# Unsupervised Neural Tracing in Densely Labeled Multispectral Brainbow Images

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## **Abstract**

Reconstructing neuron morphology is central to uncovering the complexity of the nervous system. That is because the morphology of a neuron essentially provides the physical constraints to its intrinsic electrophysiological properties and its connectivity. Recent advances in imaging technologies generated large quantities of high-resolution 3D images of neurons in the brain. Furthermore, the multispectral labeling technology, Brainbow permits unambiguous differentiation of neighboring neurons in a densely labeled brain, therefore enables for the first time the possibility of studying the connectivity between many neurons from a light microscopy image. However, lack of reliable automated neuron morphology reconstruction makes data analysis the bottleneck of extracting rich informatics in neuroscience. Supervoxelbased neuron segmentation methods have been proposed to solve this problem, however, the use of previous approaches has been impeded by the large numbers of errors which arise in the final segmentation. In this paper, we present a novel unsupervised approach to trace neurons from multispectral Brainbow images, which prevents segmentation errors and tracing continuity errors using two innovations. First, we formulate a Gaussian mixture model-based clustering strategy to improve the separation of segmented color channels that provides accurate skeletonization results for the following steps. Next, a skeleton graph approach is proposed to allow the identification and correction of discontinuities in the neuron tree topology. We find that these innovations allow our approach to outperform current state-of-the-art approaches, which results in more accurate neuron tracing as a tree representation close to human expert annotation.

# 1 Introduction

Brain circuits have long been known to arise from the physical connectivity patterns of many individual neurons (i.e., the "connectome"). It is valuable, therefore, for neuroscientists to describe the cable-like axon and dendrite morphologies to aid in the discovery of inputs and outputs of individual circuits and the roles of different cell types in these circuits (Zeng & Sanes, 2017). This presents a challenging paradigm for both data acquisition and analysis, as neural networks can encompass projection neurons spanning many centimeters and local connectivity features on the scale of hundreds of nanometers. These problems have begun to be addressed by ongoing technical innovations, however technical implementation details still require careful analysis.

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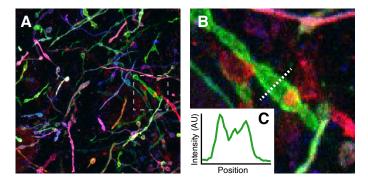


Figure 1: **A**, an example Brainbow image displaying the cable-like nature of axons and dendrites. **B**, a closeup of the box highlighted in **A**, displaying the hollow nature and noisy nature of Brainbow expression. **C**, a line intensity profile of the line in **B**. All images are 15-frame maximum intensity projections along the z-axis.

Recent advances in light microscopy and genetic strategies for labeling defined groups of neurons have enabled neuroscientists to capture these dense volumetric images of neurons in the brain. Specifically, multispectral volumetric imaging of neurons, termed "Brainbow" (Figure 1A), has emerged as a promising approach to produce densely labeled brain samples (Livet et al., 2007; Cai et al., 2013). Briefly, individual neurons in a Brainbow sample each stochastically express combinations of fluorescent proteins, effectively labeling each neuron a different composite color. This enables unambiguous identification of individual axons and dendrites within a given volume. The continued improvement of Brainbow-like tools (Li et al., 2020), together with the advent of improved imaging technologies such as expansion microscopy (Chen et al., 2015; Tillberg et al., 2016) and light-sheet microscopy (Hillman et al., 2019; Jahr et al., 2015), makes Brainbow well-poised to make significant contributions to both connectomics and hypothesis-driven circuit analysis.

Despite the technological advances for collecting these micrographs, approaches for reliably analyzing and quantifying these rich datasets remain in their infancy. Along with large data sizes (in some cases as much as several terabytes), this is a difficult problem due to a large number of channels and imaging noise which is observed in the images (Figure 1B-C). Many tools exist for the manual or semi-manual reconstruction of neuron structures, such as Neuromantic (Myatt et al., 2012), commercial software such as Neurolucida. Recently, nTracer (Roossien et al., 2019) was released, specifically built for the analysis of Brainbow images. While these tools are effective for the reconstruction of small neuronal volumes, they are difficult to apply at scale due to the reliance on human input to the annotation, which can encompass tens to hundreds of human hours for even a relatively small image. Several automated solutions to aspects of the neuron segmentation problem have been proposed for use in both optical and electron microscopy generated images (Li et al., 2019; Gornet et al., 2019; Januszewski et al., 2018; Yang et al., 2019; Quan et al., 2016; Xiao & Peng, 2013), including several which specifically focus on Brainbow (Shao et al., 2012; Bas & Erdogmus, 2010; Wu et al., 2011; Sümbül et al., 2016). The earlier methods directly operate in voxel-level, which can be extremely computation-intensive and error-prone due to insufficient color consistency. Though the computation and color inconsistency issues are addressed in Sümbül et al. (2016), we can observe that this method results in fragmented (broken) neurite segmentations (Figure 2D, red arrows). These fragmented segmentations can be caused by a flaw in the supervoxelization process or occlusions by other neurons in the raw Brainbow data. In addition, none of the segmentation methods provide a tree-like neural tracing structure, which is required for further neuroinformatics analysis.

In this work, We intend to adapt the computationally efficient supervoxel-based segmentation used in Sümbül et al. (2016) but to address its fragmented segmentation problem. Aware of that the problem may be caused by its kernel k-means or spectral clustering, which are theoretically equivalent and tend to find circular or even-sized clusters (Dhillon et al., 2004), we instead use a probabilistic Gaussian mixture model. This modification allows the modulation of the distribution of supervoxel-representation to form more robust clusters and thus reduces the segmentation errors. Next, we extract a neuron tree topology (tracing), represented as a graph connectivity network, by skeletonization of the GMM-clustered segmentation. To address breaks in the neuron tracing which arise, we implement a graph-based method which utilizes the spatial relationship of the segmentation skeleton to bridge broken links, producing a more reliable tracing result.

Using this novel approach, we compare our automatic tracing to human-generated tracing, finding a high degree of agreement. Additionally, we show that the proposed approach can deal with loss of

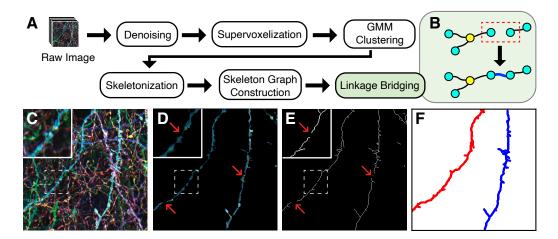


Figure 2: A, an overview of the data processing pipeline used in this paper. B, linkage bridging is used to repair broken trees, producing more robust neuron tracings. C, a raw Brainbow image. D, image C after GMM clustering is performed. E, image D after skeletonization is performed. E, the final reconstruction of the two neurites from E, pseudocolored for contrast. Arrows are used to identify places where there are erroneous breaks observed during skeletonization, which are corrected by linkage bridging. All images are maximum intensity projections of the entire image stack along the z-axis.

skeleton information and also more complicated neural structures within the input Brainbow images. In addition, whilst many hours can be spent for humans on reconstructing the neuroanatomy of such densely labeled multispectral Brainbow images, our proposed method can relieve the high demand for human annotation. This is a promising development, by which discovery of brain circuits can thus potentially be automated.

# 2 Methods

We first revisit the supervoxelization process, and then to solve the fragmentation problem, we make two innovations here: (i) To avoid biasing the segmentation being even-sized, we replace kernel k-means with Gaussian mixture model to modulate the supervoxel features which we obtain from the supervoxelization. (ii) To mitigate the gap between fragmented neurites, we develop a skeleton graph method (Figure 3) to reconstruct the tracing.

## 2.1 Denoising

Images generated by confocal microscopy suffer from noise generated in both by stochastic variance in photon counts (shot noise) and from instrument noise (Sheppard et al., 1992). Figure  $1\mathbf{B}$  demonstrates a simple example of this, where the cross sectional intensity Figure  $1\mathbf{C}$  is found to be highly varied. To reduce these noise sources while preserving structures, we use a nonlocal transform-domain filter for volumetric data denoising. Assuming the noise is Gaussian, the BM4D denoiser (Maggioni et al., 2012) is applied in individual channels of the image stack, resulting in a denoised version.

#### 2.2 Supervoxelization

Directly operating at the voxel level on Brainbow images is impractical due to computational complexity and erroneous due to the large observed color variances *in vivo*. One solution is to make supervoxels locally based on colors to oversegment the images (Sümbül et al., 2016). By making supervoxels, the computation is reduced, while also allowing more sophisticated features to be calculated at the supervoxel level. First, we restate two assumptions in a local and global context: (i) locally, neighboring voxels within the same neurites share similar colors; (ii) spatial information and color information act as a global constraint to obtain optimal segmentation. A watershed

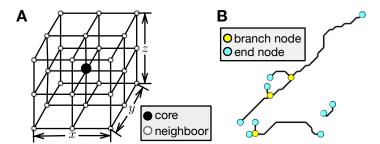


Figure 3: **A**, a diagram of 27-point stencil in euclidean space. **B**, example constructed graph visualization under *Definition 1*. Note that, the black lines between two nodes are following the path of the connected components using 27-point stencil.

transform (Meyer, 1994) is used to generate supervoxels, and each supervoxel is summarized by its mean color in LUV space (Schanda, 2007).

After supervoxelization, we yield a set of supervoxels  $S = \{s_i\}$ , where  $s_i$  denotes a supervoxel. The spatio-color constraint is imposed on supervoxel set S. We use a graph  $\mathcal{G} = (V, E)$  to represent the spatio-color relationship, where each supervoxel  $s_i$  in S represents a node in V. Edges are configured between pairs of supervoxels where: (i) the spatial distance between two supervoxels is less than  $\delta_s$  or (ii) the color dissimilarity is less than  $\delta_s$ . In this way, the affinity matrix is constructed as

$$A(i,j) = \begin{cases} e^{-\gamma d_{ij}^2}, & (i,j) \in E\\ 0, & \text{otherwise} \end{cases}$$
 (1)

where  $\gamma$  is the Gaussian kernel parameter, and  $d_{ij}$  is the dissimilarity of color between two supervoxels. Note that the affinity matrix  $A \in \mathbb{R}^{N \times N}$  is a sparse matrix where N represents the number of supervoxels. Instead of using A directly, we decompose A into lower dimension d by utilizing eigenvalue decomposition algorithm (Baglama et al., 2003), where d is the number of eigenvectors with the d largest eigenvalues. We denote the updated affinity matrix as our feature  $\mathbf{X} \in \mathbb{R}^{N \times d}$  which is of the form

$$\mathbf{X} = eig(I - D^{-\frac{1}{2}}AD^{-\frac{1}{2}}) \tag{2}$$

where I denotes identity matrix, and  $D_{ii} = \sum_{j} A_{ij}$ , so that the eigendecomposition is imposed on the symmetric normalized Laplacian matrix.

#### 2.3 Neuron Segmentation

Supervised learning methods (e.g., Gornet et al.) rely on a volumetric ground truth segmentation, which is difficult and, in many cases, infeasible. Thus, unsupervised approaches, such as kernel k-means and spectral clustering, allow more efficient solutions. However, after applying kernel k-means, we observe imperfect segmentation results, particularly with fragmentation near differences in neuron caliber (Figure 4). Thus, instead of imposing hard clusters on  $\mathbf{X}$  via kernel k-means or its variants (Dhillon et al., 2004), we approximate the distribution of the feature  $\mathbf{X}$  using mixture of Gaussians (GMM). We hypothesize that GMM will perform better because it does not bias the cluster sizes to have specific structures as does kernel k-means (Circular). We use the expectation-maximization (EM) algorithm to iteratively optimize the model and check the variational lower bound until convergence is accomplished.

# 2.4 Neuron Tracing

Despite the improvements in image segmentation, we still observe fragmented structures (Figure 2D) among the inferred neurons. To generate a compact tracing, we propose a method to merge fragmented topologies into one continuous tree. The fragmented neurites can be caused by the supervoxelization process and occlusions by the other neurons in the raw Brainbow data; the former problem has been eased by the implementation of GMM, but the latter persists. Thus, we develop a graph-based method to "bridge" the broken links within the same neurite. We first skeletonize the segmentation and use the resulting skeleton in the following operations.

**Definition 1.** Given a skeleton represented by a set of points, using a 27-point stencil, we define core points with at least 3 neighbors as branch points, and core points with only 1 neighbor as end points. This is demonstrated in Figure 3.

#### **Algorithm 1** Skeleton graph construction and linkage bridging

```
Require: skeleton point set S_p, distance threshold \Delta_s
 1: find points in S_p with at least 3 neighbors as branch points P_b and points with 1 neighbor as end
    points P_e, using a 27-point stencil
 2: for every two nodes \{p_i, p_j\} in \{P_b, P_e\} do
       represent the link L_{ij} as the path of connected components between p_i and p_j
 4: end for
 5: construct the skeleton graph G = (P, L), where P is the union set of P_b and P_e
 6: for every two subgraphs G_i and G_j in G do
       for every pair of end nodes p_e^i in G_i and p_e^j in G_j do
          if distance between p_e^i and p_e^j < distance threshold \Delta_s then link p_e^i and p_e^j (e.g., using \mathbf{A}^\star search algorithm, Dijkstra algorithm, etc.)
 8:
 9:
             remove p_e^i and p_e^j from P_e
10:
             update skeleton graph G
11:
          end if
12:
13:
       end for
14: end for
15: return updated G, denoted as compact skeleton graph G_c
```

**Skeleton graph construction.** We represent branch points  $P_b$  and end points  $P_e$  as the nodes (i.e., branch and end nodes) in the graph, where the edges or links L between every two connected nodes are coded by the paths of the connected components between two nodes (Figure 3B). Note that, in this way, the points with 2 neighbors in the set of skeleton points can be well-represented by the links, and thus there is no need to represent these points as nodes. Abandoning the points with two neighbors also reduces the computation and improves efficiency. The skeleton graph is configured as G = (P, L), where P is the union set of branch nodes  $P_b$  and end nodes  $P_e$ .

Linkage bridging. Broken linkages occur when two end points are incorrectly formed on opposite ends of a fragmented segmentation. Here, our way of constructing the graph is well-suited for bridging these broken connections. First, we extract subgraphs based on the connectivity of all the nodes. Next, we examine every pair of end nodes within two different subgraphs. When the distance, in our case a Euclidean distance, is less than threshold  $\Delta_s$ , we link the two end nodes, and thus we can obtain a more compact graph. The process is iterated until all pairs of subgraphs have been examined. A detailed description of this process is given in Algorithm 1, and we also show an alternative implementation using k-d tree in Supp. Algorithm 1.

**Trace generation.** In order to perform quantitative analysis from generated tracing, we developed a technique to generate SWC tracing files (Stockley et al., 1993). The SWC file format is used broadly by the neuroinformatics community and employed as the transaction format of various Fiji (Schindelin et al., 2012) plugins for calculating neuromorphology features. Our technique makes full use of the properties of  $G_c$ . In general, a neurite starts from an end node and stops at an end node and the path between two connected end nodes can be interpreted as part of the neurite. In practice, we try to find the shortest paths from the seed node  $p_e^0$  to following end nodes  $p_e^i$  in the same subgraph, such that the union set of these found shortest paths can be interpreted as the final tracing result T (Tracing) which is of the form

$$T = \{p_e^0 \to p_e^i\}, \quad i \in \{1, \cdots, n-1\}$$
 (3)

where n is the number of end nodes in the compact skeleton graph  $G_c$ . We note that  $p_e^0$  can be randomly selected from any end node, determined using a set of criteria (e.g., the end node furthest to the left of the image), or manually input. For our comparisons, we manually selected the end nodes to be consistent with our human annotation or chose  $p_e^0$  to be the end node with the smallest coordinate in unannotated data.

#### 2.5 Trace Comparison

To quantify differences between different neuron tracings, we make use of the DIADEM metric (Gillette et al., 2011), which was derived as a way of objectively comparing the topologies of different neuron reconstructions. We used the published evaluation code, which generates a maximum

value of 1 for perfectly-matching reconstruction, and 0 for a reconstruction which has no matched nodes to the gold standard. It is worth noting, however, that the DIADEM metric heavily weighs the branching topology of the neurite so, occasionally, visually-similar neurons will result in poor DIADEM scores. When running the DIADEM code, we used the parameter default preset '1', while additionally lessening the X-Y-Z node-matching distance to 10 pixels, to account for the diameter of large-caliber neurites in the test image.

## 3 Datasets

We generated two test images for validation of our method in this report. Expansion microscopy (Shen et al., 2020) was applied to physically expand brain tissue by  $4\times$  from a Brainbow-labeled PV/Som-Cre mouse. A 3-channel image was collected, followed by manual channel alignment and histogram matched using Fiji (Schindelin et al., 2012). The resulting image was then cropped to  $364\times372\times169$  voxels, representing an effective voxel size of  $75~\mathrm{nm}\times75~\mathrm{nm}\times175~\mathrm{nm}$  and a physical volume of  $27.3~\mu\mathrm{m}\times27.9~\mu\mathrm{m}\times29.6~\mu\mathrm{m}$ , to form a manageable test case. This image is used in Figures 2, 4, 5, and 7.

We collected a second image (Figure 6) by injecting the Brainbow viral reporter into the hippocampal CA1 region of a POMC-Cre reporter mouse. 3-channel imaging was performed as above, without the use of sample expansion. This image was cropped to  $300\times300\times300$  voxels to encompass the branches of approximately a single neuron for demonstration purposes, and represents a voxel size of  $0.42\,\mu\mathrm{m}\times0.42\,\mu\mathrm{m}\times1.00\,\mu\mathrm{m}$  and a physical volume of  $126\,\mu\mathrm{m}\times126\,\mu\mathrm{m}\times300\,\mu\mathrm{m}$ .

#### 4 Results

We first compare our neuron segmentation method (Methods 2.3) against the state-of-the-art method of Sümbül et al. by applying it to the first Brainbow image described above (Figure 4). Other than the number of clusters, the remaining parameters (described in Supp. Text) are held constant between the two methods, to ensure that differences observed are the result of algorithm changes. Overall, compared with the previous method, more continuous neuron processes are easily observed using GMM clustering. Channels which are well spectrally separated in the image result segmentations which are equivalent between the two methods (e.g., Figure 4B1 and C1). When neurons of different color intersect, we find that our method results in fewer "extra" voxels being segmented to the wrong channel (Figure 4B3 and C3; see arrows in insets). Finally, our method preserves continuous structures better, as observed by less degree of fragmentation in regions where calibers of the neurites vary (Figure 4B2,4 and C2,4). These improvements result in segmentations that are more coherent and is crucial to accurate downstream automated data analyses.

Next, we implemented a neuron tracing routine to generate skeleton-like tree structure as neuron morphology presentation (Methods 2.4). To determine if our trace-generation method was robust to information loss introduced by segmentation errors, we performed a data loss simulation (Figure 5). Briefly, we calculated the skeletons for the two neurites found in Figure 4B2, after the random removal of between 0 and 50 points out of each 100, resulting in fragmented skeletons (Figure 5A, B). Upon evaluation, we find that both reconstructions are visually robust to large amounts of data loss, however, several loop structures are formed due to the loss of connectivity in dense regions (red arrows). The artificially-fragmented skeletons were then compared against the non-removal control using the DIADEM metric (Gillette et al., 2011) (Figure 5C). The quantification of the top neurite, as indicated by the DIADEM scores close to 1 indicates that there our linkage bridging method is robust against the loss of data in this case. We observe a similar trend in accuracy loss in the bottom neurite, however, the loop structures formed in error cause the DIADEM metric to be lower. Together, these results suggest that the qualitative structure of tracing is highly robust to the loss of data.

Then, we evaluated our method on a more complexly-branched sample as shown in Figure 6. Along with large color variance in the same neuron, the interweaving neural structure of this image can be hard even for human annotation. Figure 6B shows the result of bridging the fragmented segmentation into a compact tracing. We observe that even for the neurites with low intensity (Supp. Figure 4B, red arrows), our proposed can trace the neurites and add them into the reconstructed neuron tree. It is apparent that several branches are oversegmented, as a result of segmentation cross-talk with the green channel. This behavior can be tuned by parameter choice, however, we found that neuron

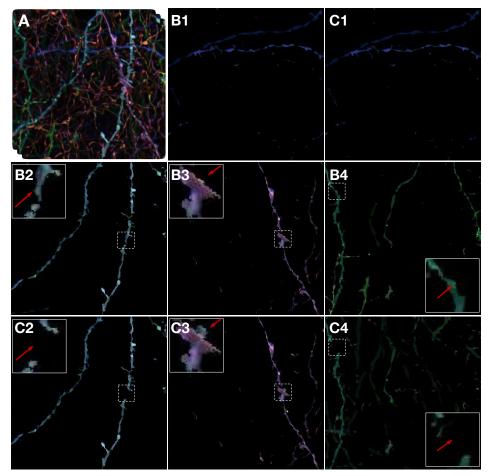


Figure 4: A, the input raw Brainbow image stack. B1–4, selected GMM segmentation results. C1–4, selected kernel k-means segmentation results. Insets are provided to show detail. The complete segmentation result can is visualized in Supp. Figure 1 and the tracings are available in Supp. Figures 2, 3. All the images are using maximum intensity projections along the z-axis and are rotated for better visualization.

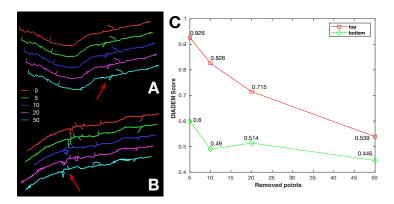


Figure 5: The study on robustness of our proposed method to loss of image information. A and B, comparisons on the tracing result of the left and right neurons found in Figure 4B2. C, the DI-ADEM quality score of each setting for A and B. Tracings have been rotated and rescaled to fit plotting area.

"pruning" requires less human intervention time when proofreading a tracing as compared to adding missed branches.

Finally, as a test of the accuracy of our algorithm and applicability for large-scale neural circuit reconstruction experiments, we generated 7 neuron tracings from our test image (Figures 7A, B) and also reconstructed the same neurons by manual tracing. The automatically-generated tracings agree

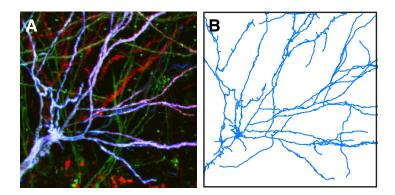


Figure 6: **A**, the projection of test image with interweaving neural branches along the z-axis. **B**, the tracing result using the proposed method for the purple neuron in the test image. Both images are maximum projections along the z-axis. Additional segmentation results are presented in Supp. Figure 4.

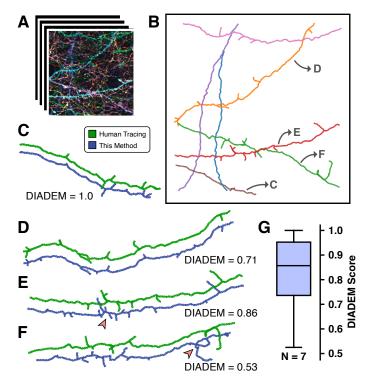


Figure 7: A, an overview zprojection of the test image, for reference. B, high caliber neurons (N = 7) were automatically reconstructed and their structures are visualized as zprojections of the resultant tracing files. C-F, several example neurons from B are shown next to manual human tracing. The DIADEM quality score for each pair is shown below each panel. Red arrows are discussed within the text. Note in C that slight differences exist between the two reconstructions, however, because they are smaller than the size limit for the algorithm, it reports a complete reconstruction. Neurons have been rotated and rescaled to fit the plotting area. **G**, the DIADEM scores of all 7 neurons in **B** ( $\mu = 0.82$ ; Range = [0.53, 1.0]).

well with the human "gold standard" results (Figures 7C-G), with an average DIADEM score of 0.82. There are several features to be noted within these reconstructions: First, we find that there are some features which are reconstructed by the proposed method are not annotated by our human tracing (e.g., Figure 7E, arrow). Upon manual inspection, some of these small features represent spines that are difficult to resolve in the image. Additionally, one outlier reconstruction (Figure 7F) performed poorly, due to a small loop introduced by a nearby similarly-colored neurite (arrow). Overall, this experiment suggests the ability to perform large, automated reconstructions of Brainbow-labeled neurons with accuracy comparable to human annotation.

#### 5 Discussion

In this paper, we present a method that enables the efficient generation of neuron structural traces from densely labeled multispectral Brainbow images. Specifically, our use of GMM clustering, as well as a graph-theoretic method for neuron trace repair, prevent fragmentation errors which result from the application of previous methods. We show by comparison to the human annotation of the same images that our method is robust and efficient while introducing minimal errors.

We hope that this work will find application with the many worldwide efforts to create wholeorganism neural maps. Human proofreading time in these experiments can be astronomical, so improving automation has the potential to accelerate science by increasing its efficiency. Further, these developments may be relevant to similar tracing-extraction problems, such as retinal tracing.

# **Broader Impact**

Here, we present an unsupervised approach for neural tracing on densely labeled multispectral Brainbow images. Since it can relieve the high demand for human labor, our proposed method can help with the human annotations on Brainbow images which can potentially enables supervised or weakly-supervised approaches to learning brain circuits. Although approaches for reliably analyzing and quantifying Brainbow images remain in their infancy, we hope our work can draw the attention of researchers to this interesting field.

#### **Author Contributions**

BD developed and implemented the algorithm. BD and LAW performed statistical analysis and drafted the manuscript, with input from all authors. DHR and FYS performed microscopy experiments. DC and YY conceptualized and oversaw the project.

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