used to decontaminate all lab surfaces and pipettes
280 prior to and after extracting or handling eDNA samples.

281 The concentration of brook trout eDNA was quantified using the TaqMan minor groove
282 assay published in (Wilcox et al., 2013), which targets a region of the brook trout cytochrome *b*
283 mitochondrial gene. All samples were run in triplicate at a 20 µl final reaction volume on a
284 Stratagene MX 3000P thermal cycler using Environmental Master Mix 2.0 and 5 µl of template
285 DNA. Forward and reverse primers were included at a final concentration of 900 nM, with the
286 probe at a final concentration of 250 nM. Each replicate was spiked with an internal positive
287 control to test for inhibition; any replicate that exhibited inhibition ($C_t > 1$ in the internal positive
288 control) was reanalyzed with diluted template DNA at 60% concentration (3 µl template + 2 µl
289 of ultrapure water); this was sufficient to relieve inhibition in all cases. Standard curve template
290 DNA was composed of a synthetic Gblock™ gene fragment (IDT, Iowa, USA) of the targeted
291 sequence. A triplicate no template control and triplicate five-point standard curve (1250
292 copies/µl, 250 copies/µl, 50 copies/µl, 5 copies/µl, 2 copies/µl template concentration) were
293 included on each 96-well plate. All qPCR reaction reagents were aliquoted into single-use
294 volumes adequate for a single plate and reactions were prepared in the dedicated eDNA room,
295 with the exception of the standard curve replicates due to the presence of high concentration
296 synthetic DNA fragments. Reactions were cycled with an initial hold at 95 °C for ten minutes
297 followed by 45 cycles of 30 seconds at 95 °C and 1 min at 60 °C. eDNA particle concentration at
298 each site was determined by averaging site-specific replicates. Final mean copy number values

299 were converted (based on total volume of water filtered per sample) to total eDNA particle
300 concentration per 1 L of sampled water (copies/L).

301 *Data Analysis*

302 Mean eDNA particle concentration (copies/L) for each lake was calculated by first
303 averaging eDNA particle concentrations of the four littoral and four pelagic samples to obtain
304 mean littoral eDNA concentration and mean pelagic eDNA concentration. The surface area of a
305 (roughly) circular object increases non-linearly in relation to perimeter and, as a result, the area
306 of the pelagic zone expressed as a fraction of the total area of a lake tends to increase with lake
307 size. The relative contribution of the littoral and pelagic zones to the overall mean concentration
308 of eDNA per lake should therefore be increasingly weighted towards the pelagic eDNA
309 concentration as lake surface area increases. Our study lakes varied substantially in size (1.7 to
310 18.5 ha); total pelagic and littoral areas were calculated for each lake using polygons on Google
311 Earth. In the absence of detailed bathymetry data, the total area of the littoral zone was calculated
312 by including all lake surface area up to 20m from the shore, with the remaining area assigned to
313 the pelagic zone. A weighted-mean eDNA concentration for each lake was then calculated by
314 weighing the littoral and pelagic eDNA concentrations based on the fraction of total lake area
315 each zone represented.

316 Mean lake eDNA particle concentration (copies/L) was modelled separately as a function
317 of the three metrics of brook trout density calculated above: individual density (individuals/ha);
318 biomass density (kg/ha); and allometrically scaled mass (ASM) ($\sum(\text{individual mass}^{0.73})/\text{ha}$).
319 eDNA particle concentration was included as a dependent variable in a linear regression and a
320 separate model for each abundance metric was fitted to the observed data. Wald F -tests were
321 used to evaluate the significance of fixed-effect terms, with AIC (Akaike, 1974) values used to

322 compare model fit as in (Lacoursière-Roussel, Côté, Leclerc, Bernatchez, & Cadotte, 2016). All
323 analyses were conducted in R (v.3.3.3) (R Development Core Team, 2017). To assess the
324 performance of CPUE as a ‘proxy’ metric of abundance, we also examined the relationship
325 between density and CPUE, as well as eDNA particle concentration and CPUE, using linear
326 regression.

327

328 *Estimating density and biomass from predicted allometrically scaled mass: a case study for*
329 *population management*

330 Most researchers/managers would be primarily interested in predicting traditional metrics
331 of abundance (i.e. density and biomass) from estimated eDNA particle concentrations in similar
332 ecosystems that lack abundance data. Predicting abundance in unknown systems from known
333 eDNA particle concentrations would require an inversion of the modelling relationship described
334 above: abundance would be modelled as a function of eDNA particle concentration. Predicted
335 estimates of ASM obtained from eDNA samples collected for systems lacking abundance data
336 cannot be directly converted to traditional metrics of abundance (e.g. individual density or
337 biomass density) because multiple density/biomass configurations (e.g. many small fish or a
338 small number of large fish) can produce equivalent ASM values. However, predicted ASM
339 point-estimates for a system with unknown abundance can be converted to traditional metrics
340 with additional individual mass distribution data from standardized size structure data. Size
341 structure data from the unknown system could be scaled allometrically and the resulting scaled
342 mass values nonparametrically bootstrapped (with replacement) until the cumulative sum of the
343 bootstrapped values equals the predicted ASM. Individual density could be estimated by totalling
344 the number of bootstrap “samples” summed to achieve the predicted ASM; biomass density

345 could then be estimated by multiplying the predicted density value by the untransformed mean of
346 the individual biomass distribution.

347 As a case study, this technique was applied to data collected from Hidden Lake (Banff,
348 Alberta, Canada). The brook trout population of Hidden Lake was targeted as part of rotenone-
349 based removal program by Parks Canada. eDNA samples from Hidden lake were collected in
350 July 2018 and extracted/analyzed using the same methodology as described above. The
351 estimated “ASM/unit area” of the lake (including 95% prediction intervals) was calculated from
352 the linear relationship obtained from our nine study lakes. Unfortunately, standardized size
353 structure data were unavailable; rotenone removal efforts began in August 2018 and no brook
354 trout remain in the system. However, prior to the use of rotenone mechanical gill netting efforts
355 were employed during brook trout removal efforts between 2011 and August 2017 (Stitt, *perse.*
356 *comm.*). By 2016 netting efforts had removed most large fish from the population. Most netted
357 fish older than age 0+ in Hidden lake were therefore between 90-140mm in length (Sullivan,
358 Sierra, 2017), although it should be noted that size distribution data obtained from these netting
359 efforts were not directly comparable to our standardized size structure assessments due to
360 different netting methodology/gear. The size distribution of fish removed by Parks Canada in
361 2016 most closely resembles the size distribution of fish in Olive lake, so the Olive size
362 distribution was utilized as a “proxy” to calculate an approximate pre-rotenone individual density
363 and biomass density of brook trout inhabiting Hidden lake in 2018. The size distribution of fish
364 from Olive lake is slightly larger (mean = 149mm) than the 2016 Hidden lake distribution; as a
365 result, population size estimates derived from this distribution will likely slightly underestimate
366 the ‘true’ number of individuals present in Hidden Lake. Bootstrap simulations to quantify
367 individual density and biomass density utilizing the Olive size distribution and predicted ASM of

368 Hidden lake were run for 1000 iterations. Parks Canada estimated the 2018 pre-rotenone
369 population of Hidden Lake to be between 3300 and 5000 individuals based on the retrieval of
370 fish corpses post-rotenone, providing some degree of external validation for our predictive model
371 (Stitt, B, 2018).

372 *Predicting allometric scaling coefficient for eDNA production in brook trout*

373 Allometric scaling coefficients are likely to fall between a value of 0.0 and 1.0; notably,
374 (\sum individual mass^{0.0})/ha is equivalent to individual density (fish/ha) and (\sum individual
375 mass^{1.0})/ha is equivalent to biomass density (kg/ha). Although we employed an allometric scaling
376 coefficient of 0.73 in our model (based on metabolic data from brook trout), the “true” allometric
377 scaling coefficient for eDNA production in our system was unknown. We used our data to
378 predict the optimal value for the scaling coefficient given the observed eDNA particle
379 concentration and biomass distribution data observed across our study lakes. To achieve this, we
380 iteratively generated ASM values from our data using scaling coefficients ranging from 0.00 to
381 1.00 (increasing by intervals of 0.01) and sequentially modelled eDNA particle concentration
382 data as a function of each ASM value. AIC values for each model were then used to evaluate
383 model fit. If eDNA production scales allometrically according to a power function, we predict
384 that the AIC values across models with scaling coefficients between 0.0 and 1.00 will exhibit an
385 approximately upward parabolic distribution with a minimum best-fit value that corresponds to
386 an “optimal” allometric scaling coefficient. According to the general rule described in (Burnham
387 & Anderson, 2002), models with AIC values within 2 units of the best-fit model AIC (e.g. Δ AIC
388 < 2) also exhibit substantial support; we predict that the ‘true’ allometric scaling coefficient for
389 brook trout eDNA production in nature will fall between the range of scaling coefficients that

390 produce models within 2 AIC of the ‘best-fit’ scaling coefficient, although future experiments
391 will be necessary to validate our predictions.

392 **Results**

393 *Population size estimates and density*

394 Population size estimates ranged from 145 to 3266 individuals, individual density ranged
395 from 63 to 1131 fish/ha, biomass density ranged from 12.6 to 52.5 kg/ha, and ASM ranged from
396 3707 to 18600 ASM/ha (Table 2, see Figure 1 for population size structure). Estimates of catch-
397 per-unit-effort (CPUE) did not exhibit a significant correlation with individual density ($F_{1,7} =$
398 0.53, $p = 0.491$, Figure S3).

399

400 *eDNA concentrations and correlations with density metrics among lakes*

401 Brook trout eDNA was successfully amplified from all samples in all lakes. No
402 amplification was observed in any negative controls or extraction blanks. The R^2 values for
403 standard curves ranged from 0.984 to 0.995, with an estimated efficiency ranging from 84.2 to
404 95.1%. Littoral and pelagic eDNA concentrations varied substantially by lake (Table 3). After
405 weighing for lake zone area, mean eDNA concentrations ranged from 592 copies/L in Cobb to
406 7805 copies/L in Olive.

407 Linear models for each density metric demonstrated positive and significant correlations
408 with eDNA particle concentration (Table 4, Figure 2). Individual density, biomass density, and
409 ASM accounted for 59%, 63%, and 78% of the variation in observed eDNA particle
410 concentration (adjusted R^2), respectively. AIC values indicated that individual density and
411 biomass density metrics provided roughly equivalent model fit; however, the ASM metric
412 provided substantially improved model fit relative to individual density and biomass density
413 (Δ AIC of 5.7 and 4.6, respectively). CPUE did not exhibit a significant correlation with eDNA
414 particle concentration (Table 4, Figure S4).

415 *Estimating density and biomass from predicted allometrically scaled mass: a case study for*
416 *population management*

417 The eDNA concentration of Hidden lake littoral and pelagic eDNA samples averaged
418 2653 and 342 copies/L, respectively, with a weighted mean average eDNA particle concentration
419 of 847 copies/L (Table 3). Based on a linear model using data from the nine study lakes, Hidden
420 lake had an estimated ASM/ha of 4279.6 (Figure 3). The predicted ASM estimate for Hidden
421 Lake was converted to traditional metrics of abundance (individual density and biomass density)
422 by bootstrap sampling allometrically scaled mass values (with replacement) from the Olive lake
423 size structure distribution (which was closest to the likely size structure of the Hidden lake
424 population) until the cumulative sum of all bootstrap sampled values equalled the predicted
425 ASM/ha from the linear model. After 1000 iterations, the mean number of individual mass
426 values sampled from the Olive size distribution was 278.4, which represents the individual
427 density (ind/ha) point-estimate for Hidden Lake; this corresponds to a total population size
428 estimate of 3286 individuals. This point estimate was similar to the 2018 pre-rotenone population
429 size estimate from Parks Canada of 3300-5000 individuals (Stitt, B, 2018), given the use of the
430 slightly larger Olive size distribution during the bootstrap procedure. Predicted total biomass was
431 143.0 kg, with a biomass density of 12.1 kg/ha. Notably, point estimates of biomass density rank
432 Hidden lower than all nine study lakes, likely as a result of previous fish removal efforts between
433 2011 and 2017 in Hidden Lake. Upper 95% prediction intervals for population size, total
434 biomass, density, and biomass were 7629 individuals, 332.0 kg, 646.5 fish/ha, and 28.1 kg/ha,
435 respectively. Due to the overall low concentration of eDNA present in the lake lower 95%
436 prediction intervals overlapped with zero for all four parameters.

437

438 *Predicting the allometric scaling coefficient for eDNA production in brook trout*

439 Based on model AIC values, a scaling coefficient of 0.72 best explained patterns of
440 eDNA particle concentration across the nine study lakes; models with scaling coefficients
441 between 0.47 and 0.89 generated Δ AIC values < 2 (Figure 4).

442 **Discussion**

443 Our study provides strong support for the hypothesis that eDNA production scales non-
444 linearly with mass according to a power function. Incorporating allometric scaling coefficients to
445 account for the distribution of biomass across individuals substantially improved predictive
446 models, indicating that the distribution of biomass across individuals within a population may
447 have an important effect when scaling individual eDNA production rates to the population-level.
448 Incorporating metabolic scaling coefficients for mass into models of eDNA particle
449 concentration and organismal abundance may therefore be particularly important in species that
450 exhibit substantial inter-population variation in size distributions. Our findings contribute to a
451 broader understanding of the ecology of eDNA production and have important implications for
452 many eDNA applications. While the focus of this study was on the relationship between eDNA
453 particle concentration and abundance using qPCR techniques, allometry in species with variable
454 size structure could, for example, partially account for the variation observed in species-specific
455 read number across environments in metabarcoding studies.

456 This study also reaffirms previous findings that metrics of population abundance
457 correlate with species-specific eDNA particle concentration in natural environments (Klobucar,
458 Rodgers, & Budy, 2017; Nevers et al., 2018; Pilliod et al., 2013; Schmelzle & Kinziger, 2016;
459 Thomsen et al., 2012). Previous research has demonstrated a moderate correlation between
460 density and/or biomass and eDNA particle concentration in lotic systems for brook trout
461 (Baldigo, Sporn, George, & Ball, 2017; Wilcox et al., 2016). We found similar relationships
462 within lentic systems, but also demonstrate that they can be considerably improved by
463 integrating allometric scaling coefficients into estimates of organismal abundance.

464 Notably, the correlation coefficients we observed between eDNA concentration and all
465 three metrics of abundance were greater than most previous studies conducted in nature (Yates et
466 al., 2019). The relatively strong correlations we observed between our abundance metrics and
467 eDNA concentration could also be due to the methodology with which we assessed population
468 size. Our estimates of population size were obtained using mark-recapture studies and unbiased
469 measures of size-structuring, which provided precise and standardized estimates of individual
470 density, biomass density, and ASM. However, such estimates are rare in published
471 eDNA/abundance studies; conducting mark-recapture studies to estimate population size are time
472 consuming and require a substantial commitment of labour and resources. To date only a handful
473 of eDNA studies in nature have specifically enumerated population size (Klobucar et al., 2017;
474 Levi et al., 2019; Tillotson et al., 2018) rather than proxies for abundance, such as CPUE (Yates
475 et al., 2019). CPUE may be appropriate if it exhibits a strong correlation with abundance, but in
476 some systems CPUE can perform poorly as a proxy for abundance (Hubert et al., 2012; Rose &
477 Kulka, 1999). In our study systems CPUE did not exhibit a significant correlation with individual
478 density and, as a result, eDNA concentration. Some of the substantial unexplained variation in
479 nature between eDNA concentration and abundance observed in other systems could result from
480 reliance on CPUE as a ‘proxy’ for abundance, although we acknowledge that for many species it
481 may often be impractical or impossible to directly estimate population size.

482 It is important to note, however, that our abundance estimates may miss a small fraction
483 of the adult population and do not account for juvenile (age 0+) abundance because fish were not
484 included in the mark-recapture study until they were at least 80mm (to avoid excessive tagging
485 mortality). Population size estimates therefore represent underestimates of true population census
486 size. Discrepancies in juvenile abundance/density across lakes could account for some of the

487 remaining unexplained variation present in our model, particularly since smaller fish would be
488 expected to exhibit higher mass-specific eDNA production rates. Similarly, temperature is
489 known to have a strong effect on metabolic rates (Brown et al., 2004) and eDNA production (Jo
490 et al., 2019). Notably, Temple lake exhibited a substantially lower concentration of eDNA than
491 expected from its ASM estimate; at 3.5 °C, Temple lake was also substantially colder than the
492 other eight study lakes during eDNA sampling (8.9-17.2 °C). Although we lacked the replication
493 to do so, integrating other important environmental variables (e.g. temperature, pH, etc.) into
494 models of eDNA particle concentration across environments could further improve predictive
495 models.

496 Despite these caveats, we demonstrate that it is possible to predict estimates of abundance
497 with eDNA samples and population size structure data in similar ecosystems that lack abundance
498 data. The population size point estimate for Hidden Lake from our ASM/eDNA model (and
499 based on the Olive “proxy” size distribution) was similar to the pre-rotenone population size
500 based on Parks Canada estimates. Although predicted density metrics for Hidden lake exhibited
501 wide upper 95% prediction intervals, they still provided enough information to facilitate relative
502 comparisons to the nine study lakes; we can predict with some certainty, for example, that
503 Hidden Lake had a lower biomass density relative to two of the nine study lakes (Dog and
504 Olive). Furthermore, 95% prediction intervals represent a relatively stringent criteria of certainty;
505 75% or 80% prediction intervals might still represent “good enough” information to help guide
506 managerial or research decisions.

507 Most significantly, our results highlight the need for further empirical studies exploring
508 and validating allometric scaling via power functions as a framework for modelling eDNA
509 particle production rates. While we demonstrate that incorporating allometric scaling coefficients

510 substantially improves models predicting abundance and eDNA concentration at the population
511 level, we have not directly quantified how eDNA production scales allometrically in brook trout
512 at the level of individual organisms. Nevertheless, recent experiments demonstrate that mass-
513 specific eDNA production rates tend to decline as individual mass increases (Maruyama et al.,
514 2014; Mizumoto et al., 2017; Takeuchi et al., 2019). We found that a scaling coefficient of 0.72
515 best described patterns of eDNA concentration for our study species across our nine study lakes;
516 this value closely aligned with the metabolic scaling coefficient for brook trout from (Hartman &
517 Cox, 2008). Scaling coefficients between 0.51 and 0.87 produced models with ΔAIC values < 2 ;
518 we therefore predict that the ‘true’ allometric scaling coefficient for eDNA production in brook
519 trout will likely fall within this interval. To validate our findings and test our subsequent
520 predictions, further experiments to quantify allometric scaling of eDNA production at the
521 individual level in brook trout are necessary.

522 As a well-supported general theory in ecology, experimental designs developed to test
523 MTE hypotheses (e.g. (Allegier et al., 2015; Hartman & Cox, 2008)) can inform future
524 experiments examining the effect of allometry on eDNA production rates. Notably, previous
525 experiments investigating allometric scaling in excretion or metabolic rates quantified rates at the
526 level of *individual* organisms (Allegier et al., 2015; Hartman & Cox, 2008; Vanni & McIntyre,
527 2016). Previous laboratory experiments quantifying the effect of biomass on eDNA
528 production/shedding rates typically pooled organisms to create different biomass treatments
529 (Doi, Uchii, Takahara, & Matsuhashi, 2015; Klymus et al., 2015; Lacoursière-Roussel, Rosabal,
530 & Bernatchez, 2016; Mizumoto et al., 2017; Takahara et al., 2012). At best, such experiments
531 pool organisms from similar size-classes, in which case eDNA production/abundance
532 relationships across ‘treatments’ only reflect changes in abundance within a specific age- or size-

533 class. Such experimental designs are likely to produce a strong relationship between eDNA
534 concentration and biomass, as has been found in a meta-analytic review (Yates et al., 2019).
535 While such studies were necessary to empirically quantify a preliminary correlation between
536 eDNA particle concentration and metrics of abundance, they might obscure critical differences in
537 mass-specific eDNA production rates across size classes that could have important consequences
538 for population-level rates. Natural populations often exhibit substantial variation in the
539 distribution of body size across individuals; the failure to account for allometric scaling in the
540 relationship between biomass and eDNA production might partially explain the failure to
541 translate the strong relationships observed in laboratory experiments to nature (Sebens, 1987).
542 Notably, our eDNA/abundance models utilizing ASM exhibited correlation coefficients
543 comparable to those typically observed in laboratory environments (Yates et al., 2019).

544 It may be possible to investigate allometry in eDNA production by pooling individuals
545 that are the same size within replicates. However, we would advise against this because
546 behavioural interactions between fish at high density in confined spaces may impact eDNA
547 production; some studies have demonstrated that eDNA production per fish increases at high
548 densities (Id et al., 2019). Brook trout, for example, are known to exhibit aggressive behaviour
549 towards conspecifics (McNicol, Scherer, & Murkin, 1985), which could increase eDNA particle
550 concentration at high densities due to increased activity and/or injuries inflicted upon each other.
551 If size classes exhibit different behaviour at high densities, this could further affect estimates of
552 allometric scaling. Future studies examining allometric scaling in eDNA production should
553 therefore incorporate individuals from a gradient of age/size classes and quantify organismal
554 eDNA production at the *individual*-level, as in (Takeuchi et al., 2019). Notably, the two studies
555 to examine eDNA production rates at an individual level across age/size classes found that

556 larger, older individuals exhibited lower mass-specific eDNA production rates (Maruyama et al.,
557 2014; Takeuchi et al., 2019). There is also a critical need to conduct such experiments *in situ* at
558 field study sites on wild organisms, as in (Pilliod, Goldberg, Arkle, & Waits, 2014). Laboratory
559 experiments, while important from a validation perspective, may not reflect natural excretion
560 processes because study organisms are housed in artificial conditions, fed artificial diets, and are
561 often subject to fasting regimes (Vanni & McIntyre, 2016). Furthermore, size-scaling
562 coefficients for metabolic processes such as nutrient excretion exhibit substantial interspecific
563 variation and can even include values greater than 1 (Allegier et al., 2015; Vanni & McIntyre,
564 2016). Allometric scaling in eDNA production may therefore exhibit similar variability across
565 species and should be investigated on a case-by-case basis.

566

567 *Conclusions*

568 Our results provide evidence supporting the hypothesis that eDNA production scales
569 allometrically with organism mass and can be modelled according to the power function:

$$570 \quad I = I_0 * M^b$$

571 We have demonstrated that the incorporation of additional (but straightforward to collect) size
572 structure data to integrate key allometric scaling predications resulted in substantial improvement
573 in models of eDNA concentration across environments. Future studies on eDNA/abundance
574 relationships in nature should consider incorporating allometry, particularly when study species
575 exhibit substantial inter-population variation in size distributions. However, there is also a need
576 to validate this hypothesis in controlled experimental contexts at the level of individual
577 organisms. As a well-developed ecological theory validated by numerous empirical studies
578 (Vanni & McIntyre, 2016), the literature on the MTE represents a robust methodological

579 foundation that future studies can utilize to explore relationships between a variety of
580 environmental and ecological factors that might influence organismal production of eDNA. Such
581 studies could further improve predictive models estimating abundance from eDNA particle
582 concentration to the extent that, in some circumstances, species-specific eDNA particle
583 concentration might be a reliable ecological indicator of abundance.

584 Predictive models would need to be calibrated on a system- and species-specific basis.
585 The extent to which models for a particular species can be extended to different ecosystems or
586 geographical regions also remains unknown. Future studies employing the methodology
587 developed herein will likely need to construct models from population size/abundance estimates
588 combined with standardized size distribution data on an individual species/system basis. These
589 studies will also need to collect size distribution data, in addition to eDNA samples, to predict
590 the density or biomass of organisms in similar ecosystems that lack abundance data. Direct
591 estimates of allometric scaling coefficients for study species would also likely improve
592 predictive models, although metabolic or excretory allometric scaling coefficients estimated in
593 other empirical studies on the same (or closely related) species may represent useful starting
594 points. In the absence of any other empirical data, the general scaling coefficient predicted by the
595 MTE (0.75) may also suffice.

596 Depending on the species studied, obtaining robust population size estimates and
597 individual size distribution data to calibrate initial models can often be difficult, labour intensive,
598 and come with a substantial monetary cost. However, the benefits might be substantial – the idea
599 that future researchers or managers might be able to obtain reasonable estimates of abundance
600 from eight water samples and a small number of gill net sets is, from an ecologist's perspective,
601 exhilarating.

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800 **Data Accessibility Statement:**

801 eDNA particle concentration data for each lake will be deposited in the Dryad Digital Repository
802 upon acceptance.

803 **Author contributions**

804 MCY collected eDNA samples and analyzed eDNA data. DG collected and analyzed mark-
805 recapture and size structure data. Statistical analyses were conducted by MCY. MCY wrote the
806 first draft of the manuscript, and all authors contributed substantially to subsequent drafts.

807 **Tables**

808 Table 1: Size structure gill net effort and fyking (mark-recapture) effort. SS refers to size
809 structure assessment, percent SS refers to the proportion of population harvested during size
810 structure assessment.

811

Site	SS Samples	Percent SS	SS CPUE	Mark/Recapture days	Total Marks Applied
Cobb	104	0.72	7	20	24
Mud	84	0.10	42	20	364
Olive	160	0.09	53	21	307
Ross	128	0.09	64	19	571
Temple	165	0.10	41	25	409
Dog	187	0.06	94	30	617
Helen	41	0.07	41	12	172
Margaret	171	0.08	43	23	414
McNair	27	0.13	27	14	118

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813

814 Table 2: Density metric estimates for each population. N = population size, ASM =
815 allometrically scaled mass. 95% confidence intervals for 'N' are given in brackets.
816

Site	N	Ha	Mean Ind. Mass (g)	Fish/ha	Kg/ha	ASM/ha	eDNA (copies/L)
Cobb	145 (94, 237)	2.3	404.8	63	25.7	5663	592.2
Dog	3266 (2715, 4097)	11.5	184.8	284	52.5	13962	5131.1
Helen	557 (420, 755)	2.5	83.9	225	18.8	6187	2445.9
Margaret	2017 (1638, 2623)	18.0	112.3	112	12.6	3707	1240.4
McNair	201 (158, 276)	1.7	137.3	121	16.6	4736	3050.5
Mud	860 (733, 1040)	7.2	141.9	119	17.0	4587	1138.7
Olive	1877 (1459, 2628)	1.7	43.1	1131	48.8	18601	7805.1
Ross	1392 (1211, 1635)	6.6	82.5	211	17.4	5559	917.4
Temple	1655 (1369, 2090)	3.3	51.1	509	26.1	9587	2076.5

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Table 3: Lake zone area and corresponding eDNA concentrations.

Site	Pelagic area (ha)	Littoral area (ha)	Pelagic eDNA (copies/L)	Littoral eDNA (Copies/L)	Weighted Mean eDNA (Copies/L)
Cobb	1.0	1.3	253.8	854.6	592.2
Dog	8.5	3.1	3447.1	9796.7	5131.1
Helen	1.2	1.3	1342.4	3514.4	2445.9
Margaret	14.4	3.6	791.9	3034.1	1240.4
McNair	0.7	1.0	2395.4	3505.0	3050.5
Mud	4.7	2.6	621.3	2280.1	1138.7
Olive	0.5	1.2	8084.6	7684.7	7805.1
Ross	4.6	2.0	790.5	1209.8	917.4
Temple	1.6	1.7	1940.8	2200.2	2076.5
Hidden	11.8	2.6	342.0	2652.9	847.2

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821

822 Table 4: Model results evaluating the relationship between eDNA particle concentration and
823 density (fish/ha), biomass (kg/ha), allometrically scaled mass (ASM/ha), and CPUE.
824

Model	F-value	P-value	Adj. R ²	Log Likelihood	AIC	ΔAIC
Density	12.37 _(1,7)	0.010	0.59	-77.78	161.6	5.7
Biomass	14.76 _(1,7)	0.006	0.63	-77.26	160.5	4.6
ASM	29.4 _(1,7)	0.001	0.78	-74.95	155.9	-
CPUE	1.92 _(1,7)	0.208	0.10	-81.27	168.5	12.6

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826

827 **Figure Captions**

828

829 Figure 1: Lake size structure distributions (g) obtained from standardized gill net sets for the nine
830 study lakes.

831

832 Figure 2: Correlation between weighted mean lake brook trout eDNA particle concentration and
833 three metrics of abundance in the nine study lakes: (a) individual density (individuals/ha, $R^2 =$
834 0.59), (b) biomass density (kg/ha, $R^2 = 0.63$), and (c) allometrically scaled mass (ASM/ha, $R^2 =$
835 0.78) ($n = 9$).

836

837 Figure 3: Predicting allometrically scaled mass (ASM/ha) for Hidden Lake based on eDNA
838 particle concentration. Black dots represent values for the nine study lakes, gray circle represents
839 the ASM/ha point estimate for Hidden Lake. Error bars represent 95% prediction intervals ($n =$
840 9).

841

842 Figure 4: AIC values for models correlating brook trout eDNA and allometrically scaled mass
843 (ASM), utilizing allometric scaling coefficients ranging from 0.00 (corresponding to individual
844 density) to 1.0 (corresponding to biomass density). Horizontal black bars and dotted lines denote
845 range of models with $\Delta AIC < 2$ relative to the 'optimal' scaling coefficient (0.72).

846

847 Figure S1: Map of the nine study lakes located in Alberta and British Columbia, Canada.

848

849 Figure S2: Timing of sampling activities in 2018.

850

851 Figure S3: Relationship between catch-per-unit-effort (CPUE) of a large and small gill net and
852 individual density (fish/ha) for the nine study lakes (adjusted $R^2 < 0$) ($n = 9$).

853

854 Figure S4: Relationship between brook trout eDNA particle concentration and catch-per-unit-
855 effort (CPUE) of a large and small gill net for the nine study lakes ($R^2 = 0.10$).







