Eco-evolutionary dynamics of prior selfing rate promotes the coexistence without niche partitioning under reproductive interference.

Running head: coexistence promoted by the evolution of selfing

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Abstract

1. When the two or more plants species share the same pollinators, pollinator-mediated reproductive interference make coexistence difficult. Recent studies suggested prior autonomous selfing mitigate reproductive interference, could enabling coexistence without pollination niche partitioning (pre-emptive selfing hypothesis). However, there are no studies to test whether evolution of prior selfing promote the coexistence, considering eco-evolutionary dynamics of population size, selfing rate and inbreeding depression.

2. To examine conditions that the evolution of prior selfing promote coexistence under mutual reproductive interference especially in the point of view for pollinator availability and dynamics of inbreeding depression, we constructed individual-based model in which two plant species compete against each other in the form of mutual reproductive interference and can evolve prior autonomous selfing rate. We expected that purging of deleterious mutations could cause evolutionary rescue because inferior species could rescue population density through the evolution of prior selfing if the strength of inbreeding depression decreases with an increase of population’s selfing rate.

3. Our simulation demonstrated that the evolution of prior selfing could promote the coexistence while reproductive interference caused competitive exclusion without evolution. We found that lower pollinator availability tended to prefer rapid evolutionary shift to higher prior selfing rate, it neutralizes the negative effect of reproductive interference, and population dynamics exhibit neutral random walk in both species. When the strength of inbreeding depression decreased with an increase in population’s selfing rate, moderate pollinator availability resulted in long-term coexistence in which relative-abundance-dependent selection on the prior selfing rate
rescue population density of inferior species intermittently.

4. Synthesis. We showed that the evolution of prior selfing could increase population growth rate of inferior species and consequently enable the long-term coexistence with evolutionary rescue. This is the new mechanisms explaining co-evolutionary coexistence of closely related plant species without niche partitioning and consistent with recent studies reported that closely related mixed-mating species are sympatrically growing even under the mutual reproductive interference.

Key-words: co-evolution, evolutionary rescue, inbreeding depression, individual based model, mixed mating, pollinator-mediated competition, selfing syndrome

Introduction

Clarifying the conditions under which competing species can coexist is a traditional and most fundamental subject in ecology (May, 1974; Chesson, 2000). Numerous empirical and theoretical works have shown that niche partitioning between competing species is required for their coexistence: i.e. the intraspecific competition should be larger than interspecific competition (Chesson, 2000; Silvertown, 2004). Closely related species, which potentially share the same or very similar resources and reproductive habits, are therefore expected to heavily compete against each other, likely being unable to coexist (Gröning & Hochkirch, 2008; Burns & Straus, 2011; Whitton, Sears & Maddison; 2017).

In flowering plants, when two or more plant species depend on the same pollinators for reproduction, interspecific pollinator-mediated pollen transfer can cause
strong reproductive interference that results in competitive exclusion of either species or niche partitioning between species (Levin & Anderson, 1970; Takakura, Nishida, Matsumoto & Nishida, 2008; Runquist & Stanton, 2013; Moreira-Hernández & Muchhala, 2019). Reproductive interference via interspecific pollen transfer can occur when both or either of increase in heterospecific pollen deposition on the stigma and conspecific pollen loss on heterospecific flower (Mitchell, Flanagan, Brown, Waser & Karron, 2009; Morales & Traveset, 2008). Specifically, Pollen deposition from closely related heterospecies is known to strongly decrease female reproductive success owing to pollen tube growth competition in the style, ovule discounting and/or hybridization (Harder, Cruzan & Thomson, 1993; Nishida, Kanaoka, Hashimoto, Takakura & Nishida, 2014; Whitton et al., 2017). Thus, reproductive interference via heterospecific pollen deposition may favour spatiotemporal segregation in flowering or floral trait displacement, with a consequence that they use different, or different body parts of the same, pollinator species (e.g. Runquist 2012; van der Niet & Johnson 2012; Huang & Shi, 2013).

Selfing has gathered much recent attention as an alternative mechanism that can mitigate reproductive interference by heterospecific pollen transfer from competing relatives (Fishman & Wyatt, 1999; de Waal, Anderson & Ellis, 2015; Katsuhara & Ushimaru, 2019). Recent studies have suggested that selfing constitutes a reproductive barrier among sympatrically coexisting related species (Fishman & Wyatt, 1999; Martin & Willis, 2007; Goodwillie & Ness 2013; Brys, van Cauwenberghe & Jaquemyn, 2016). Selfers with small and inconspicuous flower (selfing syndrome) which therefore receives fewer pollinator visits are likely to coexist with outcrossing relatives (Sicard & Lenhard, 2011; Kalisz et al., 2012). Thus, reduced heterospecific pollen deposition
owing to fewer visits and/or reproductive assurance via self-pollination might mitigate
the negative effect of reproductive interference in selfers, although it is difficult to
clarify their relative importance in general (Fishman & Wyatt, 1999; Martin & Willis,
2007; de Waal et al., 2015; Brys et al., 2016).

Recent studies further hypothesize that “prior” rather than “delayed”
autonomous selfing can mitigate the negative effect of reproductive interference via
interspecific pollen transfer and promote species coexistence independent of the
presence of pollinator visitations (the pre-emptive selfing hypothesis; Randle, Spigler &
Kalisz, 2018; Katsuhara & Ushimaru, 2019). Theoretical and empirical studies have
suggested that prior selfing unlikely evolves with frequent pollinator visitations (Lloyd,
1992; Kalisz, Vogler & Hanley, 2004; Eckert et al., 2010). However, in the presence of
reproductive interference by an abundant competitor species, frequent pollinator
visitations largely reduce outcrossing success of an inferior species. In such a situation,
the evolution of prior selfing can mitigate the negative effect of reproductive
interference from the competitor and would rescue the inferior species from competitive
exclusion.

The pre-emptive selfing hypothesis should be tested in the context of eco-
evolutionary dynamics of population size, selfing rate and inbreeding depression.
Because the negative effect of reproductive interference that decreases outcrossing
success becomes greater with an increase in the relative abundance of competing
species (Levin & Anderson, 1970; Katsuhara & Ushimaru, 2019), population dynamics
of mutually competing species should be an important driving factor of the evolution of
prior autonomous selfing of a given species. The evolution of prior selfing could rescue
the population density of competitively inferior species via mitigation of reproductive
interference while it could also result in self-extinction due to the negative effect of inbreeding depression on population growth rate depends on the strength of inbreeding depression (Cheptou, 2019; Katsuhara & Ushimaru, 2019). Therefore, dynamics of inbreeding depression is an important factor influencing the evolution of selfing because the strength of inbreeding depression is often expressed as a decreasing function of population’s selfing rate due to “purging” of deleterious, recessive alleles (Schemske & Lande, 1985; Chaelesworth, Chaelesworth & Morgan, 1990; Lloyd, 1992; Husband & Schemske, 1996; Crnokrak & Barrett, 2002; Goodwillie, Kalisz & Eckert, 2005; Charlesworth & Willis, 2009). Thus, dynamics of population size, the degree of selfing rate and inbreeding depression of competing species are ideally considered to examine the adaptive significance of prior selfing under reproductive interferences. To the best of our knowledge, however, no studies have examined the eco-evolutionary dynamics of these variables, and therefore little is known about the possibility of coexistence under reproductive interference, followed by evolution of prior selfing.

In this study, to examine the pre-emptive selfing hypothesis, we constructed a model in which two plant species sharing the same pollination niche and can evolve prior autonomous selfing compete against each other in the form of mutual reproductive interference (i.e. eco-evolutionary dynamic model). Using the model, we addressed following questions. Can prior selfing evolve under mutual reproductive interference and promote their coexistence as an evolutionary rescue agent? Is inbreeding depression an important determinant for the joint dynamics of population size and selfing rate? By answering to these questions, we discuss the conditions in which the evolution of prior selfing promotes the long-term coexistence of closely related species sharing the same pollination niche.
Model

Community structure, pollination, seed production and germination processes

We develop an individual-based model of competition between two annual flowering plant species (species with discrete generation) within a site whose carrying capacity is \( K \): \( K \) individuals of both or either of species 1 (sp\(_1\)) and 2 (sp\(_2\)) lives in the site for each generation (default \( K \) value is 2,000). Here, the relative abundance of sp\(_i\) at the \( t \)-th generation are denoted as \( q_{i,t} \) where \( i \) is either 1 or 2 and \( q_{1,t} + q_{2,t} = 1 \) holds. Thus, the number of individuals of sp\(_i\) equals \( K q_{i,t} \). In the model, we assume that ecological niches of sp\(_1\) and sp\(_2\) completely overlap with each other, although the two species produce no hybrids.

First, we describe the pollination and fertilization processes in the model. Each individual of both species produces \( n \) ovules which are fertilized via prior autonomous selfing and outcrossing mediated by pollinators and \( g \) pollen grains. The \( j \)-th individual of sp\(_i\) fertilizes their ovules via prior autonomous selfing at the rate of \( r_{i,j,t} \) in the \( t \)-th generation (\( 1 \leq j \leq Kq_{i,t} \) for \( i = 1 \) or 2). Thus, an integral number of ovules obtained by rounding \( nr_{i,j,t} \) are fertilized via prior selfing and the others were remained for pollinator-mediated outcrossing. Here, we assumed that an integral number obtained by rounding proportion \( P (0 \leq P \leq 1) \) of the \( n(1 - r_{i,j,t}) \) ovules are pollinated with outcrossed conspecific and/or heterospecific pollen grains by pollinators. Using \( P < 1 \), we can formulate pollinator limitation. Here, we assume that pollinators indiscriminately visit flowers of both species and carried their pollen in proportion to their relative flower abundances.
Pollen parent of each outcrossed ovule of individual \( j \) is randomly assigned to conspecific with the probability of
\[
\frac{\sum_{j=1}^{K} q_{i,j,t} g(1-r_{i,j,t})}{\sum_{j=1}^{K} q_{i,j,t} g(1-r_{i,j,t}) + c_h \sum_{j=1}^{K} (1-q_{i,j,t})^K g(1-r_{h,j,t})},
\]
where \( c_h, r_{i,j,t} \) and \( r_{h,j,t} \) (\( 0 \leq c_h, q_{i,j,t}, r_{i,j,t} \) and \( r_{h,j,t} \leq 1 \)) are the strength of reproductive interference from heterospecies (sp\(_ h \)) and the rates of prior selfing of the \( j \)-th individuals of sp\(_ i \) and sp\(_ h \), respectively. The parameter \( c_h \) is interpreted as the competitive ability of a heterospecific pollen grain relative to that of a conspecific one to get fertilization with individual \( j \)'s ovule. Besides, the probabilities of which pollen grains of individual \( j \) fertilize conspecific and heterospecific ovules are described as
\[
\frac{g(1-r_{i,j,t})}{\sum_{j=1}^{K} q_{i,j,t} g(1-r_{i,j,t}) + c_h \sum_{j=1}^{K} (1-q_{i,j,t})^K g(1-r_{h,j,t})}
\text{ and }
\frac{c_h g(1-r_{i,j,t})}{c_h \sum_{j=1}^{K} q_{i,j,t} g(1-r_{i,j,t}) + \sum_{j=1}^{K} (1-q_{i,j,t})^K g(1-r_{h,j,t})},
\]
respectively. In this formulation, we assume that outcross pollen proportionally decreases with the prior selfing rate in respective individuals of both species. This assumption mimics increased pollen discounting and/or anther-stigma interference with increasing the prior selfing rate (Lloyd and Webb, 1986; Webb and Lloyd, 1986; Karron, Jackson, Thumser & Schlicht 1997; Fishman, 2000; Barrett 2002). Because we assumed random pollination, it should be noted the ovule of \( j \)-th individual is fertilized by pollen of \( j \)-th individual (pollinator-mediated self-pollination; geitonogamy) with the above probability and they are treated as self-fertilized pollen as well as the ovules fertilized by prior autonomous selfing.

Second, we denote the seed production process. We assume that only ovules fertilized by self- and outcrossed-conspecific pollen can develop seeds whereas those fertilized by heterospecific pollen produce no seeds. A cost of selfing relative to outcrossing is also assumed as follows. In sp\(_ i \), all outcrossed ovules develop sound seeds whereas selfed ovules set seeds at the rate of \( 1 - I_{i,t} \), where \( I_{i,t} \) (\( 0 \leq I_{i,t} \leq 1 \)) is the
strength of inbreeding depression at generation \( t \) in sp\(_i\). Here, \( I_{i,t} \) is described as a function of the population’s selfing rate at the \((t - 1)\)th generation of sp\(_i\), \( S_{i,t-1} \):

\[
I_{i,t} = \beta e^{-\alpha S_{i,t-1}}.
\]

\( S_{i,t-1} \) is calculated as total number of selfed sound seeds divided by total number of sound seeds in sp\(_i\) in the last generation. \( I_{i,t} \) can be interpreted as an evolutionary variable, which decreases with an increase in the population’s selfing rate in the parental generation owing to the accumulation–purging balance of deleterious mutations (Schemske & Lande, 1985; Husband & Schemske, 1996; Crnokrak & Barrett, 2002).

The coefficient \( \alpha \) expresses how inbreeding depression steeply decreased with increasing the population’s selfing rate whereas the intercept \( \beta \) (\(0 \leq \beta \leq 1\)) indicates the level of inbreeding depression when complete outcrossing occurs in the population. We simulated various \( \alpha \) and \( \beta \) values to test various scenarios in the eco-evolutionary dynamics of population size and selfing rate.

As the final process, \( K \) seedlings from all seeds produced by both species are randomly selected and construct generation \( t + 1 \). We assume no interspecific differences in competitive ability at germination and establishment processes as well as other ecological and genetic features: \( c_h \), \( \alpha \), and \( \beta \) are also equal for both sp\(_1\) and sp\(_2\). In addition, our model has no spatial structure.

**Inheritance and mutation of the rate of prior autonomous selfing**

To describe the evolutionary dynamics of prior autonomous selfing, our model assumes that the prior selfing rate of individual \( j \) in the next generation \( r_{i,j,t+1} \) is determined as the parental average. Thus, the prior selfing rate is assumed to be a quantitative genetic trait value which can be influenced by various quantitative traits such as the degrees of
herkogamy and/or dichogamy and the proportion of cleistogamous flowers (Culley & Klooster, 2007; Kalisz et al., 2012). In addition, \( r_{i,j,t+1} \) can be mutated to be slightly lower or higher than the parental mean (a random value between \(-\sigma\) and \(+\sigma\) is added to the parental mean) with a probability \( \mu \). \( \mu \) and \( \sigma \) are the rate and effect size of mutation, respectively. We used 0.05 and 0.1 for \( \mu \) and \( \sigma \) as default values, respectively. If mutated \( r_{i,j,t+1} \) becomes larger than 1 or smaller than 0, we use the values 1 and 0, respectively.

**Simulation settings and categorization of eco-evolutionary consequence**

To explore conditions for the coexistence of the two species, we examined the effects of pollinator availability (\( P \)) and inbreeding depression-selfing rate relationship (\( \alpha \) and \( \beta \)) on the consequences of evolution. We tested two following scenarios for inbreeding depression-selfing rate relationship. \( I_{i,t} \) is fixed (\( \alpha = 0; \beta = 0.1, 0.3, 0.5, 0.7 \) or 0.9) or it varies in concert with the population’s selfing rate (\( \alpha = 0, 0.5, 1, 2, 4 \) or \( 8; \beta = 0.9 \)), with the whole parameter range of \( 0 \leq P \leq 1 \) (Table 1). In each simulation run, the initial numbers of individuals for both species are equal as \( K/2 \). The initial autonomous selfing rates for individuals were generated randomly with normal distribution whose mean and standard deviation are \( r_{\text{initial}} (1/2) \) and \( sd_{\text{initial}} (1/6) \) for both species. Each run continues for 2,000 generations or until either species goes extinct.

After 50 simulation runs for each parameter setting, we classified the eco-evolutionary dynamics into four categories based on ecological and evolutionary status of the species. When the simulation terminated by the extinction of either species and the population mean of prior autonomous selfing rate in survivors was higher or lower than 0.5, the result was categorized as (1) competitive exclusion by selfer or (2) that by outcrosser, respectively. Meanwhile, the runs in which the two species still coexisted at
the 2,000th generation were also divided into two categories, (3) a coexistence with evolutionary rescue by prior selfing and (4) a coexistence with neutral dynamics, based on following procedures.

To detect the evolutionary rescue, we calculated the population growth rate and selection gradient in each generation of sp. Population growth rate ($W_{i,t}$) for the $t$-th generation is calculated as $Kq_{i,t+1}/Kq_{i,t}$ ($= q_{i,t+1}/q_{i,t}$). For clarifying the selection gradient on the prior selfing rate, we identified seed and pollen parents of all seeds and calculate a correlation coefficient between selfing rate $r_{i,j,t}$ and seeding and siring success of each individual as the selection gradient ($G_{i,t}$) at the $t$-th generation. The positive (or negative) $G_{i,t}$ means that the higher (or lower) rate was adaptive at the generation in sp. Then, the evolutionary rescue by prior selfing is defined as a state following two conditions are satisfied simultaneously: (1) a significant negative correlation between $q_{i,t}$ and $G_{i,t}$ (i.e., a population decline facilitates the evolution of selfing), (2) a significant positive correlation between the population mean of prior selfing rate $\sum_{j=1}^{K} r_{i,j,t}/Kq_{i,t}$ and $W_{i,t}$ (i.e., the evolution of selfing increases population growth). Significances of these two correlations were examined by a permutation test. We permutated the variables of the last 500 generations in each run 10,000 times and made null distribution and the 95% prediction interval of each correlation to test the significance of the value of the run. When both or either of the correlation coefficients were not significant, the run was categorized into the coexistence with neutral dynamics (Fig. 1).

We compared difference in long-term stability between coexistences with neutral dynamics and evolutionary rescue. We selected a typical parameter set for each coexistence type: $P = 0.4$, $\alpha = 0.5$, $\beta = 0.9$ for that with evolutionary rescue (ER set) and
For coexistence with neutral dynamics (ND set). For each parameter set, we conducted 200 simulations for 10,000 generations and recorded the generation until which two species coexisted. We also checked how simulation results change depending on the strength of reproductive interference and the initial population’s mean selfing rate. We examined simulations in which $c_h$ (= 0.0, 0.25, 0.5, 0.75 or 1.0) and $r_{\text{initial}}$ (= 0.0, 0.25, 0.5, 0.75 or 1.0) varied with the above parameter settings (ER and ND sets) and run 50 simulations for each parameter set. Moreover, to check the population dynamics of the two species with the fixed population’s prior selfing rates, we conducted simulation runs in which $sp_1$ and $sp_2$ had the same or different fixed prior selfing rates ($0 \leq r_{\text{initial}} \leq 1$) with the same two parameter settings (ER and ND sets). Finally, we run simulations with the fixed abundance of two species to examine the effect of fixed population size on the evolution of prior selfing rate in the two parameter settings (ER and ND sets).

**Results**

*Eco-evolutionary dynamics with fixed inbreeding depression*

We found that lower pollinator availability preferred the evolution of higher selfing rate in both species, often promoting their coexistence with neutral dynamics (Fig. 2). Conditions for the coexistence with neutral dynamics was more limited by higher inbreeding depression (Fig. 2). The coexistences with neutral dynamics were always realized when the two species evolved the prior selfing rate close to 1.0, which neutralized their mutual reproductive interference (Fig. 1). During the coexistence, population dynamics of both species exhibited a random walk. Therefore, the coexistence with neutral dynamics is not stable in the long term and the extinction of
either species occurred when simulations continued for more generations (see the 
section below, Long-term stability of the coexistences). Meanwhile, when either or both 
of I and P are large, the eco-evolutionary dynamics tended to be terminated by 
competitive exclusion (Fig. 2). Especially when both of I and P are large, competitive 
exclusion by outcrosser always terminated the eco-evolutionary dynamics (Fig. 2). The 
coexistence with evolutionary rescue rarely occurred when the inbreeding depression 
was fixed and independent of the population’s selfing rate (Fig. 2).

Eco-evolutionary dynamics with variable inbreeding depression

In the scenarios with variable inbreeding depression, conditions for both types of 
coexistence were more relaxed compared to those assuming fixed inbreeding depression 
(Figs. 2, 3). Interestingly, conditions with intermediate levels of pollinator availability 
and the slope of inbreeding depression function $\alpha$ more frequently facilitated the 
coexistence with evolutionary rescue or neutral dynamics than other conditions (Fig. 3).

When inbreeding depression sharply decreases as the population’s selfing rate 
increases ($\alpha \geq 4.0$), competitive exclusion by selfer occurred in wider conditions as in 
those with lower fixed inbreeding depression ($\alpha = 0$ and $\beta = 0.1$ or 0.3; Figs. 2, 3).

Meanwhile, when inbreeding depression more gently decreased with increasing the 
population’s selfing rate ($\alpha = 0.5$), competitive exclusion by outcrosser tended to occur 
in the presence of higher pollinator availability like in the cases both of I and P are large 
in fixed inbreeding depression scenario.

Long-term stability of the coexistences with neutral dynamics and evolutionary rescue
The coexistence with evolutionary rescue continued until the 10,000-th generation if the fluctuations of the relative abundances \((q_i, t)\) and the prior selfing rates \((r_i, t)\) have once started, while the coexistence with neutral dynamics never coexisted before reaching the 10,000-th generation (Fig. 4).

**Dependence of simulation consequences on \(c_h\) and \(r_{\text{initial}}\)**

In the simulations with ER sets, we found that coexistence with evolutionary rescue nearly always occurred with high initial population’s selfing rate \((r_{\text{initial}} \geq 0.75)\) and presence of mutual reproductive interference \((c_h > 0.0)\). When the initial population’s selfing rate was low \((r_{\text{initial}} \leq 0.25)\), the both types of coexistence rarely or very infrequently occurred in both the ER and ND sets (Fig. 5). Moreover, no competitive exclusion by outcrosser was found when the initial population’s selfing rate was high \((r_{\text{initial}} \geq 0.75)\). Meanwhile, the strength of reproductive interference \((c_h)\) seems unlikely to largely influence the coexistence with neutral dynamics with the ND parameter setting. However, the coexistence of evolutionary rescue never occurred without mutual reproductive interference \((c_h = 0.0)\) with the ER set.

**Simulation consequences with fixed prior selfing rate and fixed population size**

We found that coexistence for 2,000 generations very rarely occurred when the prior selfing rates were fixed in the two species for the both parameter settings except when both species had the same and very high prior selfing rates (Fig. 6). Winners were always the species having higher prior selfing rates with the ND parameter set whereas winners were usually the species having the lower and higher prior selfing rates in the below and above areas of the line of \(r_2 = -r_1 + 0.6\), respectively, with the ER set (Fig. 6).
6). In the simulations with the fixed abundance of two species, the evolutionary shift to the higher prior selfing rate was favored only when the relative abundance of focal species was lower than 1/2 with the ER parameter set (Fig. 7). Meanwhile, under the ND set, very high prior selfing rate was always favored independent on their abundance (Fig. 7).

Discussion

Our model revealed that the evolution of prior selfing can promote the coexistence in the presence of mutual reproductive interference while the coexistence rarely occurred without the evolution of prior selfing (Figs. 2, 3, 6). In the variable inbreeding depression scenario (inbreeding depression decreases with an increase in the population’s selfing rate), both types of coexistence tended to be more occurred than in the fixed inbreeding depression scenario when comparing same pollinator availability (Figs. 2, 3). Especially when the strength of inbreeding depression gently decreased and pollinator availability was intermediate level, the coexistence with evolutionary rescue often occurred and stably continued for very long-term (Figs. 3, 4).

Firstly, we discuss the processes enabling the coexistence with evolutionary rescue in our model (Fig. 1). At the early generations, the stochastic process makes slight difference in population size and selfing rate between the two species and reproductive interference by more abundant species with higher selfing rate enlarge the difference. In such a situation, low outcross success due to increased heterospecific pollen deposition facilitates the evolution of high prior selfing rate in the inferior species. This evolutionary shift toward high selfing rate improves the population growth rate via an increase in selfed seed production (i.e., evolutionary rescue by prior selfing.
occurs) especially when inbreeding depression is weakened with increasing the population’s selfing rate in the inferior species. Meanwhile, once becoming the dominant species, reproductive interference from the competitor is getting weaker so that inbreeding depression favors lower prior selfing rate in the species. Lower prior selfing rate, in turn, can reduce total seed production of the population when pollinator availability is not high, leading to lower population growth rate compared to the competitor. This relative-abundance-dependent selection on the prior selfing rate promotes a negative relationship between and fluctuations of the prior selfing rate and population size through generations. Due to this out-of-phase fluctuations occurring both in two species, the long-term coexistence of the two species is realized under mutual reproductive interference.

Here, suitable conditions for the coexistence with evolutionary rescue are discussed by comparing to empirical knowledge. Our simulation demonstrated that the coexistence with evolutionary rescue occurred with moderate pollinator limitation, variable and moderate levels of inbreeding depression, the relatively higher initial prior selfing rate and the presence of reproductive interference. High pollinator availability always favors competitive exclusion by either outcrosser or selfers depending on the level of inbreeding depression. In other words, the long-term coexistence under the reproductive interference requires pollinator limited conditions which are prevailing in wild flowering plants (Larson & Barrett, 2000). Gently variable inbreeding depression still function as the cost of selfing even when the population’s selfing rate of given species is very high. While inbreeding depression due to deleterious recessive alleles are thought to be rapidly purged with increasing population’s selfing rate, weak late acting inbreeding depression caused by weakly deleterious mutations and heterozygous
advantage due to overdominance cannot be purged even in predominantly selfing species (Charlesworth et al., 1990; Husband & Schemske, 1996; Crnokrak & Barrett, 2002; Charlesworth & Wills, 2009). Additionally, although it may not be surprising, we found that higher initial prior selfing rate widens the possibility of the coexistence with evolutionary rescue (Fig. 5). The finding suggests that only a pair of predominantly selfing or of mixed-mating species can coexist stably under reproductive interference, being consistent with recent studies on the coexistence under mutual reproductive interference (Tokuda et al., 2015; Katsuhara & Ushimaru, 2019; Nishida et al. unpublished data). Without reproductive interference, this type of coexistence never occurred even when other parameter settings are suitable for the coexistence (Fig. 5).

This result is very interesting and proposes that mutual reproductive interference can act the cost of outcrossing and promoting more selfing (Katsuhara & Ushimaru, 2019), likely making a fluctuation pattern in the prior selfing rate throughout the generation.

The coexistence with neutral dynamics was often found in conditions with lower pollinator availability and weak fixed or moderately variable inbreeding depression (Figs. 2, 3). In such conditions, the higher prior selfing rate evolves very quickly to be almost completely 1.0 in both species (Fig. 1), which should be free from the negative effect of reproductive interference from competitor. Both species exhibit population dynamics of neutral random walk (Hubbell, 2001; Chave, 2004) and coexist, so that stochastic events will stop this type of coexistence at some point in time (Fig. 4). In our model, this type of coexistence was usually found in the parameter conditions where competitive exclusion by selfer frequently occurred, suggesting that these consequence categories do not differ qualitatively (Figs. 2, 3, 5). The rate of evolutionary change in prior selfing rate differed between these categories and the
coexistence occurred when the high prior selfing rate evolved more rapidly in both species (Fig. 1). Many predominately selfing weeds usually coexist in human-disturbed habitats where pollinators are often limited (Baker, 1974), most likely being explained by this type of coexistence. Empirical studies have shown the evolutionary shift to higher prior selfing rate (often via reduction of herkogamy) can rapidly occurred under pollinator limitation (Roels & Kelly, 2011; Brys & Jacquemyn, 2012; Gravasi & Schiestl, 2017; Cheptou, 2019). To apply our results to selfing-species coexistence in the field, the rate of evolutionary change of the prior selfing rate and pollinator availability are better to be examined in future studies.

Under conditions with high pollinator availability and strong inbreeding depression, mutual reproductive interference causes very rapid competitive exclusion by outcrosser, being consistent with expectations in the previous works that considered no limitation in outcross gamete transfer (Fig. 1, 2, 3; Levin & Anderson, 1970; Kishi & Nakazawa, 2013). Besides, competitive exclusion by selfer is frequently occurred under conditions with weak inbreeding depression and/or low pollinator availability. The exclusion occurred more slowly comparing to the exclusion by outcrosser (Fig. 1). The difference was likely due to that reproductive interference no more reduced seed production in highly selfing species.

In both types of coexistence, co-evolutionary shifts to extremely high prior selfing rate (over 0.9) was necessary in both competing species (Fig. 1). Many previous empirical studies, however, reported coexistences of an extremely selfer and a related outcrosser (Fishman & Wyatt, 1999; Brys et al., 2016; Randle et al., 2018). This difference between the field observations and our results might be explained by in two possible mechanisms which are not assumed in our model. First, some kinds of
ecological differences, such as competitive ability for germination and strength of inbreeding depression, might exist between the study species, promoting the coexistence of species with different mating systems. Second, selfers in these studies always exhibited reduced floral attractiveness which minimized the negative effect of reproductive interference via receiving few pollinator visits (Fishman & Wyatt, 1999; Brys et al., 2016; Randle et al., 2018). Meanwhile, our model assumed only the rate of prior selfing was evolvable as in the previous model (Cheptou, 2019). Such an evolution of selfing floral syndrome could enable obligatory selfers to coexist with outcrossing relatives. Some recent studies reported the mutual reproductive interference between two sympatrically growing mixed-mating species which have showy flowers with frequent pollinator visitations and traits promoting prior autonomous self-pollination (cleistogamous flowers in Impatiens noli-tangare and I. textori, Tokuda et al., 2015; bud pollination in Commleina communis and C. c. f. ciliata, Katsuhara & Ushimaru, 2019).

The coexistences found in these study systems could be explained by prior-selfing mediated evolutionary rescue, which are predicted by our model. To test this possibility, monitoring of eco-evolutionary dynamics of these competing species in the fields will be required. Although the complete test will require much time and effort, to examine the relationships among population’s selfing rate, inbreeding depression and relative abundance in the field should improve our understanding of co-evolutionary coexistence mechanisms without pollination niche partitioning as the first step.

In conclusion, our model successfully showed that the evolution of prior selfing could increase population growth rate of inferior species and consequently enable the long-term coexistence with evolutionary rescue. We successfully showed that evolutionarily variable inbreeding depression based on accumulation–purging balance...
of deleterious mutations expand the possibility of coexistence and promote the long-
term coexistence. The result suggests that genetic dynamics of inbreeding depression
within a given species may largely influence dynamics of community where pollinator-
mediated competition occurs. Finally, we propose new mechanisms explaining co-
evolutionary coexistence of closely related species under mutual without any kinds of
niche differentiation and spatial structures. The applicability and generality of the
proposed mechanisms should be investigated empirically in future.

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Reference


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**Table 1.** List of parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Definition</th>
<th>Default value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$r_{i,j,t}$</td>
<td>The ratio of ovules fertilized via prior autonomous selfing in the $j$-th individual of sp$_i$ at the $t$-th generation.</td>
<td>0-1</td>
</tr>
<tr>
<td>$q_{i,t}$</td>
<td>Relative abundance of sp$_i$ at the $t$-th generation</td>
<td>0-1</td>
</tr>
<tr>
<td>$P$</td>
<td>Pollinator availability</td>
<td>0-1</td>
</tr>
<tr>
<td>$c_h$</td>
<td>Strength of reproductive interference</td>
<td>1</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>Slope of inbreeding depression function</td>
<td>0, 0.5, 1, 2, 4, 8</td>
</tr>
<tr>
<td>$\beta$</td>
<td>Intercept of inbreeding depression function</td>
<td>0.1, 0.3, 0.5, 0.7, 0.9</td>
</tr>
<tr>
<td>$\mu$</td>
<td>Mutation rate</td>
<td>0.05</td>
</tr>
<tr>
<td>$\sigma$</td>
<td>Effect size of mutation</td>
<td>0.1</td>
</tr>
<tr>
<td>$K$</td>
<td>Carrying capacity (number of individual plant)</td>
<td>2000</td>
</tr>
<tr>
<td>$n$</td>
<td>Number of ovules per individual plant</td>
<td>200</td>
</tr>
<tr>
<td>$r_{\text{initial}}$</td>
<td>Mean of initial prior autonomous selfing rate</td>
<td>0.5</td>
</tr>
<tr>
<td>$sd_{\text{initial}}$</td>
<td>Standard deviation of initial prior autonomous selfing rate</td>
<td>1/6</td>
</tr>
</tbody>
</table>
Fig. 1. Examples of four consequences of eco-evolutionary dynamics in our simulations: (1) competitive exclusion by selfer; (2) competitive exclusion by outcrosser; (3) coexistence with evolutionary rescue; (4) coexistence with neutral dynamics. Upper and lower graphs of each category show relative abundance and population mean of prior selfing rate dynamics of sp₁ (black line) and sp₂ (grey line), respectively.
Fig. 2. Effects of pollinator availability and the strength of inbreeding depression on simulation consequence in fixed inbreeding depression scenarios. Each pie chart shows frequencies of four categories of eco-evolutionary consequences of 50 simulation runs (Fig. 1).
Fig. 3. Effects of pollinator availability and the strength of inbreeding depression on the simulation consequence in variable inbreeding depression scenarios. Each pie chart shows frequencies of four categories of eco-evolutionary consequences of 50 simulation runs (Fig. 1).
**Fig. 4.** Histograms of generation until when two species coexisted in two typical parameter sets for coexistences with evolutionary rescue (a, ER set) and with neutral dynamics (b, ND set), respectively. The graphs made from the outcomes of 200 simulation runs.
**Fig. 5.** Effects of strength of reproductive interference and initial population’s mean selfing rate in two typical parameter sets for coexistences with evolutionary rescue (a, ER set) and with neutral dynamics (b, ND set), respectively. Each pie chart shows frequencies of four categories of eco-evolutionary consequences of 50 simulation runs (Fig. 1).
**Fig. 6.** Ecological consequences with fixed population’s prior selfing rate in two typical parameter sets for coexistences with evolutionary rescue (a, ER set) and with neutral dynamics (b, ND set), respectively. X and Y axes indicate population’s mean prior selfing rate of sp\(_1\) and sp\(_2\), respectively. Blue and red areas mean that survivor is sp\(_1\) and sp\(_2\), respectively, and grey regions (shown upper right corner of each panel) indicated that coexistence continued for 2,000th generations.
Fig. 7. Evolutionary consequences with fixed relative abundance in two typical parameter sets for coexistence: with evolutionary rescue (a, ER set) and with neutral dynamics (b, ND set), respectively. Upper and lower graphs indicate the correlations between population’s mean prior selfing rate and selection gradient, and relative abundance of the focal species in last 500 of 2,000 generations, respectively.